

Sublinear-Round Byzantine Agreement under Corrupt Majority

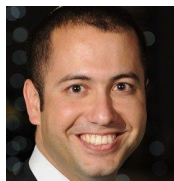
Elaine Shi @ Cornell

Joint with T-H. Hubert Chan (HKU) & Rafael Pass (Cornell)

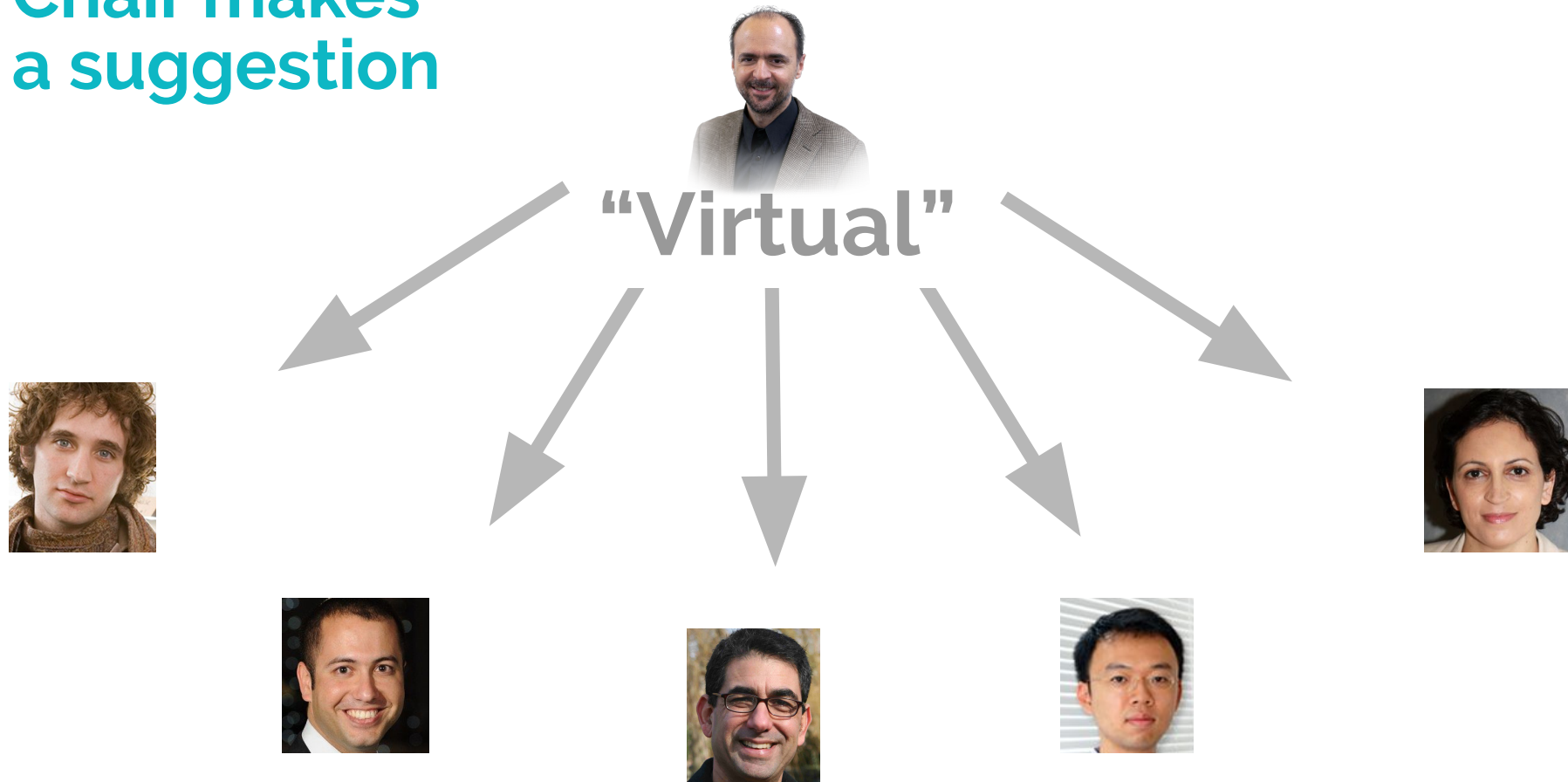


PKC'2021

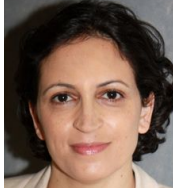
Virtual or Physical?



