

Careful with MAc-then-SIGn:  
A Computational Analysis of the EDHOC Lightweight  
Authenticated Key Exchange Protocol

Felix Günther and **Marc Ilunga**

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**ETH** zürich



## Proliferation of low-powered devices



Image by Moritz Kindler

- Limited computing power
- Bandwidth constraints
- Plagued by vulnerabilities<sup>1</sup>

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- Missing satisfactory solutions
- EDHOC: a proposal by the IETF LAKE WG.
- Use case: OSCORE<sup>1</sup> protocol (secure transport)
- 4 mutual authentication methods (static DH and/or Signature)
  - This talk: SIG-SIG
  - Design similar to TLS1.3 and based on SIGMA<sup>2</sup>

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- Q: Why not simply use TLS 1.3?
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## (D) TLS 1.3 is not lightweight: up to 7x bandwidth usage

	Total protocol size (bytes) <sup>1</sup>
DTLS 1.3 (ECDHE)	880
TLS 1.3 (ECDHE)	789
EDHOC (STAT-STAT)	101

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<sup>1</sup>empty citation.

## EDHOC in SIG-SIG Mode: An AKE based on Diffie-Hellman



INITIATOR (1)

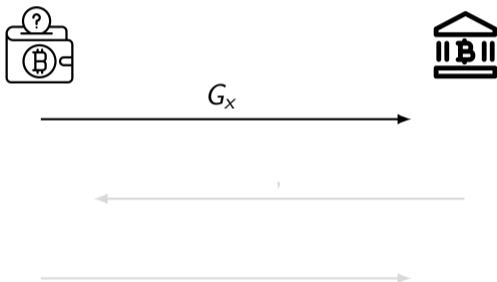
$$x \xleftarrow{\$} \mathbb{Z}_q; G_x \leftarrow xG$$

RESPONDER(1)

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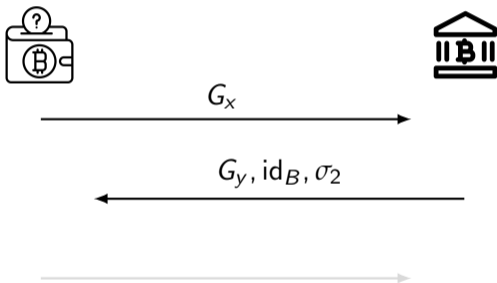
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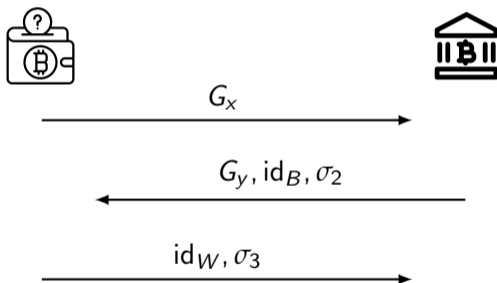
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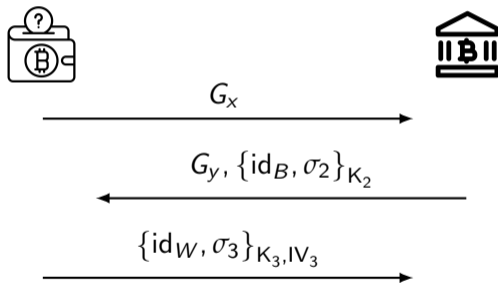
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## EDHOC in SIG-SIG Mode: An AKE with identity protection



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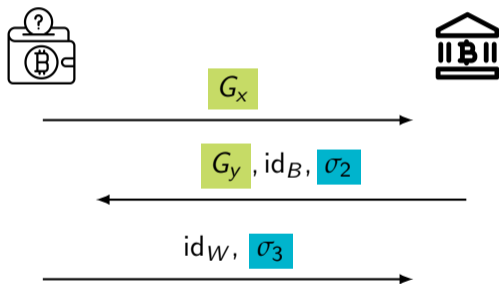
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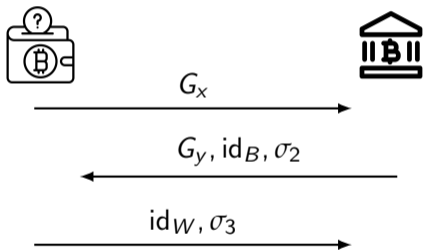
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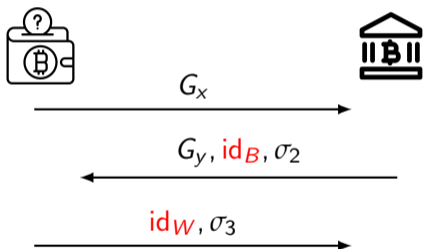
# EDHOC SIG-SIG $\approx$ SIGMA: MAC "under" signature



