

Unconditionally Secure Universally Composable



Commitments

from
Physical Assumptions

Ivan Damgård and Alessandra Scafuro

Wait...Isn't done yet?

Universally Composable

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Universally Composable

Statefull tokens [K07..]

Stateless tokens [CGS08..]

Trusted PUFs [BFSK11]

Malicious PUFs [OSVW13]

(trusted)

Signature card [HMQU11..]

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this work

Trusted PUFs [BFSK11]

Trusted PUFs

Malicious PUFs [OSVW13]

this work

(trusted)

Signature card [HMQU11..]

Unconditionally Secure

Universally Composable

Commitments

Unconditionally Secure

Universally Composable

Commitments

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R

Unconditionally Secure

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Commitments

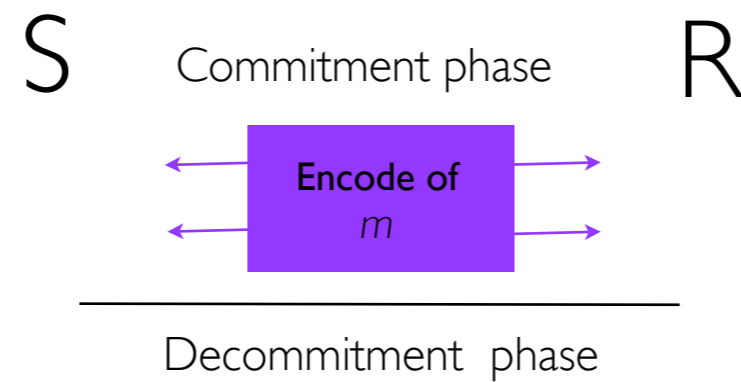
S Commitment phase R

Decommitment phase

Unconditionally Secure

Universally Composable

Commitments



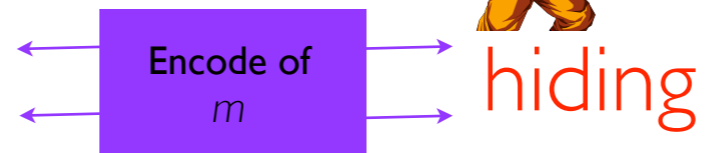
Unconditionally Secure

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Decommitment phase

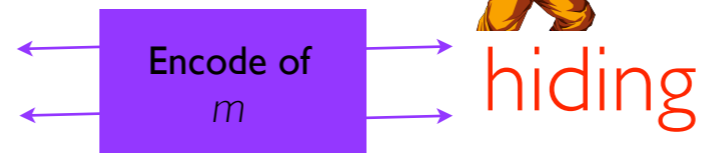
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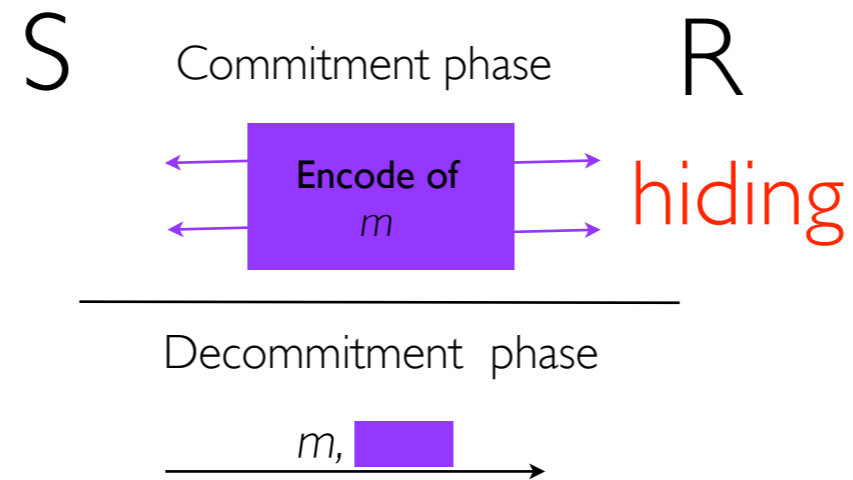
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Unconditionally Secure

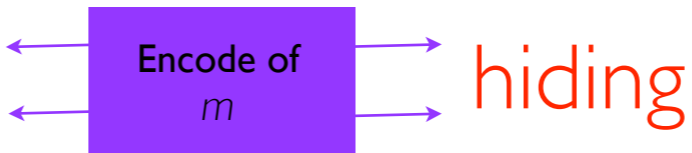
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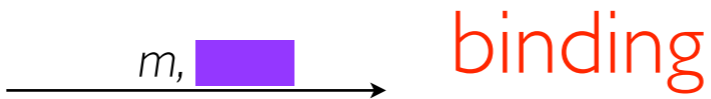


Commitment phase

R



Decommitment phase



Unconditionally Secure

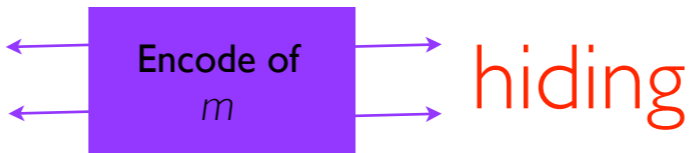
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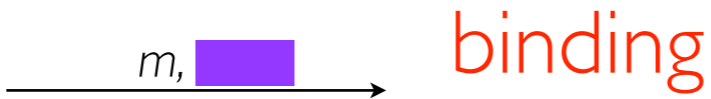


Commitment phase

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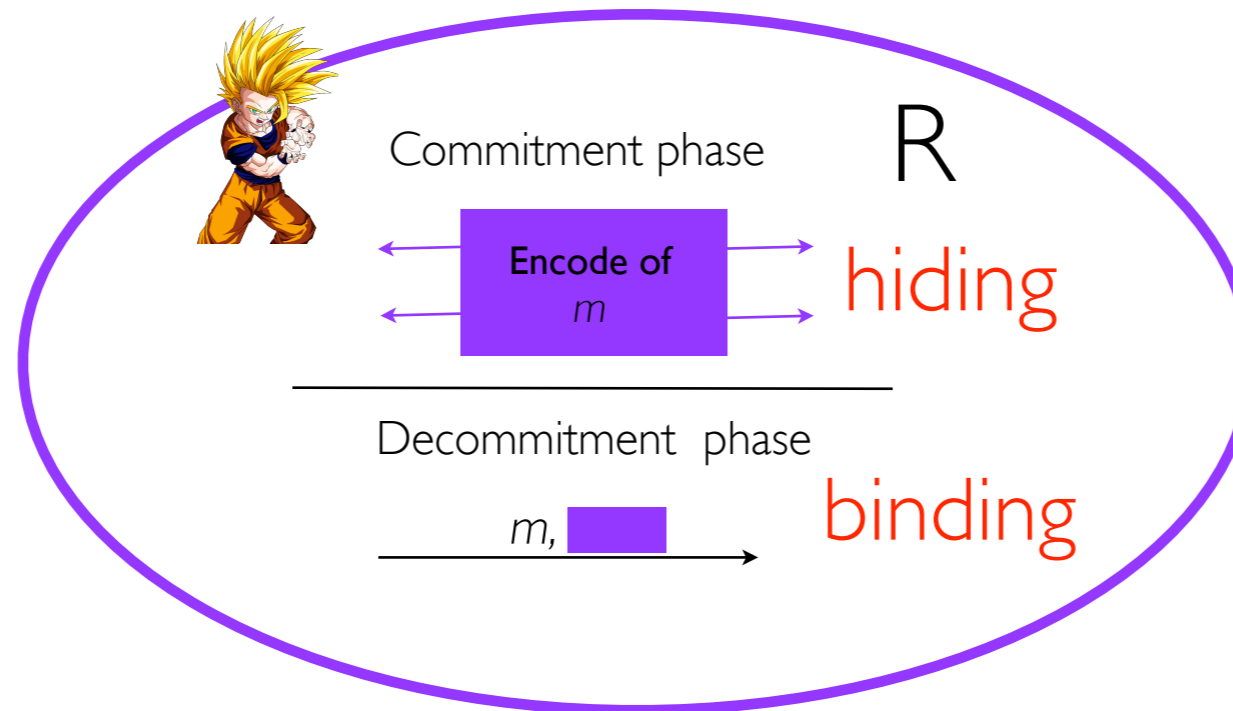
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Unconditionally Secure

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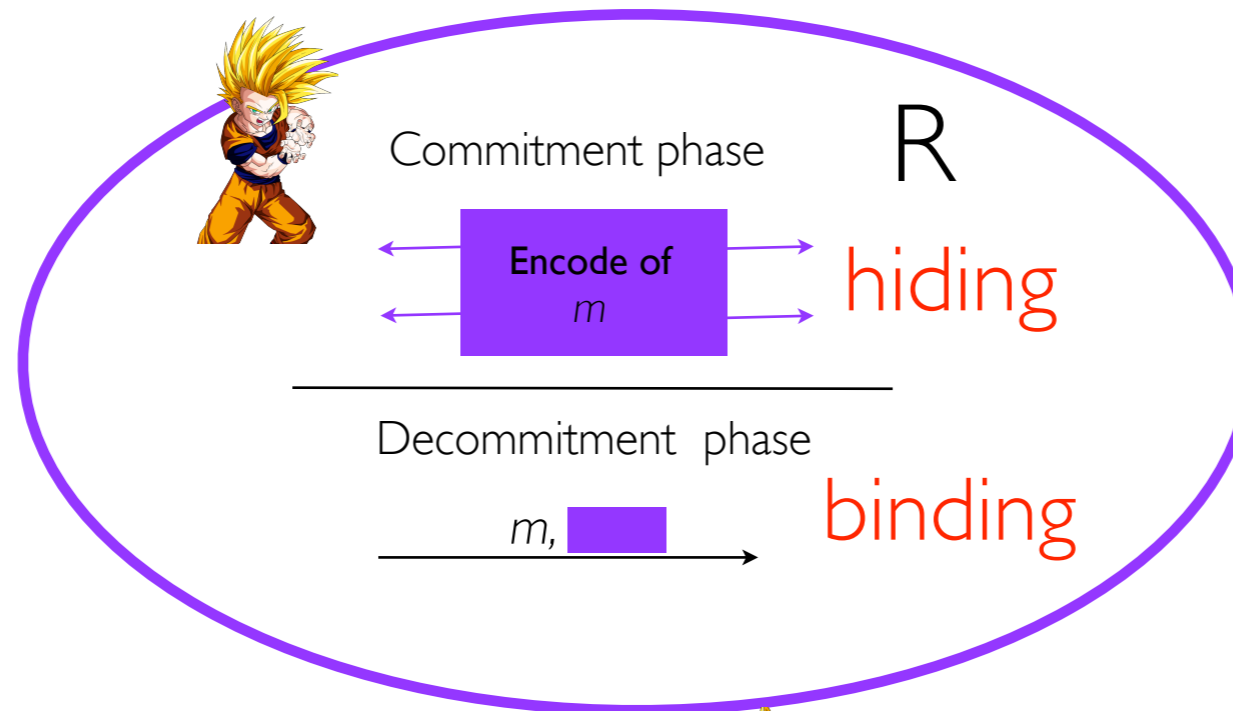
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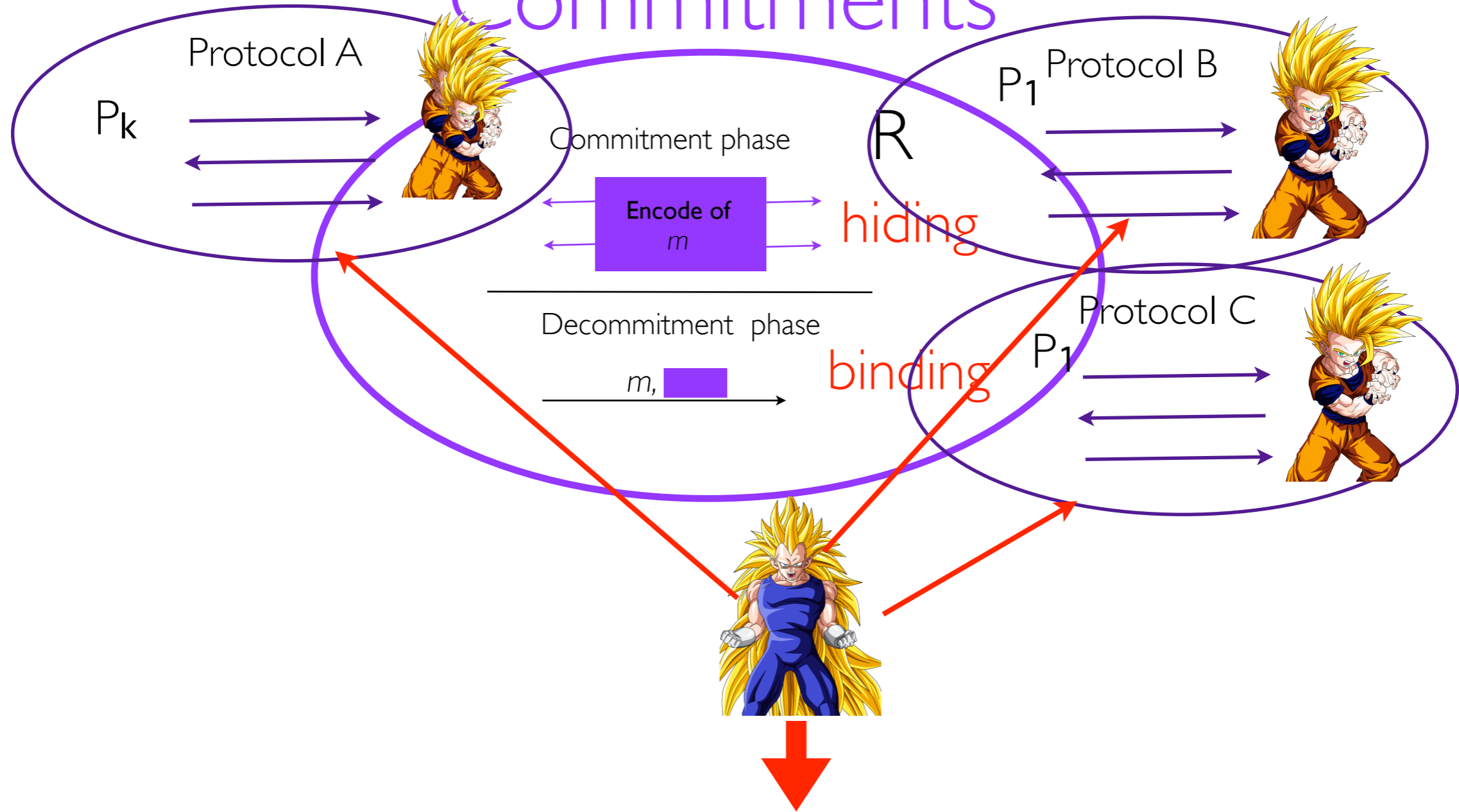
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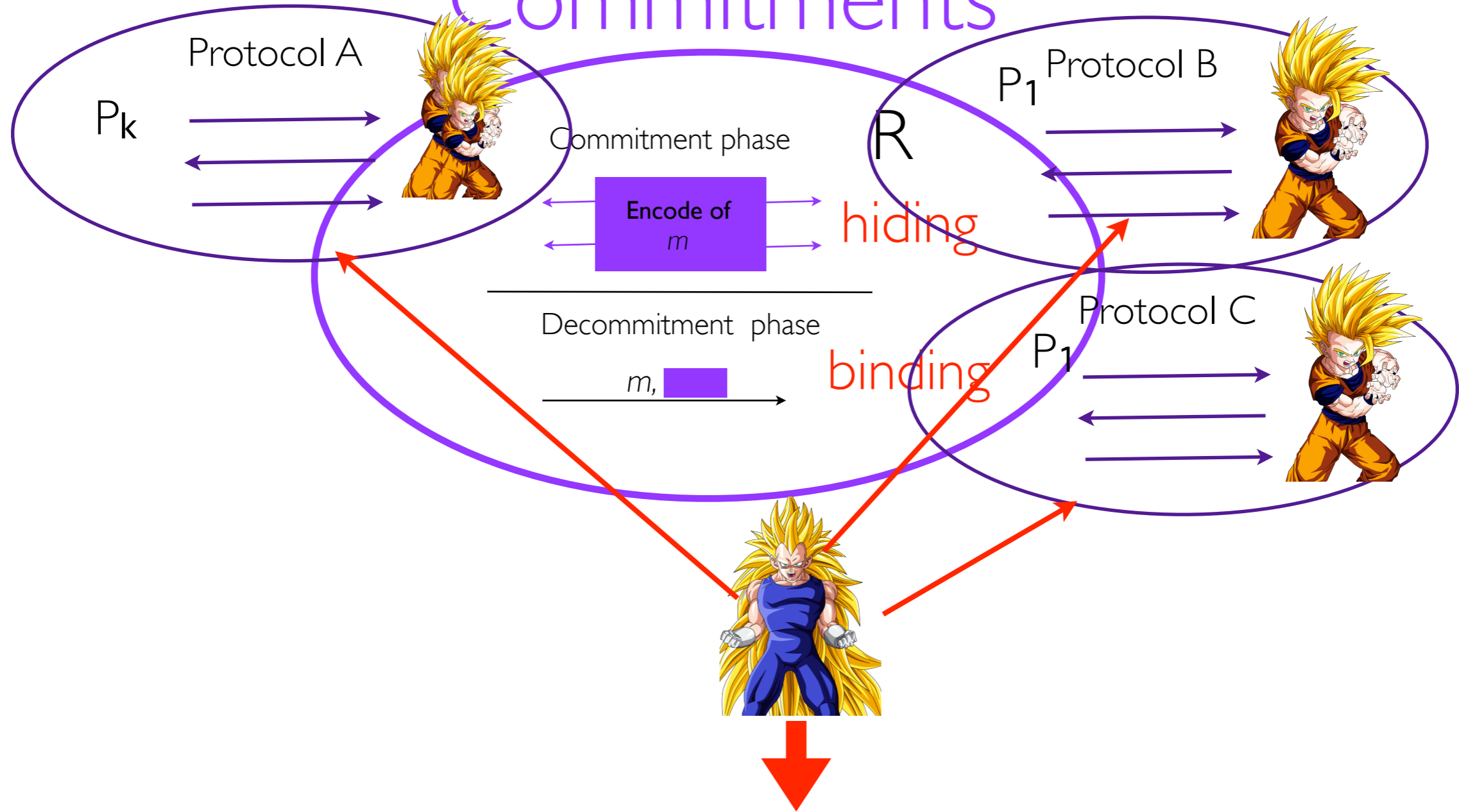


[CKL03] Setup Assumptions

Unconditionally Secure

Universally Composable

Commitments

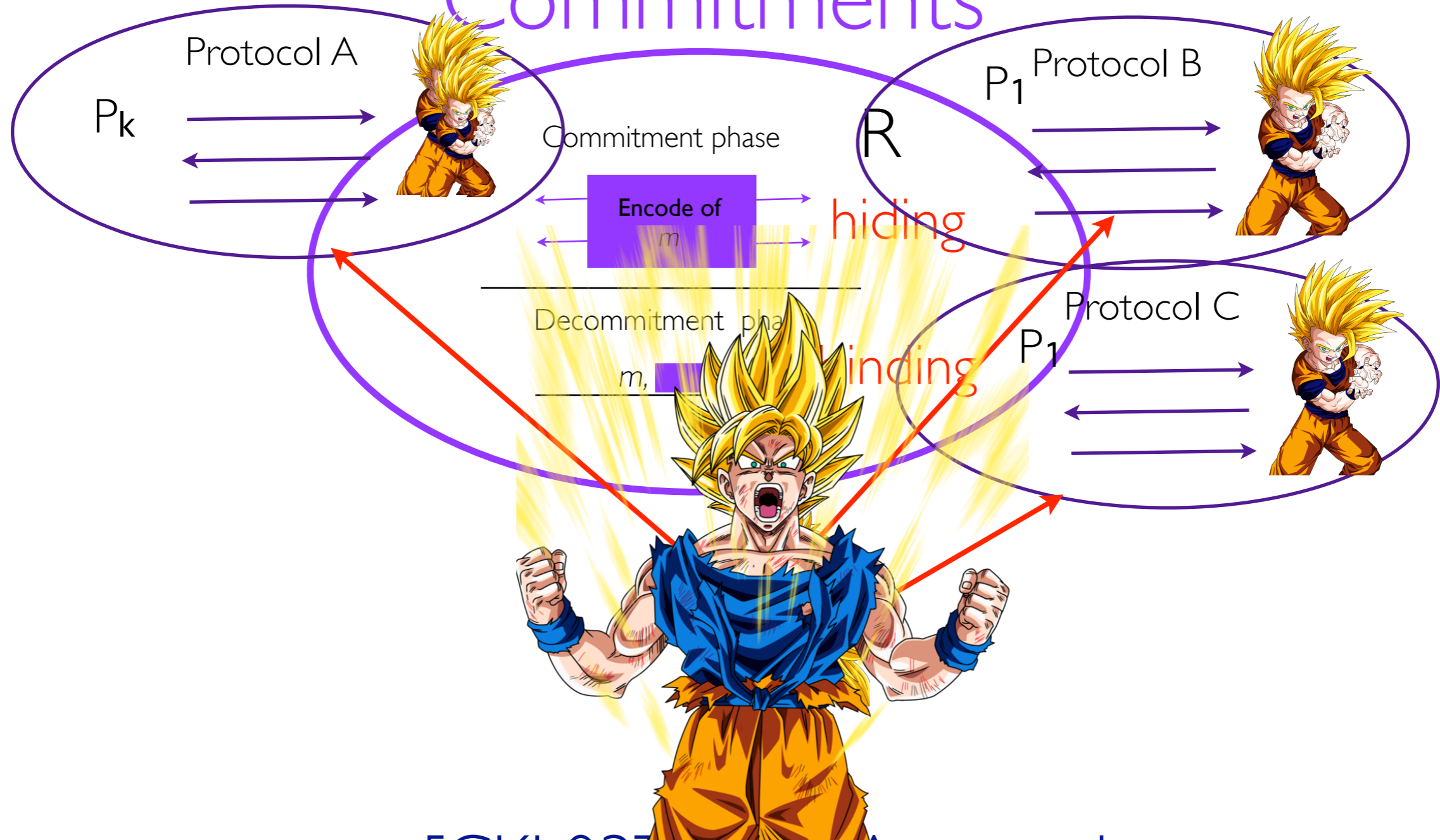


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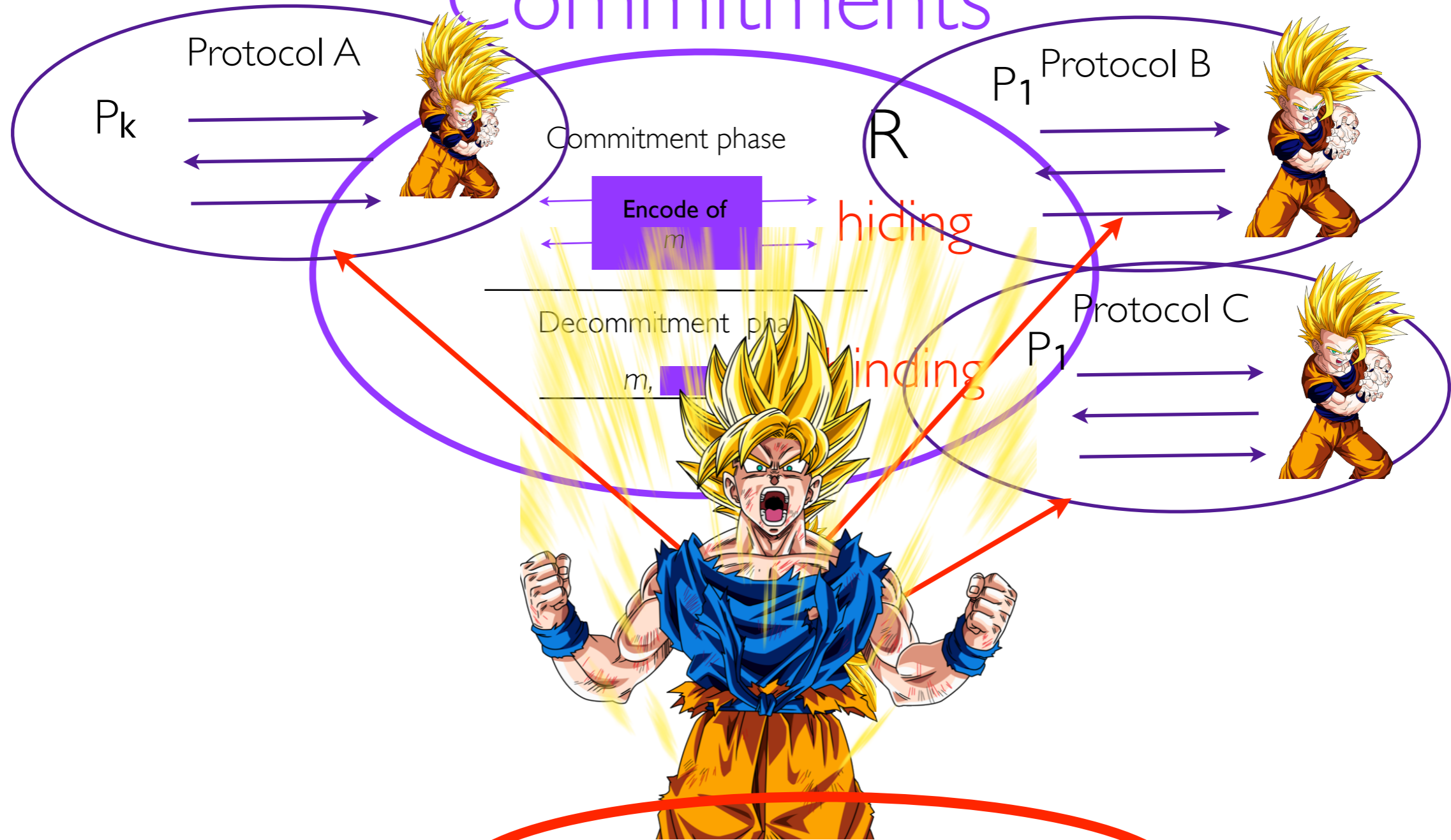


