

# A Modular Approach to the Incompressibility of Block-Cipher-Based AEADs

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# Backgrounds

# Black-Box Model

Attacker

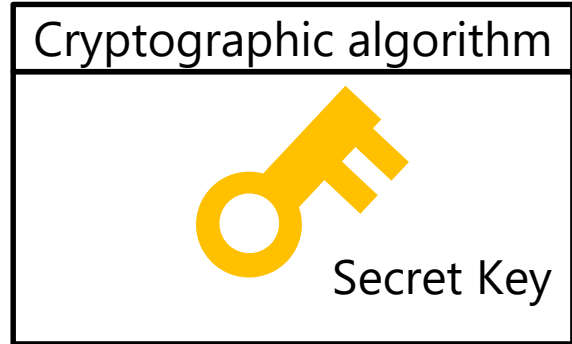


Query



Response

## Black-Box



No direct access to the implementation of the algorithm

# Real-World Threats

Attacker



Query

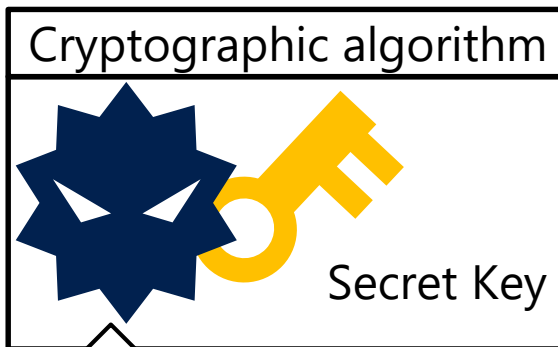


Response



Information  
(leakage)

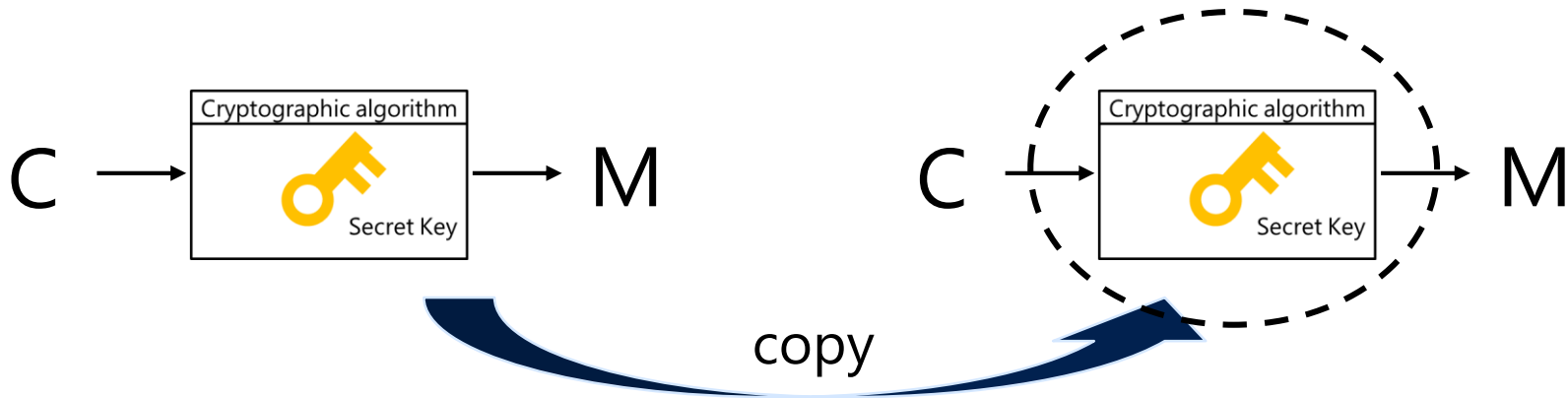
## Black-Box



Malware w/  
full access to the  
implementation

# White-Box Cryptography [Chow et al. 2002]

- Technique to protect data against attackers who may have **full direct** access to implementations of cryptographic algorithms
- Requirement: Resistance against **key extraction** and **code lifting**
  - Key extraction...an attack to recover the secret key
  - Code lifting...an attack to copy the entire implementation



# Incompressibility [Delerablée et al. 2013]

- Security notion against code lifting
- Hardness of compressing cryptographic implementations while keeping functionality
  - An encryption algorithm  $E_K$  is compiled to a large (e.g., 10GB) program  $\mathbf{P}[E_K]$
  - $\mathbf{P}[E_K]$  is *incompressible* if, even if  $\mathbf{P}[E_K]$  is given, it's hard to build a smaller program that is functionally equivalent to  $\mathbf{P}[E_K]$
  - Incompressible  $\Rightarrow$  hard for malwares to leak useful information
  - Many variants exist (ENC-COM [Fouque et al. 2016], SPACE-Hardness [Bogdanov-Isobe 2015], etc.)
- Achievable without relying on special secure hardware
  - There exist high demands for software-only solutions in various scenarios (e.g., cloud-based payment services) [Bogdanov et al. 2016]

# Motivation of Research

- There exist secure & efficient incompressible BCs, but no modes of operation to convert them into incompressible AEADs
  - GCM [MV04] is *not* incompressible even if instantiated with an incompressible BC: Once the hashing key for GHASH is leaked, universal forgery is possible
  - Similar attacks also work for CCM [WHF02], OCB [KR11], GCM-SIV [GL15],...
- There is no incompressible AE scheme achieving both of confidentiality & authenticity (w/o special hardware, when  $\exists$  leakage)
  - Can't we reduce incompressibility-like security notions of an AEAD mode to those of BCs?
- New security notions are necessary
  - For both of BCs and AEADs...because existing security notions do not seem suitable for reductions from AEADs to BCs
  - Authenticity notions achieved so far in the white-box setting are only (a kind of) universal unforgeability, much weaker than black-box model

