Group Signatures and More from Isogenies and Lattices: Generic, Simple, and Efficient

#### Yi-Fu Lai<sup>2</sup> Joint work with

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#### Eurocrypt2022

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Introduction

Preliminaries

**Technical Overview** 

Results







#### Introduction

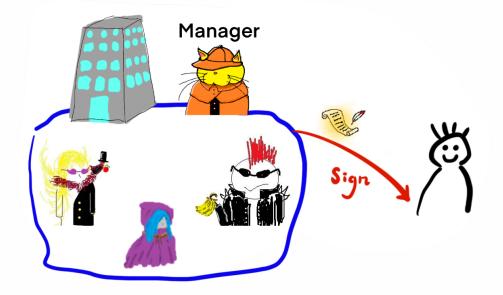
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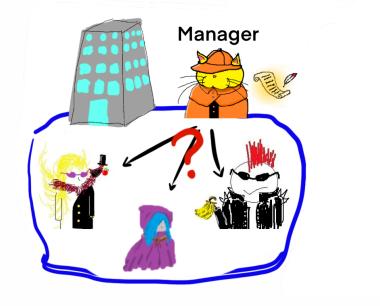
## Group Signatures (GS)



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- 1. Any member in the group can sign anonymously for the group.
- In case of abuse, there is a manager (opener) who can open any signature from the group and know who is the signer and provides a proof.

The requirements for an GS  $^{1}$ :

- 1. **CCA (resp. CPA) Anonymity:** Given a signature from any two people chosen by the adversary (resp. withiout access to the opening oracle), it's impossible to tell from which of the two.
- 2. (Full) Unforgeability: Any colluding members (with the opener) cannot forge a signature not tracing to one of them.
- 3. **Traceability:** A valid signature should be able to be opened to one and only one user in the group.

### **Brief History**

- Firstly proposed by Chaum and van Heyst [CV91] by using RSA or DLP assumptions.
- It is formalized in [BMW03,BSZ05] provided with frameworks using verifiable IND-CCA PKE + signature schemes (sign-and-encrypt paradigm).
- Applications and real-world deployments: e.g. directed anonymous attestation and enhanced privacy ID ([BCC04,BL07]), also in a variety of the blockchain and cryptocurrency studies.
- Post-Quantum Proposals: LLLS13, ELL+15, LLNW16, LNWX18, KY19 etc.
- Recently, several proposals have achieved logarithmic property [BCN18, dLS18, EZS<sup>+</sup>19, ESZ22] where the signature size is logarithmic in the number of the members.

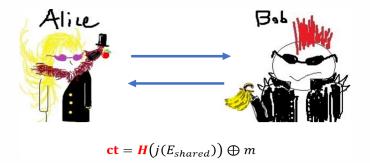


# Can we have an isogeny group signature competitive among the post-quantum proposals?

- CCA-Anonymity: The standard sign-and-encrypt technique requires IND-CCA verifiable encryption scheme (PKE) because we use
  - 1. verifiability + signature scheme  $\rightarrow$  unforgeability
  - 2. the decryption oracle (IND-CCA) to answer the opening oracle queries for CCA anonymity.

Full Unforgeability and Traceability: requires NIZK for the ciphertext and the plaintext.

However, no such practical tools in isogenies with the standard assumptions.



 Solutions: We construct a new verifiable IND-CPA PKE with online-extractable NIZK (but weakly decryptable).

- 1. A new practical framework for GS based on group actions with isogeny and lattice instantiations.
- 2. Logarithmic signature size.
- 3. Tightly secure variants for the two instantiations.
- 4. The first GS from isogenies and the only logarithmic one.
- 5. The isogeny instantiation has the smallest signature size in the literature.

Comparison with other isogeny-based group signature proposals.

