

Categorization of Faulty Nonce Misuse Resistant Message Authentication

Yu Long Chen¹

Bart Mennink²

Bart Preneel¹

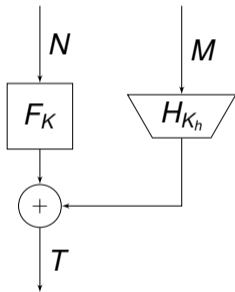
imec-COSIC, KU Leuven

Digital Security Group, Radboud University

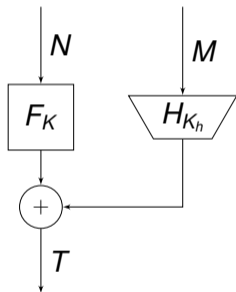
December, 2021

Nonce-Based MAC Algorithms and Wegman-Carter

Wegman and Carter (1981)



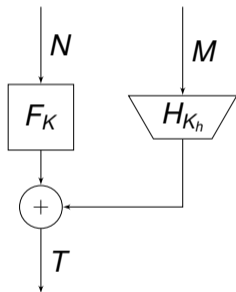
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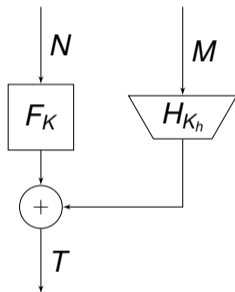
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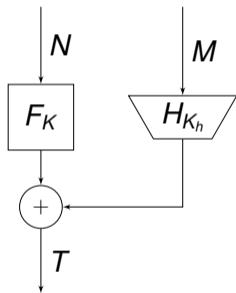
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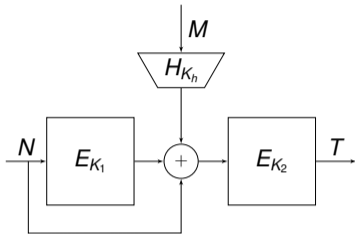
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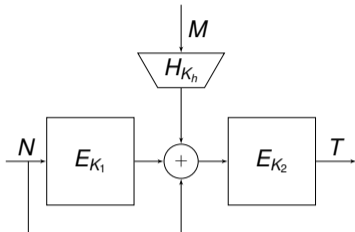
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- Broken by nonce repetition

Encrypted Wegman-Carter with Davies-Meyer



Cogliati and Seurin (2016)

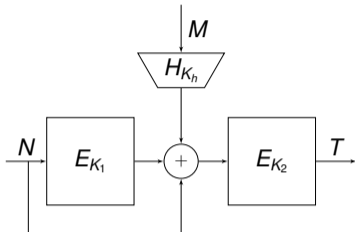
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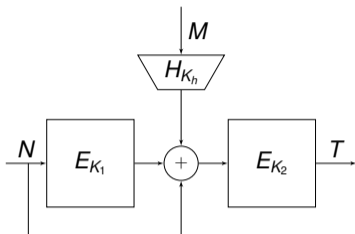
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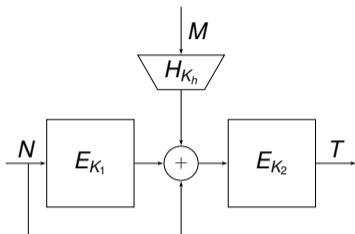
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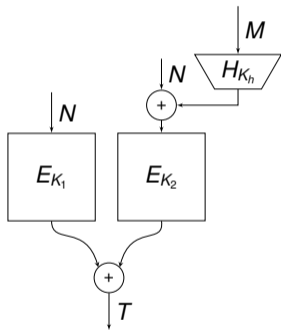


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- Datta et al. (2018): DWCDM using one block cipher call with its inverse

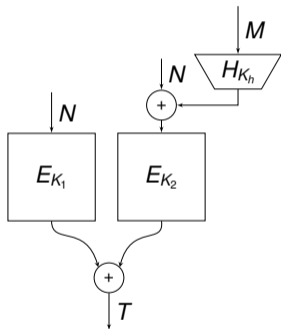
Nonce-Based Enhanced Hash-then-Mask

Dutta et al. (2019)



