

Attaining GOD Beyond Honest Majority With Friends and Foes

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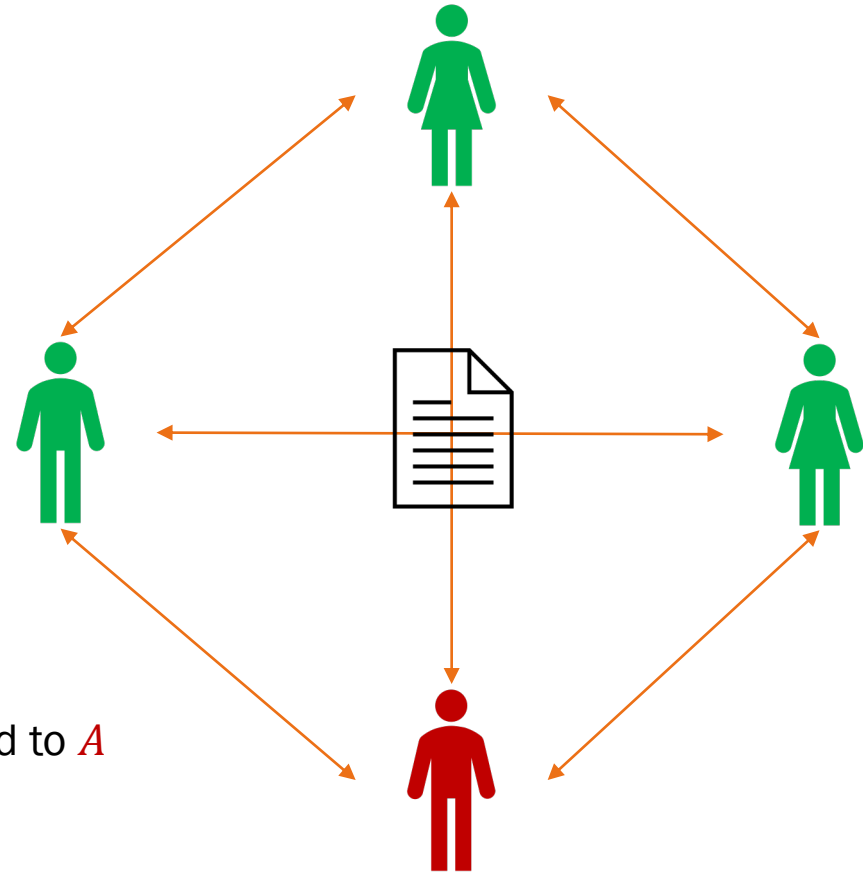


Secure Multiparty Computation

- n mutually distrusting parties P_1, P_2, \dots, P_n
- P_i has private input x_i
- n -input function f
- t corrupted by a (centralized) adversary A

Goals:

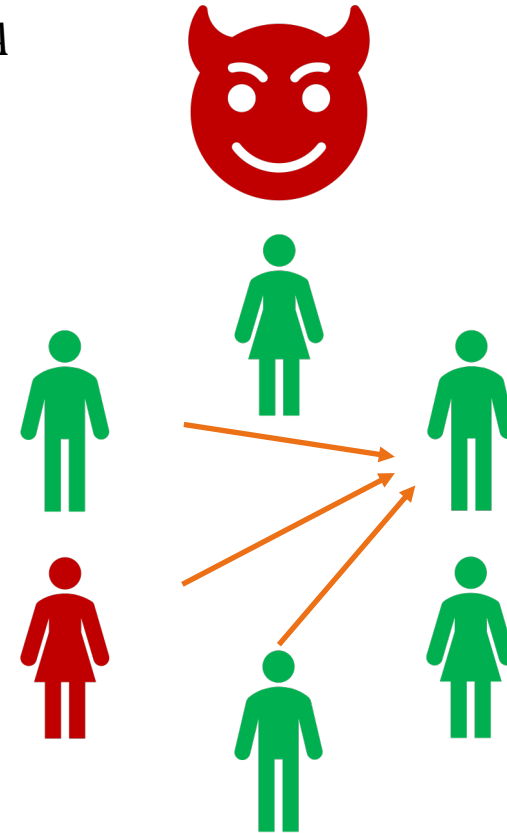
- Correctness: Compute $y = f(x_1, x_2, \dots, x_n)$
- Privacy: Nothing beyond the function output is revealed to A