Notions	Signature Size	Anonymity	Manager
			Accountable
[LD21]	$\mathcal{O}(N\log(N))$	CPA	No
[CHH <sup>+</sup> 21]	$\mathcal{O}(N^2)$	CPA	Partially
This Work	$\mathcal{O}(\log(N))$	CCA	Yes

- N: number of members.
- Manager Accountablility: Manager cannot frame an honest member.





#### Introduction

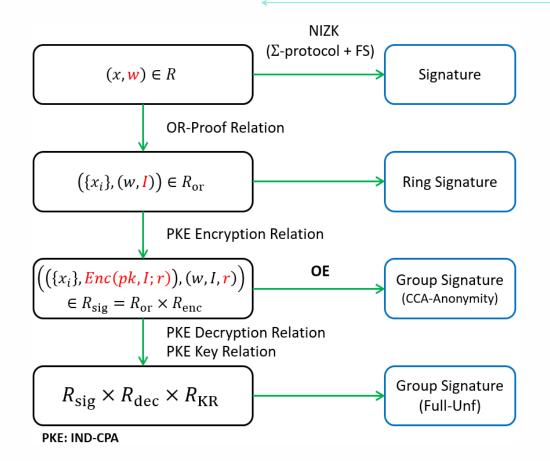
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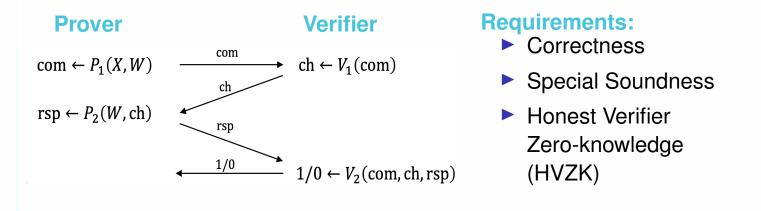
### Super High Level Idea



Let *R* be a relation and  $(X, W) \in R$ . A sigma protocol ( $\Sigma$ -protocol) for *R* is a three-move interactive protocol

 $\Pi_{\Sigma} = (P = (P_1, P_2), V = (V_1, V_2))$ 

between a prover P with (X, W) and a verifier V with X.



## **Group Actions**

A group G acts on a set X by an action  $\star : G \times X \to X$  if

- 1. Identity:  $\star(e, x) = x$
- 2. Compatibility:  $\star(g, \star(h, x)) = \star(gh, x)$

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#### Example

Let *n* be a natural number,  $G = \mathbb{Z}_n$ , and X a cyclic group of order *n*. Define  $g \star x := x^g$ .

The hardness here is based on the discrete logarithm problem over X.

CSIDH ([CLM<sup>+</sup>18,BKV19]) gives an ideal class group *G* and a set of supersingular curves  $X = E_p(O, \pi)$  such that

- G acts on X (freely and transitively),
- ►  $E_0 \in X^2$ .

$${}^{2}E_{0}: y^{2} = x^{3} + x$$

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#### **GAIP** Problem

Let  $s \leftarrow G$ . Given  $E = s \star E_0$ , it's hard to recover  $s \in G$ .

$${}^{2}E_{0}: y^{2} = x^{3} + x$$

There are two groups  $G, G_M$  both acting on a set X.

 $G_{M}$  containing the message space  $\mathcal{M}$  acts on  $\mathcal{X}$  by a public action  $\star_{M}$ .

• KeyGen gives  $pk = (\star_{pk}, X_{pk})$  and  $sk \leftarrow G$ .

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- Dec(sk, ct) is not specified.
- We assume the PKE scheme is IND-CPA.

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- KeyGen outputs sk  $\leftarrow G$  and pk =  $(E_0, X_{pk} = (E_0, sk \star E_0))$ .

