

KHAPE: Asymmetric PAKE from Key-Hiding Authenticated Key Exchange

Crypto 2021

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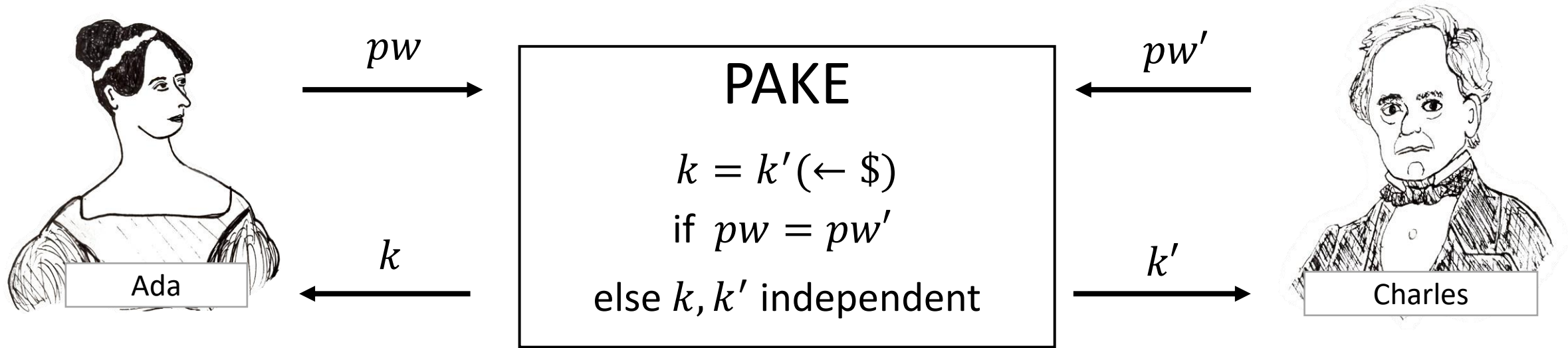
Hugo Krawczyk



PAKE: Password Authenticated Key Exchange

[BM92,...,BPR00,BMP00,...,GL01,KOY01,...,CHKLM05,...]

Authentication in the symmetric password-only setting



Most efficient PAKE's: "password-blinded" Diffie-Hellman Key Exchange (DH KE):

EKE [BM92], *SPEKE* [Jab96], *PPK* [BMP00], *SPAKE2* [AP05], *TBPEKE* [PW17], *CPace* [HL19], ...

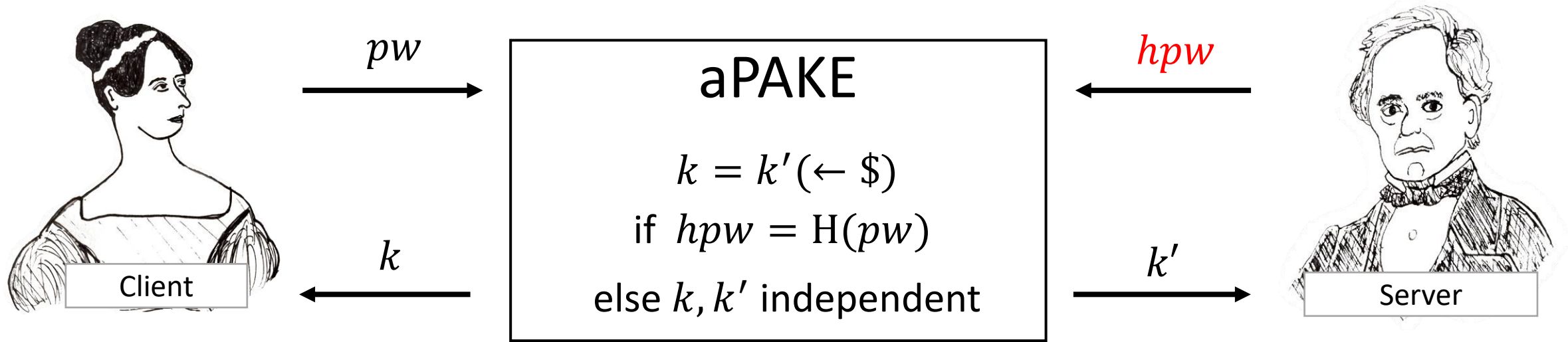
Low overhead over DH KE $\rightarrow \text{cost}(\text{PAKE}) \approx \text{cost}(\text{KE})$

(for cost-comparisons we assume prime-order groups + ROM)

asymmetric PAKE (aPAKE): for **client-server setting**

[Jablon97,...,GMR06,...,BP13,...]

Server Initialization: on input pw , compute a “hashed password”, $hpw = H(pw)$
 H : one-way hash



Benefit of aPAKE: **server compromise** leaks $pw = H^{-1}(hpw)$ **only via brute-force search**

Most efficient aPAKE's: PAKE + pw-based PKE [BMP00,...,HJKLSX18,Shoup20] or Signature [...,GMR06,HJKLSX18]

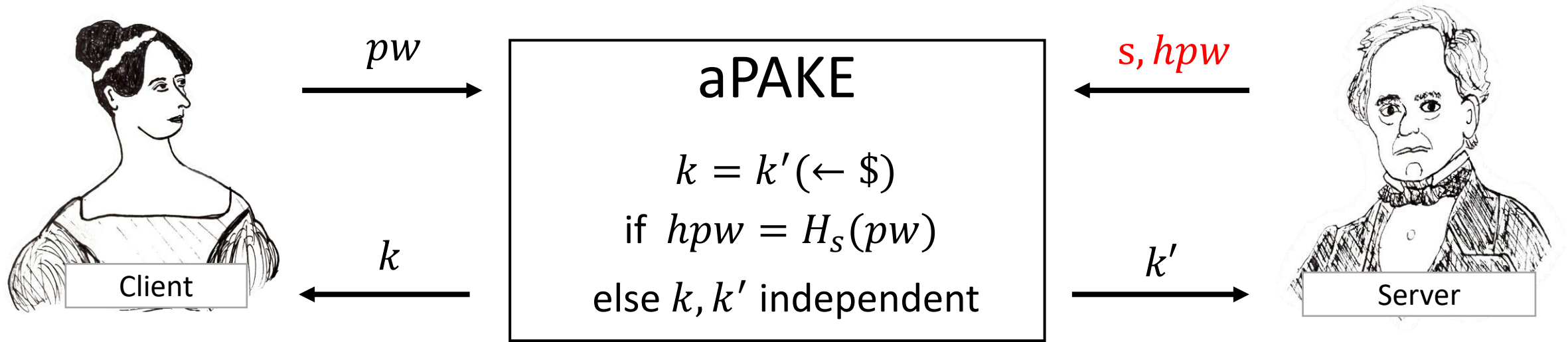
$\text{cost(aPAKE)} \approx 1.5 \times \text{cost(KE)}$, using Schnorr signatures