[CKL03] Setup Assumptions

Unconditionally Secure

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Physical Assumptions

Physical Assumptions

Tamper-proof
hardware token

Physically Uncloneable Functions
PUFs

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Physical Assumptions

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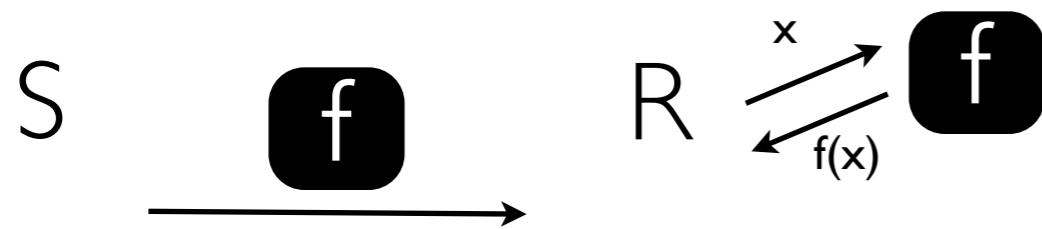
Physically Uncloneable Functions
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Physical Assumptions

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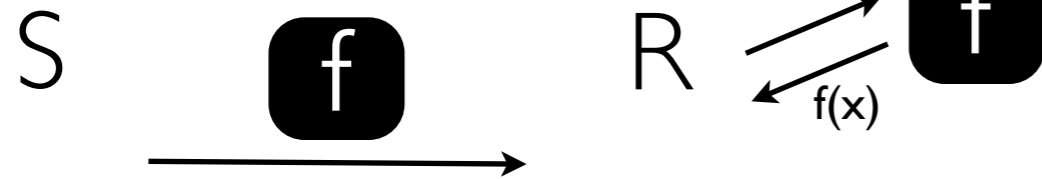
Physical Assumptions

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Physically Uncloneable Functions
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Assumption: tamper-proof

R learns only $f(x)$



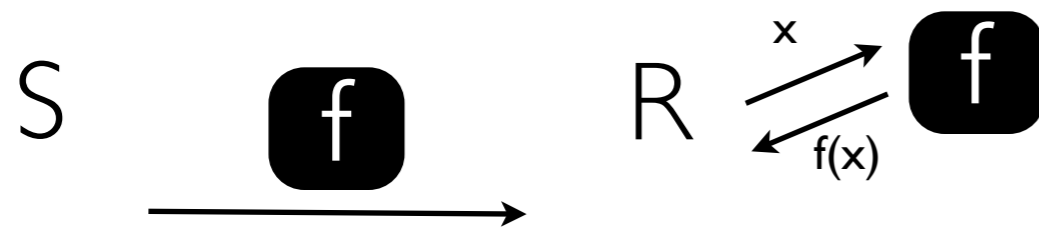
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Stateful

Stateless

- (tamper-proof) updatable memory
- reset attacks

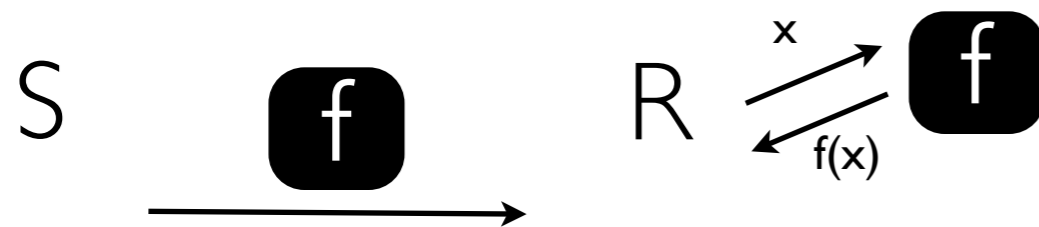
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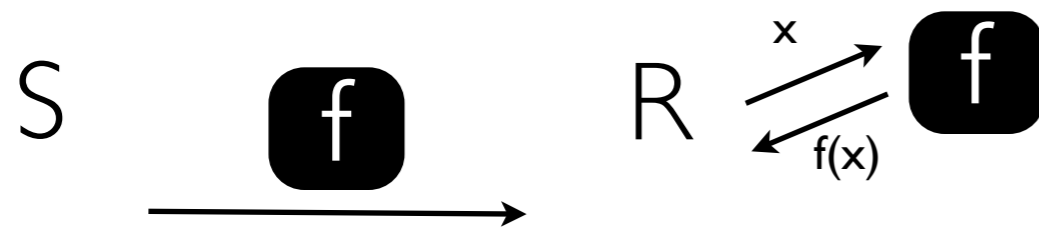
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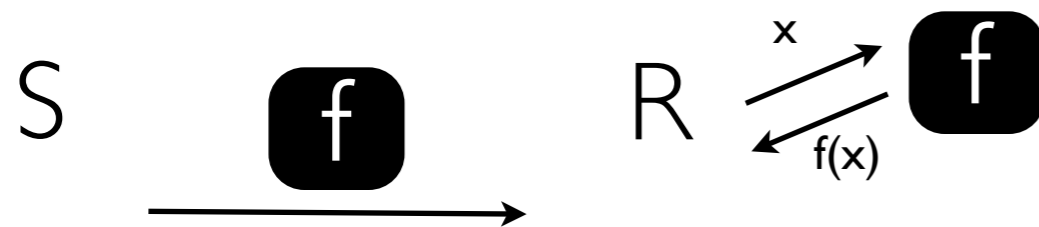
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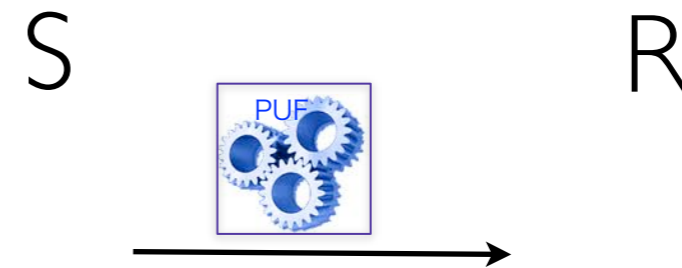


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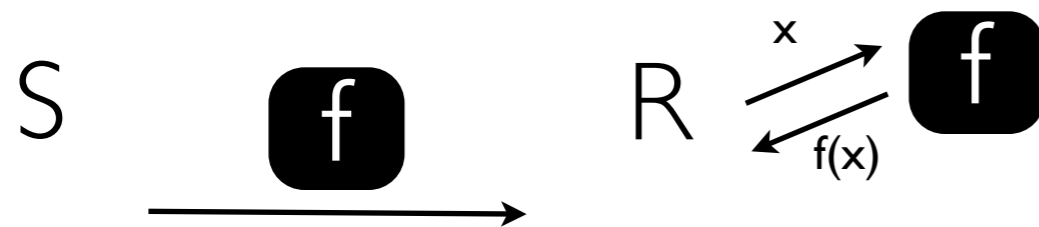


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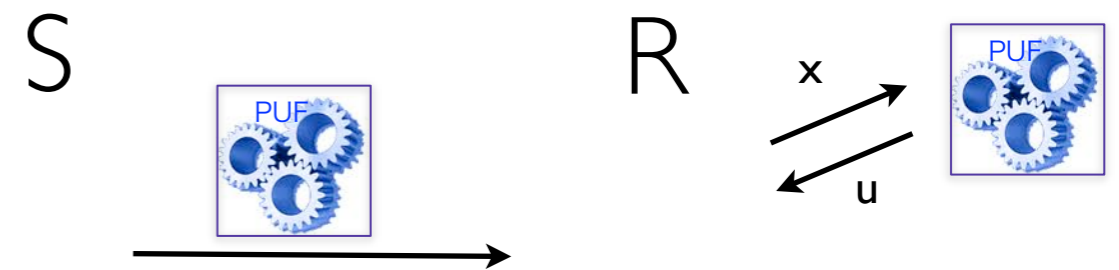
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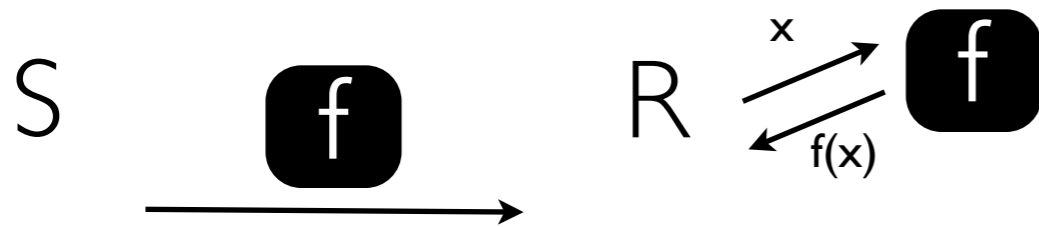
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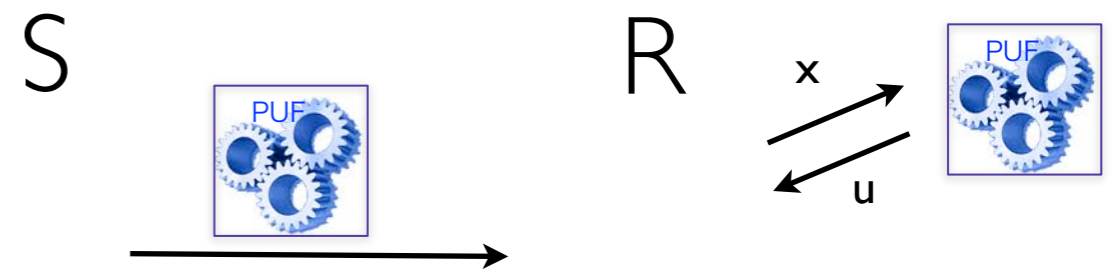
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Physically Unclonable Functions
PUFs

Assumption: unpredictability

R cannot predict the answer on $y \neq x$ (with y far from x)

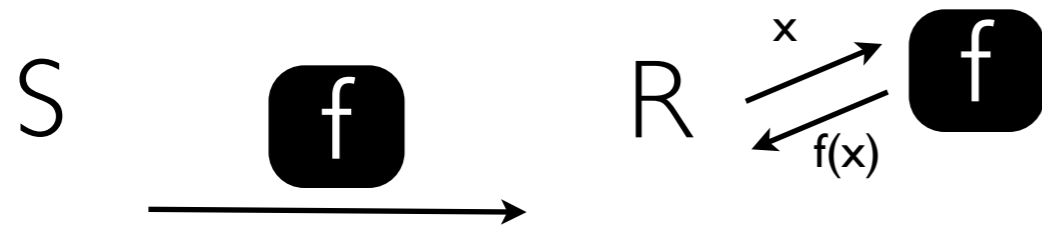


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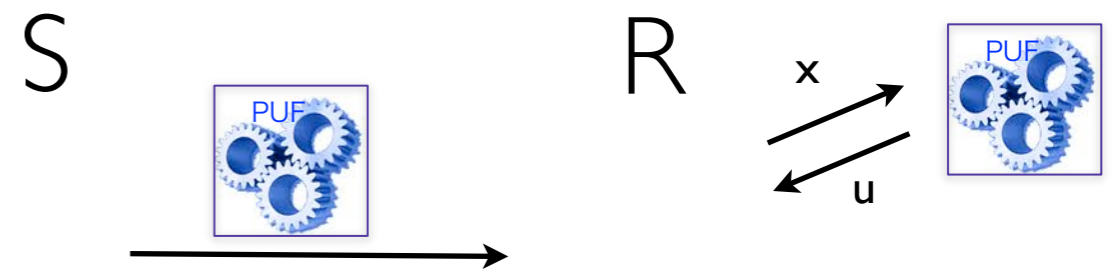
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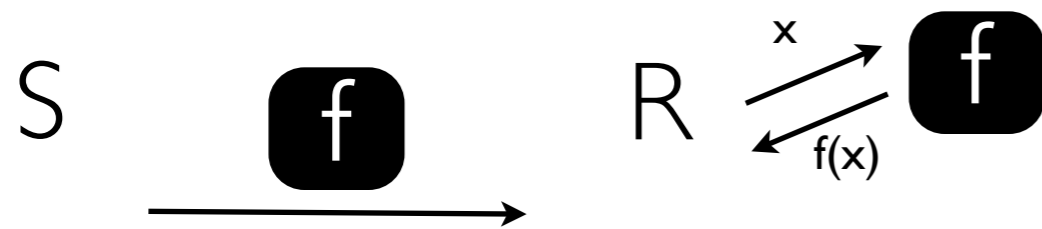
unpredictability holds for "far enough" challenges

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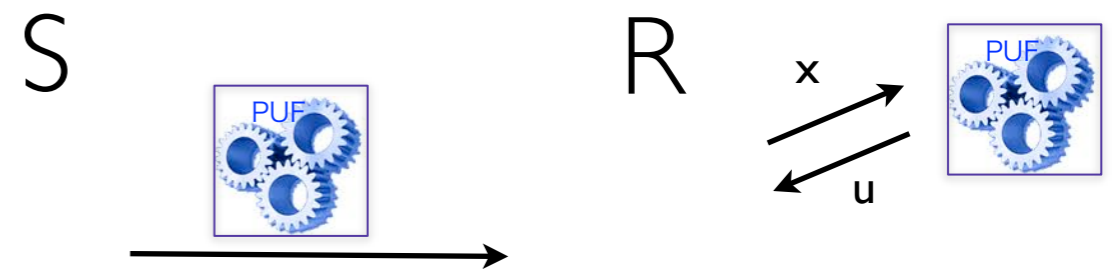
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Assumption

physically uncloneable

UC-Modeling Physical Assumptions

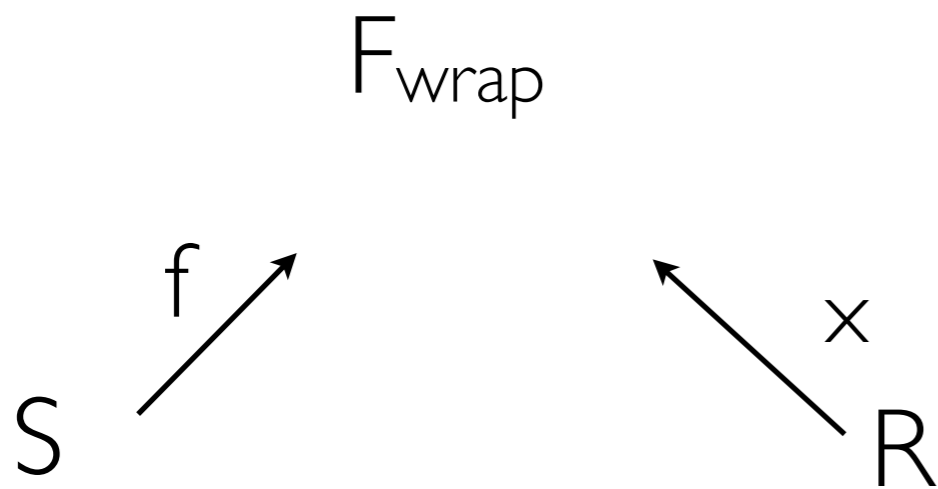
Tamper-proof Model
[Katz07]

(Malicious) PUF- Model
[BFKS11, OSVW13]

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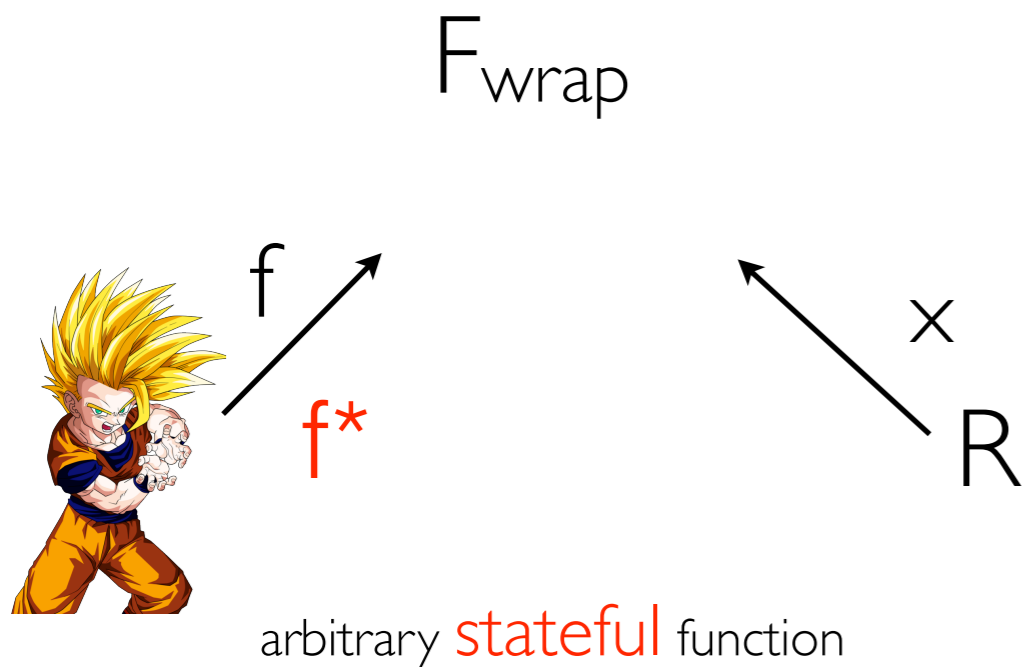
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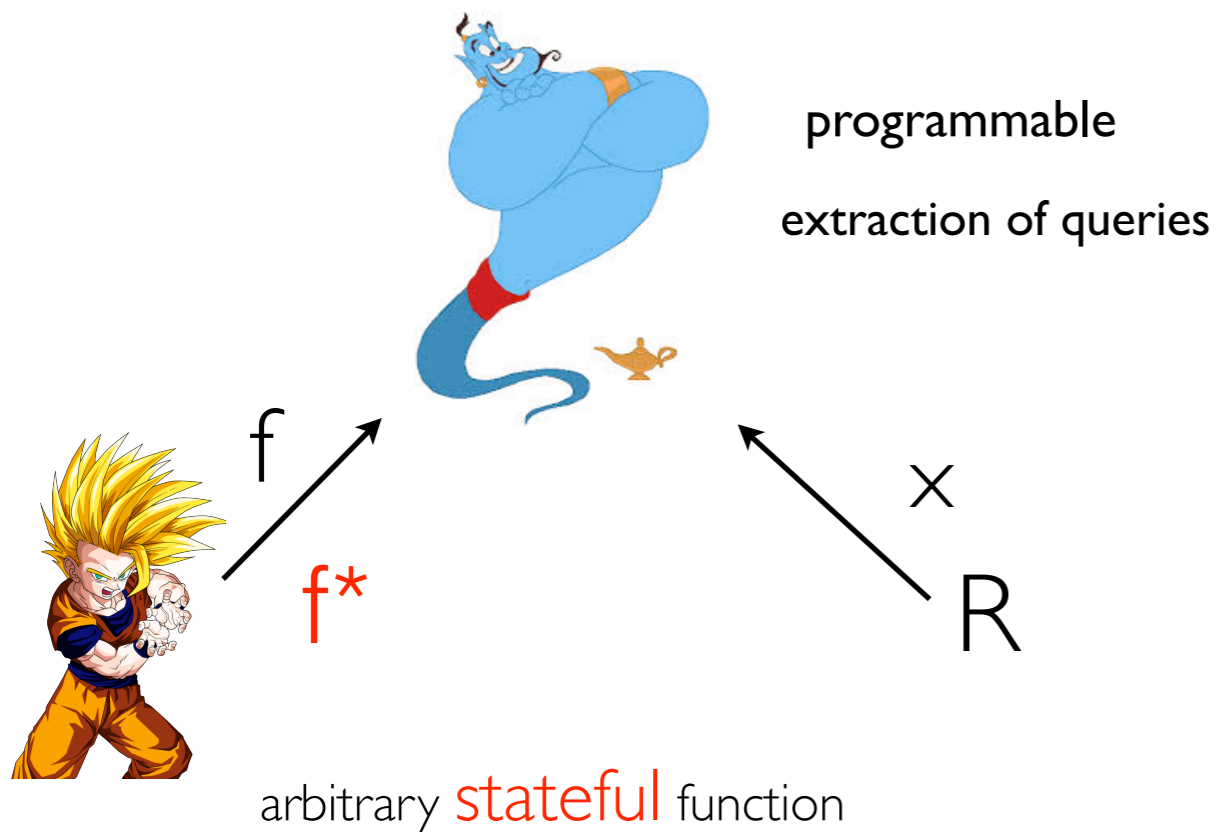
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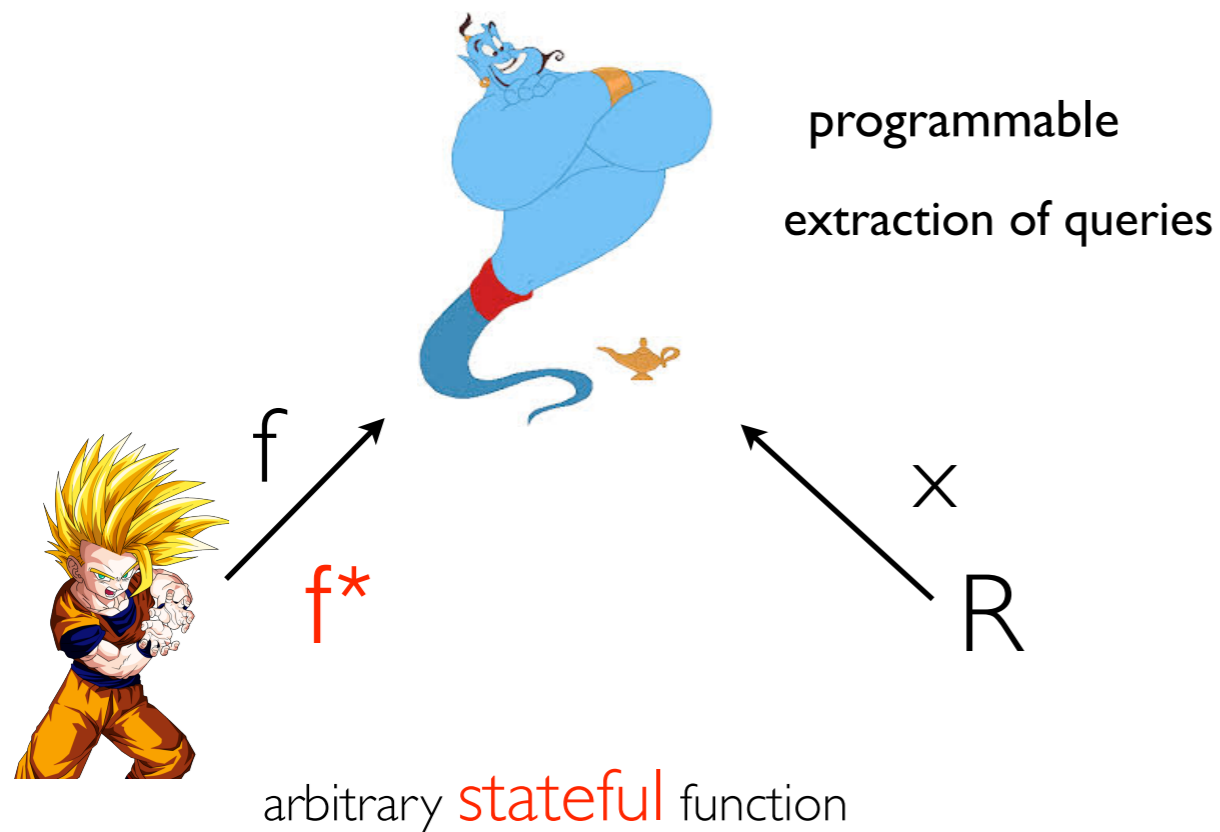
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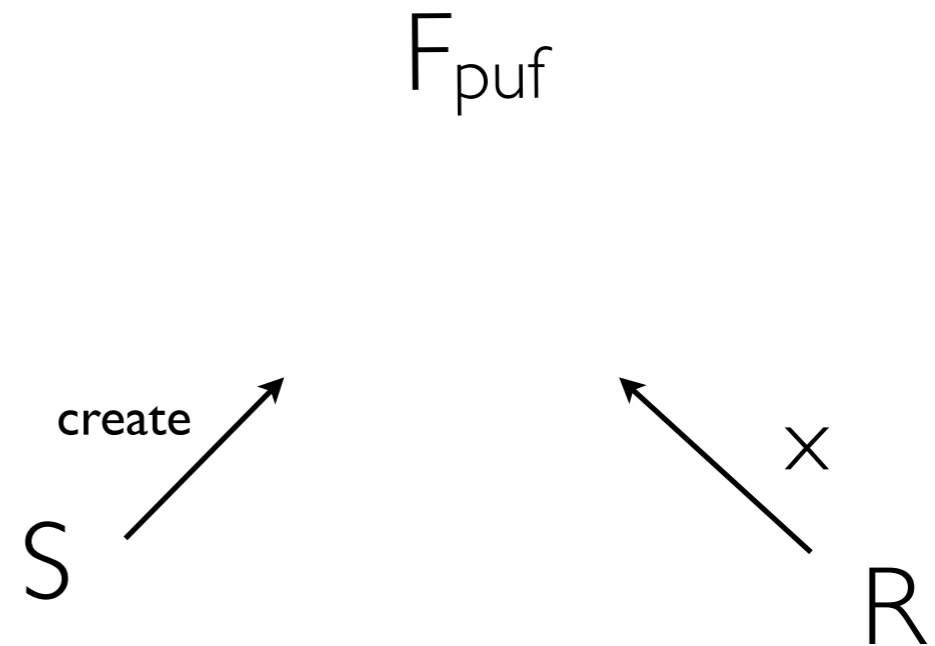


