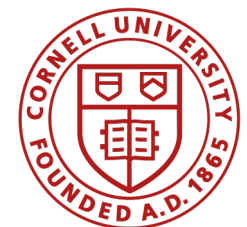


Order-Fairness for Byzantine Consensus

Mahimna Kelkar

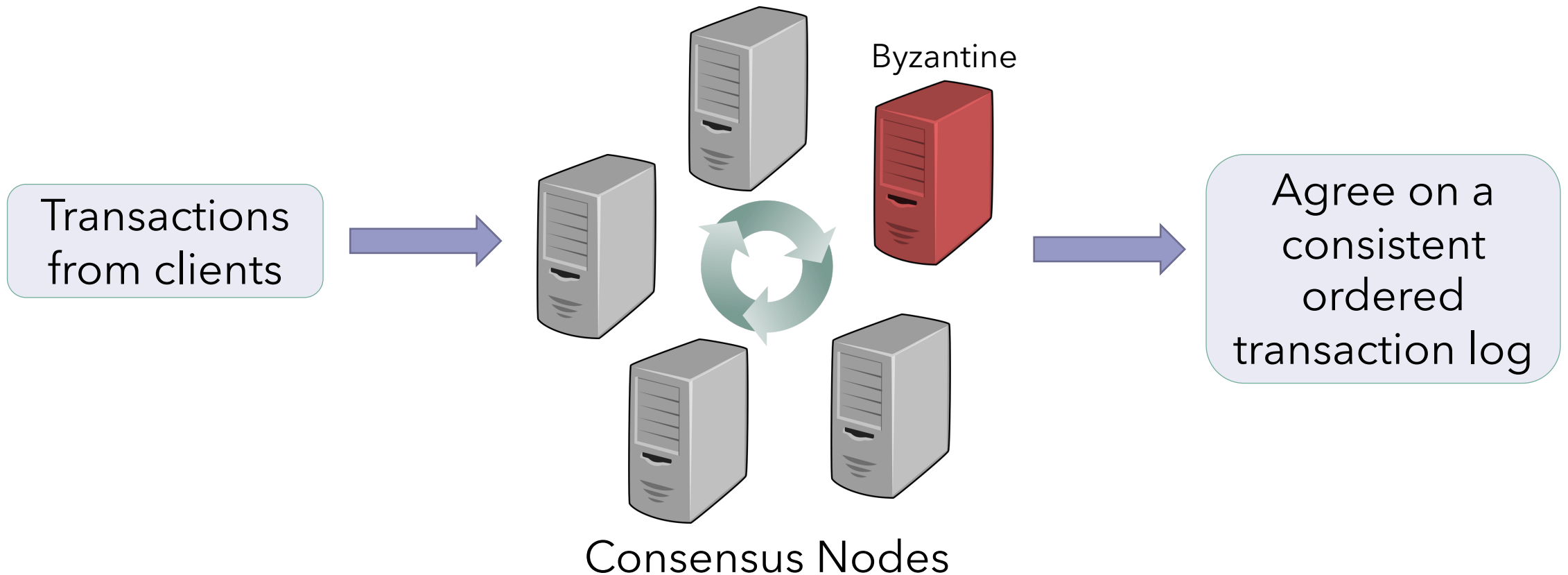
Cornell University and Cornell Tech

Joint work with
Fan Zhang,
Steven Goldfeder,
and Ari Juels



State Machine Replication (SMR)

also Byzantine consensus, linearly-ordered log



State Machine Replication (SMR)

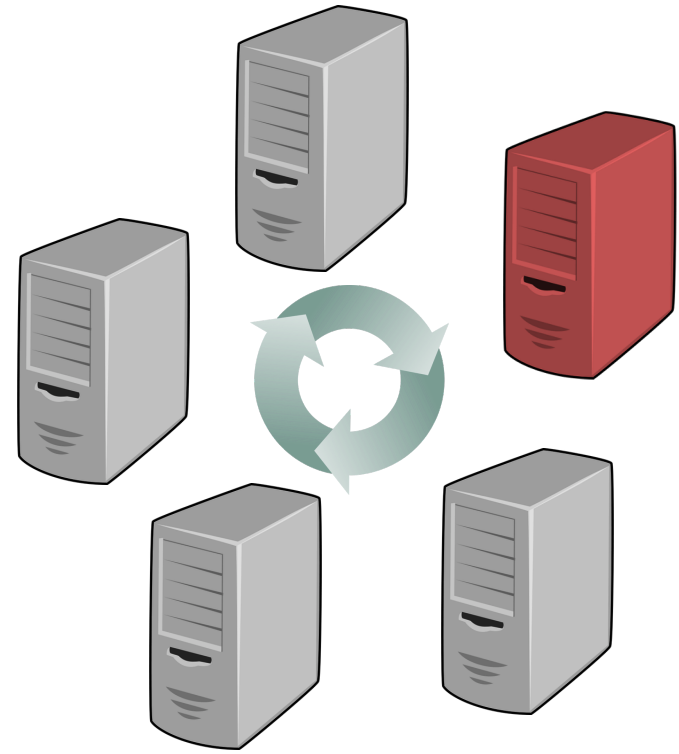
also Byzantine consensus, linearly-ordered log

