

Oblivious Transfer from Zero-Knowledge Proofs

or How to Achieve Round-Optimal Quantum Oblivious Transfer and Zero-Knowledge Proofs on Quantum States

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Q_uSoft



ASIACRYPT 2023














Multi-Party Computing (MPC)



Oblivious
Transfer

Oblivious Transfer

m_0

m_1





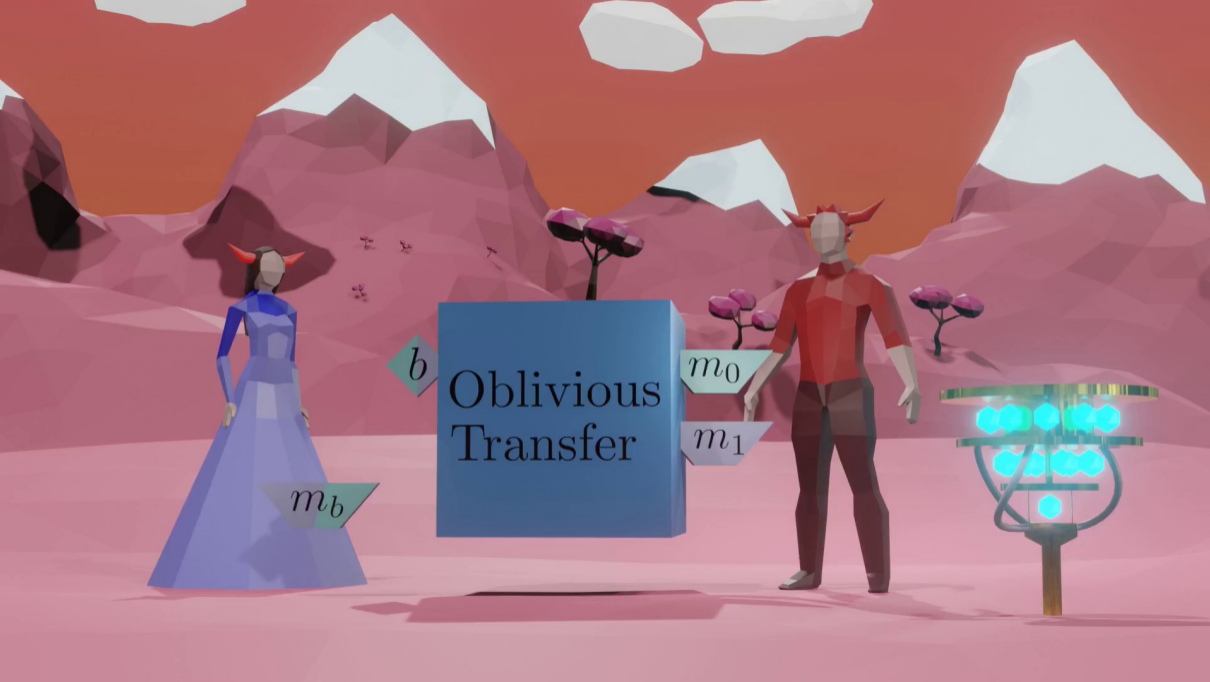
b

Oblivious
Transfer

m_0

m_1





Oblivious
Transfer

b

m_0

m_1

m_b

OT: state of the art

Oblivious Transfer (OT) : studied a lot ([Rab81], [EGL85], [PVW08], [BD18], [GLSV22], [BCKM21]...)

State of the art

Classical



Requires trapdoors

(= CryptoMania, asymmetric crypto)



2 messages

Quantum



No structure is necessary

(= hash function)



7 messages ([CK88]/[BBCS92]...)
→ **3 messages** ([ABKK23]) ←

With **pre-shared EPR pairs**:

[BKS23]: 1-message **random** receiver bit string OT & 2-message OT

[Agarwal, Bartusek, Khurana, Kumar 23] raises the question:

? Is there an OT protocol in 2-messages (optimal) without structure?

Our contributions

Yes !

Theorem 1 (informal)

There exists a 2-message (optimal) quantum OT protocol secure in the Random Oracle Model (i.e. no structure) assuming the existence of a hiding collision-resistant hash function.

Our approach

 No structure is necessary
(= hash function)

 2 messages

Methods

Remove cut-and-choose: classical Zero-Knowledge proofs + quantum protocol
= prove a statement on a quantum state non-destructively.





Proof



Proof



Proof



Proof

Either:
Qubits 1 & 2 collapsed
or qubits 2 & 3 collapsed

Proof



Either:
Qubits 1 & 2 collapsed
or qubits 2 & 3 collapsed

I trust you!
But which are the
collapsed ones?

Proof



Secret !

I trust you!
But which are the
collapsed ones?

Proof



Our contributions

We can prove that a received quantum state belongs to a fixed set of quantum state:

Theorem 2 (informal)

For any arbitrary predicate \mathcal{P} , there exists a protocol such that:


- *The prover chooses a secret subset S of qubits such that $\mathcal{P}(S) = \top$*
- *At the end of the protocol, the verifier ends up with a quantum state such that qubits in S are collapsed (measured in computational basis), even if the prover is malicious*
- *S stays unknown to the verifier*

(\mathcal{P} allows us to get string-OT, k -out-of- n OT...)