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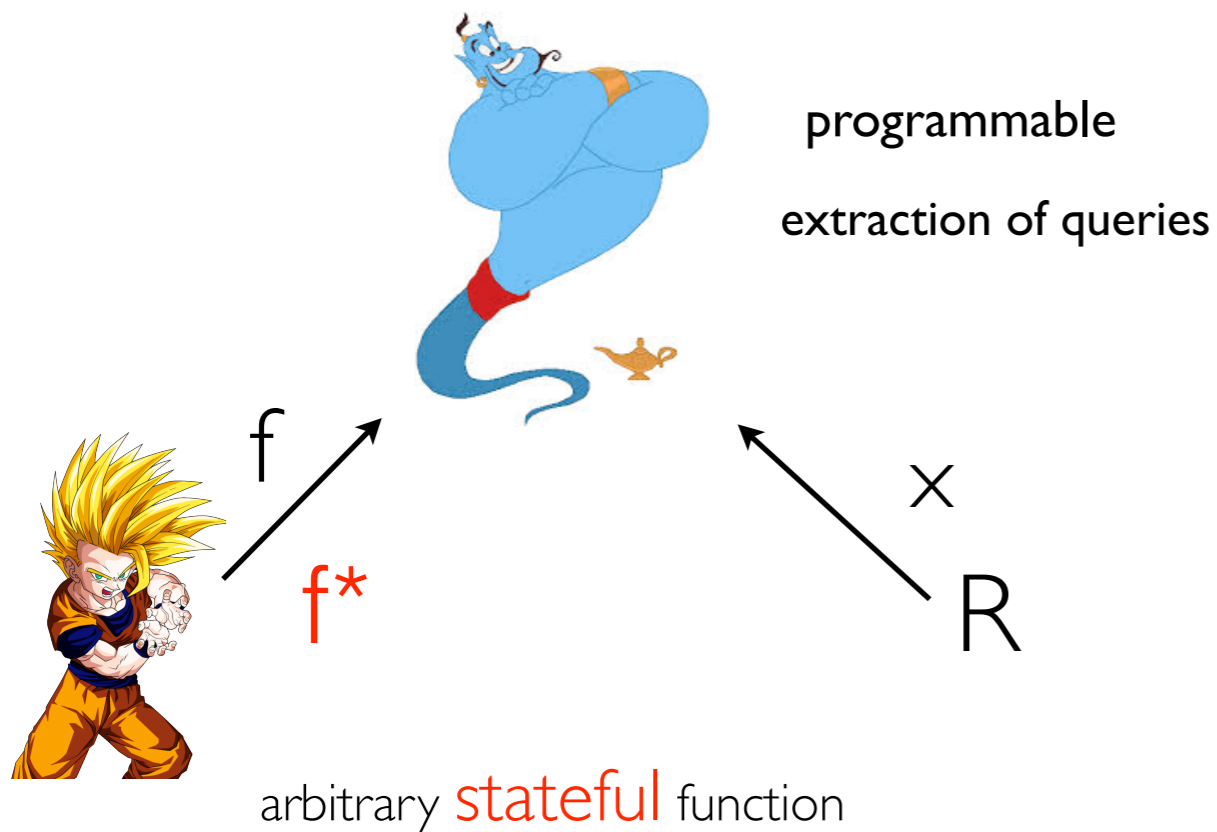


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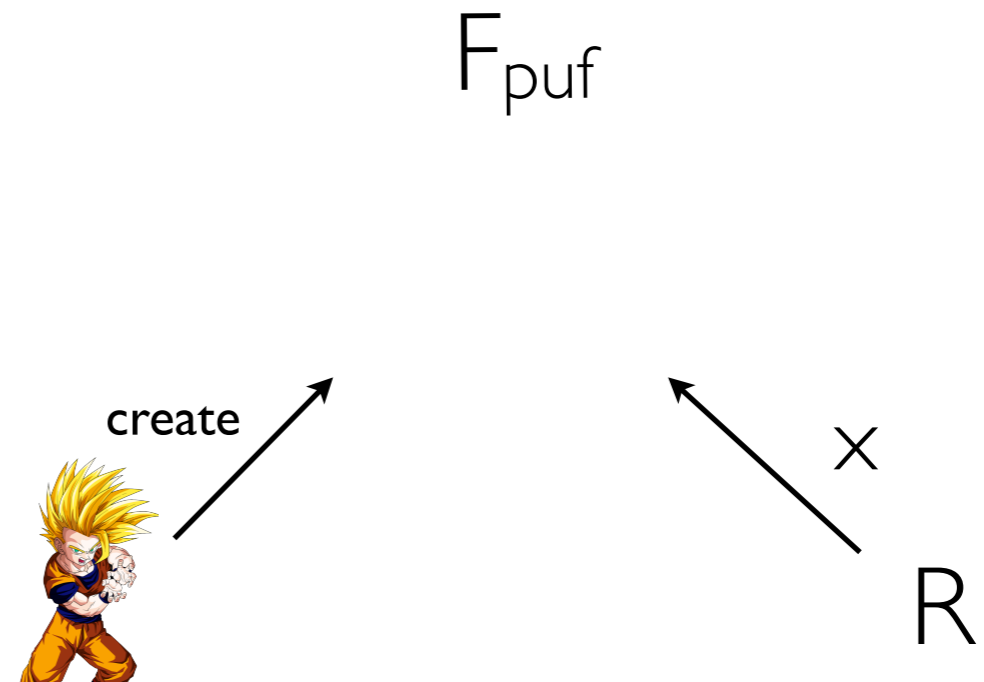


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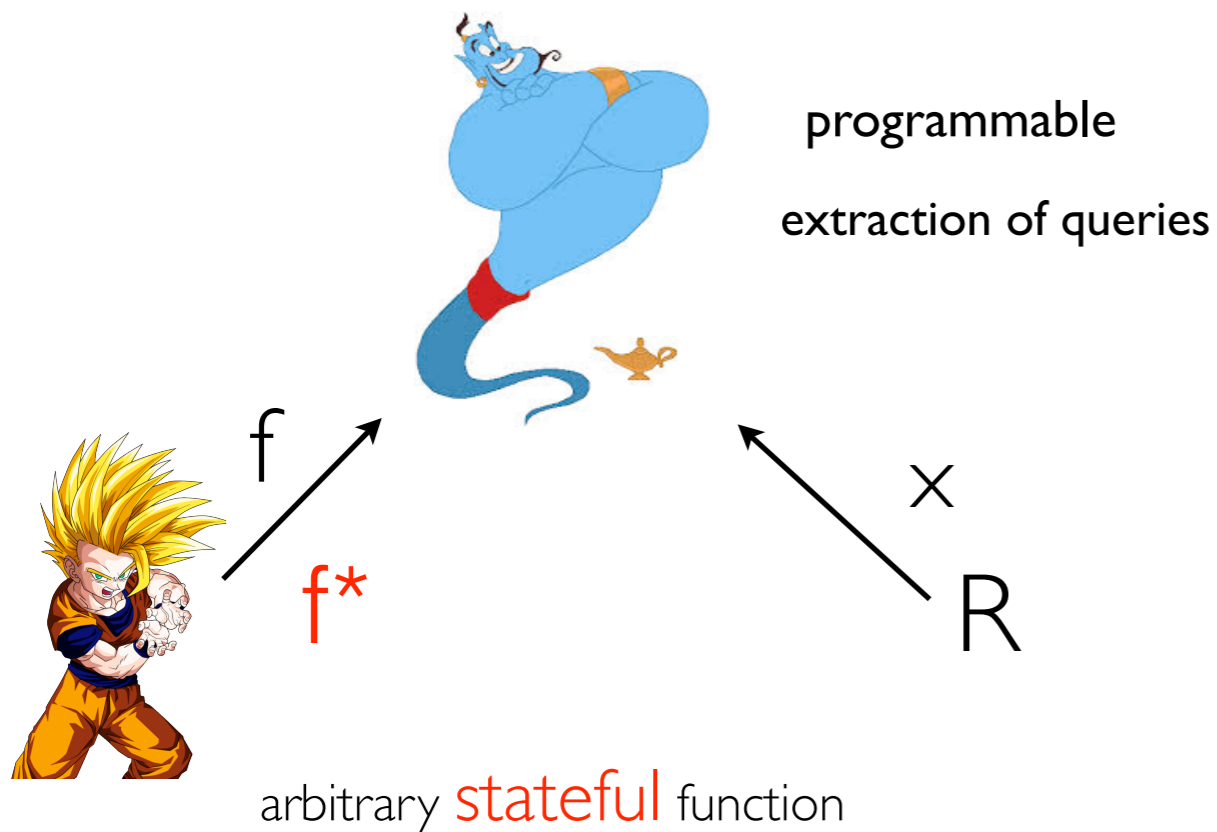


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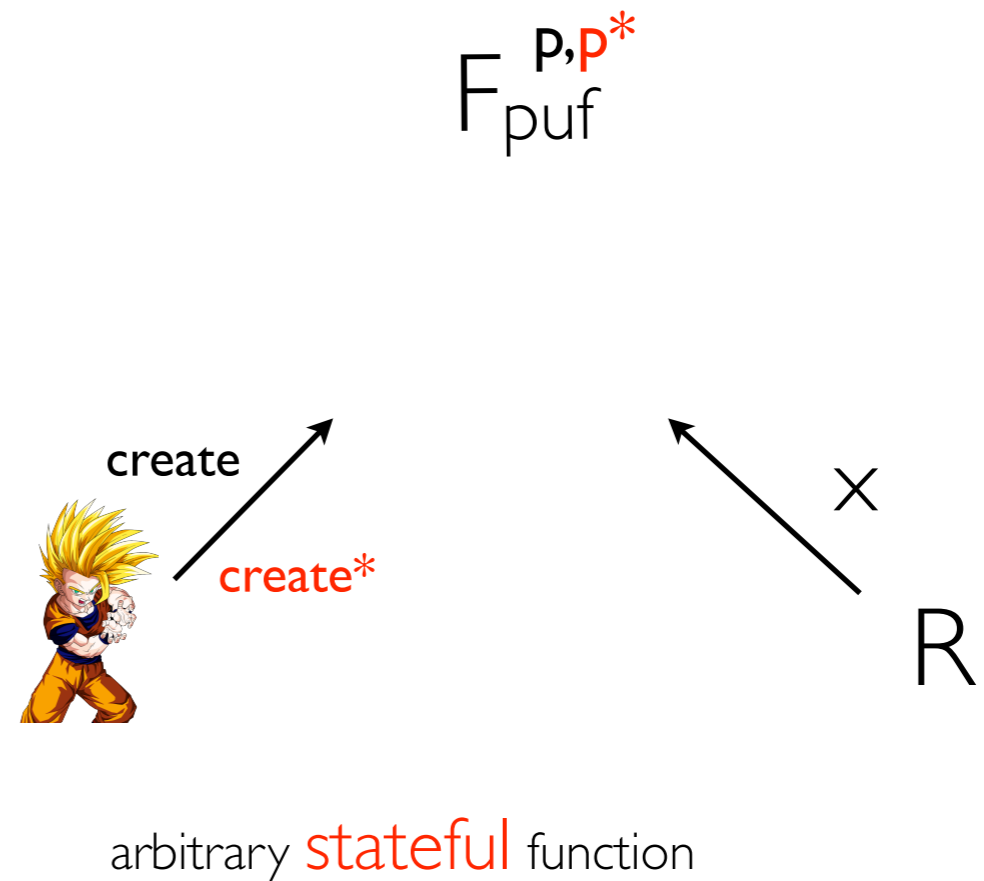


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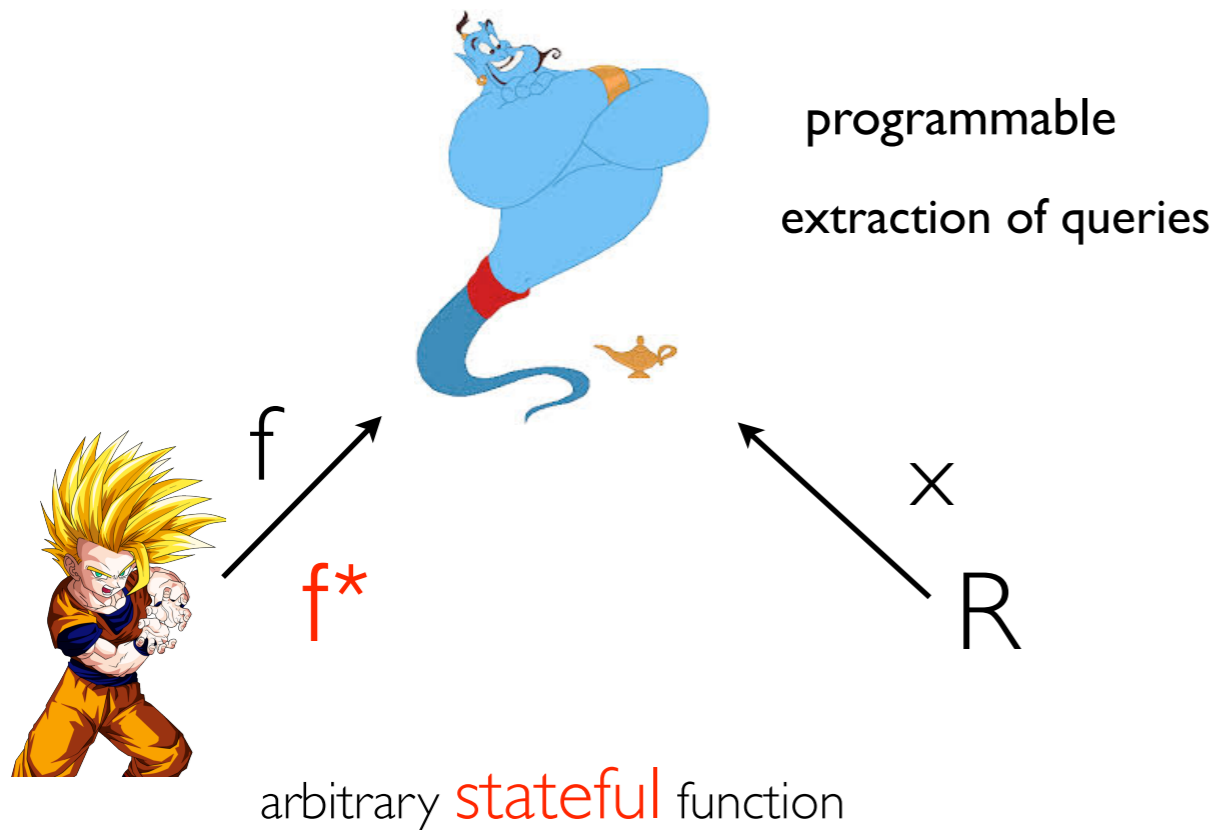


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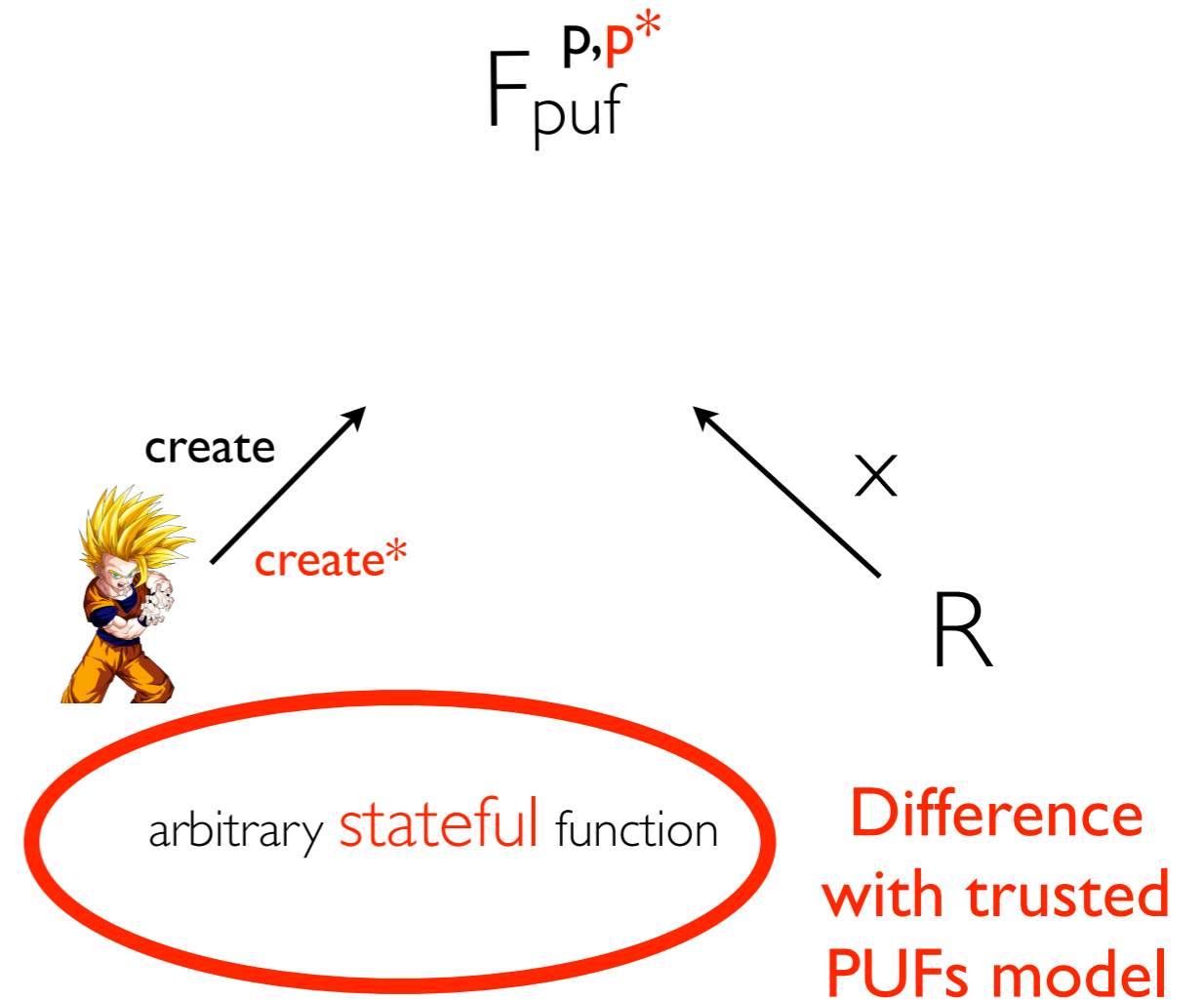