Chair makes a suggestion



Everyone discusses



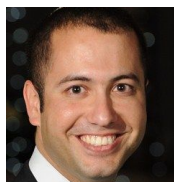
Everyone decides



Virtual



Virtual



Virtual



Virtual



Virtual

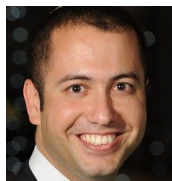


Virtual



Some are unhappy

(e.g., had papers rejected from pkc)





Consistency
happy players agree on decision

Validity
if chair happy, agree on chair's suggestion



Byzantine Broadcast

[Lamport'82]

Consistency

happy players agree on decision

Validity

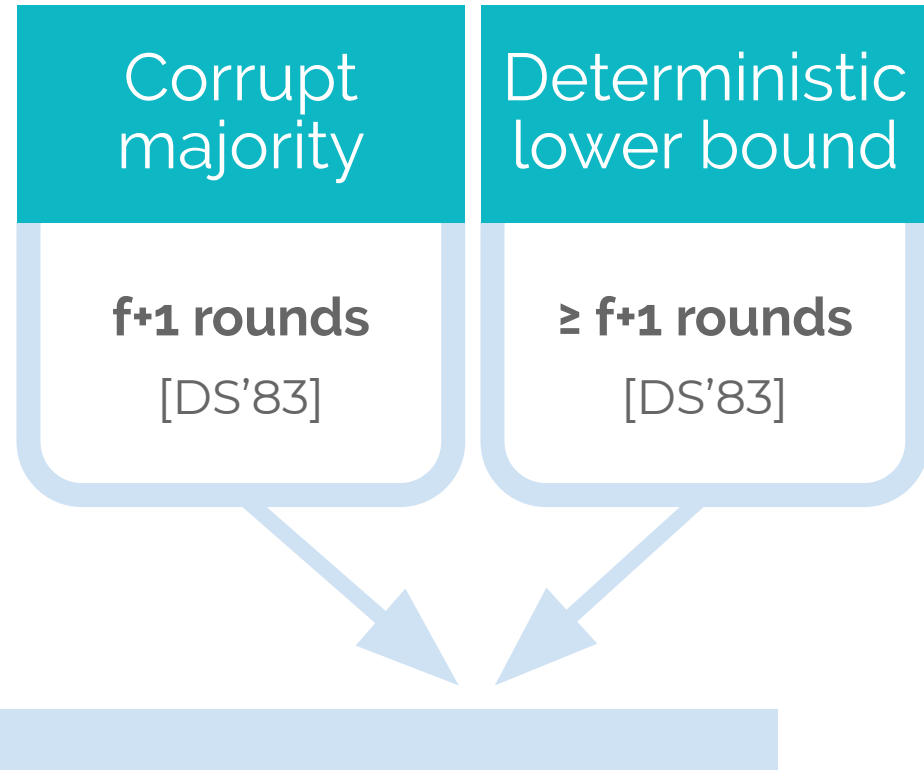
if chair happy, agree on chair's suggestion

