

IBE with Incompressible Master Secret and Small Identity Secrets

Sruthi Sekar

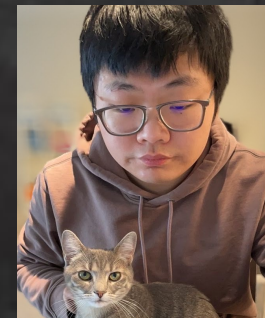
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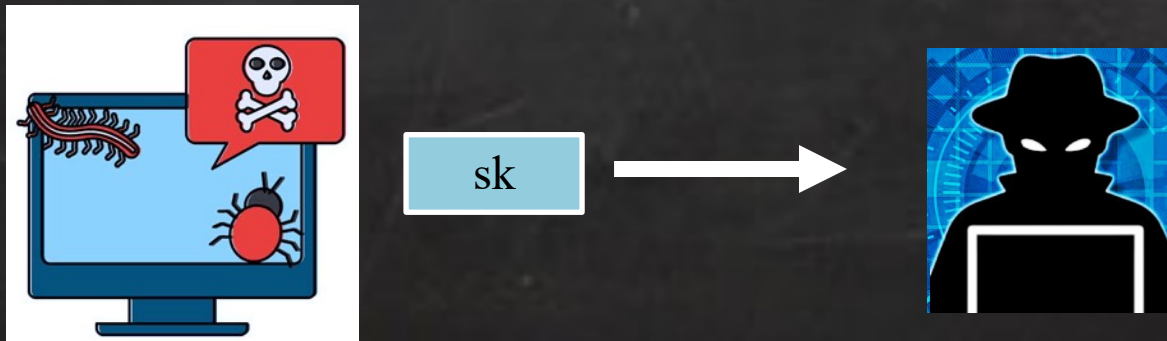
Big-key Cryptography

Motivation: Exfiltration Attacks

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Advanced persistent threat

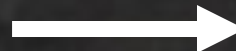
From Wikipedia, the free encyclopedia

An **advanced persistent threat (APT)** is a stealthy **threat actor**, typically a **nation state** or state-sponsored group, which gains unauthorized access to a **computer network** and remains undetected for an extended period.^{[1][2]} In recent times, the term may also refer to non-state-sponsored groups conducting large-scale targeted intrusions for specific goals.^[3]

Such threat actors' motivations are typically political or economic.^[4] Every major **business sector** has recorded instances of **cyberattacks** by advanced actors with specific goals, whether to steal, spy, or disrupt. These targeted sectors include government, **defense**, **financial services**, **legal services**, industrial, **telecoms**, consumer goods and many more.^{[5][6][7]} Some groups utilize traditional **espionage** vectors, including **social engineering**, **human intelligence** and **infiltration** to gain access to a physical location to enable network attacks. The purpose of these attacks is to install custom **malware** (malicious software).^[8]



sk



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“We have to think in a totally different way about how we are going to protect computer systems assuming there are APTs inside already which cannot be detected. Is everything lost? I claim that not: there are many things that you can do, because the APT is basically going to have a very, very narrow pipeline to the outside world. . . . I would like, for example, all the small data to become big data, just in terms of size. I want that the secret of the Coco-Cola company to be kept not in a tiny file of one kilobyte, which can be exfiltrated easily by an APT I want that file to be a terabyte, which cannot be [easily] exfiltrated.”



sk



Adi Shamir
@RSA 2013

Big-key Cryptography

Bounded Retrieval Model

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Big-key primitives: symmetric key encryption [BKR16], public-key encryption [ADN+10, MW20], authenticated key agreement [Dzi06, CDD+07, ADW09].