 ${}^{3}m \star_{M} (E_{1}, E_{2}) := (E_{1}, m \star E_{2}) \text{ and } r \star_{pk} (E_{1}, E_{2}) := (r \star E_{1}, r \star E_{2})$ 

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- We have an Elgamal-type encryption<sup>3</sup>:

 $\mathsf{ct} = (r \star E_0, (r + m) \star E_{\mathsf{pk}}) \leftarrow \mathsf{Enc}(\mathsf{pk}, m; r \leftarrow G).$ 

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#### **Decisional CSIDH Problem**

Let  $a, b \leftarrow G$ . Given  $(E_0, a \star E_0, b \star E_0, E)$ , where *E* is either  $(a + b) \star E_0$  or  $E = c \star E_0$  for some  $c \leftarrow G$ . It's difficult to distinguish the distribution of *E*.





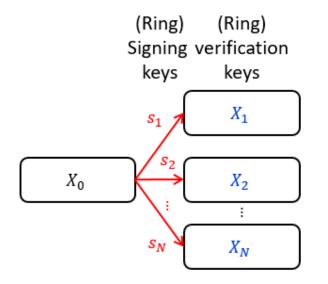
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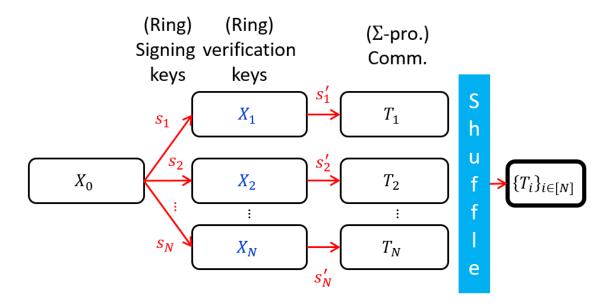
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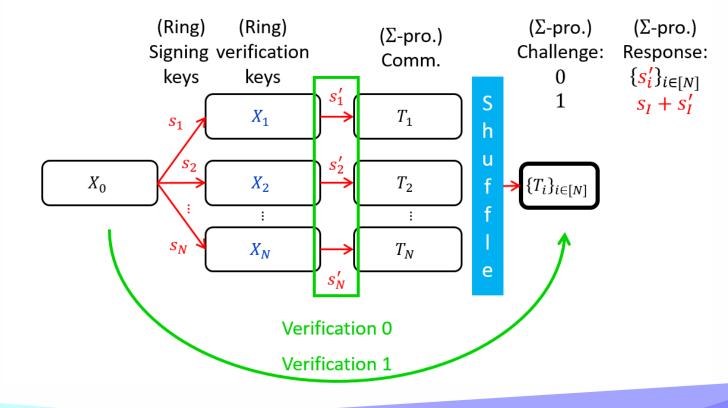
$$R_{\rm or} = \left\{ \left( \{X_i\}_{i \in [N]}, (s_I, I) \right) \mid s_I \star X_0 = X_I \in \{X_i\}_{i \in [N]} \right\}$$



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### **Encryption Relation**

The idea here is to concatenate and shuffle two proofs together.

$$R_{\text{or}} \times R_{\text{enc}} = \left\{ \left( \{X_i\}_{i \in [N]}, \text{pk, ct, } (s_I, I, r) \right) \mid \begin{array}{c} s_I \star X_0 = X_I \in \{X_i\}_{i \in [N]} \\ \text{ct} = \text{Enc}(\text{pk}, I; r) = I \star_M r \star_{\text{pk}} X_{\text{pk}} \end{array} \right\}$$

$$\left( \begin{array}{c} \text{(Ring)} \\ \text{Signing} \\ \text{Signing} \\ \text{verification keys} \\ \text{keys} \end{array} \right)$$

