

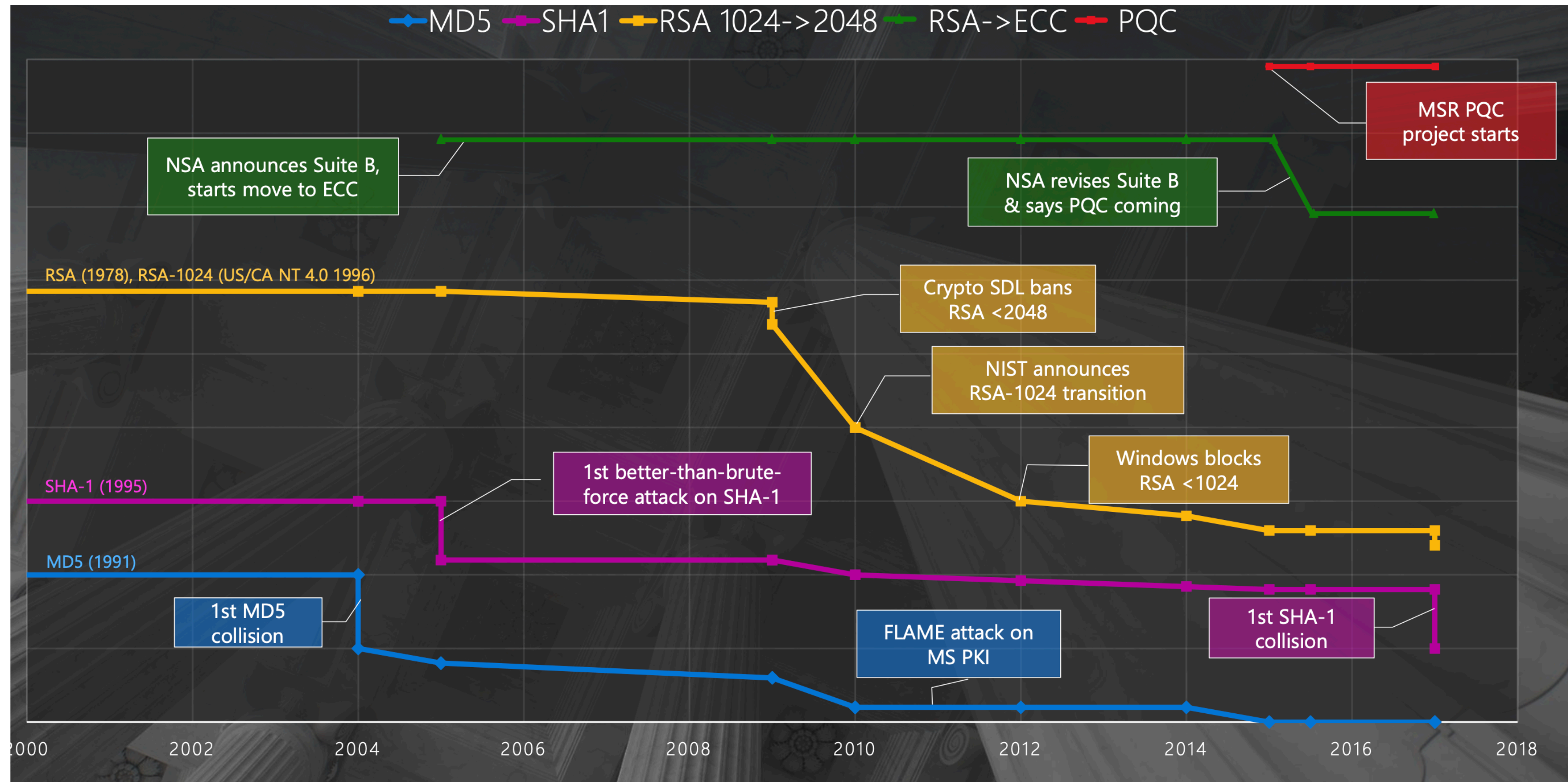
# Agile Cryptography: A Universally Composable Approach

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Input Output, Switzerland

Michele Ciampi  
The University of Edinburgh, UK

Aggelos Kiayias  
The University of Edinburgh &  
Input Output, UK

# Cryptographic algorithms need updates



Credit to Brian LaMacchia. The Long Road Ahead to Transition to Post-Quantum Cryptography, Invited Opening Keynote, IEEE Secure Development Conference 2022, Atlanta, GA, October 18-20