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## EDHOC SIG-SIG $\approx$ SIGMA: Abbreviated identities

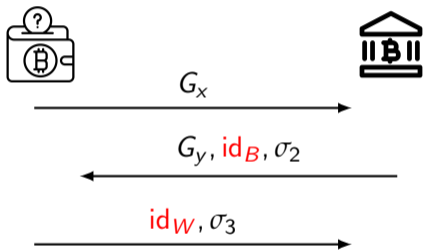


- $id_X$  Short credential identifier for  $X$
- size  $\ll$  X.509 Cert

- need not be unique<sup>1</sup>

*applications MUST NOT assume that 'kid' values are unique and several keys associated with a 'kid' may need to be checked [by the recipient] before the correct one is found.*

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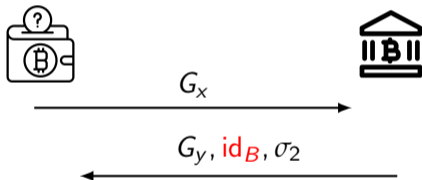


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<sup>1</sup>Selander, Mattsson, and Palombini, *Ephemeral Diffie-Hellman Over COSE (EDHOC) – draft-ietf-lake-edhoc-17*, Section 3.5.3.

## Abbreviated identifiers introduce new challenges



RUNINIT2

---

...

**foreach**  $(U, pk_U)$  **with**  $id_U = id_B$  :

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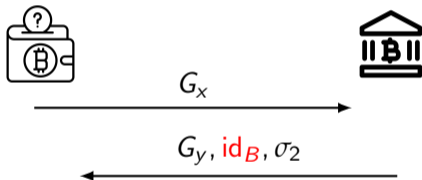
**if**  $\text{Sig.Vf}(pk_U, \tau_2, \dots, \sigma_2) = 1$  :

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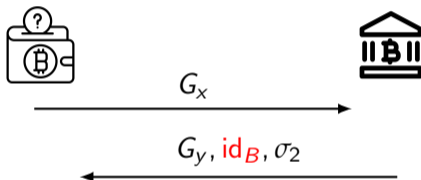
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What if an attacker also uses  $id_B$ ?

Duplicate Signature Key Selection attacks.

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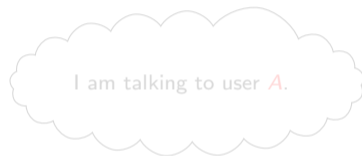
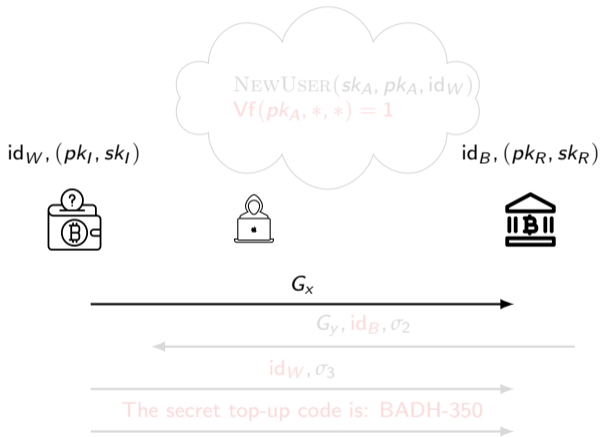
## DSKS attacks: Signature unforgeability is not enough

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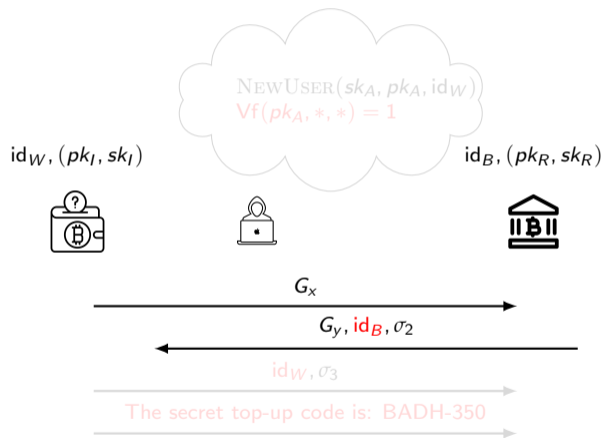
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# DSKS vs SIGMA



What about EDHOC?