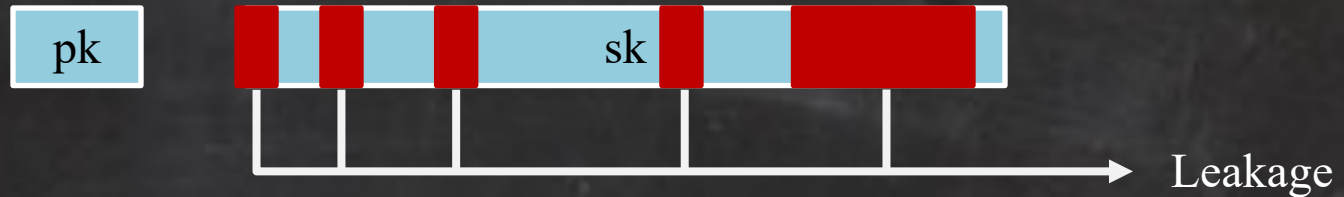
Big-key (Public-key) Encryption

The Model

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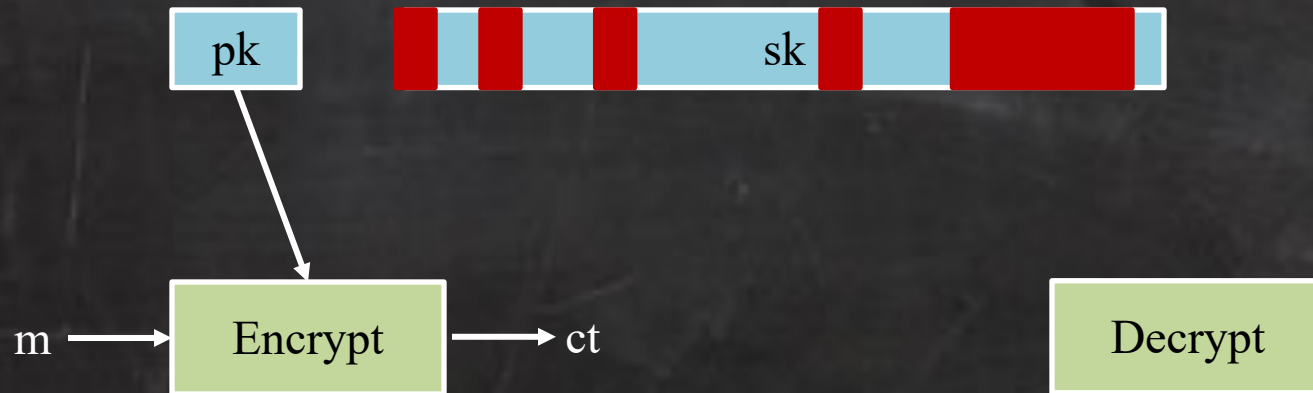
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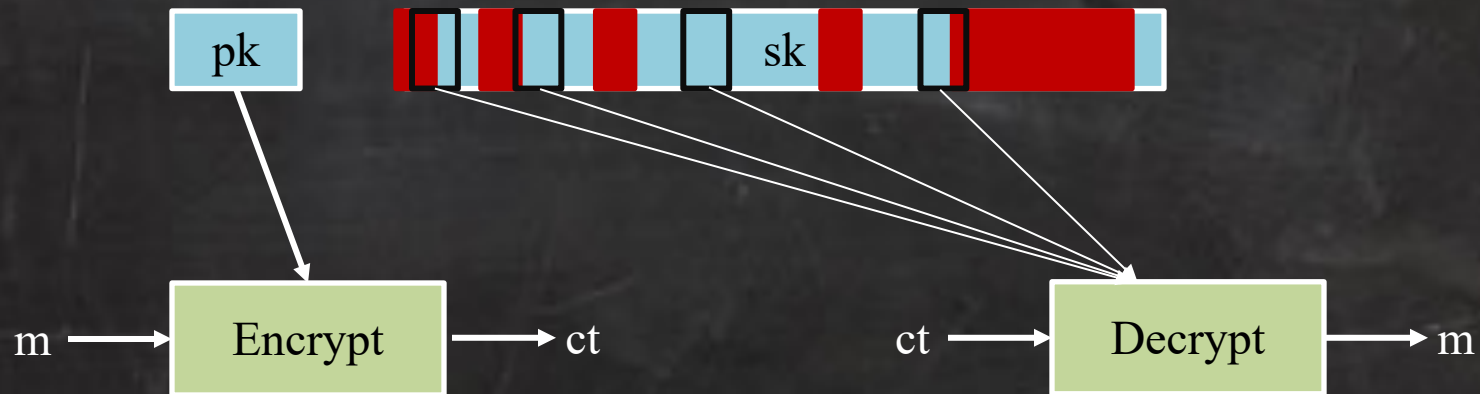
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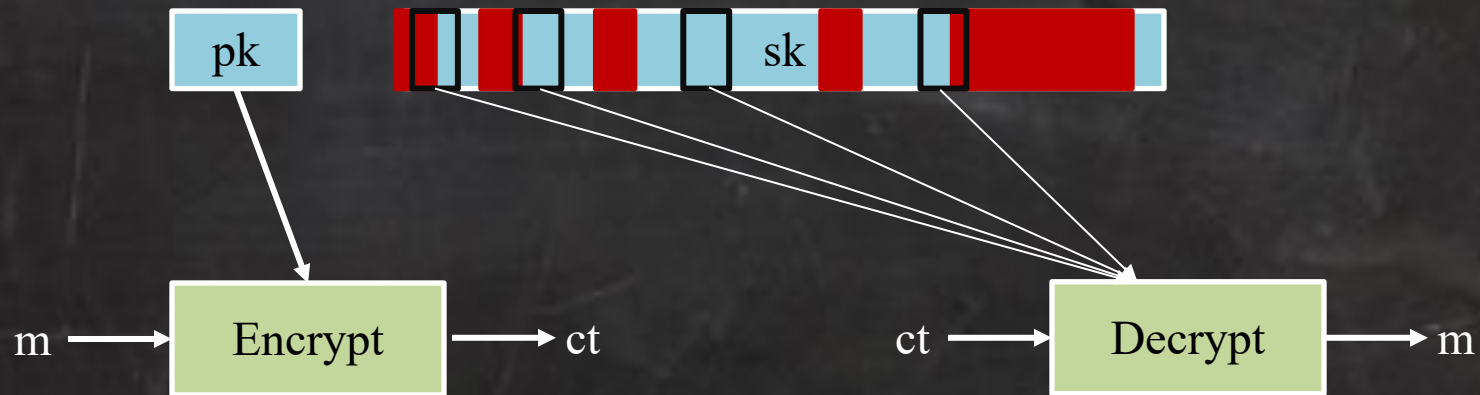


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Security: semantic security of fresh ciphertexts generated after arbitrary leakage on sk is given to the adversary.