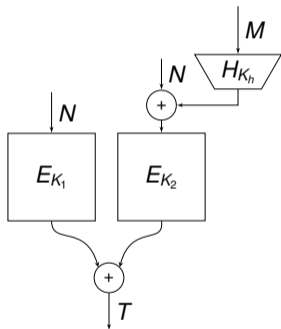
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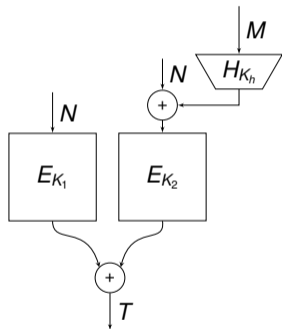
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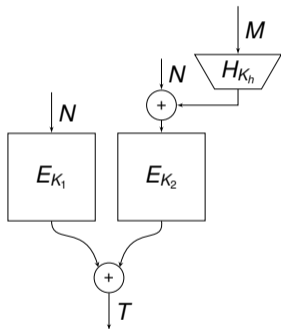
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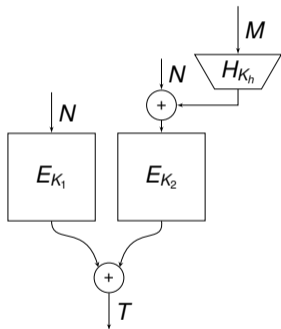
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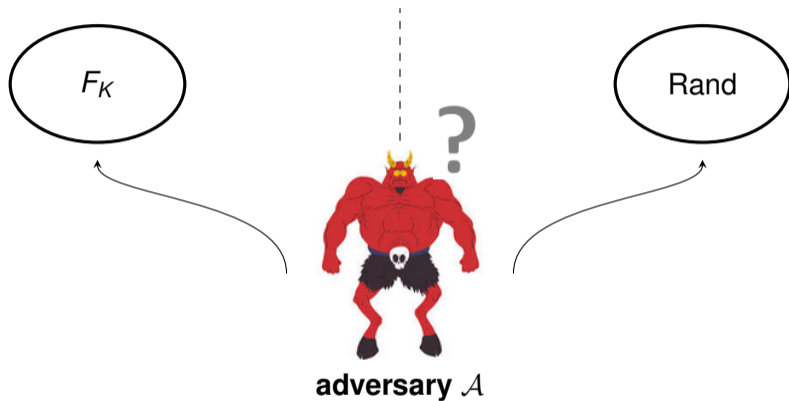
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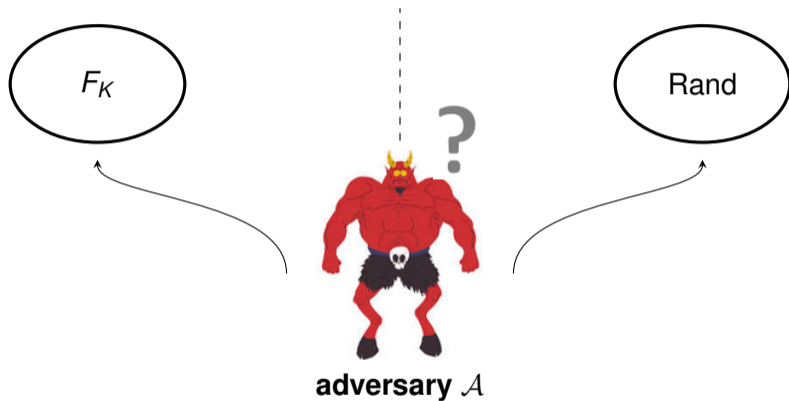
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- Choi et al. (2020): $3n/4$ -bit security if number of faulty queries $\leq 2^{3n/8}$