View Leakage

- **Loophole** in the classical security definition:
 - Adversary can leak information to honest parties
 - Protocol might require leaking info to honest parties → **GOD via TTP!**

(t) -Malicious
 A



Friends and Foes (FaF)

(t, h^*) -FaF security

- t maliciously corrupted parties (**Foes**)
- h^* semi-honest parties (**Friends**)

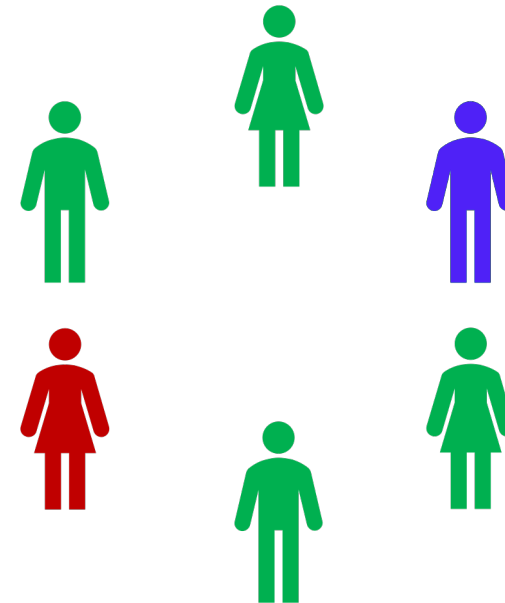
$$\text{View}_{\text{Foes}}^{\text{Ideal}} \approx \text{View}_{\text{Foes}}^{\text{Real}}$$

$$\text{View}_{\text{Friends}}^{\text{Ideal}} \approx \text{View}_{\text{Friends}}^{\text{Real}}$$

(t) -Malicious
 A



(h^*) -S.H.
 A_H



Our Results

- Theoretical
 - Necessity of Oblivious Transfer (OT) for generic (t, h^*) -FaF secure protocol with $n \leq 2t + 2h^*$
- Practical
 - QuadSquad: Robust/Fair $(1,1)$ -FaF secure 4PC
 - Optimal corruption threshold

Any n -party functionality f can be computed with robust/fair computational (t, h^*) -FaF security, iff $n > 2t + h^*$.

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 - Preprocessing paradigm
 - Operates over rings
 - Application in Privacy-Preserving Machine Learning (PPML)

Preprocessing Phase

- Input independent
- Computationally intensive tasks

Online Phase

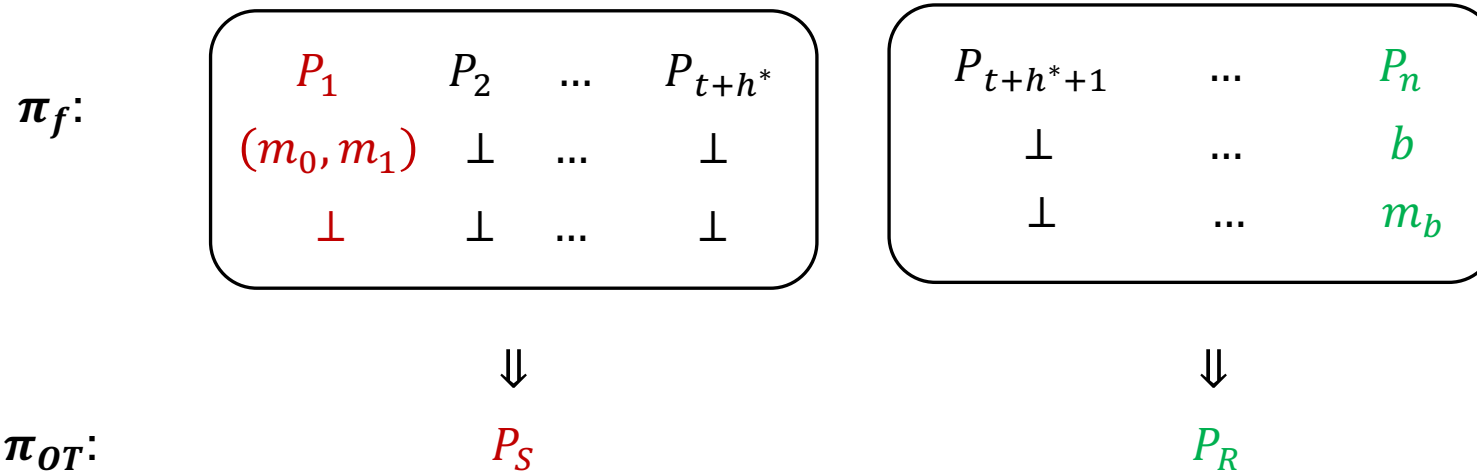
- Input dependent

Necessity of OT

π_f : (t, h^*) -FaF Protocol
 $f(x_1, x_2, \dots, x_n) = (y_1, y_2, \dots, y_n)$

\Rightarrow

π_{OT} : 2-party OT Protocol
 $f((m_0, m_1), b) = (\perp, m_b)$



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Comparison with existing work