(for cost-comparisons we assume prime-order groups + ROM)

strong asymmetric PAKE (saPAKE)

[JKX'18,BJX'19,JKX'21]

Server Initialization: on input pw , pick random “salt” s , compute $hpw = H_s(pw)$
 H : keyed one-way hash



Benefit of saPAKE: the brute-force attack on server compromise **cannot be precomputed**

Most efficient saPAKE: *OPAQUE* = (OPRF + AKE) [JKX18]

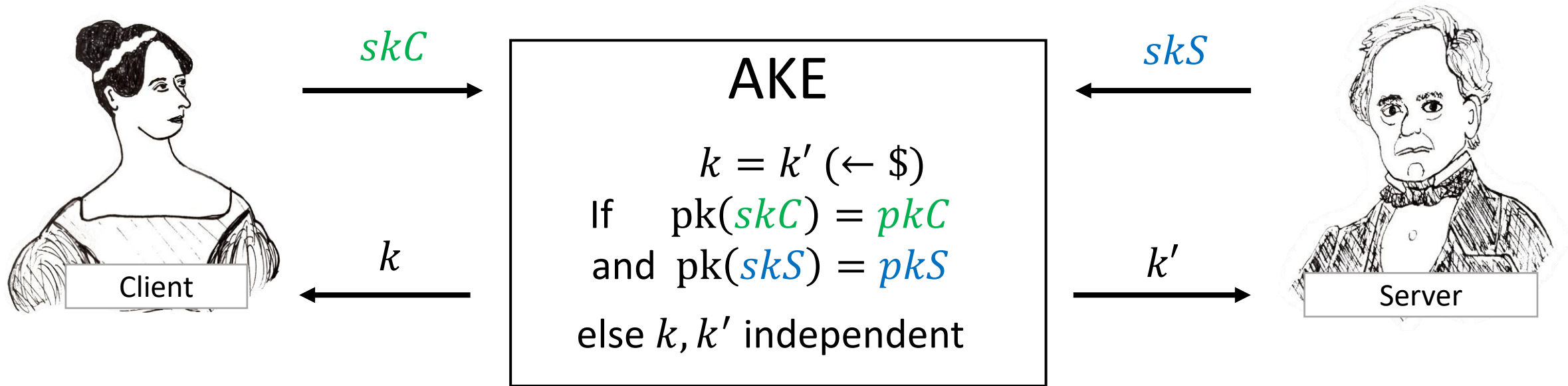
$\text{cost}(\text{saPAKE}) = \text{cost}(\text{OPRF}) + \text{cost}(\text{AKE}) \approx 2 \times \text{cost}(\text{KE})$ [JKX18,JKX21]

(for cost-comparisons we assume prime-order groups + ROM)

Authenticated Key Exchange (AKE) [Br93,Kra96,CK01,Kra03,...]

public key setting: each party generates (sk, pk)

Public keys pk_C and pk_S assumed known by both Client and Server



Most efficient AKE: *HMQR* [Kra05]

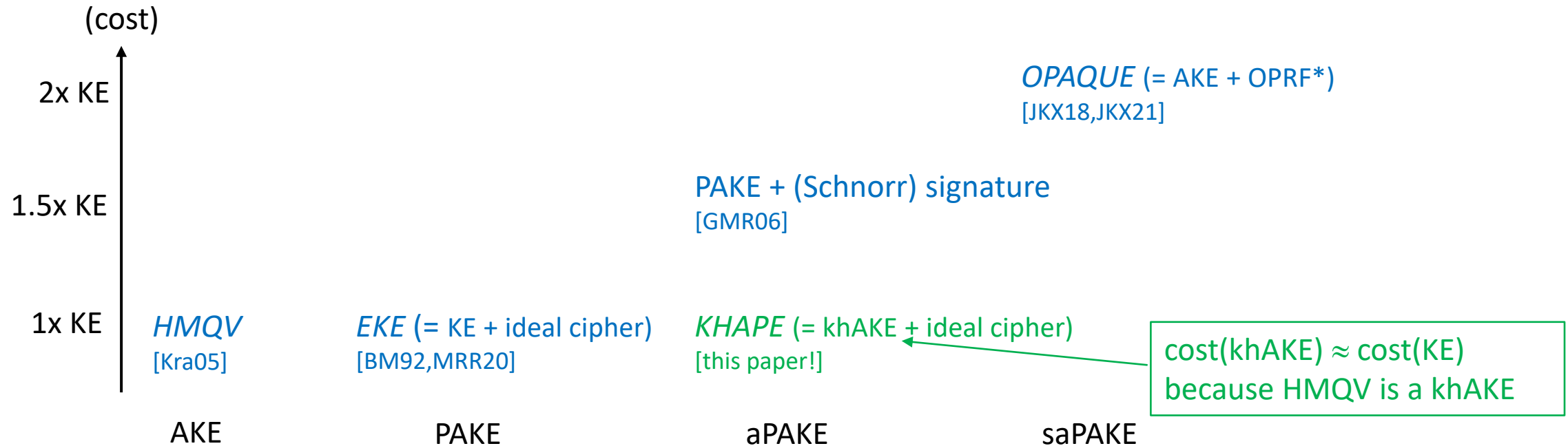
$\text{cost}(\text{AKE}) \approx \text{cost}(\text{KE})$

(for cost-comparisons we assume prime-order groups + ROM)

must aPAKE cost more than KE / AKE / PAKE?