Complexity theory:

⇒ **generalize ZK proofs to quantum languages (ZKstatesQMA)**

(we do not characterize ZKstatesQMA/ZKstatesQIP completely, but we define them and show they are not trivial)




Zero
Knowledge

Our
Work



Our
Work

Oblivious
Transfer




NIZK
[Unr15]

Our
Work



Our Work

Oblivious
Transfer
(2-messages)



ZK plain-model
[HSS11]

Our
Work



Our Work

Oblivious
Transfer
(plain-model)

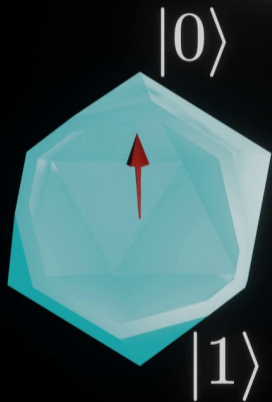
Theorem 3 (ZK \Rightarrow quantum OT, informal)

Assuming the existence of a collision-resistant hiding function, there exists a protocol turning any n -message, post-quantum Zero-Knowledge (ZK) proof of knowledge into an $(n + 1)$ -message quantum OT protocol assuming a Common Random String model or $n + 2$ without further setup assumptions.

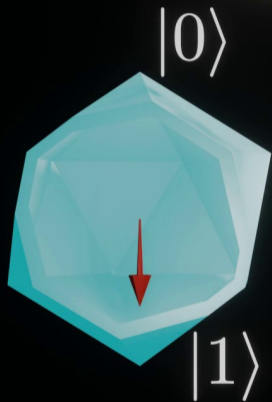
The security properties (statistical security, etc.) and assumptions (setup, computational assumptions, etc.) of the ZK protocol are mostly preserved.

Article	Classical	Setup	Messages	MiniQCrypt	Composable	Statistical
This work + [Unr15]	No	RO	2	Yes	Yes	No
This work + [HSS11]	No	Plain M.	> 2	No (LWE)	Yes	No
This work + S-NIZK	No	Like ZK	2	Like ZK	Yes	Sender
This work + NIZK proof	No	Like ZK	2	Like ZK	Yes	Receiver
This work + ZK	No	Like ZK	ZK + 1 or 2	Like ZK	Yes	Like ZK