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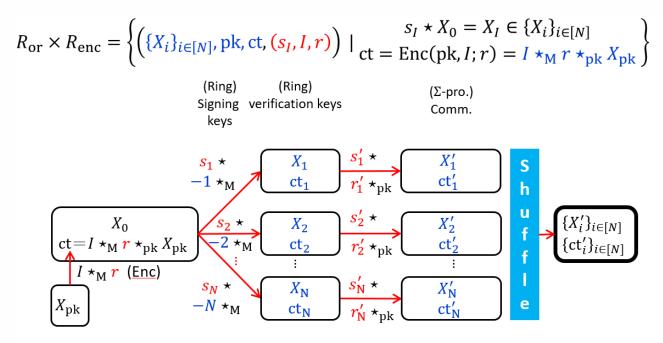
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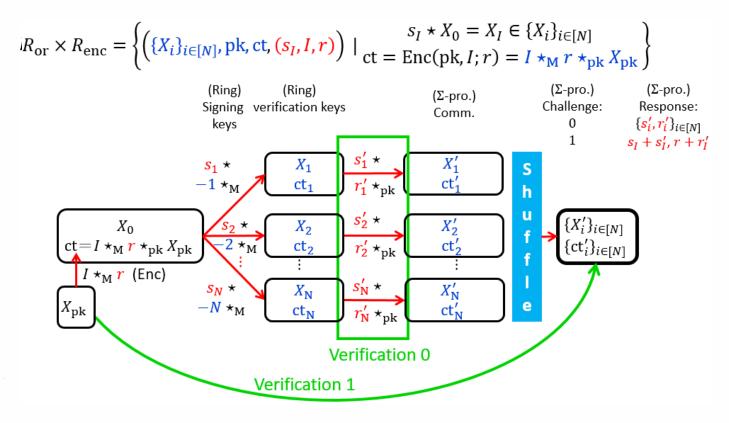
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### Logarithmic Proof

Optimize by using PRNG, Merkle Trees, commitment schemes.

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Seed  $\in \{0,1\}^{\lambda} \rightarrow PRNG \rightarrow s', r', \{bit_i \in \{0,1\}^{\lambda}\}_{i \in [N]}$ 

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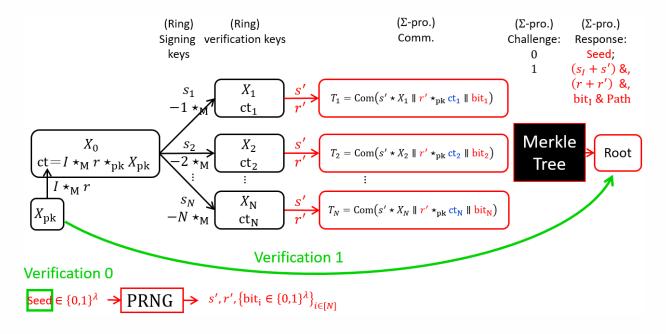
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$$(\text{Ring)} \quad (\text{Ring)} \quad (\Sigma \text{-pro.}) \quad (\Sigma \text{-pro.}) \quad (\Sigma \text{-pro.}) \\ \text{Signing verification keys} \quad Comm. \quad Challenge: \text{Response:} \\ \text{Response:} \\ \text{Response:} \\ 0 \quad \text{Seed}; \\ 1 \quad (s_i + s') \&, \\ (r + r') \&, \\ \text{bit}_l \& \text{Path} \\ \hline \\ \text{Ct} = l \star_M r \star_{\text{pk}} X_{\text{pk}} \quad S_2 \quad X_2 \quad s' \\ -N \star_M \quad Ct_N \quad r' \quad T_2 = \text{Com}(s' \star X_2 \parallel r' \star_{\text{pk}} \text{ct}_2 \parallel \text{bit}_2) \quad Merkle \\ \text{Tree} \quad \text{Root} \\ \hline \\ \text{Tree} \quad \text{Root} \\ \hline \\ \text{Verification 0} \\ \hline \\ \text{Verification 0} \\ \hline \\ \text{Seed} \in \{0,1\}^{\lambda} \rightarrow \text{PRNG} \rightarrow s', r', \{\text{bit}_i \in \{0,1\}^{\lambda}\}_{i \in [N]} \\ \end{array}$$

## Online-Extractability (OE)

We show OE by modeling PRNG/commitment schemes/Merkle trees as a random oracle.