Consistency or **Safety**

Honest nodes output the same log

Liveness

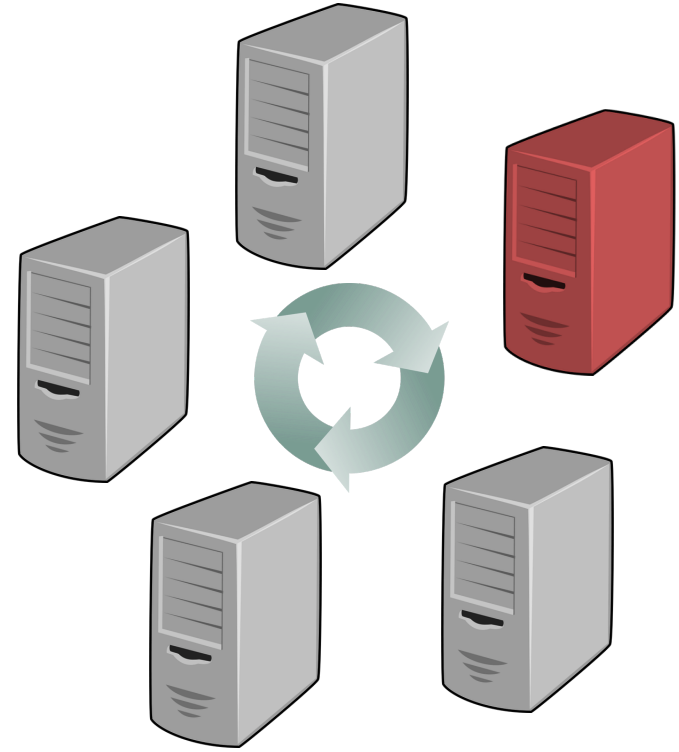
New TXs are incorporated soon



State Machine Replication (SMR)

also Byzantine consensus, linearly-ordered log

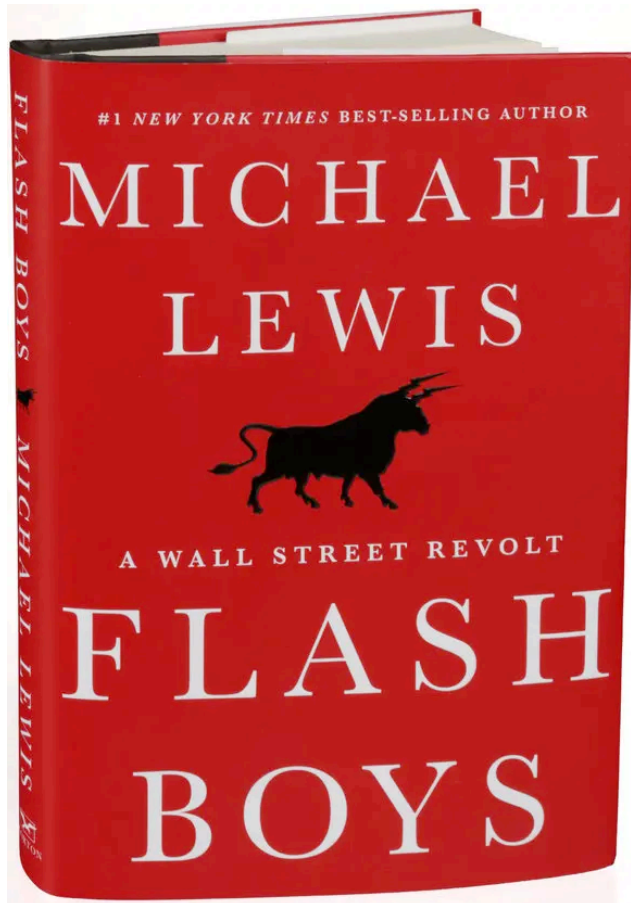
- **No restriction** on the **actual ordering**
- Often **easy to manipulate**



- Almost all classical consensus protocols are leader-based
 - E.g., PBFT, Paxos, Hotstuff etc.
- Leader node **can propose any ordering**
 - Adversarial leader can arbitrarily manipulate ordering
- No previous protocol guarantees fair ordering.