comparisons for prime-order groups, assuming DH (OneMore-DH for *) and ROM

our main contribution: *KHAPe*: aPAKE from *key-hiding* AKE (khAKE)



AKE:	Authenticated KE	<i>parties hold public keys</i>
PAKE:	Password-Authenticated KE	<i>parties hold shared password</i>
aPAKE:	asymmetric PAKE	<i>server holds password hash</i>
saPAKE:	strong asymmetric PAKE	<i>server holds randomized password hash</i>

our contributions

1. *KHAPE*: generic construction of aPAKE = IdealCipher + key-hiding AKE

- assumes Ideal Cipher on (elliptic curve) group
 - option 1: uniform EC point encoding, e.g. Elligator2 [BHKT13] or Elligator² [Tib14]
 - option 2: “weak IC” of [MRR20], one RO-indifferentiable hash onto curve per enc/dec [still to confirm]

2. UC notion of key-hiding AKE (khAKE)

- realized (in ROM) by *HMQRV* [Kra03], *3DH* [MP16], *SKEME* [Kra96] (first proofs of UC security for these AKEs)
- *SKEME* is a generic construction → post-quantum aPAKE from lattice KEM (alternative to e.g. [GMR06,HJKLSX18])

→ $\text{cost(aPAKE)} \approx \text{cost(KE)}$ (if *KHAPE* is instantiated with khAKE = *HMQRV*)

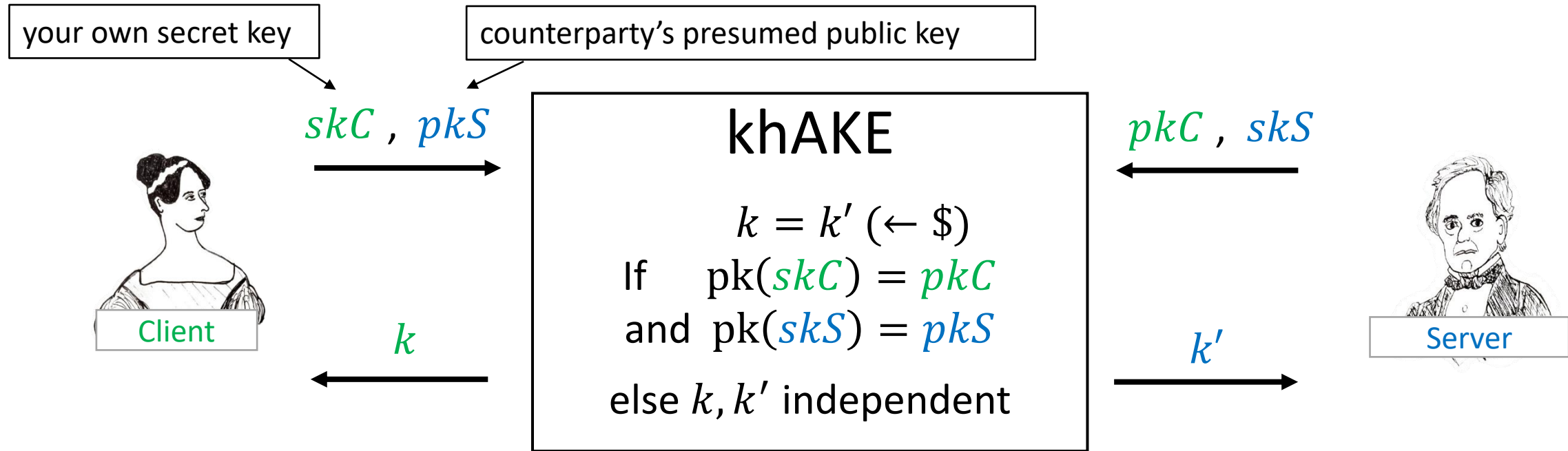
- price: 4 flows (3 if S starts) vs 3 flows of *SPAKE2+* [APE05,Shoup20], *GMR+EKE* [GMR06], *OPAQUE* [JKX18]

→ efficient instantiation of saPAKE construction *OPAQUE'* (= OPRF + aPAKE) [JKX18]

- alternative to *OPAQUE* (= OPRF + AKE) [JKX18]
- advantages: graceful security degradation from saPAKE to aPAKE if OPRF key leaks
application examples: outsourced/distributed OPRF, quantum-insecure OPRF
- disadvantages: added protocol flow, need *key-hiding* AKE (e.g. cannot use *Sigma* AKE [Kra03] from TLS)

UC notion of key-hiding AKE (khAKE)

public key setting: each party generates (sk, pk)



Key-Hiding AKE properties (assume attacker plays **client**'s role):

- Server's output k' reveals only if adversary's values (skC^*, pkS^*) matches Server's inputs (pkC, skS)
- **no perfect-forward secrecy (pfs) / privacy (pfp)**: k' can be computed for (skC^*, pkS^*) leaked in the future
 - pfs: easy to achieve with key confirmation messages
 - pfp: harder (can be achieved with less efficient protocols, e.g. "input-commit + SPHF")

[why not include pfs/pfp? we model minimal khAKE properties sufficient for our khAKE-to-aPAKE compiler]

key-hiding AKE example 1: $3DH$ [MP16]

Diffie-Hellman KE/KEM $\approx$ ElGamal PKE

Client Init: $skC \leftarrow Z_p$, $pkC = g^{skC}$

Server Init: $skS \leftarrow Z_p$, $pkS = g^{skS}$

Input: skC , pkS

Input: pkC , skS



$x \leftarrow Z_p$

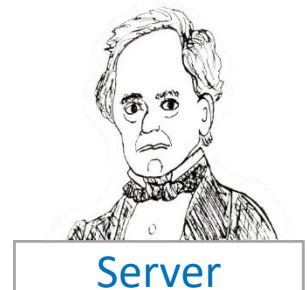
$X = g^x$



$Y = g^y$



$y \leftarrow Z_p$



Output computation: $k = H[DH(X, pkS), DH(pkC, Y), DH(X, Y)]$

- H is an RO hash (also taking session and party identifiers as inputs)
- DH is a Diffie-Hellman KE function, i.e. $DH(g^a, g^b) = g^{a \cdot b}$

key-hiding AKE example 2: *HMQV* [Kra05]