Security Definition



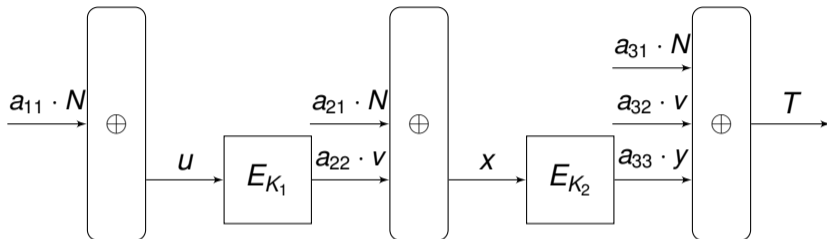
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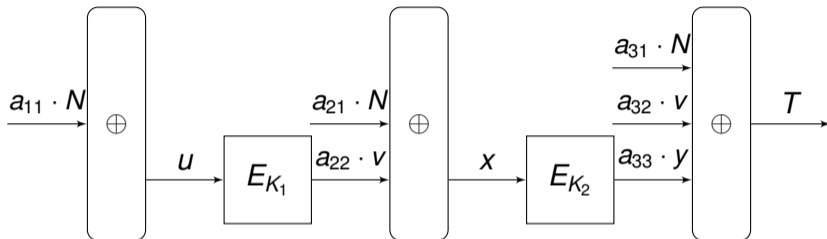
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- Good **PRF** $\iff \mathcal{A}$ cannot determine which world it is interacting with

Generalized Fixed-Input-Length PRF Construction



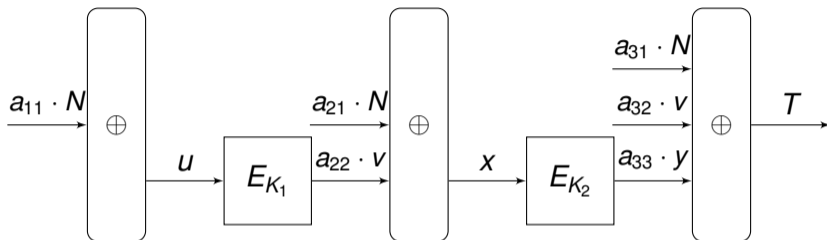
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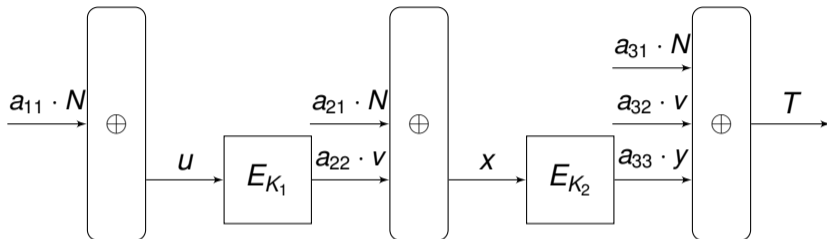
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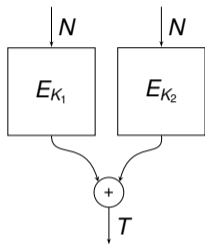
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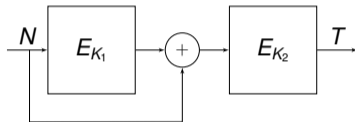


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- We are only interested in beyond birthday bound secure PRFs

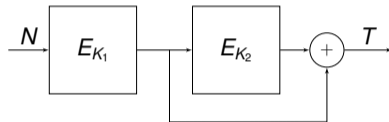
SoP, EDM, and EDMD



Sum of Permutations
(Bellare et al. 1998)

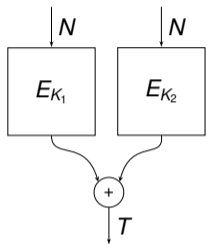


Encrypted Davies-Meyer
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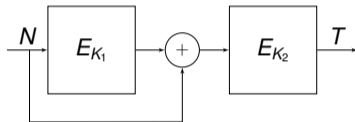