- New white-box security notions for AEAD/BC/PRF/etc.
- A weak variant of public indifferentiability implies reduction
- SIV w/ Sponge & CTR is a white-box secure AEAD mode of BCs
  - Secure up to  $2^{n/4}$  black-box queries (n : block length of BC)
- New white-box-secure 256-bit block cipher, "SPACE256-16"
  - Variant of SPACE-16 [Bogdanov-Isobe 2015]
  - We conjecture it is secure (w.r.t. our new incompressibility security notion)
- Model & Assumption
  - Malwares can be detected if they consume lots of computational resources / send huge data outside
  - No assumptions on hardware





# New Security Notions

# How to Define Security Notions for AEADs?

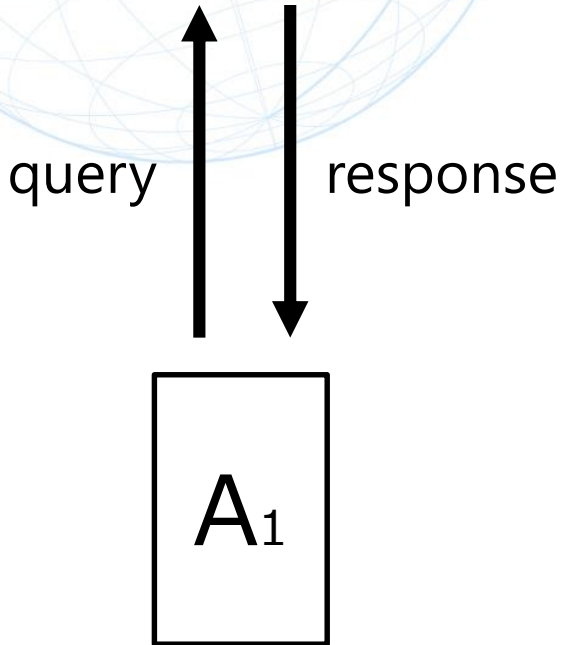
- Real-Ideal distinguishing games
  - Like various conventional AEAD security notions
- Limits on the amount of leakage / malware running time
  - expecting malware can be detected if the leakage / running time are large
- Security **after** code lifting (= after malware stops)
  - no security is guaranteed during code lifting
- Leakage means nonce-repeat
  - Malware may leak valid plaintext-ciphertext pairs under some nonces that haven't been queried by the attacker, so nonce-misuse resistance is necessary
- We cannot prohibit the attacker to forward outputs from the encryption oracle to the decryption oracle

We extend the **Pseudo Random Injection (PRI) security** [RS06]  
Ideal object: Random Injection (and its inverse)