Big-key (Public-key) Encryption

Caveats of The Model

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User must carry entire large secret key on all its devices.
(since parts of sk needed to decrypt are unknown a priori)



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1. Leads to wastage of limited storage space on small mobile devices.



Big-key (Public-key) Encryption

Caveats of The Model

User must carry entire large secret key on all its devices.

1. Leads to wastage of limited storage space on small mobile devices.
2. Replication of the large secret makes use more susceptible to leakage (e.g., the loss of a mobile device will leak whole of sk!)



Our Solution: Big-key IBE

Our IBE-based Model

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Use the advantages of identity-based encryption-

- Setup: generates master public and secret keys (mpk,msk).
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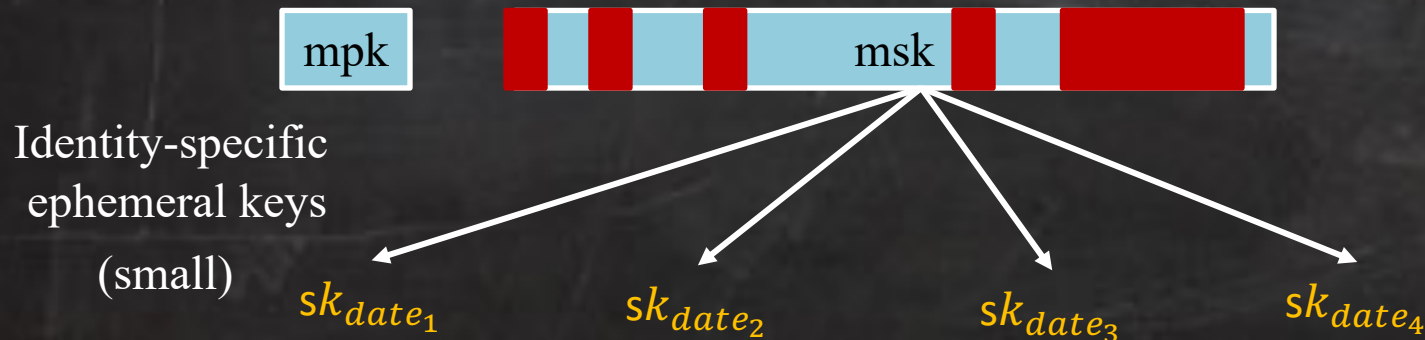


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- Decryption uses short identity-specific ephemeral keys sk_{id} .



