

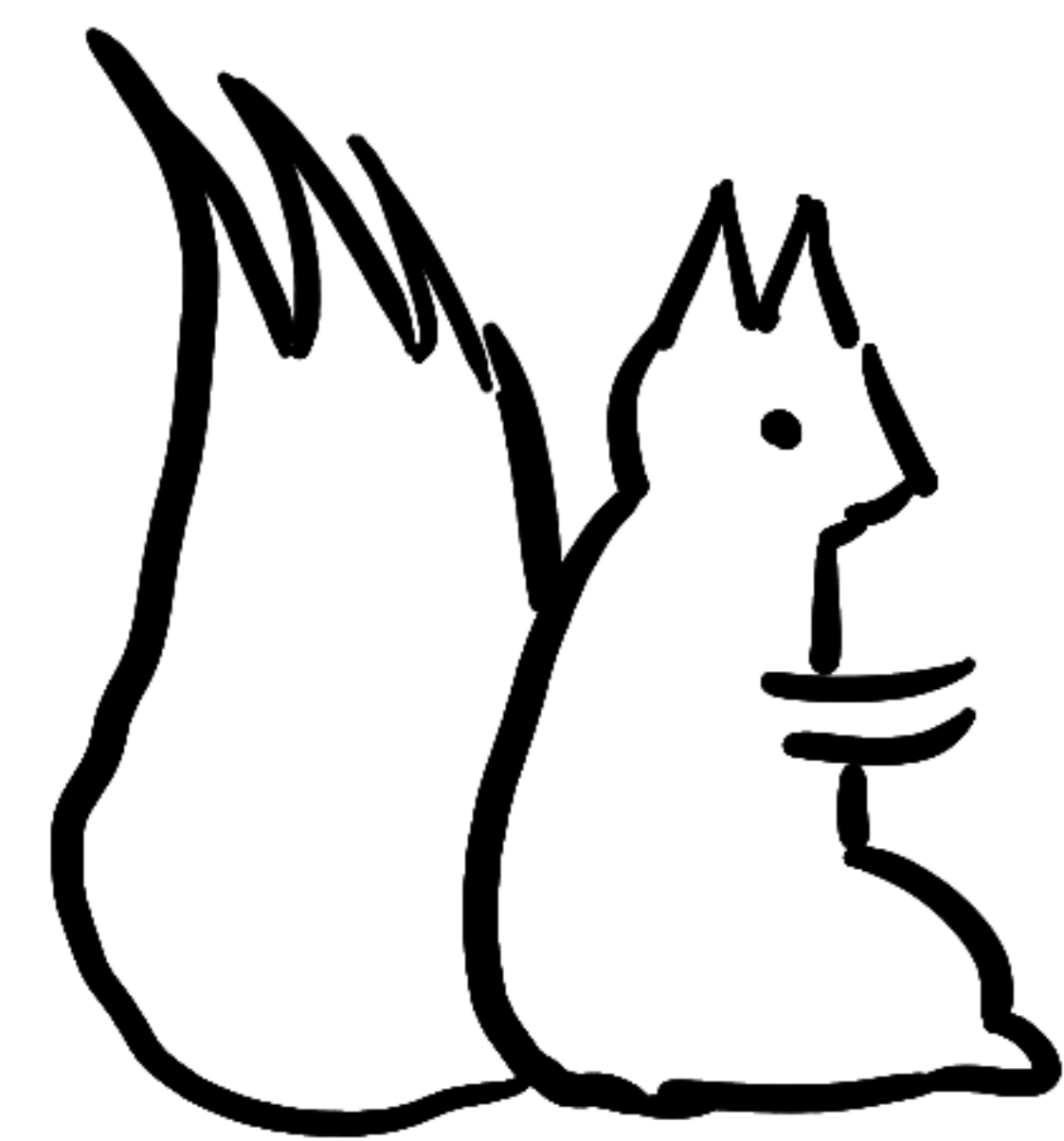
The Abe - Okamoto Partially Blind Signature Scheme Revisited

Julia Kastner
ETH Zürich
Switzerland

Julian Loss
CISPA
Germany

Jiayu Xu
Oregon State University
USA

Partially Blind Signatures [AF96]



sk

e.g. 1\$, "best before 24. 12."

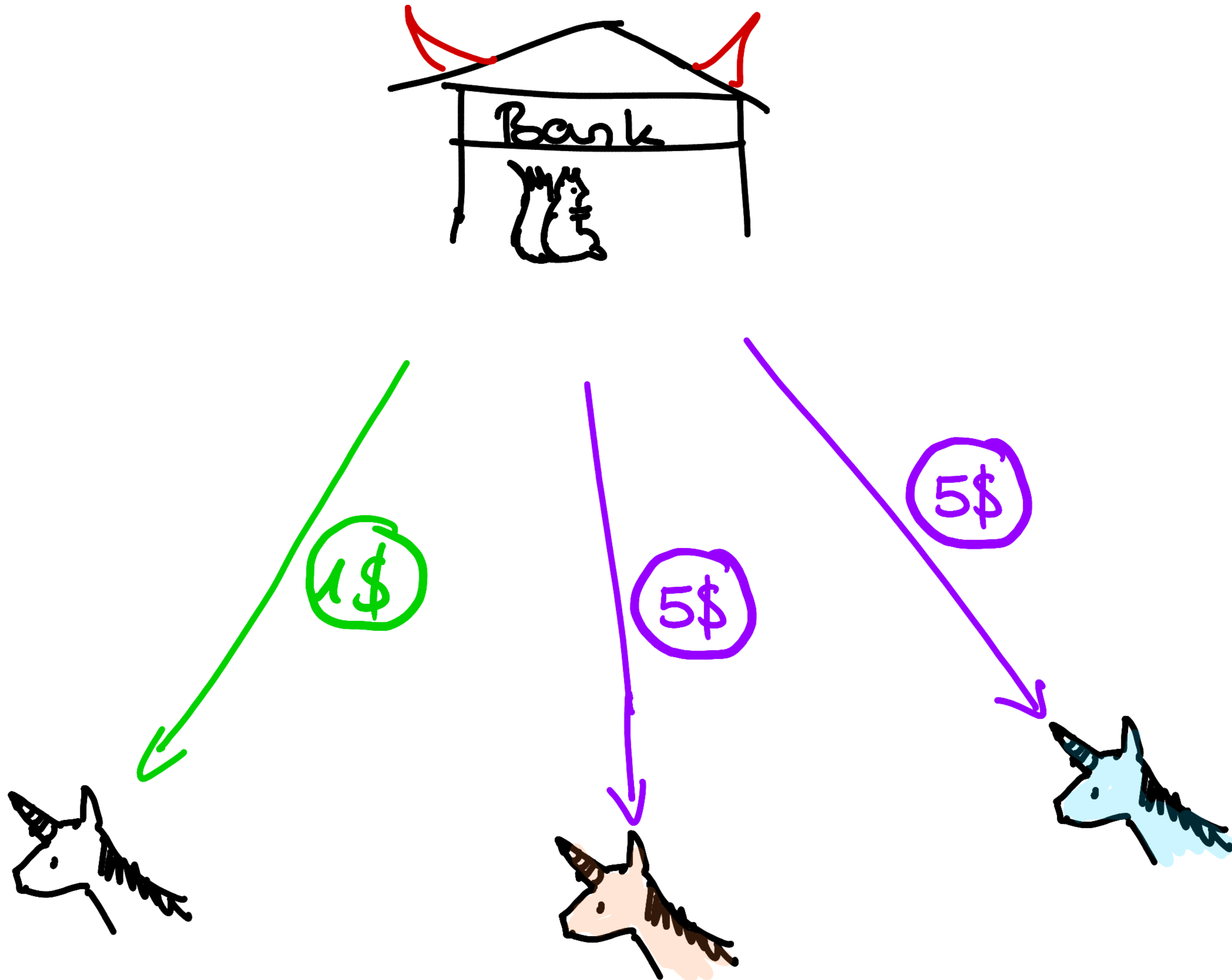
info



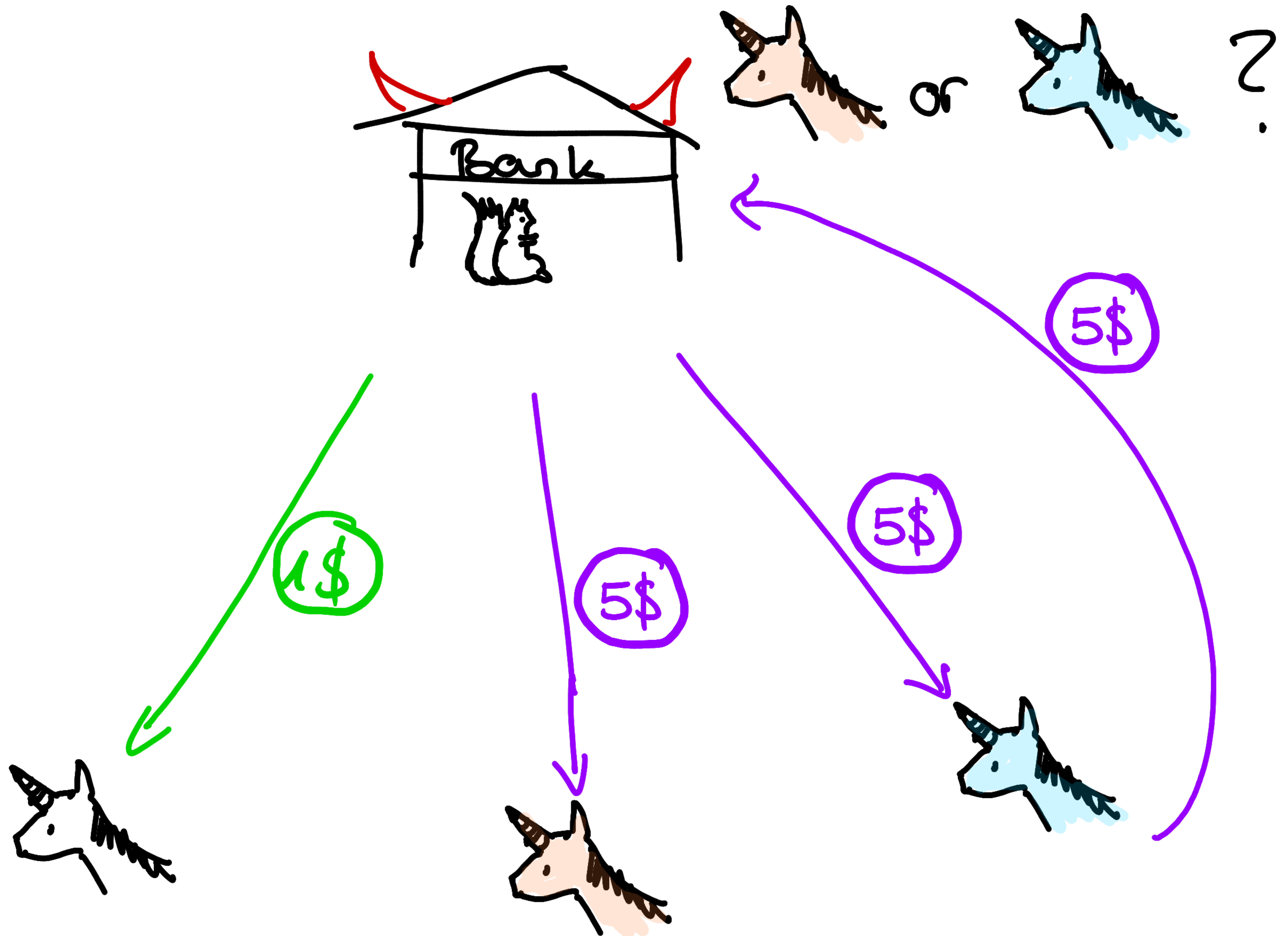
pk, m



Electronic Cash



Electronic Cash



Partial Blindness



pk, mo, mx, info



Partial Blindness



$p_k, m_0, m_x, \text{info}$



b $1-b$

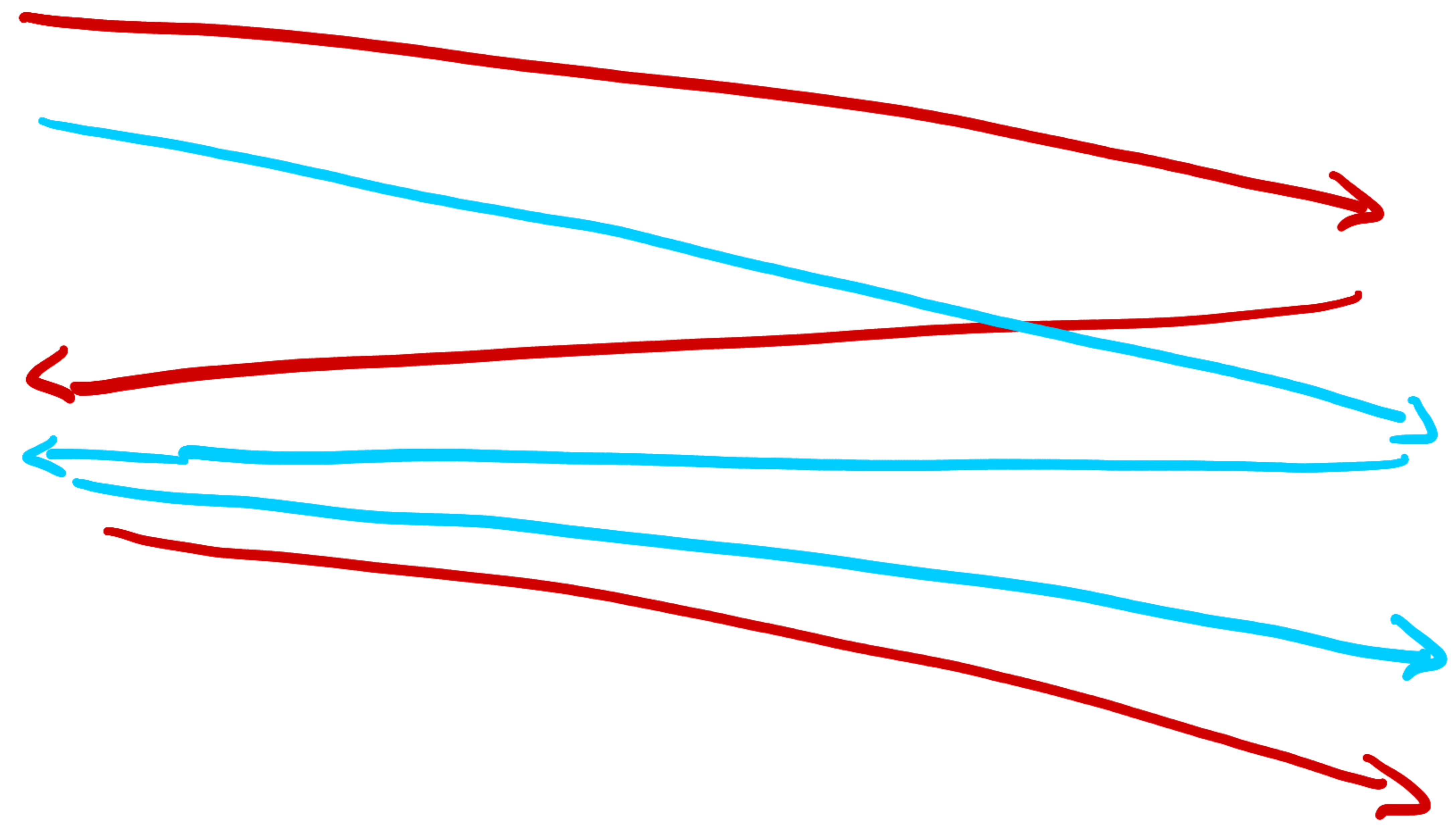
Partial Blindness



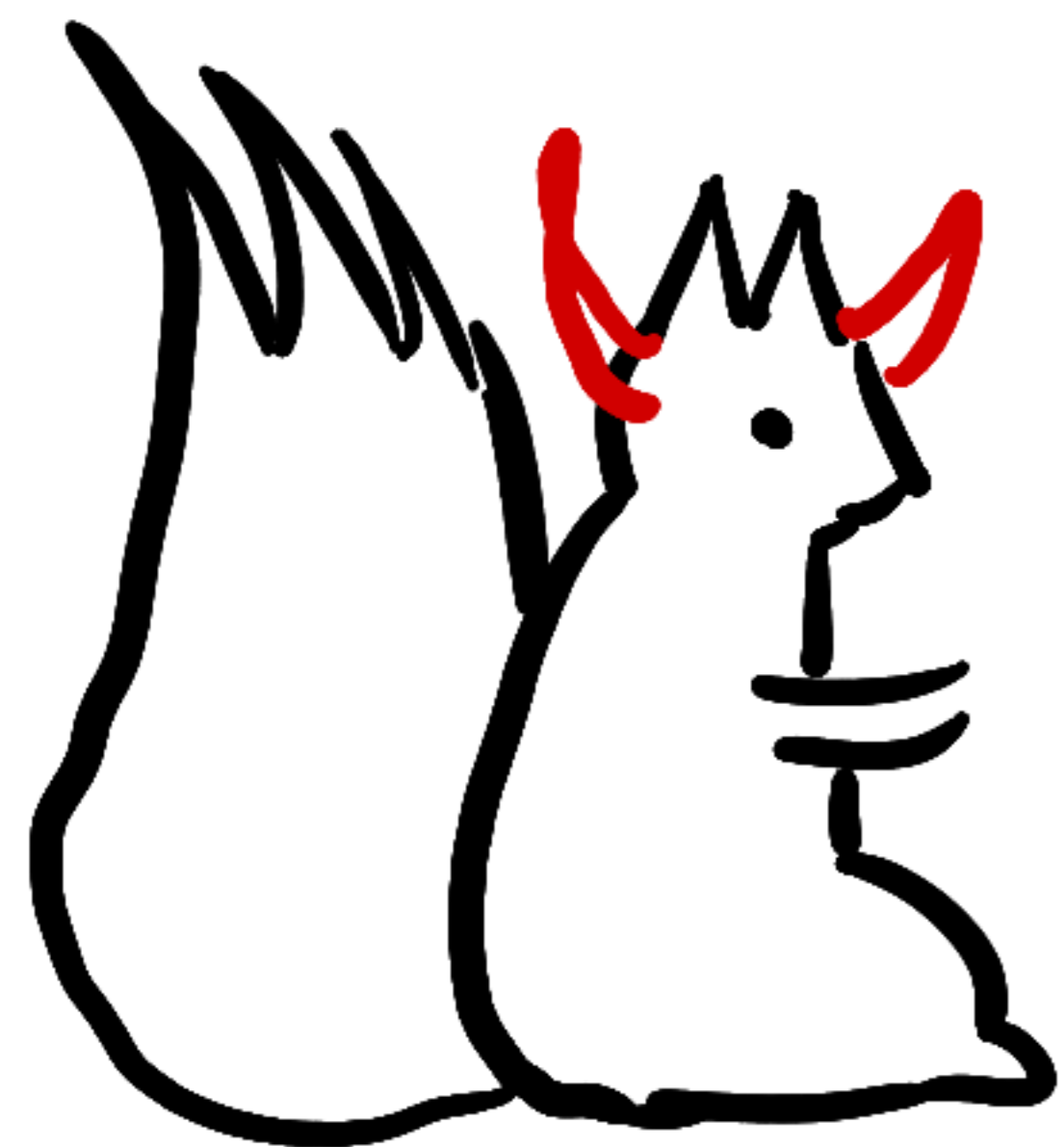
$p_k, m_0, m_x, \text{info}$



b $1-b$



Partial Blindness

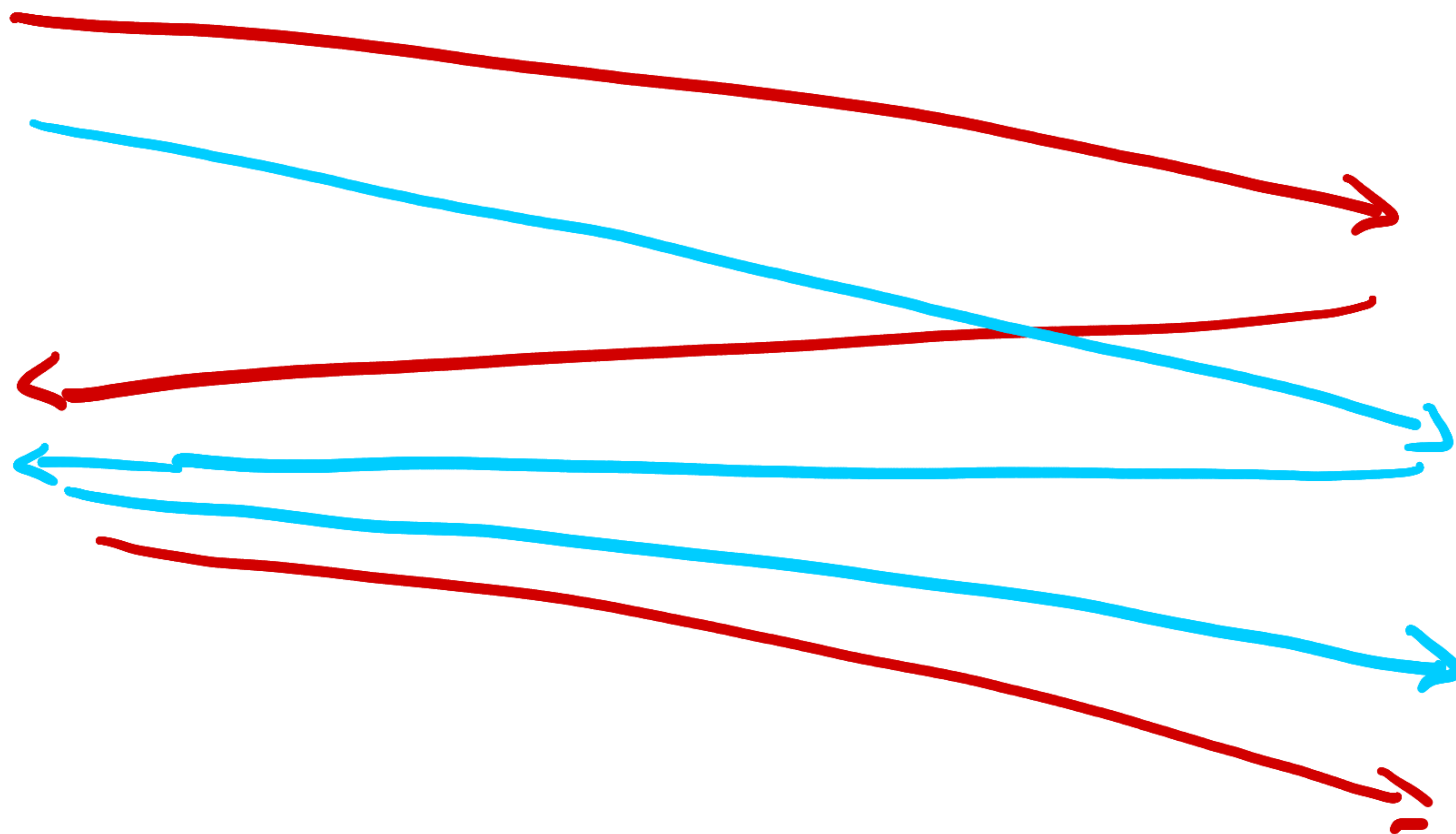


$p_k, m_0, m_1, \text{info}$



b

$1-b$



(m_0, σ_0)
 (m_1, σ_1)

or \perp

Partial Blindness

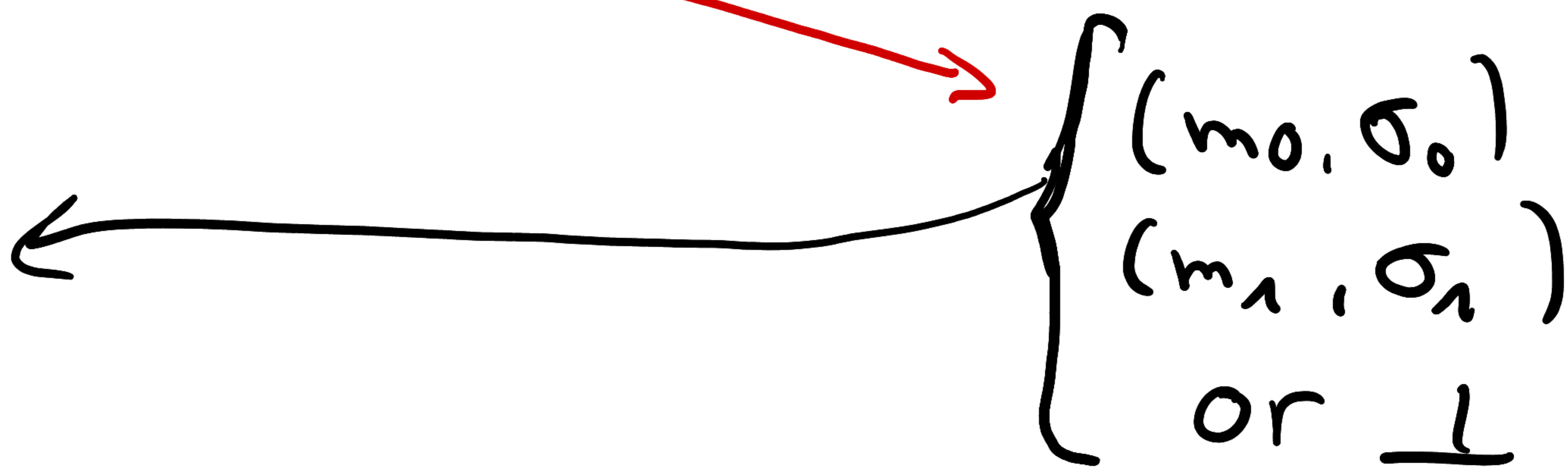
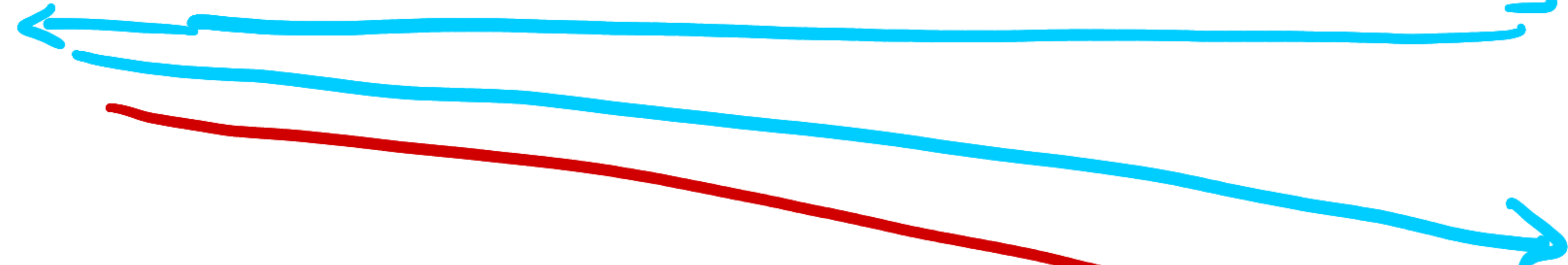
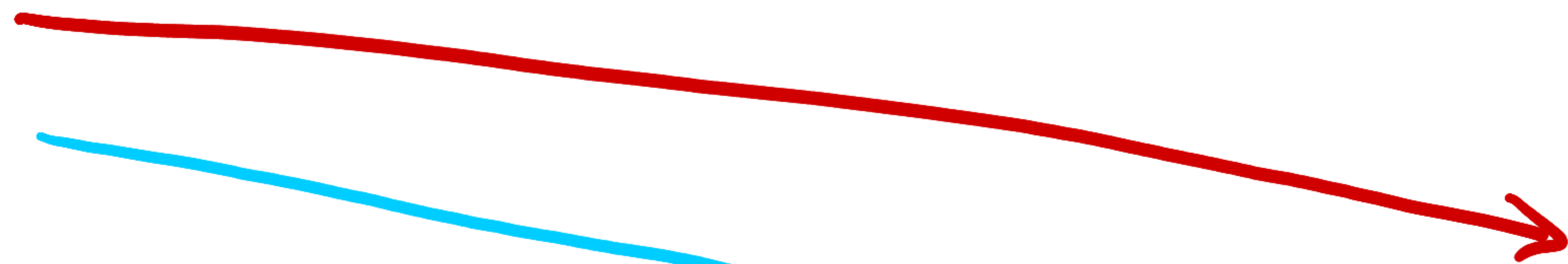