Diffie-Hellman KE/KEM $\approx$ ElGamal PKE

Client Init: $skC \leftarrow Z_p$, $pkC = g^{skC}$

Server Init: $skS \leftarrow Z_p$, $pkS = g^{skS}$

Input: skC, pkS

Input: pkC, skS

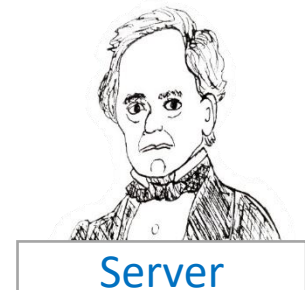


$x \leftarrow Z_p$

$X = g^x$

$Y = g^y$

$y \leftarrow Z_p$



Output computation: $k = H[DH(X \cdot (pkC)^{H'(X)}, Y \cdot (pkS)^{H'(Y)})]$

- H is an RO hash (also taking session and party identifiers as inputs)
- DH is a Diffie-Hellman KE function, i.e. $DH(g^a, g^b) = g^{a \cdot b}$

cost(HMQV)
 $\approx$ cost(DH KE)

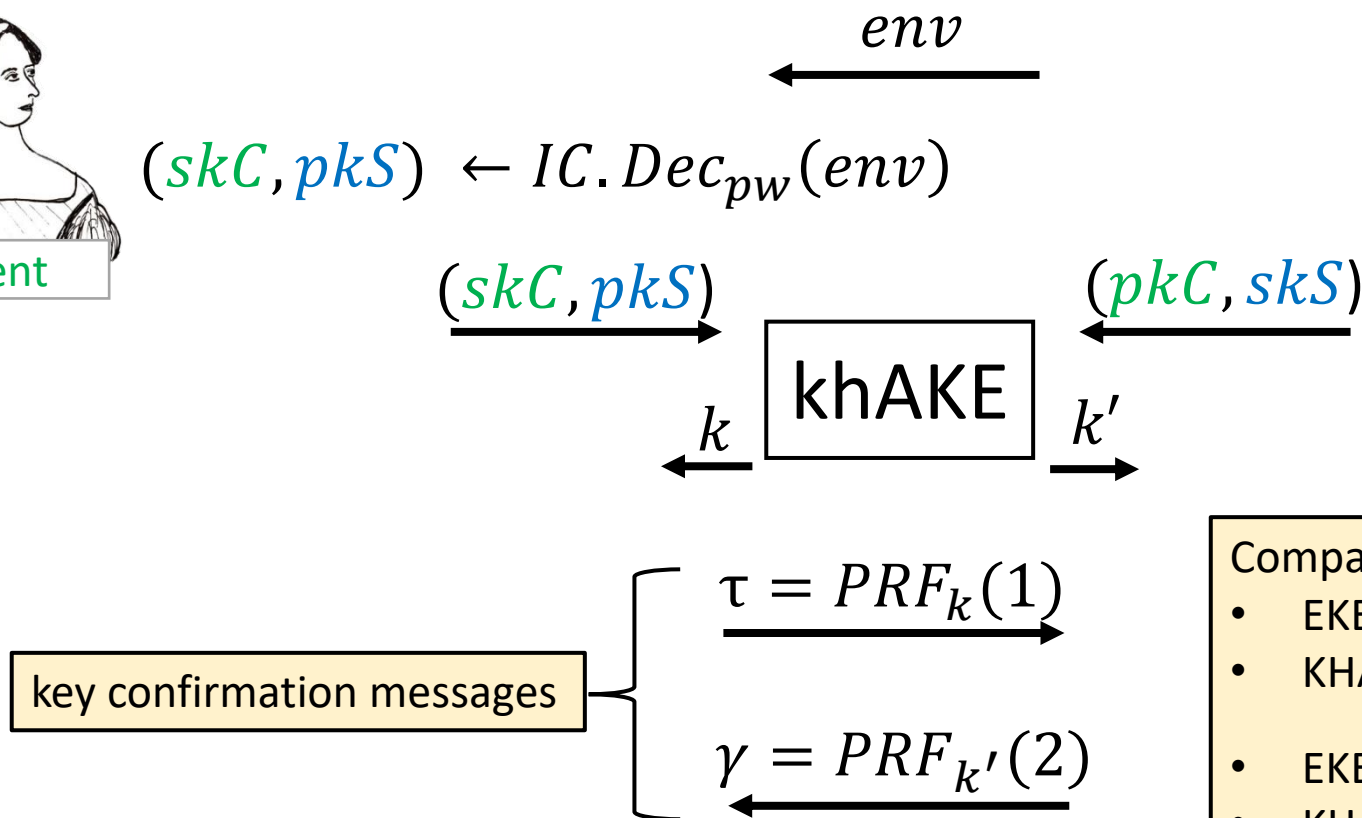
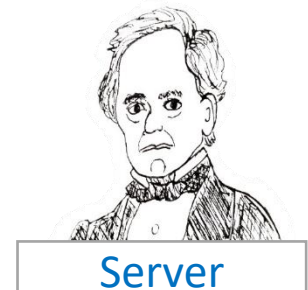
KHAPE: aPAKE from key-hiding AKE + Ideal Cipher

Initialization: $(skC, pkC) \leftarrow AKE.KG, (skS, pkS) \leftarrow AKE.KG$
 $env \leftarrow IC.Enc_{pw}(skC, pkS)$ ← group element

Input: pw



Input: $hpw = (env, pkC, skS)$



Compare to “EKE” PAKE of [BM92]:

- EKE = KE $\rightarrow$ PAKE compiler
- KHAPE = AKE $\rightarrow$ aPAKE compiler
- EKE uses IC to pw-encrypt each KE message
- KHAPE uses IC to pw-encrypt C’s AKE inputs

KHAPE: aPAKE from key-hiding AKE + Ideal Cipher

Initialization: $(skC, pkC) \leftarrow AKE.KG, (skS, pkS) \leftarrow AKE.KG$
 $env \leftarrow IC.Enc_{pw}(skC, pkS)$