Byzantine Broadcast

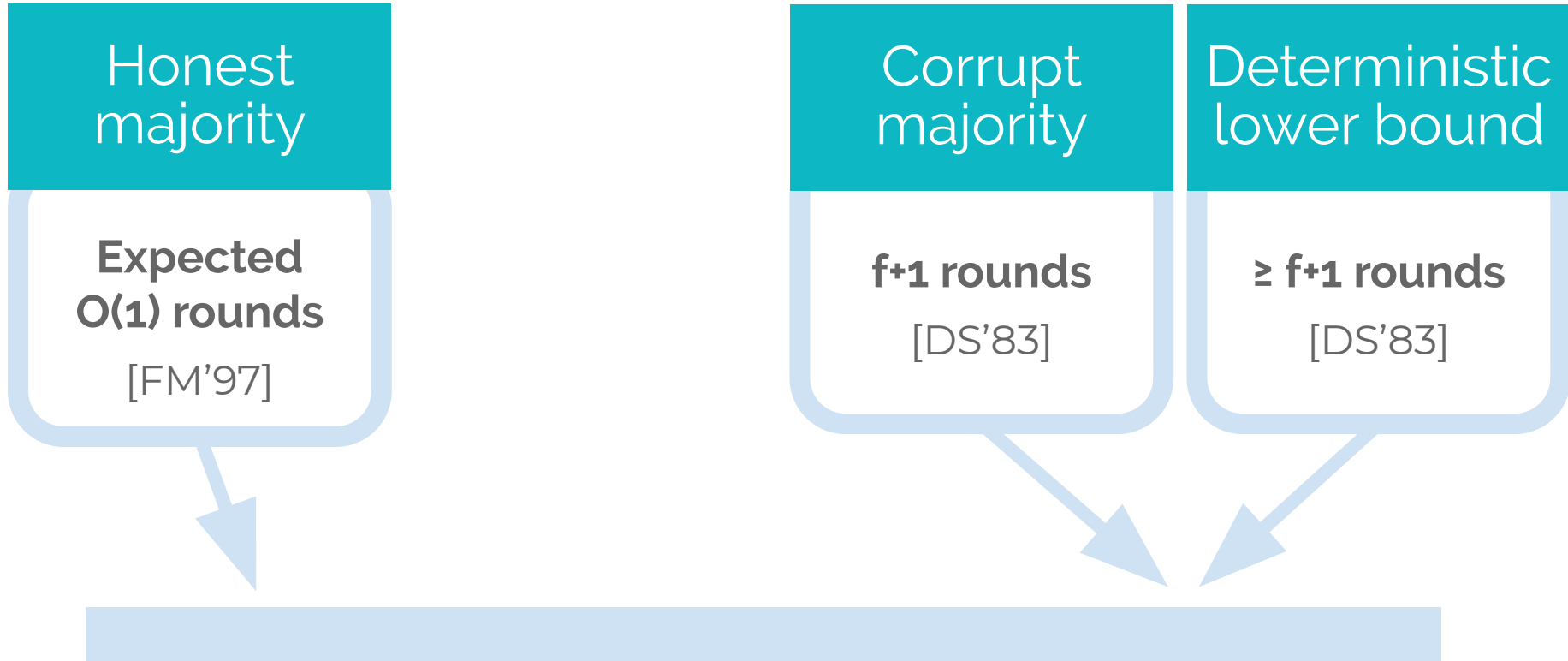
f : number of corrupt players



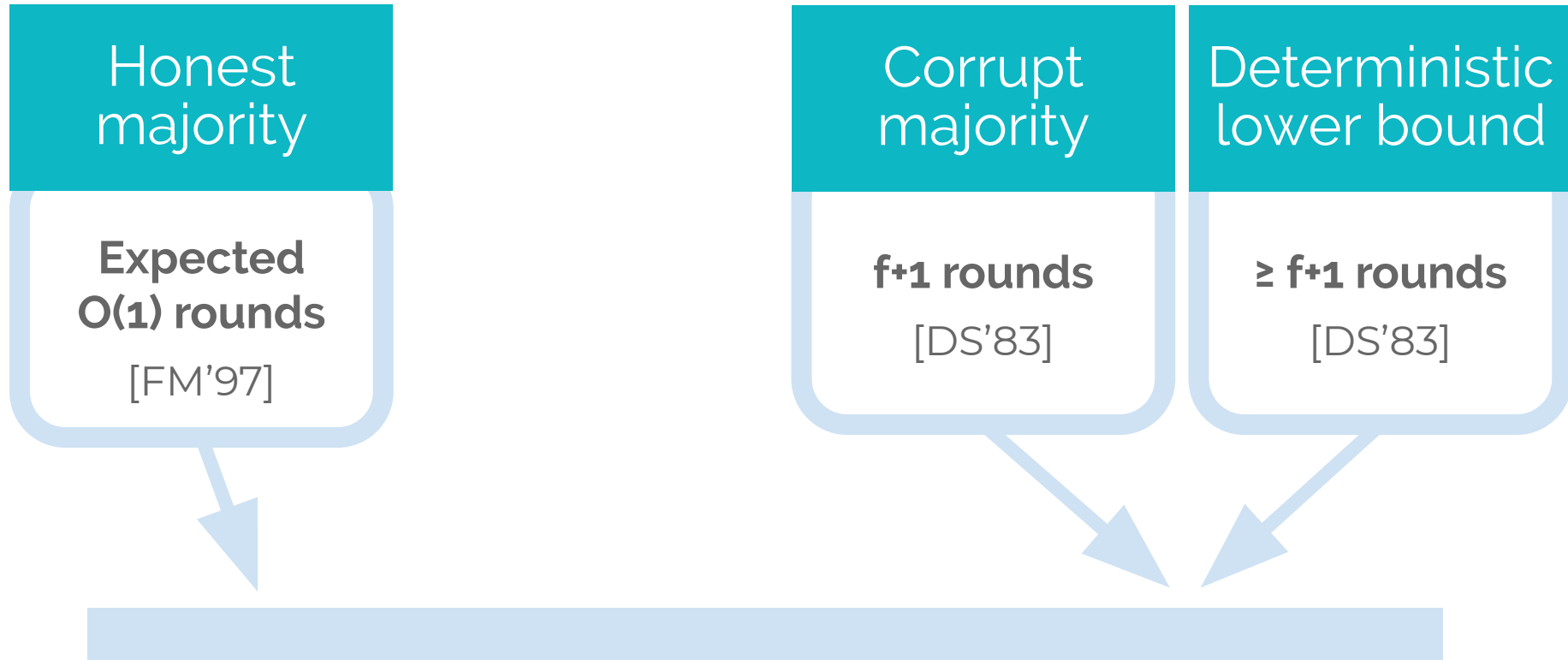
Byzantine Broadcast



