

Tightly-Secure Authenticated Key Exchange, Revisited

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Authenticated Key Exchange (AKE)


- Used to establish a shared session key between two parties
- One of the most widely-used cryptographic primitives, e.g. TLS

Outline

- Security model and tightness
- Comparison to previous work
- AKE from key encapsulation mechanisms (KEMs)
- Security requirements for KEM

Two-Message Authenticated Key Exchange

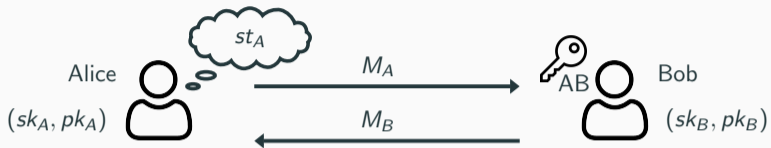
Alice
 (sk_A, pk_A) 

Bob
 (sk_B, pk_B) 

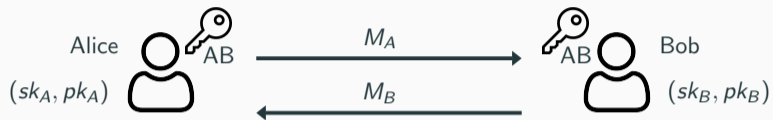
Two-Message Authenticated Key Exchange



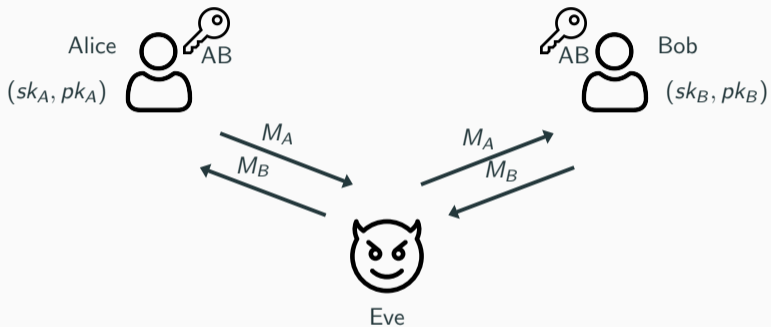
Two-Message Authenticated Key Exchange



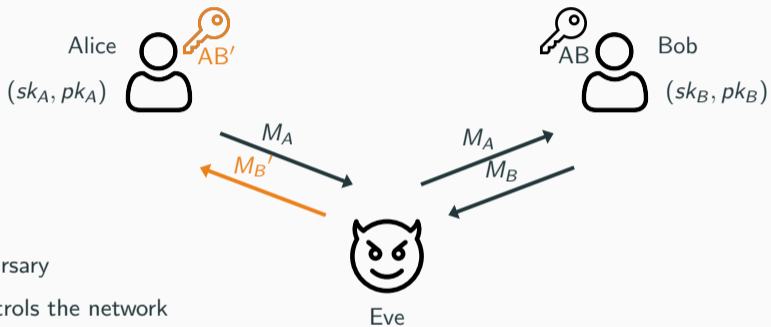
Two-Message Authenticated Key Exchange



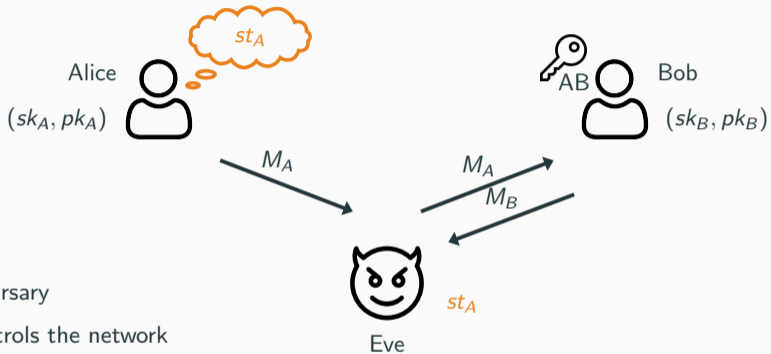
Two-Message Authenticated Key Exchange



Two-Message Authenticated Key Exchange



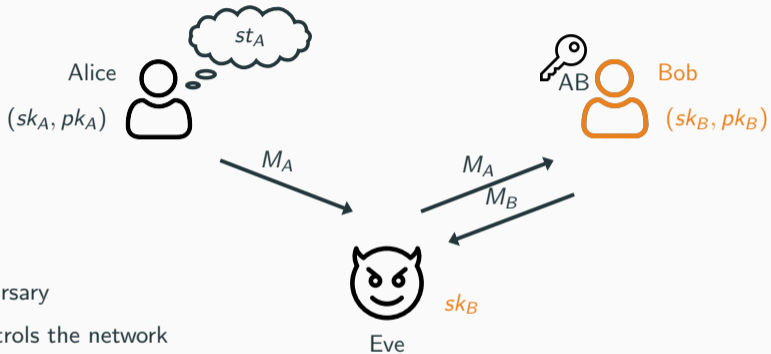
Two-Message Authenticated Key Exchange



The adversary

- controls the network
- reveals secret states

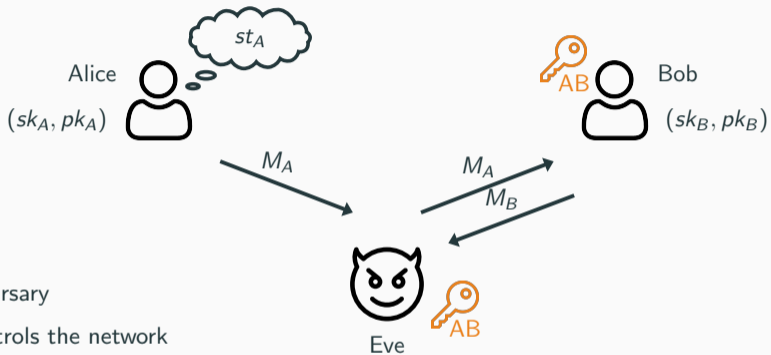
Two-Message Authenticated Key Exchange



The adversary

- controls the network
- reveals secret states
- adaptively corrupts long-term keys

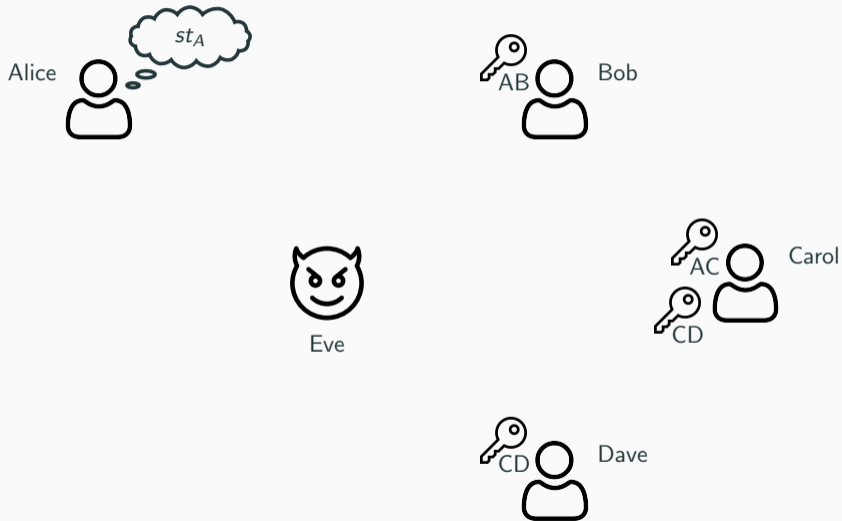
Two-Message Authenticated Key Exchange



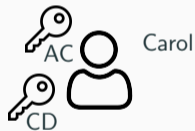