$p_k, m_0, m_1, \text{info}$



b

$1-b$



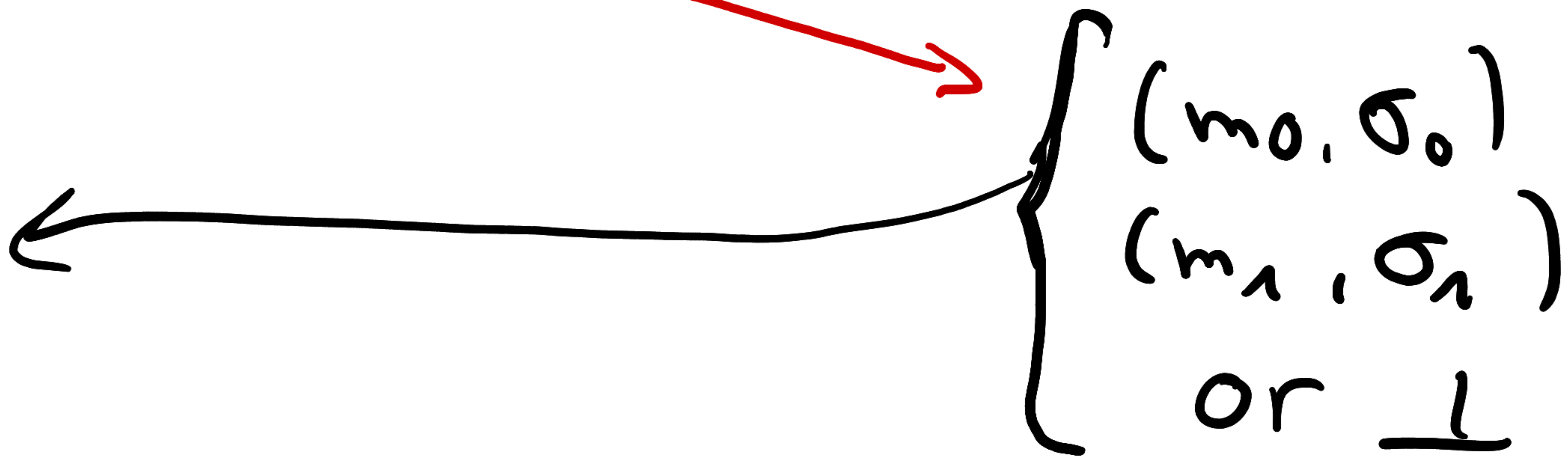
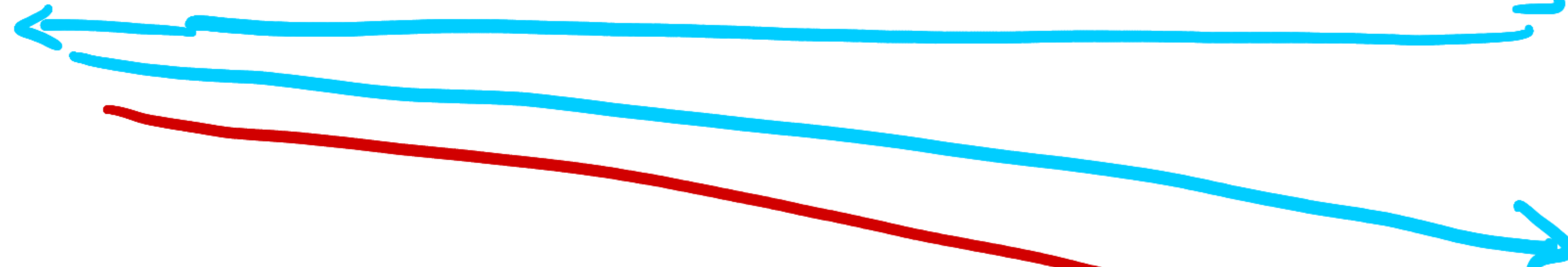
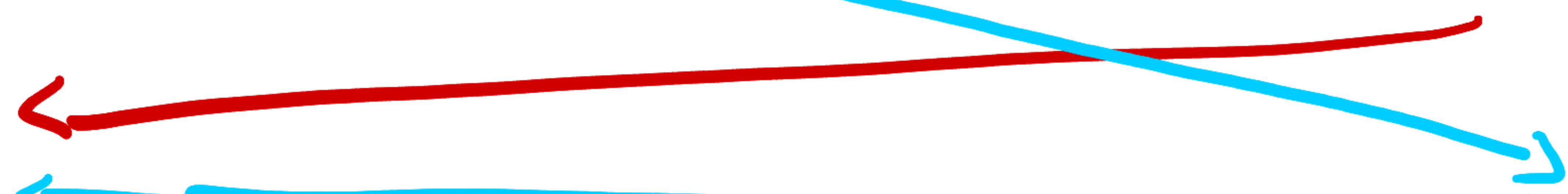
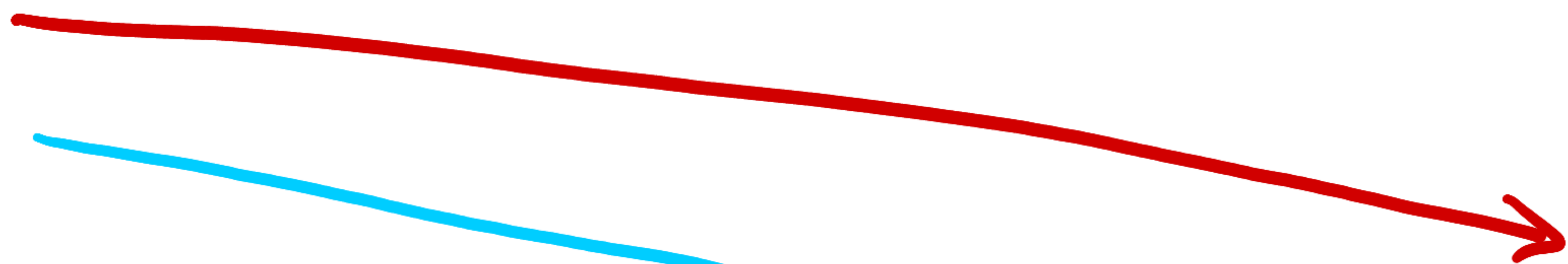
Partial Blindness



$p_k, m_0, m_1, \text{info}$

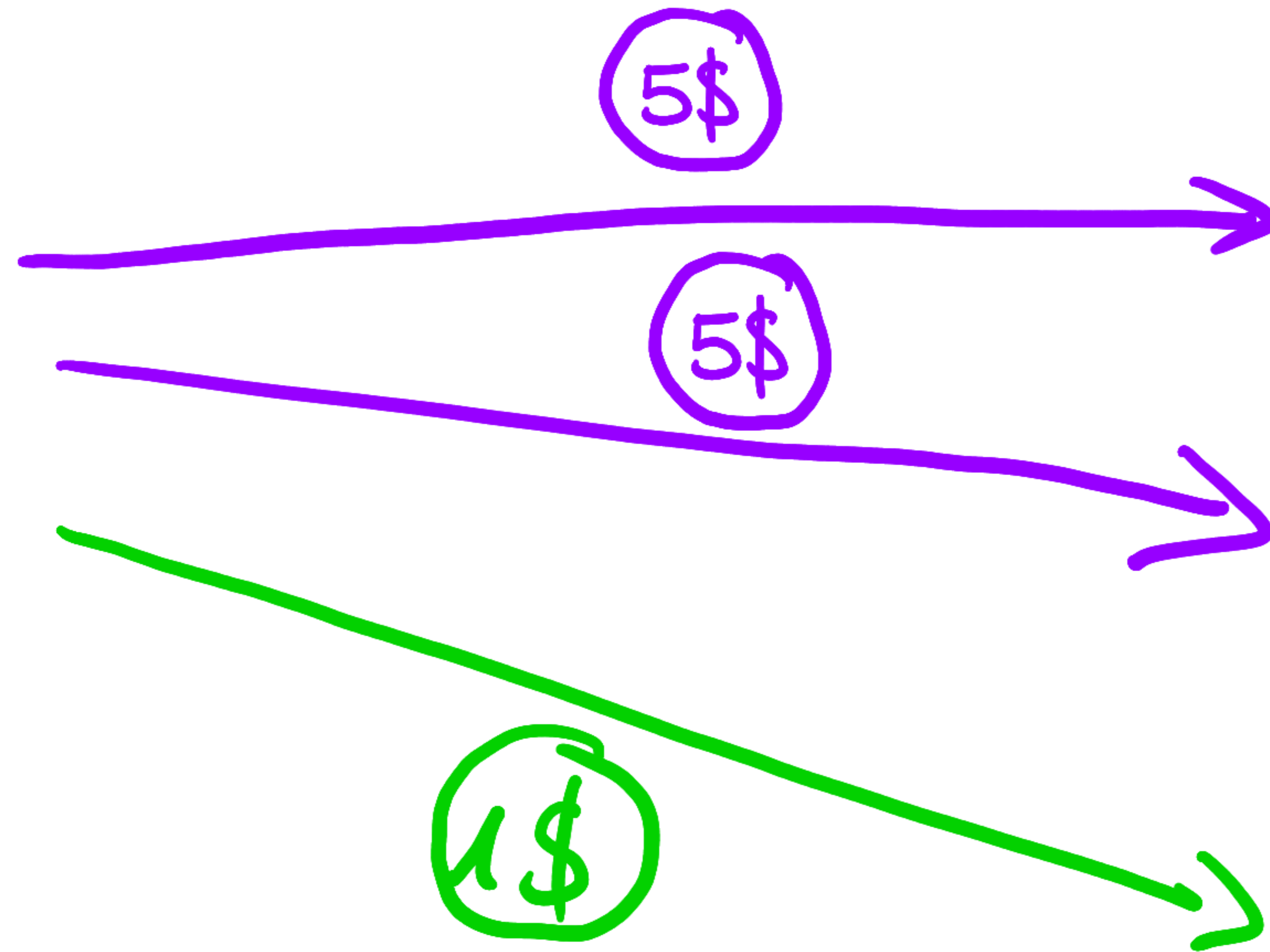


b $1-b$

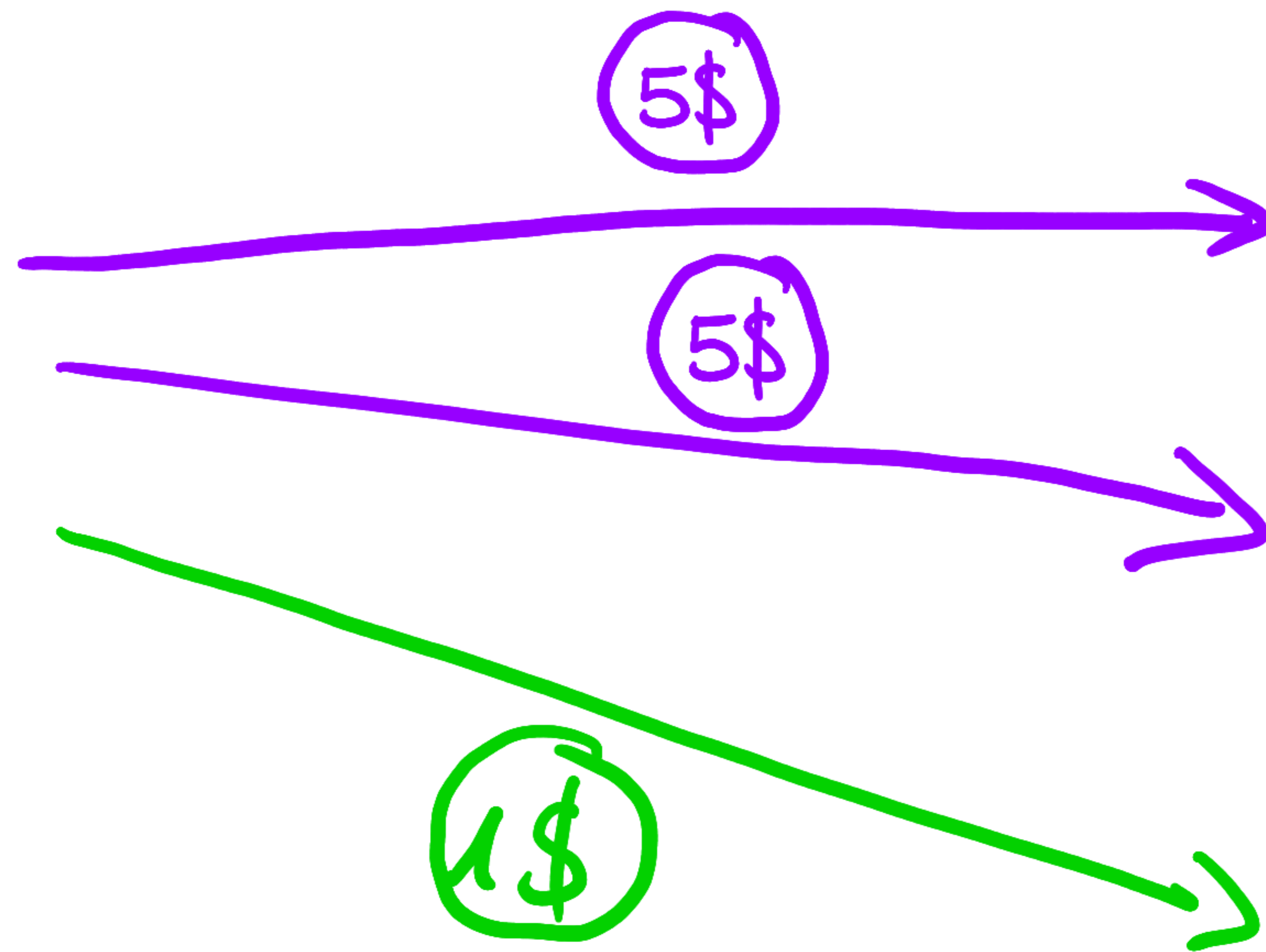


m_0 m_1
or m_0 m_1 ?

Electronic Cash



Electronic Cash



One-more Unforgeability



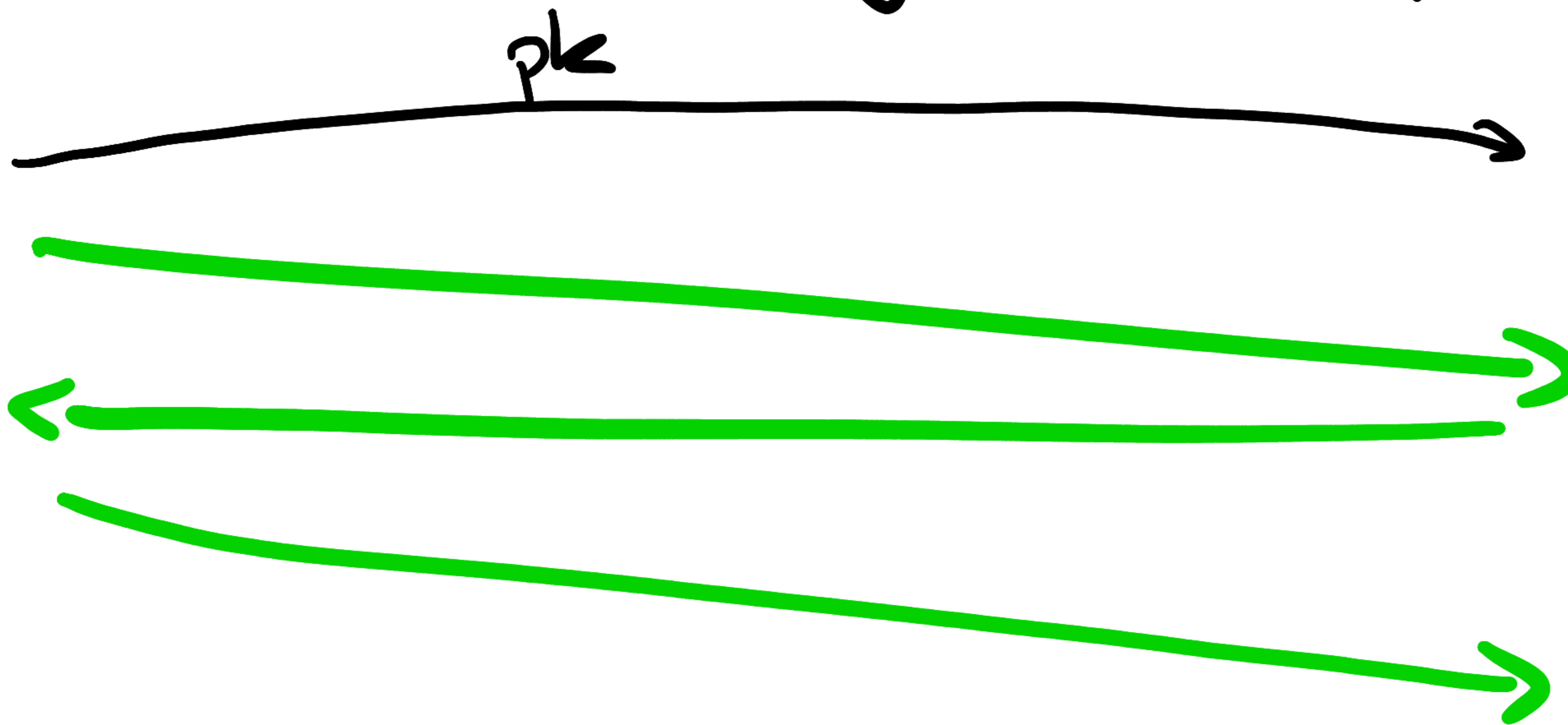
sk



One-more Unforgeability



sk

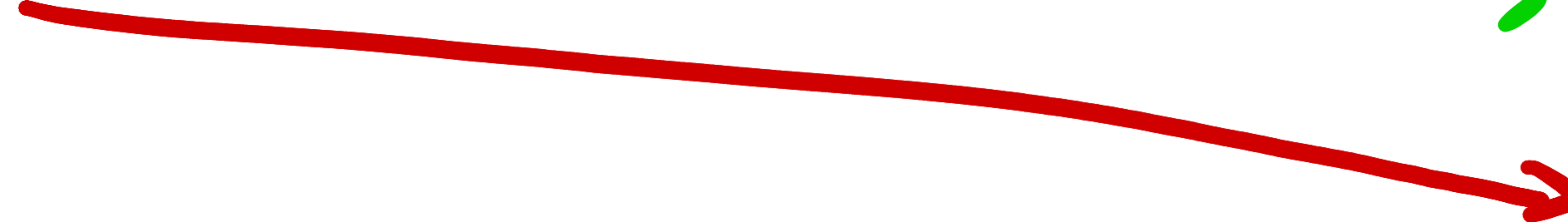
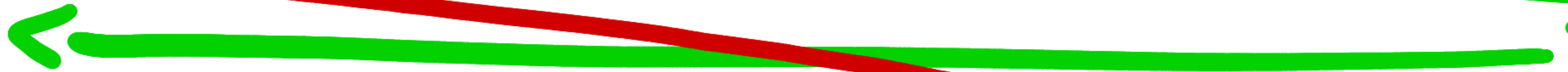
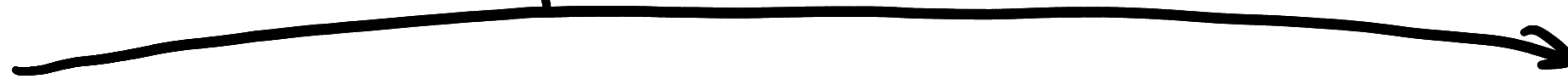


One-more Unforgeability



Sk

pk

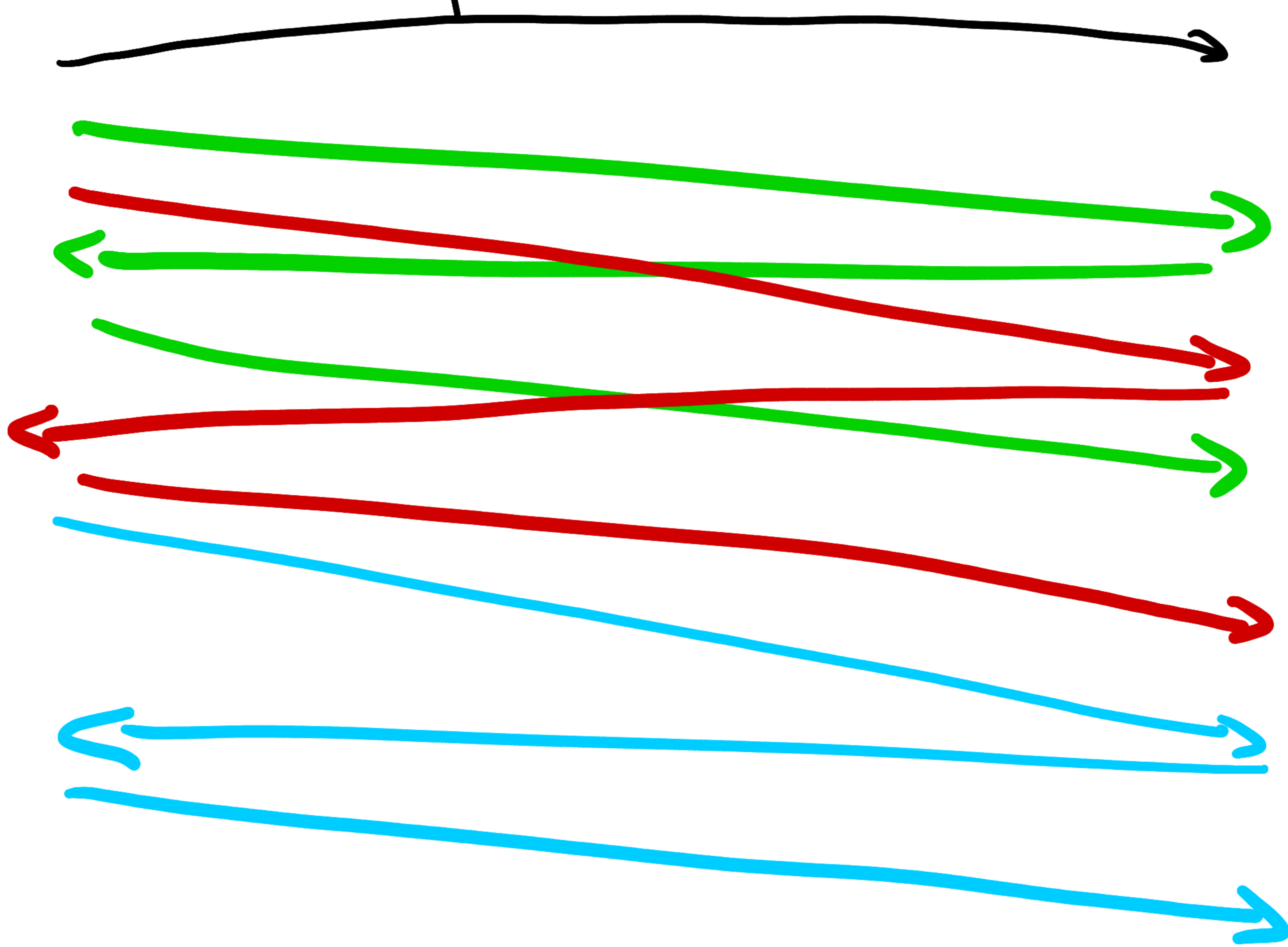


One-more Unforgeability



S_k

pk



One-more Unforgeability

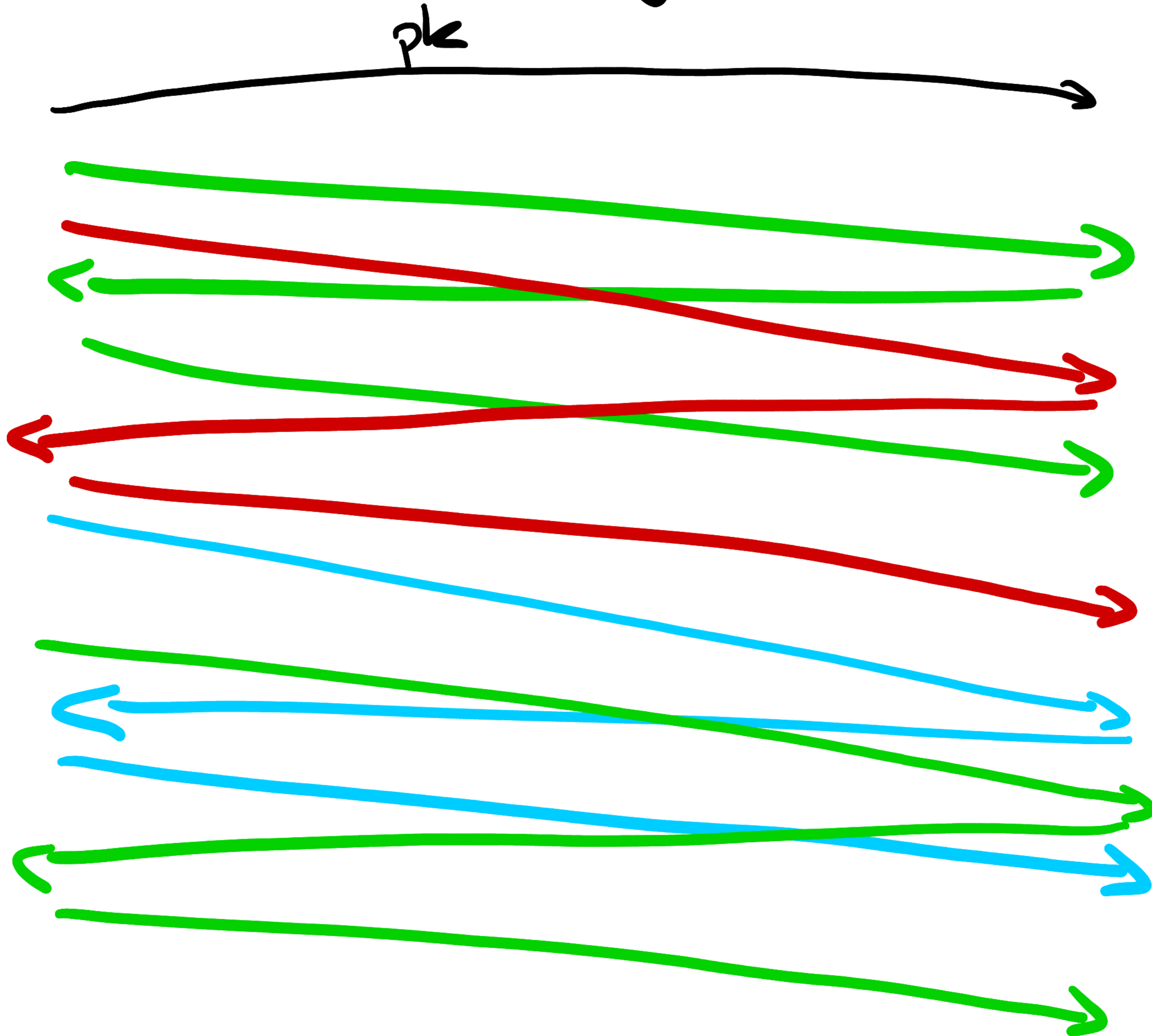


Sk

pk



Q

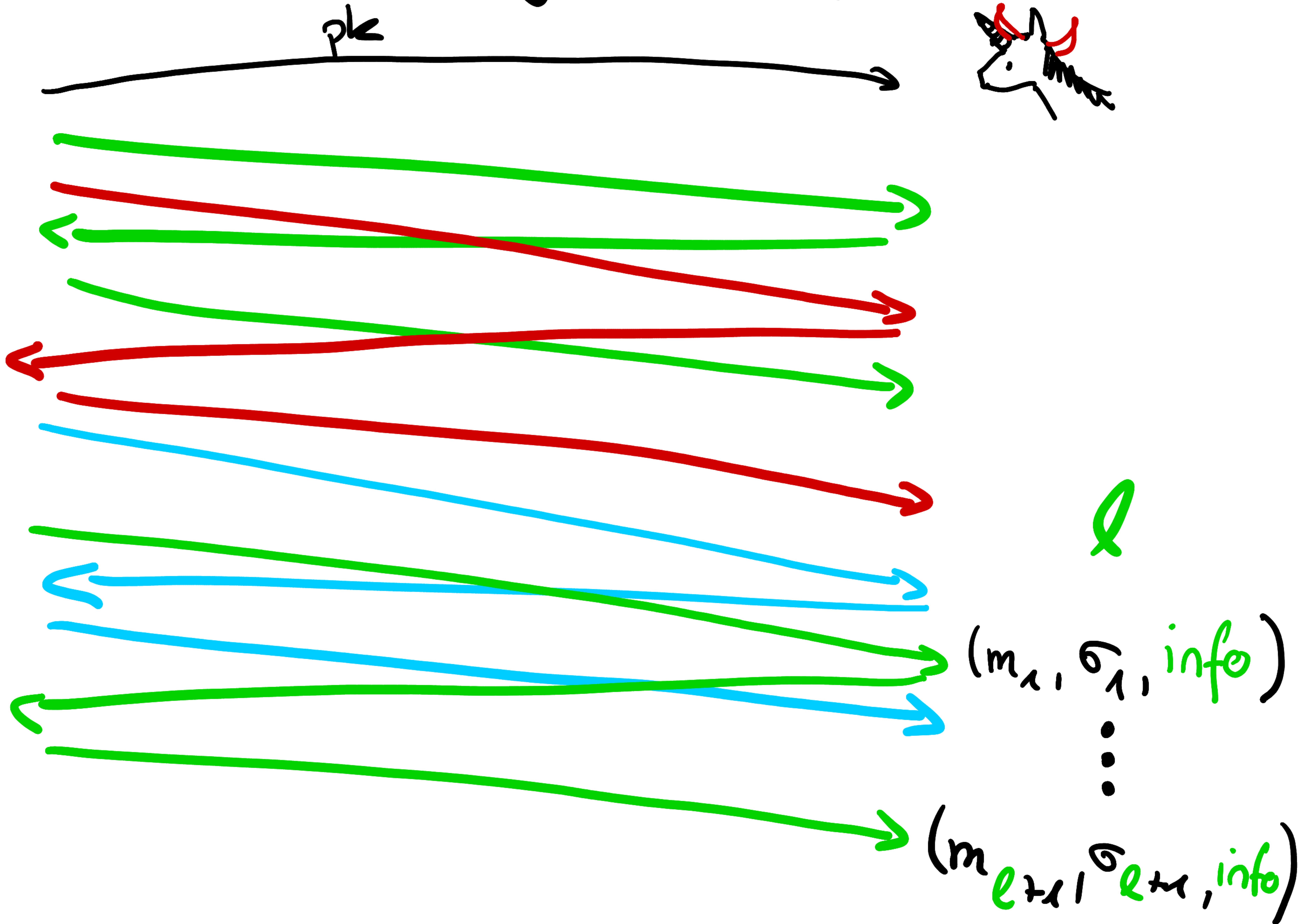


One-more Unforgeability



S_k





pk




Motivation


- [AO'00] efficient DL-based PBS
- inspiration for several other schemes
eg. [Abe 01], [BL13], [AHJ21]
- Proof strategy of interest for other similar schemes