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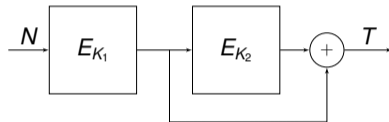
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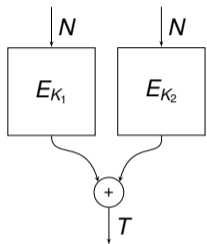
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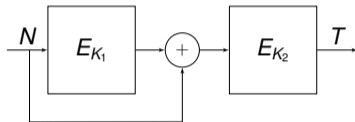
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n -bit security

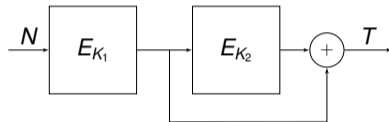
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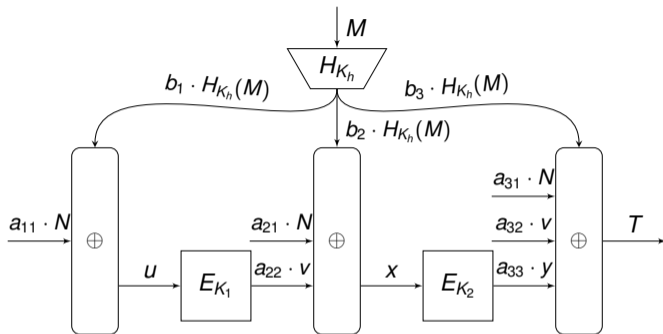


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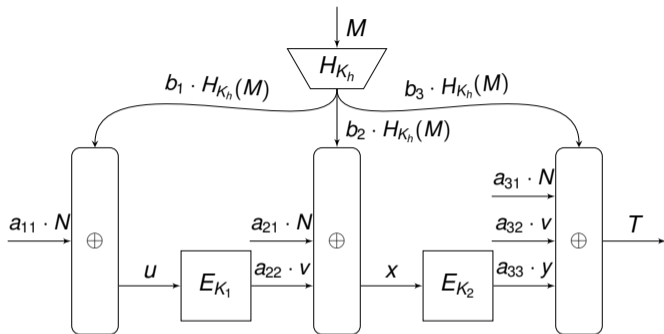
+ natural siblings of these 3 PRFs consist of XORing the input to the output

Generalized Nonce-Based MAC Algorithms



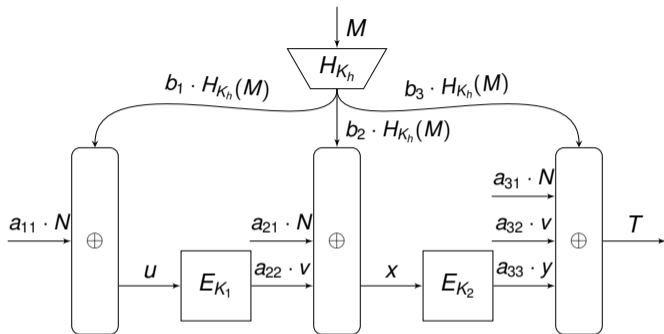
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Generalized Nonce-Based MAC Algorithms



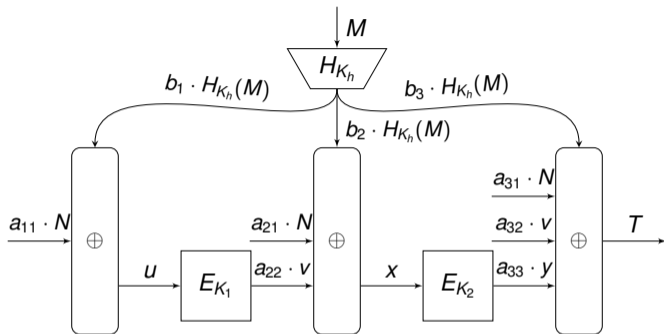
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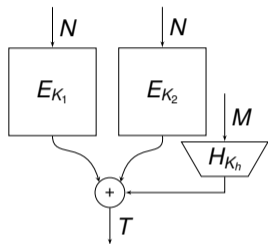
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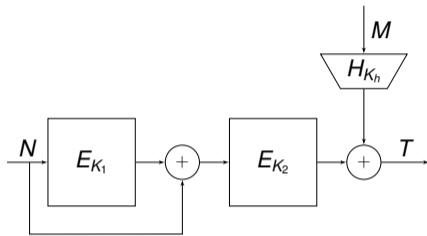


