

### Differential Meet-in-the-Middle **Cryptanalyis**

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# Can we use meet-in-the-middle related techniques to improve differential attacks?



#### **Differential Attack**



 $\Delta_{out}$ 

 $\begin{array}{l} \text{top } P[\Delta_{in} \rightarrow \Delta_X] = 2^{-c_{in}} \\ \text{middle } P[\Delta_X \rightarrow \Delta_Y] = 2^{-p} \\ \text{bottom } P[\Delta_{out} \rightarrow \Delta_Y] = 2^{-c_{out}} \end{array}$ 

#### Main idea

Given  $\alpha 2^{c_{in}} 2^{p}$  pairs with difference  $\Delta_{in}$ , we expect on average  $\alpha$  pairs following the differential in the middle rounds and thus the **right value** for  $k_{in} \cup k_{out}$  should appear  $\alpha$  times.



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Given one pair of data, how to determine possible values for  $k_{in} \cup k_{out}$  ?

### **Differential Attack - Retrieving Key Candidates**



- Early abort technique
- Rebound-like procedure
- Knowing both input/output differences around an Sbox leads to the actual values
- Might be very complex depending on the key schedule and the cipher









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Time complexity  $\approx 2^k$  encryptions, with 2k-bit keys!

### More complicated (Dong et al., CRYPTO'21)







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- Reduce complexities of MitM attacks
- Rely on truncated differential characteristics only





#### **Procedure:**

- 1. Ask for one plaintext/ciphertext pair (P, C)
- 2. Construct the set of the  $|k_{in}|$  possible plaintexts  $\mathcal{P}$
- 3. Construct the set of the  $|k_{out}|$  possible ciphertexts C
- 4. Search for valid  $(P', C') \in \mathcal{P} \times \mathcal{C}$  by looking for a collision





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- 4. Search for valid  $(P', C') \in \mathcal{P} \times \mathcal{C}$  by looking for a collision
- Pro: Much easier to deal with the key
  - Specific improvement for ciphers with partial key addition
  - More memory than for classical differential attacks



- SKINNY-128-384: First attack against 25 rounds in the single tweakey model!
- AES-256: First attack against 12 rounds requiring only 2 related keys!



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Seem to work well when the key size is larger than the block size



#### **Two Targets - New Results**

• SKINNY-128-384: First attack against 25 rounds in the single tweakey model!

# Rounds	Data	Time	Memory	Туре	Ref.
21	2 <sup>123</sup>	2 <sup>353.6</sup>	2 <sup>341</sup>	ID	Yang et al.
21	$2^{122.89}$	2 <sup>347.35</sup>	2 <sup>336</sup>	ID	Hadipour et al.
22	2 <sup>96</sup>	2 <sup>382.46</sup>	2 <sup>330.99</sup>	DS-MITM	Shi et al.
22	2 <sup>92.22</sup>	2 <sup>373.48</sup>	$2^{147.22}$	ID	Tolba et al.
23	2 <sup>104</sup>	2 <sup>376</sup>	2 <sup>8</sup>	MITM	Dong et al.
23	2 <sup>117</sup>	2 <sup>361.9</sup>	$2^{118.5}$	Diff. MITM	new
24	$2^{117}$	2 <sup>361.9</sup>	2 <sup>183</sup>	Diff. MITM	new
24	$2^{122.3}$	2 <sup>372.5</sup>	2 <sup>123.8</sup>	Diff. MITM	new
25	2 <sup>122.3</sup>	2 <sup>372.5</sup>	2 <sup>188.3</sup>	Diff. MITM	new



### **Differential on SKINNY-128**

• For the 25-round attack, we use the following differential on 15 rounds:



• CP model from Delaune et al. (2021) to estimate its probability:  $2^{-p} \ge 2^{-116.5}$ 

• Note that the best differential characteristic has probability  $2^{-131}$ 



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• For the 25-round attack, we use the following differential on 15 rounds:



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  - Note that the best differential characteristic has probability  $2^{-131}$
- Extended by adding 4 rounds to the plaintext, 5 rounds to the ciphertext and one extra free round



#### 4 rounds to the plaintext





#### **Extra Free Round**



- The round key is only applied to the first two rows
- Consider structure of 2<sup>64</sup> plaintext/ciphertext pairs
- The attack is performed on the 2<sup>64</sup> pairs in parallel





#### **Procedure:**

- 1. Ask for one structure of  $2^{64}$  plaintext/ciphertext pair (P, C)
- 2. Construct the set of the  $|k_{in}|$  possible plaintexts  ${\cal P}$
- 3. Construct the set of the  $|k_{out}|$  possible ciphertexts C
- 4. Search for valid  $(P', C') \in \mathcal{P} \times \mathcal{C}$  by looking for a collision





#### Procedure: repeat 2<sup>p</sup> times

- 1. Ask for one structure of  $2^{64}$  plaintext/ciphertext pair (P, C)
- 2. Construct the set of the  $|k_{in}|$  possible plaintexts  ${\cal P}$
- 3. Construct the set of the  $|k_{out}|$  possible ciphertexts C
- 4. Search for valid  $(P', C') \in \mathcal{P} \times \mathcal{C}$  by looking for a collision





#### **Procedure:** repeat $2^p/2^{64}$ times

- 1. Ask for one structure of  $2^{64}$  plaintext/ciphertext pair (P, C)
- 2. Construct the set of the  $|k_{in}|$  possible pairs of plaintexts  $\mathcal{P}$
- 3. Construct the set of the  $|k_{out}|$  possible pairs of "ciphertexts" C
- 4. Search for valid  $((P, P'), (C, C')) \in \mathcal{P} \times \mathcal{C}$  by looking for a collision



#### Conclusion

- New cryptanalysis technique: the Differential MITM attack
- More improvements described in the paper (e.g. data reduction)
- First attack against 25-round SKINNY-128-384 in the single tweakey model
- First attack against 12-round AES-256 with only two related keys
- Many open questions and future works:
  - When is this framework better than classical differential attacks?
  - Can we automatize the search of such attacks?
  - Can this framework work with truncated differentials?
  - Can we combine MitM attacks with other cryptanalysis techniques?
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## Thank you for your attention!