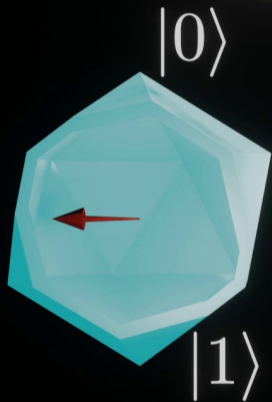
Qubits



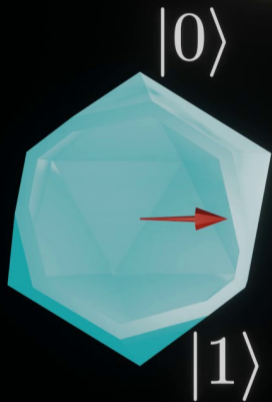
Qubits



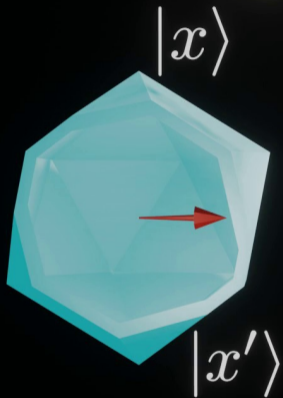
Qubits



Qubits



Qubits



Superposition

$$a_x |x\rangle + a_{x'} |x'\rangle$$

Qubits



Superposition

$$a_x |x\rangle + a_{x'} |x'\rangle$$

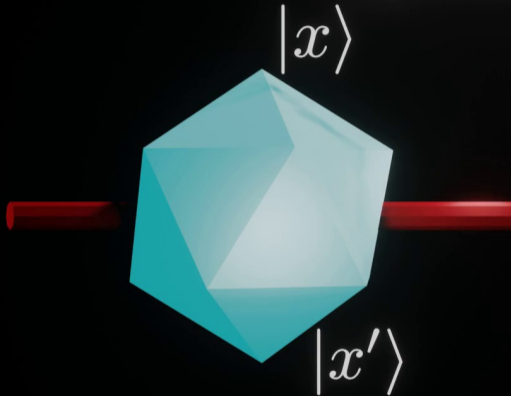
Qubits



Superposition

$$a_x |x\rangle + a_{x'} |x'\rangle$$

Qubits



Superposition

$$a_x |x\rangle + a_{x'} |x'\rangle$$

Qubits

$|x\rangle$

Superposition

d

$$a_x |x\rangle + a_{x'} |x'\rangle$$

$|x'\rangle$



Oblivious
Transfer

b

m_0

m_1

m_b





b

m_0

m_1



If $b = 0$



m_0

m_1



If $b = 0$



m_0

m_1



If $b = 1$



m_0

m_1



r

If $b = 1$



m_0

m_1

r



One qubit comp. basis



If $b = 1$



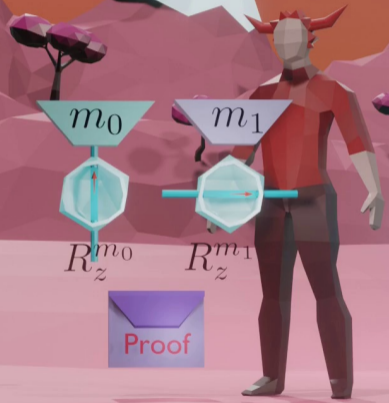
r



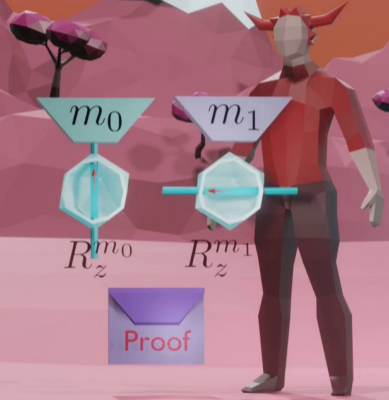
If $b = 1$



r



If $b = 1$



Proof



If $b = 1$



r



m_0



m_1



Proof



If $b = 1$



r



m_0

m_1



s_0

Proof



If $b = 1$



r

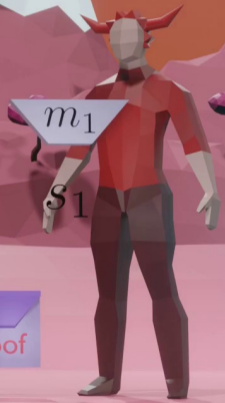


m_0

m_1

s_0

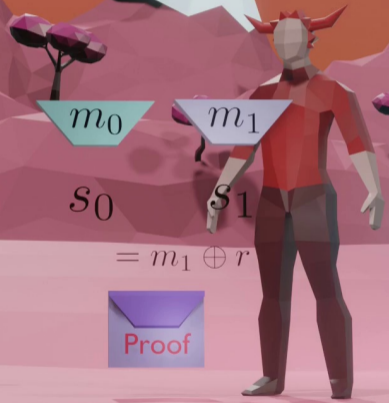
s_1



Proof



If $b = 1$



r

s_0

s_1

$$= m_1 \oplus r$$



If $b = 1$

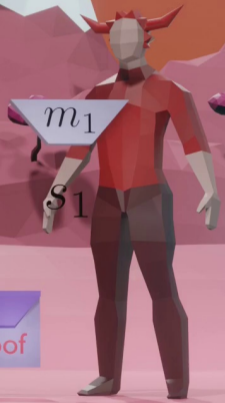


r



m_0

s_0



m_1

s_1

Proof



If $b = 1$

r s_0 s_1

m_0

m_1

Proof



If $b = 1$

$r \quad s_0 \quad s_1$

$$m_b = s_b \oplus r$$

Proof



This is not secure!

Problem of naive construction

Problem: Alice can cheat by sending two $|+\rangle$ states instead of one $|0/1\rangle$ and one $|\pm\rangle$.