# Real World

Black-box oracle

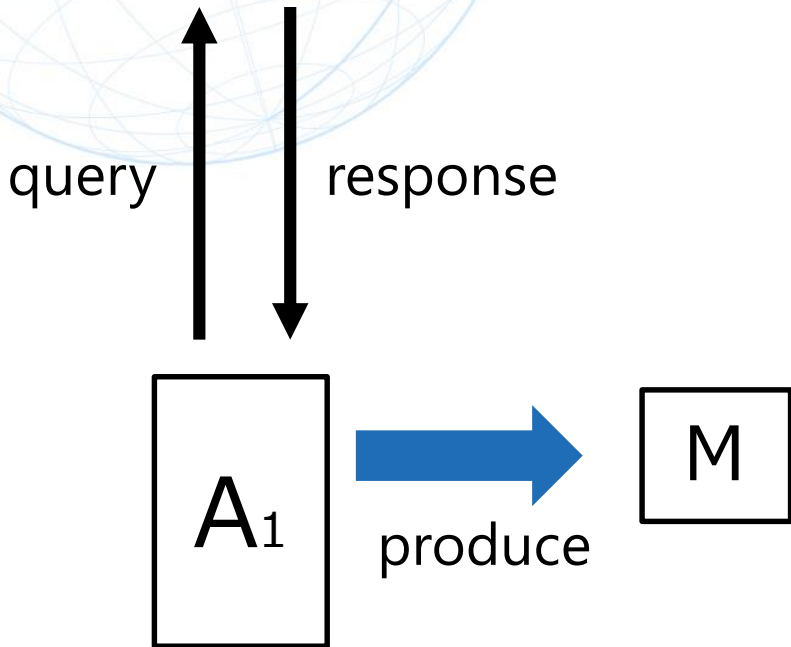
$Enc_K / Dec_K$



# Real World

Black-box oracle

$Enc_K / Dec_K$



# Real World

Black-box oracle

$Enc_K / Dec_K$

White-Box  
Implementation

query

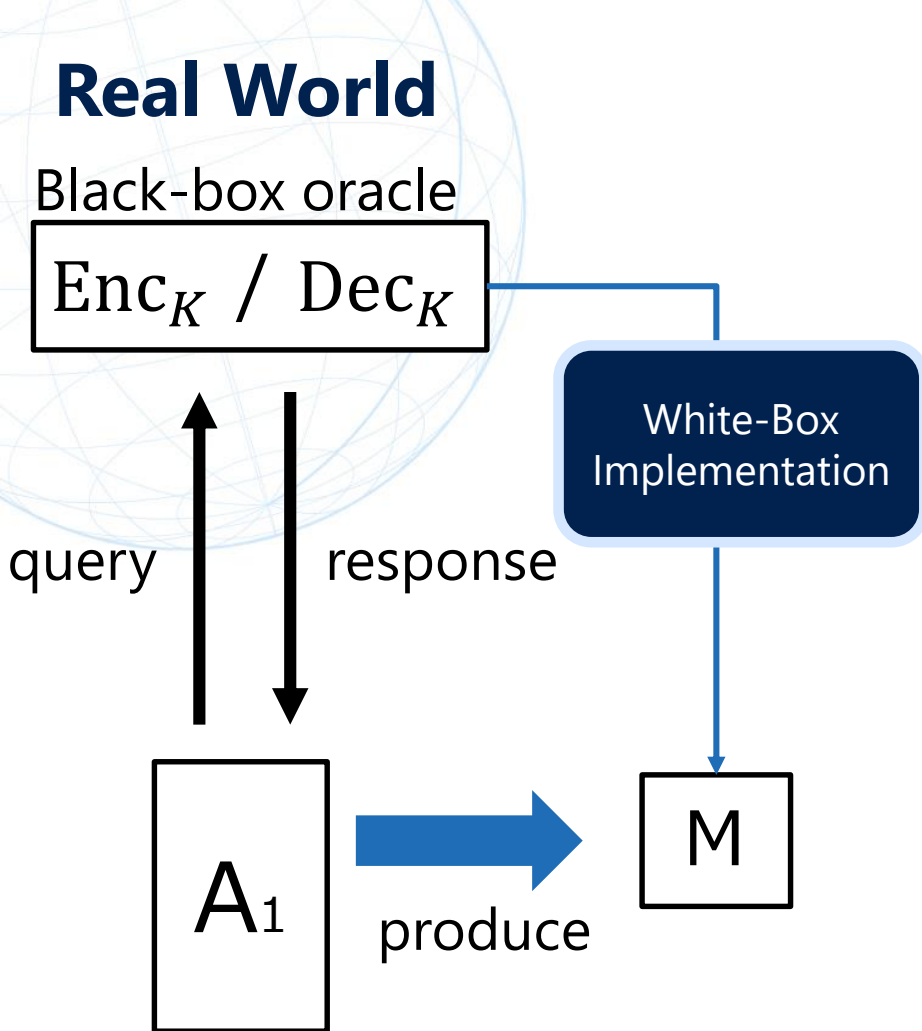
response

$A_1$



produce

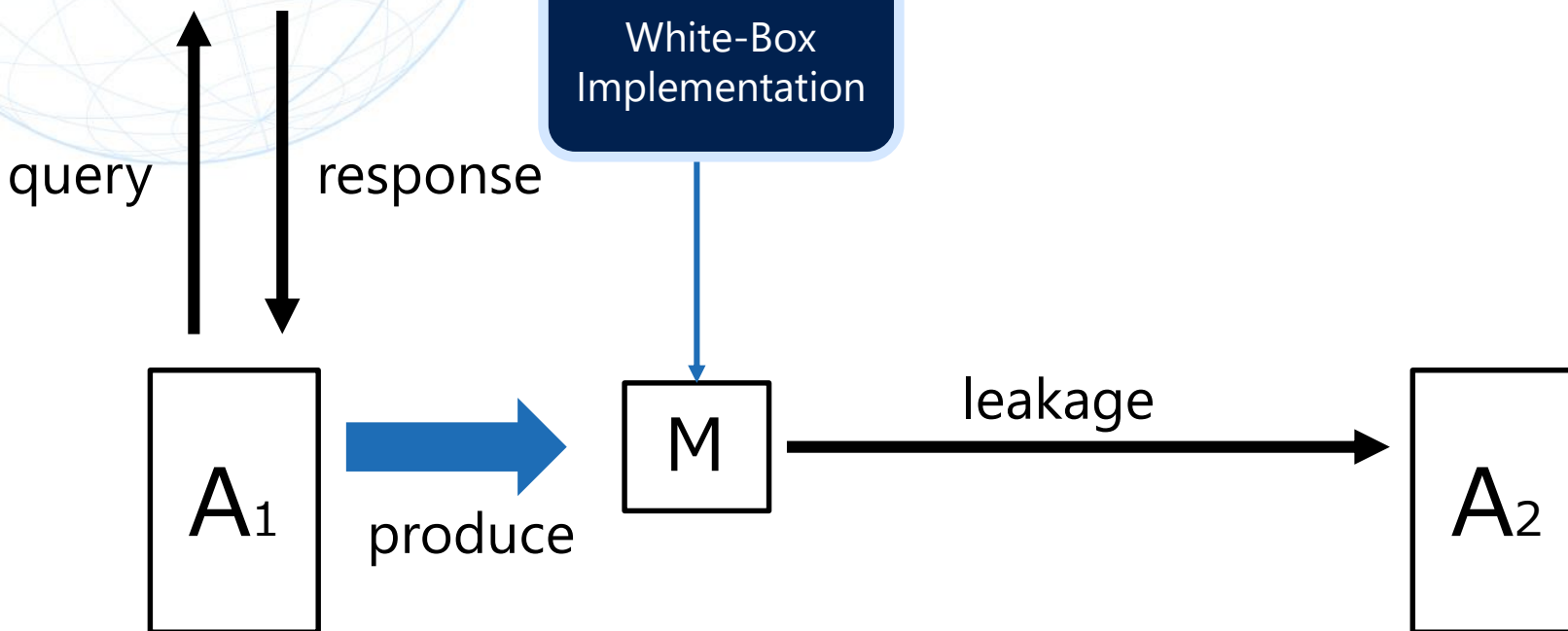
M



# Real World

Black-box oracle

$Enc_K / Dec_K$

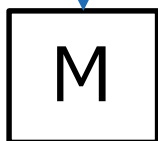
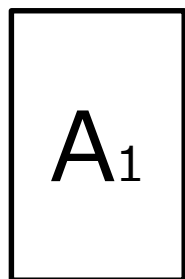
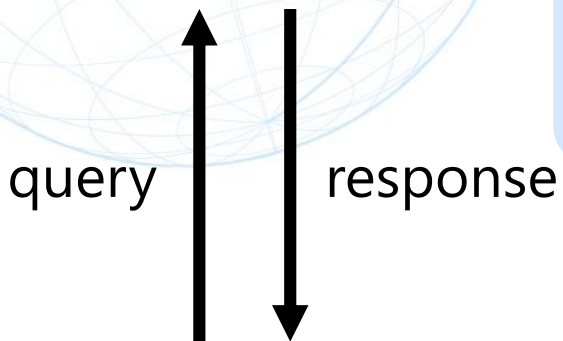


