#### Non-Interactive Publicly-Verifiable Delegation of Committed Programs

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# **Problem Setup**



















Input Provider











![](_page_13_Figure_0.jpeg)

![](_page_14_Figure_0.jpeg)

![](_page_15_Figure_0.jpeg)

![](_page_16_Picture_0.jpeg)

#### Goals

![](_page_17_Picture_1.jpeg)

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![](_page_18_Picture_1.jpeg)

Non-Interactive Delegation	<ul> <li>Uni-directional Arrows</li> <li>No Back and Forth Communication</li> </ul>	
Public Verification	• Same proof ∏ for all verifiers	
Public Delegation	<ul> <li>No pre-processing specific to <i>P</i> before delegating to Worker</li> <li>No dependence of <i>H<sub>P</sub></i> on input <i>x</i></li> </ul>	
Succinctness	•     : poly ( $\lambda$ , log   $P$  ,   $x$  ) • Verifier run-time: poly ( $\lambda$ , log   $P$  ,   $x$  ) • Prover run-time: poly ( $\lambda$ ,   $P$  ,   $x$  )	

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Very recent work [CJJ21] comes the closest by achieving "SNARG for P from LWE"

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Main Theorem

Assuming the hardness of the LWE problem, there exists a construction for publicly verifiable non-interactive succinct delegation for committed programs with CRS size, proof size and verifier time poly( $\lambda$ , log |P|, |x|) and prover run time being poly( $\lambda$ , |P|, |x|).

Such a delegation scheme in the CRS model involves the following PPT algorithms:

- Setup( $1^{\lambda}$ ): Randomized setup algorithm that outputs crs
- ProgAuth( $1^{\lambda}$ , crs): Randomized algorithm that outputs P, state,  $H_P$
- Prover(crs, *P*, *state*,  $H_P$ , *x*): Deterministic algorithm that outputs a value *y* and proof  $\prod$
- Verifier(crs,  $H_P$ , x, y, $\Pi$ ): Deterministic verifier which either accepts or rejects

**Completeness** 

For all PPT ProgAuth, if *crs* is appropriately generated and Prover runs honestly then,  $Pr[V(crs, H_P, x, y, \prod) = 1 \land P(x) = y] = 1$ 

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#### Soundness

For all PPT adversaries  $(A_1, A_2)$  and all ProgAuth, if *crs* is appropriately generated and  $(x, aux) \leftarrow A_1(crs)$ ,  $(y, \prod) \leftarrow A_2(crs, P, H_P, x, aux)$ , then

 $\Pr[V(crs, H_P, x, y, \prod) = 1 \land P(x) \neq y] \leq negl(\lambda)$ 

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![](_page_53_Figure_2.jpeg)

![](_page_54_Picture_1.jpeg)

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- Now, we can use the techniques from CJJ21 to construct a **SEMI-TRUSTED** SNARG For NP.

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 Nothing changes in the real world. In the simulated world, we can switch the CRS to have a commitment of 1 and the NIZK/NIWI proof will not use ∏ at all. **THANK YOU!**