Ref.	Preprocessing Comm.	Online		Model	Security
		Rounds	Comm.		
Tetrad (R)	2	1	3	Honest Majority ($t = 1$)	GOD
Fantastic Four (R)	NA	1	6	Honest Majority ($t = 1$)	GOD
MASCOT (F)	7713	2	12	Dishonest Majority ($t = 3$)	Abort
QuadSquad (R)	1558	3	7	FaF ($t = 1, h^* = 1$)	Fair
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^ The communication cost is reported in terms of field/ring elements.

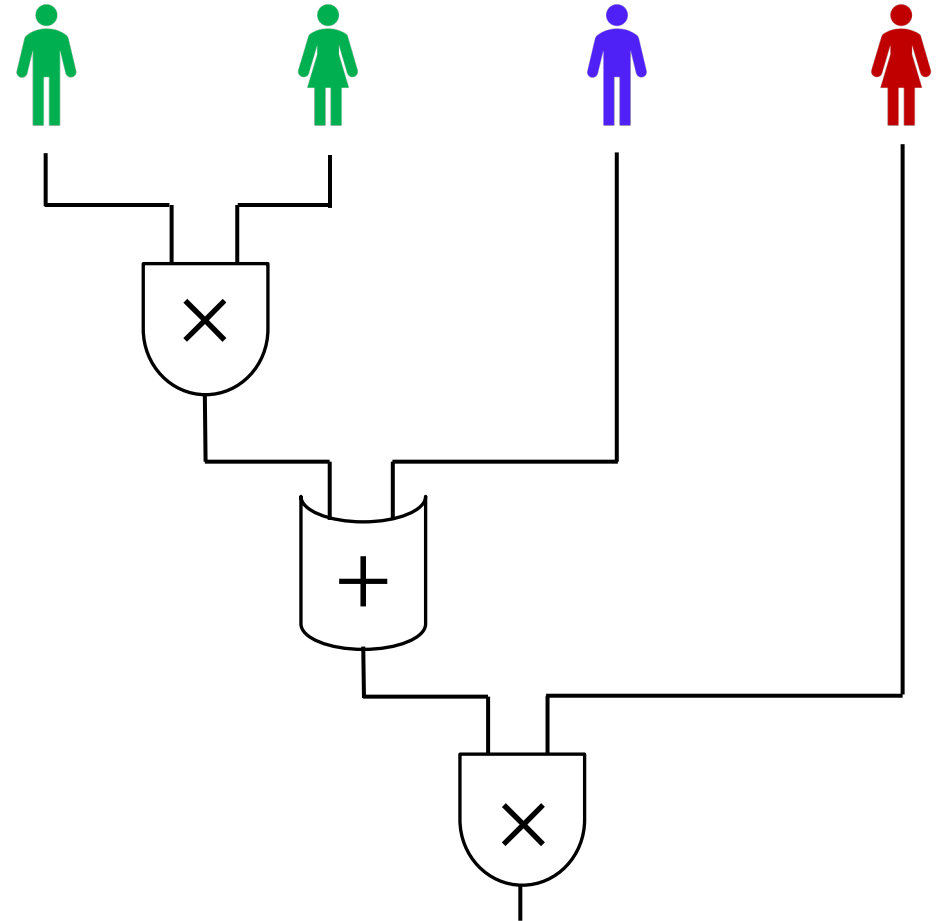
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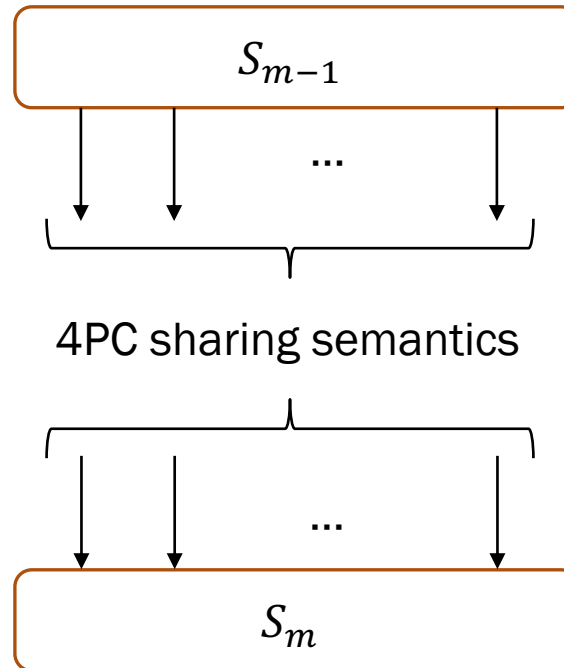
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Approach