Our Contribution

- identify gap  in original
- mend gap   OMUF proof 
- achieve similar bounds to original work

The Abe-Okamoto Scheme [AO 00]

 $sk = x$
 $z = H^*(info)$ e.g. $(1\$)$

$pk = g^x = y$
 $z = H^*(info)$


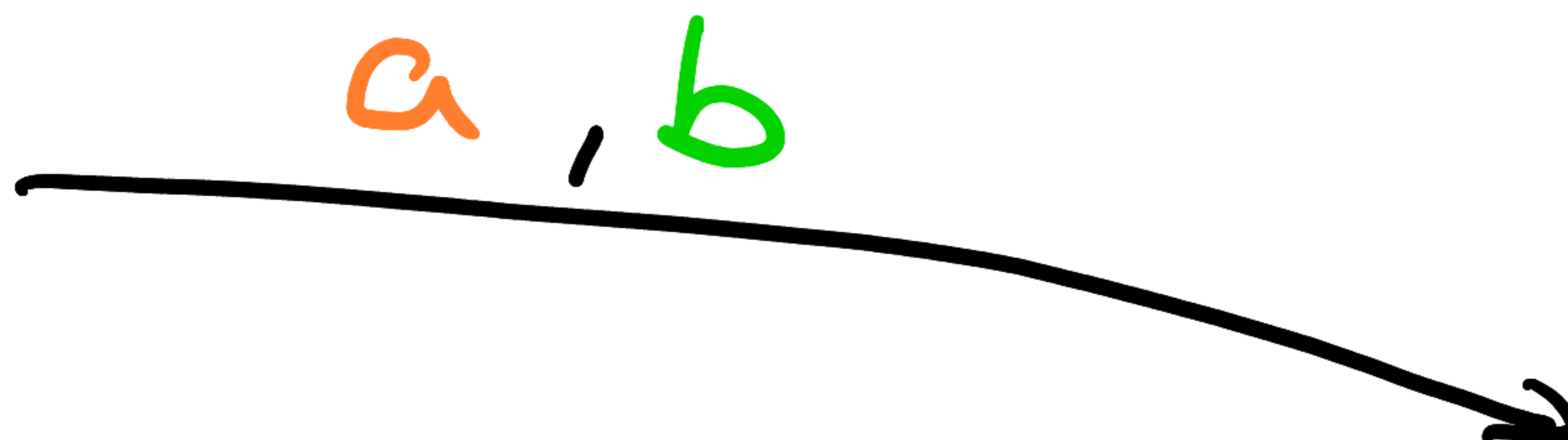
The Abe-Okamoto Scheme [AO 00]



$$sk = x$$

$$z = H^*(info)$$

a, b



a, b



$$pk = g^x = y$$

$$z = H^*(info)$$

The Abe-Okamoto Scheme [AO 00]



$$sk = x$$

$$z = H^*(info)$$

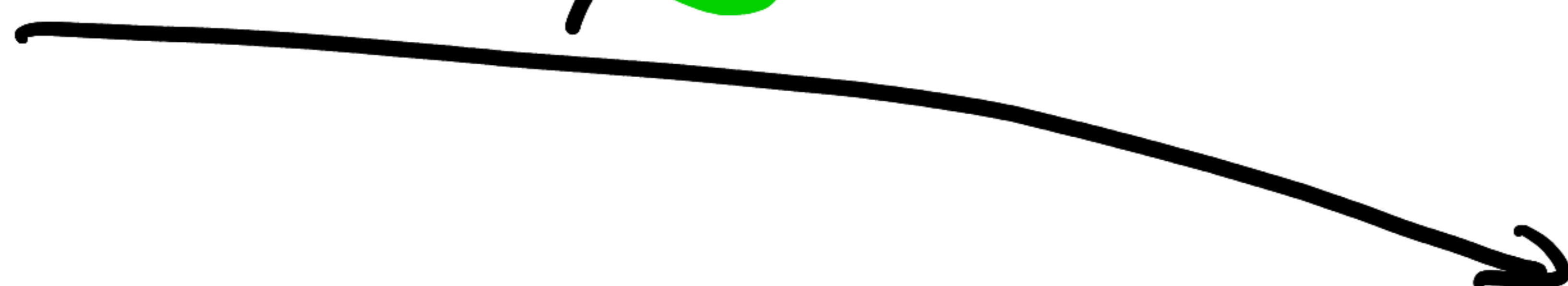


$$pk = g^x = y$$

$$z = H^*(info)$$

a, b

a, b



$a \rightsquigarrow \alpha$

$b \rightsquigarrow \beta$

$e \rightsquigarrow H(\alpha, \beta, m, info)$



The Abe-Okamoto Scheme [AO 00]



$$sk = x$$

$$z = H^*(info)$$



$$pk = g^x = y$$

$$z = H^*(info)$$

a, b

a, b



$$a \rightsquigarrow \alpha$$

$$b \rightsquigarrow \beta$$

$$e \rightsquigarrow H(\alpha, \beta, m, info)$$



c, r, d, s



$$c, r \rightsquigarrow \omega, \rho$$

$$d, s \rightsquigarrow \delta, \sigma$$

The Abe-Okamoto Scheme [AO 00]



$$sk = x$$

$$z = H^*(info)$$

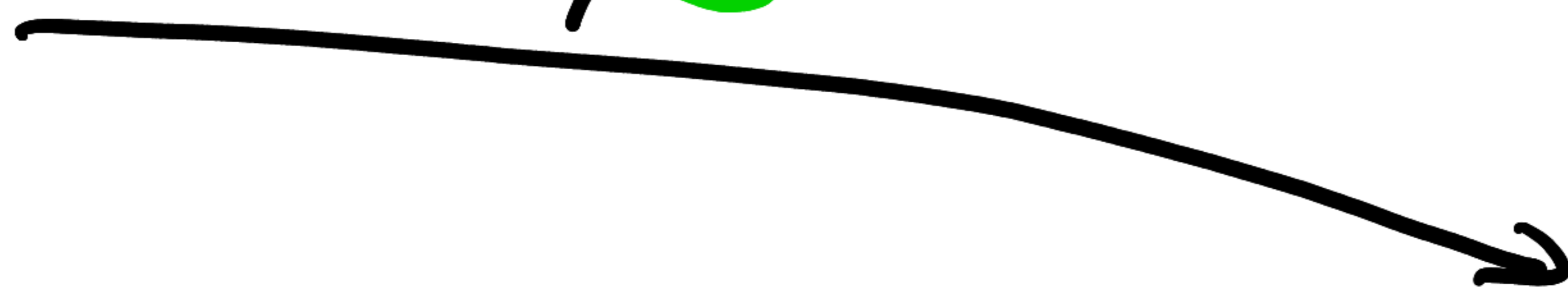


$$pk = g^x = y$$

$$z = H^*(info)$$

a, b

a, b



$$a \rightsquigarrow \alpha$$

$$b \rightsquigarrow \beta$$

$$e \rightsquigarrow H(\alpha, \beta, m, info)$$



c, r, d, s



$$c, r \rightsquigarrow \omega, \rho$$

$$d, s \rightsquigarrow \delta, \sigma$$

$$sig = (\omega, \rho, \delta, \sigma)$$

Verification

$$w + \delta \stackrel{?}{=} H(\gamma^w \cdot g^p, z^\delta \cdot g^q, m, \text{info})$$

"OR-Proof of two Schnorr-Signatures"

Proving One-more Unforgeability

Idea:

Simulate using x , extract $d \log z$

OR

Simulate using $d \log z$, extract x

Reduction strategy

1. Pick "secret key" x or $d \log z$

Reduction strategy

1. Pick "secret key" x or $d \log z$

2. Run adversary once

Reduction strategy

1. Pick "secret key" x or $d \log z$
2. Run adversary once
3. Re-program D_0

Reduction strategy

1. Pick "secret key" x or $d \log z$
2. Run adversary once
3. Re-program \mathcal{E}
4. Run adversary another time


Reduction strategy

1. Pick "secret key" x or $d \log z$
2. Run adversary once
3. Re-program \mathcal{E}
4. Run adversary another time
5. Hope to get "other key"

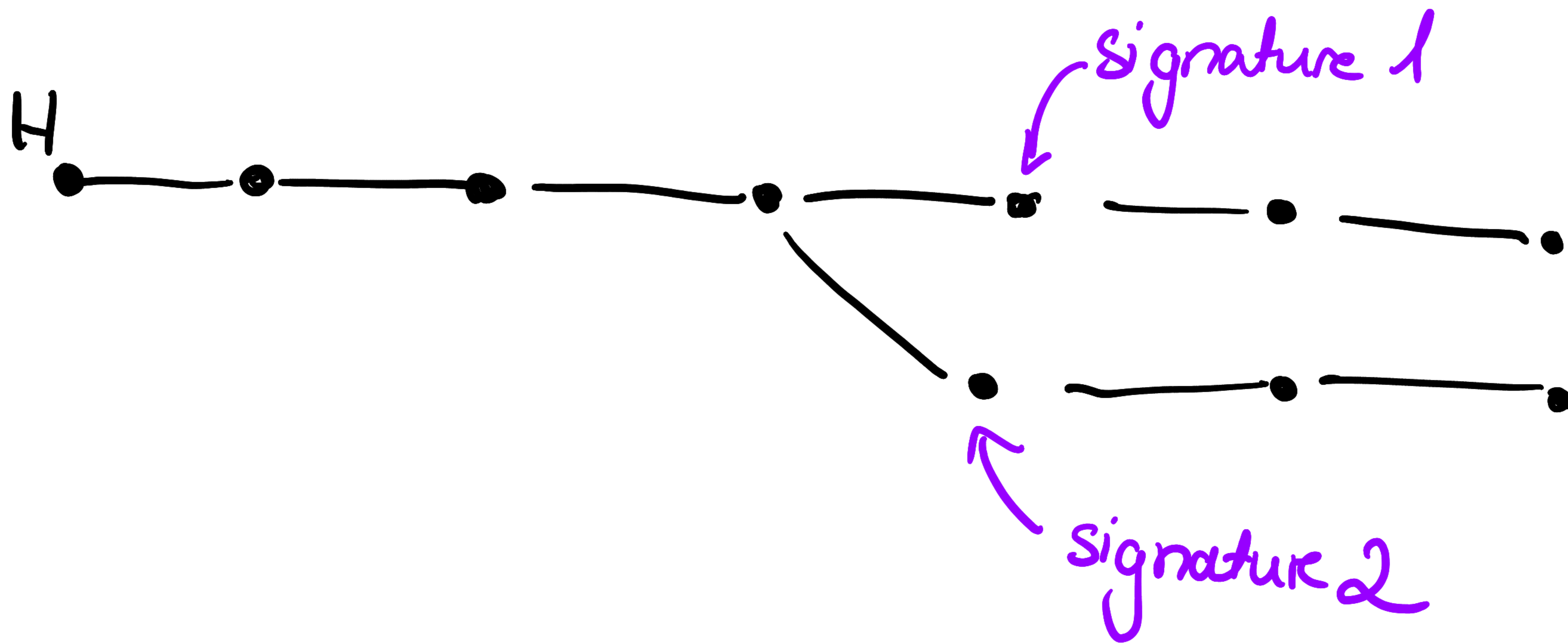
Reduction strategy

1. Pick "secret key" x or $d \log z$
2. Run adversary once
3. Re-program \mathcal{D}
4. Run adversary another time
5. Hope to get "other key"
6. Return "other key" as solution to DL

Reduction strategy

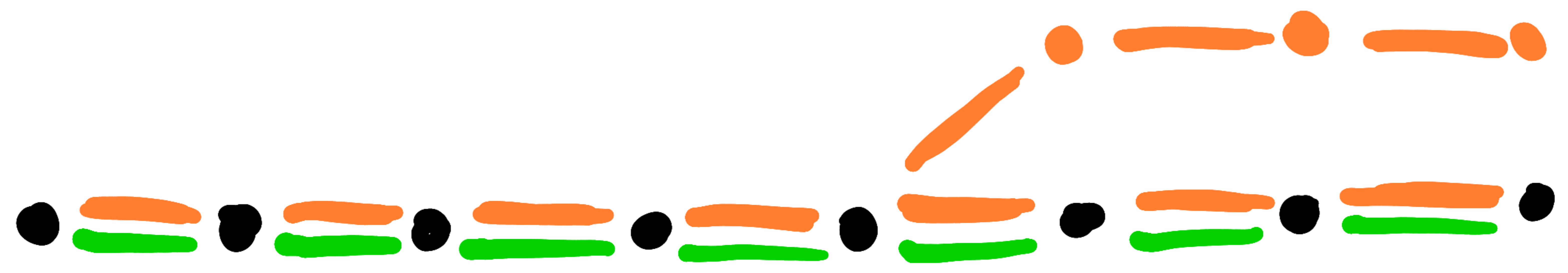
1. Pick "secret key" x or $d \log z$
2. Run adversary once
3. Re-program \mathcal{E}
4. Run adversary another time
5. Hope to get "other key" 
6. Return "other key" as solution to DL

Forking [PS96]



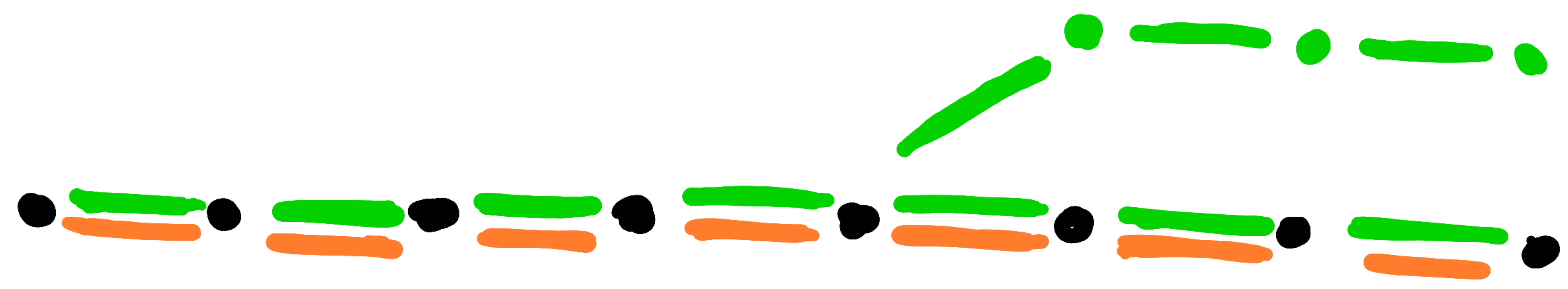
$$E(\text{signature 1, signature 2}) \rightsquigarrow X$$
$$E(\text{signature 1, signature 2}) \rightsquigarrow d \log z$$

Forking with an OR Proof



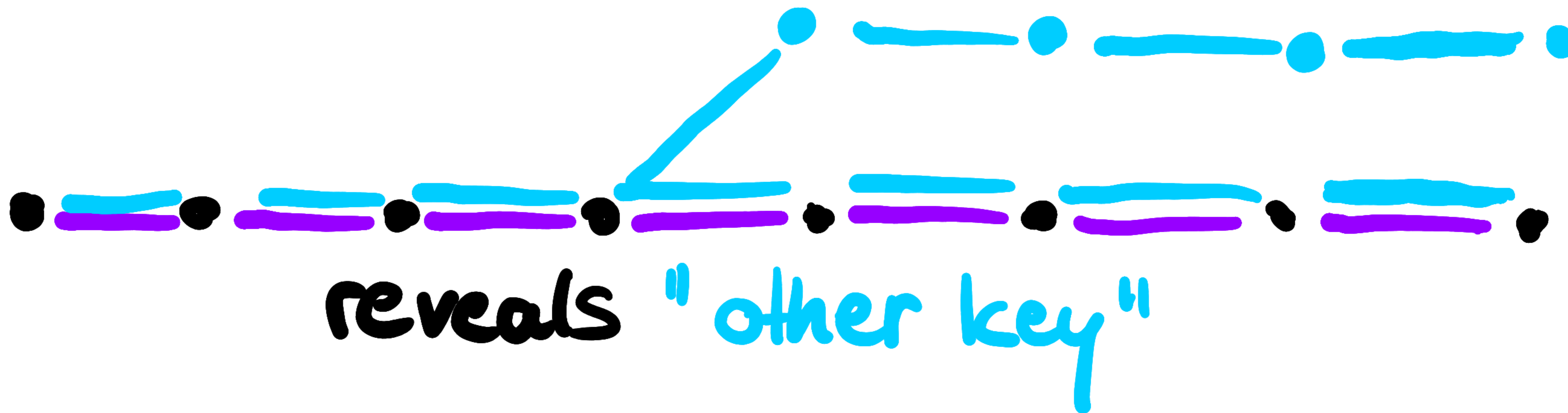
get x

OR



get dlogz

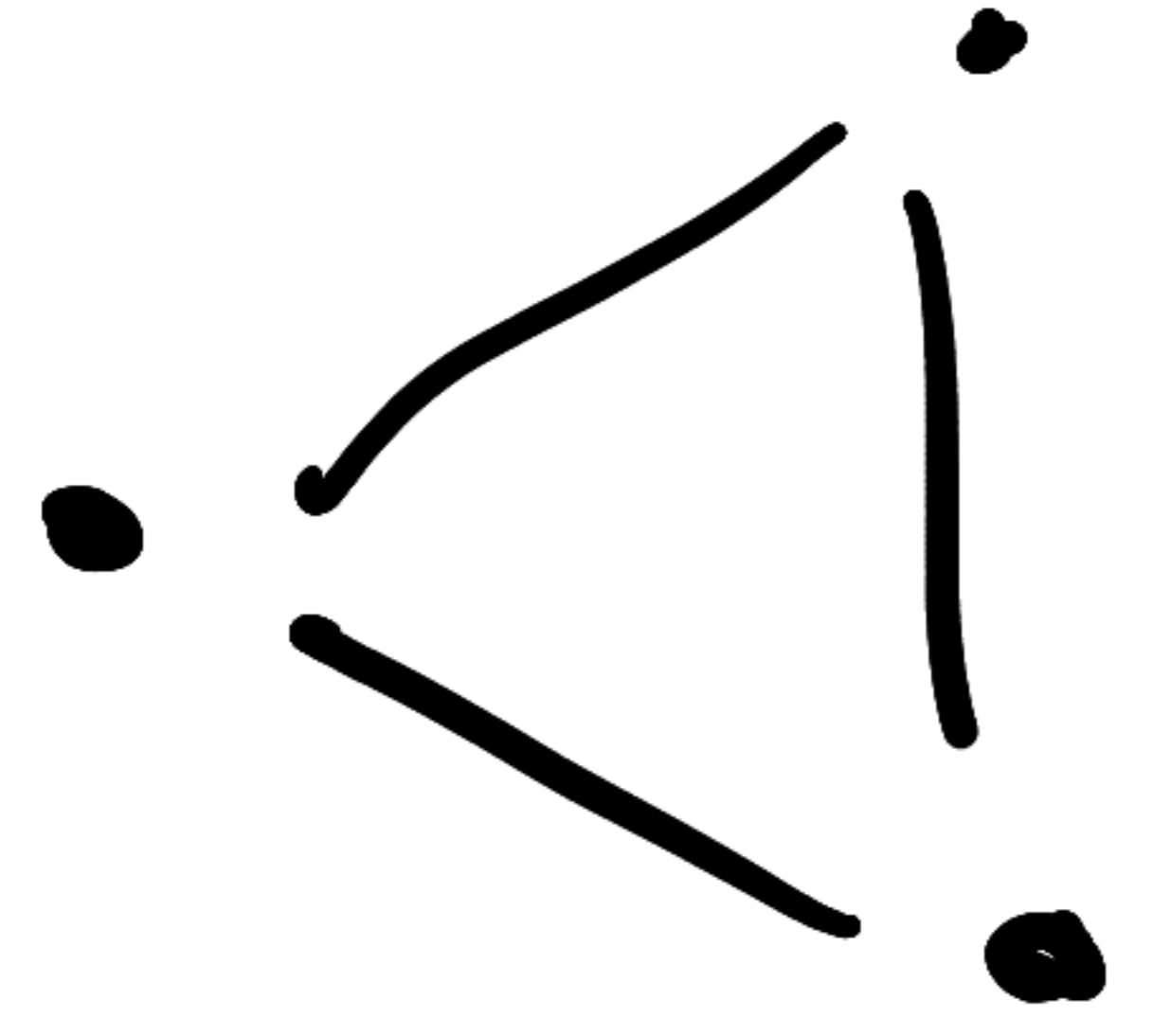
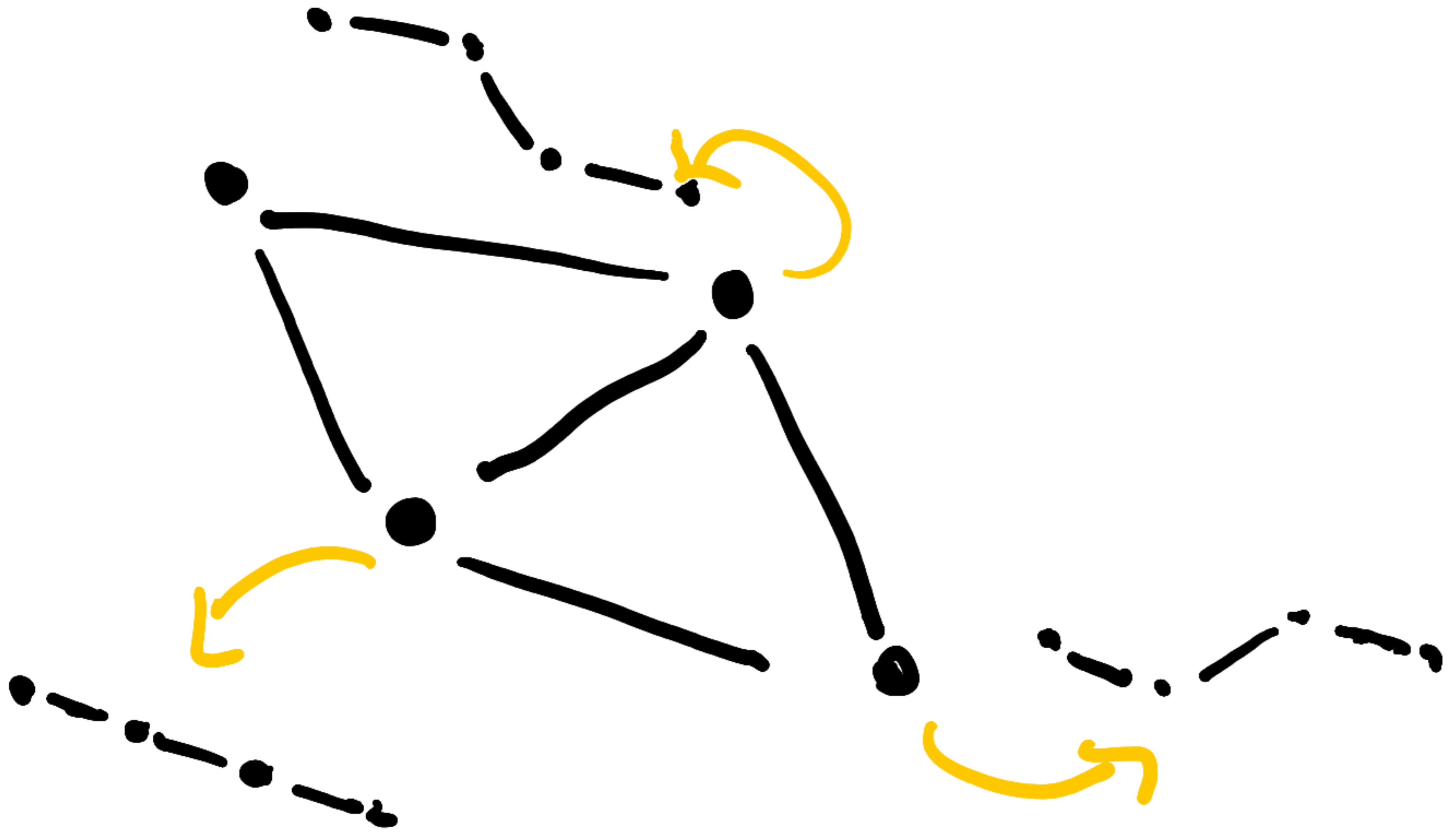
Reduction Goal



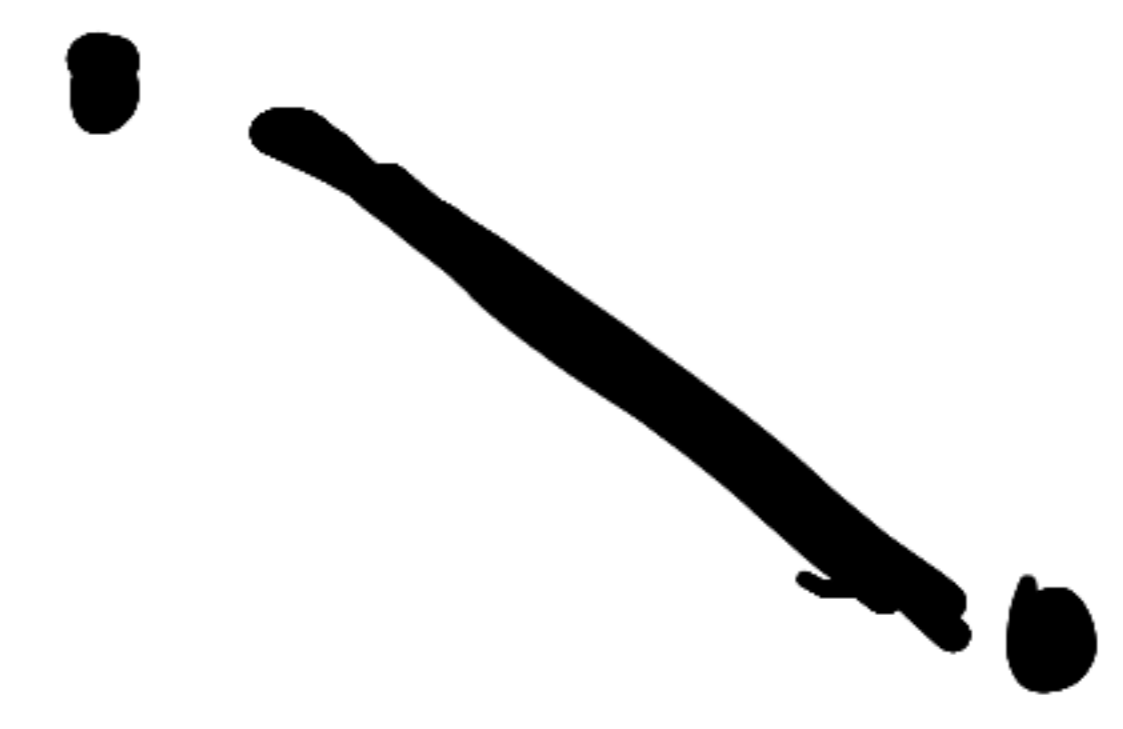
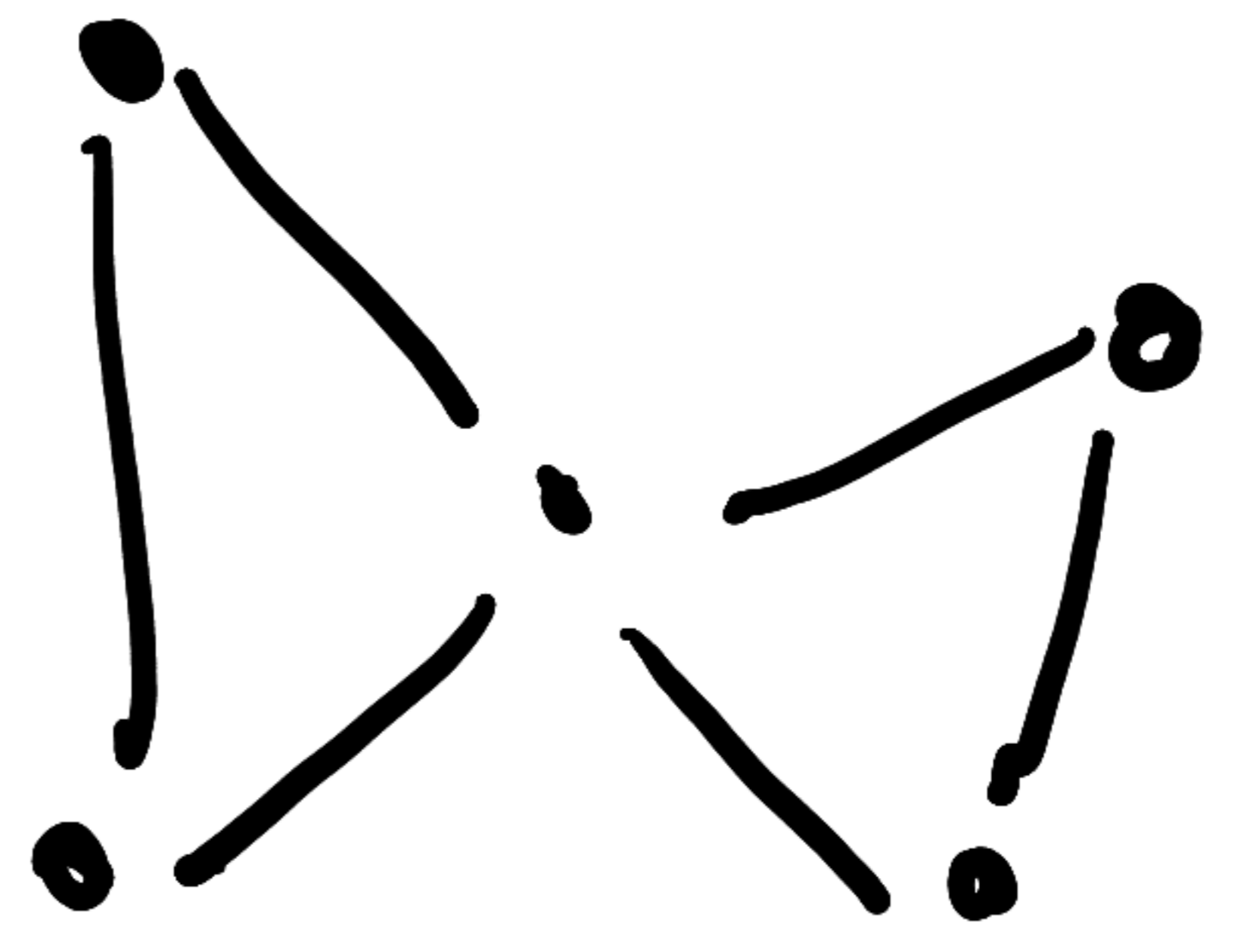


Abstraction in
progress...