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- In total 10 interesting constructions
(5 based on EDM, 3 based on SoP, and 2 based on EDMD)

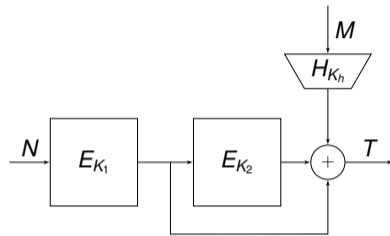
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SoP Wegman-Carter

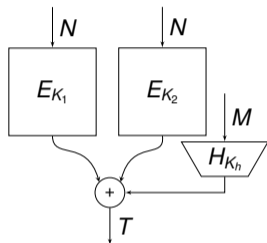


EDM Wegman-Carter

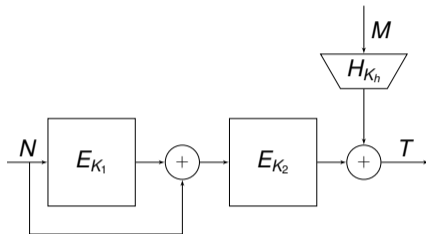


EDMD Wegman-Carter

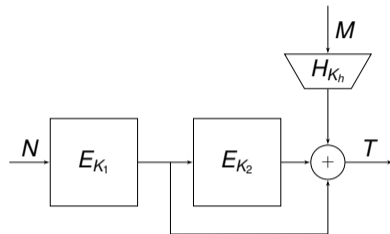
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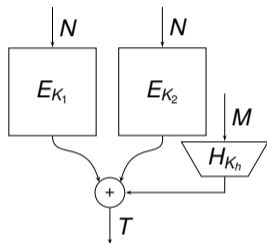
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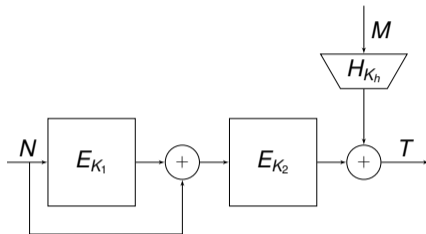
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n -bit security in nonce-respecting scenario

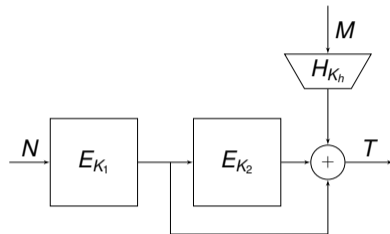
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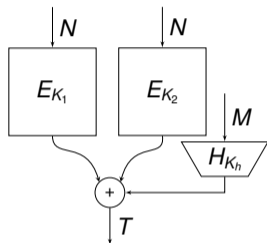


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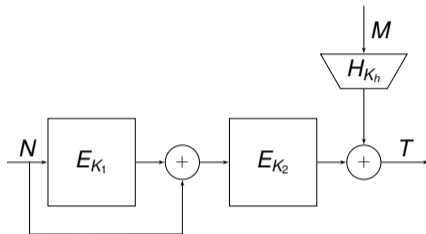
n -bit security in nonce-respecting scenario

Totally broken if a single nonce is re-used

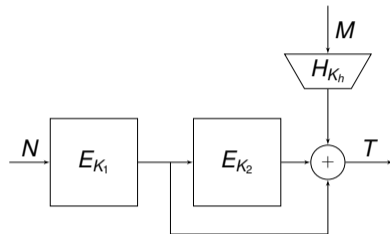
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SoP Wegman-Carter