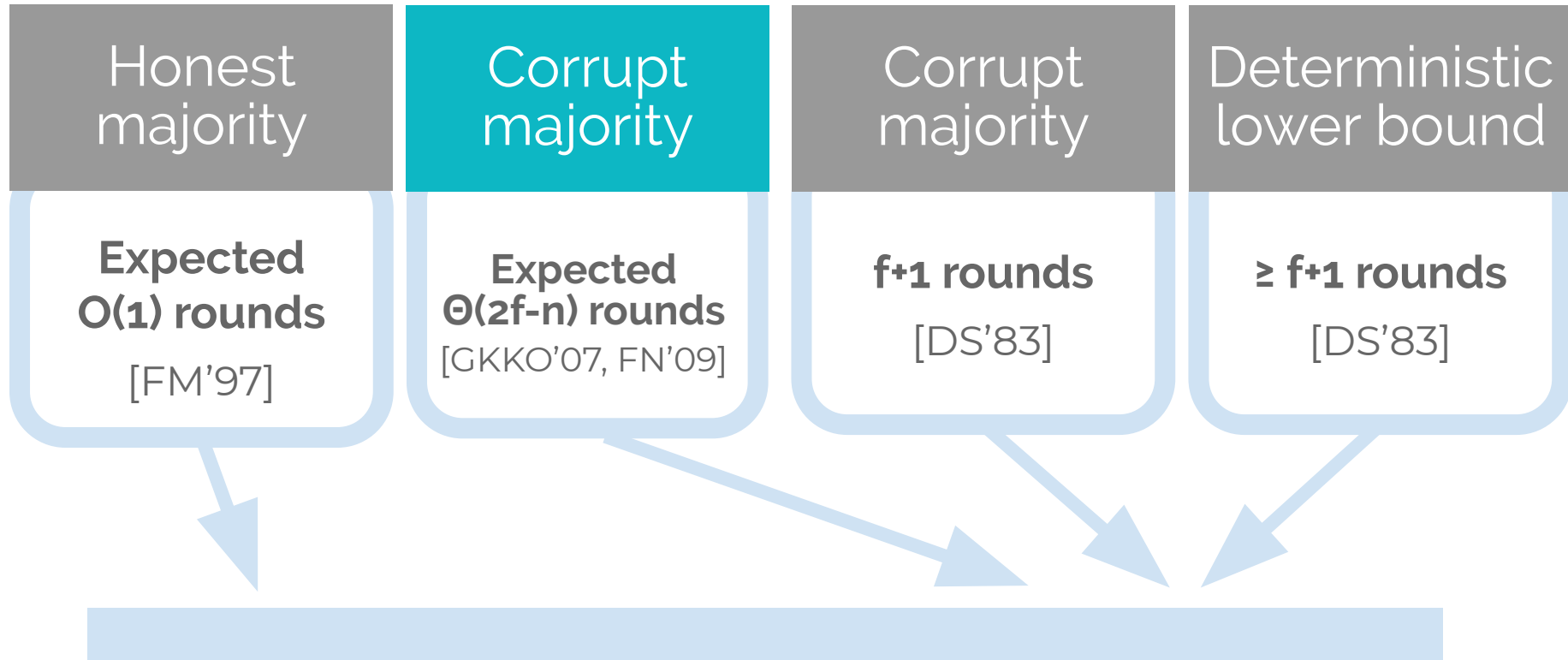
Byzantine Broadcast



Can we achieve **sublinear rounds** under **corrupt majority** (with randomization) ?