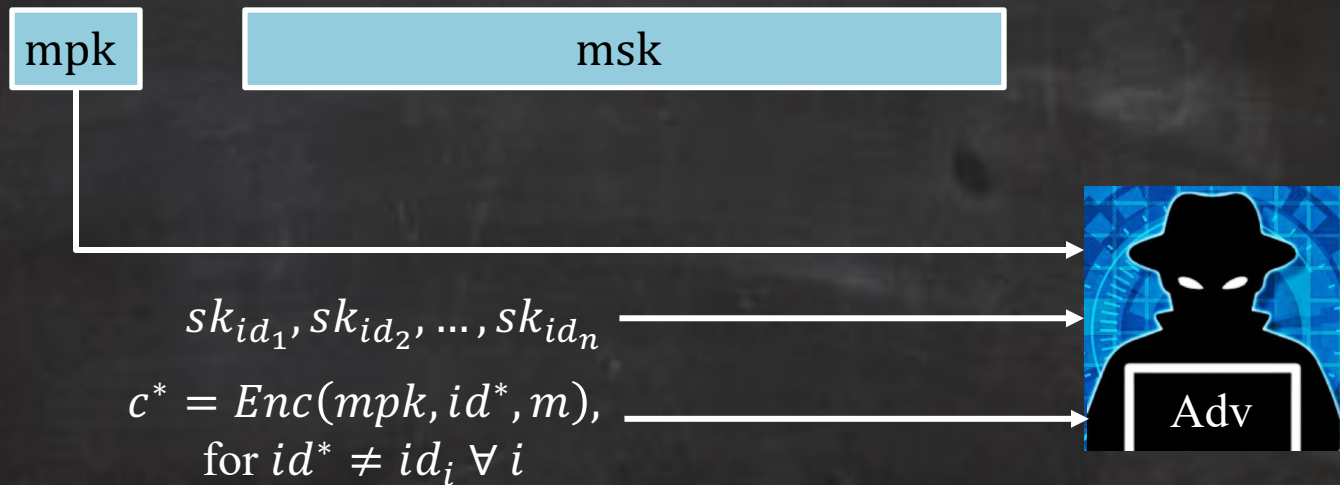
Big-key IBE

Challenges in Defining Security

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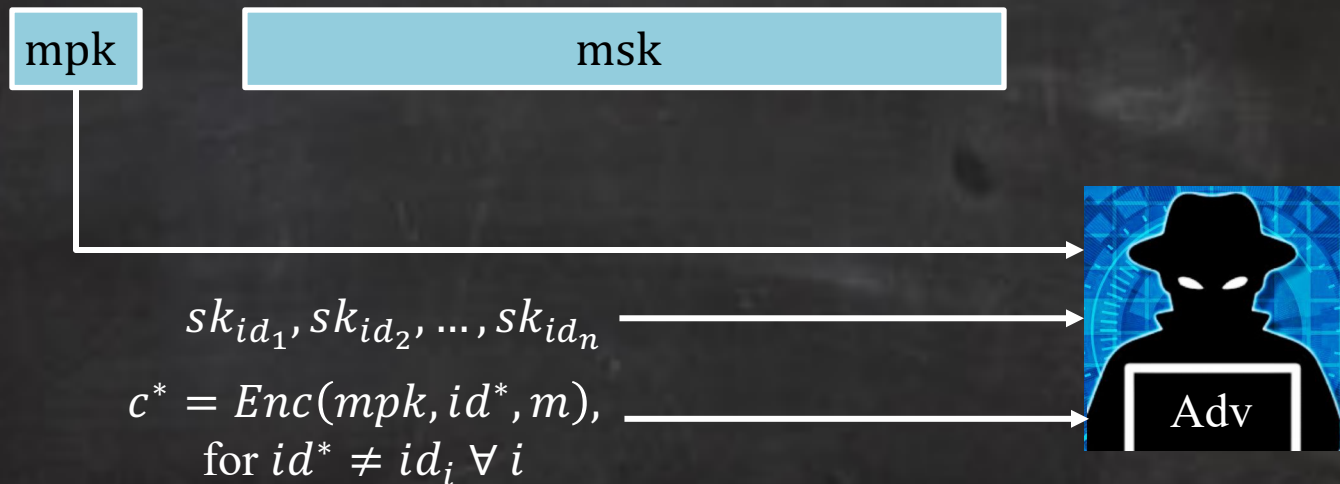
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Selective security: id^* given by Adv before seeing mpk .

Full security: id^* given by Adv after seeing mpk .

Big-key IBE

Challenges in Defining Security

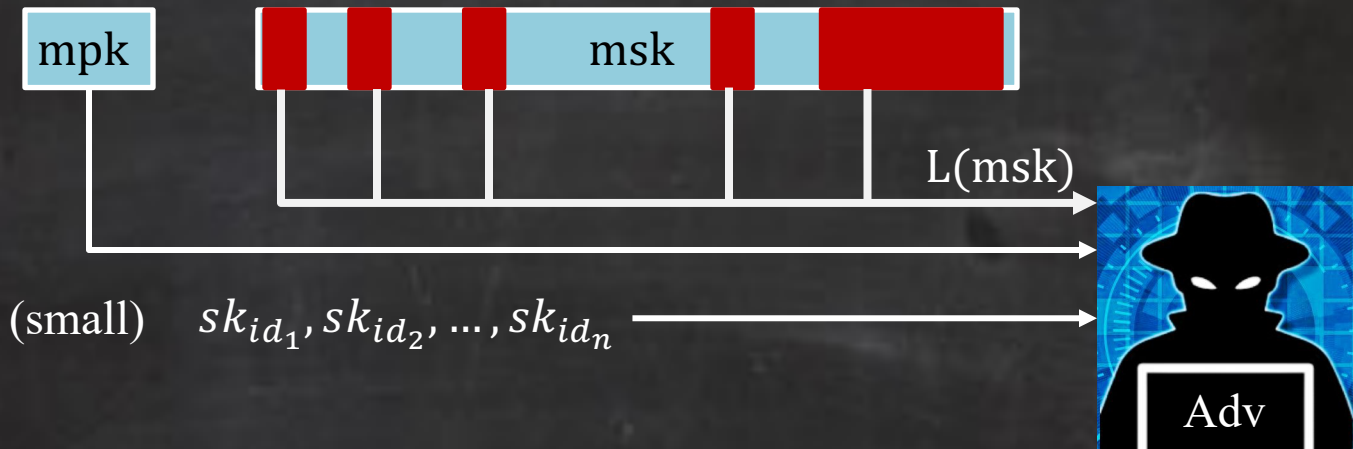
- Big-key IBE security: Adv gets $L(\text{msk})$ in addition to polynomial number of sk_{id} 's.