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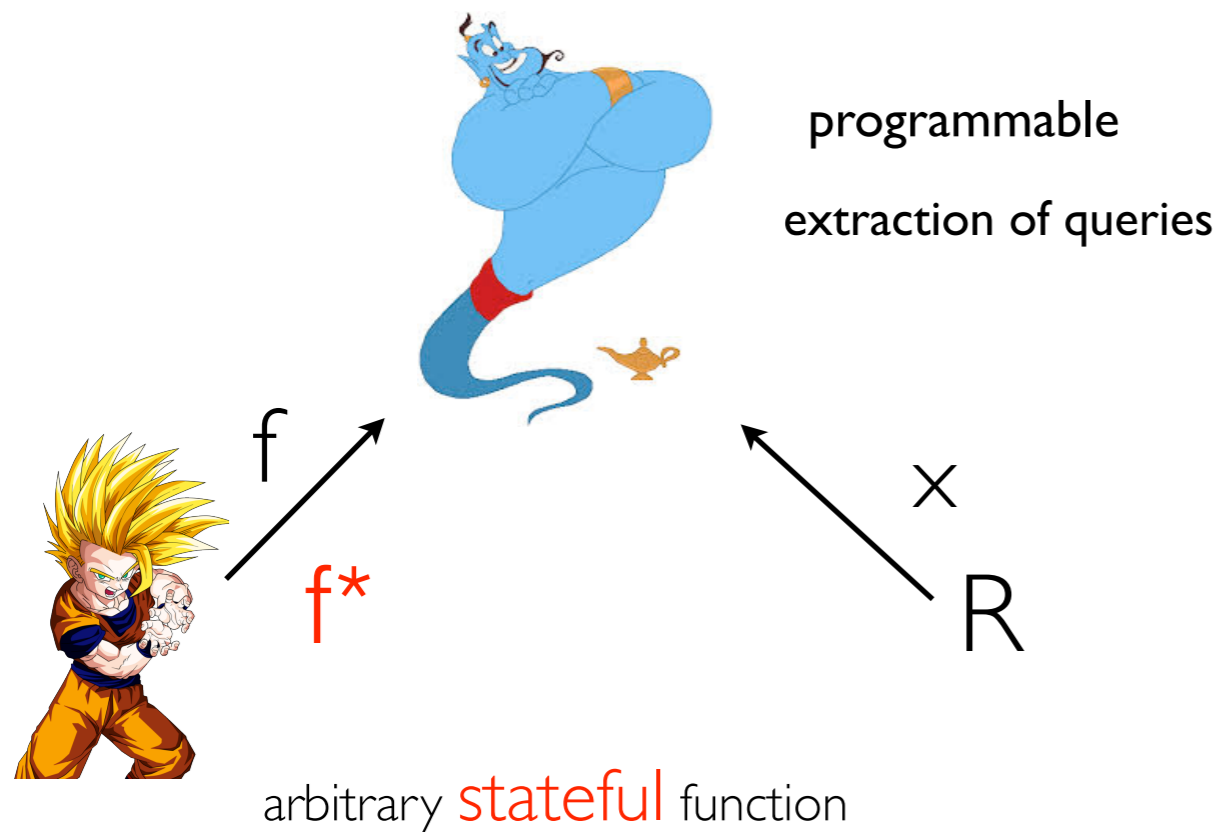


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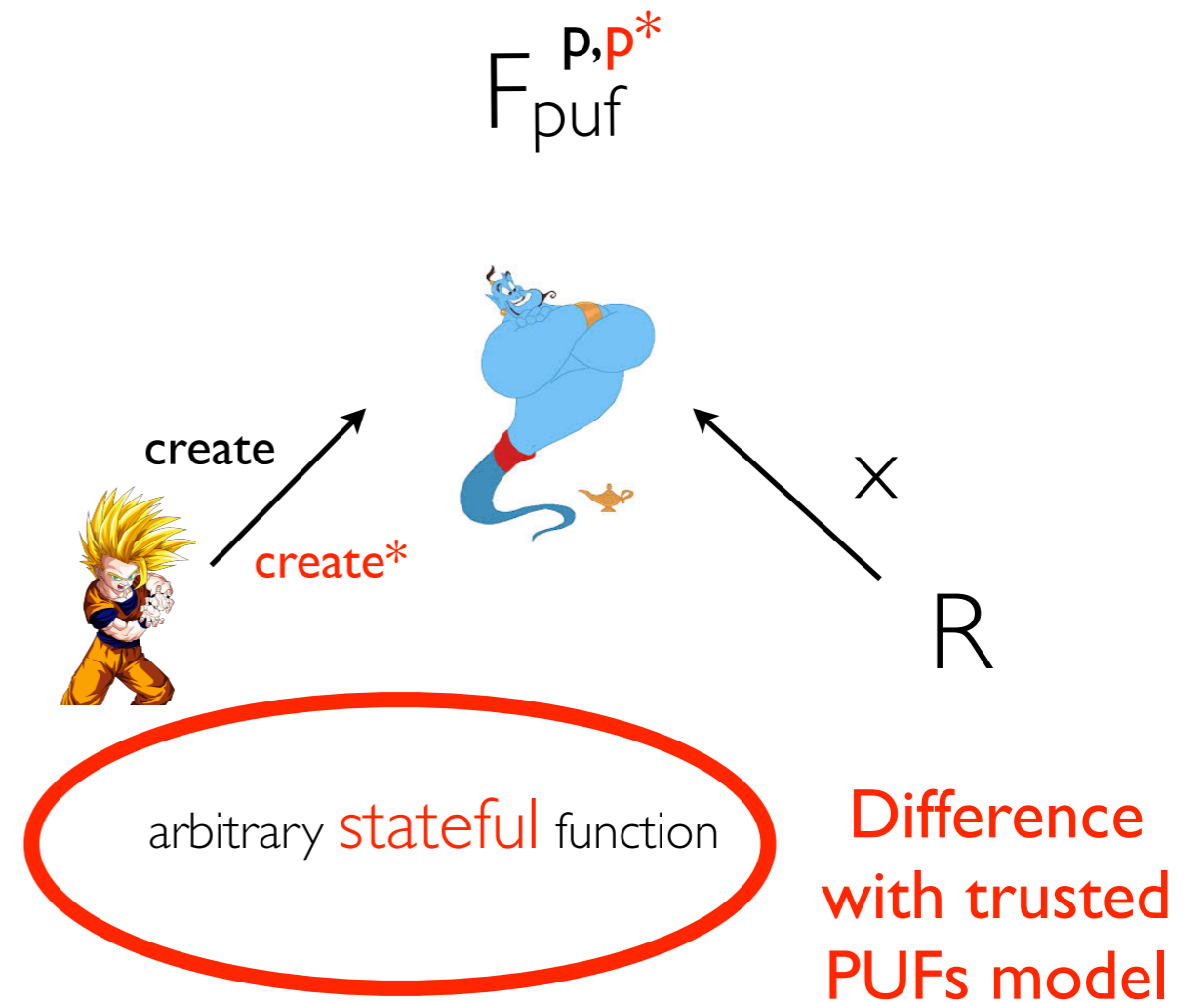


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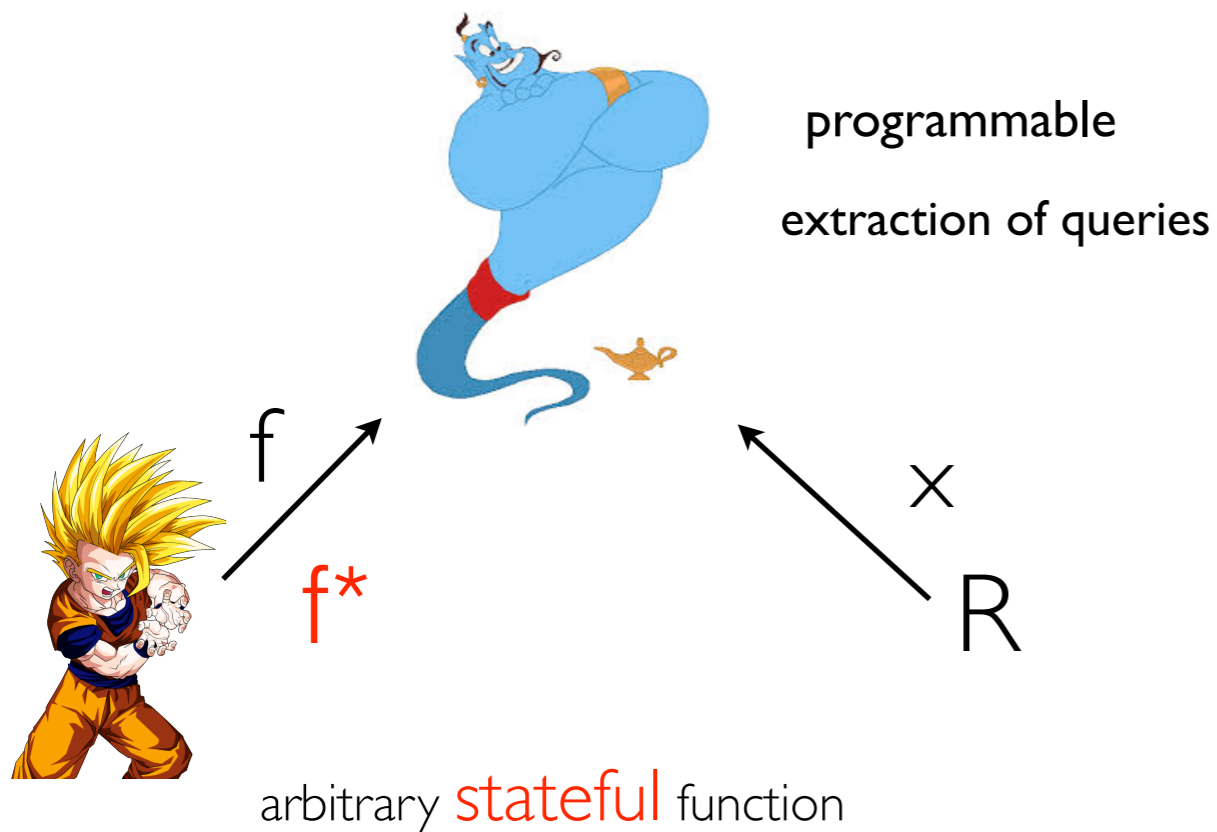


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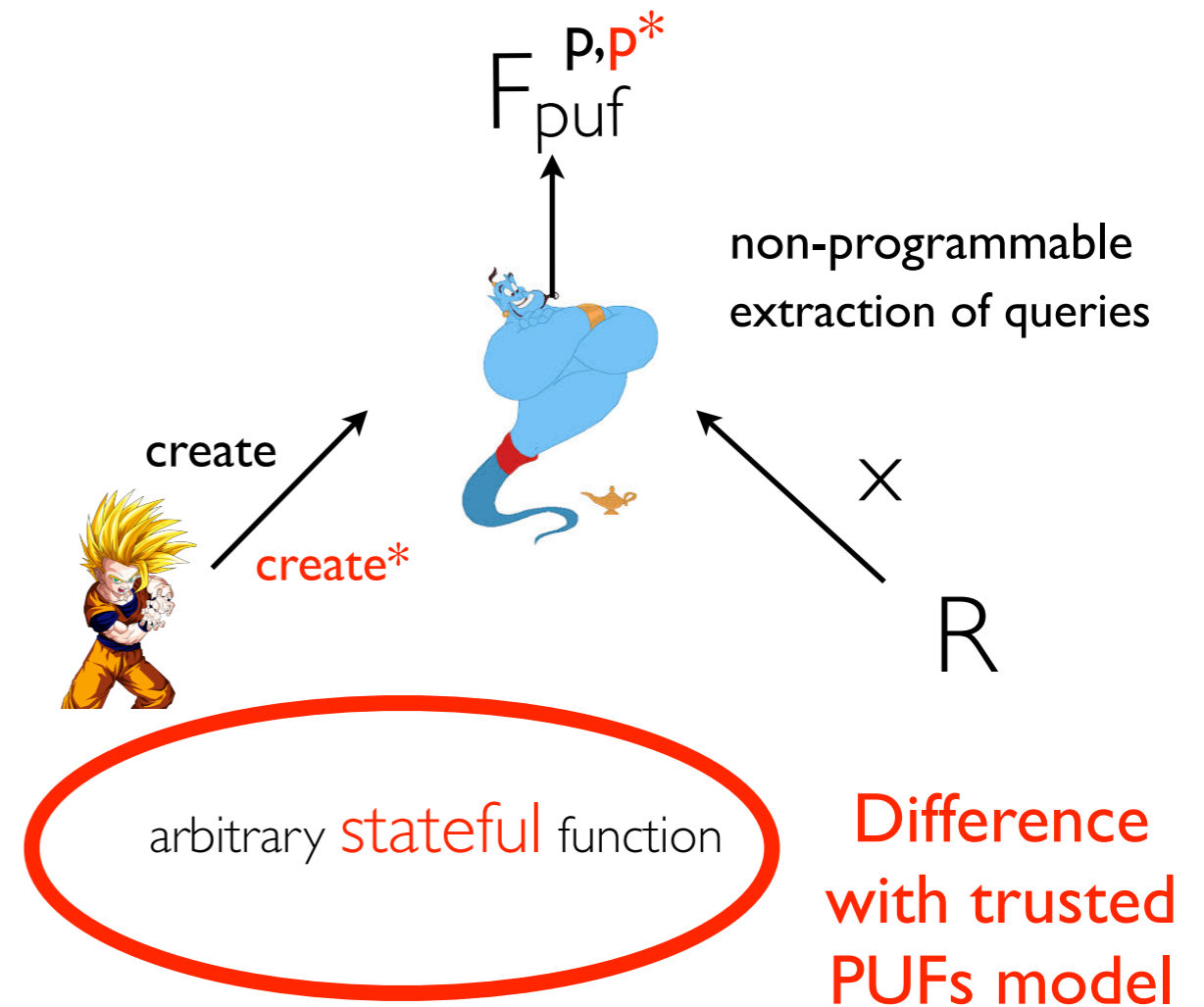


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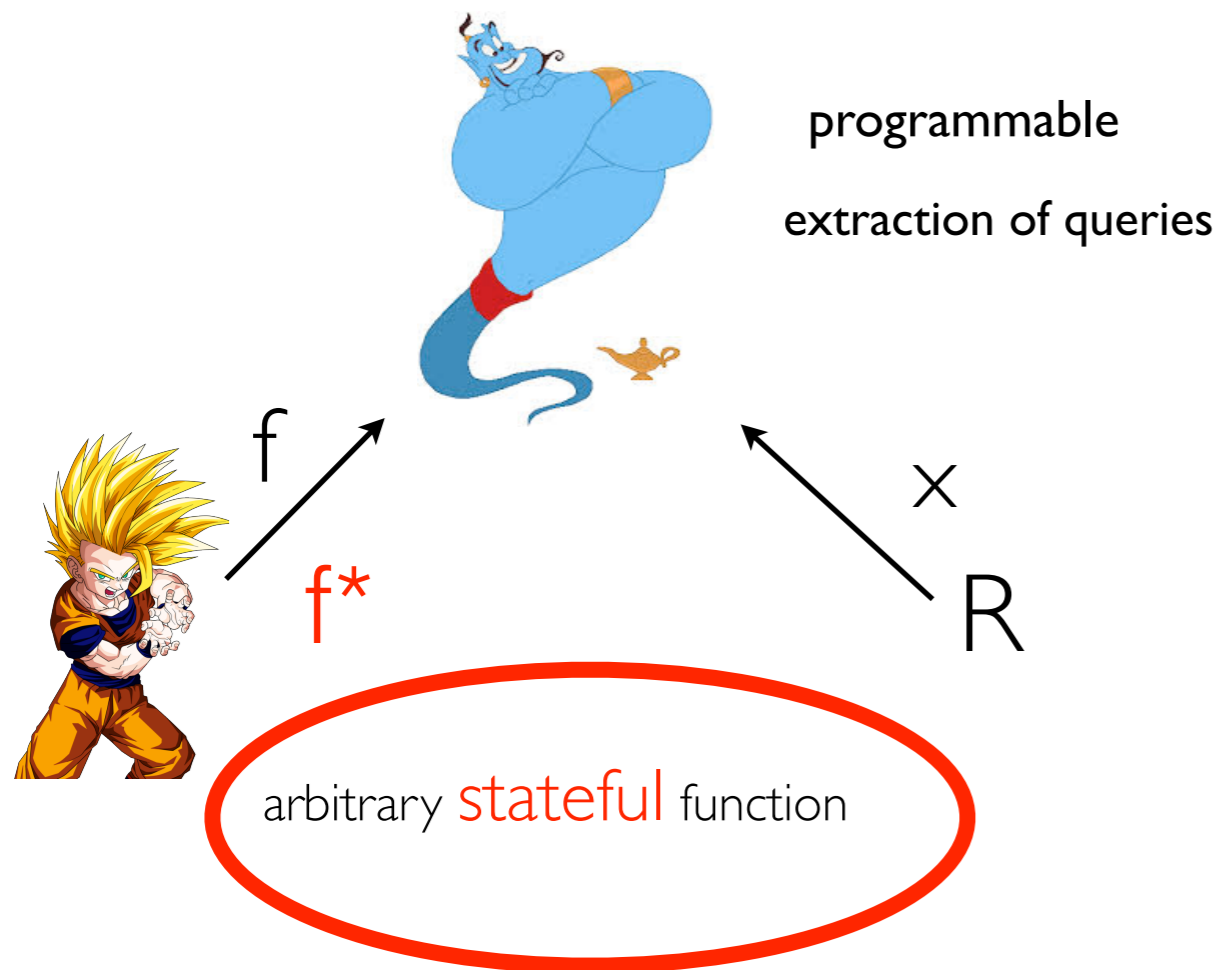


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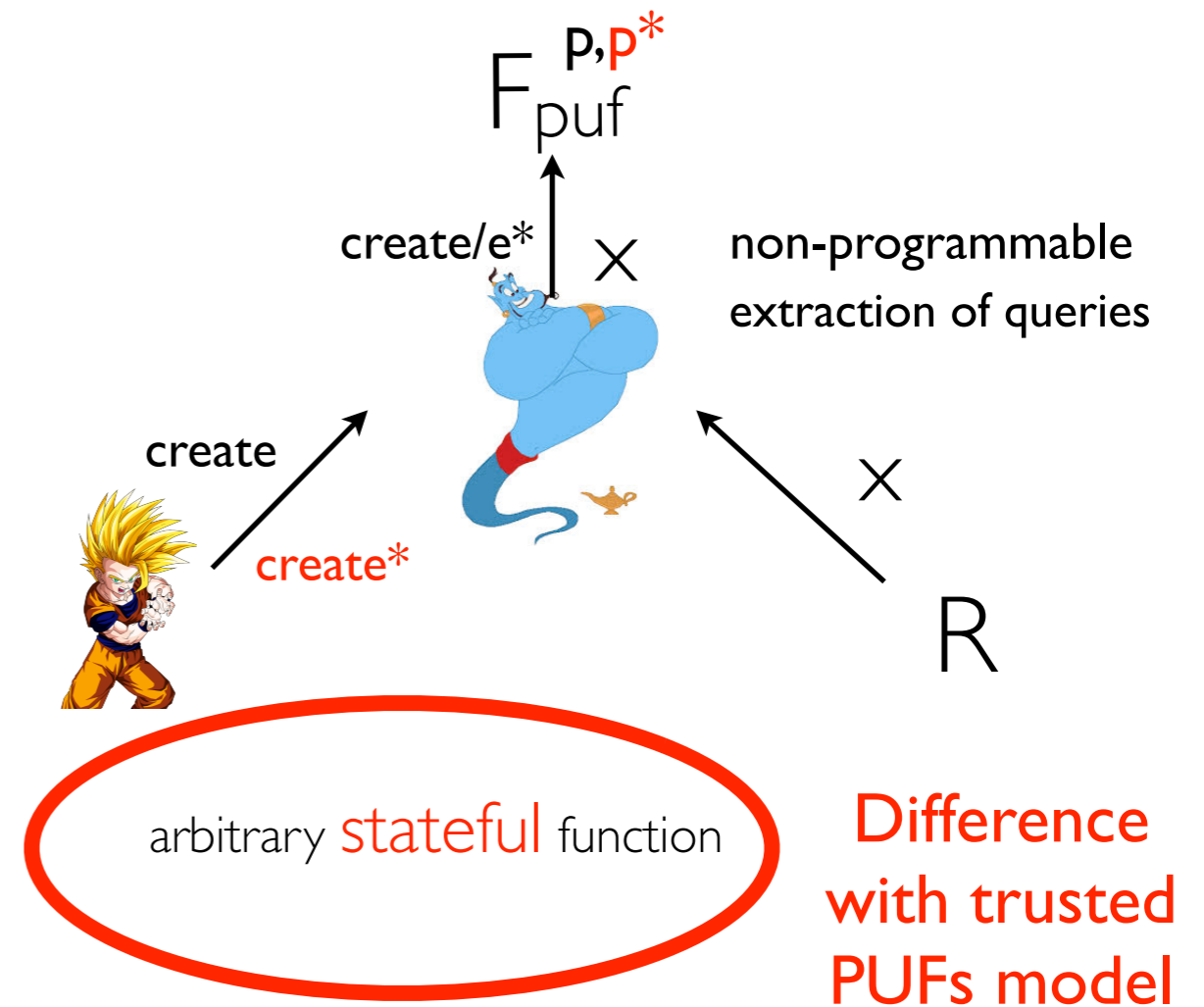


UC-Modeling Physical Assumptions

Tamper-proof Model
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(Malicious) PUF- Model
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Crucial: the security of each party depends only on the "goodness" of its own hardware

State of the art

	Unconditional UC Oblivious Transfer	Unconditional UC Commitment
Stateless Tokens		
(Malicious) PUFs		

State of the art

	Unconditional UC Oblivious Transfer	Unconditional UC Commitment
Stateless Tokens	Impossible [GIMS10]	
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	Unconditional UC Oblivious Transfer	Unconditional UC Commitment
Stateless Tokens	Impossible [GIMS10]	stand-alone Com [GIMS10] restricted adversary
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(Malicious) PUFs	?	stand-alone Com [OSVW13] ?