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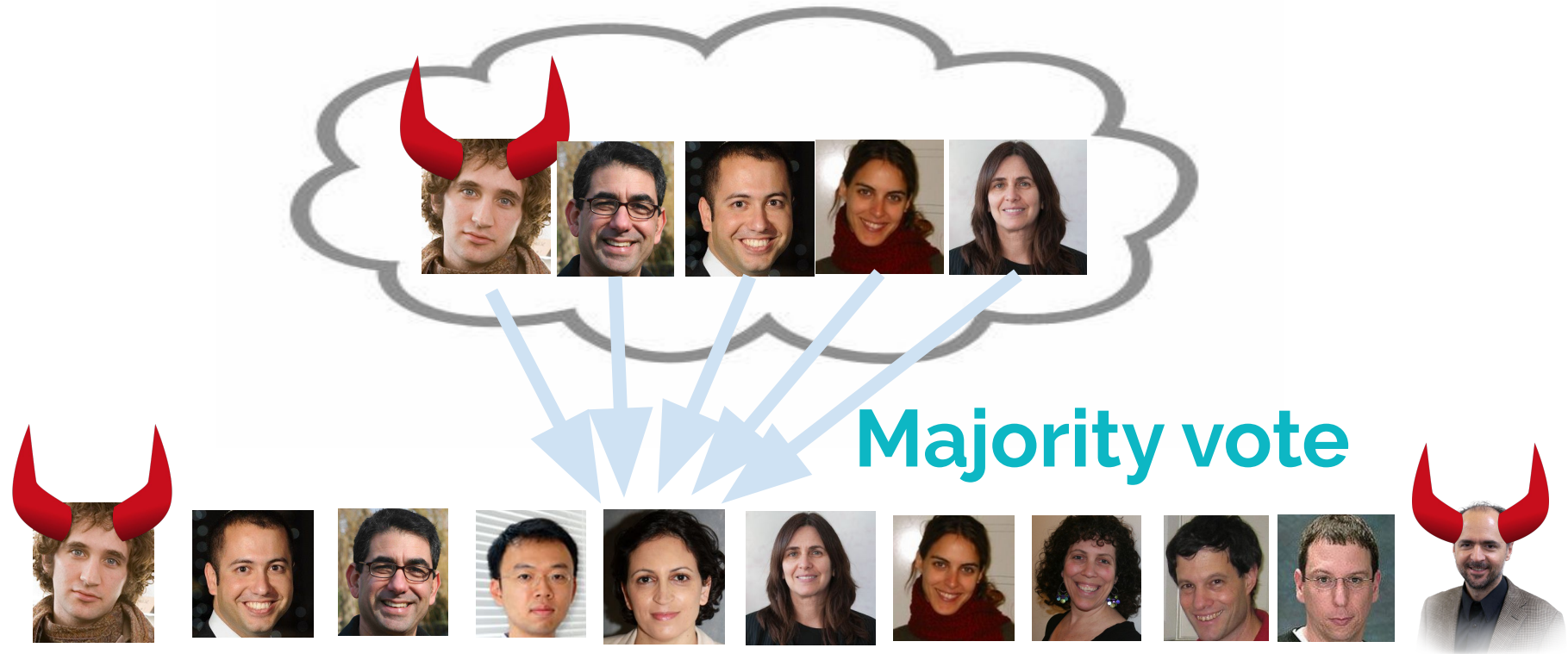
Can we achieve sublinear rounds under corrupt majority (with randomization) ?

📍 **Hard even for **static** corruption**

📍 **Folklore committee election fails**



Folklore committee election



Folklore committee election



Corrupt majority: majority voting fails

Can we achieve sublinear rounds under corrupt majority (with randomization) ?

📍 **Hard even for **static** corruption**

📍 **Nothing known for **51%** corrupt**

Our Result

Assume trusted setup and standard hardness assumptions, there exists **poly-log round BB** even in the presence of 99.9% **weakly adaptive corruptions**.

See paper for a more generalized statement.