The adversary

- controls the network
- reveals secret states
- adaptively corrupts long-term keys
- reveals real session keys

Two-Message Authenticated Key Exchange



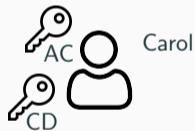
Two-Message Authenticated Key Exchange



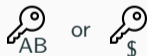
Multiple challenge queries
- with **multiple** challenge bits



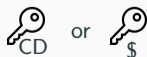
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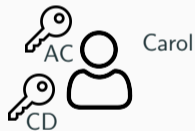
Multiple challenge queries
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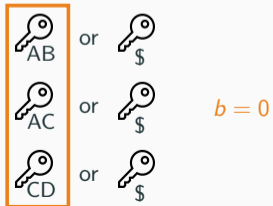
$b_2 = 1$



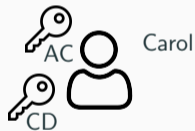
Two-Message Authenticated Key Exchange



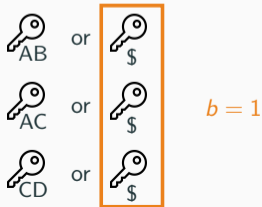
Multiple challenge queries
- with a **single** challenge bit



Two-Message Authenticated Key Exchange



Multiple challenge queries
- with a **single** challenge bit



Single challenge bit

- Well-established notion for multi-challenge security definitions
- Equivalent to “Real-or-Random” security
- Tightly composes with symmetric primitives

Security properties

- Forward secrecy
- Resistance against key compromise impersonation attacks
- Resistance against maximal exposure attacks

Provable Security

Security is modelled as a game between a challenger and an adversary.