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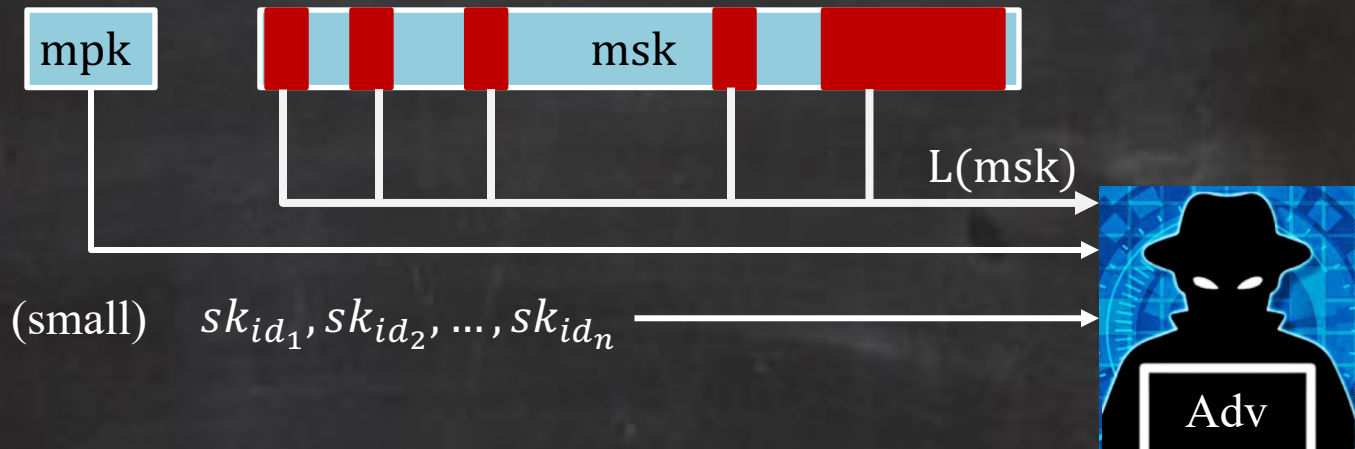


Key Challenge in defining security: Adv can get the challenge sk_{id^*} directly through $L(\text{msk})$ (since the output length of L is large)—breaks security.

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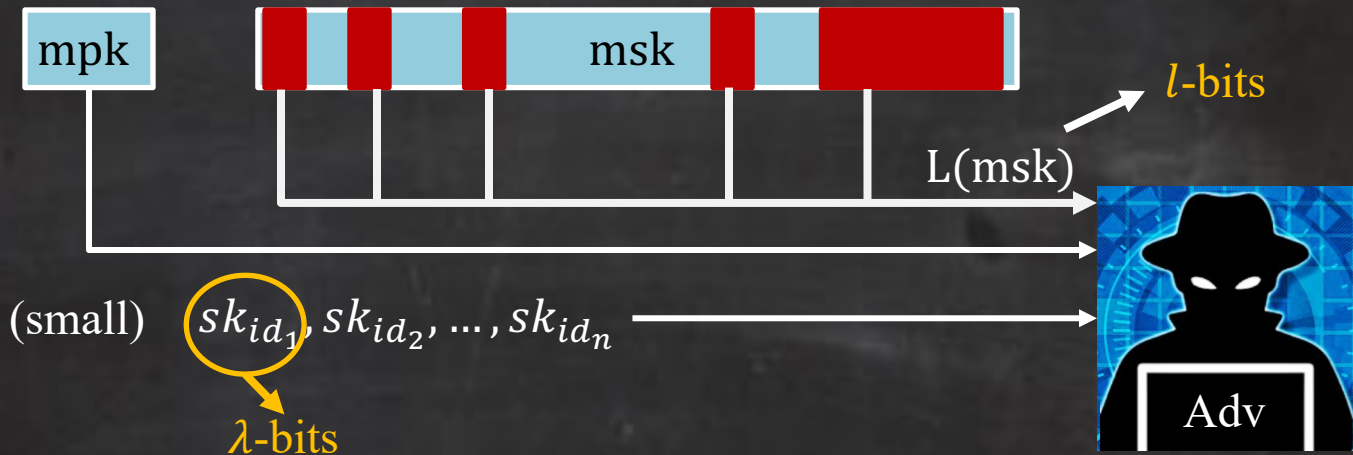
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Prior Leakage-resilient IBEs [ADN+10, CDRW10, LRW11, HLWW13, CZLC16, NY19]
—had large sk_{id} 's and msk is either large or allows no leakage.

Big-key IBE

Towards Defining Security

- Big-key IBE security: Adv gets $L(\text{msk})$ in addition to polynomial number of sk_{id} 's.