If $b = 1$



m_0

m_1

r_1



One qubit comp. basis





m_0

m_1

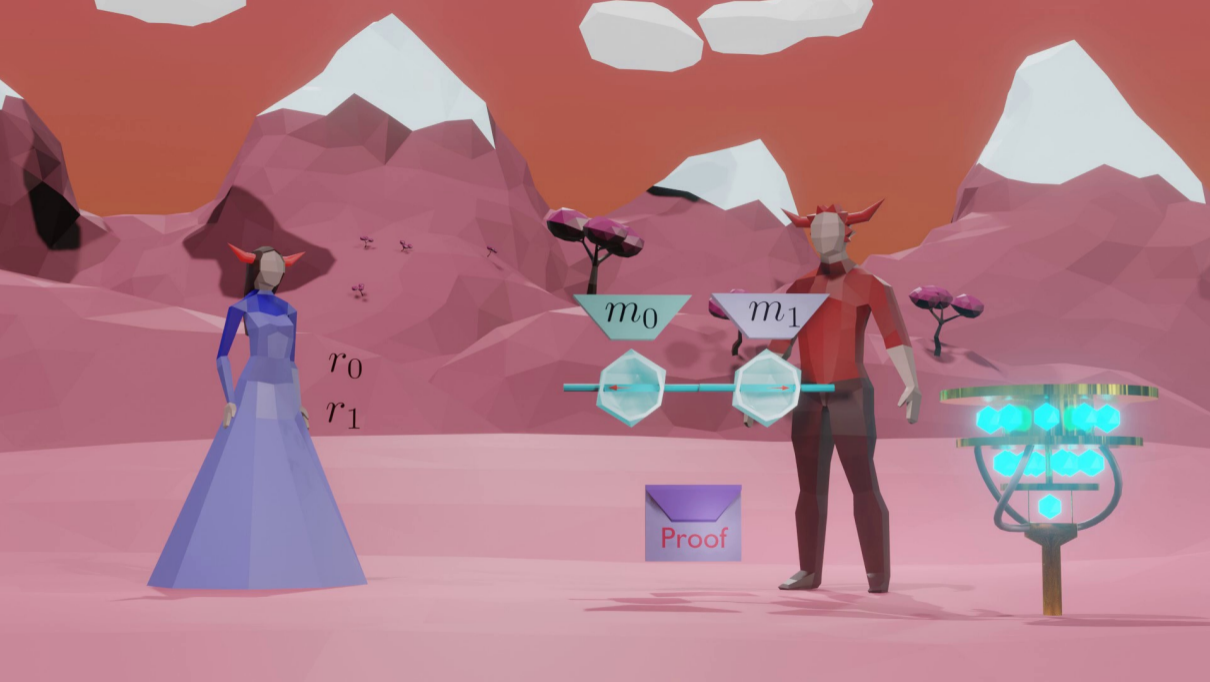
r_0

r_1



One qubit comp. basis



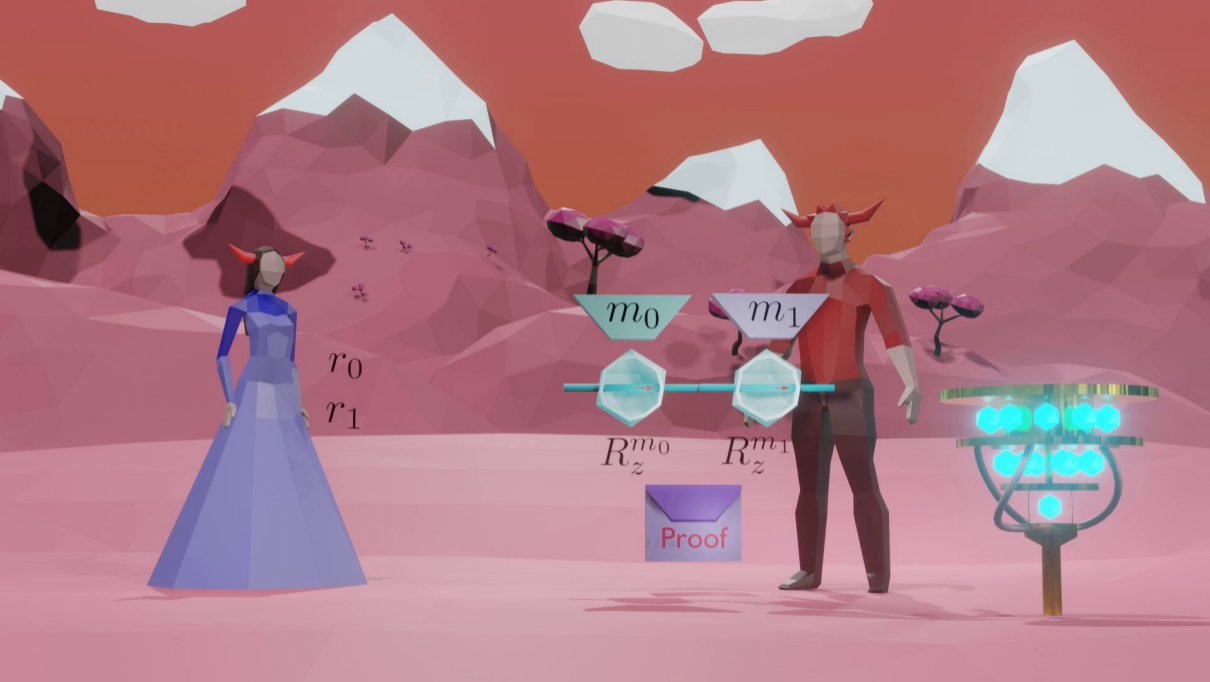


r_0
 r_1



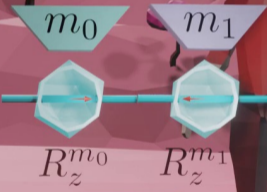
Proof







r_0
 r_1



Proof



r_0
 r_1

m_0

m_1

Proof



r_0
 r_1

m_0

m_1

s_0

Proof

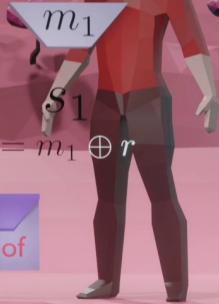




r_0
 r_1

m_0

s_0
 $= m_0 \oplus r'$

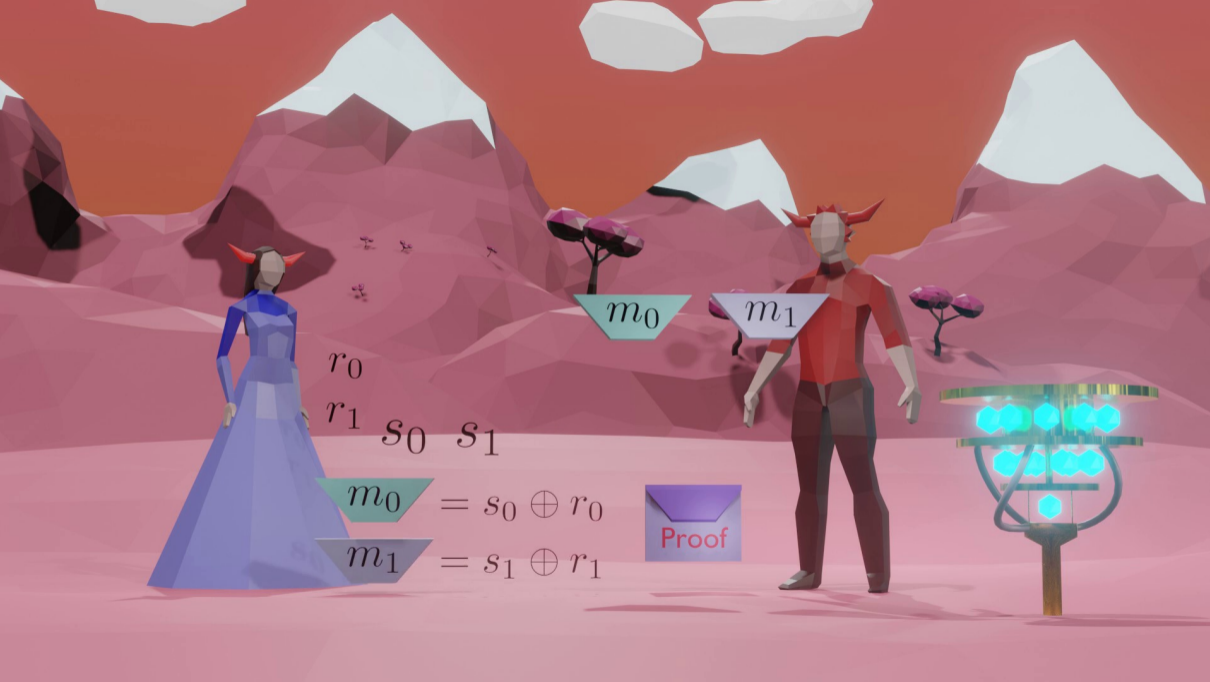


m_1

s_1
 $= m_1 \oplus r$

Proof





r_0
 r_1 s_0 s_1

$$m_0 = s_0 \oplus r_0$$

$$m_1 = s_1 \oplus r_1$$

Proof

Classical Zero-Knowledge



Classical Zero-Knowledge

Solution exists?



1	⊙	⊙	⊙
⊙	⊙	4	⊙
⊙	⊙	3	⊙
⊙	2	⊙	⊙



Classical Zero-Knowledge

Yes!
I won't reveal it.

Solution exists?

1	⊙	⊙	⊙
⊙	⊙	4	⊙
⊙	⊙	3	⊙
⊙	2	⊙	⊙



Classical Zero-Knowledge

Yes!
I won't reveal it.

I don't trust you.