Caveat: Adv allowed to only poly queries

In this paper

	Unconditional UC Oblivious Transfer	Unconditional UC Commitment
Stateless Tokens	Impossible [GIMS10]	stand-alone Com [GIMS10] restricted adversary ?
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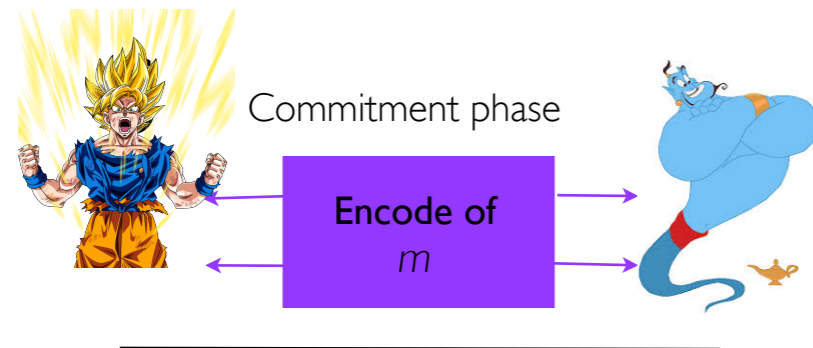
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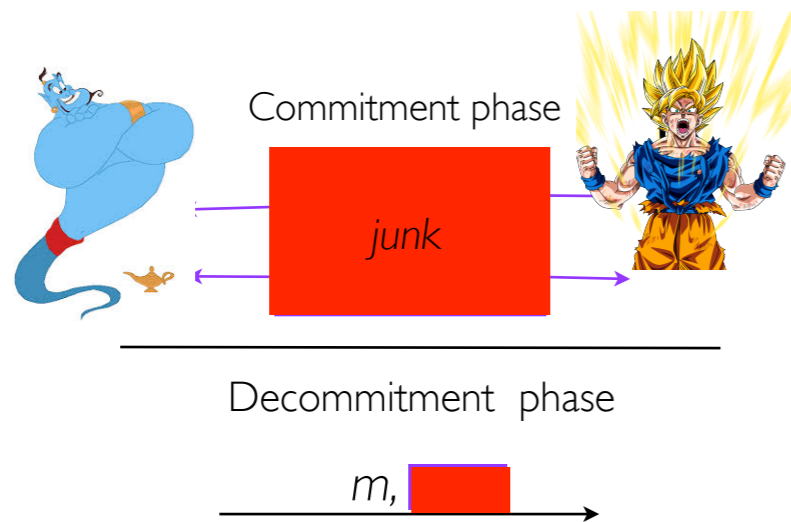
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(Malicious) PUFs	?	Yes

UC-Commitments with Physical Assumptions



Straight-line extractable



Straight-line equivocal



Our Technique

Our Technique

- Black-box Unconditional compiler

Our Technique


- Black-box Unconditional compiler

Extractable Com \Rightarrow Equivocal + Extractable Com

Our Technique

- Black-box Unconditional compiler

Extractable Com \Rightarrow Equivocal + Extractable Com

- Extractable Com 

```
graph LR; A[Extractable Com] --> B["(Malicious) PUF"]; A --> C[Stateless Token]
```

Black-Box Compiler

Black-box Proof of Equality of Commitments

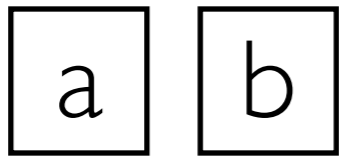
S

R

Black-box Proof of Equality of Commitments

S

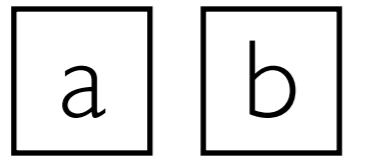
R



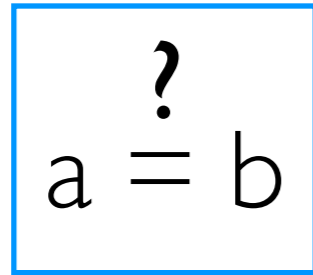
Black-box Proof of Equality of Commitments

S

R



zero-
knowledge



Black-box Proof of Equality of Commitments

Kilian 92

S

R

\boxed{a} \boxed{b}



zero-
knowledge

$\boxed{?}$
 $a = b$

Black-box Proof of Equality of Commitments

Kilian 92

S

R

S

R

\boxed{a} \boxed{b}



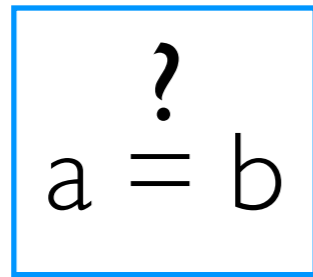
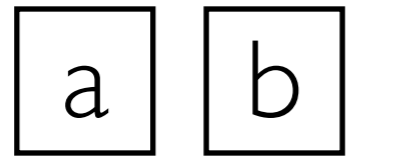
zero-
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$\boxed{?}$
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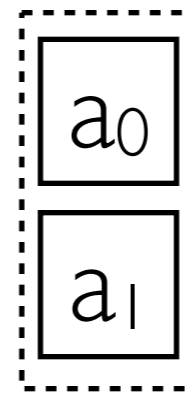
Kilian 92

S R



zero-
knowledge

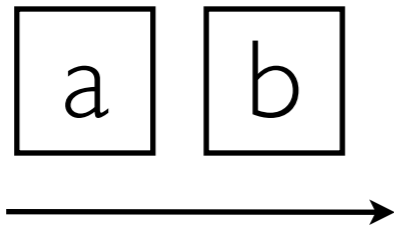
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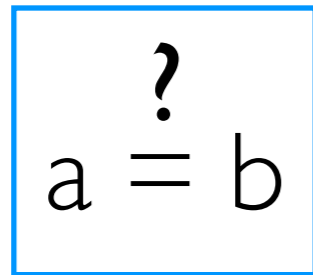
Black-box Proof of Equality of Commitments

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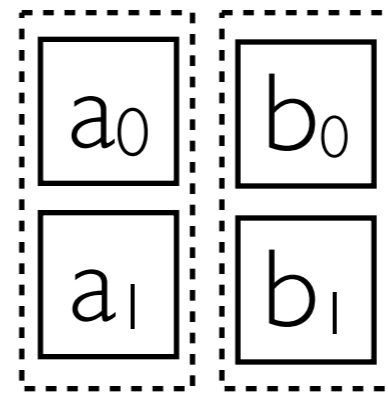
S R



zero-
knowledge



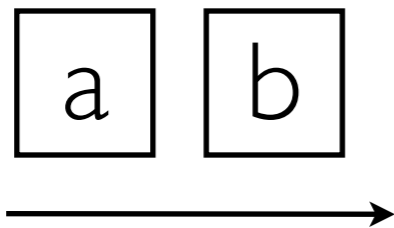
S a b R



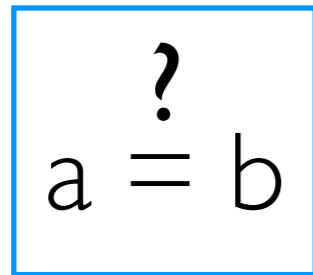
Black-box Proof of Equality of Commitments

Kilian 92

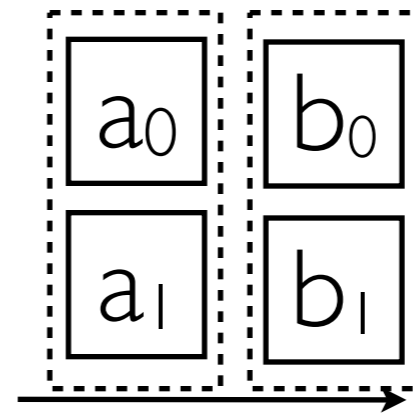
S R



zero-
knowledge



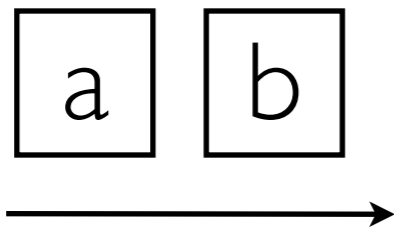
S a b R



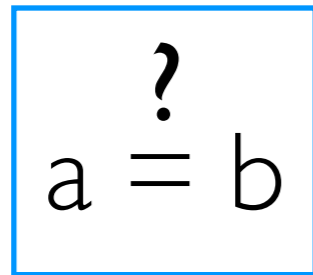
Black-box Proof of Equality of Commitments

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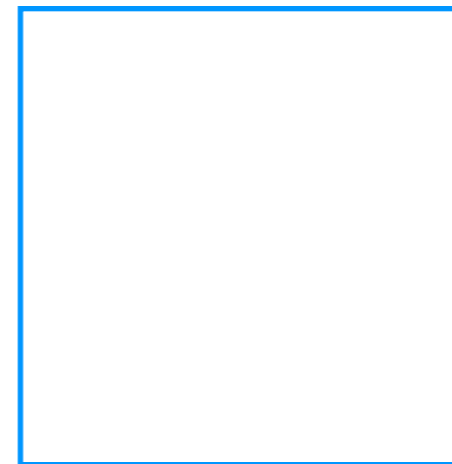
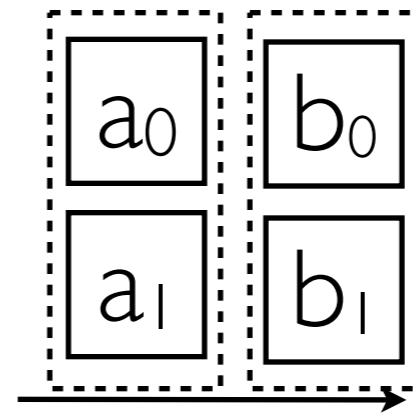
S R



zero-
knowledge



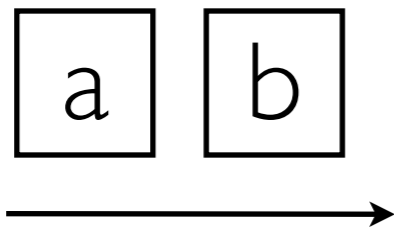
S a b R



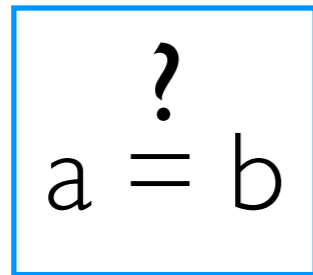
Black-box Proof of Equality of Commitments

Kilian 92

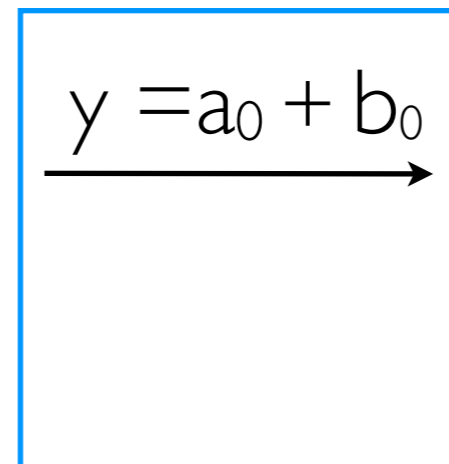
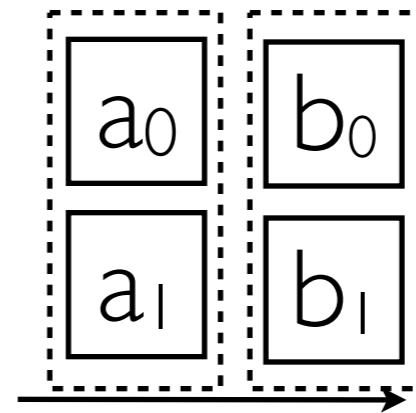
S R



zero-
knowledge



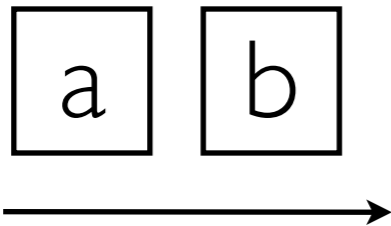
S a b R



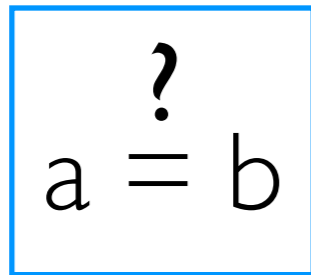
Black-box Proof of Equality of Commitments

Kilian 92

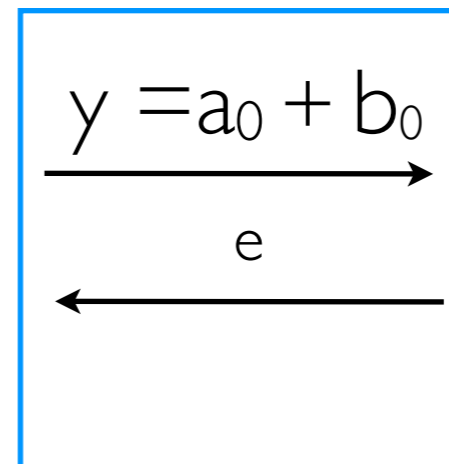
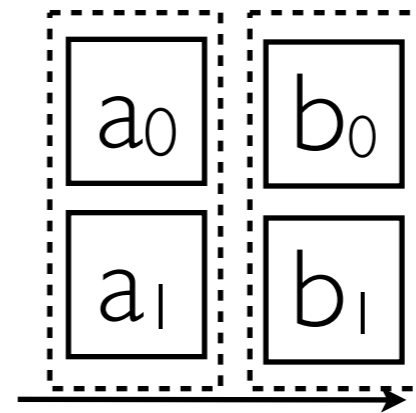
S R



zero-
knowledge



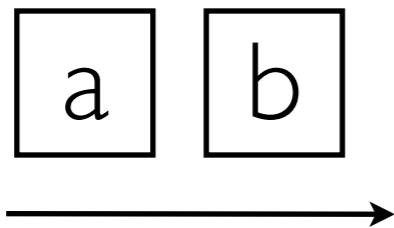
S a b R



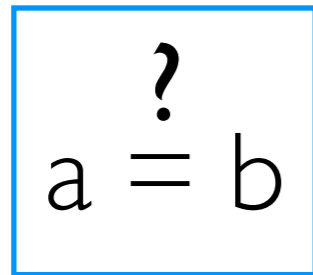
Black-box Proof of Equality of Commitments

Kilian 92

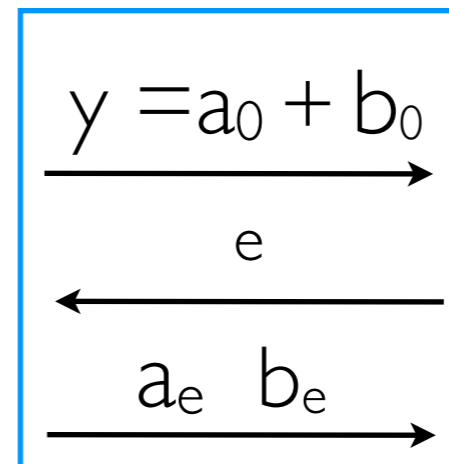
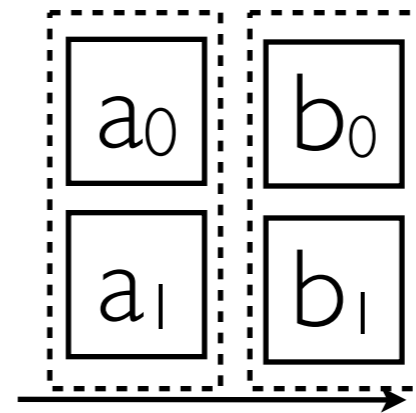
S R



zero-
knowledge



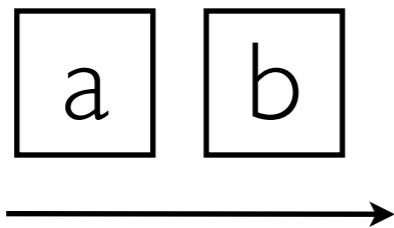
S a b R



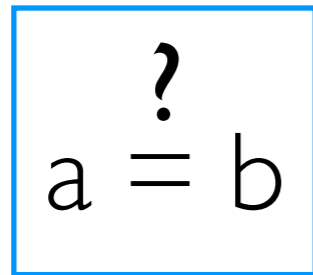
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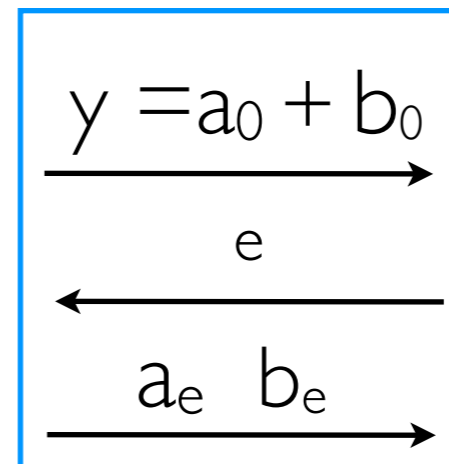
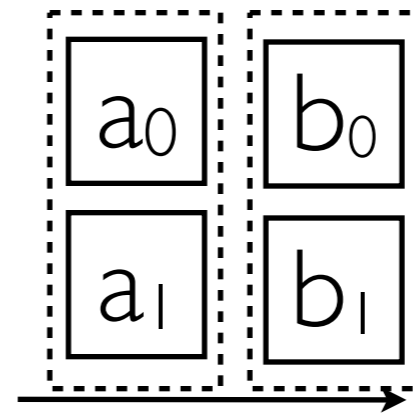
S R



zero-
knowledge



S a b R

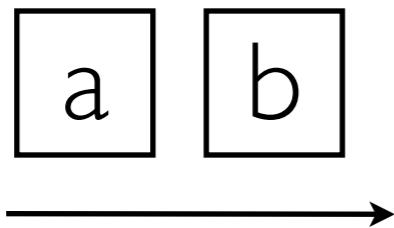


$y = a_e + b_e$

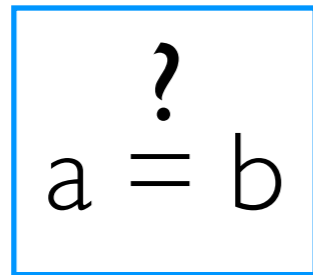
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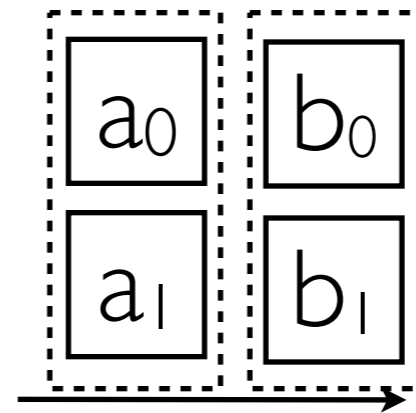
S R



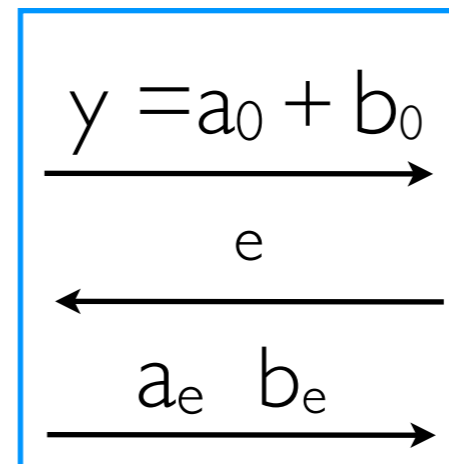
zero-
knowledge



S a b R



zero-
knowledge

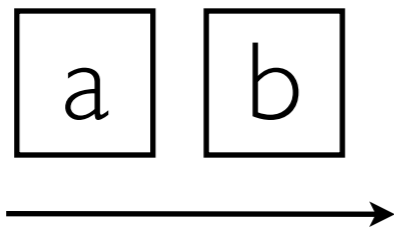


$y = a_e + b_e$

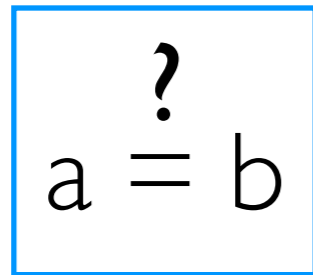
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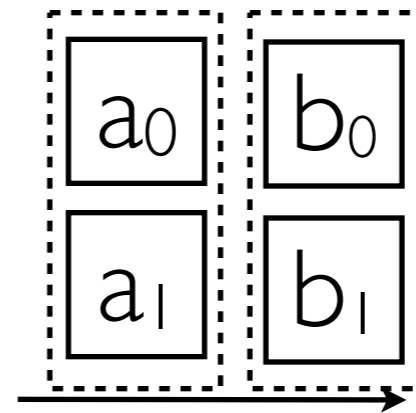
S R