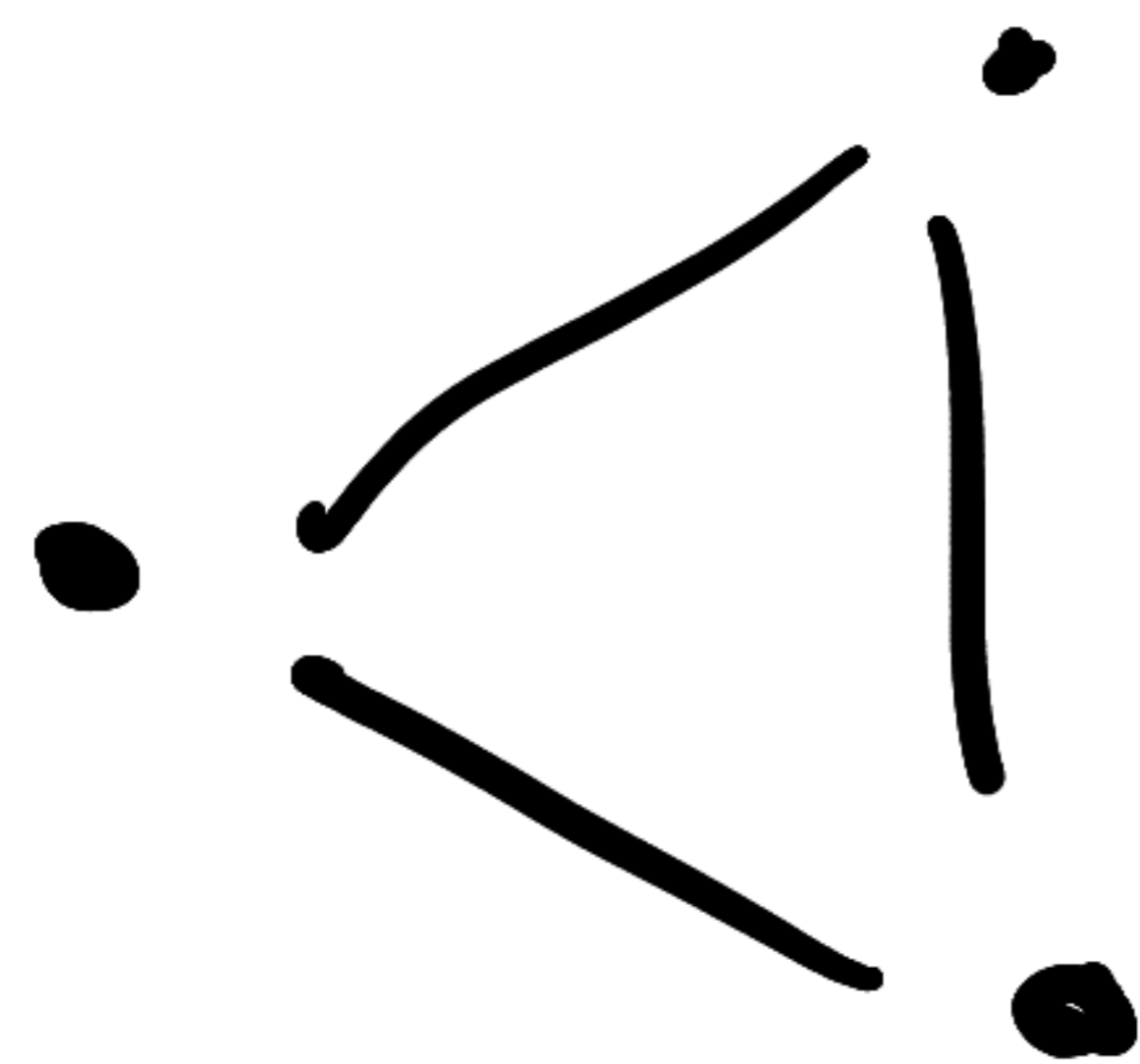
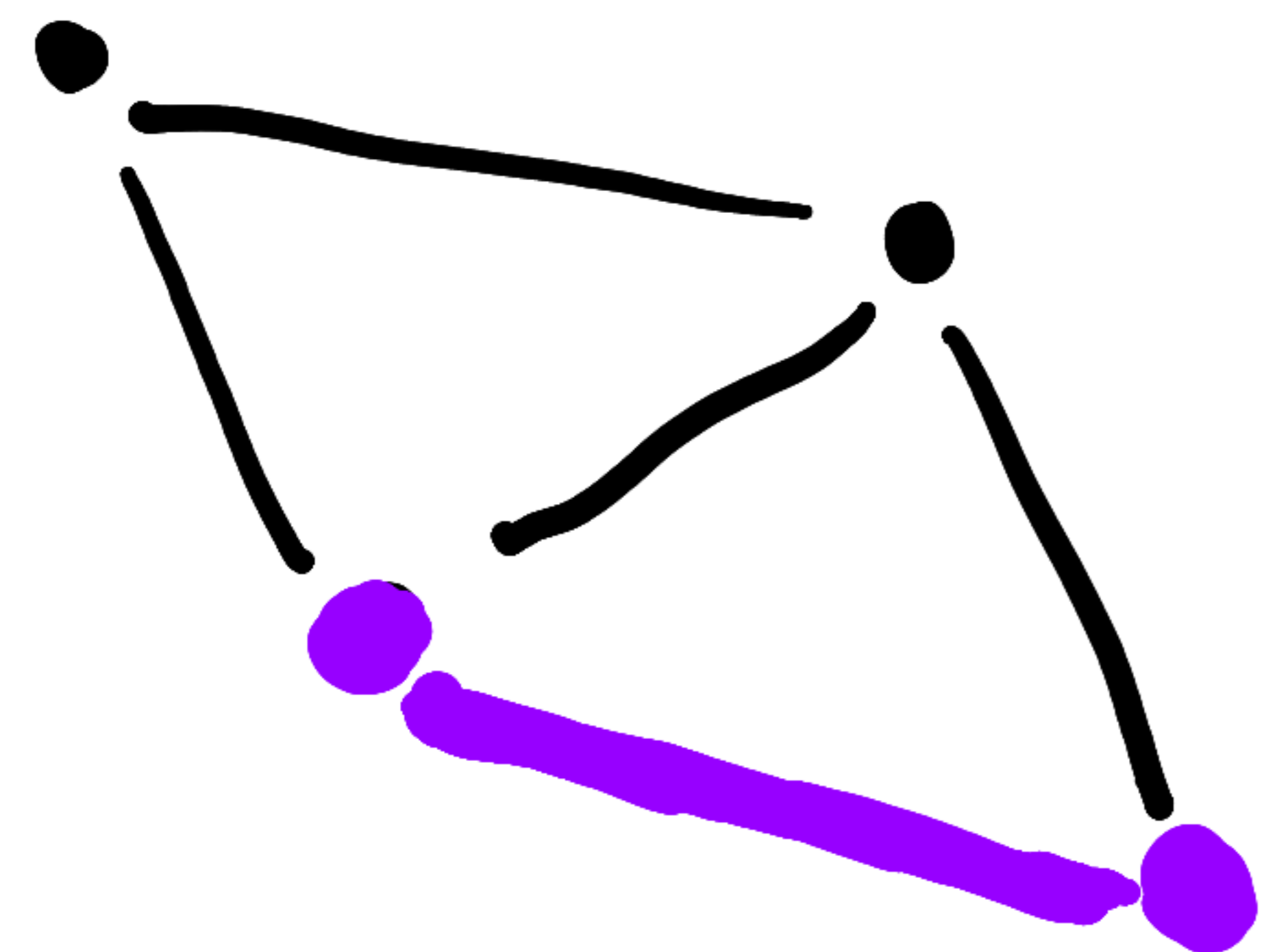
X



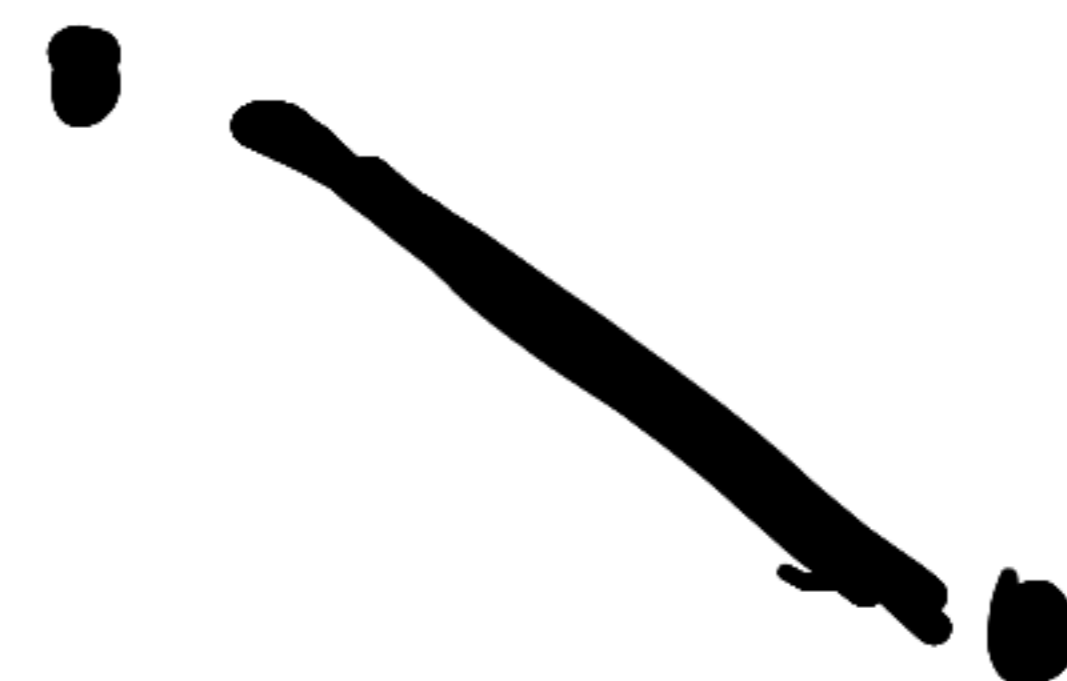
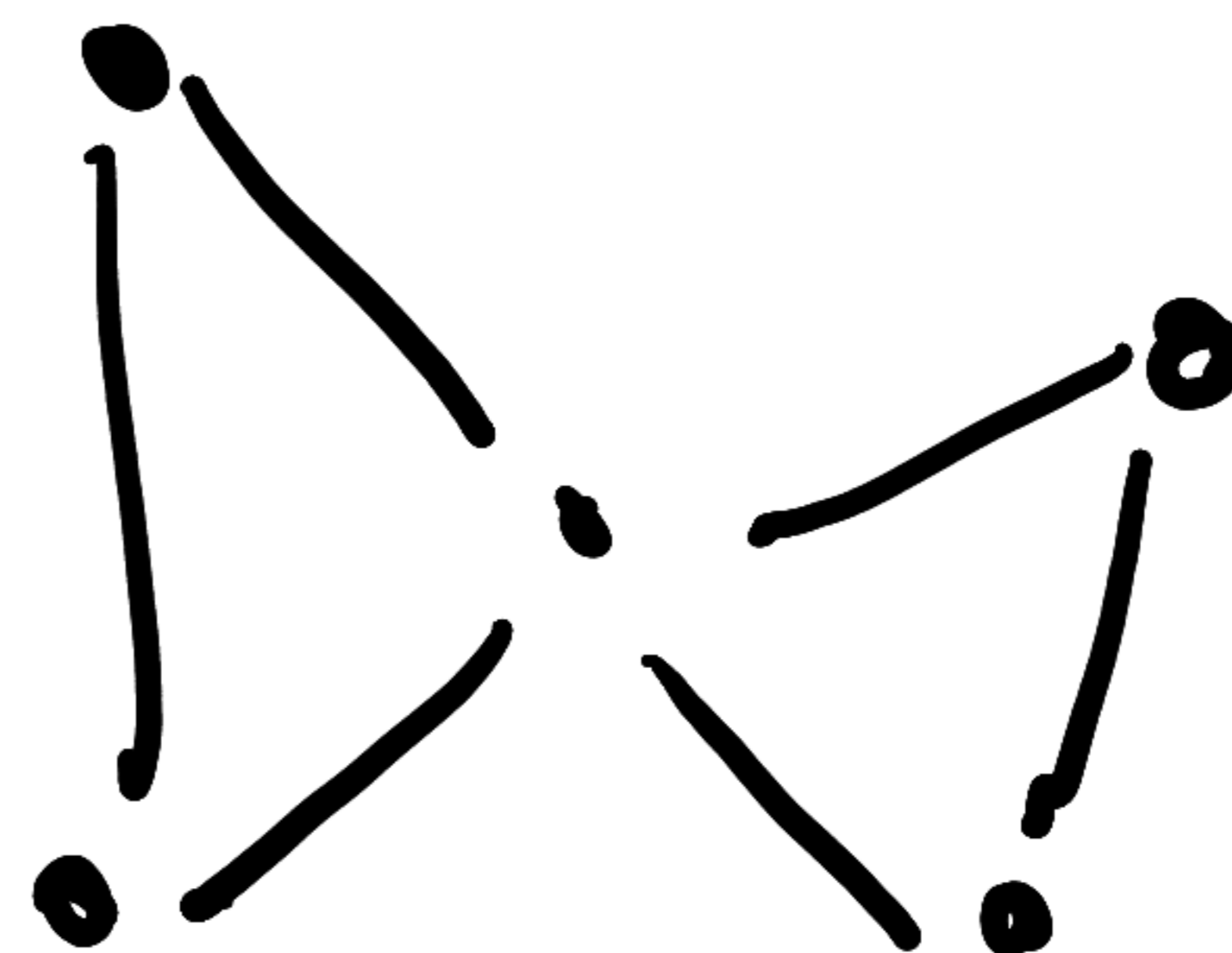
$d \log 2$



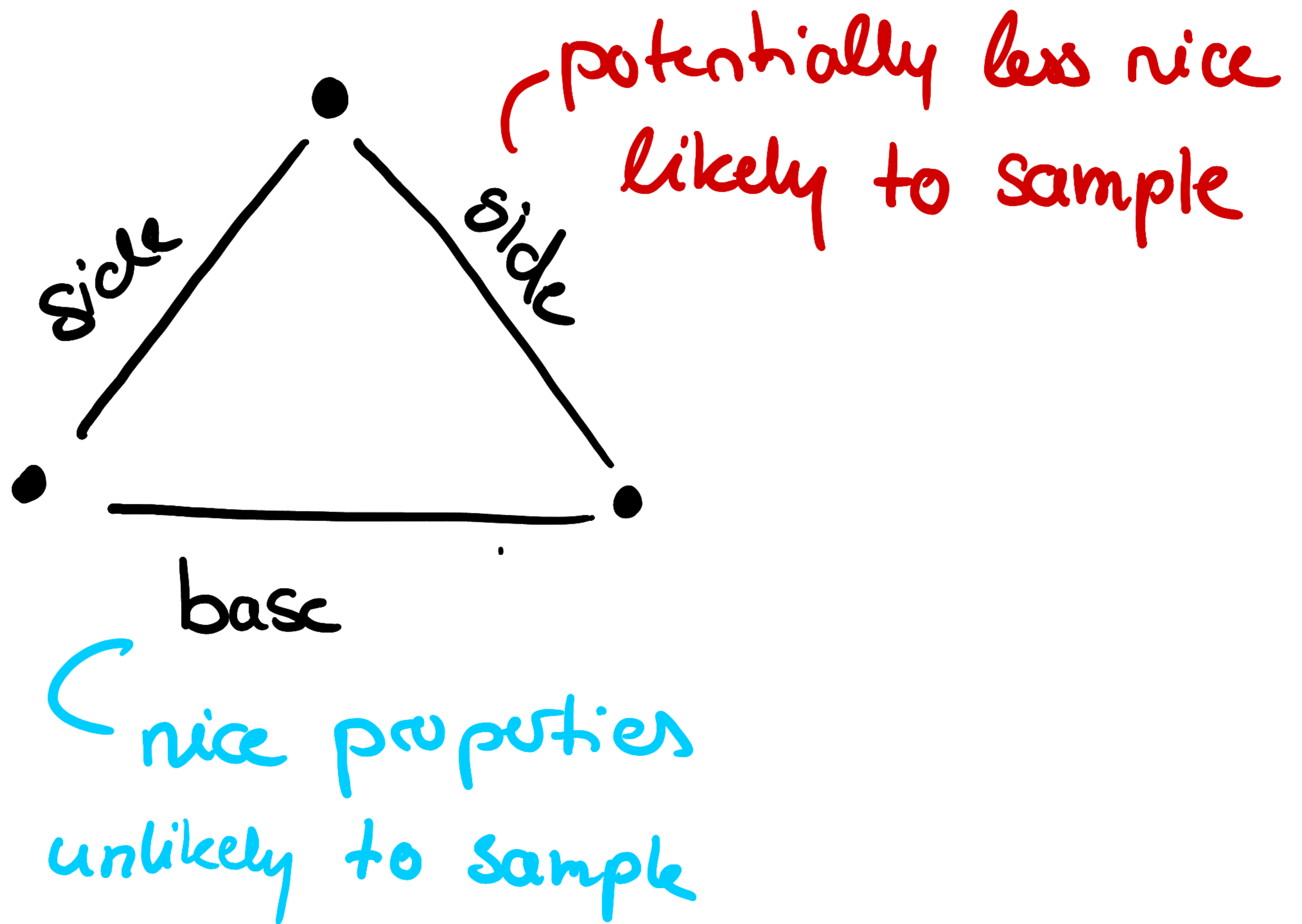
X



$d \log 2$



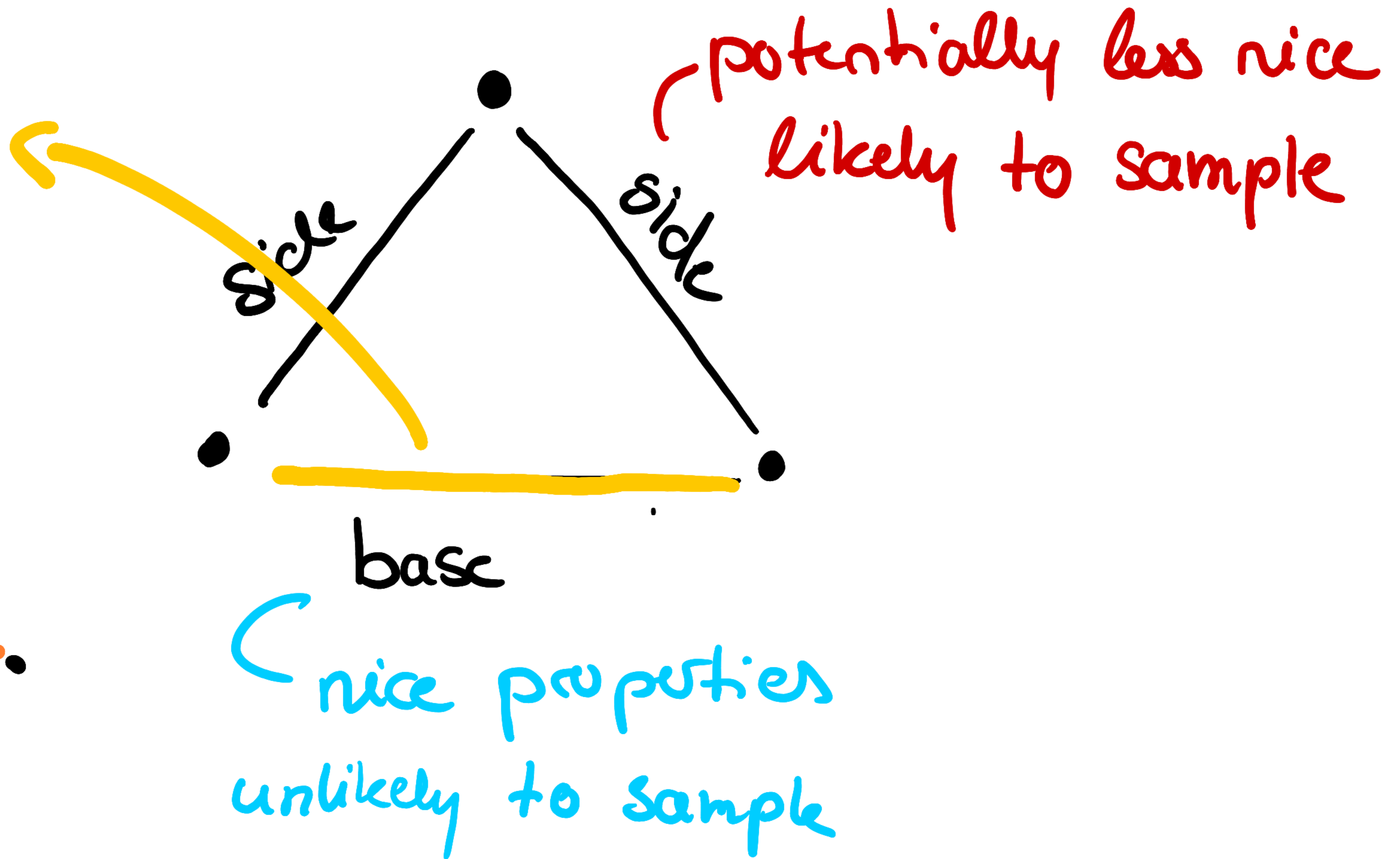
Triangles [40'00]



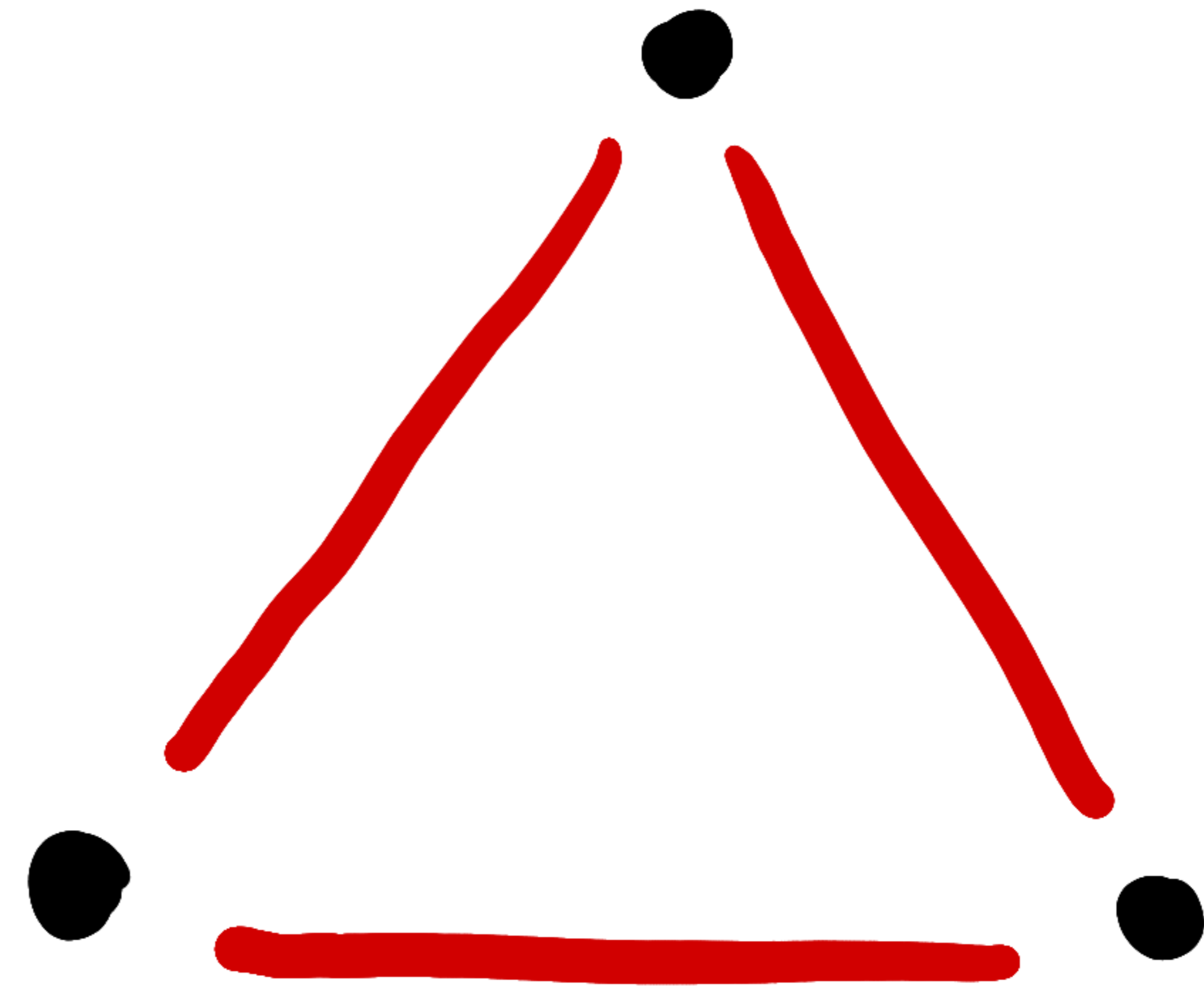
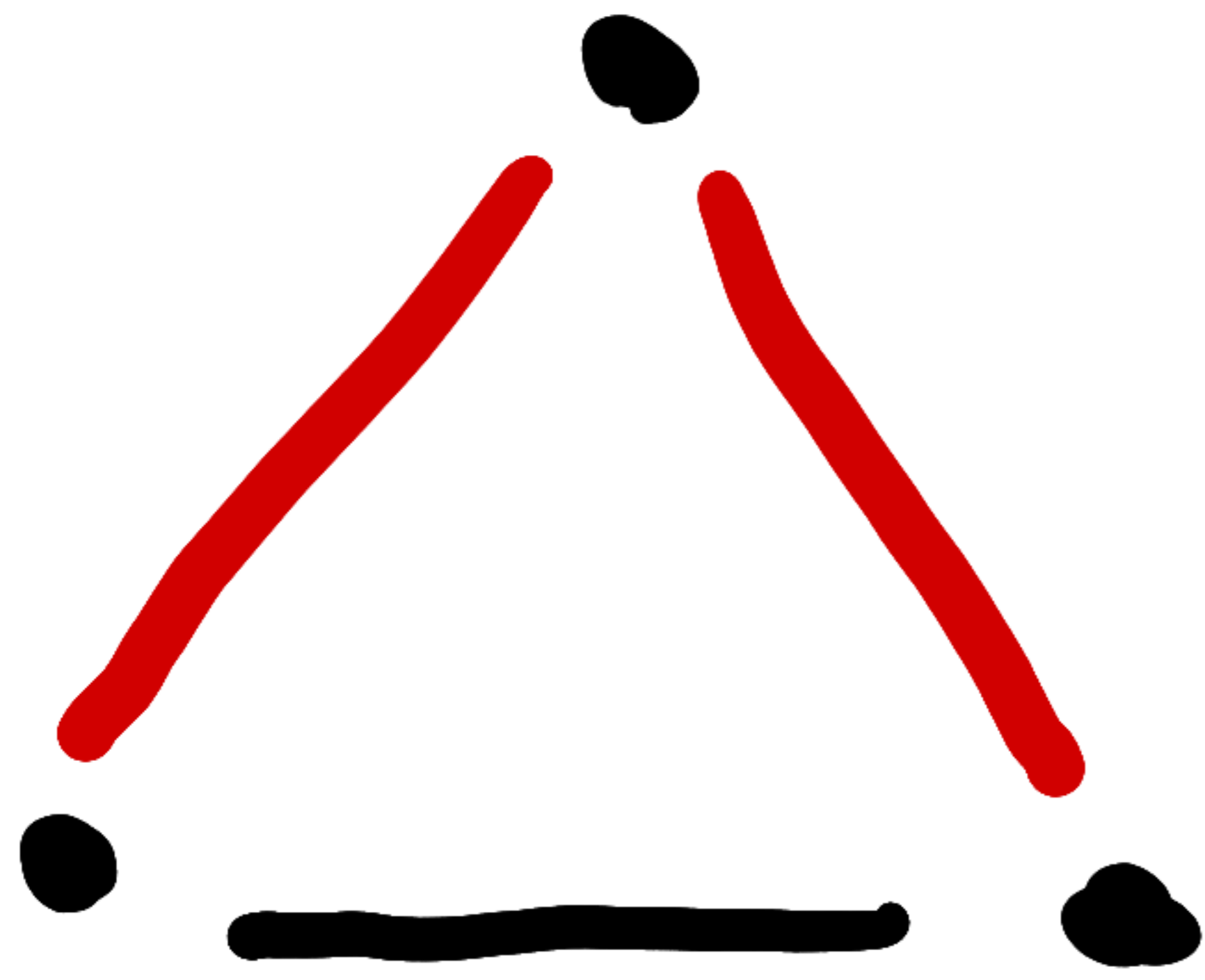
Triangles [40'00]