The main reason is the challenge space size is 2 and one response can be obtained by observing the oracle queries.



Repeat  $\lambda$  times, the interactive protocol will have  $2^{\lambda}$  strength.

Via Fiat-Shamir transform, the protocol can be transformed into a non-interactive ring signature of form  $({X_i}_{i \in [N]}, pk, ct, \sigma)$ .

Roughly,

- Online Extractability + IND-CPA  $\rightarrow$  CCA anonymity
- ► Online Extractability + Hardness assumption of the action → Unforgeability
- ► The ciphertext is  $ct = Enc(pk, I; r) = I \star_M r \star_{pk} X_{pk}$ . The manager with the decryption key can open the signature.
- It suffices to construct an NIZK for the decryption and key relations (for traceability/full-unf).

### The Decryption and Key Validation Relations

By using a similar method, we construct NIZKs for the decryption relations and PKE key relations for our GAPKEs.

Isogeny:

 $\{((E_0, E_1, E_2, E_3, \mathsf{M}), \mathsf{sk}) \mid E_1 = \mathsf{sk} \star E_0, \mathsf{M} \star \mathsf{sk} \star E_2 = E_3\}.$ 

Lattice:

$$\left\{ ((\mathbf{A}, \mathbf{e}, \mathbf{b}, \mathbf{c}, c, \mathbf{M}), \mathbf{sk} = (\mathbf{s}, \mathbf{z})) \mid \mathbf{b} = \mathbf{As} + \mathbf{z}, \\ \mathbf{s}, \mathbf{z}, c - \mathbf{c}^T \mathbf{s} - \mathbf{M} \lfloor q/2 \rceil \text{ are short.} \right\}.$$

The opener provides the proof for the opening result using NIZK for the relation. Traceability and full-unforgeability will follow.

- Reduce the signature size:
  - Using the unbalanced challenge space (#0s>#1s).
- Lattice instantiation:
  - We give GAPKE by using Lindner-Peikert framework [LP11].
  - The signature size can be further reduced by using the Bai-Galbraith method.
- Tightly secure variant:
  - Using the Katz-Wang method.
  - The (unforgeability) reduction loss is only 1/2. ( $\epsilon^2/N^2$  mostly.)
  - The additional cost is only a constant<sup>4</sup>.

<sup>&</sup>lt;sup>4</sup>Increased by 0.5 KB; signing, verification slow down by factor 2.





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#### Comparison with other post-quantum group signature proposals.

		N				Hardness	Security	Anonymity	Manager
	2	$2^5$	$2^6$	$2^{10}$	$2^{21}$	Assumption	Level		Accountable
Isogeny	3.6	6.0	6.6	9.0	15.5	CSIDH-512	*	CCA	Yes
Lattice	124	126	126	129	134	MSIS/MLWE	NIST 2	CCA	Yes
Lattice	86	88	89	91	96	MSIS/MLWE	NIST 2	CCA	No
[ESZ22]	/	12	/	19	/	MSIS/MLWE	NIST 2	CPA	No
[KKW18]	/	/	280	418	/	LowMC	NIST 5	selfless-CCA	No

- N: number of memebers. Signature size is in KB.
- \*: estimated to be 60 bits of quantum security in [Pei20].
- Non-Selfless: anonymous against full-key exposure.
- Manager Accountablility: Manager cannot frame an honest member.



- 1. A new framework for GS based on group actions with isogeny and lattice instances achieving all ideal security properties specified in [BSZ05].
- 2. Our framework is logarithmic. Concretely, the size of
  - the isogeny instance has the smallest order of magnitude in the literature (e.g. 6.6 KB for 64 members).
  - the lattice instance has the smallest growth rate in the lattice literature<sup>5</sup>.
- 3. The first two tightly secure post-quantum GS.
- 4. The first GS from isogenies and the only logarithmic proposal.



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# **Thanks for listening!**

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