# Real World

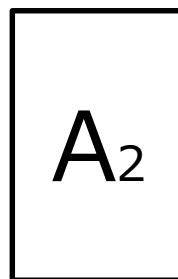
Black-box oracle

$Enc_K / Dec_K$

White-Box  
Implementation



leakage



# Real World

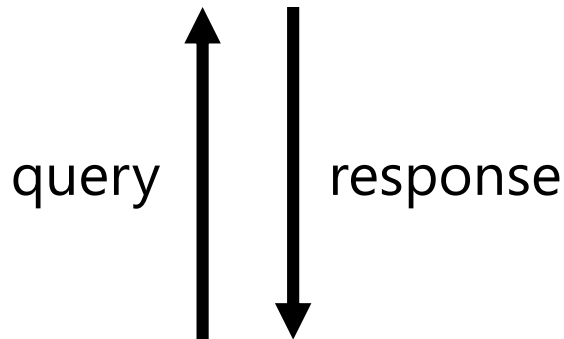
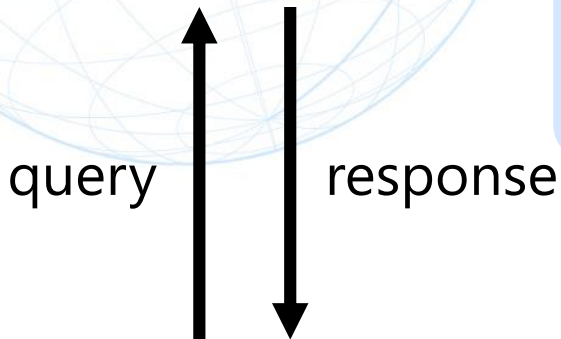
Black-box oracle

$Enc_K / Dec_K$

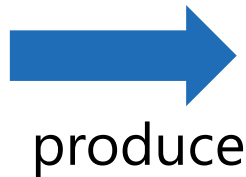
Black-box oracle

$Enc_K / Dec_K$

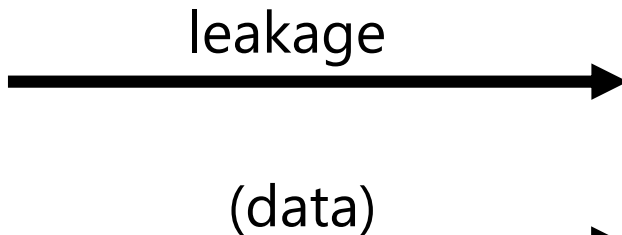
White-Box Implementation



$A_1$



M



$A_2$



# Real World

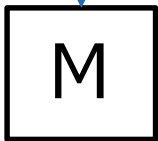
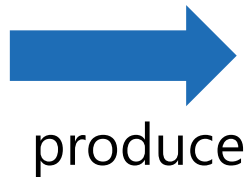
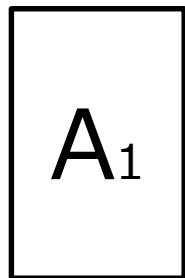
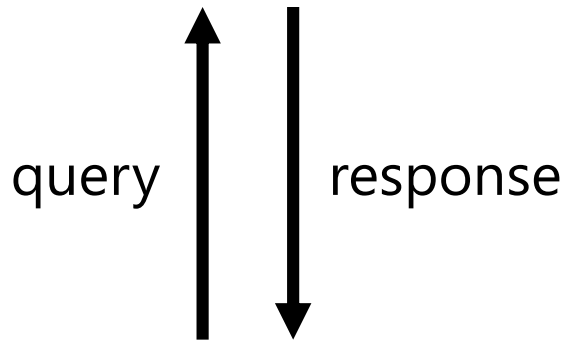
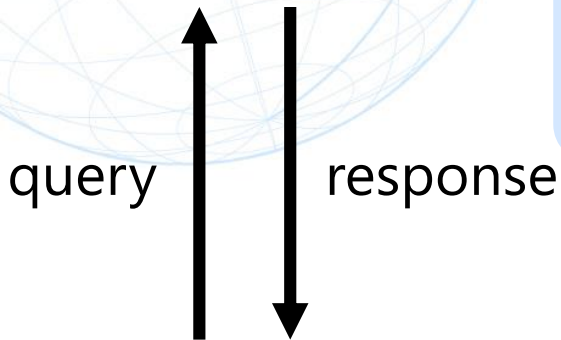
Black-box oracle

$Enc_K / Dec_K$

Black-box oracle

$Enc_K / Dec_K$

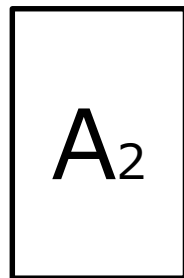
White-Box Implementation



leakage



(data)