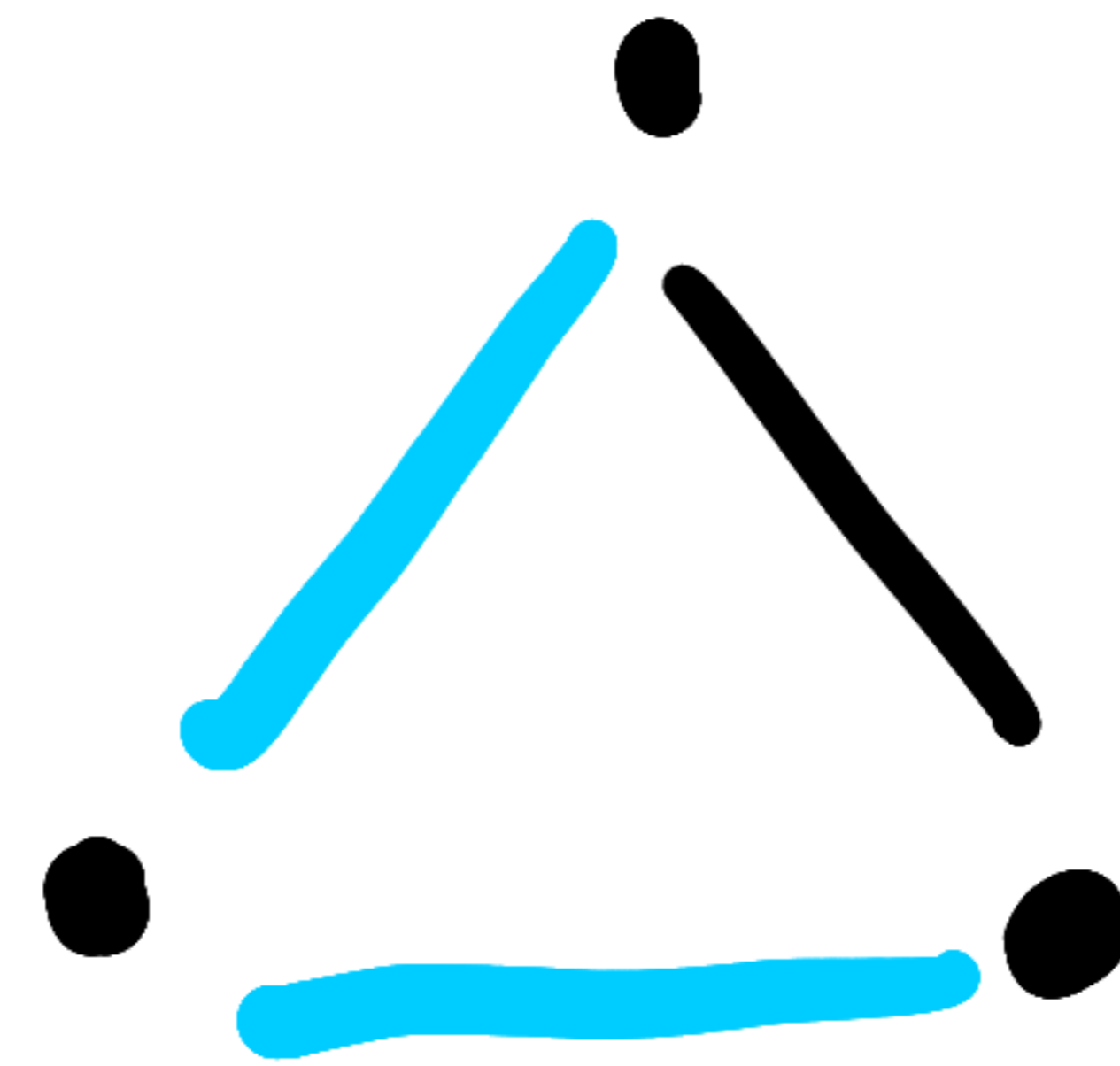
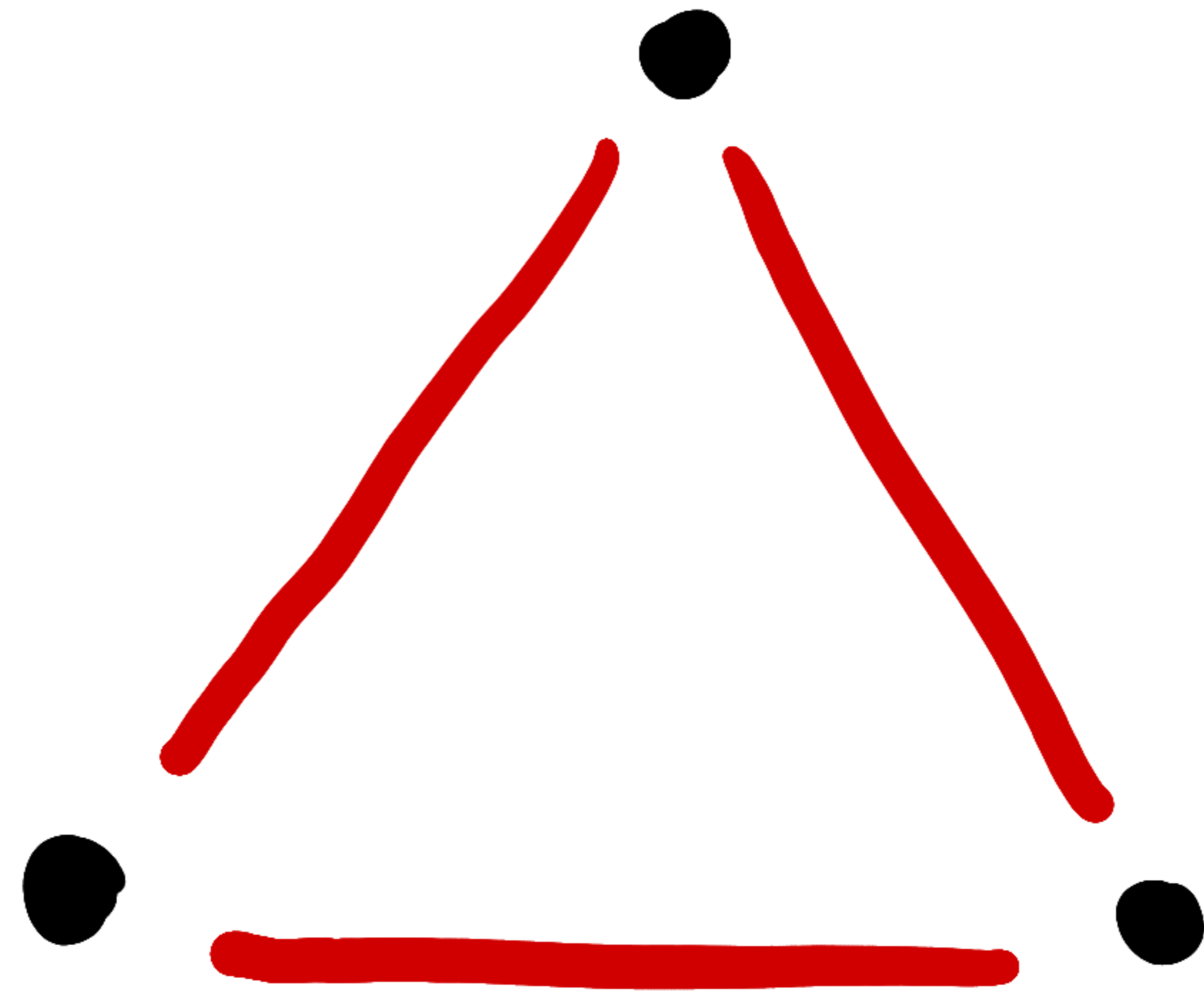
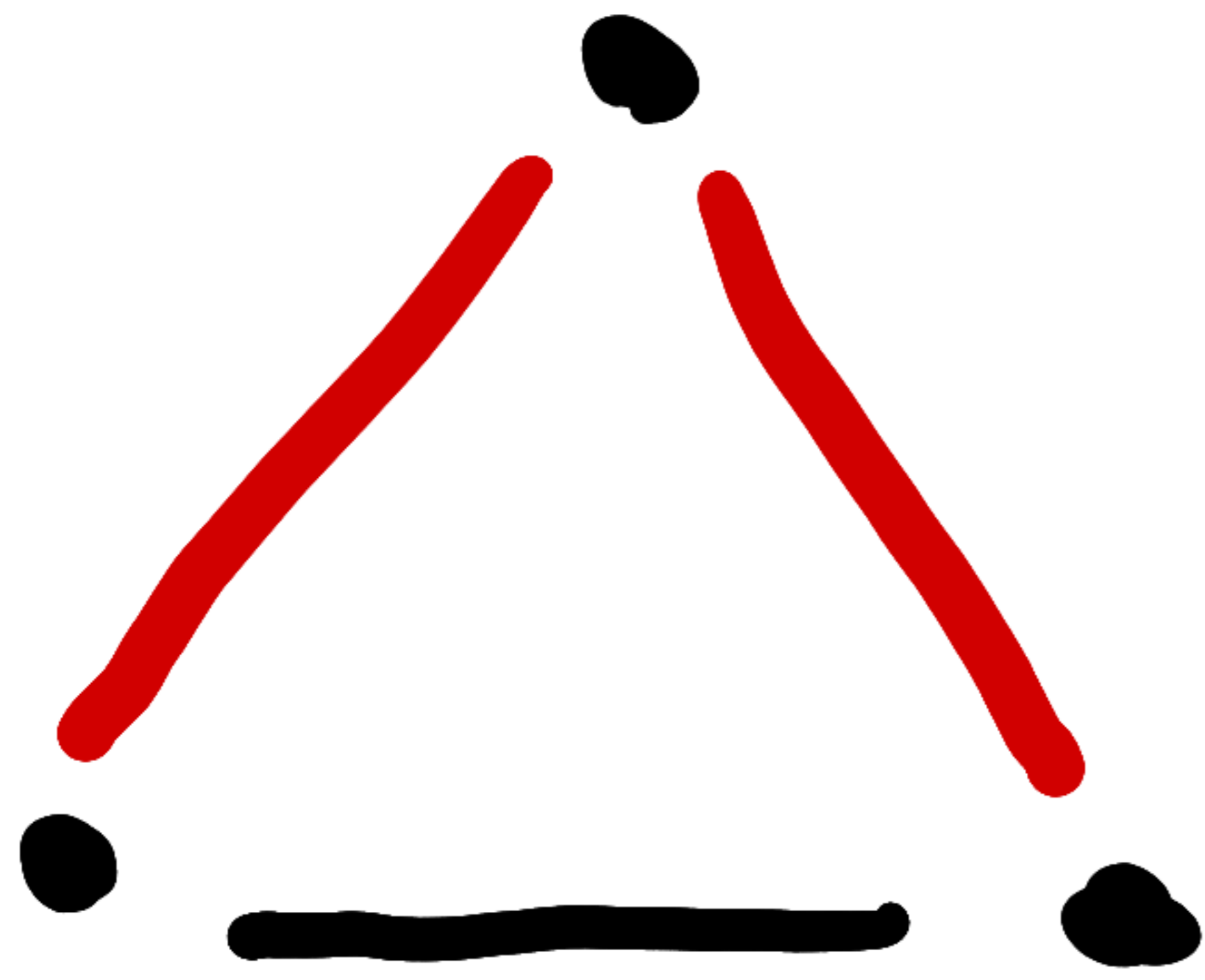
can use either
 x or $d \log z$



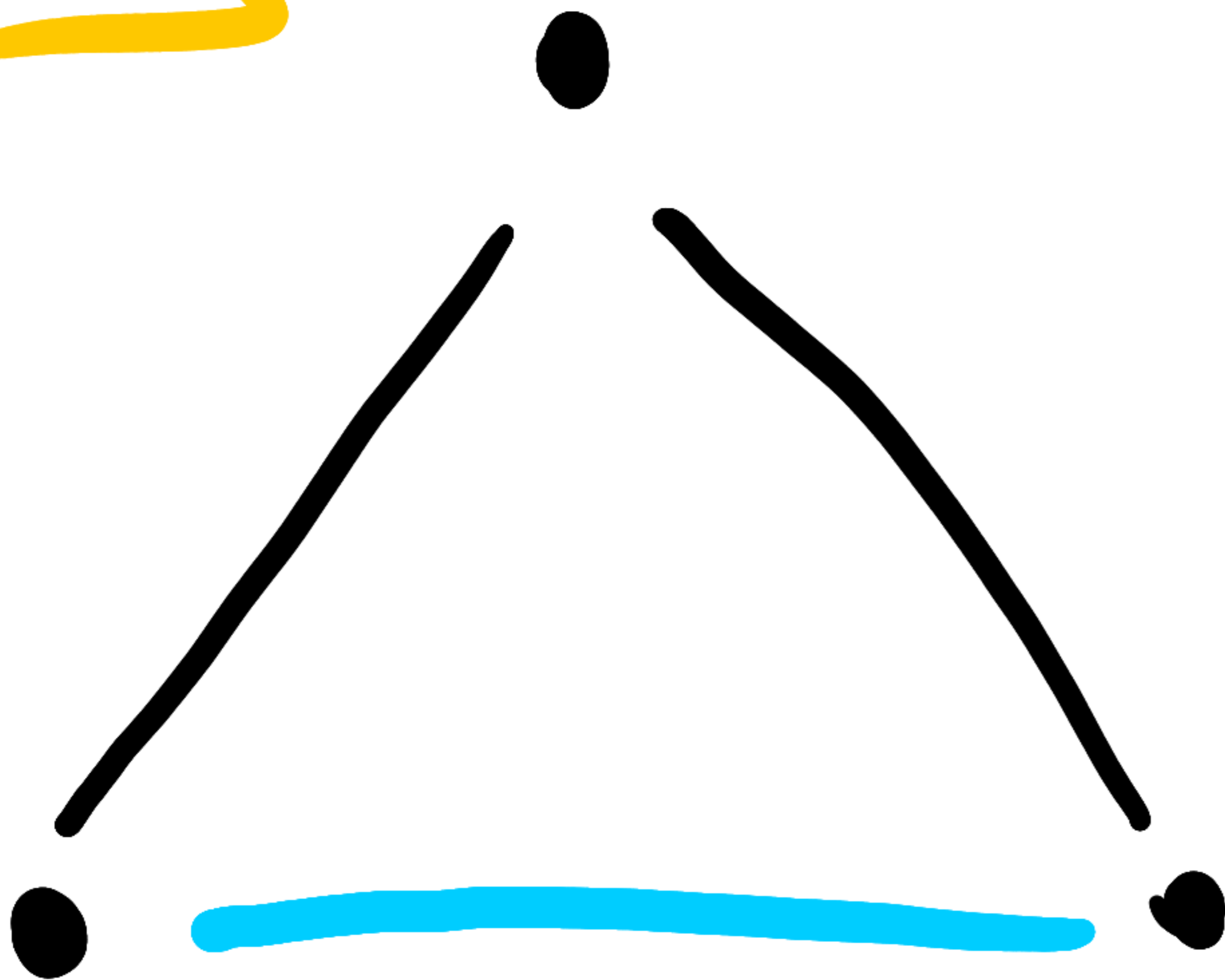
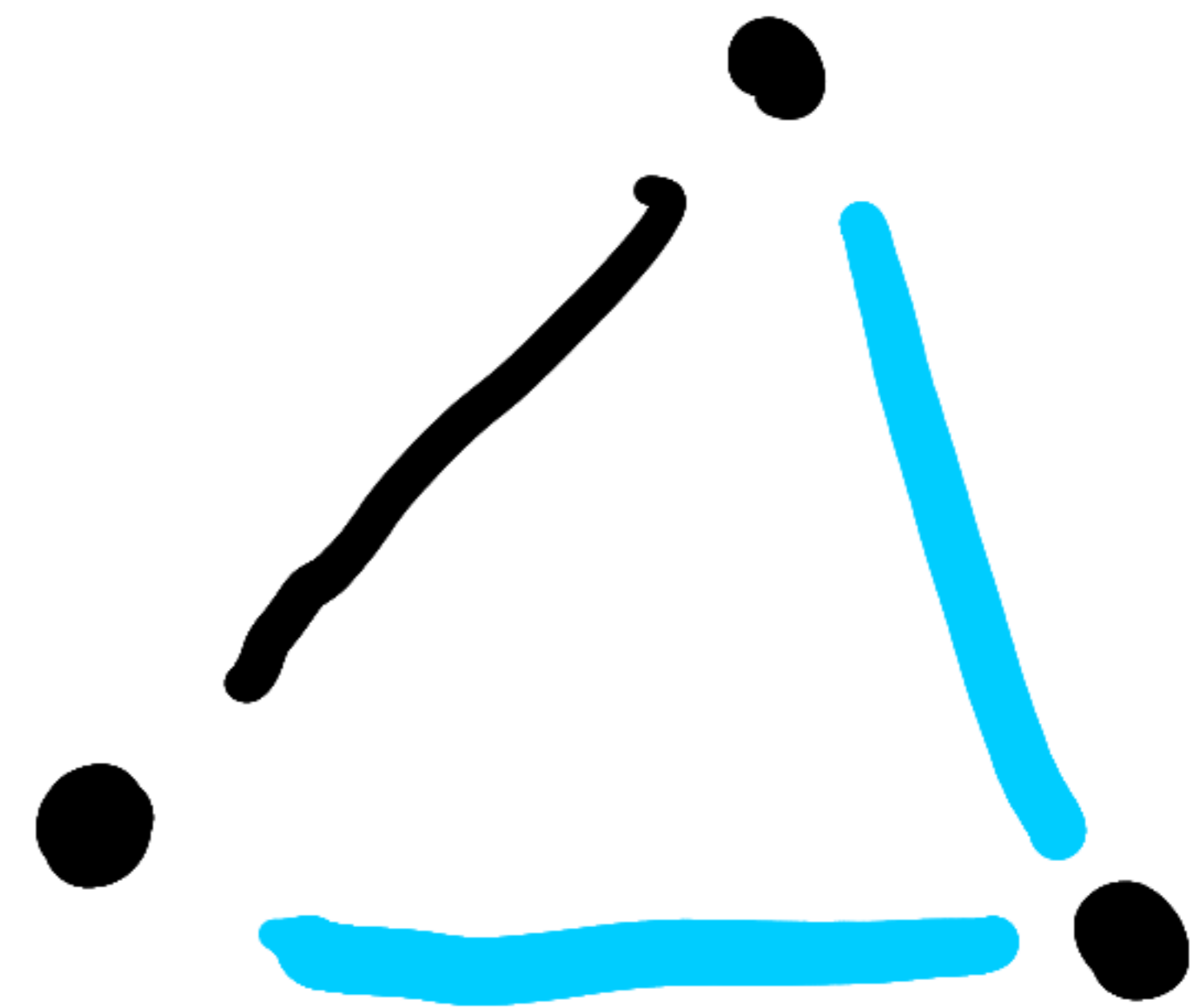
Triangle Properties