Why is ***fair ordering*** important?

Why is *fair ordering* important?



- 2014 exposé on *high-frequency trading* on wall street.
- HFT characteristics
 - Front-running
 - Arbitrage
- Investigation and fines after Lewis' book (FBI, SEC, etc.)

Why is *fair ordering* important?

- HFT back in a new form on decentralized exchanges
- Wild west without much regulation

Flash Boys 2.0: Frontrunning, Transaction Reordering, and Consensus Instability in Decentralized Exchanges

Philip Daian <i>Cornell Tech</i> phil@cs.cornell.edu	Steven Goldfeder <i>Cornell Tech</i> goldfeder@cornell.edu	Tyler Kell <i>Cornell Tech</i> sk3259@cornell.edu	Yunqi Li <i>UIUC</i> yunqil3@illinois.edu	Xueyuan Zhao <i>CMU</i> xyzhao@cmu.edu
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Iddo Bentov <i>Cornell Tech</i> ib327@cornell.edu	Lorenz Breidenbach <i>ETH Zürich</i> lorenz.breidenbach@inf.ethz.ch	Ari Juels <i>Cornell Tech</i> juels@cornell.edu
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Daian et al. (IEEE S&P 2020)

Why is *fair ordering* important?

Independent Theoretical Motivation

- Natural Analog of **Validity** condition in Byzantine Agreement (BA)
- Validity **forgotten** when BA generalized to SMR

If all honest nodes are
input value v ,
then all honest nodes will
agree on v .

Agreement Validity



If all honest nodes are
input m_1 before m_2 ,
then all honest nodes will
agree on m_1 before m_2 .

Order-Fairness

Comparison to current techniques

- Censorship Resistance [HoneybadgerBFT, Omniledger etc]
 - Reordering and insertion still possible
- Random leader election [Algorand, Ouroboros etc]
 - Adversarial leader can still order unfairly
- Threshold Encryption [HoneybadgerBFT]
 - Transactions ordered before content is revealed
 - Can still reorder transactions from colluding client first
 - Possible to blindly reorder

Order-Fairness is
strictly stronger than
previous notions

Defining Fair Ordering

Model

- Permissioned system with n nodes, f of which may be adversarial
- Clients **can** collude with protocol nodes

Model

- **External Network**

- Communication between clients and protocol nodes
- Clients send transactions to **all** nodes
- Adversary \mathcal{A} **not** in charge of message delivery

- **Internal Network**

- Communication amongst protocol nodes
- Adversary \mathcal{A} handles all message delivery

Model: Synchrony Definitions

Δ_{ext} -External Synchrony

If a transaction is input to some node in round r ,
then all honest nodes will receive it as input by round $r + \Delta_{ext}$.

Δ_{int} -Internal Synchrony

If a message is sent by an honest node in round r ,
then all recipient(s) will receive it by round $r + \Delta_{int}$.

So how do we define the **fair ordering**?

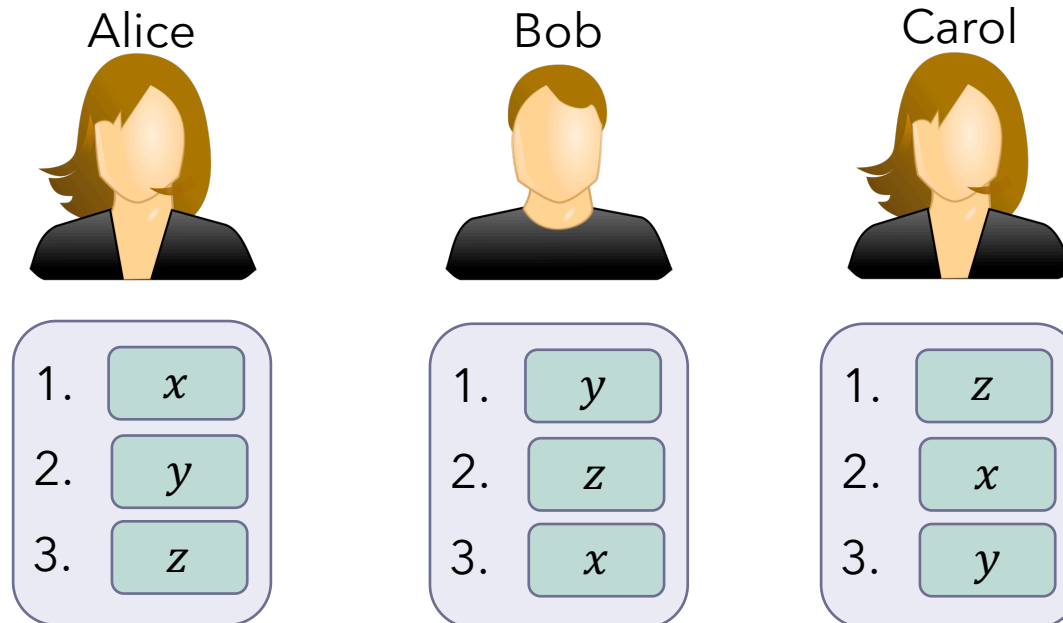
Definition (informal): γ -Receive-Order-Fairness