Input: pw



$(skC, pkS) \leftarrow IC.Dec_{pw}(env)$

(skC, pkS)

env

(pkC, skS)

khAKE

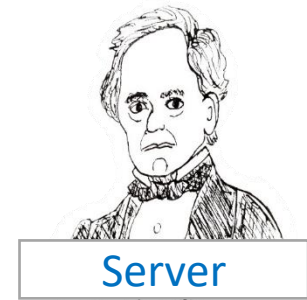
k

k'

$\tau = PRF_k(1)$

$\gamma = PRF_{k'}(2)$

Input: $hpw = (env, pkC, skS)$



For passive attacker:

- IC $\rightarrow$ each pw^* maps to (skC^*, pkS^*)

If attacker plays server role:

- IC $\rightarrow$ ciphertext env^* commits to single pw^* s.t. $IC.Dec_{pw^*}(env^*)$ is non-random
 - $\rightarrow$ single pkS^* for which Adv knows skS^*
 - $\rightarrow$ single pw^* on which Adv attacks the Client

KHAPE: aPAKE from key-hiding AKE + Ideal Cipher

Initialization: $(skC, pkC) \leftarrow AKE.KG, (skS, pkS) \leftarrow AKE.KG$
 $env \leftarrow IC.Enc_{pw}(skC, pkS)$

Input: pw



$(skC, pkS) \leftarrow IC.Dec_{pw}(env)$

(skC, pkS)

env

(pkC, skS)

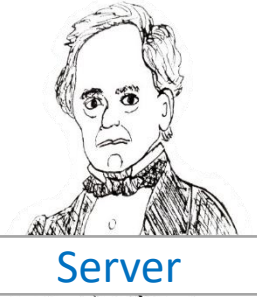
khAKE

k k'

$\tau = PRF_k(1)$

$\gamma = PRF_{k'}(2)$

Input: $hpw = (env, pkC, skS)$



For passive attacker:

- IC $\rightarrow$ each pw^* maps to (skC^*, pkS^*)

If attacker plays the **server** role:

- IC $\rightarrow$ ciphertext env^* commits to single pw^* s.t. $IC.Dec_{pw^*}(env^*)$ is non-random
 $\rightarrow$ single pkS^* for which Adv knows skS^*
 $\rightarrow$ single pw^* on which Adv attacks the Client

Can we omit **Client's** key conf msg τ ?

If attacker plays the **client** role:

- khAKE block has **no Perfect Forward Secrecy**
 $\rightarrow$ Adv could then test (skC^*, pkS^*) against S's key
 $\rightarrow$ Adv could then test off-line test any pw^*
- C's key conf msg commits to single (skC^*, pkS^*)
 $\rightarrow$ C's key conf msg commits to single pw^*

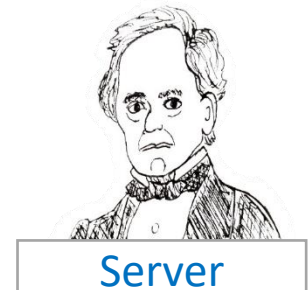
KHAPE: aPAKE from key-hiding AKE + Ideal Cipher

Initialization: $(skC, pkC) \leftarrow AKE.KG, (skS, pkS) \leftarrow AKE.KG$
 $env \leftarrow IC.Enc_{pw}(skC, pkS)$

Input: pw



Input: $hpw = (env, pkC, skS)$



$(skC, pkS) \leftarrow IC.Dec_{pw}(env)$

(skC, pkS) (pkC, skS)

khAKE

k k'

$\tau = PRF_k(1)$

$\gamma = PRF_{k'}(2)$

For passive attacker:

- IC $\rightarrow$ each pw^* maps to (skC^*, pkS^*)

If attacker plays server role:

- IC $\rightarrow$ ciphertext env^* commits to single pw^* s.t. $IC.Dec_{pw^*}(env^*)$ is non-random
- $\rightarrow$ single pkS^* for which Adv knows skS^*
- $\rightarrow$ single pw^* on which Adv attacks the Client

Can we omit Server's key conf msg γ ?

If attacker plays the server role:

- khAKE block has **no Perfect Forward Secrecy**
- $\rightarrow$ Adv can compute Client's key if it compromises Server and learns (pkC, skS) in the future
- S's key conf msg verifies Adv knows (pkC, skS) before Client outputs a key

conclusions & some follow-up questions

Our contributions:

- *KHAPE*, new aPAKE from key-hiding AKE
 - optimal computational efficiency ($\approx$ KE), black-box from KEM
- UC notion of key-hiding AKE, realized by *HMQV*, *3DH*, *SKEME*
- efficient instantiation of saPAKE protocol *OPAQUE'*
 - offers graceful security degradation from saPAKE to aPAKE if OPRF key leaks

Some follow-up questions:

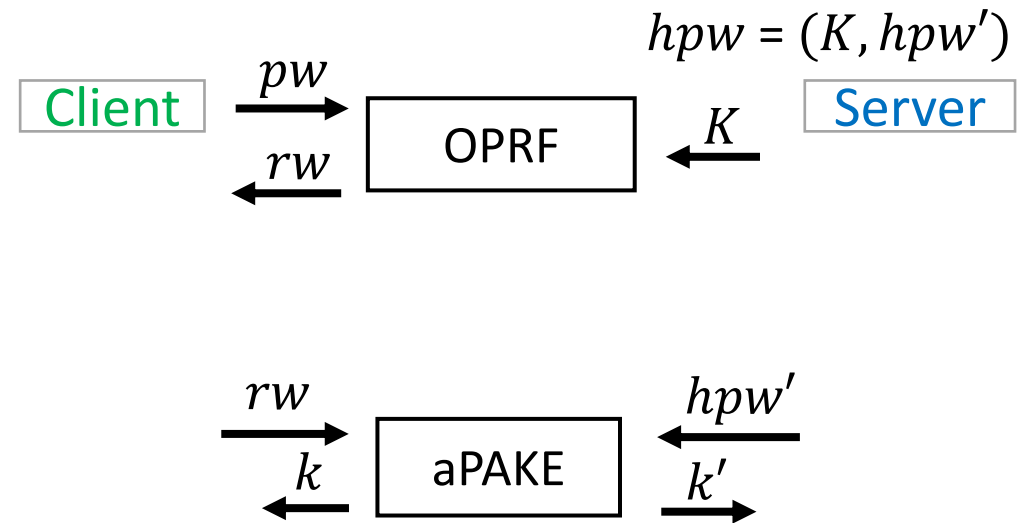
- optimal-cost aPAKE with 3 flows? *[we have some results in preparation]*
- using lattice-based key-private KEMs for post-quantum security
 - Ideal Cipher for post-quantum?
 - Ideal Cipher for long bitstrings? *[we have some results in preparation]*
 - efficient post-quantum (UC) OPRF?