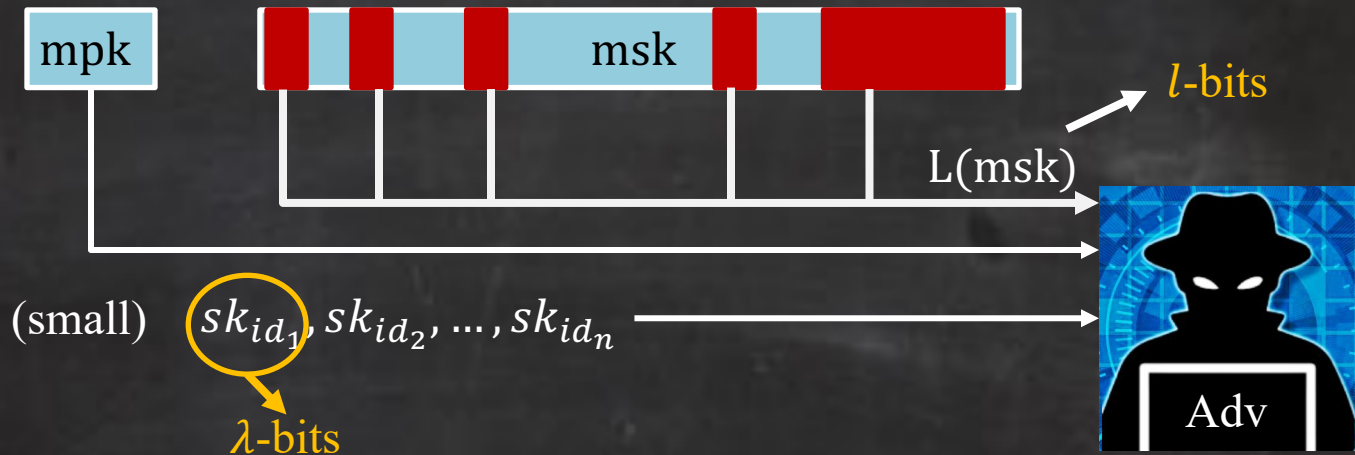


- Adv through the l -bit leakage allowed by L can get upto $\frac{l}{\lambda} = \Theta(l)$ sk_{id} 's.

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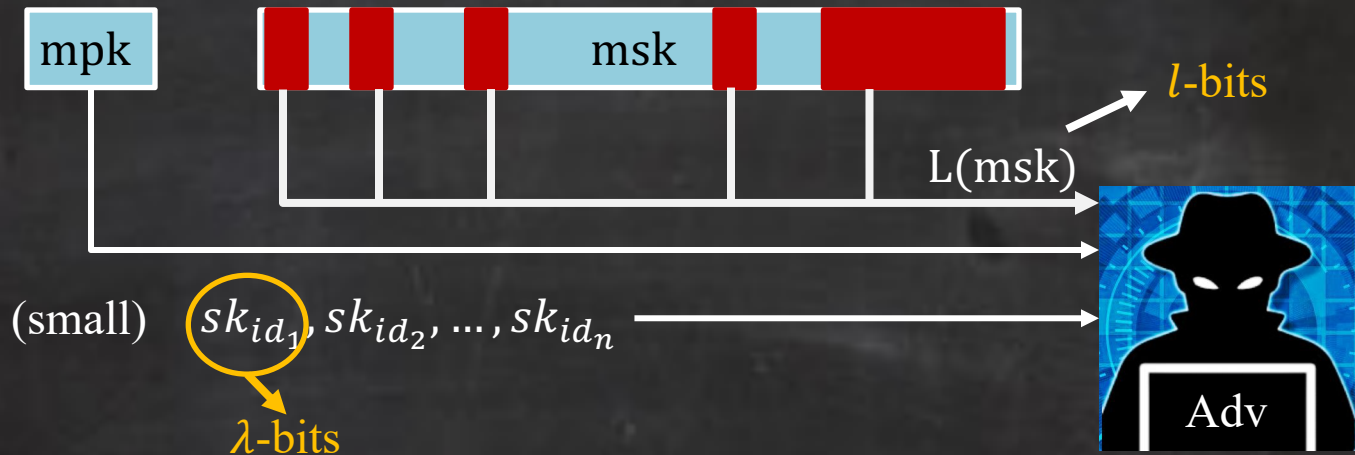


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Particularly, given l -bit leakage, we want Adv to not break security for $\geq l + 1$ identities.

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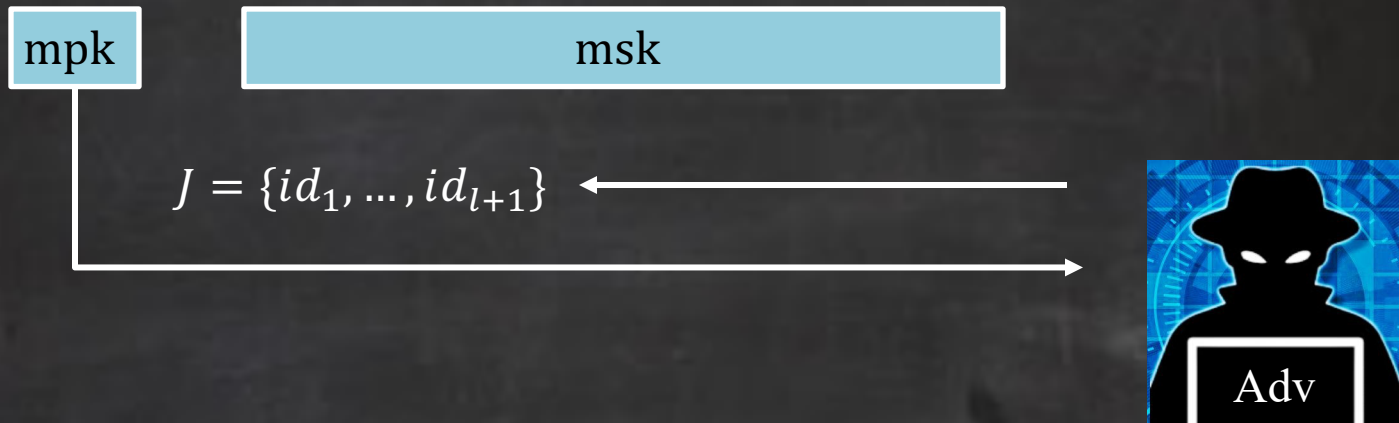
Our Security Model