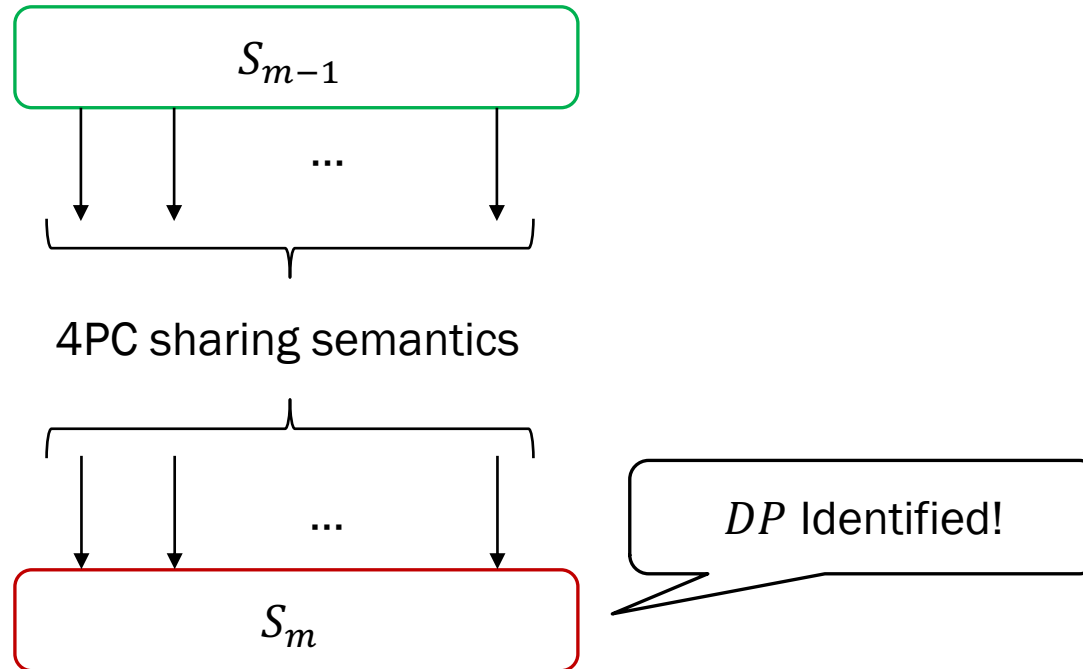
- Function expressed as a circuit
- Evaluated in a topological order
 - Input sharing
 - Evaluation
 - Output reconstruction
- High-level idea for sub-protocols
 - Completes successfully, OR
 - Identifies a dispute pair DP (includes corrupt party)
 - Run semi-honest 2PC (for GOD)
- Segmented evaluation to get GOD for free