EDM Wegman-Carter



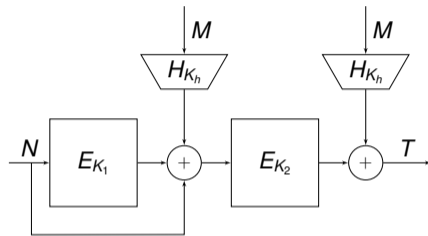
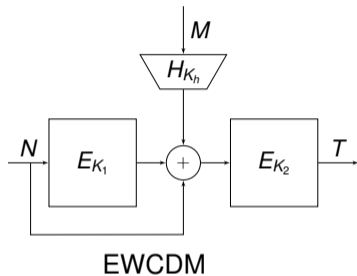
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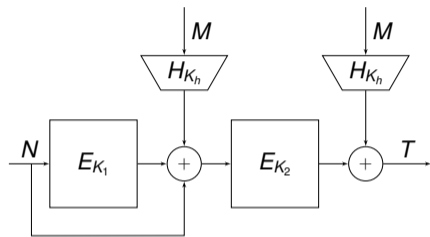
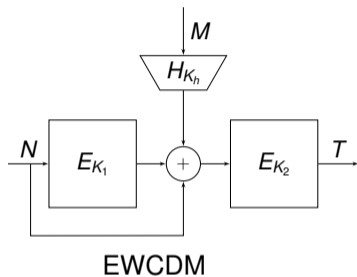
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Schemes left: 4 based on EDM, 2 based on SoP, and 1 based on EDMD

Nonce-Based MAC Algorithms Based on EDM (1)

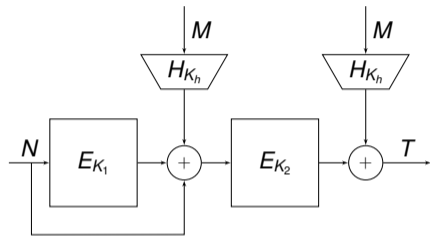
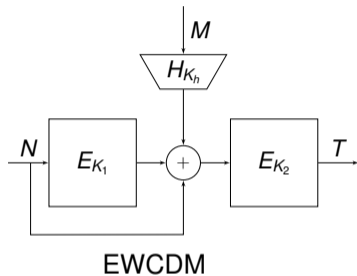


Nonce-Based MAC Algorithms Based on EDM (1)



$3n/4$ -bit security with concrete proof in nonce-respecting scenario

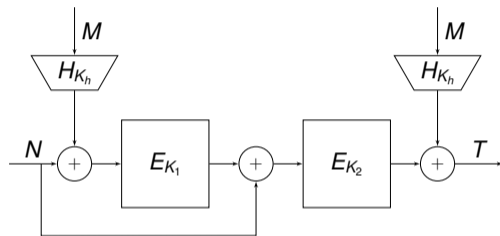
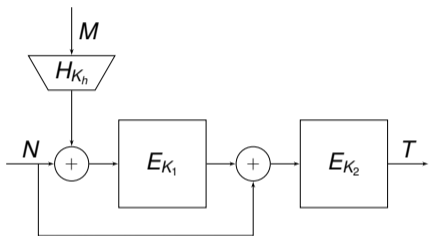
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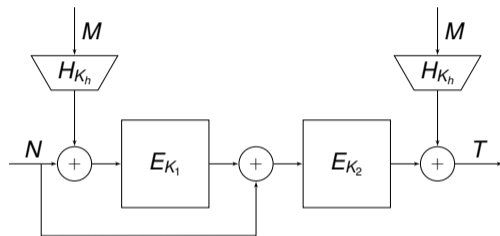
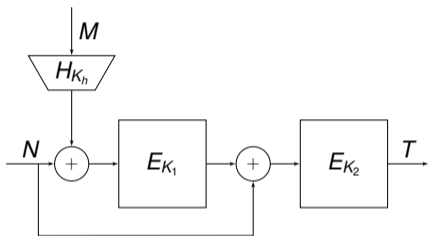
$3n/4$ -bit security with concrete proof in nonce-respecting scenario

