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## Improving the Collision Search on SHA-0

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## Contribution

1. We find two conditions ( $b_{0,9}=0, b_{0,11}=1$ ) are necessary in sufficient conditions of Wang et al.
2. We propose new message modifications for sufficient conditions in step 21-24.

	Complexity
Method of Wang et al	<del><math>2^{39}</math></del> $\rightarrow$ $2^{41}$ SHA-0 operations
Our Method	$2^{36}$ SHA-0 operations

## Main Idea of Message Modifications for Step 21-24



- **Message modifications of the method of Wang et al.**
  - Sufficient conditions in step 17-20 are corrected by inputting a differential in  $m_{15}$ .  
(A start point of a differential is step 16)
- **Problem of the method of Wang et al.**
  - It is difficult to correct sufficient conditions after step 20 by inputting a differential in  $m_{15}$ .
- **Solution of this problem**
  - We solve this problem by using an idea of local collision.
  - By using this idea, a start point of a differential changes from step 16 to step 19.
  - We can correct sufficient conditions until step 24

## Outline of Our Message Modification



Step	Differential	
11	$\Delta a_{11}=2^j$	← Input <b>a differential</b> in $m_{10}$
.	$\vdots$	
.	$\Delta e_{15}=2^{j-2}$	} Execute a certain procedure to cancel <b>this differential</b>
16	0	
.	$\vdots$	} Differentials of chaining values are <b>0</b> ( <b>Non differential</b> )
.	0	
19	$\Delta a_{19}=2^k$	← <b>A differential</b> is appeared from message expansion
.	correct ↓	} By <b>this differential</b> , sufficient conditions until step 24 can be corrected
.	Sufficient condition	
24		

## Example of Our Message Modification ( $a_{22,2}=m_{21,2}$ )

- We input a differential  $2^{20}$  in  $m_{10}$  ( $m_{10} \leftarrow m_{10} \oplus 2^{20}$ ).
- This differential is canceled by following procedure in six steps.

step	Message Modify	Differentials	Extra Conditions
11	$m_{10} \leftarrow m_{10} \oplus 2^{20}$	$\Delta a_{11} = \pm 2^{20}$	$a_{11,21} = m_{10,21}$
12	$m_{11} \leftarrow m_{11} \oplus 2^{25}$	$\Delta b_{12} = \pm 2^{20}$	$m_{11,26} \neq m_{10,21}$
13		$\Delta c_{13} = \pm 2^{18}$	$a_{10,23} = a_{9,23}$
14		$\Delta d_{14} = \pm 2^{18}$	$a_{12,19} = 0$
15		$\Delta e_{15} = \pm 2^{18}$	$a_{13,19} = 1$
16	$m_{15} \leftarrow m_{15} \oplus 2^{18}$	<b>Non Differential</b>	$m_{15,19} \neq m_{10,21}$

Input  
a differential

Canceling  
the differential

## Example of Our Message Modification ( $a_{22,2}=m_{21,2}$ )

- From message expansion, differential  $\Delta m_{18} = \pm 2^{18}$  is appeared in step 19.
- By this differential, the differential moves  $a_{22}$  as follows.  

$$\Delta a_{19} = \pm 2^{18} \rightarrow \Delta a_{20} = \pm 2^{23} \rightarrow \Delta a_{21} = \pm 2^{28} \rightarrow \Delta a_{22} = \pm 2$$
- By the differential  $\Delta a_{22} = \pm 2$ ,  $a_{22,2}$  is corrected.

Message modifications for sufficient conditions  
 $a_{21,4} = (\neq) a_{20,4}$ ,  $a_{22,4} = (\neq) a_{21,4}$ , and  $a_{23,2} = m_{22,2}$   
 are similar to this message modification

## Example of Collision

M1= f459644c b87cd4e1 ed98d4a6 7f5c304b a8606648 073dda8d 9f044c3a 2386c95f  
8b611aa4 d66ed3b9 c4854f6e d57662b3 d687ebe0 f61cefe5 6d0252c2 01f298bc

M2= 76c21fb3 8a725c5a 13a6039c a23c1950 53e65762 b70bbb88 705ec5b6 079e5dd5  
f58793f6 d67d305e 352ee1b8 87c36500 fd012cb5 a51c4269 6a72aabd 7a2449cc

M2'= f6c21ff1 8a725c5a 93a603de a23c1910 53e65722 b70bbbca f05ec5b4 879e5dd7  
f58793b6 567d305e b52ee1f8 07c36502 fd012cb7 251c4229 ea72aabd fa24498c

$$H(M1||M2)=H(M1||M2')$$

# Thank you