EXTRAS...

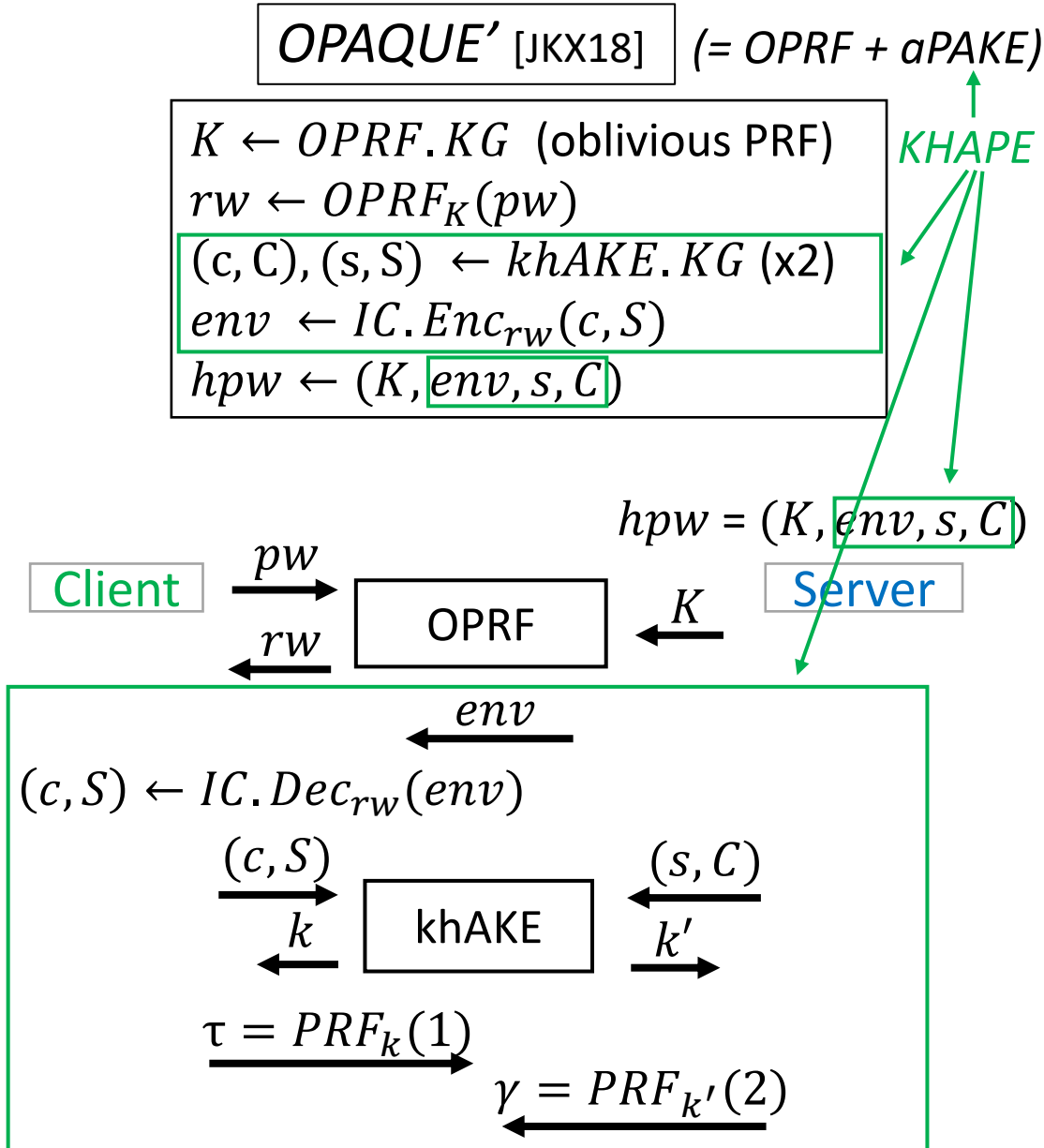
→ efficient instantiation of saPAKE *OPAQUE'* [JKX18]

OPAQUE' [JKX18] (= *OPRF* + *aPAKE*)

$K \leftarrow \text{OPRF.KG}$ (oblivious PRF)
 $rw \leftarrow \text{OPRF}_K(pw)$
 $hpw' \leftarrow \text{aPAKE.Hash}(rw)$
 $hpw \leftarrow (k, hpw')$



→ efficient instantiation of saPAKE *OPAQUE'* [JKX18]