1	⊙	⊙	⊙
⊙	⊙	4	⊙
⊙	⊙	3	⊙
⊙	2	⊙	⊙



Classical Zero-Knowledge

Yes!
I won't reveal it.

I don't trust you.

1	⊙	⊙	⊙
⊙	⊙	4	⊙
⊙	⊙	3	⊙
⊙	2	⊙	⊙



Classical Zero-Knowledge

Yes!
I won't reveal it.

Ok, I trust you.



Generalizable in a non-interactive way to NP problems.



How can Alice prove that one qubit is in the **computational** basis and the other is in the **Hadamard** basis?



How can Alice prove that one qubit is in the **computational** basis and the other is in the **Hadamard** basis?

⇒ Known to be possible using LWE (Colisson, Grosshans, Kashefi (2022))

Problem: need structure + not suitable for statistical security.

What about a weaker statement?



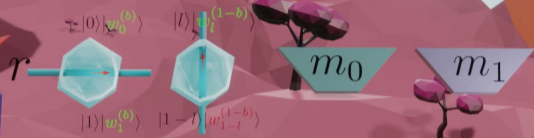
How can Alice prove that one qubit is in the **computational** basis and the other is in the **Hadamard** basis?

⇒ Known to be possible using LWE (Colisson, Grosshans, Kashefi (2022))

Problem: need structure + not suitable for statistical security.

What about a weaker statement?

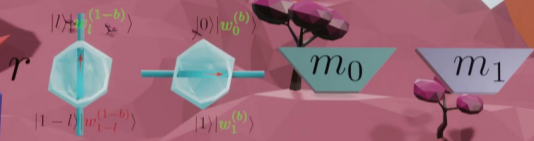
If $b = 0$



Random string starting with 0

Random string starting with 1

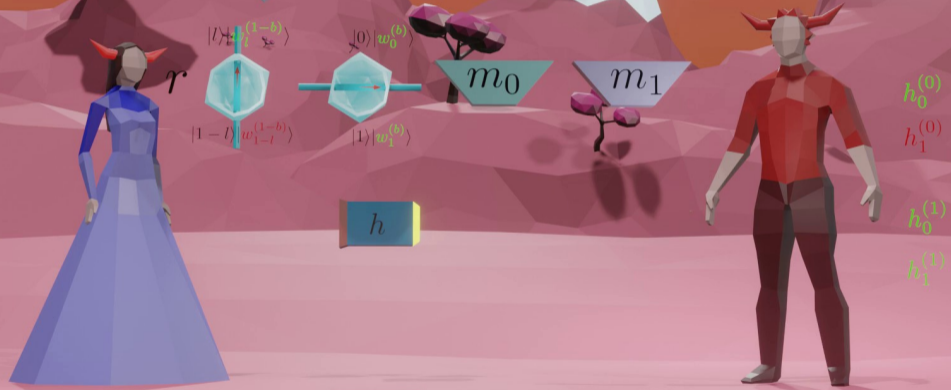
If $b = 1$



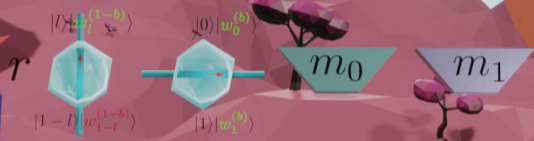
Random string starting with 0

Random string starting with 1

If $b = 1$



If $b = 1$



Proof

Prove that $\exists (w_d^{(c)})_{c,d}$, s.t. $\forall c, d, h_d^{(c)} = h(d||w_d^{(c)})$
and $\exists c, d$ s.t. $w_d^{(c)}[1] = 1$

$h_0^{(0)}$
 $h_1^{(0)}$
 $h_0^{(1)}$
 $h_1^{(1)}$

If $b = 1$



r



m_0

m_1

$|l\rangle|w_l^{(1-b)}\rangle$

$|0\rangle|w_0^{(b)}\rangle$

$|1-l\rangle|w_{1-l}^{(1-b)}\rangle$

$|1\rangle|w_1^{(b)}\rangle$



$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

$h_1^{(1)}$

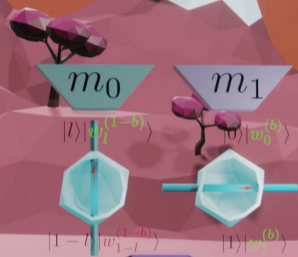


Proof

If $b = 1$



r



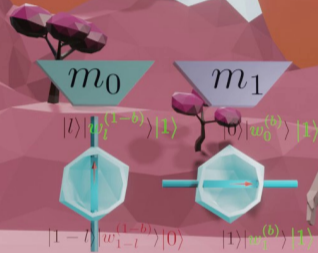
Proof

$h_0^{(0)}$
 $h_1^{(0)}$
 $h_0^{(1)}$
 $h_1^{(1)}$



If $b = 1$

r



$\forall c$, run on state c the unitary $U_{f^{(c)}}$ with:
 $f^{(c)}(x, w) = w[1] \neq 1 \wedge \exists d, h(x||w) = h_d^{(c)}$

$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

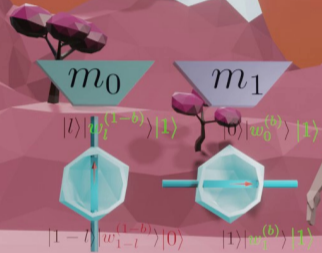
$h_1^{(1)}$

Proof

If $b = 1$



r



$h_0^{(0)}$
 $h_1^{(0)}$
 $h_0^{(1)}$
 $h_1^{(1)}$

$\forall c$, run on state c the unitary $U_{f^{(c)}}$ with:
 $f^{(c)}(x, w) = w[1] \neq 1 \wedge \exists d, h(x||w) = h_d^{(c)}$