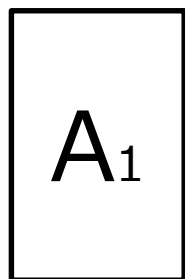
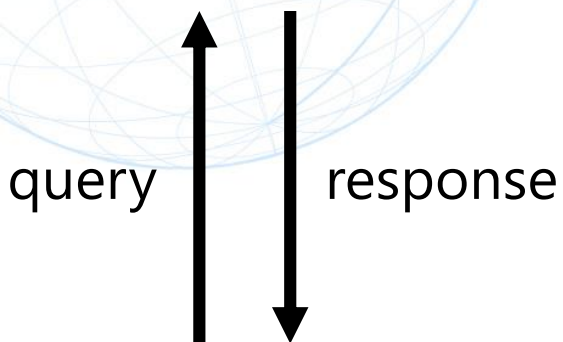


output

# Ideal World

Random Injection

$$F / F^{-1}$$

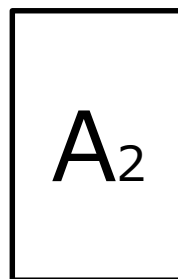
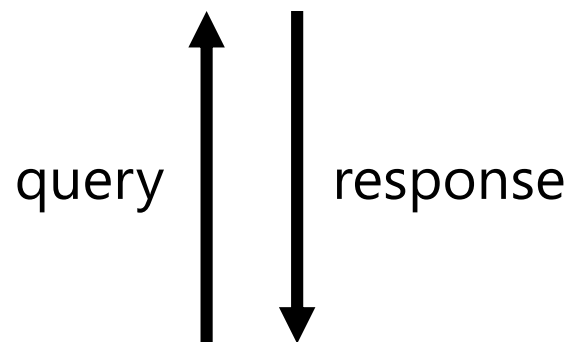


produce



Random Injection

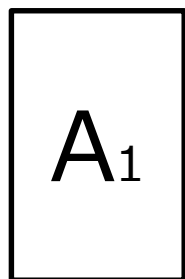
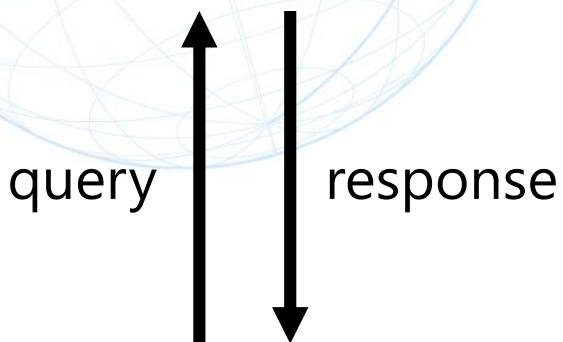
$$F / F^{-1}$$



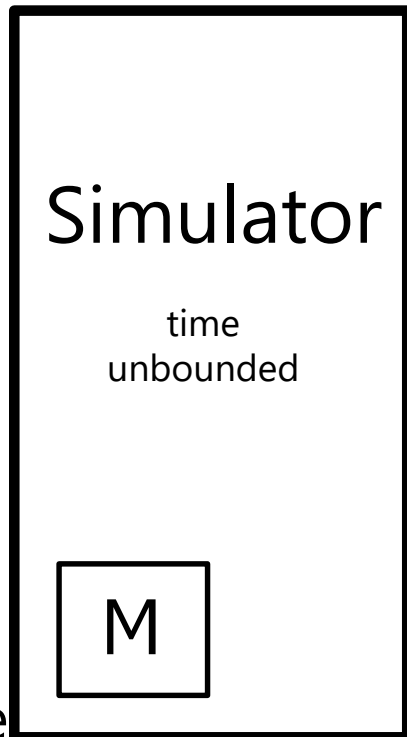
# Ideal World

Random Injection

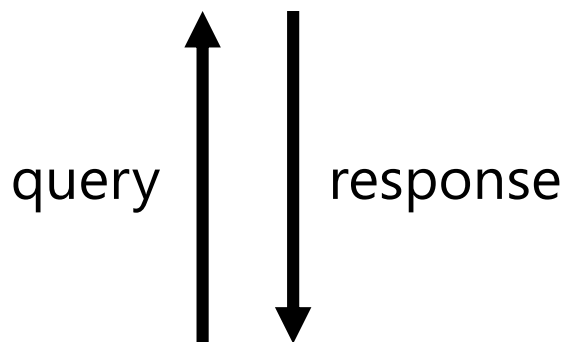
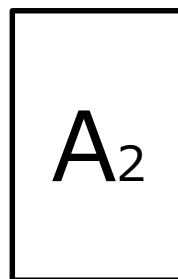
$$F / F^{-1}$$



produce



(data)

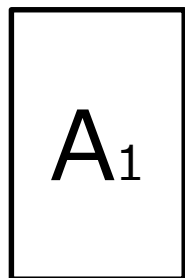
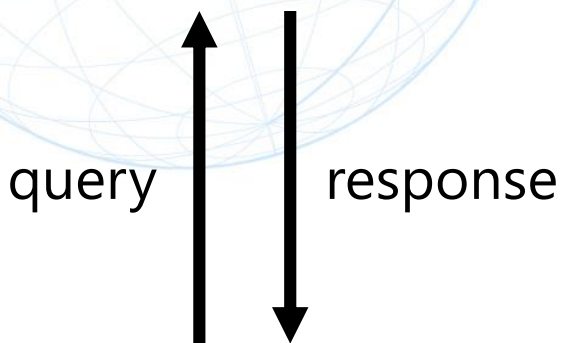
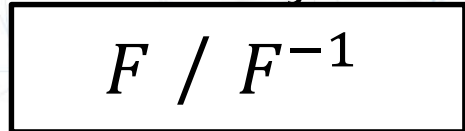