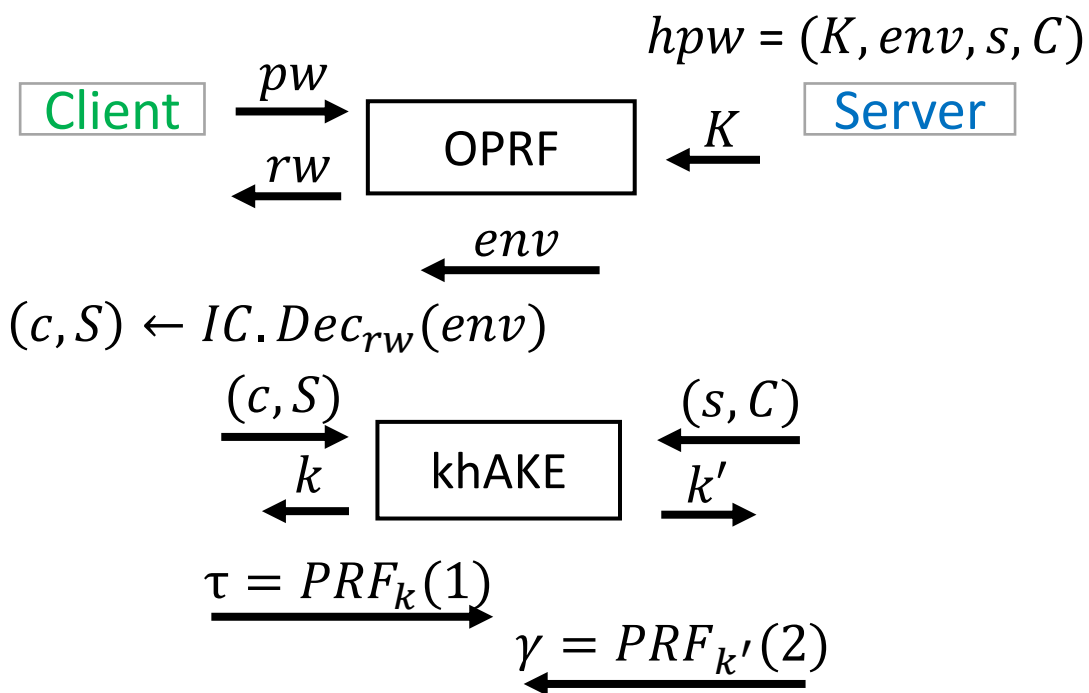


→ efficient instantiation of saPAKE *OPAQUE'* [JKX18]

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 $rw \leftarrow \text{OPRF}_K(pw)$
 $(c, C), (s, S) \leftarrow \text{khAKE.KG} \text{ (x2)}$
 $env \leftarrow \text{IC.Enc}_{rw}(c, S)$
 $hpw \leftarrow (K, env, s, C)$

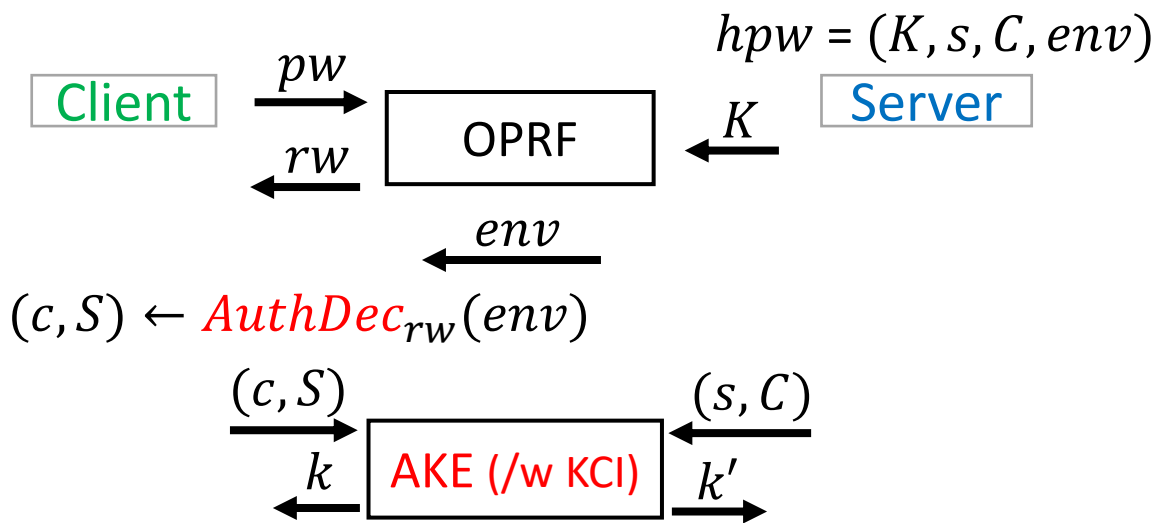
↑
KHAPE



→ efficient instantiation of saPAKE *OPAQUE'* [JKX18]

OPAQUE [JKX18] (= OPRF + AuthEnc + AKE)

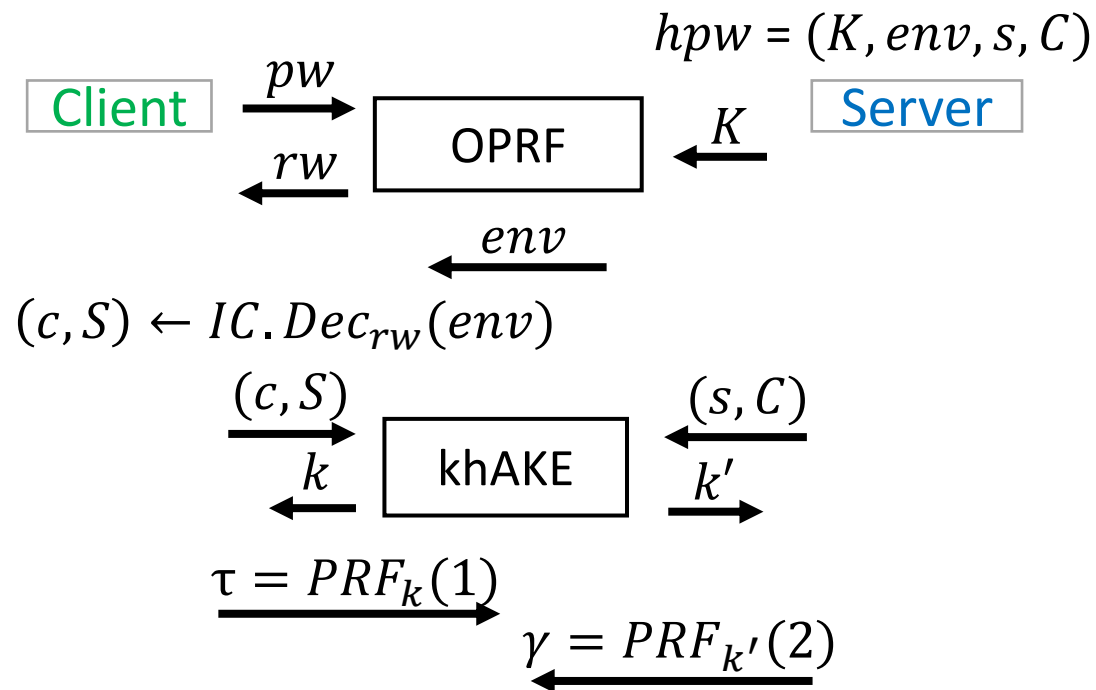
$K \leftarrow \text{OPRF.KG}$
 $rw \leftarrow \text{OPRF}_K(pw)$
 $(c, C), (s, S) \leftarrow \text{AKE.KG} (\times 2)$
 $env \leftarrow \text{AuthEnc}_{rw}(c, S)$
 $hpw \leftarrow (k, env, s, C)$