Triangle Properties

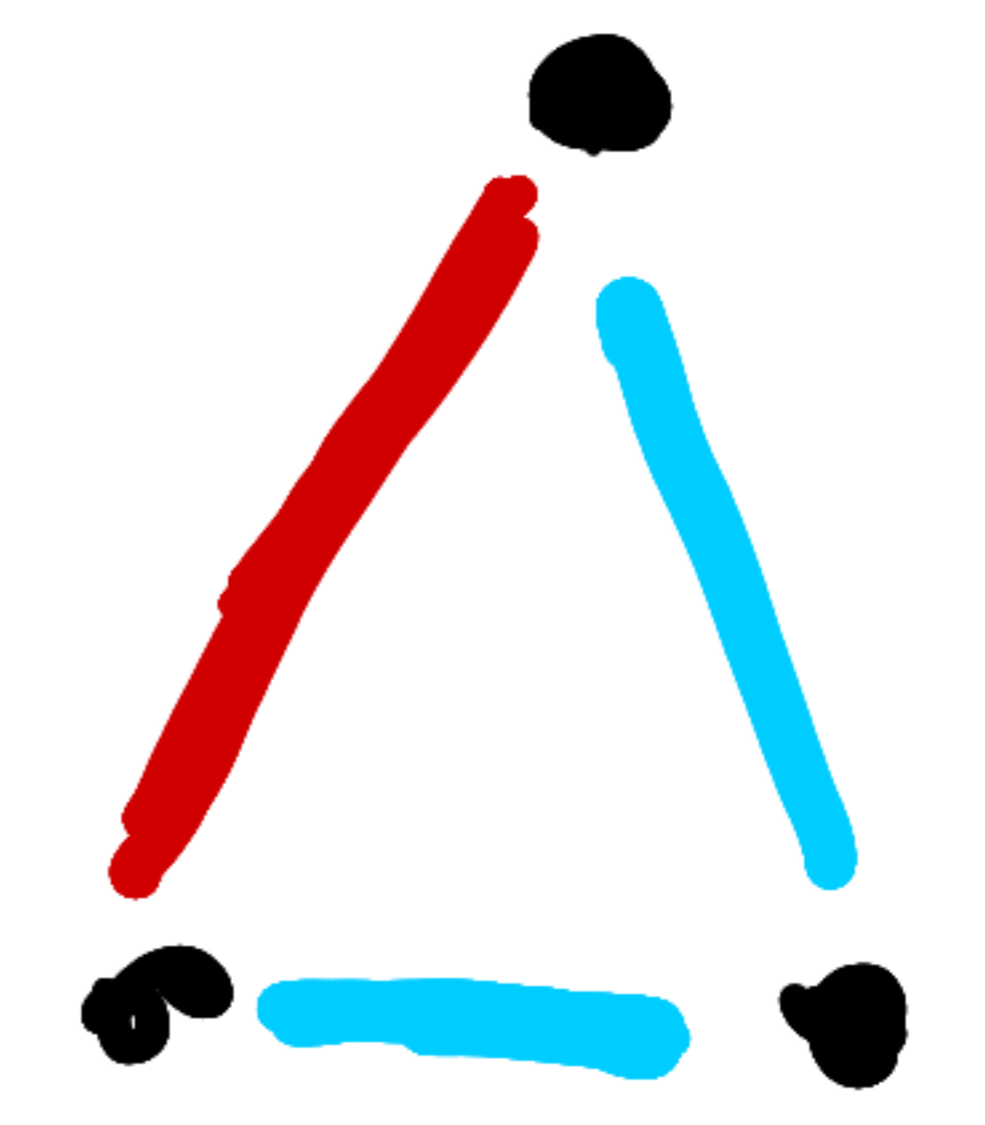
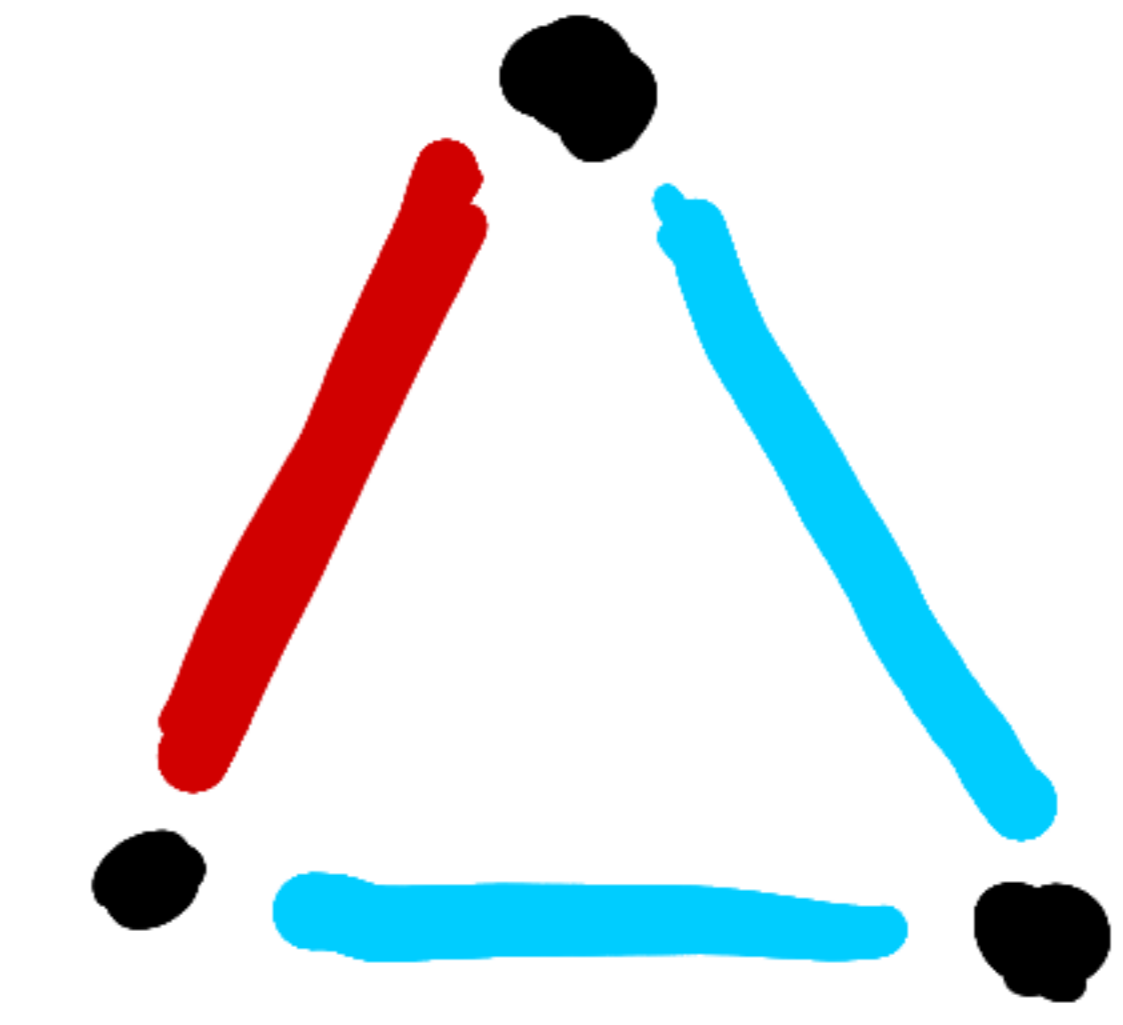
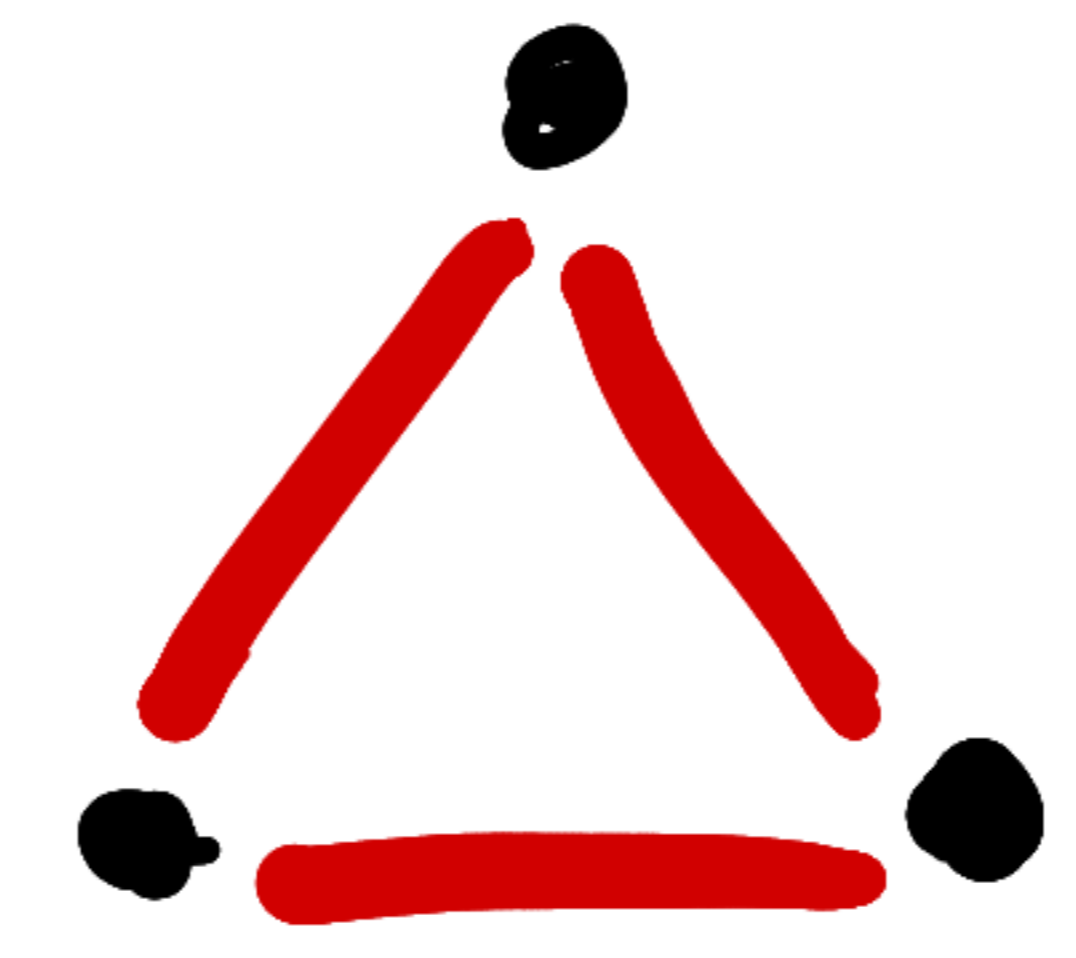
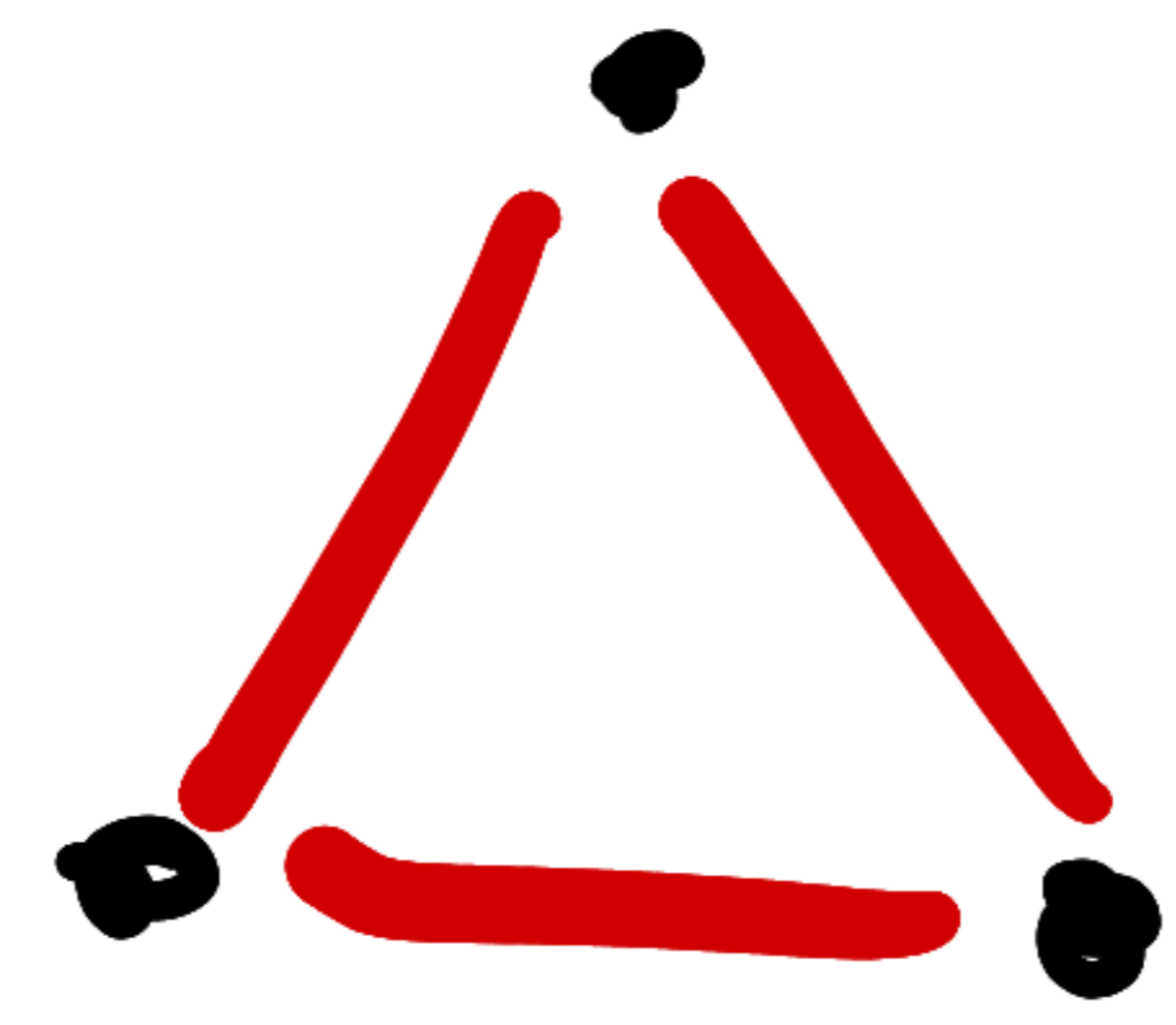
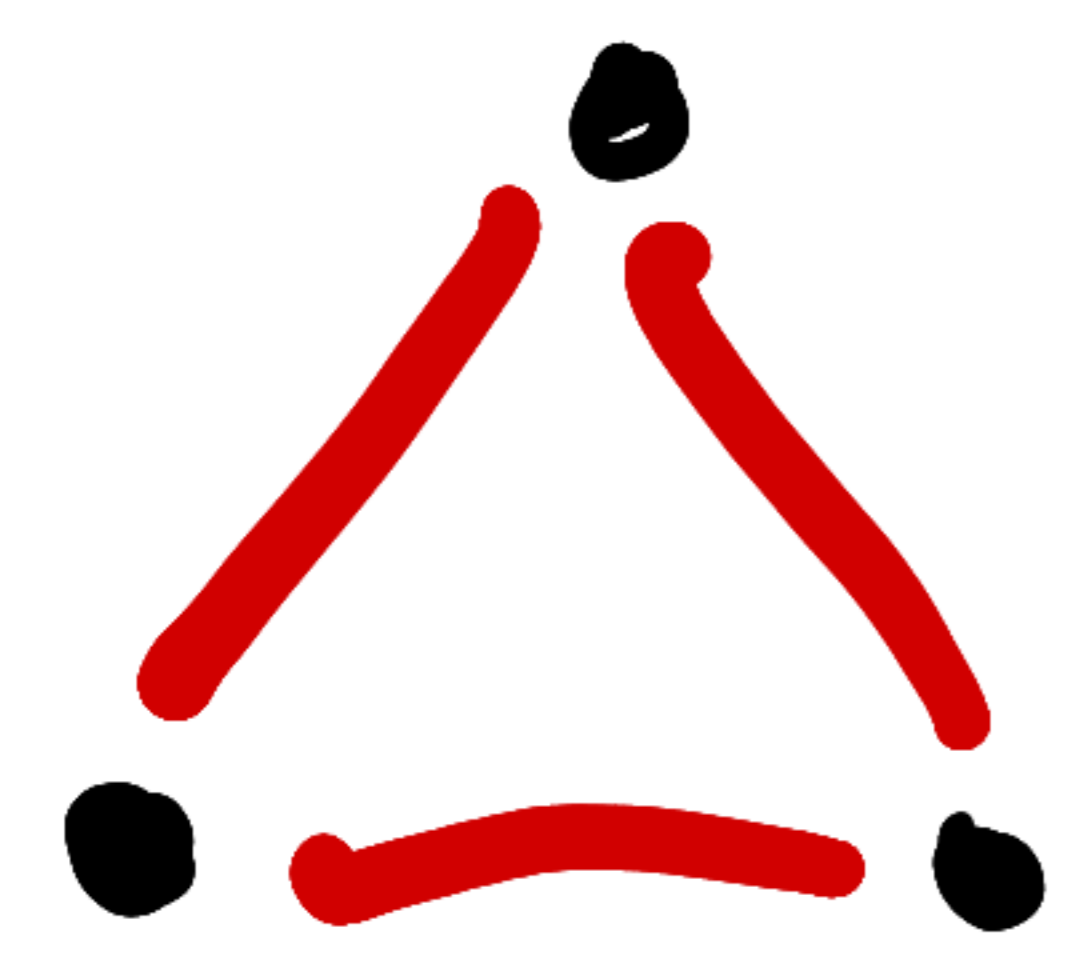


Or

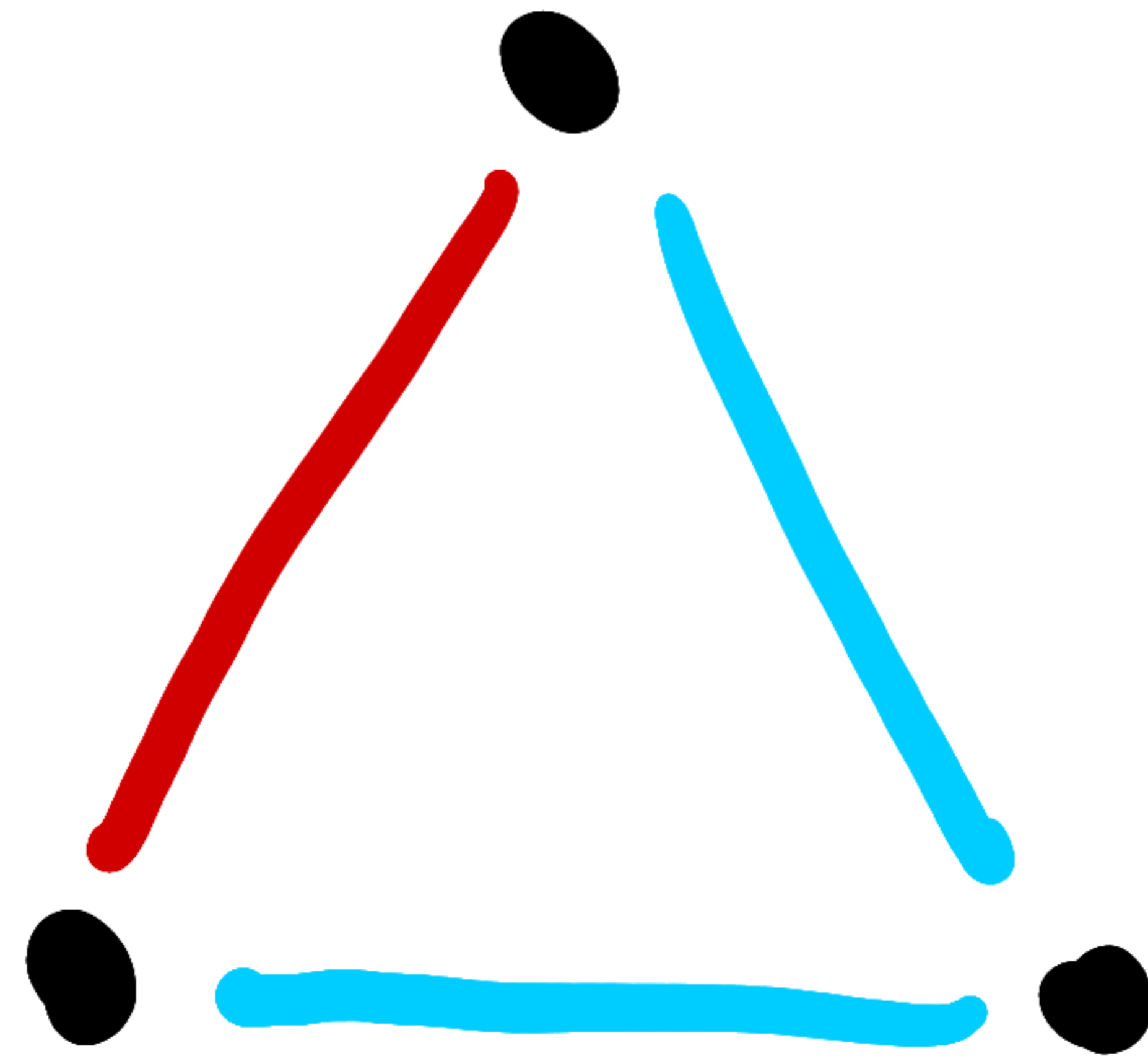
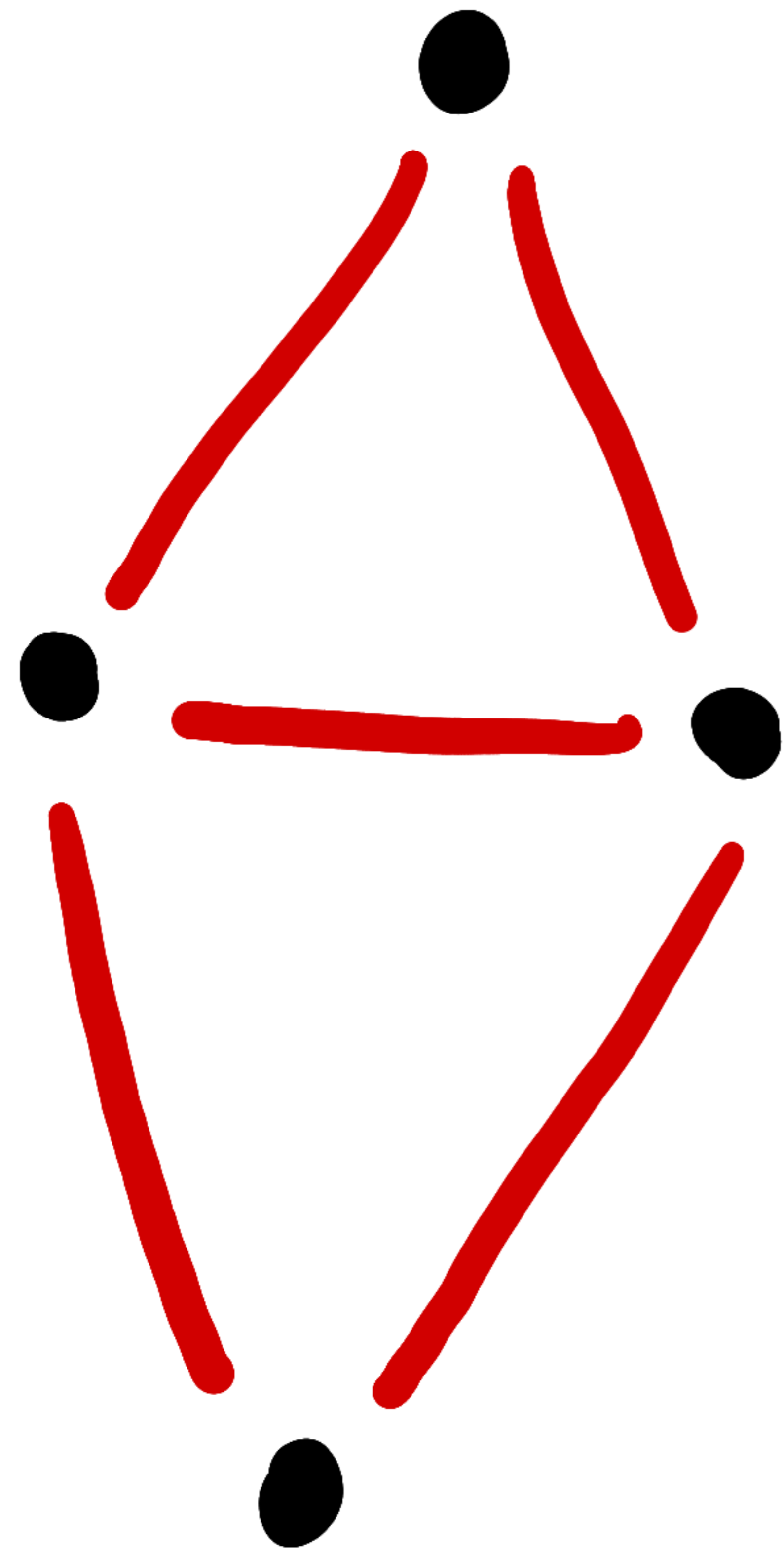


The Gap in $[40'00]$ 

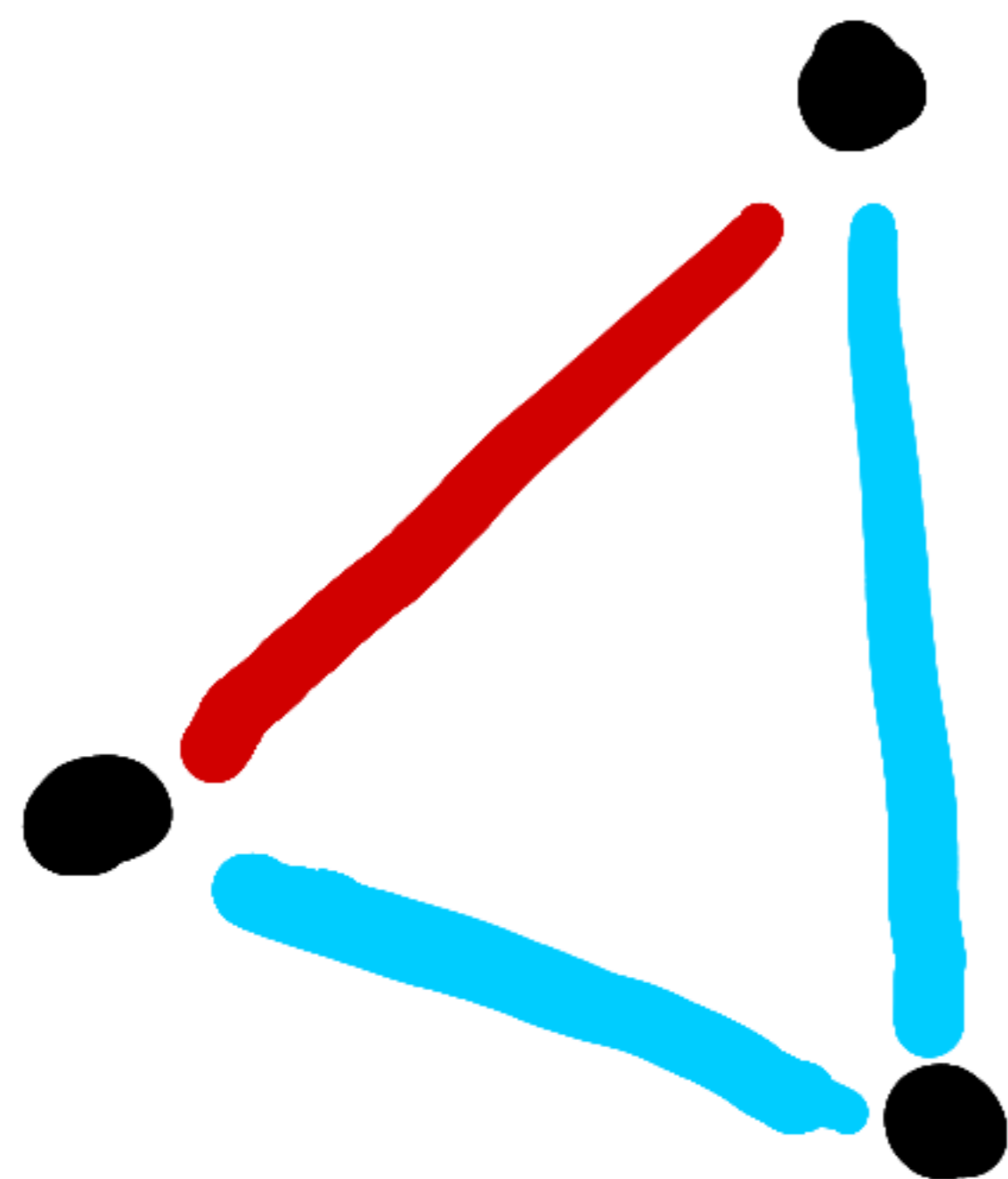
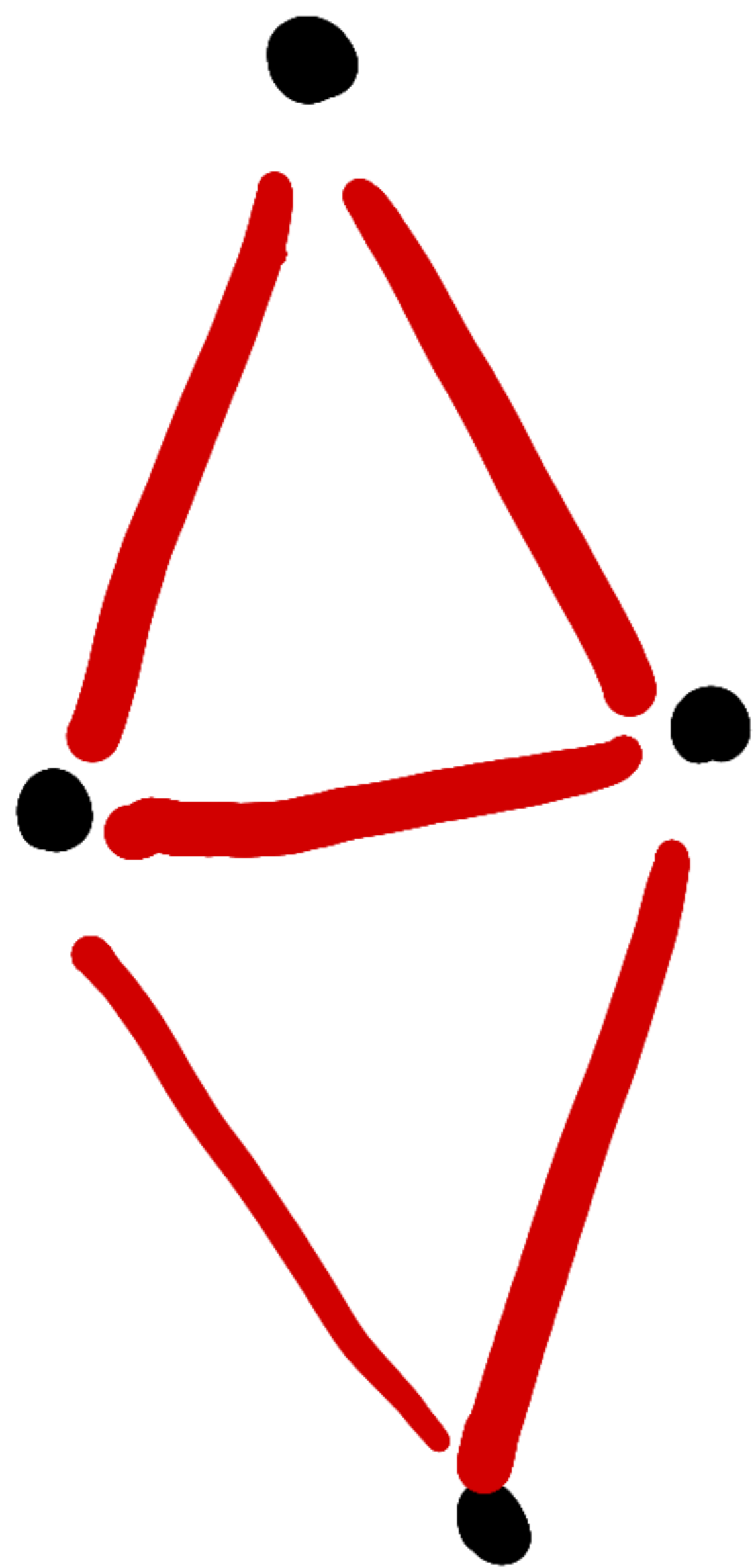
" if $\frac{4}{5}$ of triangle sides yield the **bad witness**
then $\frac{3}{5}$ of triangle bases yield the
bad witness"



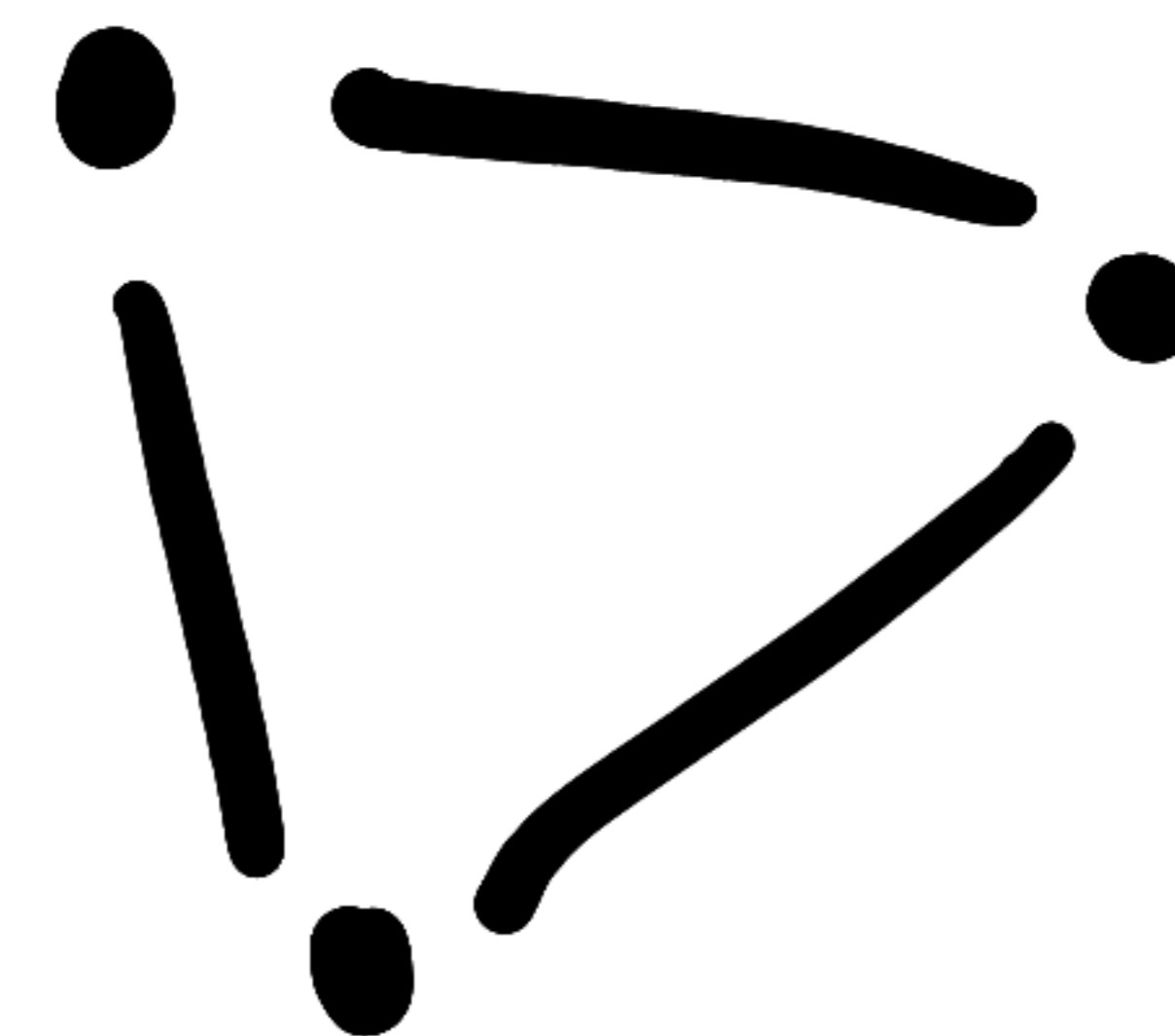
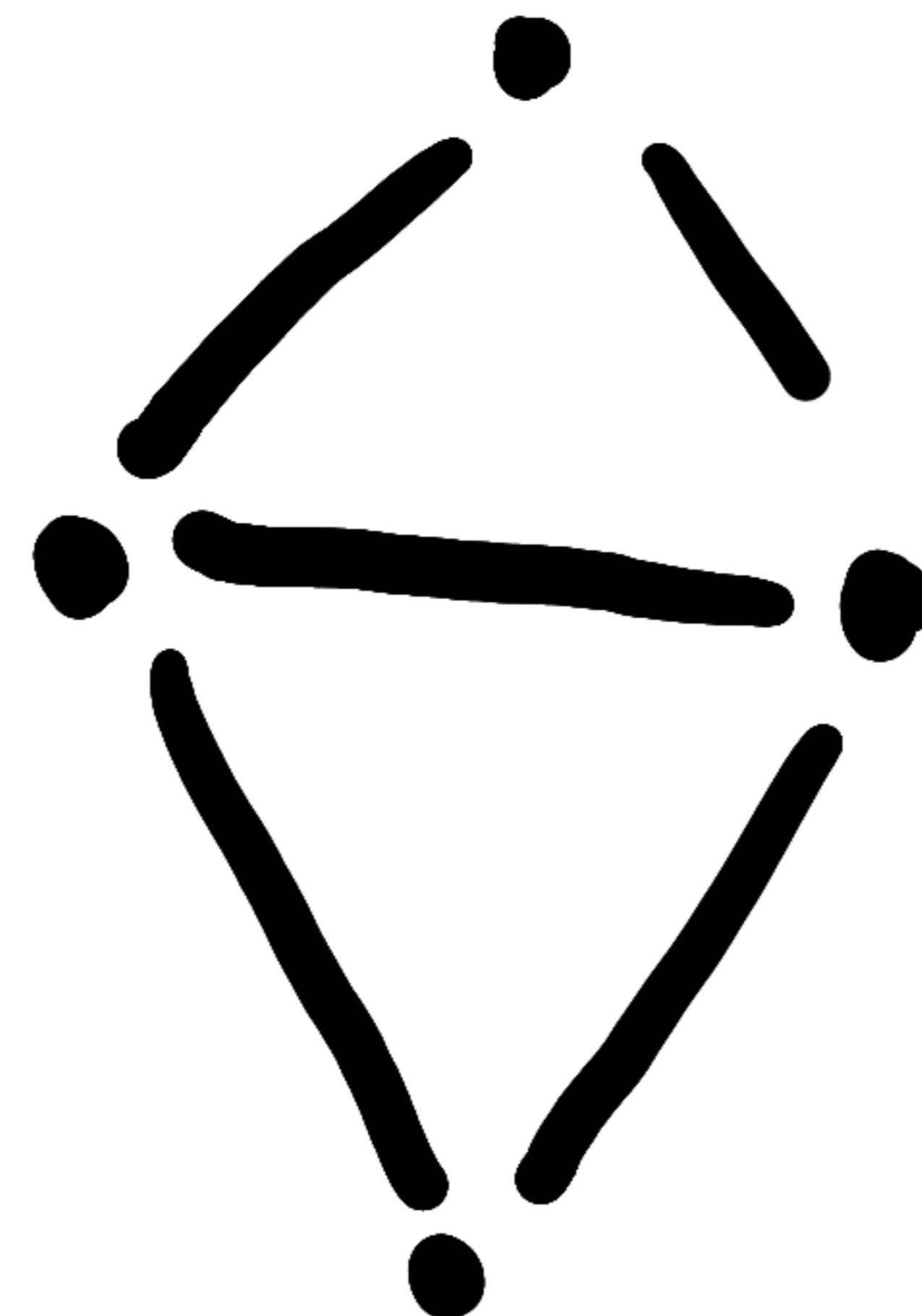
Sharing Triangle "Bases"