$$\frac{1}{2} < \gamma \leq 1$$

If γn nodes are input m_1 before m_2 ,
then all honest nodes will deliver m_1 before m_2 .

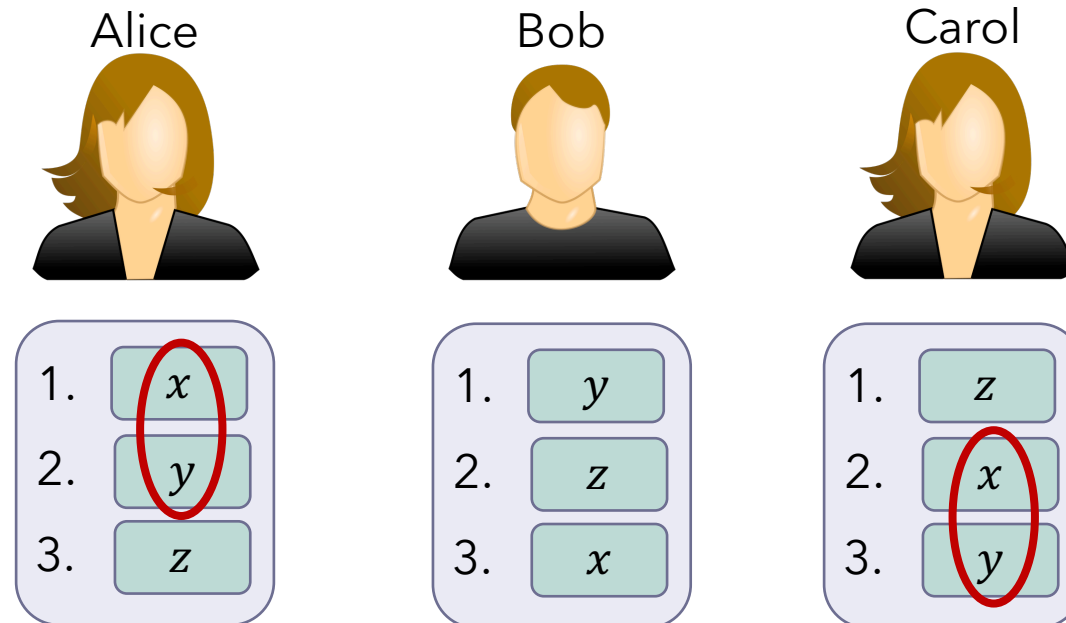
Condorcet Paradox

- Global ordering can be **non-transitive** even when individual orderings are transitive