OPAQUE' [JKX18] (= OPRF + aPAKE)

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↑
KHAPE



*KCI = key compromise impersonation [security]
 $\approx$ perf. forward secrecy $\approx$ key conf. flows

→ efficient instantiation of saPAKE *OPAQUE'* [JKX18]

OPAQUE [JKX18] (= OPRF + AuthEnc + AKE)

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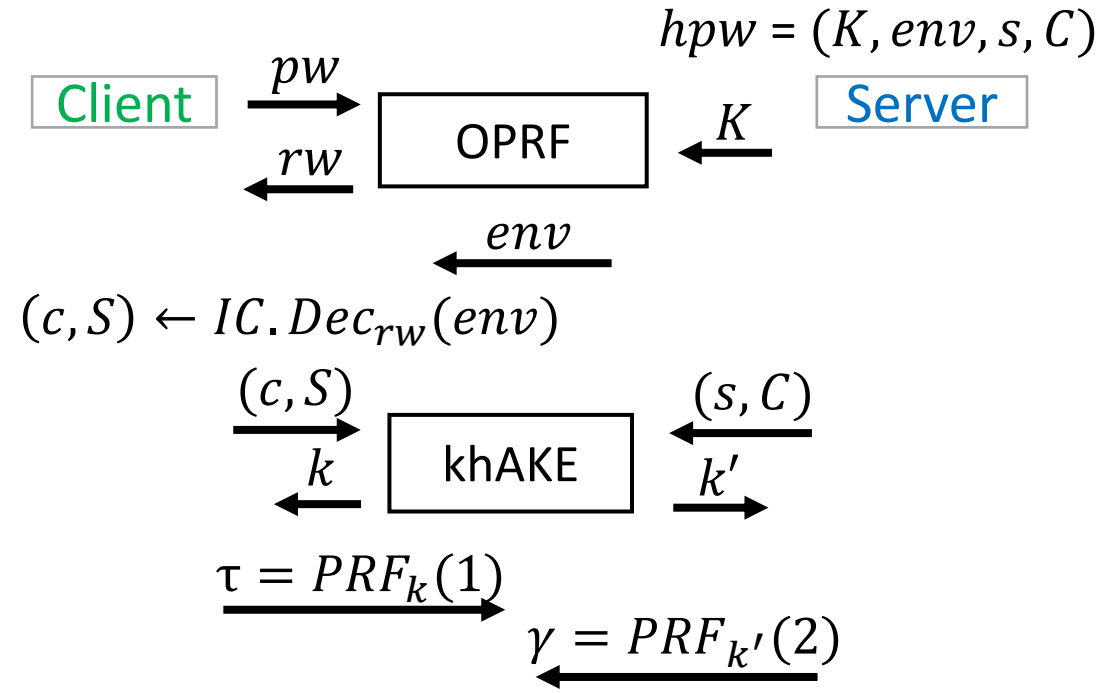
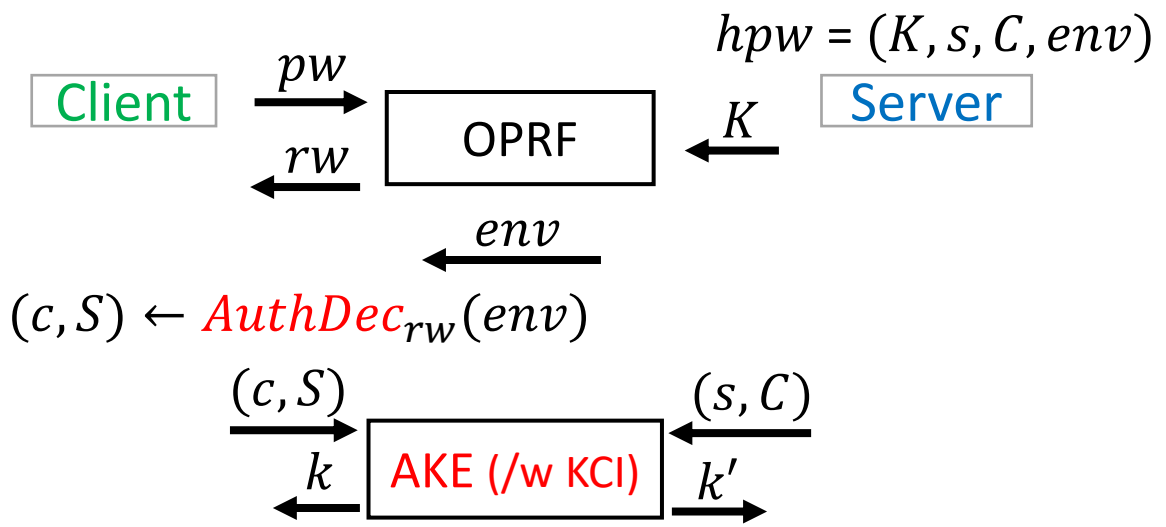
OPAQUE vs OPAQUE'

3 flows	4 flows
any* KCI-AKE	khAKE
*e.g. <i>Sigma</i> [Kra03] of TLS	
if (IT)OPRF key leaks:	
pw leaks	⇒ aPAKE

OPAQUE' [JKX18] (= OPRF + aPAKE)

$K \leftarrow \text{OPRF.KG}$ (oblivious PRF)
 $rw \leftarrow \text{OPRF}_K(pw)$
 $(c, C), (s, S) \leftarrow \text{khAKE.KG (x2)}$
 $env \leftarrow \text{IC.Enc}_{rw}(c, S)$
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↑
KHAPE



*KCI = key compromise impersonation [security]
 ≈ perf. forward secrecy ≈ key conf. flows