Challenge 1

**Convey decision
to those outside
the committee**

**Adaptive
corruption of
the committee**

Challenge 2

- 1 Dolev-Strong among the committee
- 2 Non-committee-members participate as non-voters

b  r : bit b with r sigs from distinct s including
committee size: $C = \text{polylog}(\lambda)$



b_{pin} : bit b with r sigs from distinct s including
committee size: $C = \text{polylog}(\lambda)$



Round 0:



multicasts $b_{\text{pin}} 1$

$b \text{ } \text{👤}$ r : bit b with r sigs from distinct 👤 s including
committee size: $C = \text{polylog}(\lambda)$



Round 0:  multicasts $b \text{ } \text{👤}$ 1

Round $r = 1.. C$:

Committee:

if committee member j sees $b \text{ } \text{👤}$ r
if b not in E_j : add b to E_j , multicasts $b \text{ } \text{👤}$ $(r + 1)$

$b \text{ } \text{📌} \text{ } r$: bit b with r sigs from distinct 👤 s including
committee size: $C = \text{polylog}(\lambda)$



Round 0:



multicasts $b \text{ } \text{📌} \text{ } 1$

Round $r = 1.. C$:

add its own sig

Committee:

if committee member j sees $b \text{ } \text{📌} \text{ } r$

if b not in E_j : add b to E_j , multicasts $b \text{ } \text{📌} \text{ } (r + 1)$

$b \text{ } \text{Ⓜ} \text{ } r$: bit b with r sigs from distinct Ⓜ s including
committee size: $C = \text{polylog}(\lambda)$



Round 0:  multicasts $b \text{ } \text{Ⓜ} \text{ } 1$

Round $r = 1.. C$:

Committee:

if committee member j sees $b \text{ } \text{Ⓜ} \text{ } r$
if b not in E_j : add b to E_j , multicasts $b \text{ } \text{Ⓜ} \text{ } (r + 1)$

Finally: player j outputs elem in E_j if its size is 1, else output 0

Lemma 1: if in round $r < C$, honest player j has b in its E_j ,
then in round $r+1$, every honest player i has b in E_i

Lemma 2: if in round C , honest player j has b in its E_j ,
then in round C , every honest player i has b in E_i



$b \text{ } \text{Ⓜ} \text{ } r$: bit b with r sigs from distinct Ⓜ s including
committee size: $C = \text{polylog}(\lambda)$



Phase 0:  multicasts $b \text{ } \text{Ⓜ} \text{ } 1$

Phase $r = 1.. C$:

Relay round (everyone):

if player i sees $b \text{ } \text{Ⓜ} \text{ } r$

if b not in E_i : add b to E_i , multicast $b \text{ } \text{Ⓜ} \text{ } r$



Voting round (committee):

if committee member j sees $b \text{ } \text{Ⓜ} \text{ } r$

if b not in E_j : add b to E_j , multicasts $b \text{ } \text{Ⓜ} \text{ } (r + 1)$

Finally: player j outputs elem in E_j if its size is 1, else output 0

Challenge 1

**Convey decision
to those outside
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**Adaptive
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the committee**

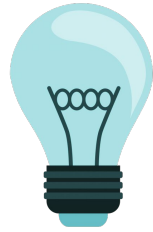
Challenge 2



- Secret committee election
- Reveal membership on voting

Adaptive corruption of the committee

Challenge 2



Player j is member of the b-committee iff

Player j itself:

$$\begin{aligned} \rho, \Pi &= \text{VRF}(sk_j, b) \\ &\& \rho < D \end{aligned}$$



Player j is member of the b -committee iff

Player j itself: $\rho, \Pi = \text{VRF}(\text{sk}_j, b)$
& $\rho < D$

Everyone else: $\text{VRF.Vf}(\text{pk}_j, b, \rho, \Pi) = 1$
& $\rho < D$




Membership in the two committees
decided **independently**

Player j itself:

$$\rho, \Pi = \text{VRF}(sk_j, b) \\ \& \rho < D$$

Everyone else:


$$\text{VRF.Vf}(pk_j, b, \rho, \Pi) = 1 \\ \& \rho < D$$

b  r : bit b w/ r votes from distinct s including 
committee size: $C = \text{polylog}(\lambda)$



Phase 0:  multicasts b  1

Phase $r = 1.. \text{polylog}(\lambda)$:

Relay round:

if player i sees b  r
if b not in E_i : add b to E_i , multicast b  r

Voting round:

if player j sees b  r and is member of b -committee:
if b not in E_j : add b to E_j , multicasts b  $(r + 1)$

Finally: player j outputs elem in E_j if its size is 1, else output 0

Open Questions and Ongoing Work

- Can we achieve **expected constant rounds** with corrupt majority?

<https://eprint.iacr.org/2020/590>

- Can we achieve a similar result in the **strongly adaptive** model?

Thank you! runting@gmail.com