No graceful security degradation, $n/2$ -bit security if a single nonce is re-used

Nonce-Based MAC Algorithms Based on EDM (2)

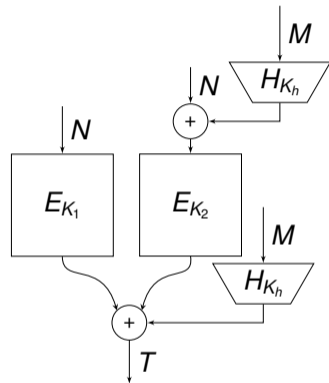
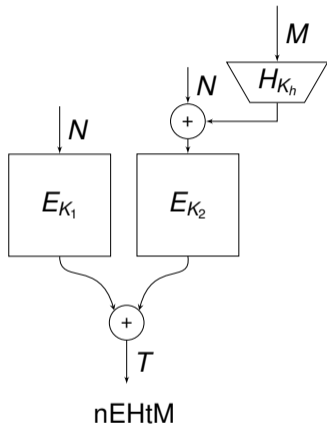


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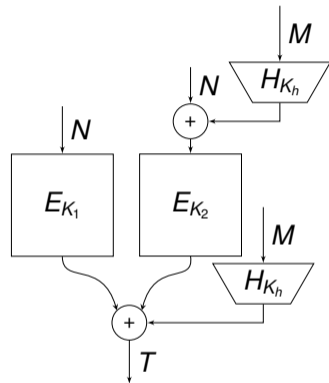
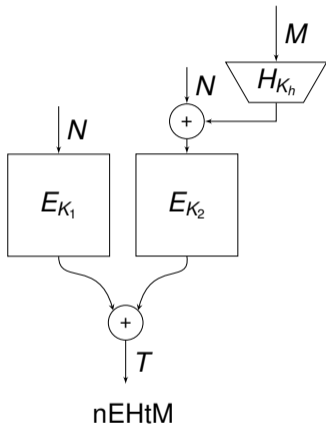


$3n/4$ -bit security if number of faulty queries $\leq 2^{n/2}$

Nonce-Based MAC Algorithms Based on SoP

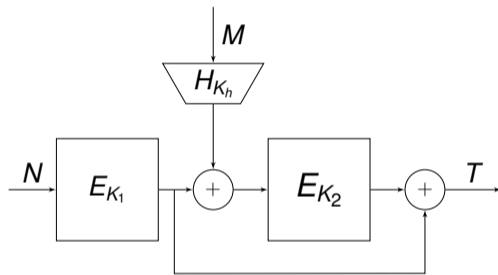


Nonce-Based MAC Algorithms Based on SoP

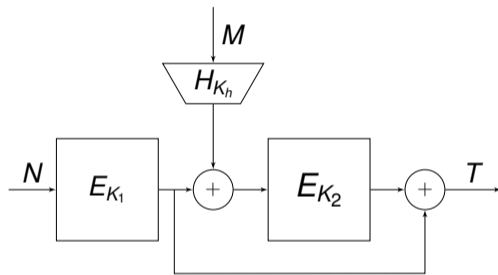


$3n/4$ -bit security if number of faulty queries $\leq 2^{3n/8}$

Nonce-Based MAC Algorithm Based on EDMD

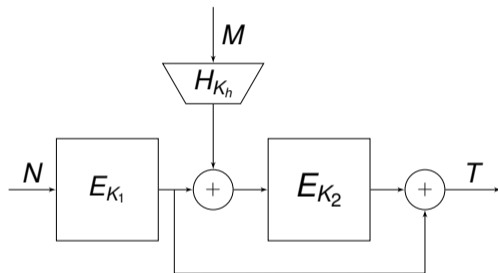


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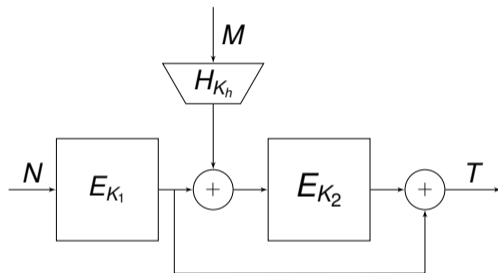
- Outputs of E_{K_1} are not known