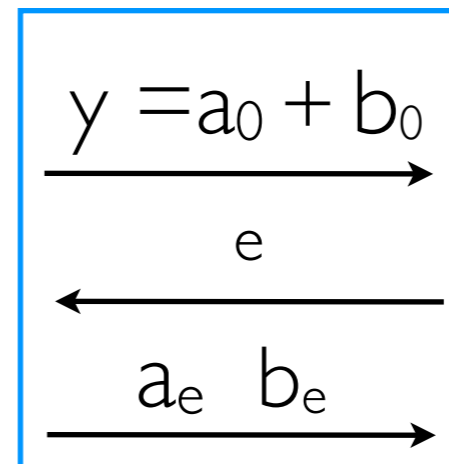
zero-
knowledge



S a b R



zero-
knowledge



Soundness 1/2

?
 $y = a_e + b_e$

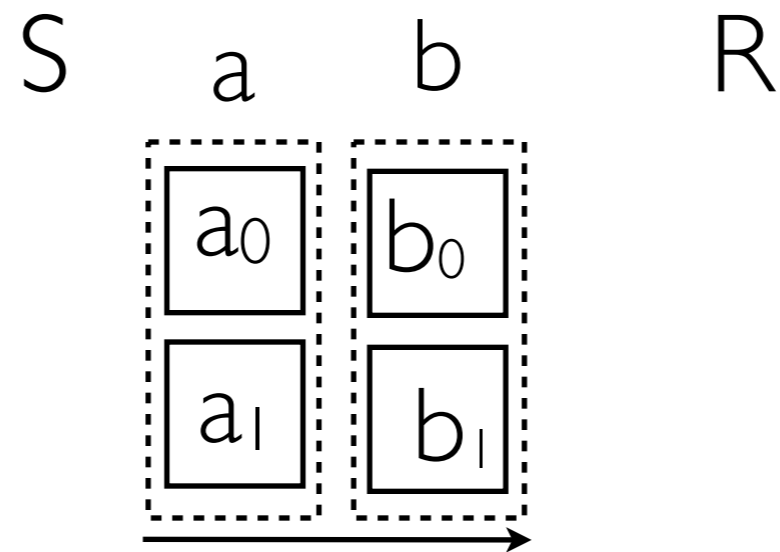
Straight-line ZK BB proof of equality

Straight-line ZK BB proof of equality

Assume boxes are
extractable

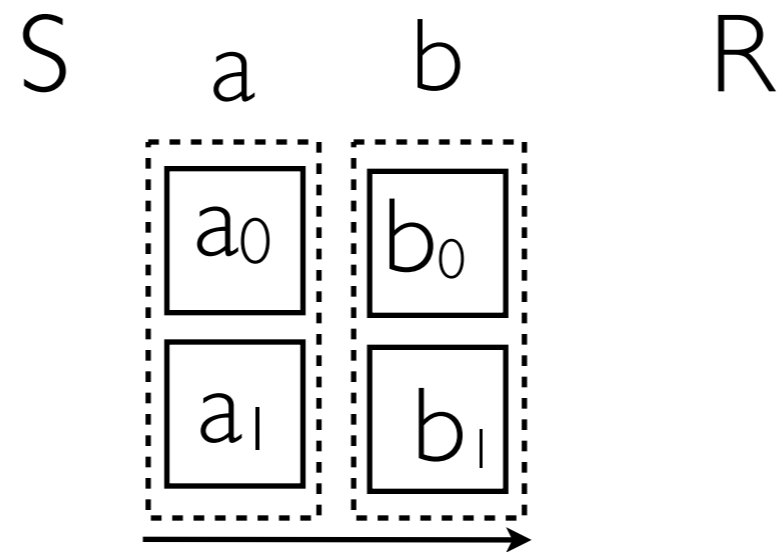
Straight-line ZK BB proof of equality

Assume boxes are
extractable

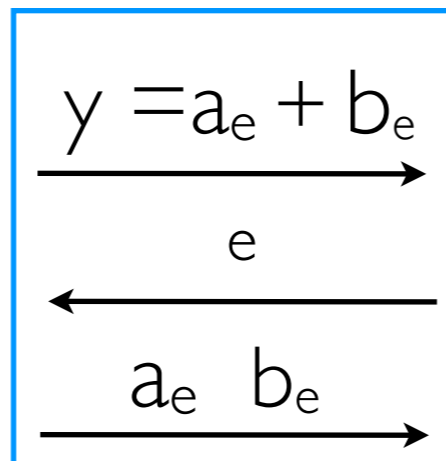


Straight-line ZK BB proof of equality

Assume boxes are
extractable

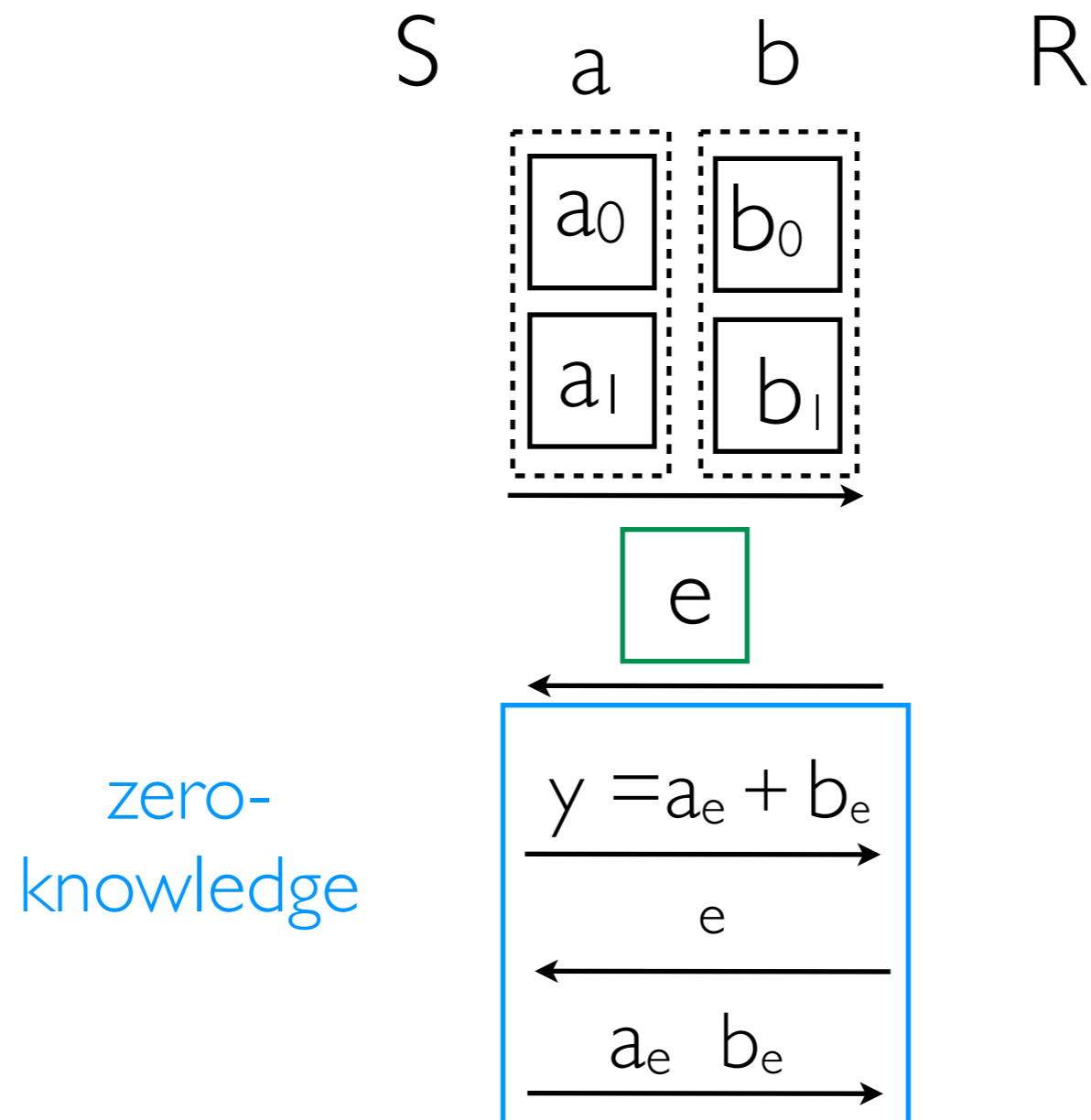


zero-
knowledge



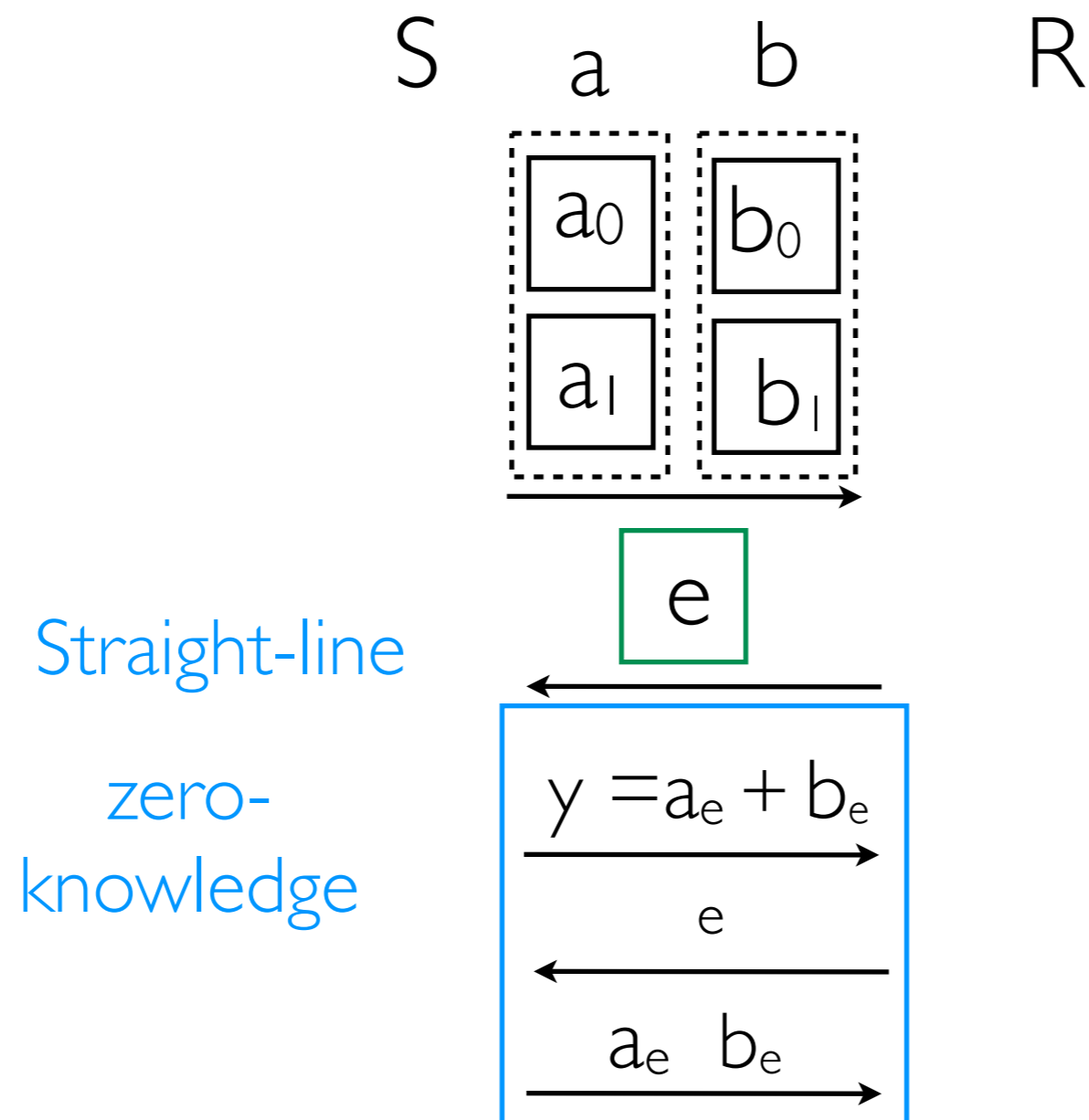
Straight-line ZK BB proof of equality

Assume boxes are
extractable



Straight-line ZK BB proof of equality

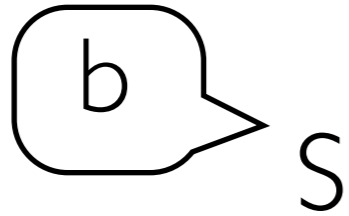
Assume boxes are
extractable



Compiler

Extractable Commitment \Rightarrow Equivocal + Extractable

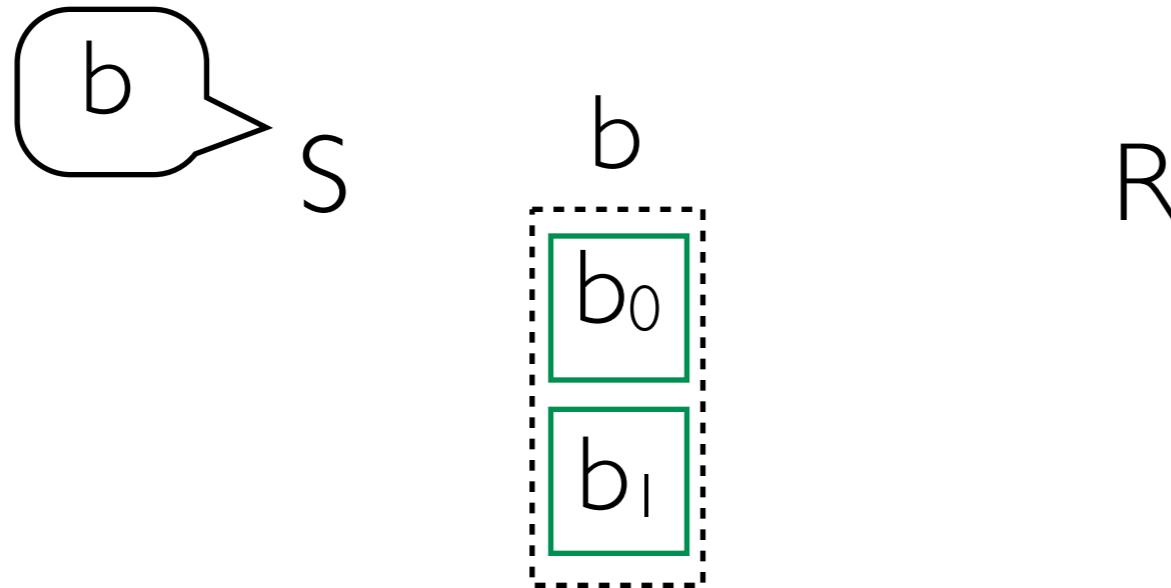
Compiler: Equivocal commitments from Extractable Commitments



R

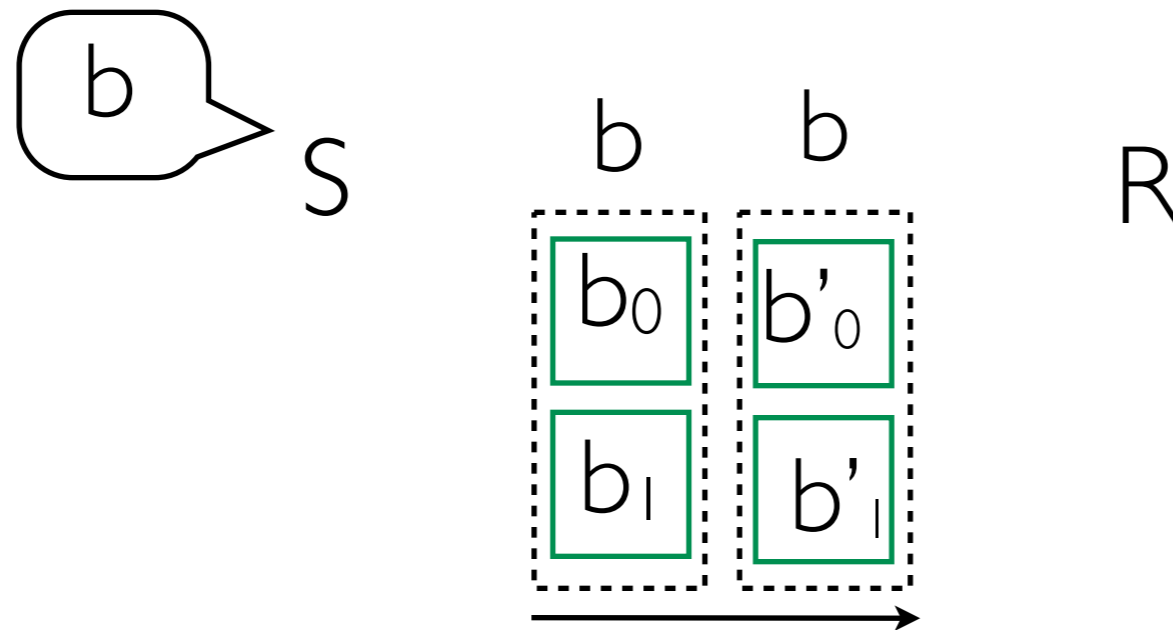
Decommitment

Compiler: Equivocal commitments from Extractable Commitments



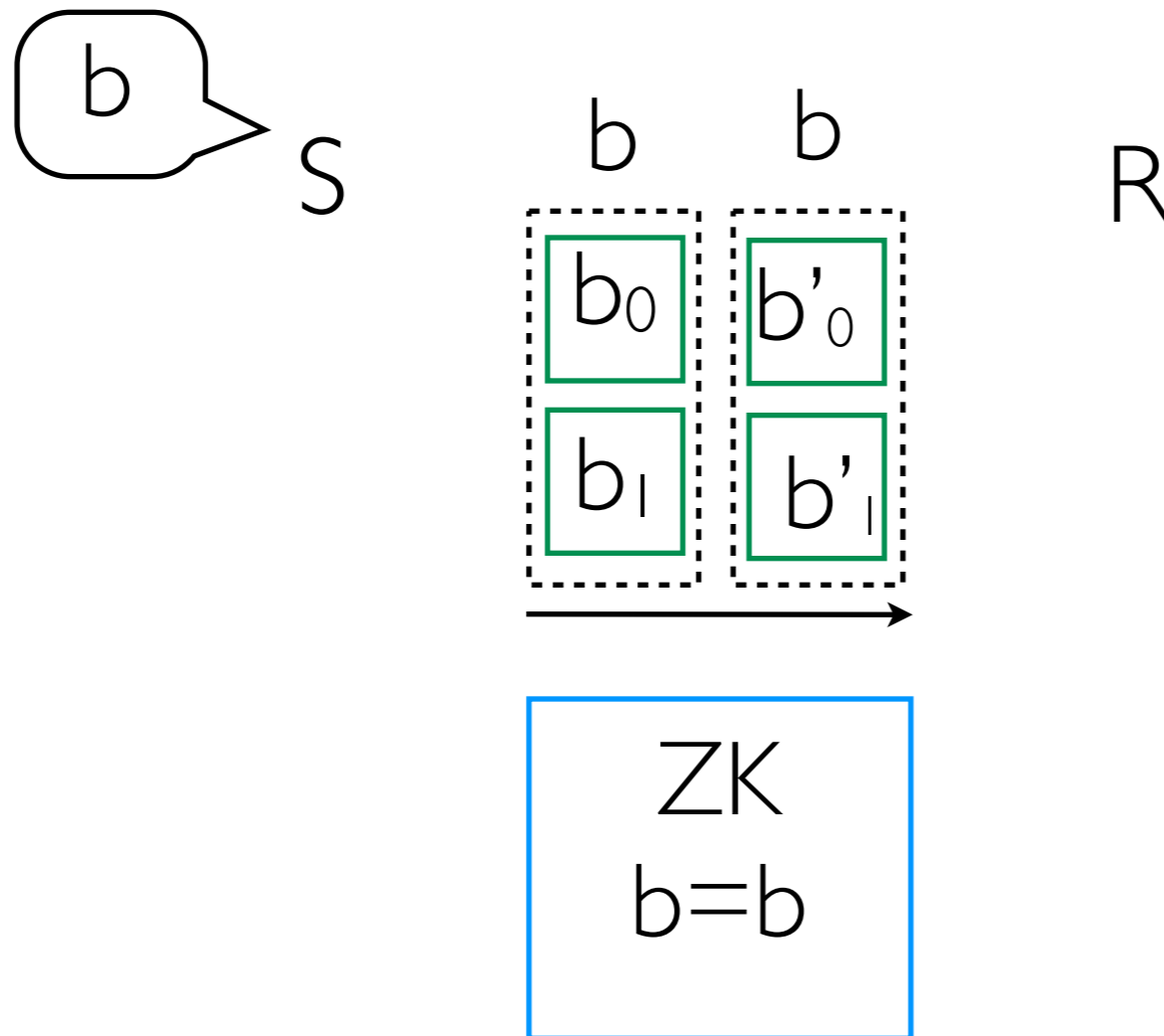
Decommitment

Compiler: Equivocal commitments from Extractable Commitments



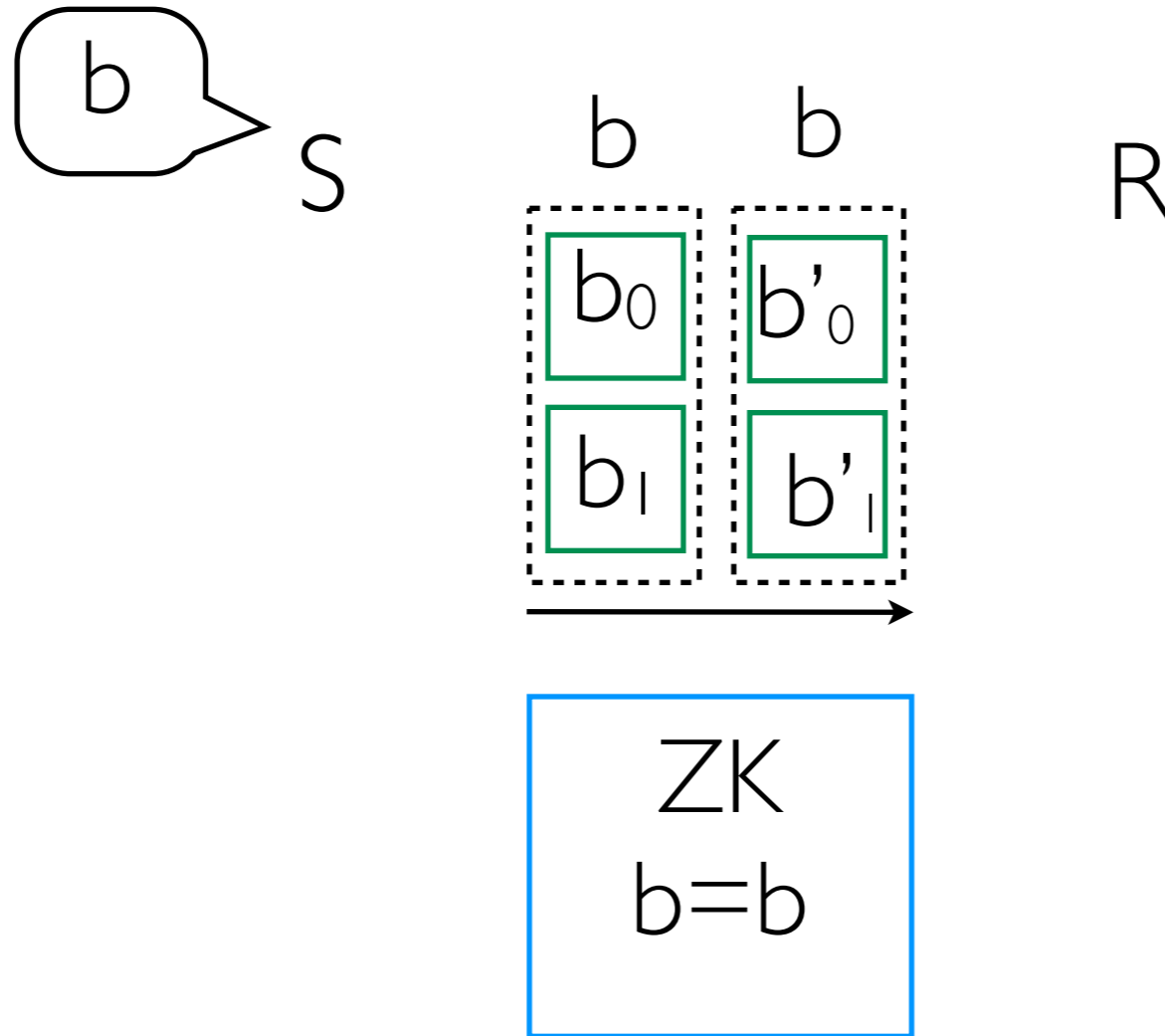
Decommitment

Compiler: Equivocal commitments from Extractable Commitments



Decommitment

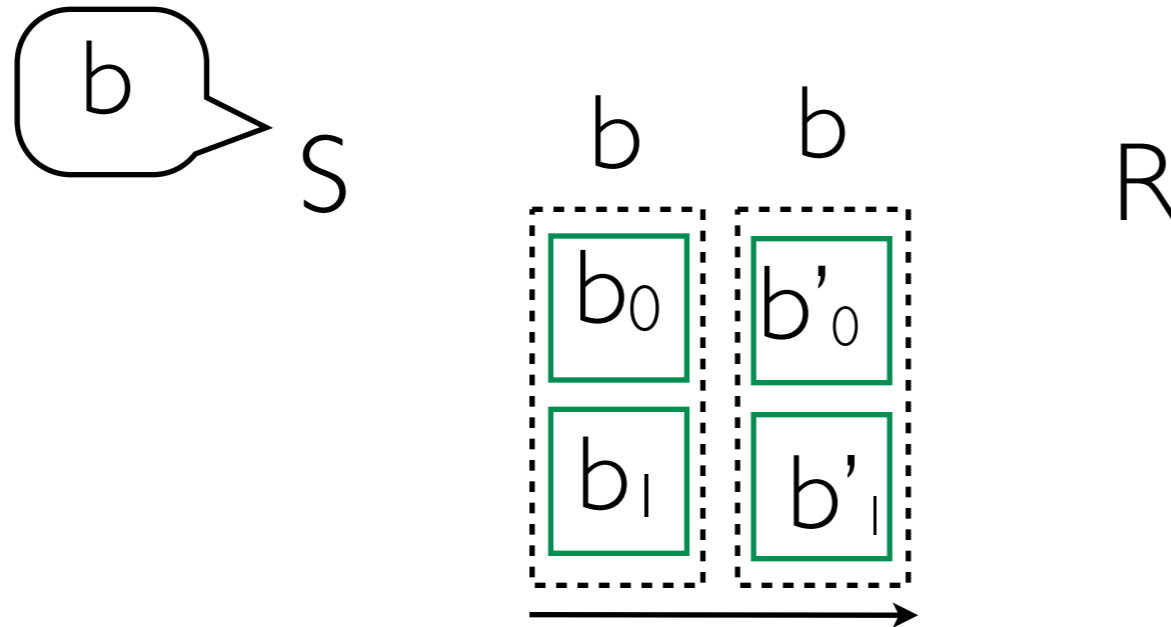
Compiler: Equivocal commitments from Extractable Commitments



Decommitment

open **either**
first or second com

Compiler: Equivocal commitments from Extractable Commitments



idea used
in Hofl I

ZK
 $b=b$

Decommitment

open **either**
first or second com

Equivocality

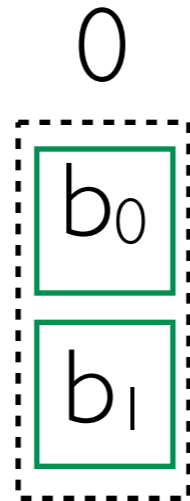
Straight-line
equivocality



Decommitment

Equivocality

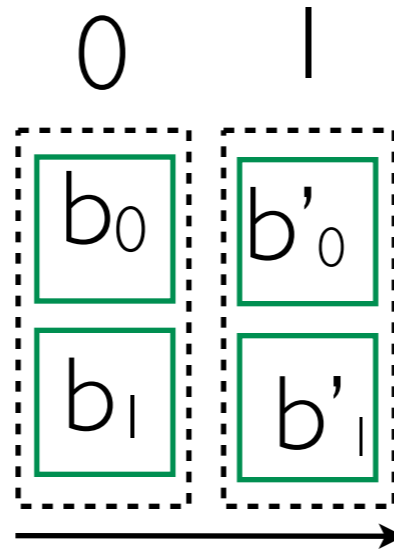
Straight-line
equivocality



Decommitment

Equivocality

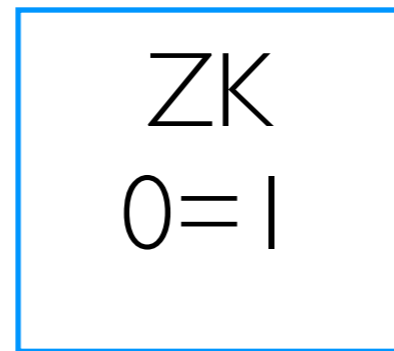
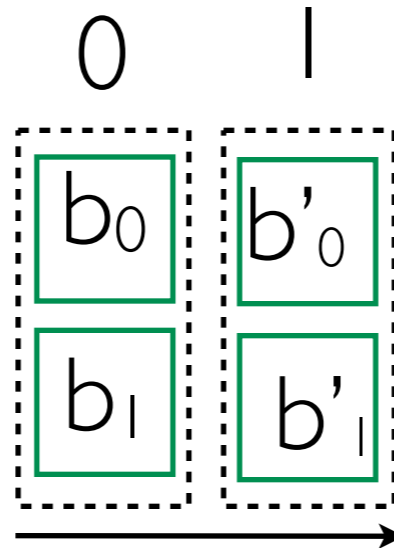
Straight-line
equivocality