$J = \{id_1, \dots, id_{l+1}\}$



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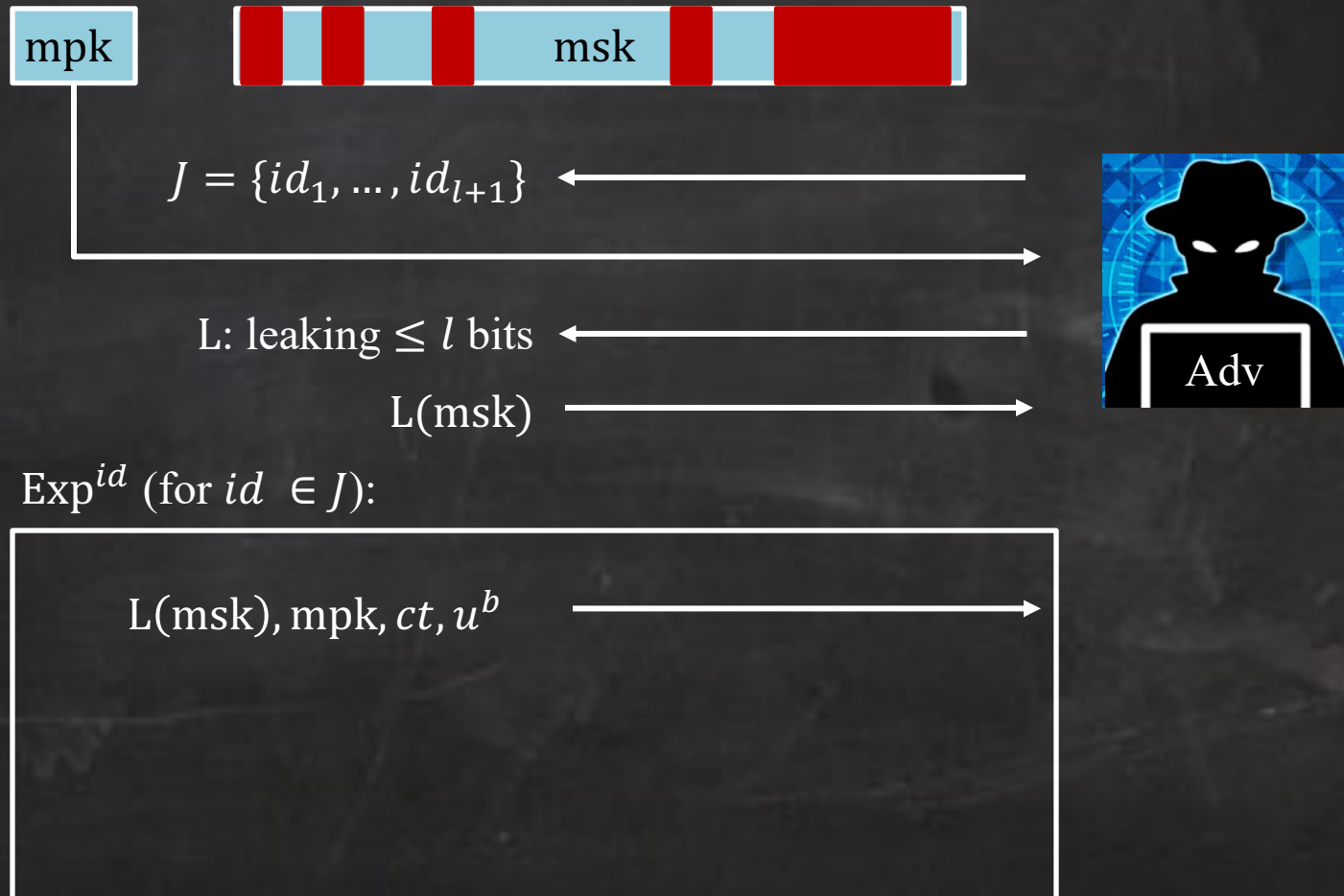


Exp^{id} (for $id \in J$):