Nonce-Based MAC Algorithm Based on EDMD



- Outputs of E_{K_1} are not known
- Outputs of E_{K_2} are also not known due to feed-forward (we only know T)

Nonce-Based MAC Algorithm Based on EDMD



- Outputs of E_{K_1} are not known
- Outputs of E_{K_2} are also not known due to feed-forward (we only know T)
- Impossible to apply any other currently known technique

- Patarin's H-coefficient technique

$$\frac{\Pr(X_{\mathcal{O}} = \tau)}{\Pr(X_{\mathcal{P}} = \tau)} \geq 1 - \epsilon$$

$$\mathbf{Adv}(\mathcal{A}) \leq \epsilon + \Pr(X_{\mathcal{P}} \in \mathcal{T}_{\text{bad}})$$

Security Analysis

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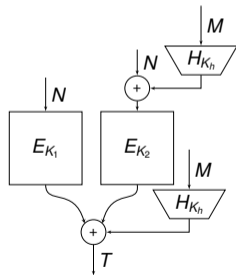
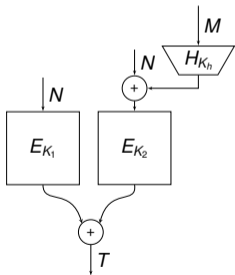
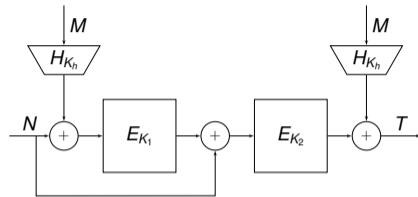
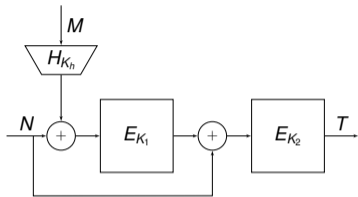
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- Patarin's mirror theory to obtain ϵ , transcript graph should be
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 - ▶ non-zero path label
 - ▶ these two properties define $\Pr(X_{\mathcal{P}} \in \mathcal{T}_{\text{bad}})$

Comparison

MAC	nonce-resp. security (\log_2)	nonce-misuse security (\log_2)	computing E_{K_1} without M	sequential/ parallel	security tightness	note
$F_{B_1}^{\text{EDM}}$	n	0	✓	S	tight	WC-with-EDM
$F_{B_1}^{\text{SoP}}$	n	0	✓	P	tight	WC-with-SoP
$F_{B_1}^{\text{EDMD}}$	n	0	✓	S	tight	WC-with-EDMD
$F_{B_2}^{\text{EDM}}$	$3n/4$ (n)	$n/2$	✓	S	not (tight)	EWCDM
$F_{B_3}^{\text{EDM}}$	$3n/4$	$n/2$	✓	S	not	this work
$F_{B_4}^{\text{EDM}}$	$3n/4$	$3n/4$ ($\mu < 2^{n/2}$)	—	S	?	this work
$F_{B_5}^{\text{EDM}}$	$3n/4$	$3n/4$ ($\mu < 2^{n/2}$)	—	S	?	this work
$F_{B_2}^{\text{SoP}}$	$3n/4$	$3n/4$ ($\mu \leq 2^{n/4}$)	✓	P	?	nEHtM
$F_{B_3}^{\text{SoP}}$	$3n/4$	$3n/4$ ($\mu \leq 2^{n/4}$)	✓	P	?	this work
$F_{B_2}^{\text{EDMD}}$?	?	✓	S	—	—

Four MAC Algorithms with Graceful Security Degradation



Conclusion

New results

- All PRFs based on two block cipher calls
- All MAC algorithms based on one universal hash function and two block cipher calls
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Thank you for your attention!