Decommitment

Equivocality

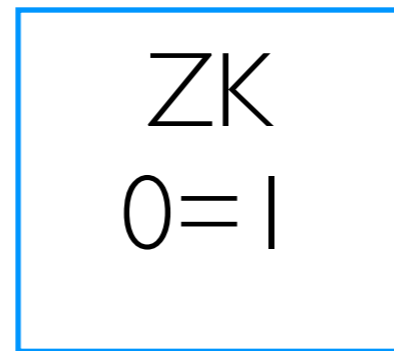
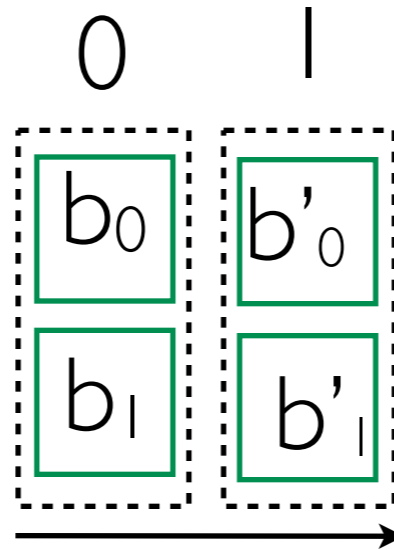
Straight-line
equivocality



Decommitment

Equivocality

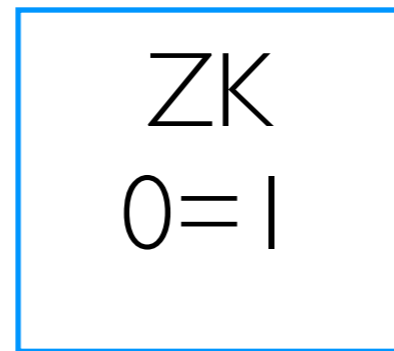
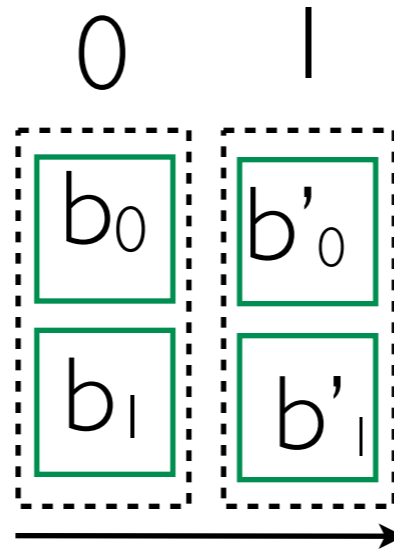
Straight-line
equivocality



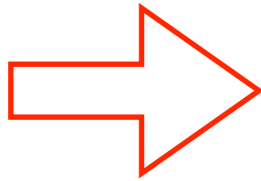
Decommitment

Equivocality

Straight-line
equivocality



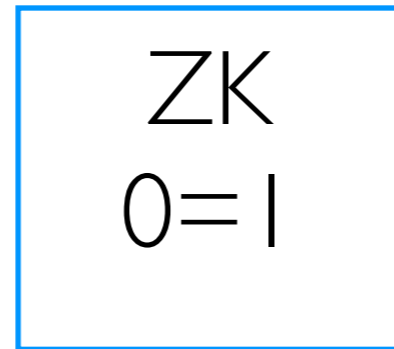
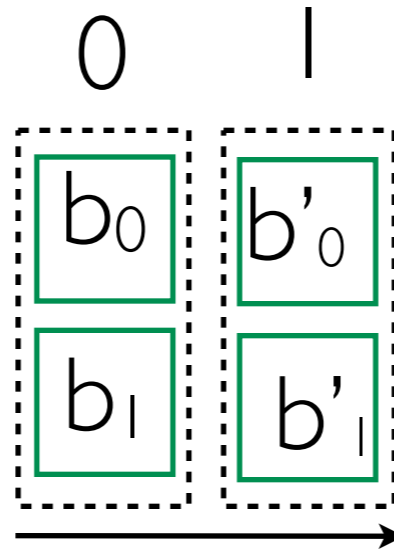
b



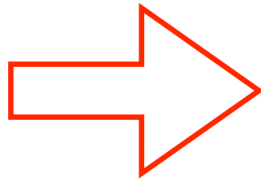
Decommitment

Equivocality

Straight-line
equivocality



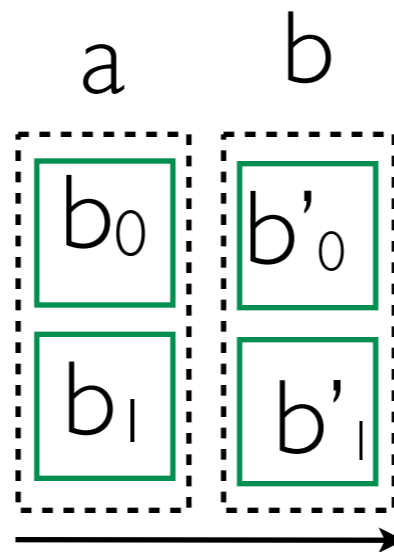
b



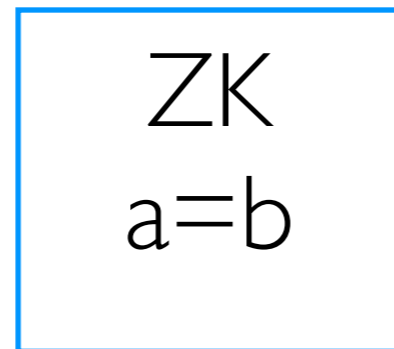
Decommitment

open **b**

Extractability



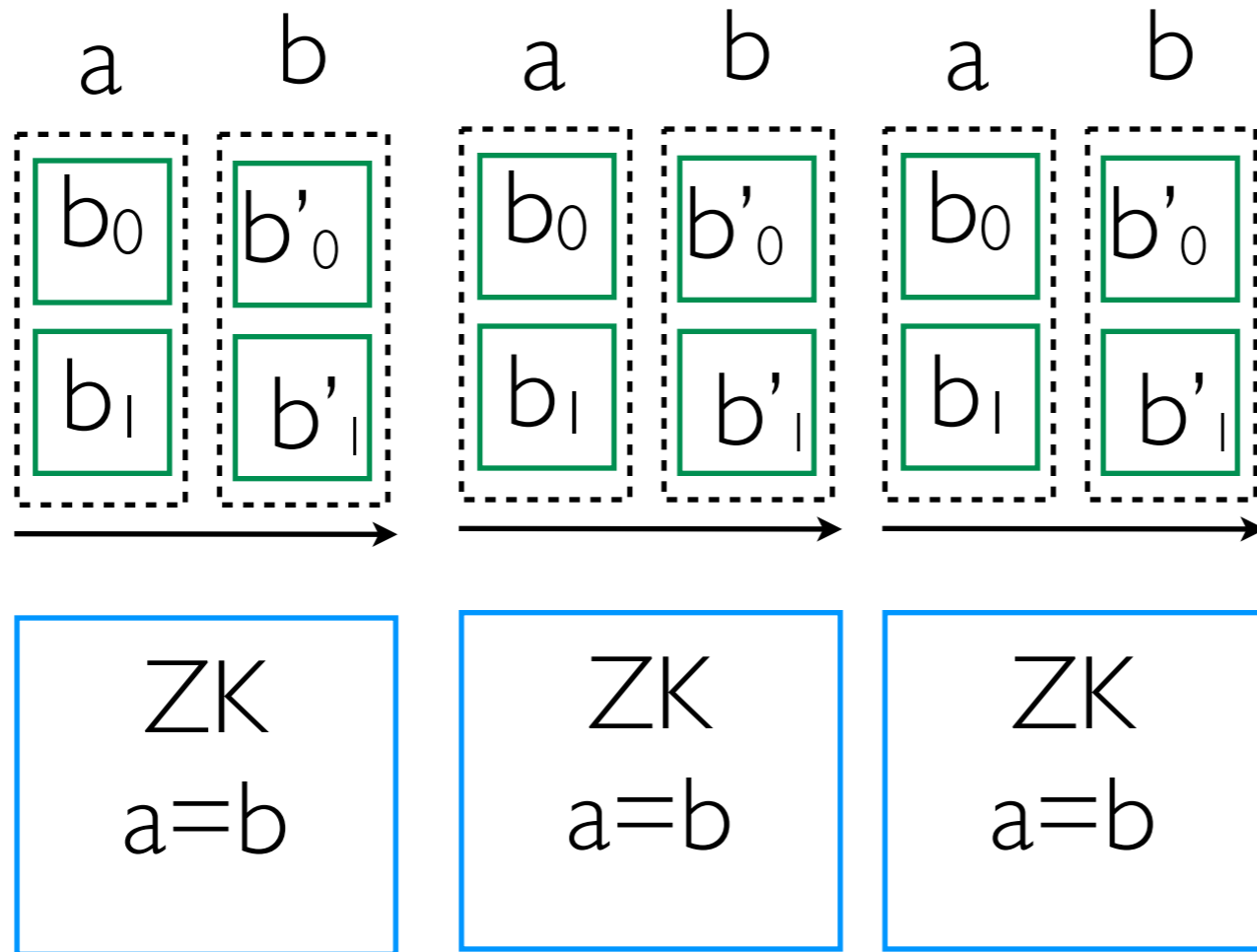
Straight-line
extractability



Decommitment

open **either**
a or b

Extractability



Extractability



Decommitment

open **either**
a or b

open **either**
a or b

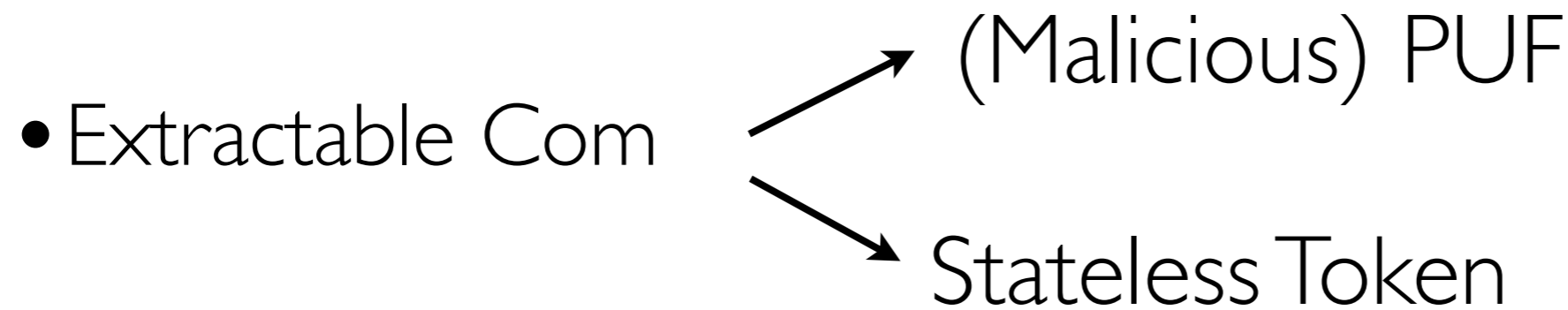
open **either**
a or b

check that all open
to the same bit

Our Technique

- Black-box compiler

Extractable Com \Rightarrow Equivocal + Extractable Com





Extractable Commitment from (malicious) PUFs

Extractable Commitment from (malicious) PUFs



Extractable Commitment from (malicious) PUFs

for free: stand-alone
unconditional commitment
from [OSVW13]
PUF-Com

Extractable Commitment from (malicious) PUFs

S

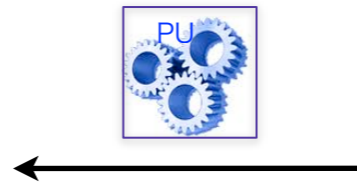
R

for free: stand-alone
unconditional commitment
from [OSVW13]
PUF-Com



Extractable Commitment from (malicious) PUFs

S

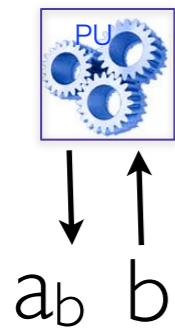


R

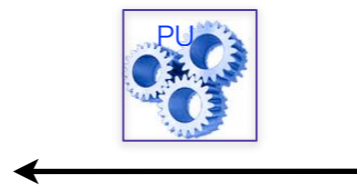
for free: stand-alone
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Extractable Commitment from (malicious) PUFs



S

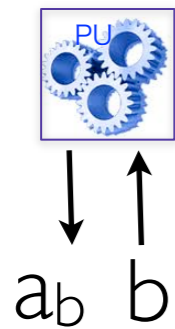


R

for free: stand-alone
unconditional commitment
from [OSVW13]
PUF-Com



Extractable Commitment from (malicious) PUFs



S



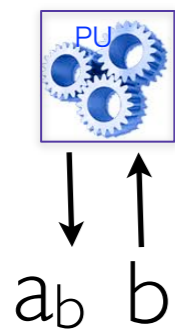
R

$$c = \text{PUF-Com}(a, b)$$

for free: stand-alone
unconditional commitment
from [OSVW13]
PUF-Com



Extractable Commitment from (malicious) PUFs



S

R



$$c = \text{PUF-Com}(a_b)$$



for free: stand-alone unconditional commitment from [OSVW13] PUF-Com

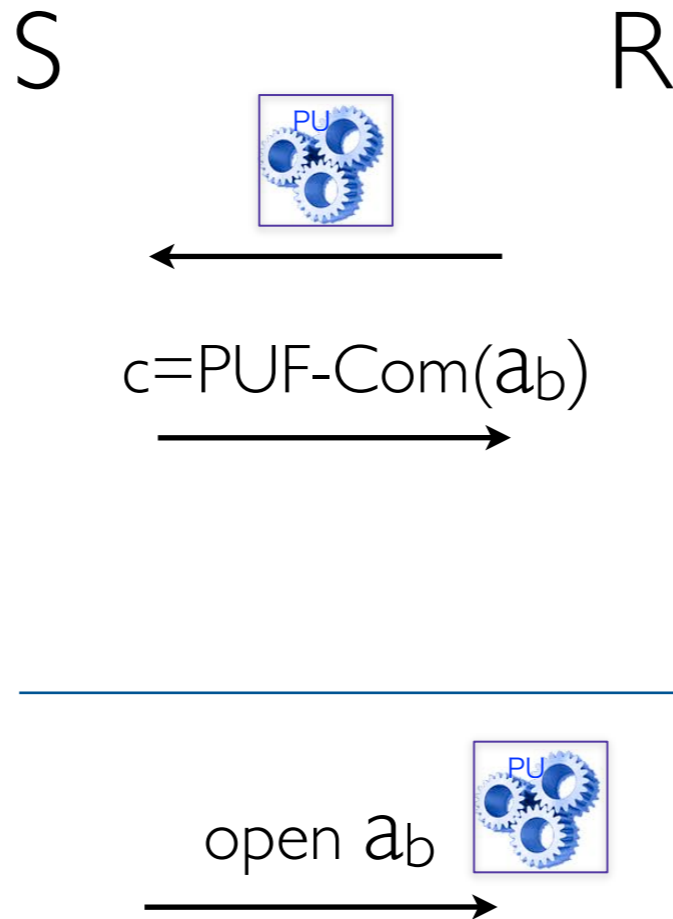
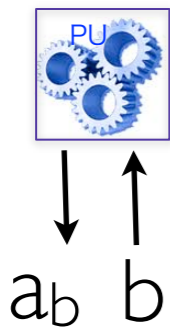


open a_b



Extractable Commitment from (malicious) PUFs

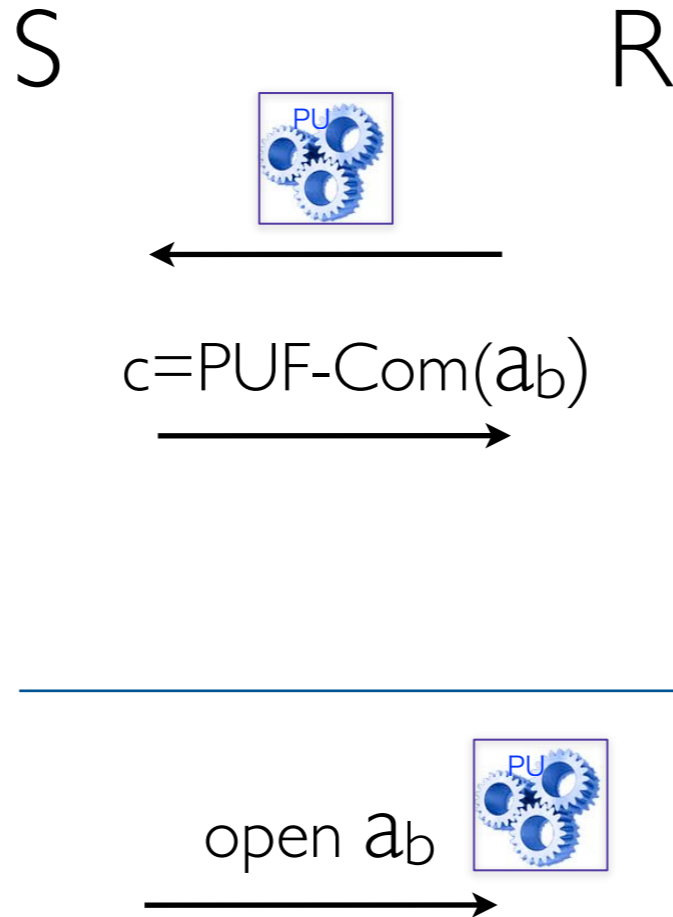
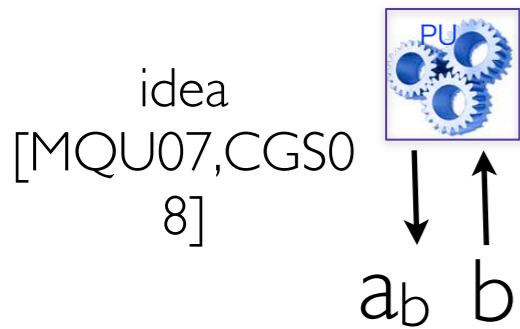
Problem 1: Adv can query with 0/1



for free: stand-alone unconditional commitment from [OSVW13] PUF-Com

Extractable Commitment from (malicious) PUFs

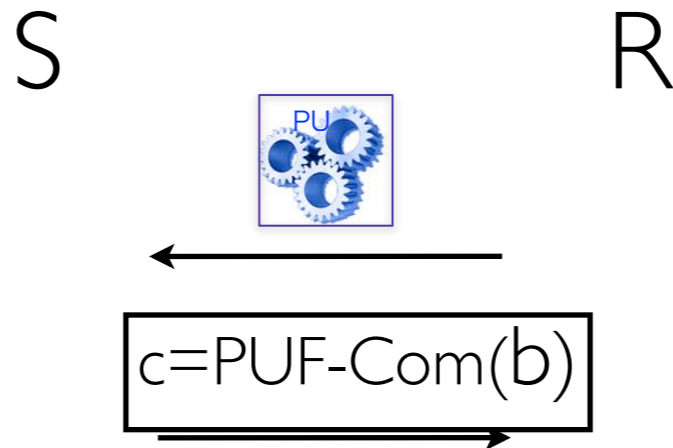
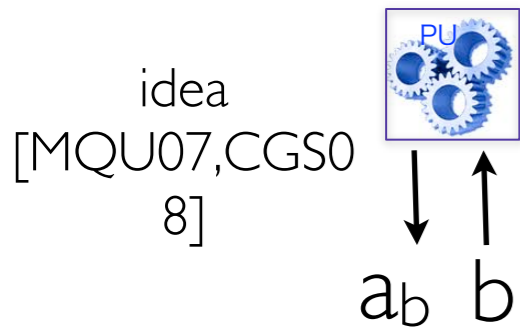
Problem 1: Adv can query with 0/1



for free: stand-alone unconditional commitment from [OSVW13] PUF-Com

Extractable Commitment from (malicious) PUFs

Problem 1: Adv can query with 0/1



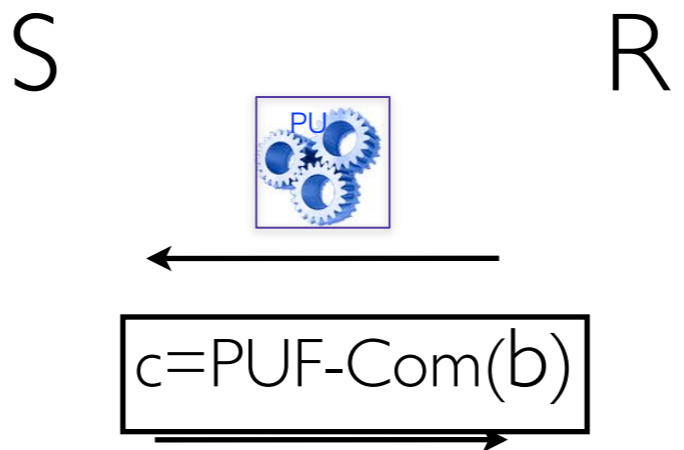
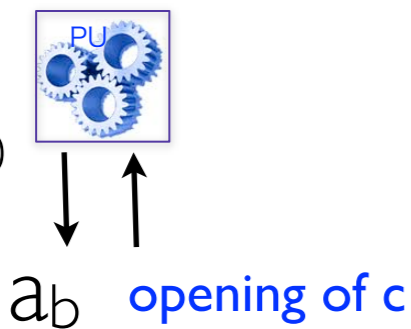
for free: stand-alone unconditional commitment from [OSVW13] PUF-Com



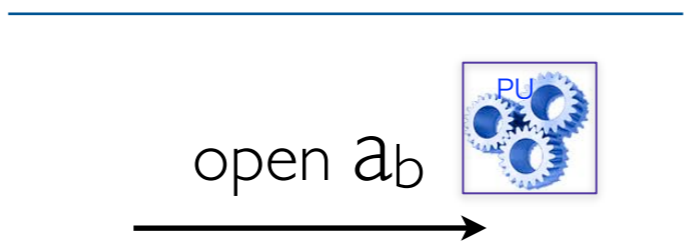
Extractable Commitment from (malicious) PUFs

Problem 1: Adv can query with 0/1

idea
[MQU07,CGS08]