Security reduction

- We turn adversary \mathcal{A} against the scheme into an adversary \mathcal{B} that solves a computationally hard problem.

A reduction is called *tight* if \mathcal{A} and \mathcal{B}

- have about the same advantage.
- run in about the same time.

Relevance: tells us how to choose system parameters

Comparison with Previous Work

	Standard Model	Tight Proof	Ephemeral State Reveal	Single Challenge Bit
BHJKL15	✓	✓	✗	✗
GJ18	✗	✓	✗	✗
CCGJJ19	✗	✗	✗	✓
LLGW20	✓	✓	✗	✗
This work	✗	✓	✓	✓

Our AKE Protocols

Generic Construction



Generic Construction



Main question: What security properties do we need for the KEM to achieve tightness?



Alice



Bob

$(\tilde{s}k, \tilde{p}k) \leftarrow \text{Gen}$

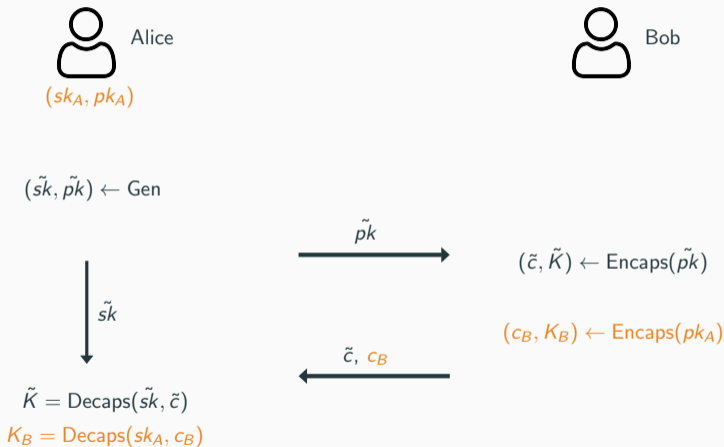


$\tilde{K} = \text{Decaps}(\tilde{s}k, \tilde{c})$

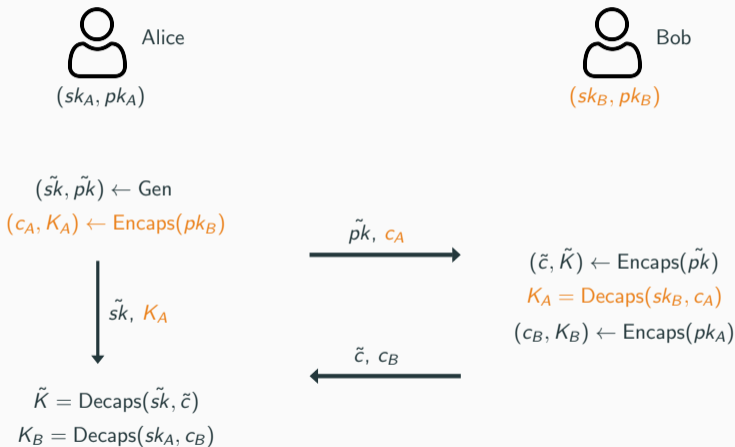


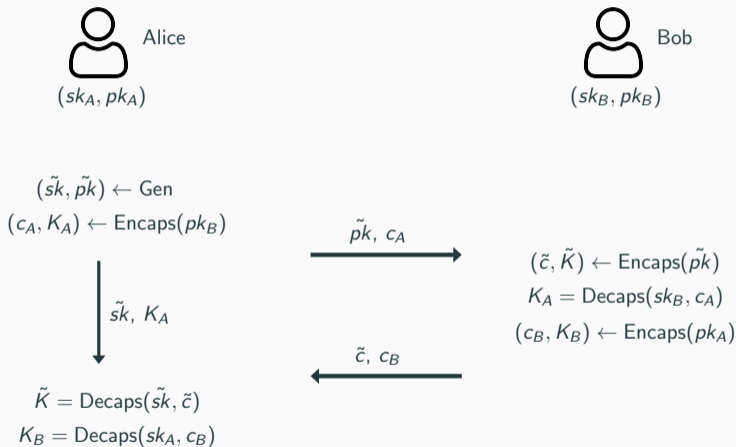
$(\tilde{c}, \tilde{K}) \leftarrow \text{Encaps}(\tilde{p}k)$