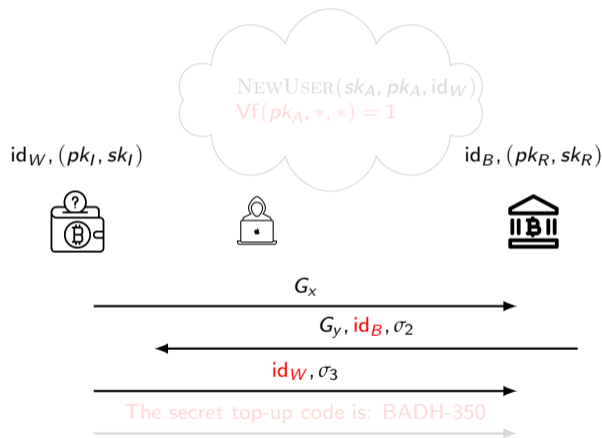
# DSKS vs SIGMA



I am talking to user *A*.

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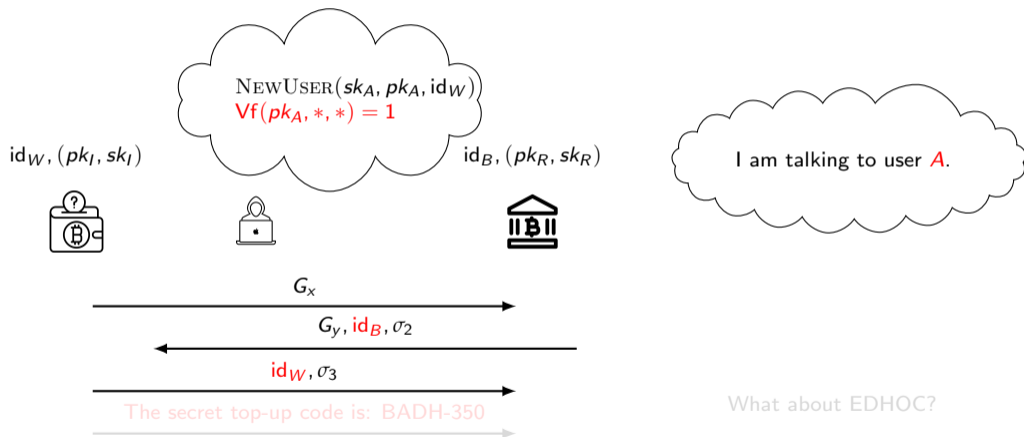
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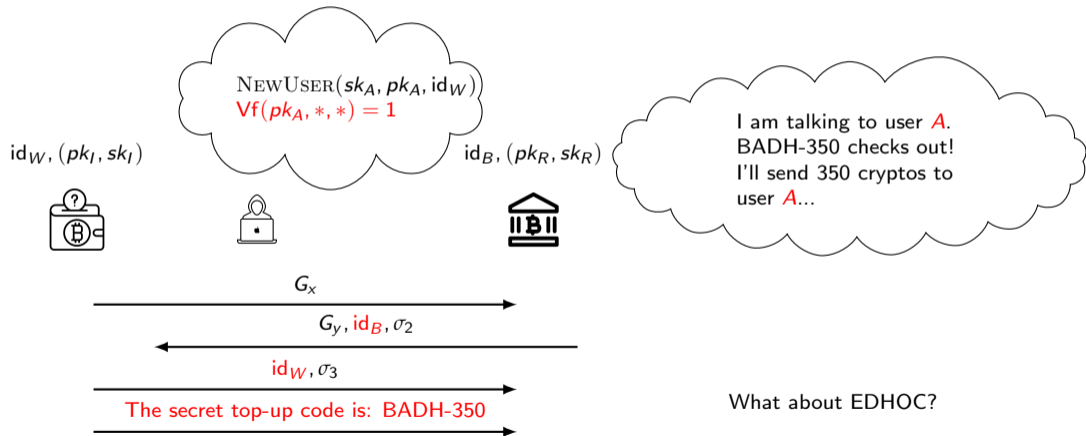
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## EDHOC provides strong authentication guarantees even under colliding identifiers

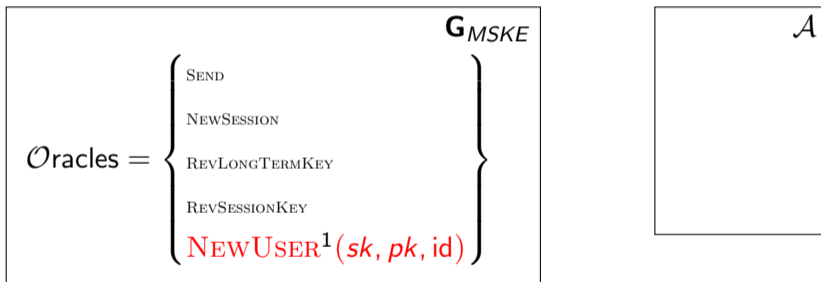
- Assuming **universal exclusive ownership**<sup>1</sup> of the signature schemes
- S-UEO for signature scheme  $\Sigma$  (informal):
  - Key pair:  $(pk, sk) \xleftarrow{\$} \Sigma.\text{KGen}()$
  - Adversary  $\mathcal{A}$  obtains  $\text{set}(m_i, \sigma_i)$  (produced by  $sk$ )
  - Goal of  $\mathcal{A}$ : Produce  $(pk^*, m^*)$  s.t  $\forall f(pk^*, m^*, \sigma_j) = 1$  and  $pk \neq pk^*$
  - S-UEO  $\implies \mathcal{A}$  cannot succeed.