Condorcet Paradox

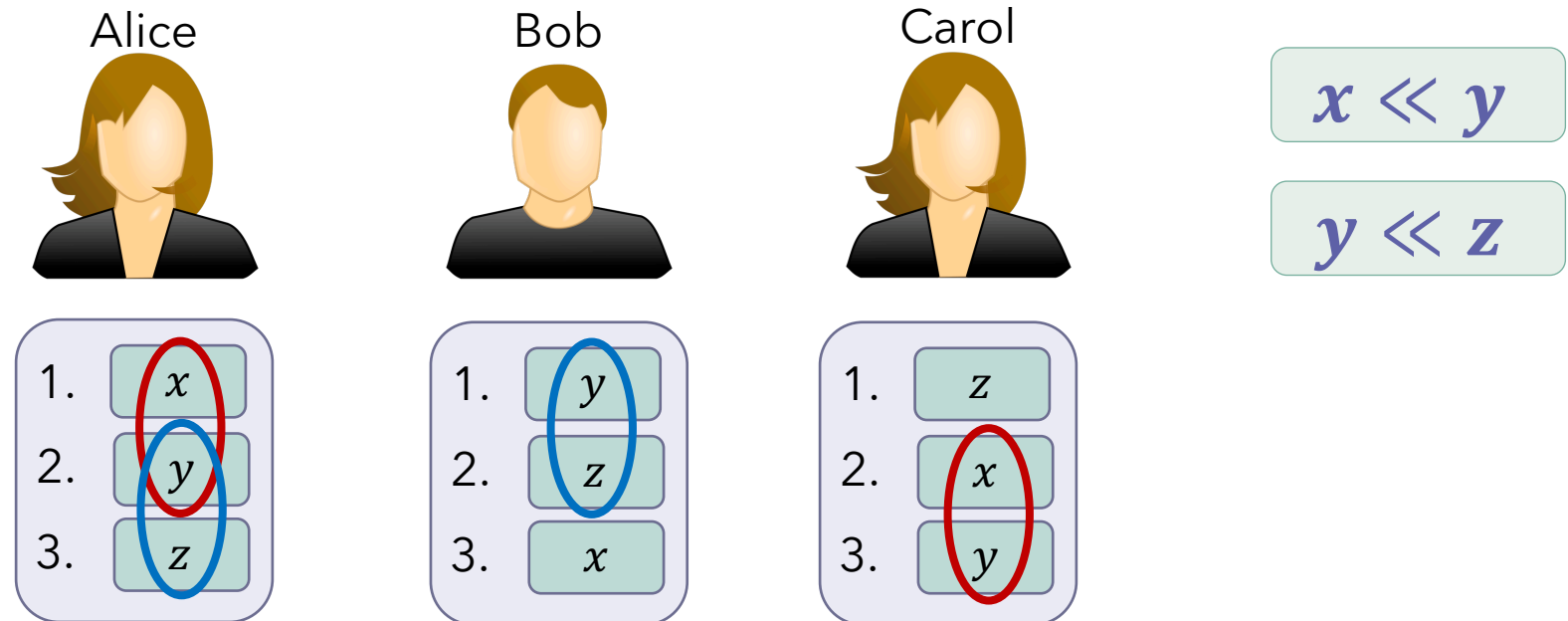
- Global ordering can be **non-transitive** even when individual orderings are transitive



$$x \ll y$$

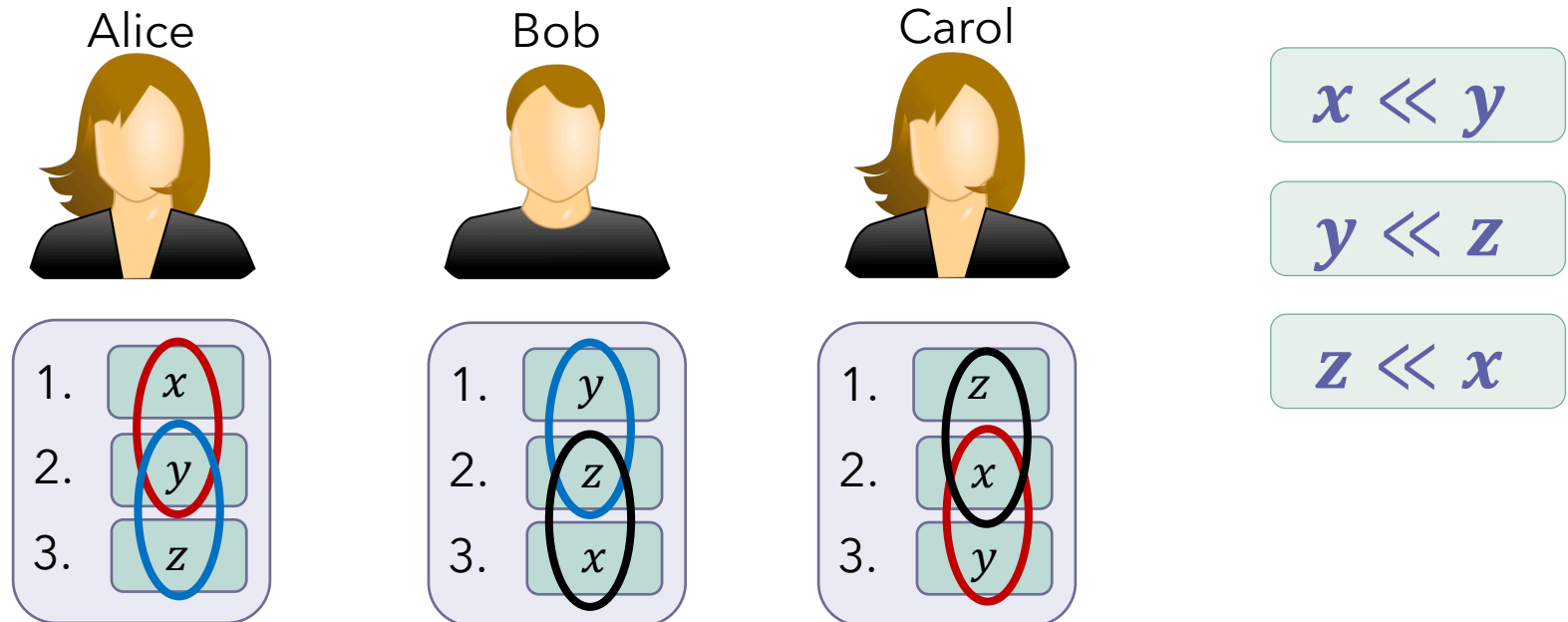
Condorcet Paradox

- Global ordering can be **non-transitive** even when individual orderings are transitive