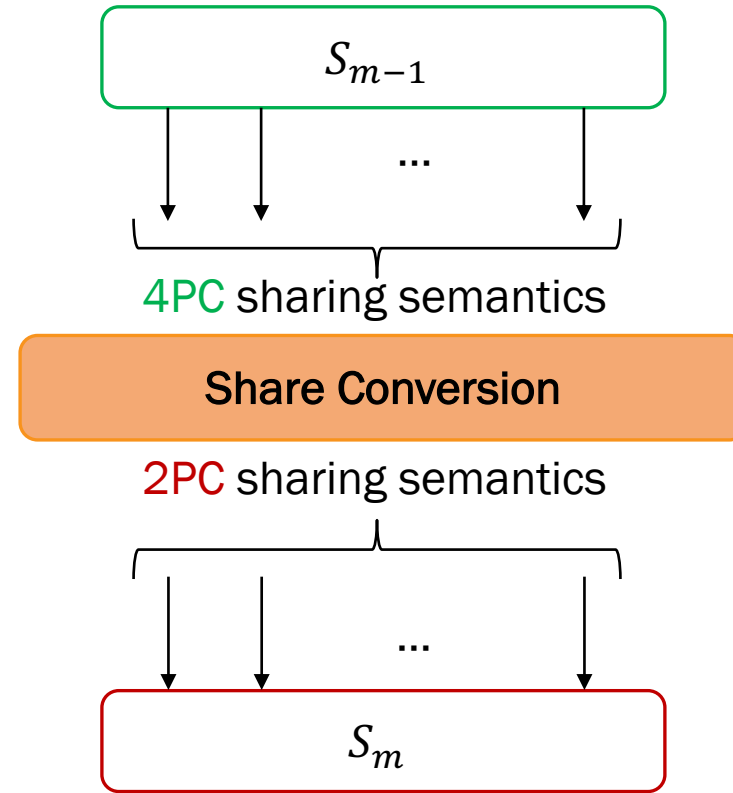
Fair to GOD: Segmentation



Fair to GOD: Segmentation



Fair to GOD: Segmentation



Sharing Semantics

(n, t) Replicated Secret Sharing (RSS)

- Total number of shares = $\binom{n}{t}$
- Shares per party = $\binom{n-1}{t}$

- QuadSquad

- $(4,2)$ RSS: Accounts for $t = 1, h^* = 1$
- $s = \langle s \rangle_{12} + \langle s \rangle_{13} + \langle s \rangle_{14} + \langle s \rangle_{23} + \langle s \rangle_{24} + \langle s \rangle_{34}$



$(\langle s \rangle_{12}, \langle s \rangle_{13}, \langle s \rangle_{14})$



$(\langle s \rangle_{12}, \langle s \rangle_{23}, \langle s \rangle_{24})$

- Contrast with H.M./D.M. Setting

- Honest Majority: $(4,1)$ -RSS \Rightarrow 4 shares per secret, High Redundancy
- Dishonest Majority: $(4,3)$ -RSS \Rightarrow 4 shares per secret, Low redundancy

Sharing Semantics



$(\beta_x, \langle \alpha_x \rangle_{12}, \langle \alpha_x \rangle_{23}, \langle \alpha_x \rangle_{24})$



$(\beta_x, \langle \alpha_x \rangle_{12}, \langle \alpha_x \rangle_{13}, \langle \alpha_x \rangle_{14})$



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$(\beta_x, \langle \alpha_x \rangle_{14}, \langle \alpha_x \rangle_{24}, \langle \alpha_x \rangle_{34})$

$[[\cdot]]$ -sharing of a value x :

- $\langle \cdot \rangle$ -sharing of random α_x
- Masked value $\beta_x = x + \alpha_x$

Can be viewed as $\langle \cdot \rangle$ -sharing of x :

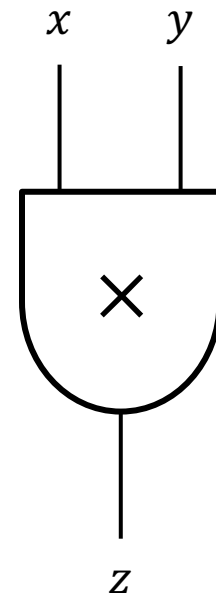
$$x = \beta_x - \alpha_x$$
$$\langle x \rangle = \beta_x - \langle \alpha_x \rangle$$

Multiplication

- Given $\llbracket x \rrbracket = (\beta_x, \langle \alpha_x \rangle)$ and $\llbracket y \rrbracket = (\beta_y, \langle \alpha_y \rangle)$
- Compute $\llbracket z \rrbracket = (\beta_z, \langle \alpha_z \rangle)$

$$\begin{aligned}\beta_z &= z + \alpha_z \\ &= xy + \alpha_z \\ &= (\beta_x - \alpha_x)(\beta_y - \alpha_y) + \alpha_z \\ &= \beta_x\beta_y - \beta_x\alpha_y - \beta_y\alpha_x + \alpha_x\alpha_y + \alpha_z\end{aligned}$$

- Can be reduced to 1 $\langle \cdot \rangle$ -reconstruction (online)