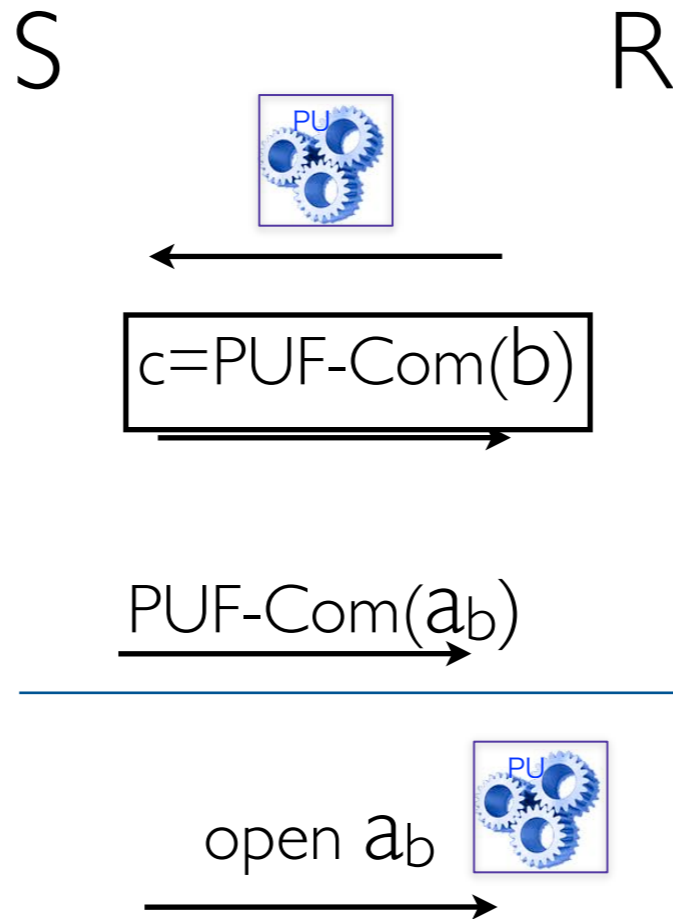
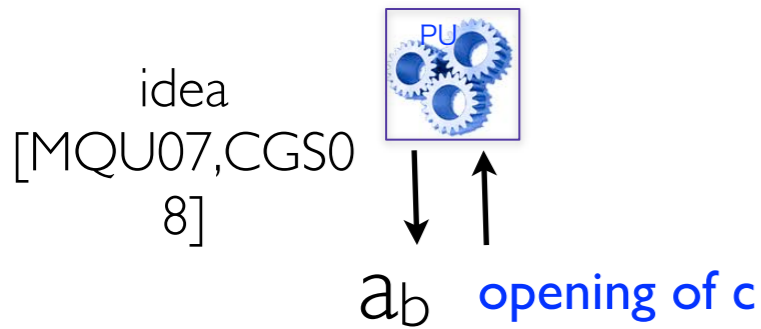


for free: stand-alone unconditional commitment from [OSVW13] PUF-Com



Extractable Commitment from (malicious) PUFs

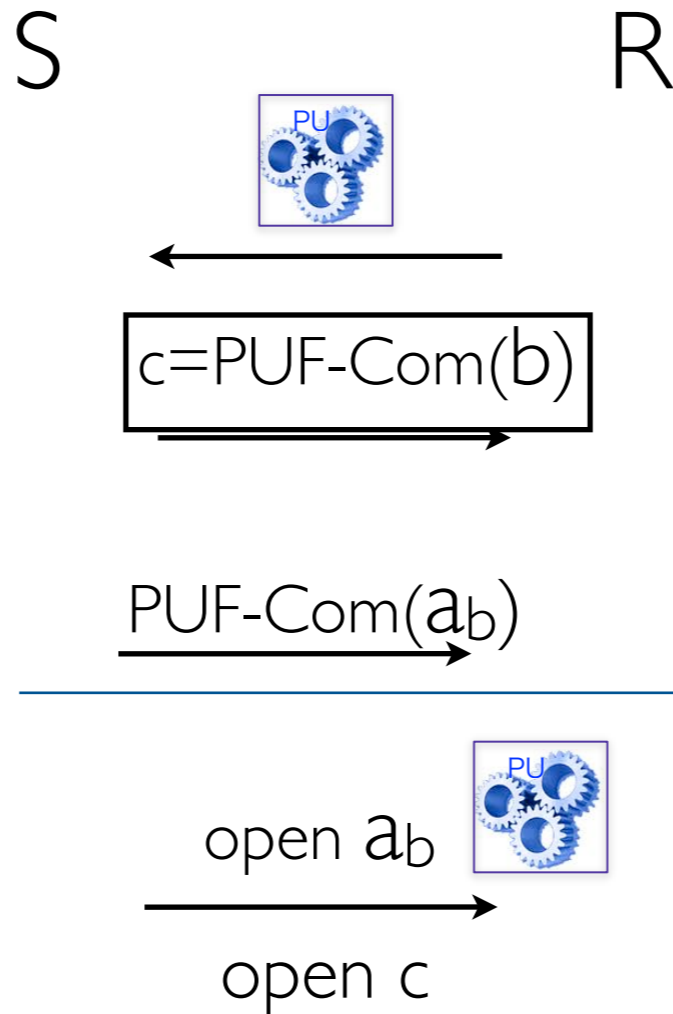
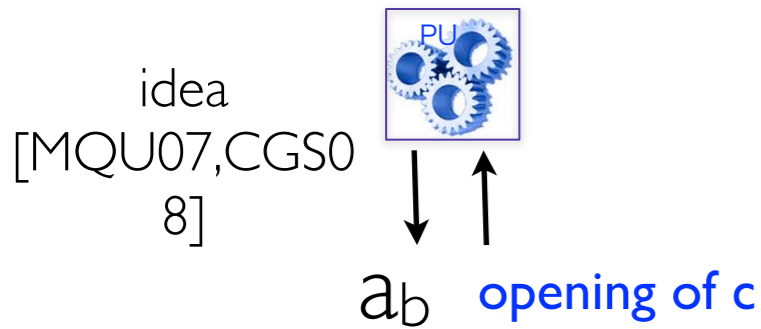
Problem 1: Adv can query with 0/1



for free: stand-alone unconditional commitment from [OSVW13] PUF-Com

Extractable Commitment from (malicious) PUFs

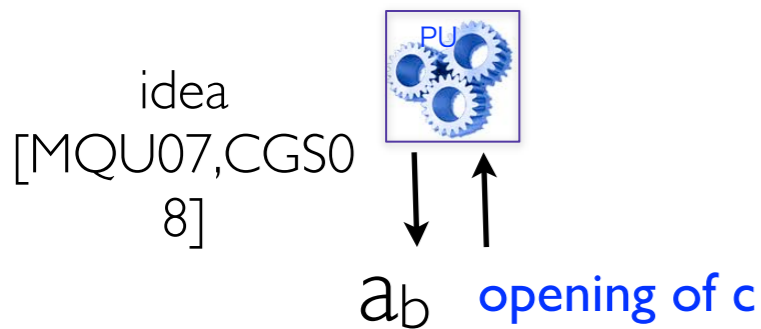
Problem 1: Adv can query with 0/1



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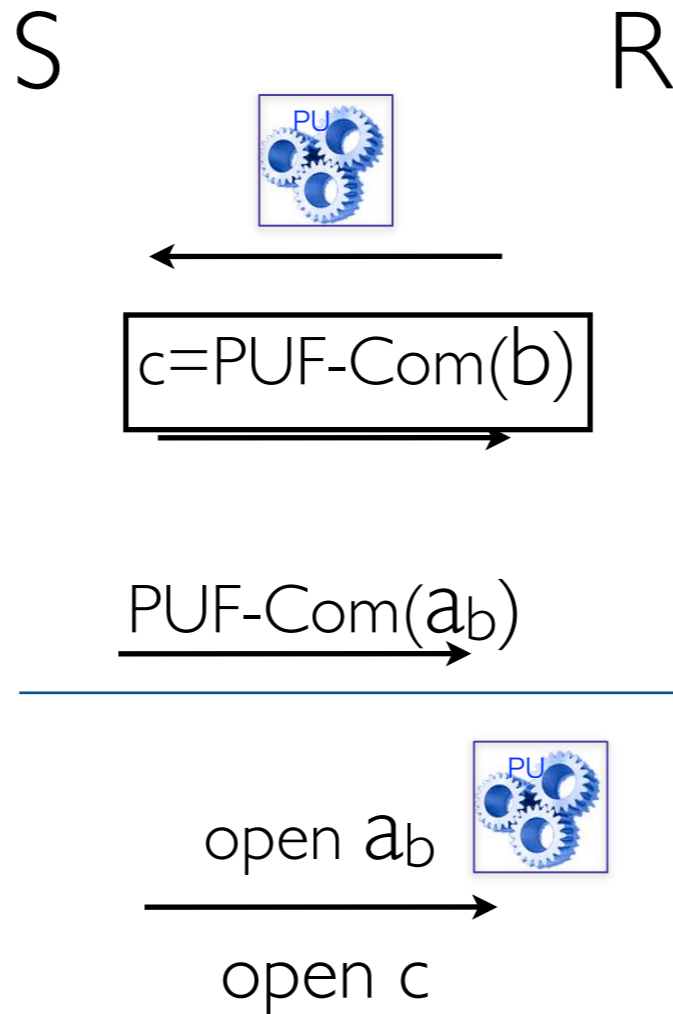
Extractable Commitment from (malicious) PUFs

Problem 1: Adv can query with 0/1



Problem 2: Adv queries with strings that are “close” to the actual opening

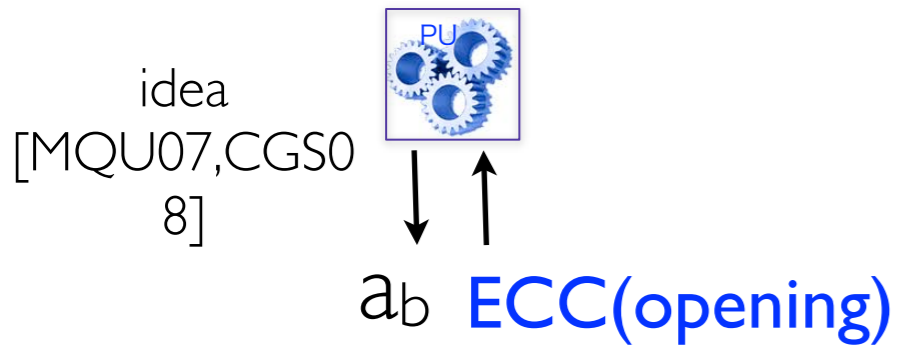
unpredictability does not hold for close queries



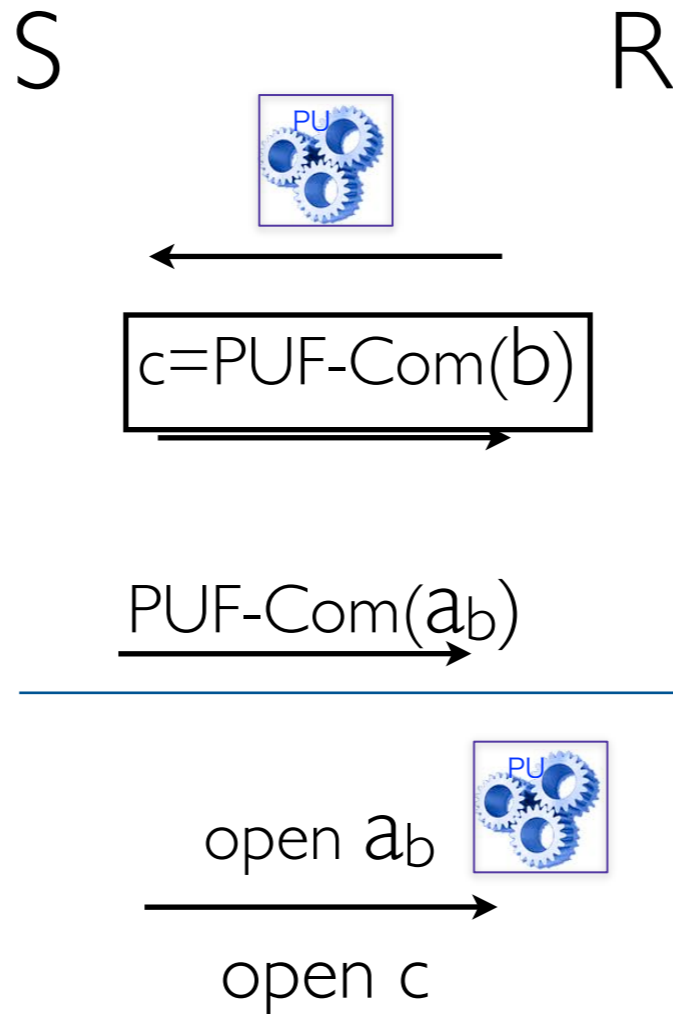
for free: stand-alone unconditional commitment from [OSVW13] PUF-Com

Extractable Commitment from (malicious) PUFs

Problem 1: Adv can query with 0/1



for free: stand-alone unconditional commitment from [OSVW13] PUF-Com

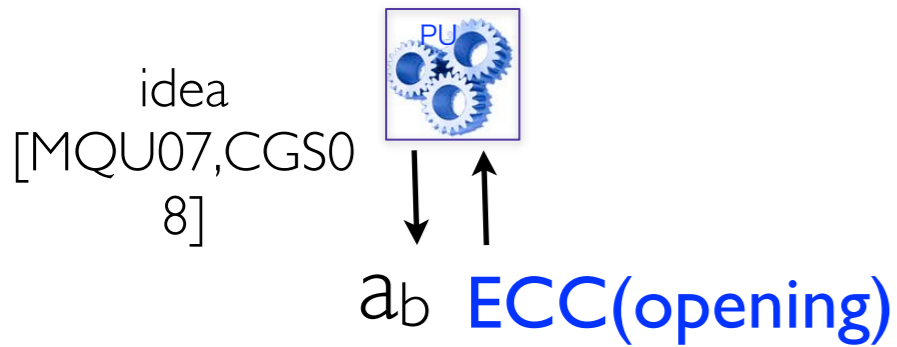


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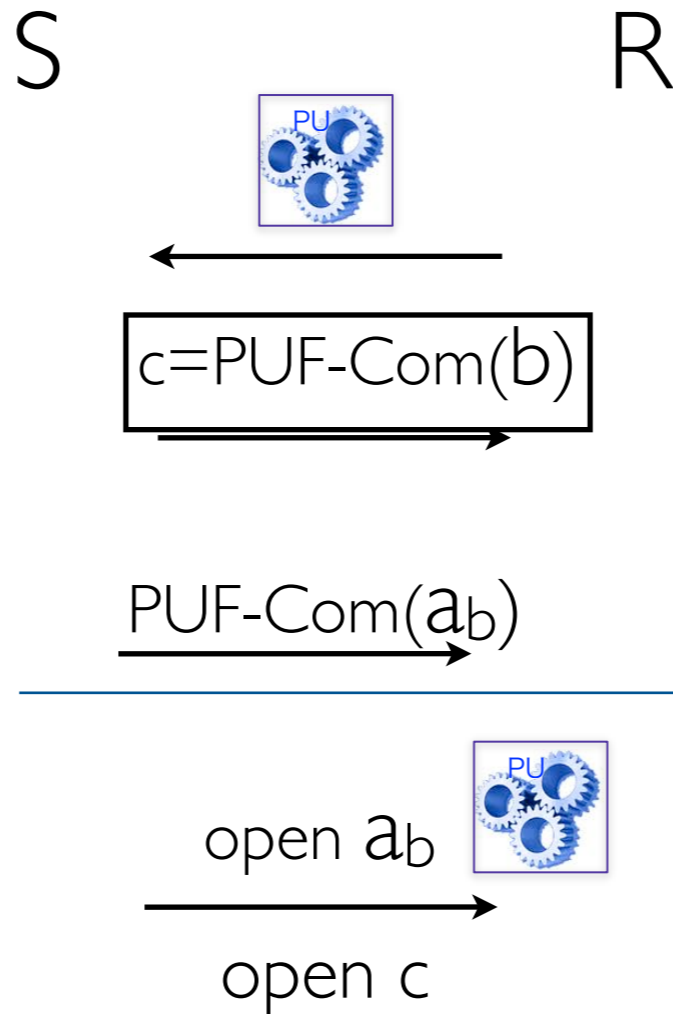
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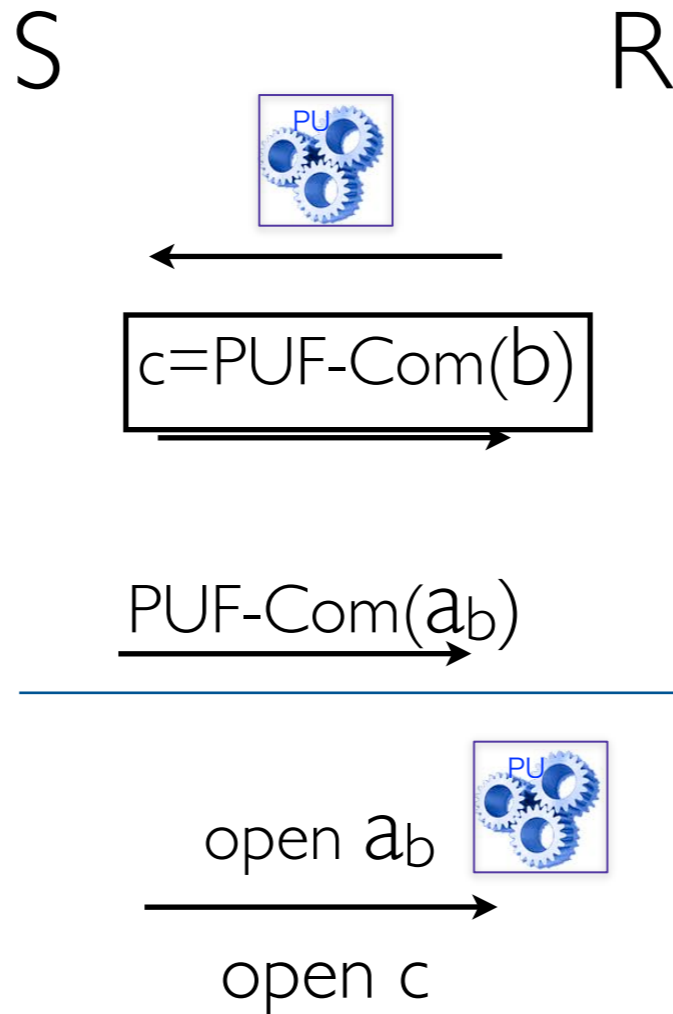
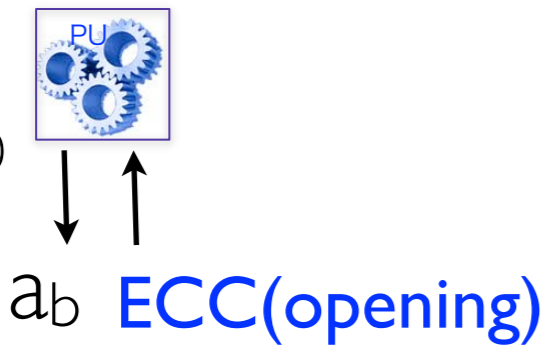
token

we construct: stand-alone unconditional commitment from malicious tokens

Extractable Commitment from (malicious) PUFs

Problem 1: Adv can query with 0/1

idea
[MQU07,CGS08]



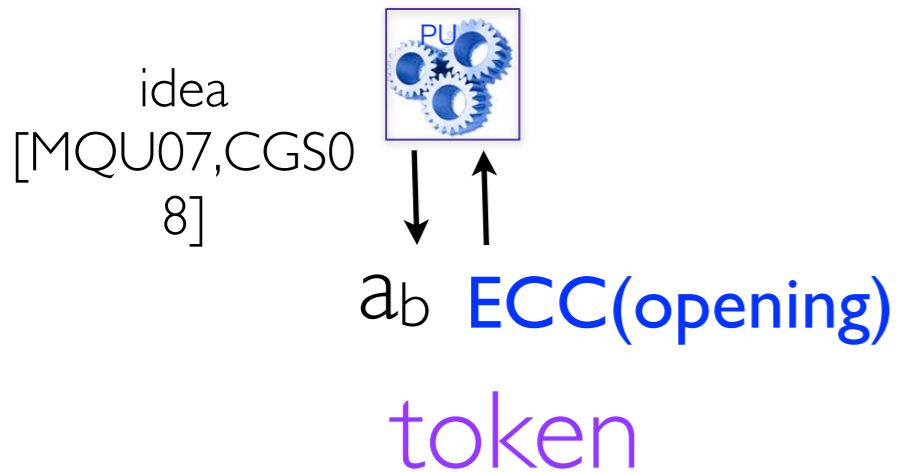
for free: stand-alone unconditional commitment from [OSVW13] PUF-Com

token

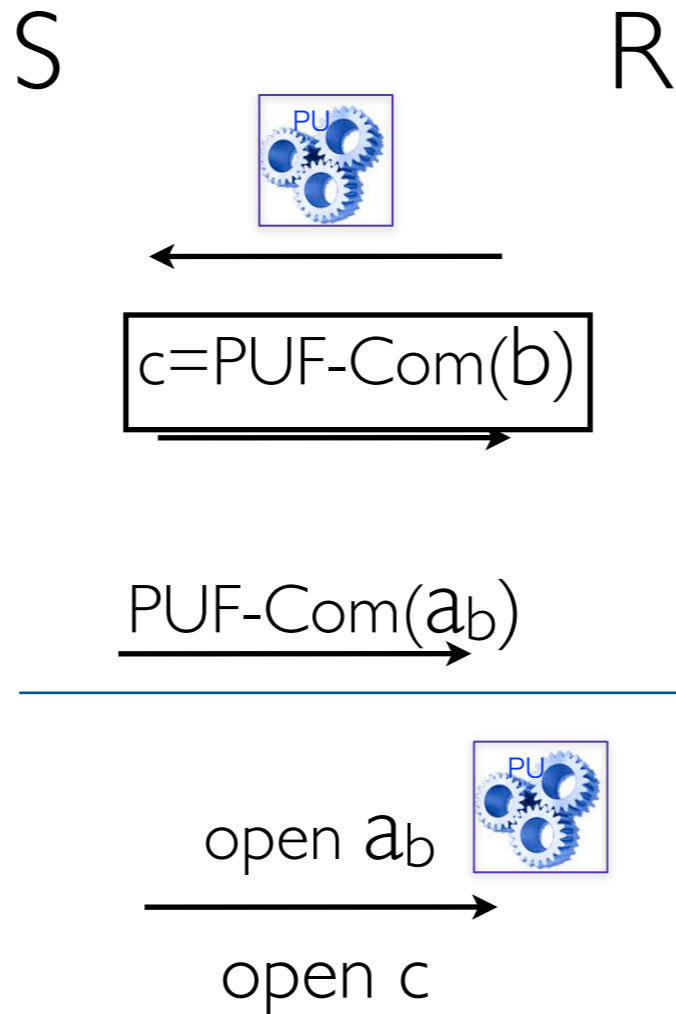
we construct: stand-alone unconditional commitment from malicious tokens

Extractable Commitment from (malicious) PUFs

Problem 1: Adv can query with 0/1



no unconditional unpredictability for free: prevent uncontrolled access to the (stateless) token



for free: stand-alone unconditional commitment from [OSVW13] PUF-Com

token

we construct: stand-alone unconditional commitment from malicious tokens

Conclusion

- black-box compiler **any** extractable commitments \Rightarrow UC-commitments
- Extractable commitments from Malicious PUFs \Rightarrow the first unconditional UC-security with PUFs
- Extractable commitments from Stateless token admitting arbitrary malicious adversary \Rightarrow the first unc. UC-secure protocol with stateless tokens. Complete the picture of unconditional UC security with stateless tokens.
- Unconditional OT with malicious PUFs??



Thanks