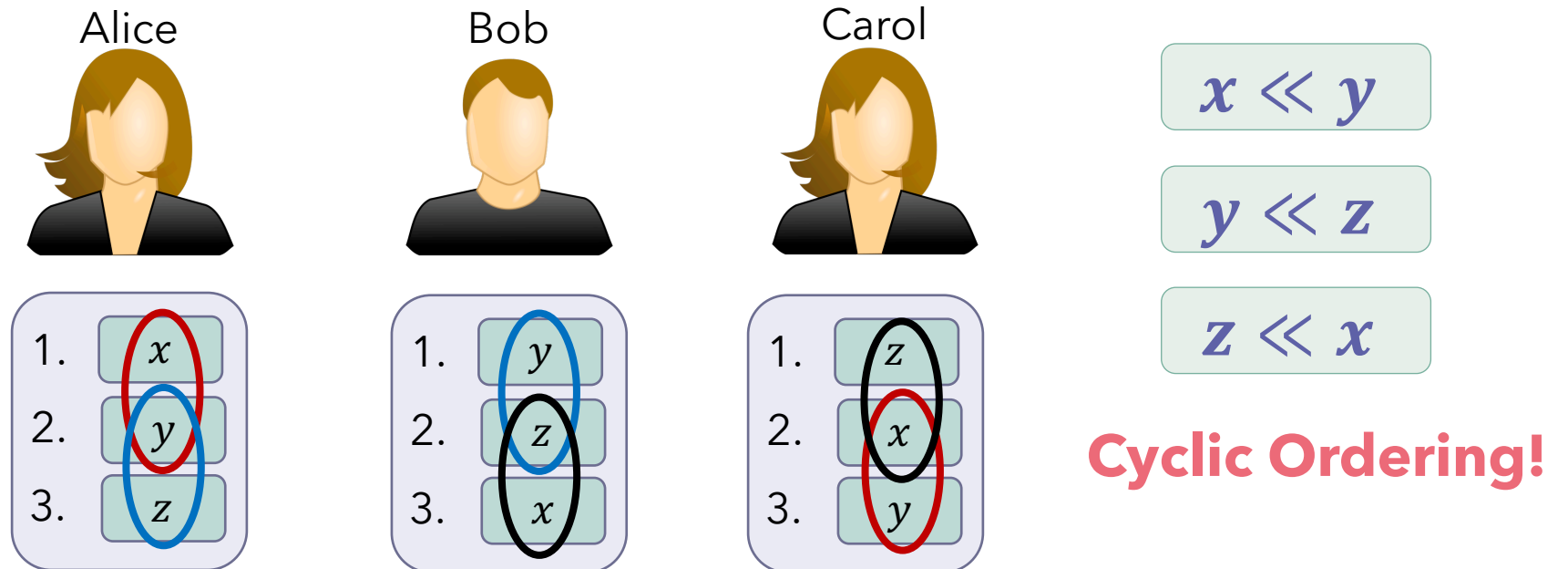
Condorcet Paradox

- Global ordering can be **non-transitive** even when individual orderings are transitive



Condorcet Paradox

- Global ordering can be **non-transitive** even when individual orderings are transitive



Theorem (informal): **Impossibility of Receive-Fairness**

For any $n, f \geq 1$ and γ , no protocol can achieve all of consistency, liveness and γ -receive-order-fairness when $\Delta_{ext} \geq n$.

Block-Order-Fairness

Definition (informal): γ -Block-Order-Fairness

If γn nodes are input m_1 before m_2 ,
then all honest nodes will deliver m_1 no later than m_2 .

Block-Order-Fairness

Definition (informal): γ -Block-Order-Fairness

If γn nodes are input m_1 before m_2 ,
then all honest nodes will deliver m_1 no later than m_2 .

- Key Idea: Deliver transactions with non-transitive ordering in the same block

Why can't we just order based on **median** timestamp?

- A single adversarial node can cause unfair ordering

		A	B	C	D	E
Round Number	1	tx ₁	tx ₁			
	2	tx ₂	tx ₂			tx ₁
	3					tx ₂
	4			tx ₁	tx ₁	
	5			tx ₂	tx ₂	

Why can't we just order based on **median** timestamp?