x

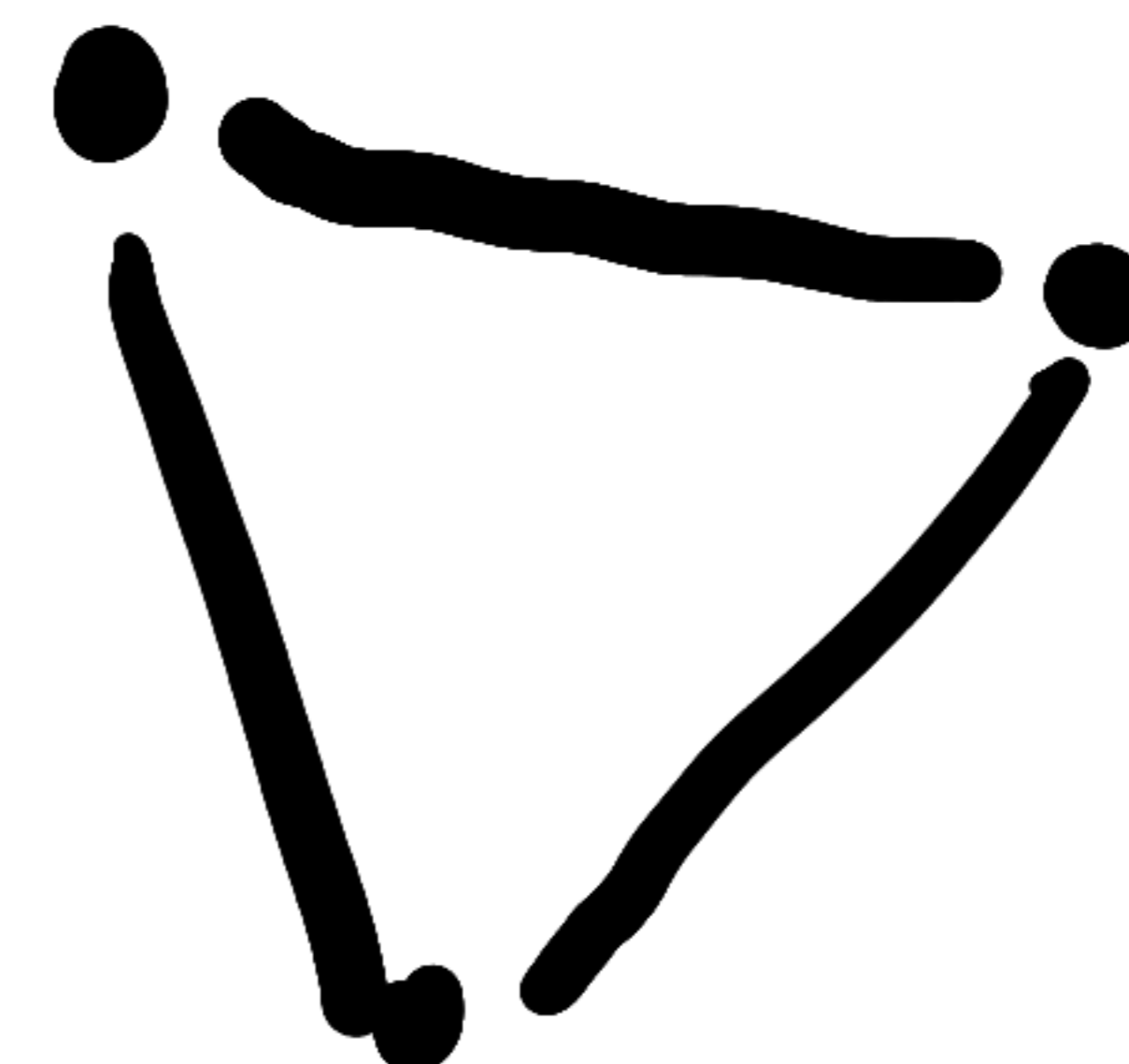
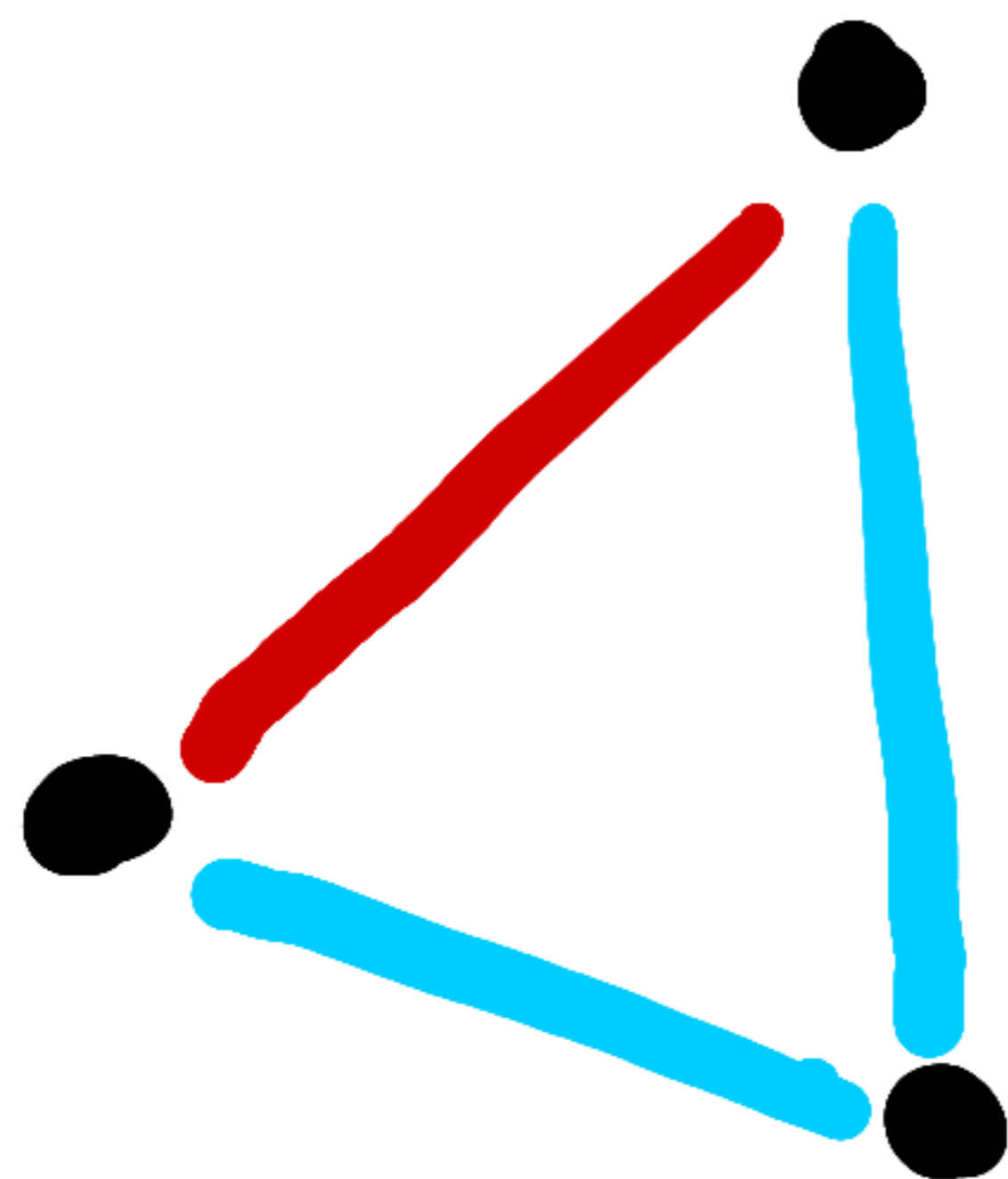
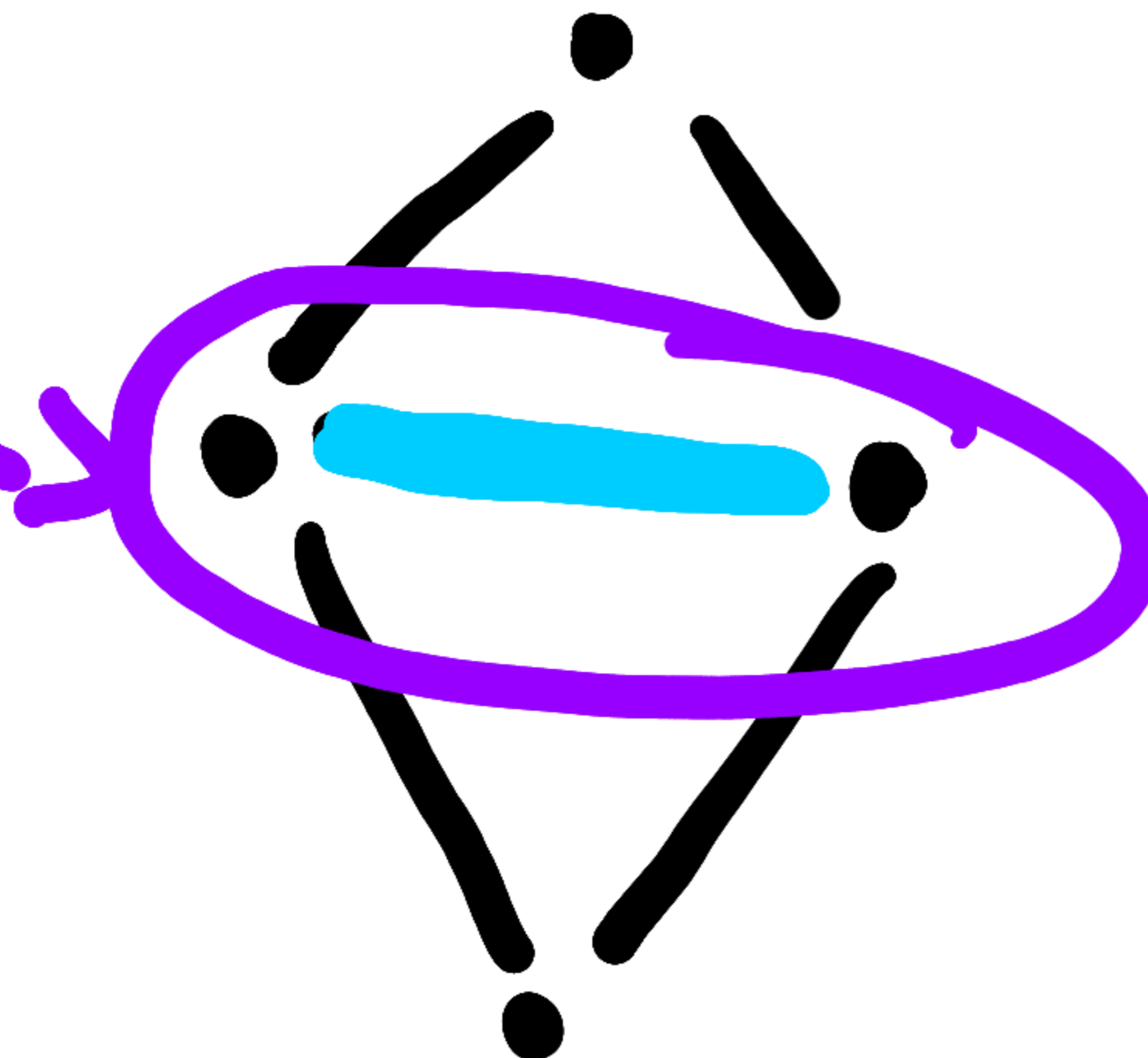
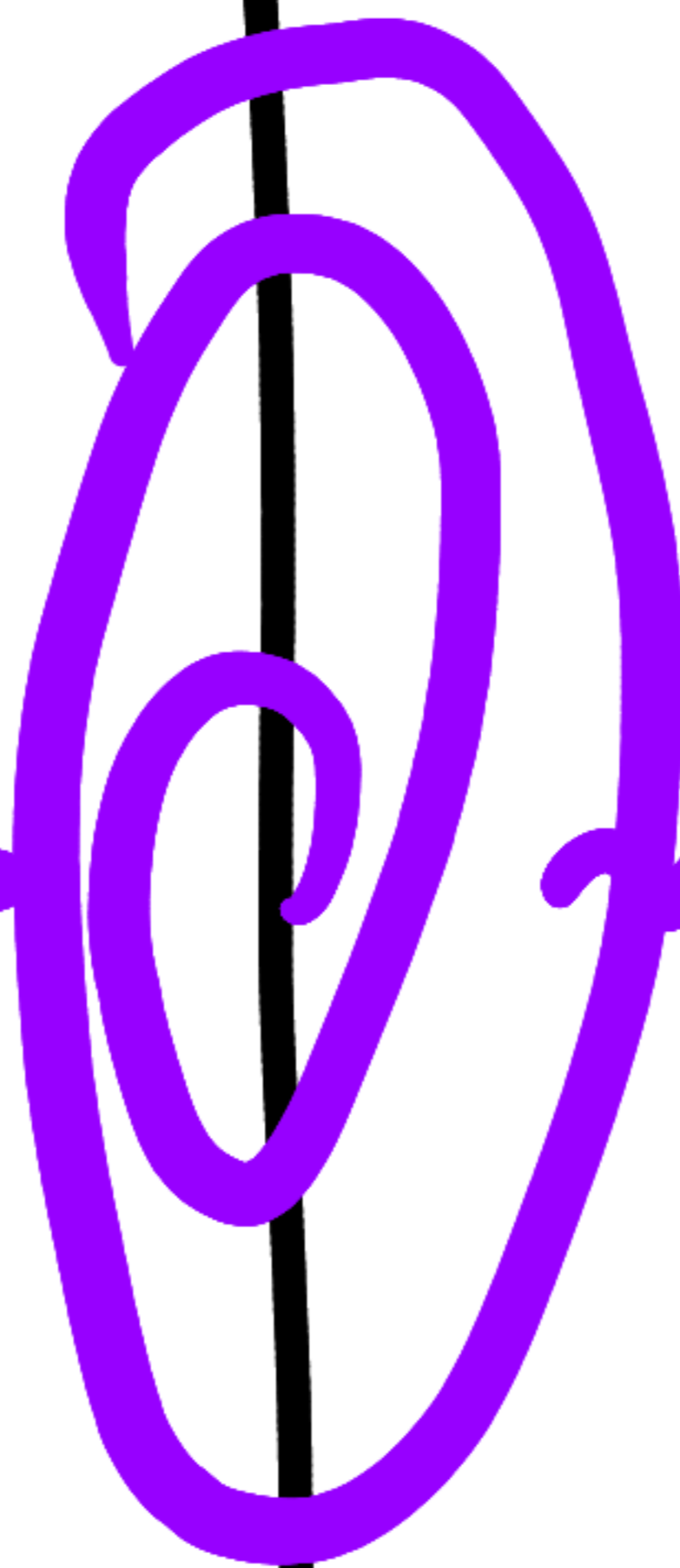
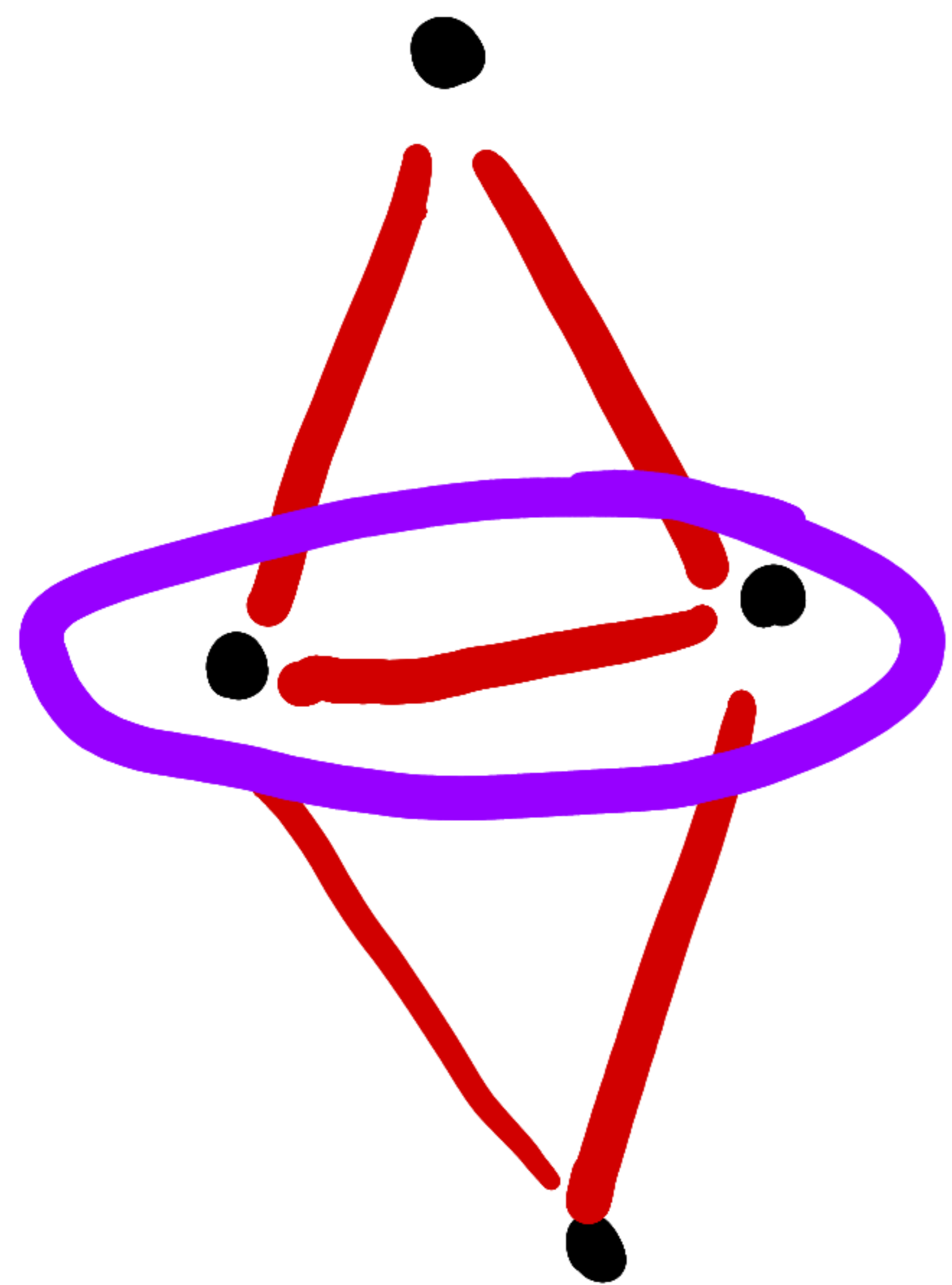


$d \log z$

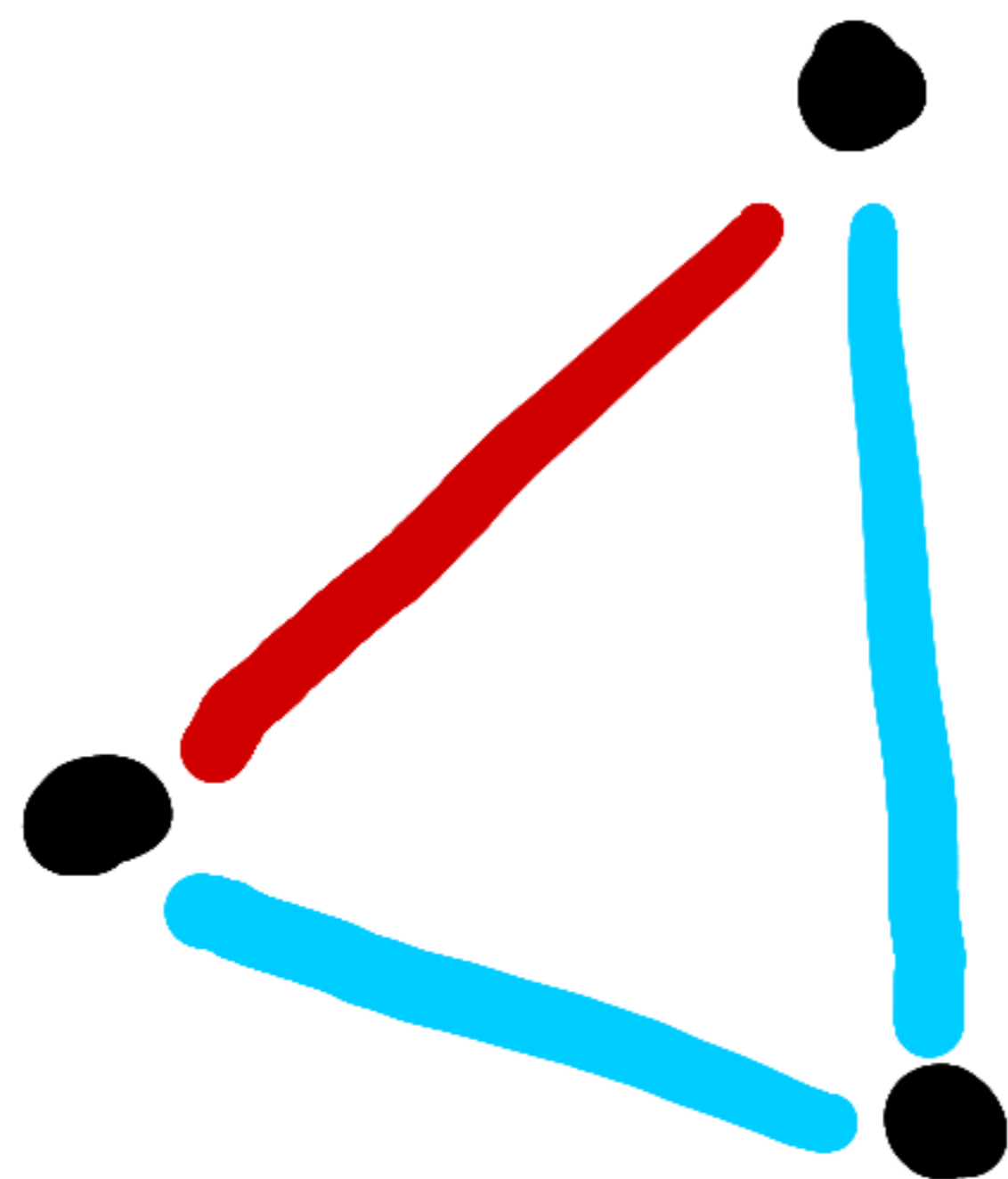
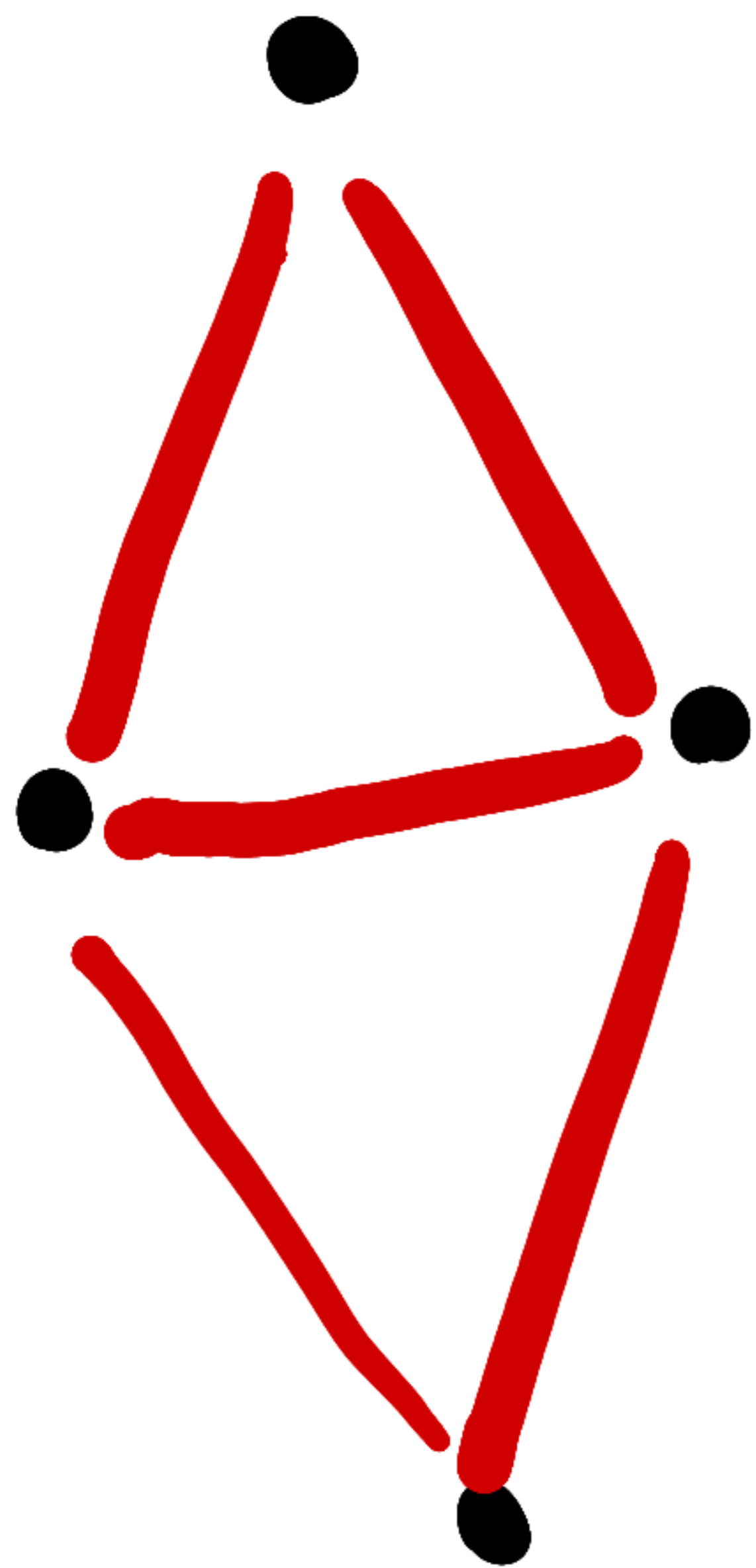