AKE[KEM]





$$K = H(A, B, pk_A, pk_B, \tilde{pk}, c_A, c_B, \tilde{c}, K_A, K_B, \tilde{K})$$

Security Requirements for KEM

Corruption queries

- Need to output long-term secret keys adaptively (sk_A, sk_B)
- Previously sent ciphertexts must decrypt correctly

Non-Committing
Key Encapsulation

Reveal-key vs. challenge queries

- Ciphertexts may be revealed or used in challenges
- Need to decrypt ciphertexts coming from the adversary

State reveals

- Need to output ephemeral secret keys (\tilde{sk})
- Key indistinguishability even when state is compromised

Non-Committing Key Encapsulation from DDH

Public parameter: group description (\mathbb{G}, p, g) and $h = g^\omega$ for $\omega \xleftarrow{\$} \mathbb{Z}_p$

KeyGen

$$sk = (x_0, x_1) \xleftarrow{\$} \mathbb{Z}_p^2$$

$$pk = g^{x_0} h^{x_1}$$

Decaps(sk, c_0, c_1)

$$K = H(pk, c, c_0^{x_0} c_1^{x_1})$$

Encaps(pk)

$$r \xleftarrow{\$} \mathbb{Z}_p$$

$$(c_0, c_1) = (g^r, h^r)$$

$$K = H(pk, c_0, c_1, pk^r)$$

SimEncaps(sk)

$$(r, s) \xleftarrow{\$} \mathbb{Z}_p^2$$

$$(c_0, c_1) = (g^r, h^s)$$

$$K = H(pk, c_0, c_1, c_0^{x_0} c_1^{x_1})$$

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Properties

- Encaps \approx_c SimEncaps
- Holds even given sk

Encaps(pk)

$$r \xleftarrow{\$} \mathbb{Z}_p$$
$$(c_0, c_1) = (g^r, h^r)$$
$$K = H(pk, c_0, c_1, pk^r)$$

SimEncaps(sk)

$$(r, s) \xleftarrow{\$} \mathbb{Z}_p^2$$
$$(c_0, c_1) = (g^r, h^s)$$
$$K = H(pk, c_0, c_1, c_0^{x_0} c_1^{x_1})$$

$$(c_0, c_1) \in \mathcal{L}_{\text{DDH}}$$

$$(c_0, c_1) \notin \mathcal{L}_{\text{DDH}}$$

Non-Committing Key Encapsulation from DDH

Public parameter: group description (\mathbb{G}, p, g) and $h = g^\omega$ for $\omega \xleftarrow{\$} \mathbb{Z}_p$

KeyGen

$$sk = (x_0, x_1) \xleftarrow{\$} \mathbb{Z}_p^2$$

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Encaps(pk)

$$r \xleftarrow{\$} \mathbb{Z}_p$$

$$(c_0, c_1) = (g^r, h^r)$$

$$K = H(pk, c_0, c_1, pk^r)$$

$$(c_0, c_1) \in \mathcal{L}_{\text{DDH}}$$

Decaps(sk, c₀, c₁)

$$K = H(pk, c, c_0^{x_0} c_1^{x_1})$$

SimEncaps(sk)

$$(r, s) \xleftarrow{\$} \mathbb{Z}_p^2$$

$$(c_0, c_1) = (g^r, h^s)$$

$$K = H(pk, c_0, c_1, c_0^{x_0} c_1^{x_1})$$

$$(c_0, c_1) \notin \mathcal{L}_{\text{DDH}}$$

Properties

- Encaps \approx_c SimEncaps
- Holds even given sk
- Without knowledge of sk :
 $K \approx_s \$$

Contributions

- Non-committing key encapsulation from hash proof systems in the ROM
- Two tightly-secure AKE protocols
 - with state reveals
 - with a single challenge bit

ePrint: ia.cr/2020/1279

Follow-Up Work

- Tightly-secure AKE and signatures in the standard model (CRYPTO 2021)

Thank you!