- A single adversarial node can cause unfair ordering

		A	B	C	D	E
Round Number	1	tx_1	tx_1			
	2	tx_2	tx_2			tx_1
	3					tx_2
	4			tx_1	tx_1	
	5			tx_2	tx_2	

$$\begin{aligned} 2 &= \text{med}(tx_1) \\ &\leq \\ \text{med}(tx_2) &= 3 \end{aligned}$$

Why can't we just order based on **median** timestamp?

- A single adversarial node can cause unfair ordering

Round Number	A	B	C	D	E
	1	tx_1	tx_1		
	2	tx_2	tx_2		tx_2
	3				tx_1
	4		tx_1	tx_1	
	5		tx_2	tx_2	

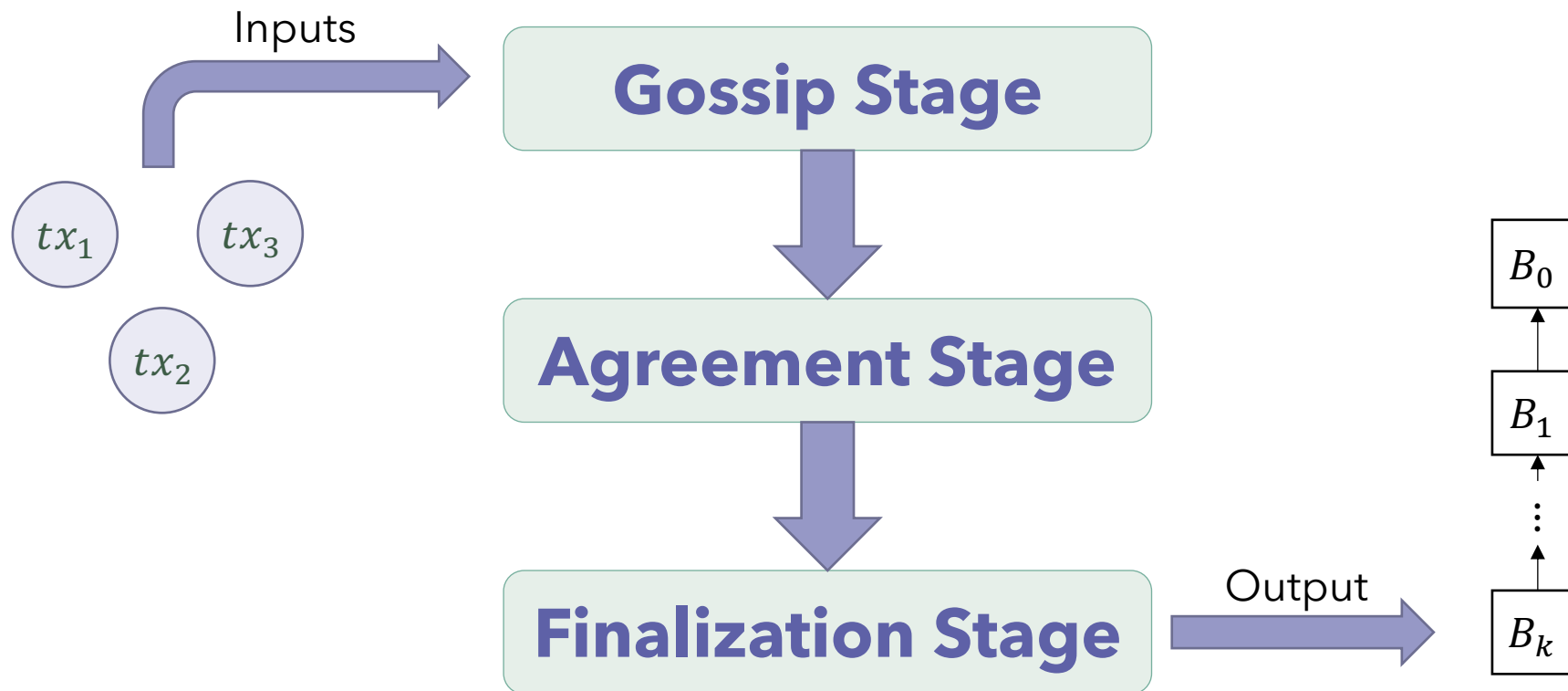
$$3 = med(tx_1)$$

\neq

$$med(tx_2) = 2$$

Fair Ordering Protocols

Aequitas: A Fair-Ordering Protocol



The Gossip Stage

- (1) Honest nodes broadcast transactions they to all nodes as they are received
- (2) Honest nodes store broadcasts received from other nodes in *local logs* $locallog_i^j$ contains i 's view of broadcasts by j