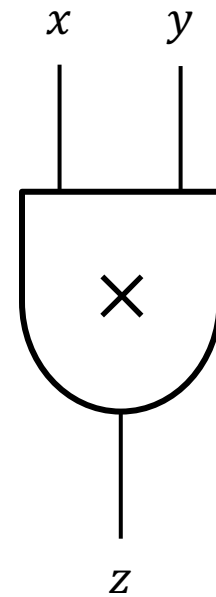


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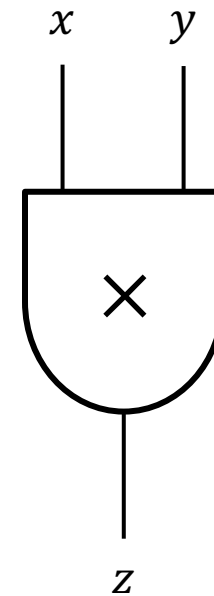


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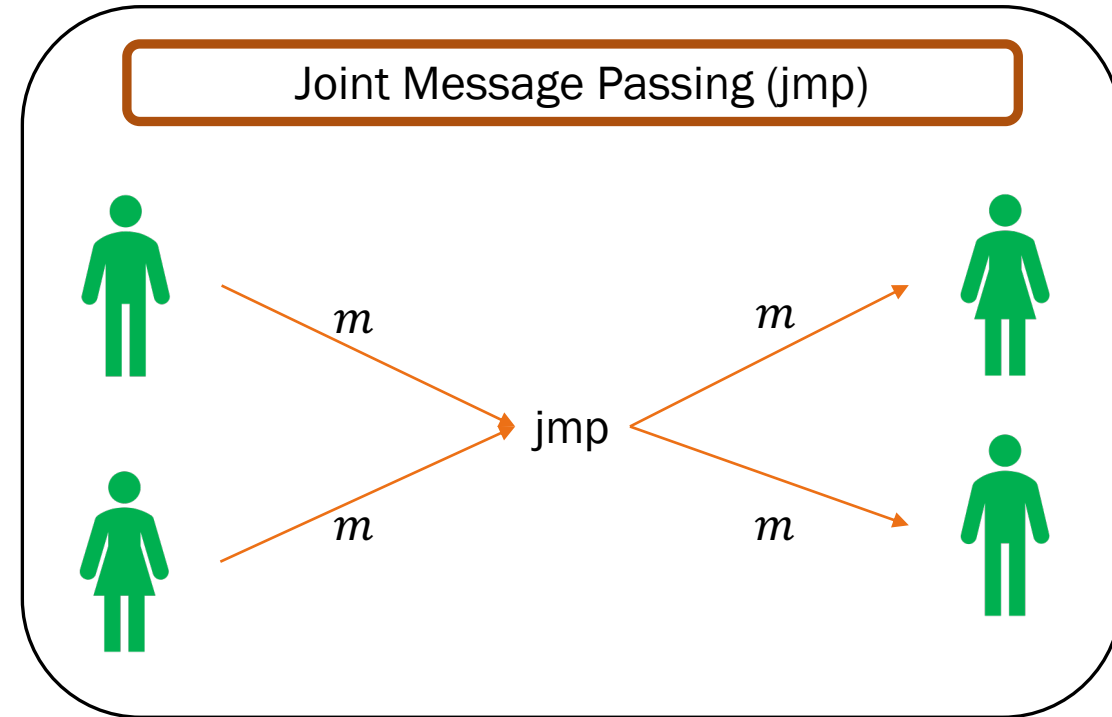
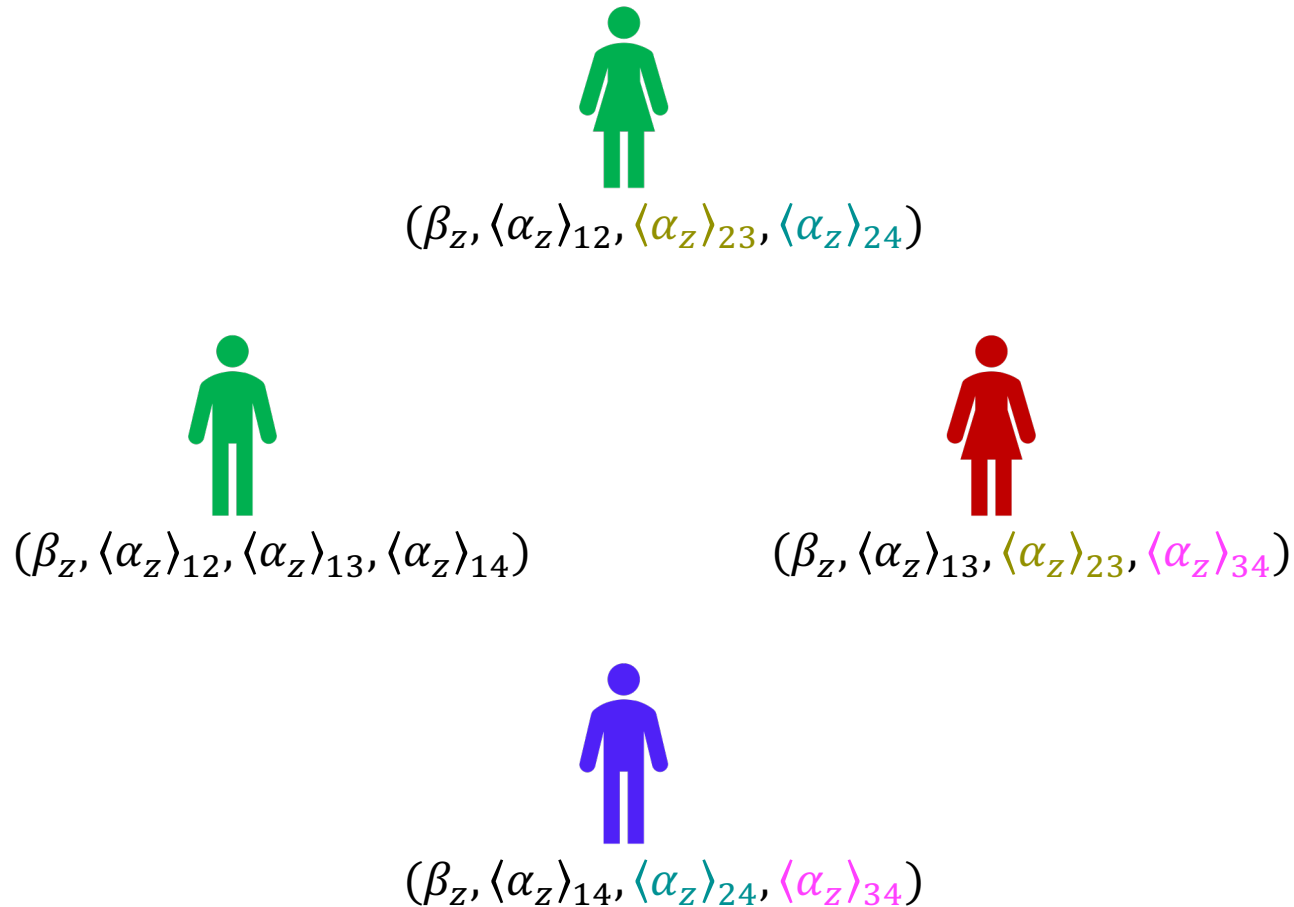
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- Can be reduced to 1 $\langle \cdot \rangle$ -reconstruction (online)
- Reduced to obtaining $\langle \alpha_x \alpha_y \rangle$ from $\langle \alpha_x \rangle$ and $\langle \alpha_y \rangle$ (preprocessing)