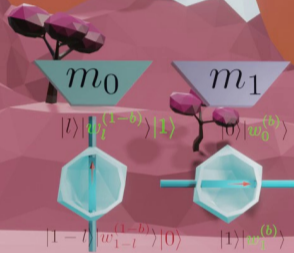
Measure output, check = 1



If $b = 1$



r



$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

$h_1^{(1)}$

$\forall c$, run on state c the unitary $U_{f^{(c)}}$ with:
 $f^{(c)}(x, w) = w[1] \neq 1 \wedge \exists d, h(x||w) = h_d^{(c)}$

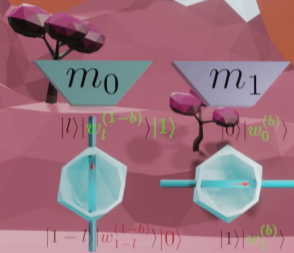
Measure output, check = 1

Proof

If $b = 1$



r



$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

$h_1^{(1)}$

$\forall c$, run on state c the unitary $U_{f^{(c)}}$ with:
 $f^{(c)}(x, w) = w[1] \neq 1 \wedge \exists d, h(x||w) = h_d^{(c)}$

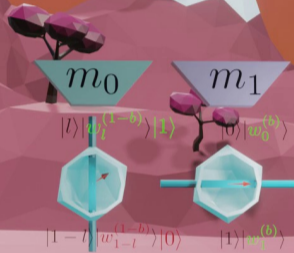
Measure output, check = 1

Proof

If $b = 1$



r



$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

$h_1^{(1)}$

Proof

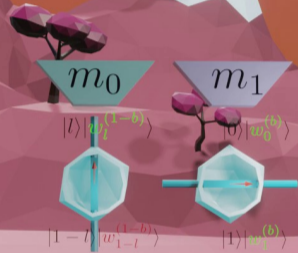
$\forall c$, run on state c the unitary $U_{f^{(c)}}$ with:
 $f^{(c)}(x, w) = w[1] \neq 1 \wedge \exists d, h(x||w) = h_d^{(c)}$

Measure output, check = 1

If $b = 1$



r



$h_0^{(0)}$
 $h_1^{(0)}$
 $h_0^{(1)}$
 $h_1^{(1)}$

$\forall c$, run on state c the unitary $U_{f^{(c)}}$ with:
 $f^{(c)}(x, w) = w[1] \neq 1 \wedge \exists d, h(x||w) = h_d^{(c)}$

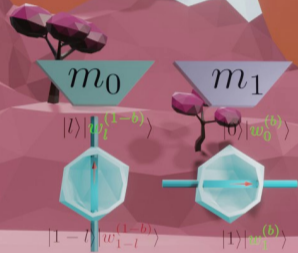
Measure output, check = 1



If $b = 1$



r



Mesure the second register in H basis



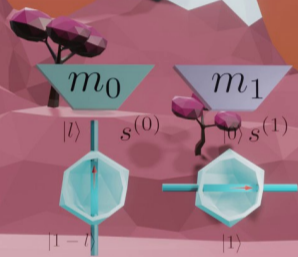
$h_0^{(0)}$
 $h_1^{(0)}$
 $h_0^{(1)}$
 $h_1^{(1)}$



If $b = 1$



r



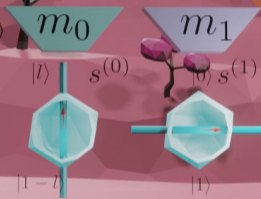
$h_0^{(0)}$
 $h_1^{(0)}$
 $h_0^{(1)}$
 $h_1^{(1)}$

Mesure the second register in H basis



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$



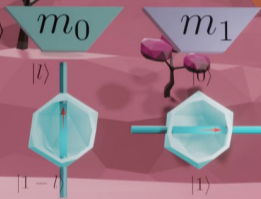
Mesure the second register in H basis

$$\begin{aligned} h_0^{(0)} \\ h_1^{(0)} \\ h_0^{(1)} \\ h_1^{(1)} \end{aligned}$$

Proof

If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$



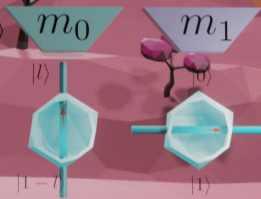
$$\begin{aligned} h_0^{(0)} \\ h_1^{(0)} \\ h_0^{(1)} \\ h_1^{(1)} \end{aligned}$$

Mesure the second register in H basis

Proof

If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$



$$h_0^{(0)}$$

$$h_1^{(0)}$$

$$h_0^{(1)}$$

$$h_1^{(1)}$$

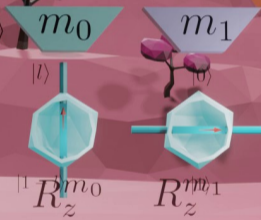
We got (NI)ZKoQS !

(one state is collapsed, Bob does not know which one)
 (NI)ZKoQS = Non-Interactive Zero-Knowledge Proof on Quantum State



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$



$$h_0^{(0)}$$
$$h_1^{(0)}$$
$$h_0^{(1)}$$
$$h_1^{(1)}$$

Proof

If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

$$m_0$$

$$m_1$$

$$|l\rangle$$



$$R_z^{m_0}$$

$$R_z^{m_1}$$

$$h_0^{(0)}$$

$$h_1^{(0)}$$

$$h_0^{(1)}$$

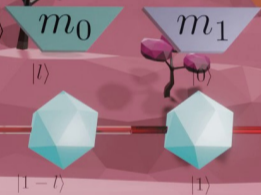
$$h_1^{(1)}$$

Proof



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$



$$\begin{aligned} h_0^{(0)} \\ h_1^{(0)} \\ h_0^{(1)} \\ h_1^{(1)} \end{aligned}$$