---

<sup>1</sup>Pornin and Stern, "Digital Signatures Do Not Guarantee Exclusive Ownership".



## Security Model: Multi-Stage Key Exchange Model



<sup>1</sup>Boyd et al., "ASICS: Authenticated Key Exchange Security Incorporating Certification Systems".

## MSKE: Security goals

- Key indistinguishability
- Forward security
- Explicit authentication: When a session accepts with an authenticated peer, there is indeed a corresponding session of that peer.

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Let  $\mathcal{A}$  be an MSKE adversary. For at most  $n_U$  users and  $n_S$  sessions, there exists adversaries  $\mathcal{B}_j$  such that:

$$\begin{aligned} \text{Adv}_{\mathcal{A}}^{\text{MSKE}}(\text{EDHOC-Sig-Sig}) \leq & \frac{n_S^2}{q} + \\ & \text{Adv}_{\mathcal{B}_4}^{\text{CR}}(\text{H}) + \\ & 4n_S \left( n_U \cdot \text{Adv}_{\mathcal{B}_{1,2}}^{\text{SUF-CMA}}(\text{Sig}) + \right. \\ & \quad \left. \text{Adv}_{\mathcal{B}_{1,4}}^{\text{S-UEO}}(\text{Sig}) \right) + \\ & 4n_S \left( n_U \cdot \text{Adv}_{\mathcal{B}_{11,A2}}^{\text{EUF-CMA}}(\text{Sig}) + \right. \\ & \quad \left. \text{Adv}_{\mathcal{B}_{11,B2}}^{\text{snPRF-ODH}}(\text{Extract}) + \right. \\ & \quad \left. \text{Adv}_{\mathcal{B}_{11,B3}}^{\text{PRF}}(\text{Expand}) \right) \end{aligned}$$

Assumption	scheme	
Collision resistance	SHA2, Shake128	✓
SUF-CMA	Ed25519	✓
	ECDSA	✗
S-UEO	Ed25519	✓
	ECDSA	✗
EUF-CMA	Ed25519	✓
	ECDSA	✓
PRF-ODH	HKDF.Extract	✓
	KMAC	(?)
PRF	HKDF.Expand	✓
	KMAC	✓

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	KMAC	(?)
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	KMAC	✓

## ECDSA might be fine for EDHOC

- S-UEO **✗**: EDHOC includes the pub key alongside messages to be signed (✓)
- SUF-CMA **✗**: Implementations could use “canonical” signatures (✓ ?).

## Positive collaboration with the LAKE working group

- Numerous contributions to EDHOC by several parties
  - Jacomme et al.: Full symbolic analysis of latest draft<sup>1</sup>
  - Cottier & Pointcheval: Computation analysis of STAT-STAT<sup>2</sup>
  - Norman et al.: Early symbolic analysis<sup>3</sup>
- Reminiscent of development of TLS 1.3

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<sup>1</sup>Jacomme et al., "A comprehensive, formal and automated analysis of the EDHOC protocol".

<sup>2</sup>Cottier and Pointcheval, *Security Analysis of the EDHOC protocol*.

<sup>3</sup>Norrman, Sundararajan, and Bruni, "Formal Analysis of EDHOC Key Establishment for Constrained IoT Devices".



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- Worked through drafts (12-17)
- In an ideal world: tooling for automated proofs

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## Contributions overview: Insights from our computational analysis

- Dedicated session key ( $\text{PRK}_{out}$ ) added in draft 14 (with Jacomme et al.<sup>1</sup>)
- Full credentials in transcript hashes in key derivation.
- Transcript hashes from plaintext instead of ciphertexts
- Key separation in key derivation

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## Conclusion

- EDHOC is a LAKE for constrained environments with new security challenges
- Our contributions:
  - Strong security model for the LAKE setting
  - Security analysis and proof that EDHOC(SIG-SIG) is a secure LAKE in a strong adversarial model
  - Design contributions to EDHOC
- LAKE WG highly welcoming of security analysis and inputs

See EuroS&P 2023 Paper  
(eprint [ia.cr/2022/1705](https://ia.cr/2022/1705))  
[marc.ilunga@trailofbits.com](mailto:marc.ilunga@trailofbits.com)

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