Reconstruction Phase



Reconstruction Phase



$(\beta_z, \langle \alpha_z \rangle_{12}, \langle \alpha_z \rangle_{23}, \langle \alpha_z \rangle_{24})$



$(\beta_z, \langle \alpha_z \rangle_{12}, \langle \alpha_z \rangle_{13}, \langle \alpha_z \rangle_{14})$



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Online:

- P_2, P_3 jmp-send $\langle \alpha_z \rangle_{23}$
- P_2, P_4 jmp-send $\langle \alpha_z \rangle_{24}$
- P_3, P_4 jmp-send $\langle \alpha_z \rangle_{34}$

Communication: 3 elements

Reconstruction towards all: 12 elements

Optimized reconstruction: 7 elements

Triple Generation

$$\alpha_x \alpha_y = \sum_{1 \leq i < j \leq 4} \langle \alpha_x \rangle_{ij} \cdot \sum_{1 \leq k < m \leq 4} \langle \alpha_y \rangle_{km} = \sum \langle \alpha_x \rangle_{ij} \langle \alpha_y \rangle_{ij} + \sum \langle \alpha_x \rangle_{ij} \langle \alpha_y \rangle_{ik} + \sum \langle \alpha_x \rangle_{ij} \langle \alpha_y \rangle_{km}$$