Proof



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1

$s_0 \quad s_1$

$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

$h_1^{(1)}$

Proof



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1

$$m_b = s_b \oplus$$

$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

$h_1^{(1)}$

Proof



If $b = 1$

$$m_b = s_b \oplus r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1

$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

$h_1^{(1)}$

Proof



If $b = 1$

$$m_b = s_b \oplus r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1

$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

$h_1^{(1)}$

Proof



If $b = 1$

$$m_b = s_b \oplus r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1

$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

$h_1^{(1)}$

Proof

If $b = 1$

$$m_b = s_b \oplus r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1

$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

$h_1^{(1)}$

Proof

If $b = 1$

$$m_b = s_b \oplus r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1

$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

$h_1^{(1)}$

Proof

Alice ($b \in \{0, 1\}$)

Bob ($(m_0, m_1) \in \{0, 1\}^2$)

$$\forall d \in \{0, 1\}, w_d^{(b)} \leftarrow_{\$} \{0\} \times \{0, 1\}^n$$

$$l \leftarrow_{\$} \{0, 1\}$$

$$w_l^{(1-b)} \leftarrow_{\$} \{0\} \times \{0, 1\}^n$$

$$w_{1-l}^{(1-b)} \leftarrow_{\$} \{1\} \times \{0, 1\}^n$$

$$\forall (c, d) \in \{0, 1\}^2, h_d^{(c)} := h(d \| w_d^{(c)})$$

$\pi :=$ (NI)ZK proof that:

$$\exists (w_d^{(c)})_{c,d}, \forall c, d, h_d^{(c)} = h(d \| w_d^{(c)})$$

$$\text{and } \exists c, d \text{ s.t. } w_d^{(c)}[1] = 1.$$

$$r^{(b)} \leftarrow_{\$} \{0, 1\}$$

$$|\psi^{(b)}\rangle := |0\rangle |w_0^{(b)}\rangle + (-1)^{r^{(b)}} |1\rangle |w_1^{(b)}\rangle$$

$$|\psi^{(1-b)}\rangle := |l\rangle |w_l^{(1-b)}\rangle$$

If the ZK proof is interactive, then we actually run the ZK protocol (before sending the quantum state) instead of sending the proof (of course this adds additional rounds of communication).

$$\xrightarrow{\forall (c, d) : h_d^{(c)}, \pi, |\psi^{(0)}\rangle, |\psi^{(1)}\rangle}$$

Check (or run if interactive proof) π .

$\forall c$, apply on $|\psi^{(c)}\rangle |0\rangle$ the unitary:

$$x, w \mapsto w[1] \neq 1 \wedge \exists d, h(x \| w) = h_d^{(c)},$$

measure the last (output) register and check that the outcome is 1.

$\forall c$, measure the second register of $|\psi^{(c)}\rangle$

in the Hadamard basis (with outcome $s^{(c)}$).

At that step, $|\psi^{(b)}\rangle = |0\rangle \pm |1\rangle$ and $|\psi^{(1-b)}\rangle = |l\rangle$, but Bob does not know b (NIZKoQS).

..... End of NIZKoQS

$\forall c$, apply Z^{m_c} on $|\psi^{(c)}\rangle$ and measure it

in the Hadamard basis (with outcome $z^{(c)}$).

$$\xleftarrow{\forall c, s^{(c)}, z^{(c)}}$$

$$\text{Compute } \alpha := r^{(b)} \oplus \bigoplus_i s^{(b)} [i] (w_0^{(b)} \oplus w_1^{(b)}) [i]$$

return $\alpha \oplus z^{(b)}$ / Should be m_b

Security Proof

Composable security (informal)

The protocol quantum-standalone realizes the OT functionality, assuming that:

- h is **collision resistant** (security against malicious Alice),
- h is **hiding**¹ (i.e. no information leaks on x given $h(x||r)$, security against malicious Bob).
- There exists a ZK **proof of knowledge**

Moreover, it is secure against **statistically unbounded parties** if the ZK protocol is secure in that setting and if the corresponding assumptions statistically hold (e.g. injective h for unbounded Alice, lossy h for unbounded Bob).

¹ Note that we can get an even weaker assumption (h is one-way) by using hardcore bits and the Goldreich-Levin construction, but we leave the formalization of this proof for future work.

If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1

$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

$h_1^{(1)}$

Proof



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1

$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

$h_1^{(1)}$

Proof



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1

$h_0^{(0)}$

$h_1^{(0)}$

$h_0^{(1)}$

$h_1^{(1)}$



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1



If $= 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1



If $\sigma = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1

h_0

h_1

h_2

h_3

Proof



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1



h_0

h_1

h_2

h_3



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1



h_0

h_1

h_0

h_1

At most 4 elements in the superposition
(or collision with the extracted values)



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_0

m_1



$h_0^{(b)}$

$h_1^{(b)}$

$h_0^{(b)}$

$h_1^{(b)}$

No element map to the dummy hash
(or collision with the extracted values)



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_1

h_0

h_1

h_2

h_3

No element map to the dummy hash
(or collision with the extracted values)



If $b = 1$

$$r \oplus \langle s^{(b)}, w_0^{(b)} \oplus w_1^{(b)} \rangle$$

m_1

h_0
 h_1
 h_2
 h_3

No element map to the dummy hash
(or collision with the extracted values)

Proof

Quantum language and ZK on quantum state

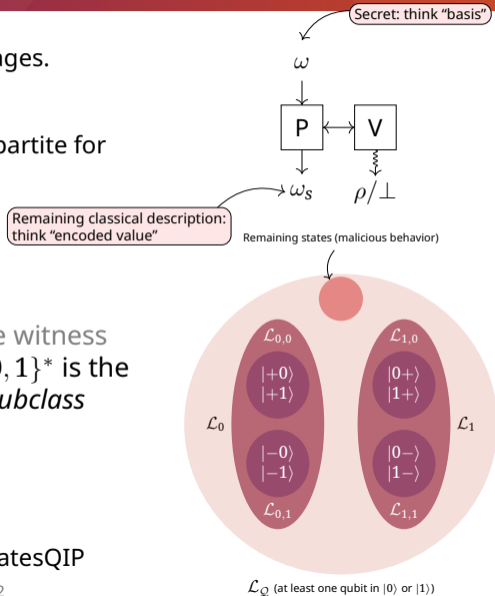
Quantum language and ZKoQS

Quantum language = generalization of classical languages.