Random Injection

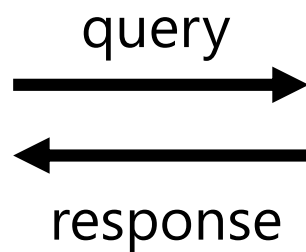
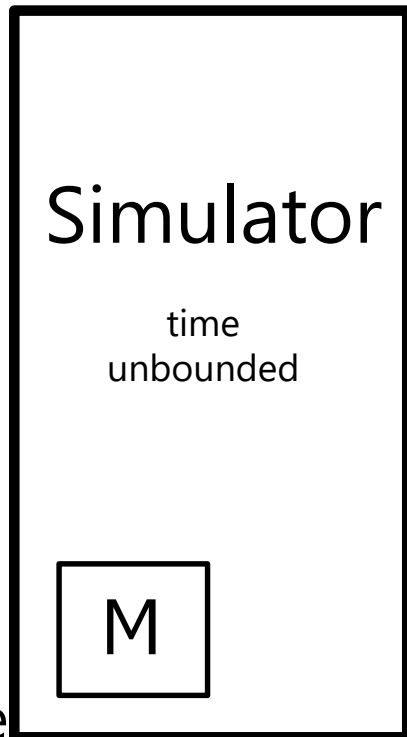
$$F / F^{-1}$$

# Ideal World

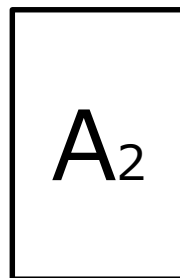
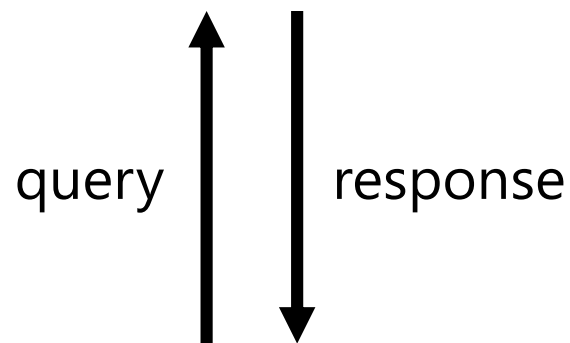
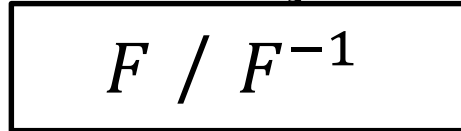
Random Injection



produce

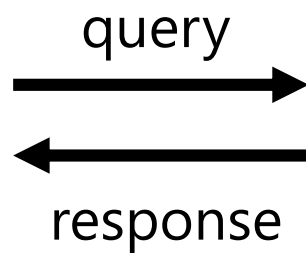
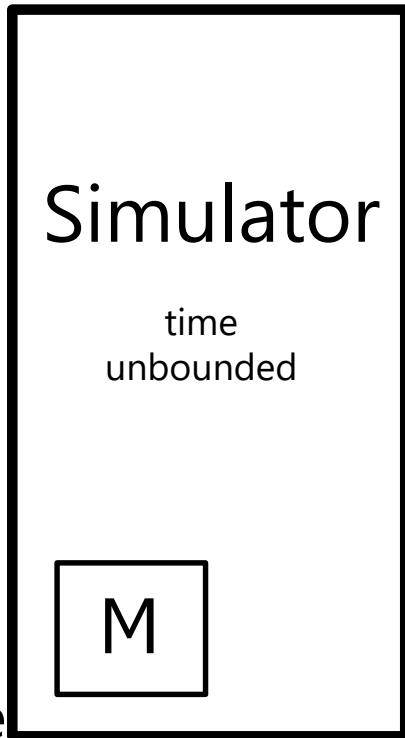
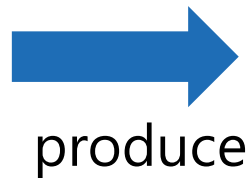
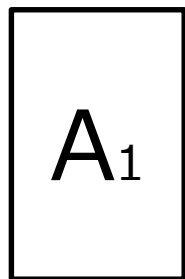
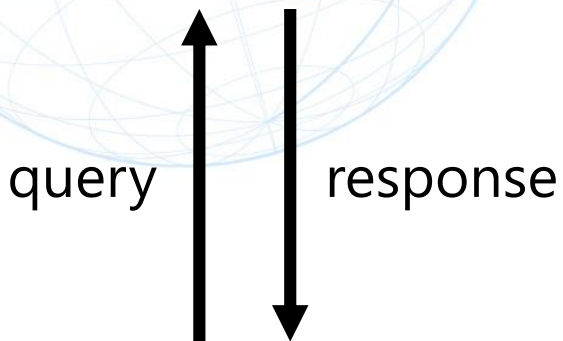
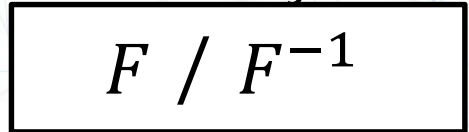


Random Injection

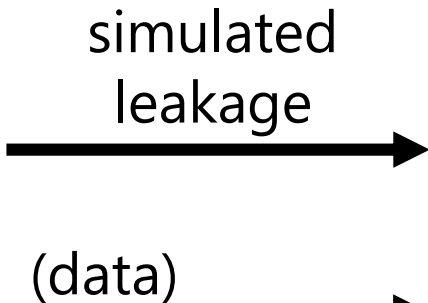
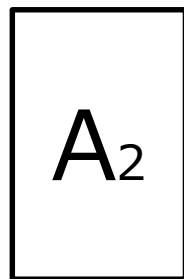
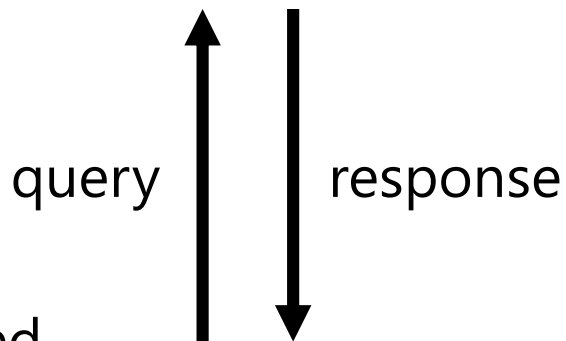
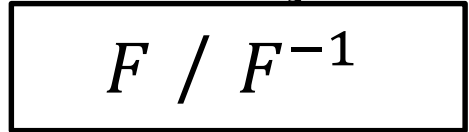