	$\langle \alpha_x \rangle_{12}$	$\langle \alpha_x \rangle_{13}$	$\langle \alpha_x \rangle_{14}$	$\langle \alpha_x \rangle_{23}$	$\langle \alpha_x \rangle_{24}$	$\langle \alpha_x \rangle_{34}$
$\langle \alpha_y \rangle_{12}$	S_2	S_1	S_1	S_1	S_1	S_0
$\langle \alpha_y \rangle_{13}$	S_1	S_2	S_1	S_1	S_0	S_1
$\langle \alpha_y \rangle_{14}$	S_1	S_1	S_2	S_0	S_1	S_1
$\langle \alpha_y \rangle_{23}$	S_1	S_1	S_0	S_2	S_1	S_1
$\langle \alpha_y \rangle_{24}$	S_1	S_0	S_1	S_1	S_2	S_1
$\langle \alpha_y \rangle_{34}$	S_0	S_1	S_1	S_1	S_1	S_2

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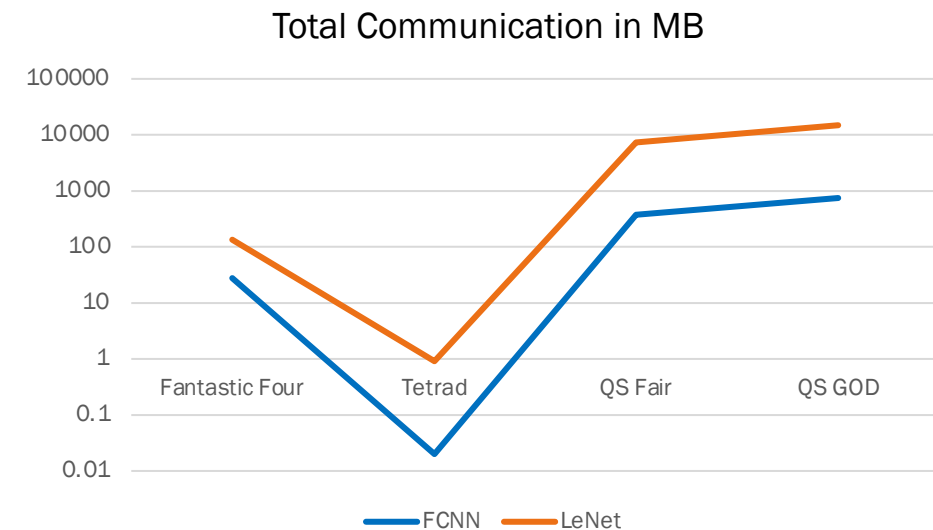
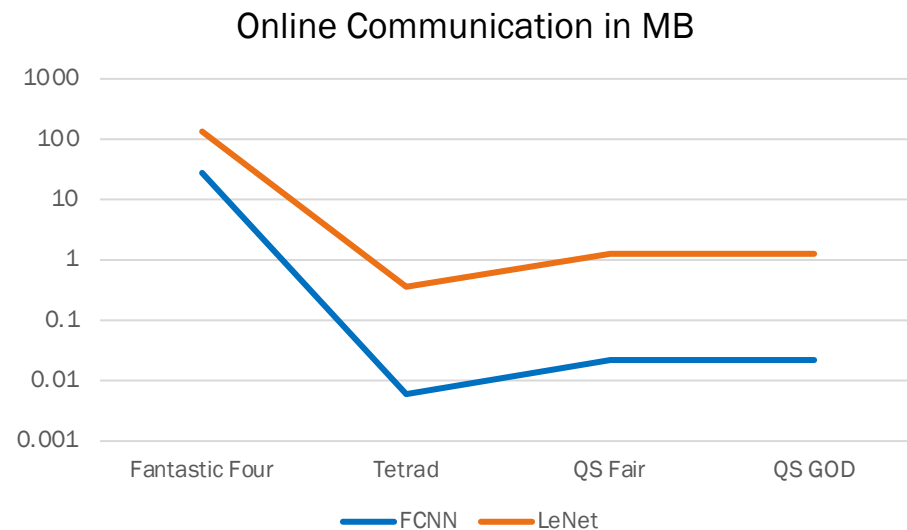
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PPML Benchmarks

- Neural Network inference over MNIST dataset
- Benchmarking over WAN instantiated using Google Cloud
- Code available at: <https://github.com/cris-iisc/quadsquad>



Thank You!