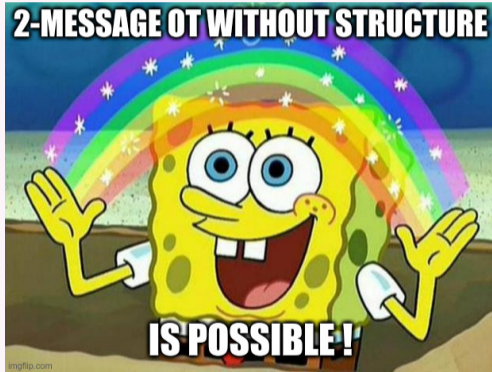
Properties of ZK on Quantum States (informal):

- **Soundness:** \mathcal{L}_Q = **subset of quantum states** (bipartite for the adversary).
 - Classically $x \in \mathcal{L}$ if V accepts
 - Quantumly $\rho \in \mathcal{L}_Q$ if V accepts
- **Correctness:**
 - Classically: $x \in \mathcal{L}_w \subset \mathcal{L}$, $w \in \{0, 1\}^*$ is the witness
 - Quantumly: $\rho \in \mathcal{L}_{\omega, \omega_s} \subseteq \mathcal{L}_\omega \subseteq \mathcal{L}_Q$, $\omega \in \{0, 1\}^*$ is the witness or *class*, and $\omega_s \in \{0, 1\}^*$ is the *subclass*
- **Zero-Knowledge:**
 - Classically: Bob can't learn info on w
 - Quantumly: Bob can't learn info on ω

⇒ We introduce complexity classes ZKstatesQMA/ZKstatesQIP



Take-home message



(and Zero-Knowledge proofs on quantum states)

Open questions and ongoing works

- **Characterize ZKstatesQMA**

What are the other ZKoQS properties that can(not) be verified?
Under which assumption?

- **Role of entanglement**

Prove (im)possibility of similar ZKoQS with only **single-qubit** operations? (entanglement seems important)

- **Other applications?**

Quantum money, reducing communication complexity in other protocol...

- ...



Thank you!



Thank you!

Supplementary materials

Comparison with existing works

Article	Classical	Setup	Messages	MiniQCrypt	Composable	Statistical
[PVW08]	Yes	CRS	2	No (LWE)	Yes	Either
[BD18]	Yes	Plain M.	2	No (LWE)	Sender	Receiver
[CK88] + later works	No	Depends	7	Yes	Yes [DFL+09],[Unr10]	Either
[GLSV21]	No	Plain M./ CRS	poly/ $\text{cte} \geq 7$	Yes	Yes	No
[BCKM21]	No	Plain M./ CRS	poly/ $\text{cte} \geq 7$	Yes	Yes	Sender
[ABKK23]	No	RO	3	Yes	Yes	No
This work + [Unr15]	No	RO	2	Yes	Yes	No
This work + [HSS11]	No	Plain M.	> 2	No (LWE)	Yes	No
This work + S-NIZK	No	Like ZK	2	Like ZK	Yes	Sender
This work + NIZK proof	No	Like ZK	2	Like ZK	Yes	Receiver
This work + ZK	No	Like ZK	ZK +1 or 2 ¹	Like ZK	Yes	Like ZK

Classical Zero-Knowledge



Classical Zero-Knowledge

Solution exists?



1			
		4	
		3	
	2		



Classical Zero-Knowledge

Yes!
I won't reveal it.

Solution exists?

1	⊙	⊙	⊙
⊙	⊙	4	⊙
⊙	⊙	3	⊙
⊙	2	⊙	⊙



Classical Zero-Knowledge

Yes!
I won't reveal it.

I don't trust you.

1	⊙	⊙	⊙
⊙	⊙	4	⊙
⊙	⊙	3	⊙
⊙	2	⊙	⊙



Classical Zero-Knowledge

Yes!
I won't reveal it.

I don't trust you.

1	⊙	⊙	⊙
⊙	⊙	4	⊙
⊙	⊙	3	⊙
⊙	2	⊙	⊙



Classical Zero-Knowledge

Yes!
I won't reveal it.

I don't trust you.

1	4	2	3
2	3	4	1
4	1	3	2
3	2	1	4



Classical Zero-Knowledge

Yes!
I won't reveal it.

I don't trust you.



1	⊙	⊙	⊙
⊙	⊙	4	⊙
⊙	⊙	3	⊙
⊙	2	⊙	⊙



Classical Zero-Knowledge

Yes!
I won't reveal it.

I don't trust you.



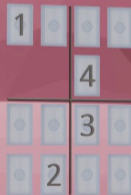
1	⊙	⊙	⊙
⊙	⊙	4	⊙
⊙	⊙	3	⊙
⊙	2	⊙	⊙



Classical Zero-Knowledge

Yes!
I won't reveal it.

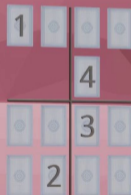
I don't trust you.



Classical Zero-Knowledge

Yes!
I won't reveal it.

I don't trust you.



Classical Zero-Knowledge

Yes!
I won't reveal it.

I don't trust you.



Classical Zero-Knowledge

Yes!
I won't reveal it.

Ok, I trust you.



Classical Zero-Knowledge



Generalizable in a non-interactive way to NP problems.