# Ideal World

Random Injection

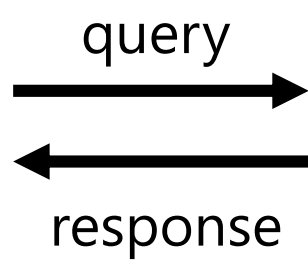
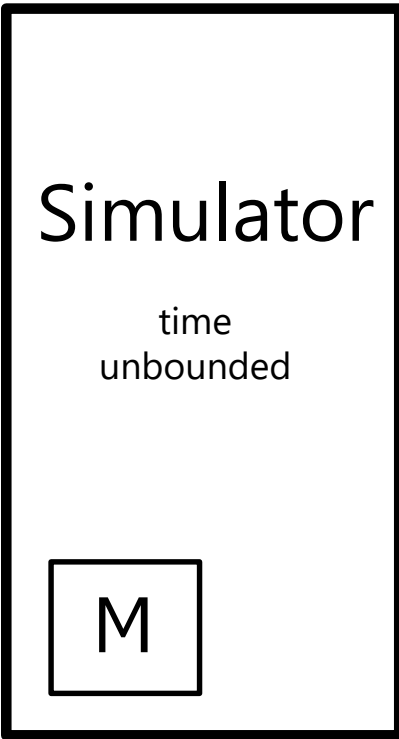
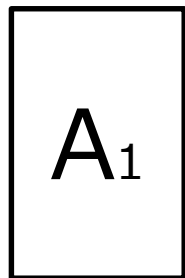
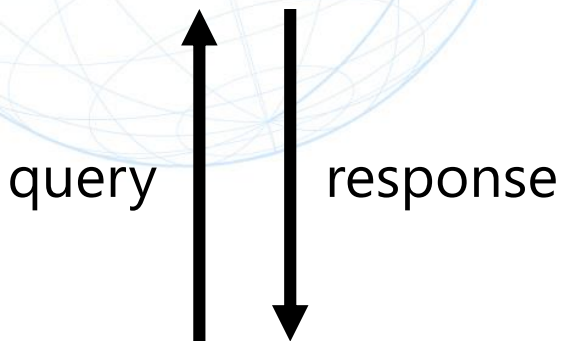
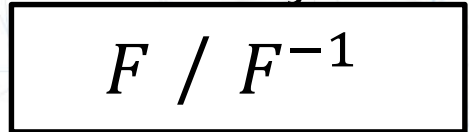


Random Injection

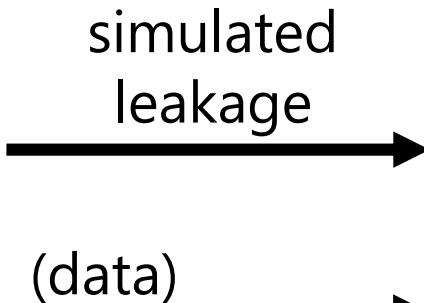
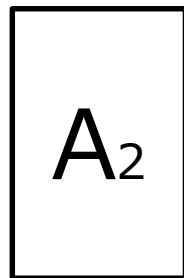
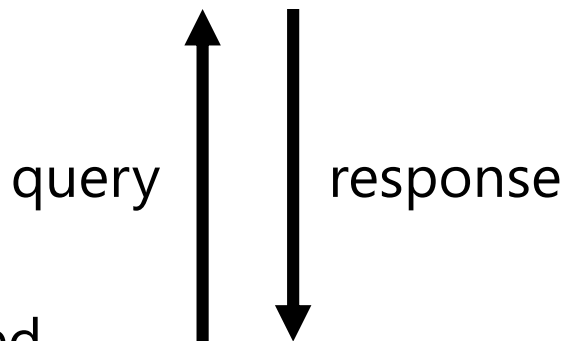
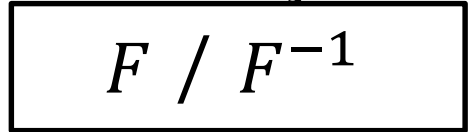


# Ideal World

Random Injection



Random Injection



# Security Notion for AEADs : whPRI

We say an AEAD scheme is *whPRI-secure* if

- For any "efficient"  $A = (A_1, A_2)$ ,
- there exists a time-unbounded simulator  $S$  making "reasonable amount of" queries to  $F / F^{-1}$  s.t.

$$Adv_S^{whPRI}(A) := \Pr[\text{Game-Real} \Rightarrow 1] - \Pr[\text{Game-Ideal} \Rightarrow 1]$$

is small

# Interpretation of whPRI-security

$\exists$  simulator s.t. Adv becomes small



$\lambda$ -bit leakage by malware can contain only  $\lambda$ -bit information of valid plaintext-ciphertext pairs



The implementation is incompressible  
privacy & authenticity lost by  $\lambda$ -bit leakage is only  $\lambda$ -bit



# Security Notion for other schemes

- Security notions for other schemes (BCs, keyed functions,...) are similarly defined
- The new notion for BCs : “whPRP” (extension of PRP security)
- **Conjecture**: The **SPACE cipher** [Bogdanov-Isobe 2015] is whPRP-secure w.r.t. some reasonable parameters
- **Our Goal**: Reduce whPRI-security of an AEAD mode of BCs to whPRP-security of a BC (e.g., SPACE)