x

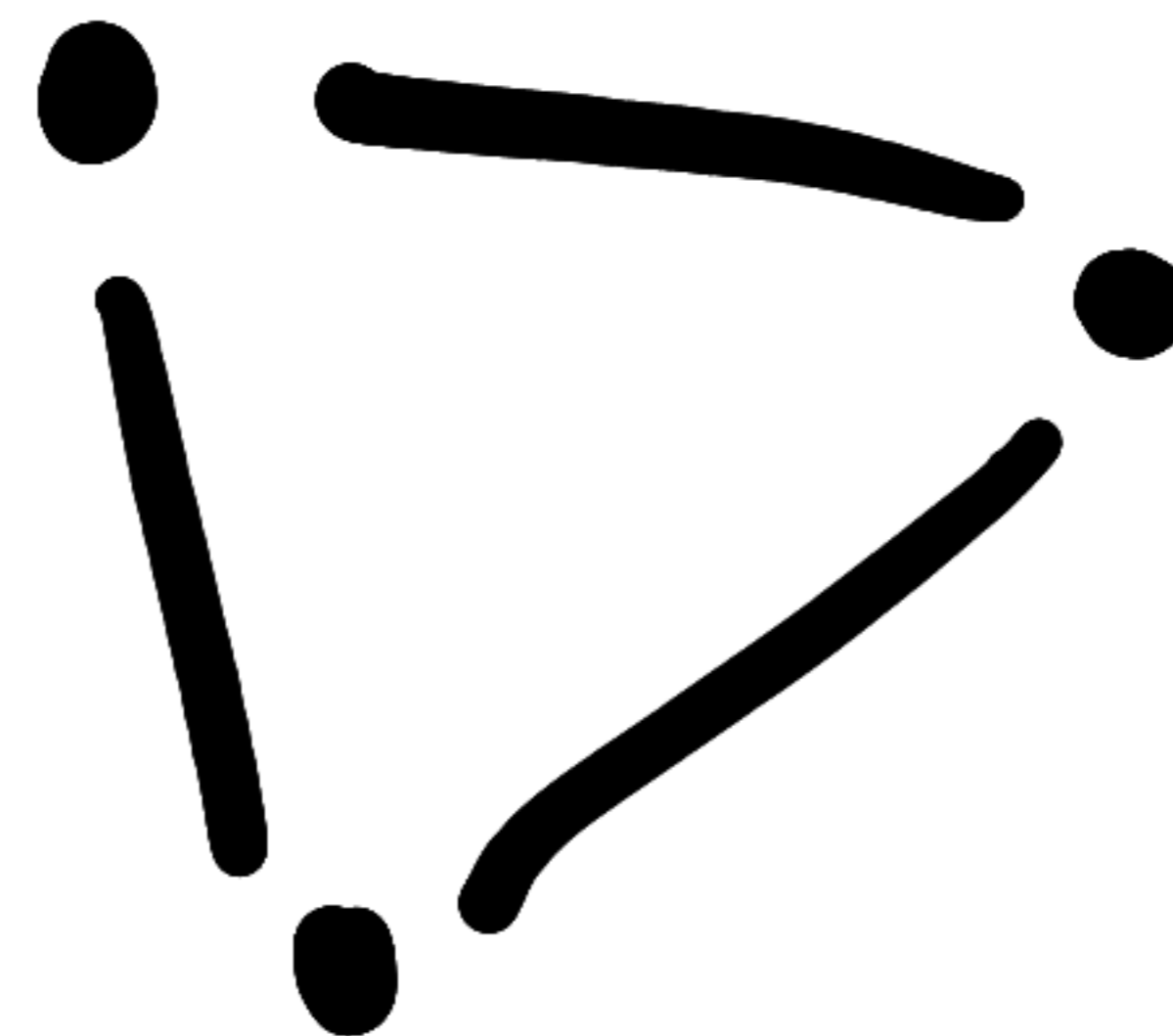
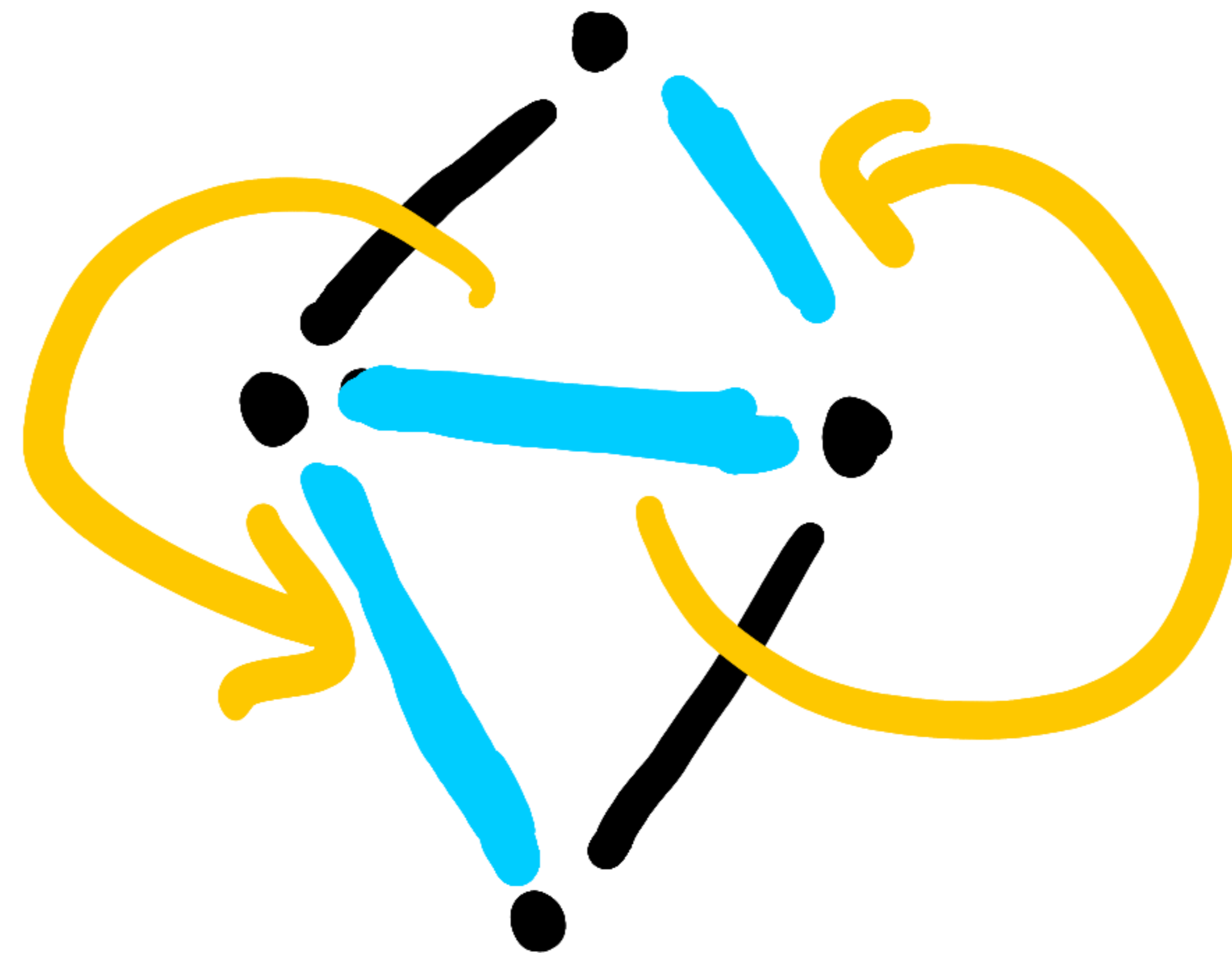
$d \log z$



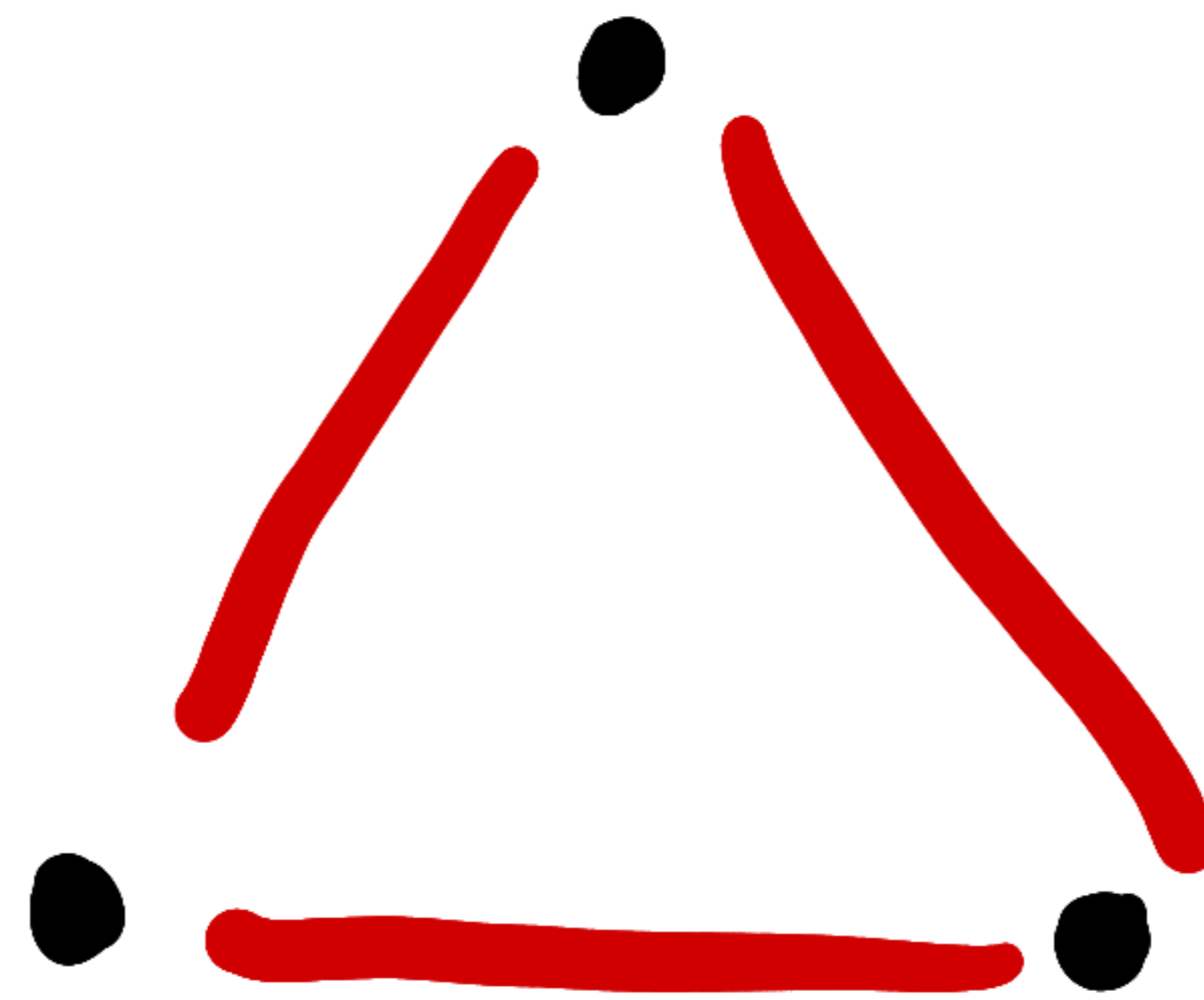
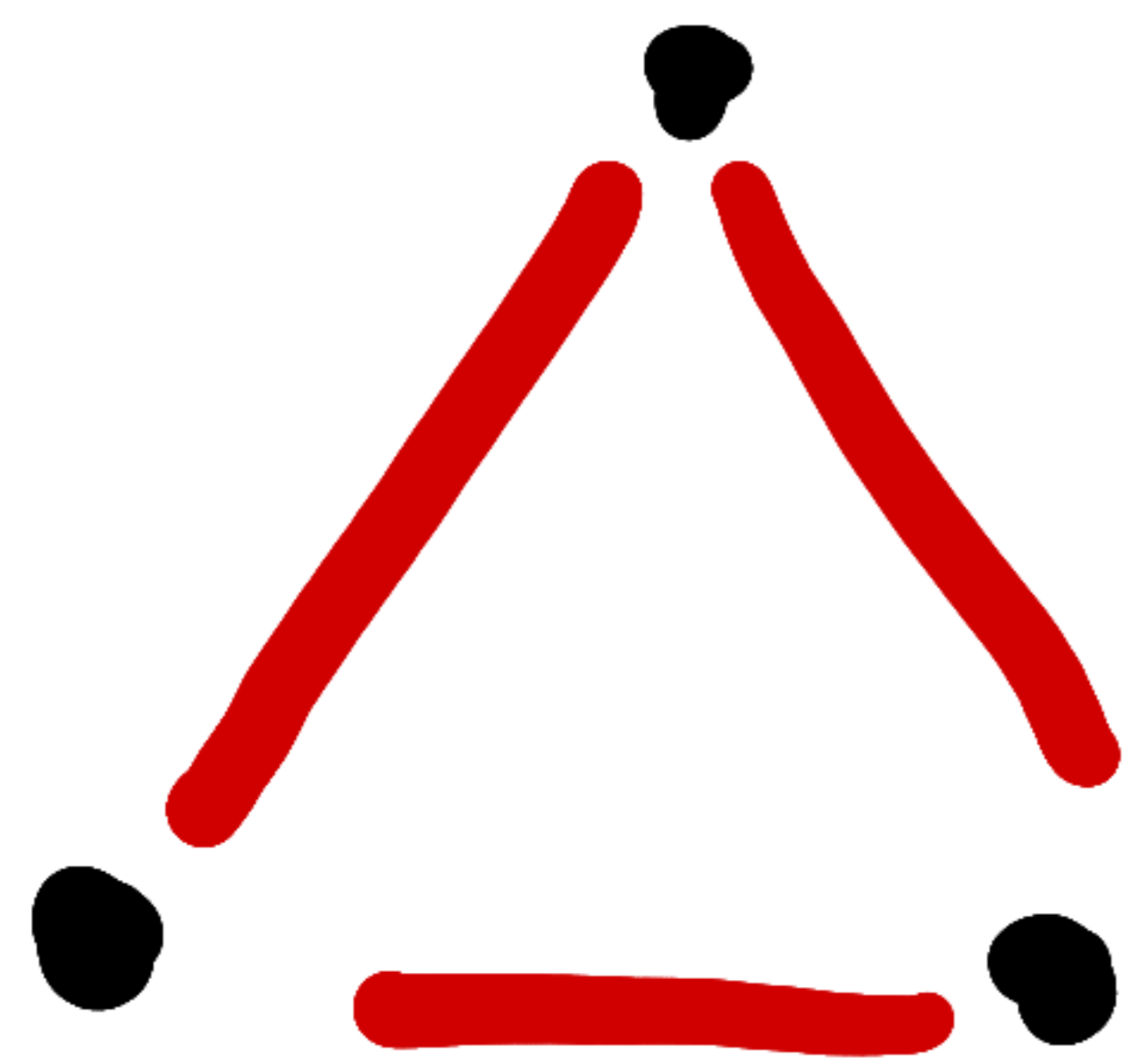
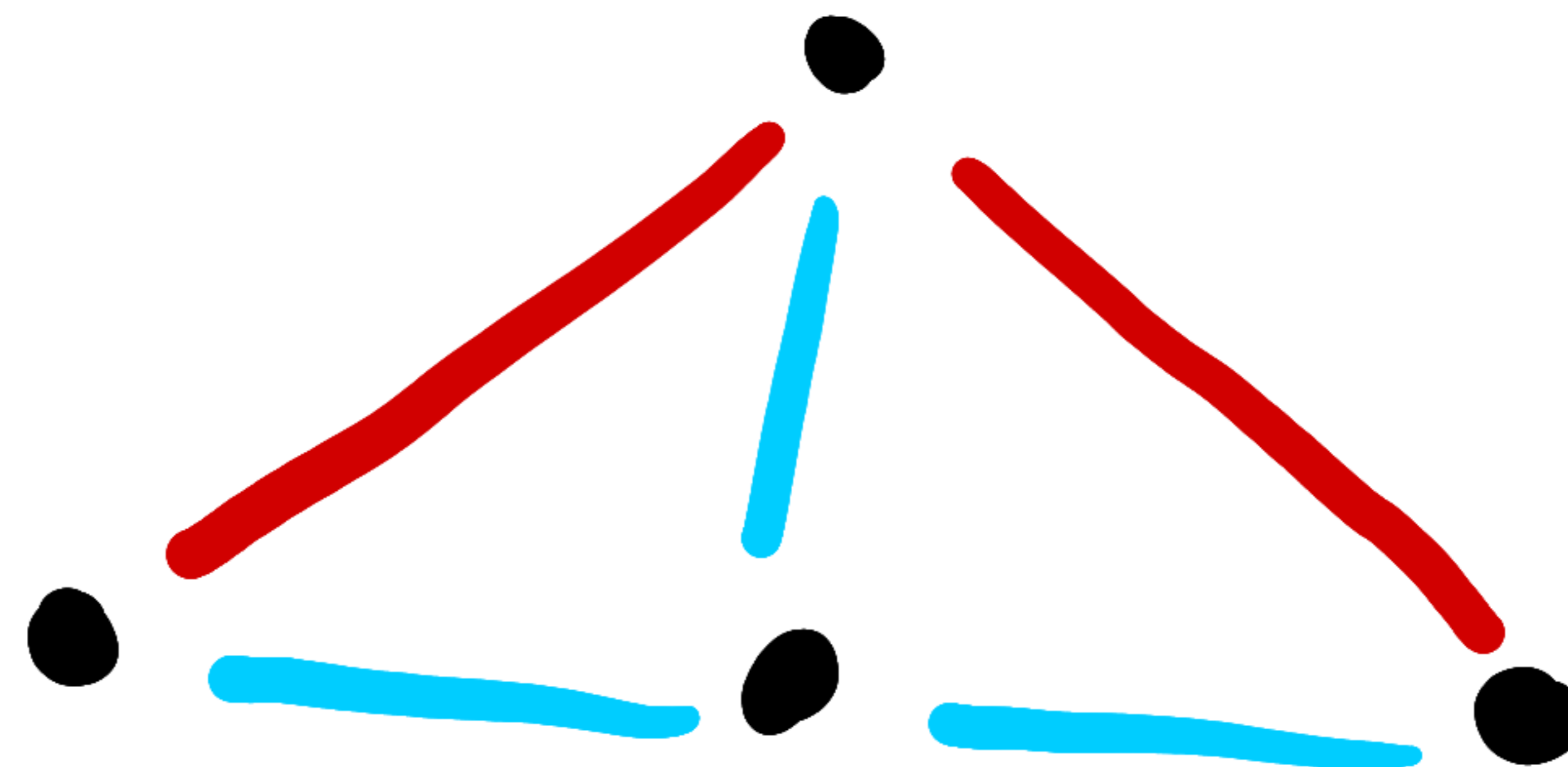
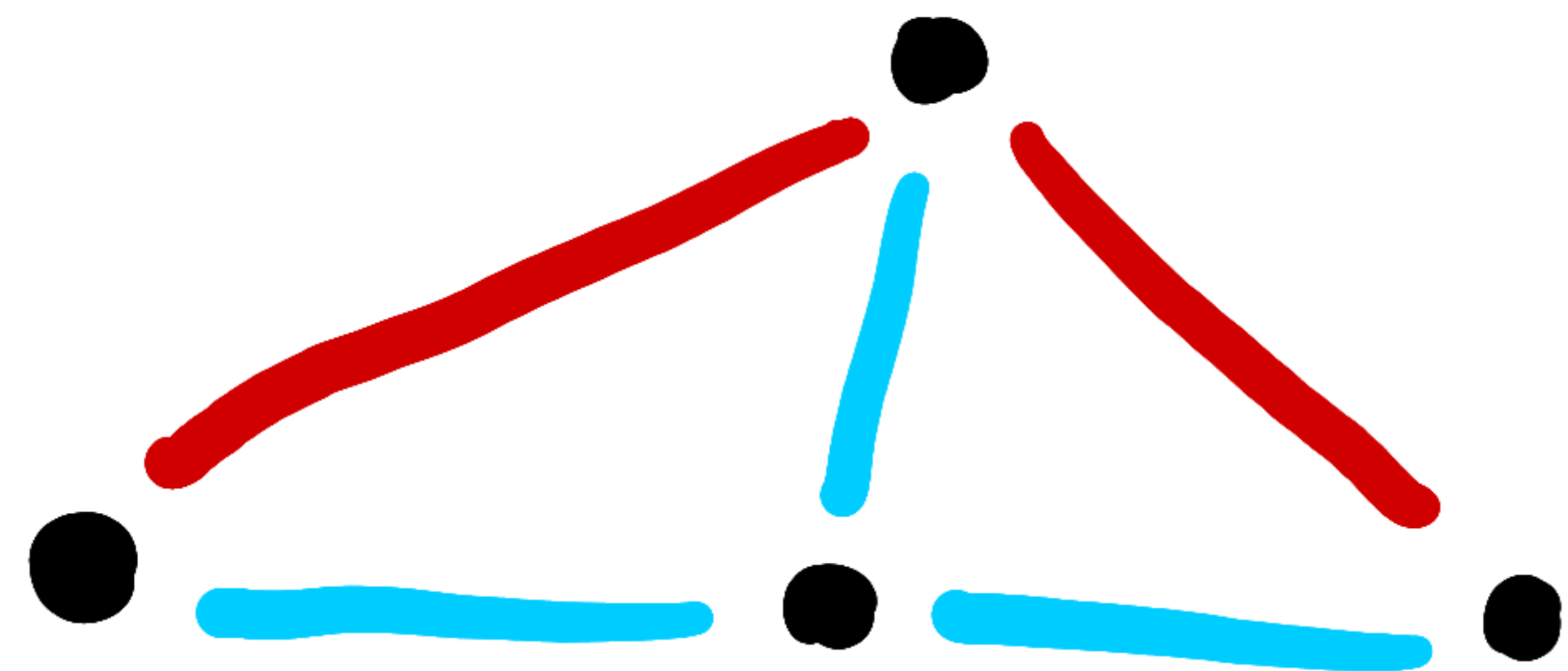
x



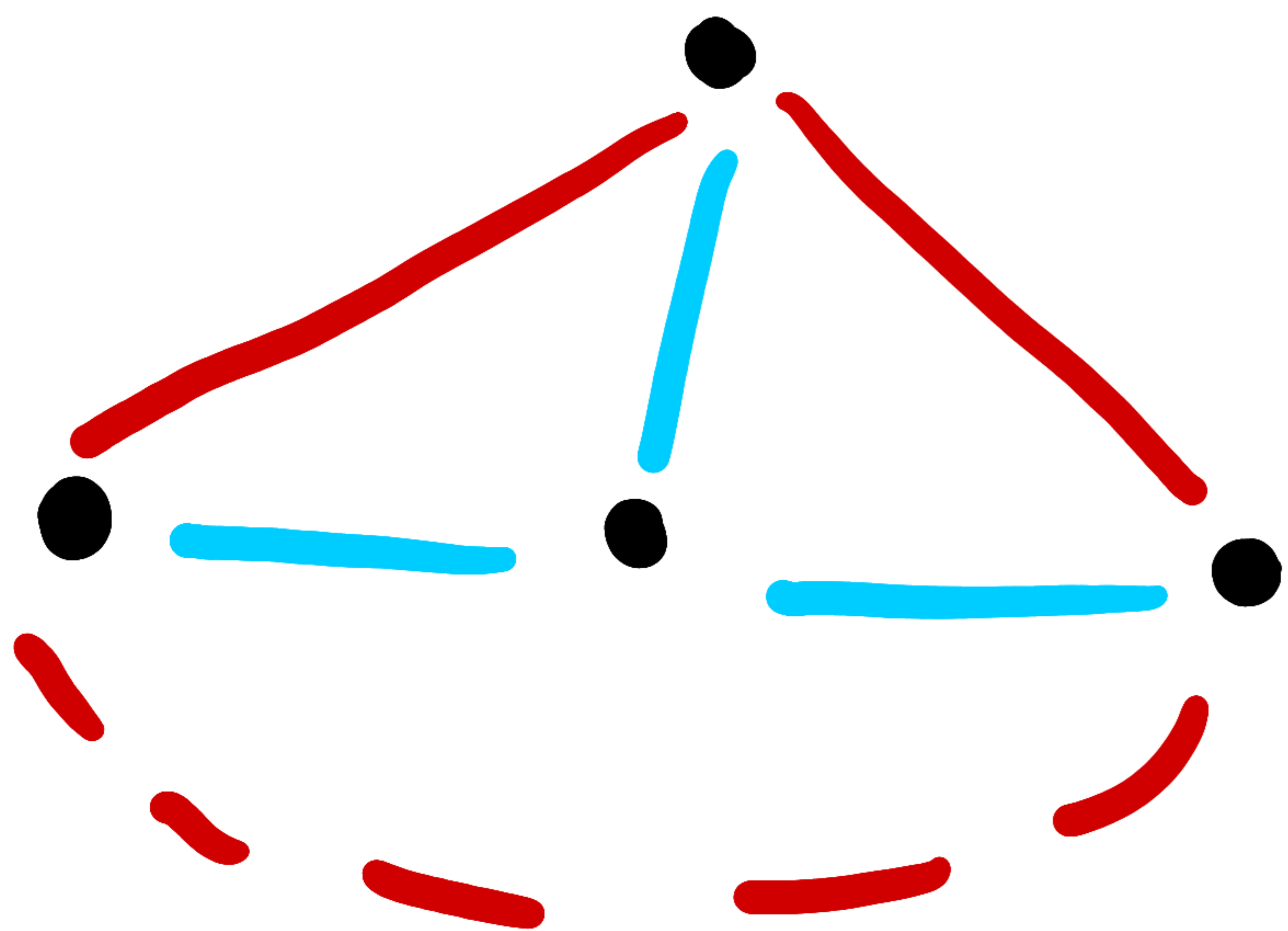
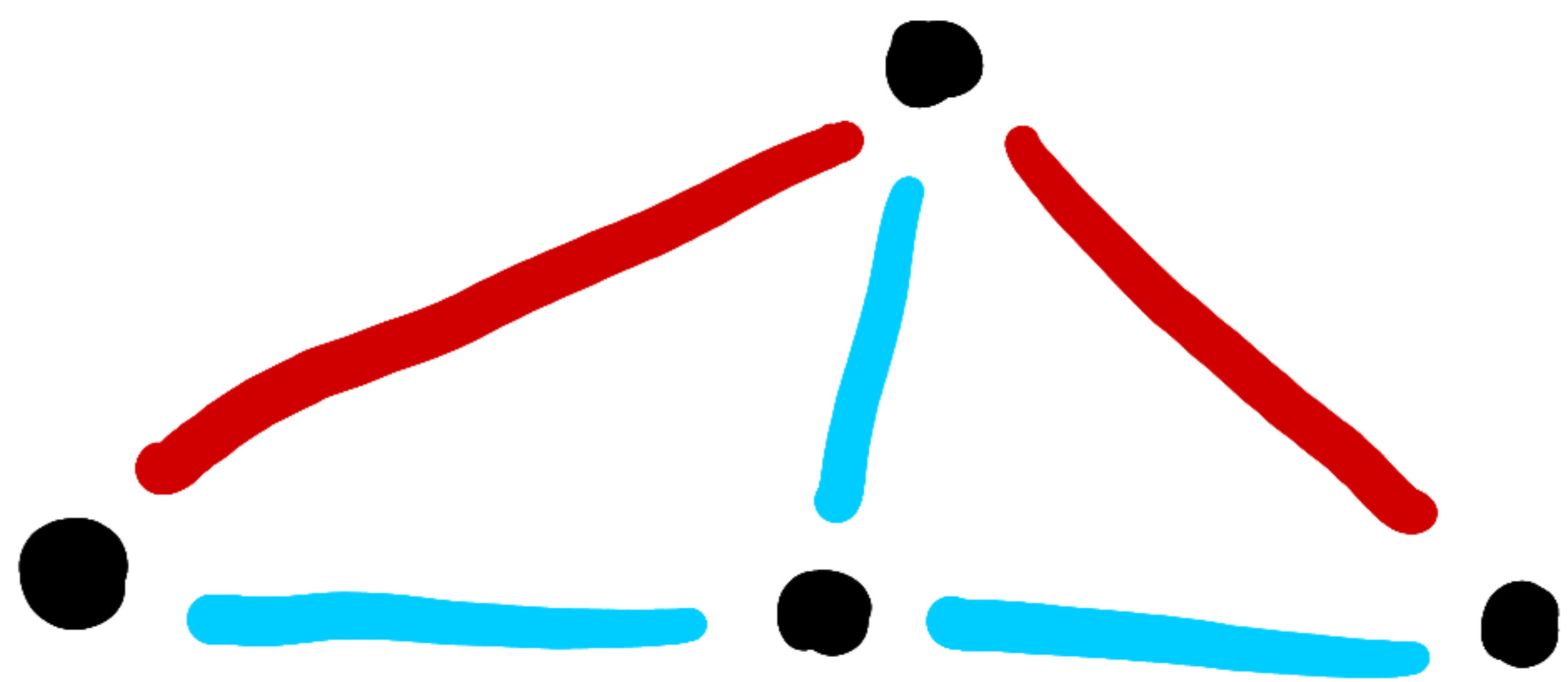
$d \log n$



Sharing Triangle "Sides"



Bounding



← can't happen "too often"
by combinatorics

Summary

- [AO'00] efficient partially blind signature scheme

Summary

- [AO '00] efficient partially blind signature scheme
- Mending some gaps in proof

Summary

- [AO '00] efficient partially blind signature scheme
- Mending some gaps in proof
- Similar reduction loss to original work

Summary

- [AO '00] efficient partially blind signature scheme
- Mending some gaps in proof
- Similar reduction loss to original work
 - ↳ Small nr of signing sessions

Summary

- [AO '00] efficient partially blind signature scheme
- Mending some gaps in proof
- Similar reduction loss to original work
 - ↳ Small nr of signing sessions

Open Questions

- Schemes with polynomial nr of signing sessions?
 - ↳ overcome loss

Summary

- [AO '00] efficient partially blind signature scheme
- Mending some gaps in proof
- Similar reduction loss to original work
 - ↳ Small nr of signing sessions

Open Questions

- Schemes with polynomial nr of signing sessions?
 - ↳ candidate: [Abe 01]