Guarantees that honest nodes have **consistent** local logs

The Gossip Stage

- **FiFo (First-In-First-Out) Broadcast**

- Messages broadcast by an honest sender are delivered in the **same order** as they were broadcast
- Messages broadcast by an adversarial sender are delivered in a consistent order by all honest nodes
- Can be realized from standard reliable broadcast [HDvR 07]

Agreement Stage

- Agree on which local logs to use to order a transaction
- Can be done using standard Byzantine agreement

Guarantees that honest nodes use the same local logs to *finalize* a transaction

Finalization Stage

- The finalization stage orders the transaction in the final output log
- Leaderless
 - No extra communication

Finalization Stage

Ordering two transactions

- If many (e.g., $\gamma n - f$) local logs contain tx' before tx , then tx is said to **wait** for tx'
- Relations between transactions are viewed in a **dependency** or **waiting graph**.
 - Vertices represent transactions
 - Edge (a,b) represents b waiting for a

Leaderless Finalization

What if there is no clear winner in the two transactions?

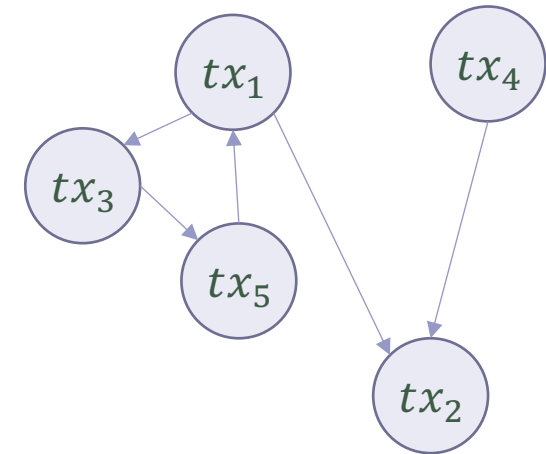
Two problems to solve

1. Graph may not be complete or even connected.
 - Some transactions may not be comparable
2. Graph may not be acyclic.

Leaderless Finalization

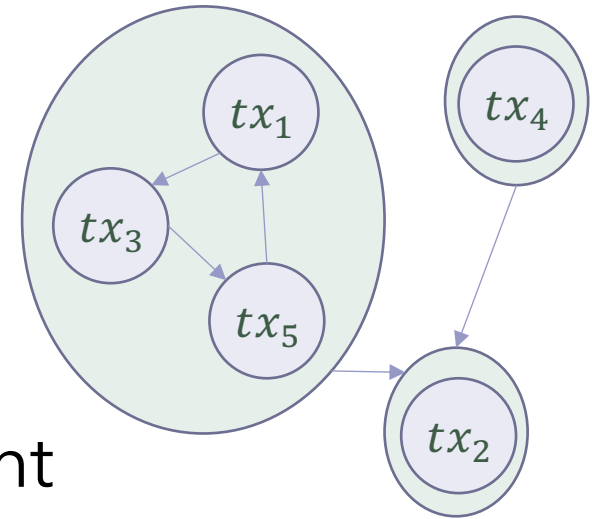
Key Idea

- Wait for common descendant for transactions without an edge in the graph
- Order using maximum number of dependents



Leaderless Finalization

- Graph can still have cycles
- To get a total ordering, compute the **condensation** graph by collapsing the strongly-connected components
- Deliver transactions in the same component into the **same block**.



- Synchronous protocol requires $n > \frac{2f}{2\gamma-1}$
 - i.e., $n > 2f$ even when $\gamma = 1$
- Asynchronous protocol requires $n > \frac{4f}{2\gamma-1}$

Some Caveats

- Only Achieves **Weak-Liveness**
 - New transactions must be input *sufficiently late* in order to deliver current transactions
 - Conventional Liveness achieved when external network has *small synchrony bound*

Some Caveats

- Adversary can unfairly order if it controls the **entire** Internet, i.e. if it can also control a client's connection to the consensus protocol nodes
- In our modeling, this is handled by assuming adversary **does not** control the external network

A general order-fairness compiler

- FiFo-broadcast and Byzantine Agreement are weak primitives
 - They can be realized from any consensus protocol
- General compiler that takes **any** consensus protocol and transforms it into one that also provides order-fairness

Final Thoughts

- Our work is the first to formalize order-fairness and provide protocols that realize it
- Order-Fairness is important for many blockchain applications
 - Decentralized exchanges (2.4 billion USD market)
 - ICO token sales (12 billion USD market)
 - Decentralized Finance in general



Thank you

mahimna @ cs.cornell.edu

ia.cr/2020/269