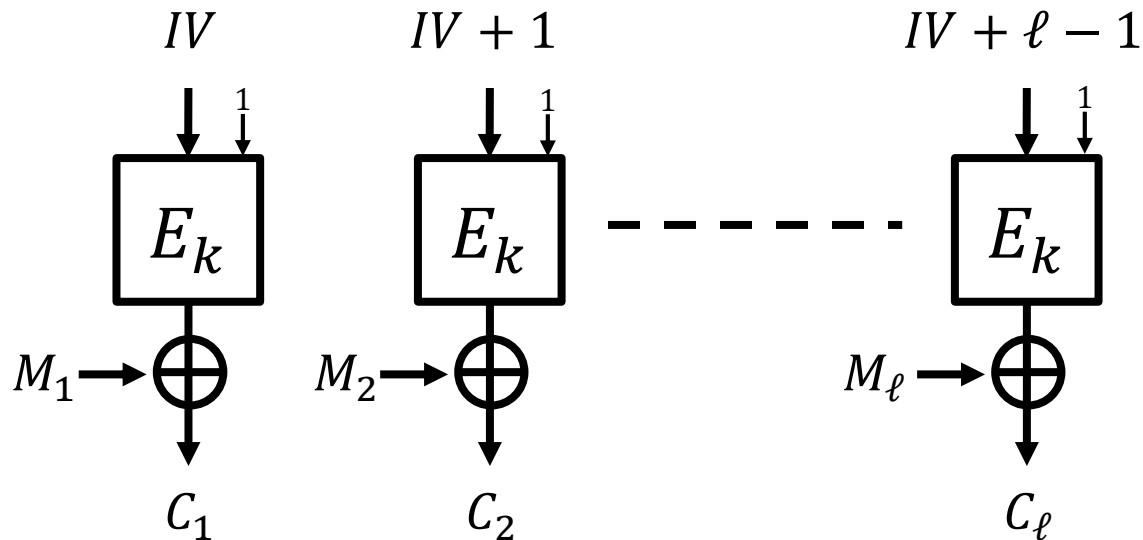
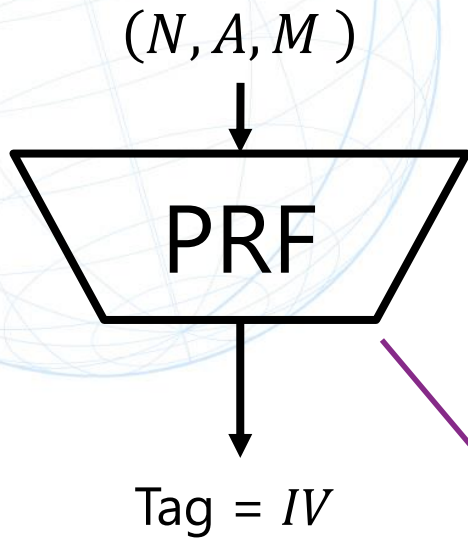
## (Some variants of) Indifferentiability Implies Reductions **NTT**

- The structure of a scheme is indifferentiable from the random object (when the primitive is ideally random)
  - ⇒  $\exists$  reductions between new white-box security notions
- In fact some weaker variants of indifferentiability are sufficient to show reductions
  - public indifferentiability [Dodis et al. 2009] [Yoneyama et al. 2009]
  - “**weak public indifferentiability**” (new!)

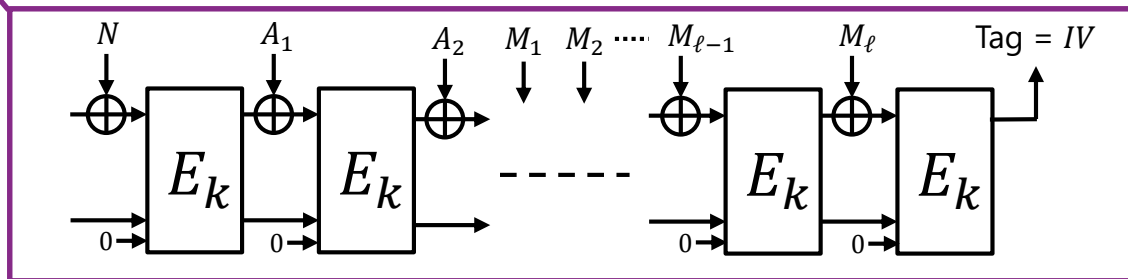


# **Incompressible AEAD Mode of BCs & New Incompressible BC**

# SIV [RS06] with Sponge [BDPV08] Based PRF + CTR NTT



The structure is public indifferentiable from a random injection!



# 256-bit Block Variant of SPACE Cipher

- (Very roughly,) the mode is secure up to  $2^{n/4}$  black-box queries
- SPACE cipher seems to be whPRP-secure, but  $n=128$ 
  - The security of the resulting AEAD is only up to  $2^{32}$  complexity
- SPACE256-16 : a new 256-bit block cipher
  - Based on SPACE(-16) [Bogdanov-Isoobe 2015]
  - The resulting AEAD becomes secure up to  $2^{64}$  complexity
  - We conjecture it is secure if {query, malware time}  $\ll 2^{64}$  & leakage  $\ll 2^{20}$
- The resulting AEAD (w/ SPACE256-16) is practical :  $\approx 530$  cycle/B
  - Intel platform, 1KB message
  - Not so much worse than raw SPACE-16 (305.11 cycle/B) [Bogdanov et al. 2016]



# Summary

# Summary

- New white-box security notions for AEAD/BC/PRF/etc.
- A weak variant of public indifferentiability implies reduction
- SIV w/ Sponge & CTR is a white-box secure AEAD mode of BCs
  - Secure up to  $2^{n/4}$  black-box queries (n : block length of BC)
- New white-box-secure 256-bit block cipher, "SPACE256-16"
  - Variant of SPACE(-16)
  - We conjecture it is secure (w.r.t. our new incompressibility security notion)
- Model & Assumption
  - Malwares can be detected if they consume lots of computational resources / send huge data outside
  - No assumptions on hardware

Thank you!