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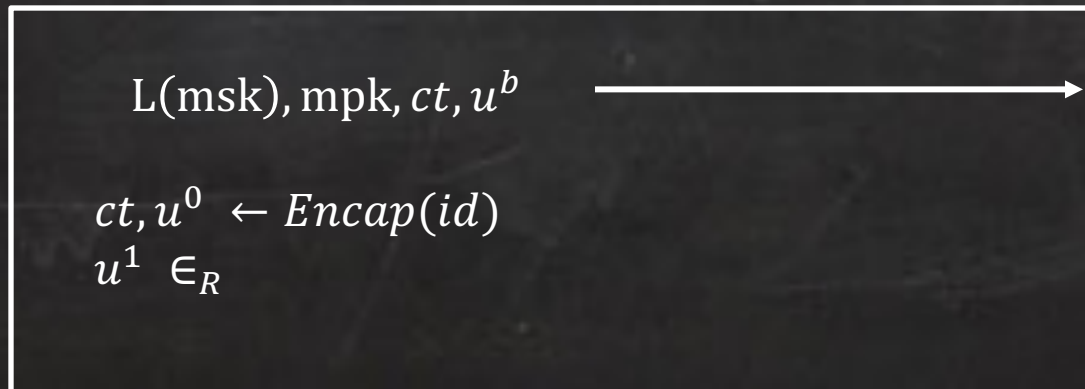


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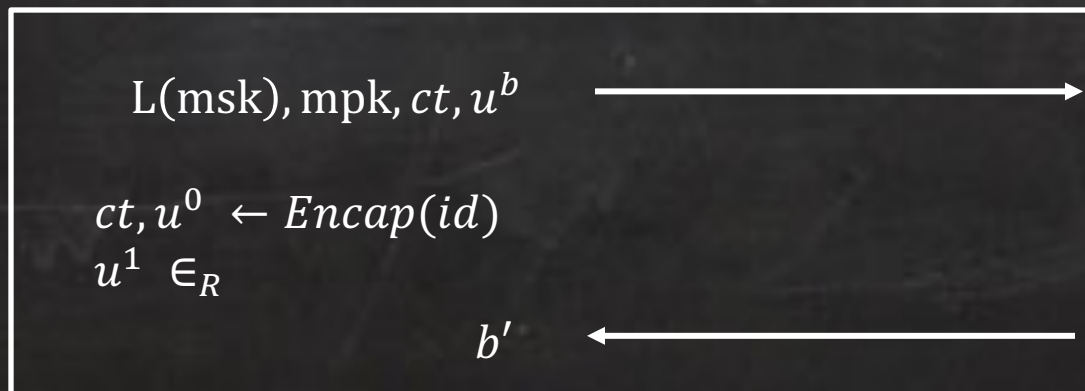


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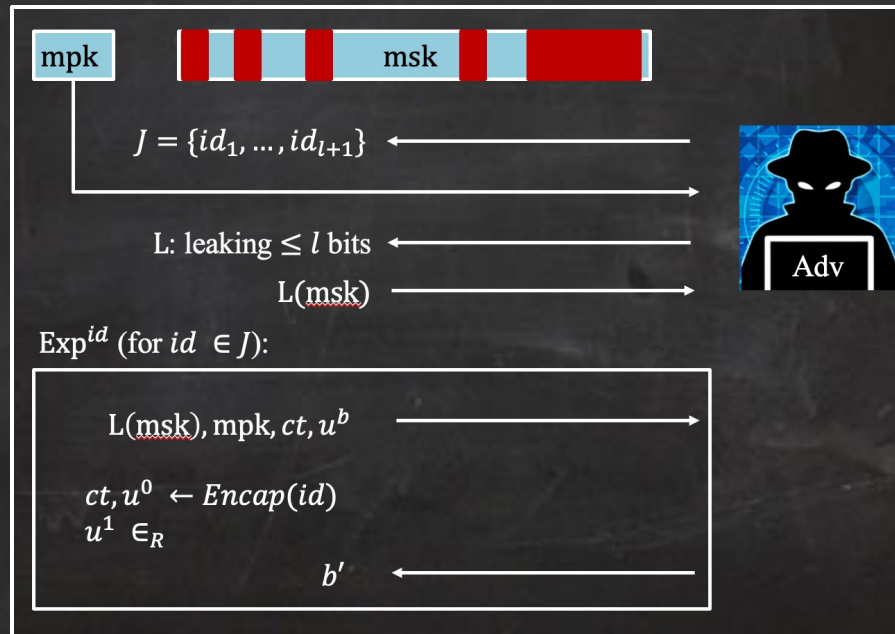


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Selective Security:

$\Pr[\forall id \in J, |\Pr[b' = b] - 1/2| \geq \varepsilon]$ is negligible.

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Construction Overview

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Pseudo-entropy
Function

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Leakage-resilient Encryption
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Reusable 2-round MPC [BL20]

Big-key IBE with large mpk

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Laconic OT
[CDG+17]

Big-key IBE

*Security relies on hardness of standard assumptions on groups with bilinear pairing

Open Problems

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- How to make the big-keys useful, a.k.a. catalytic?
(as in the work of [MW20])

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THANK YOU

[eprint/2022/649](#)