# Cryptographic agility

*“The ability to reconfigure an application or system with a different cryptographic algorithm (or implementation)\*”*

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- Ongoing transition to new algorithms
- Updates or changes to an implementation
- Modifying key configuration parameters
- Retiring deprecated algorithms

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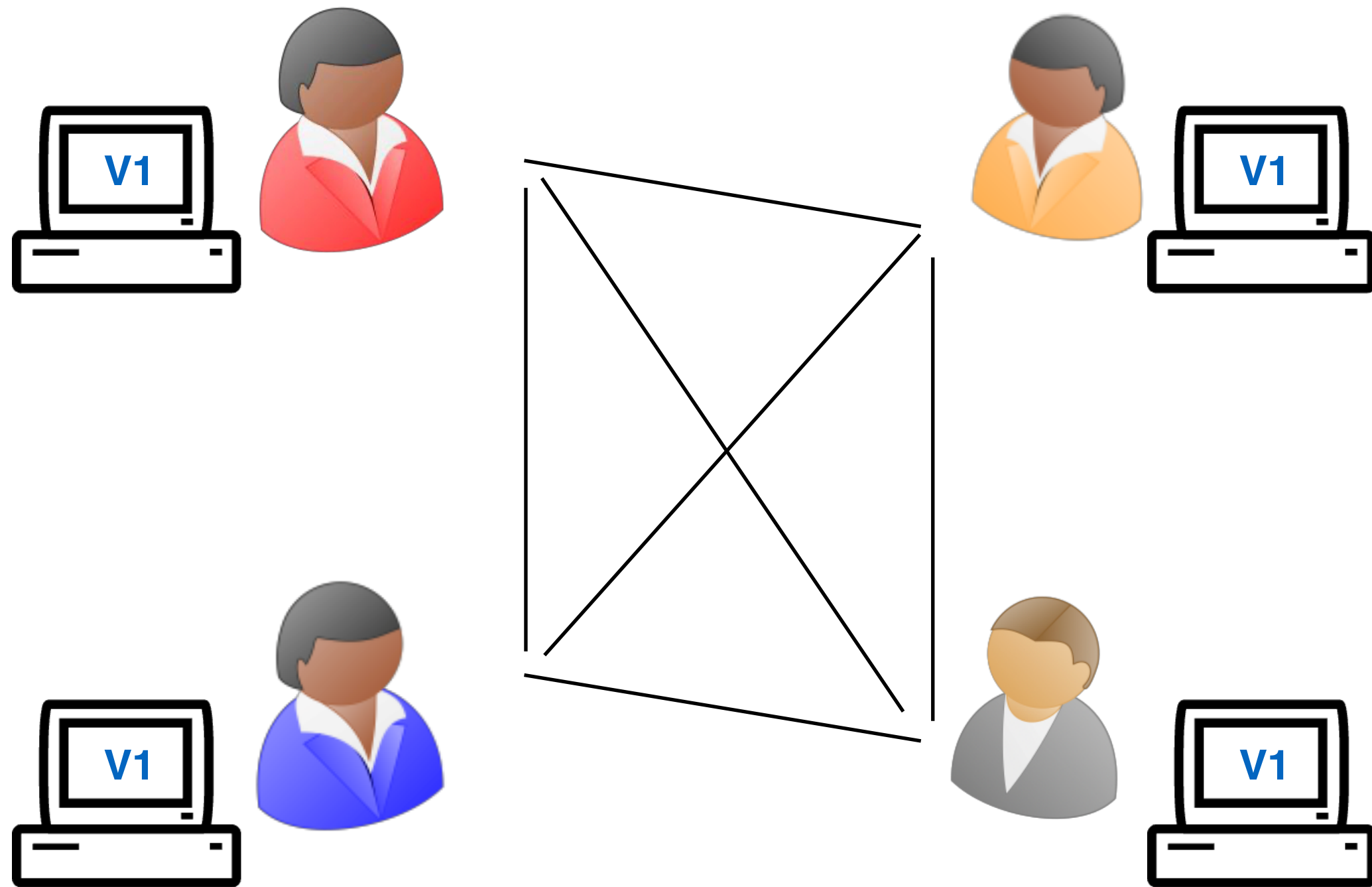
*“The ability to reconfigure an application or system with a different cryptographic algorithm (or implementation)\*”*

Cryptographic protocols need to be updated in practice. Why not in theory as well?

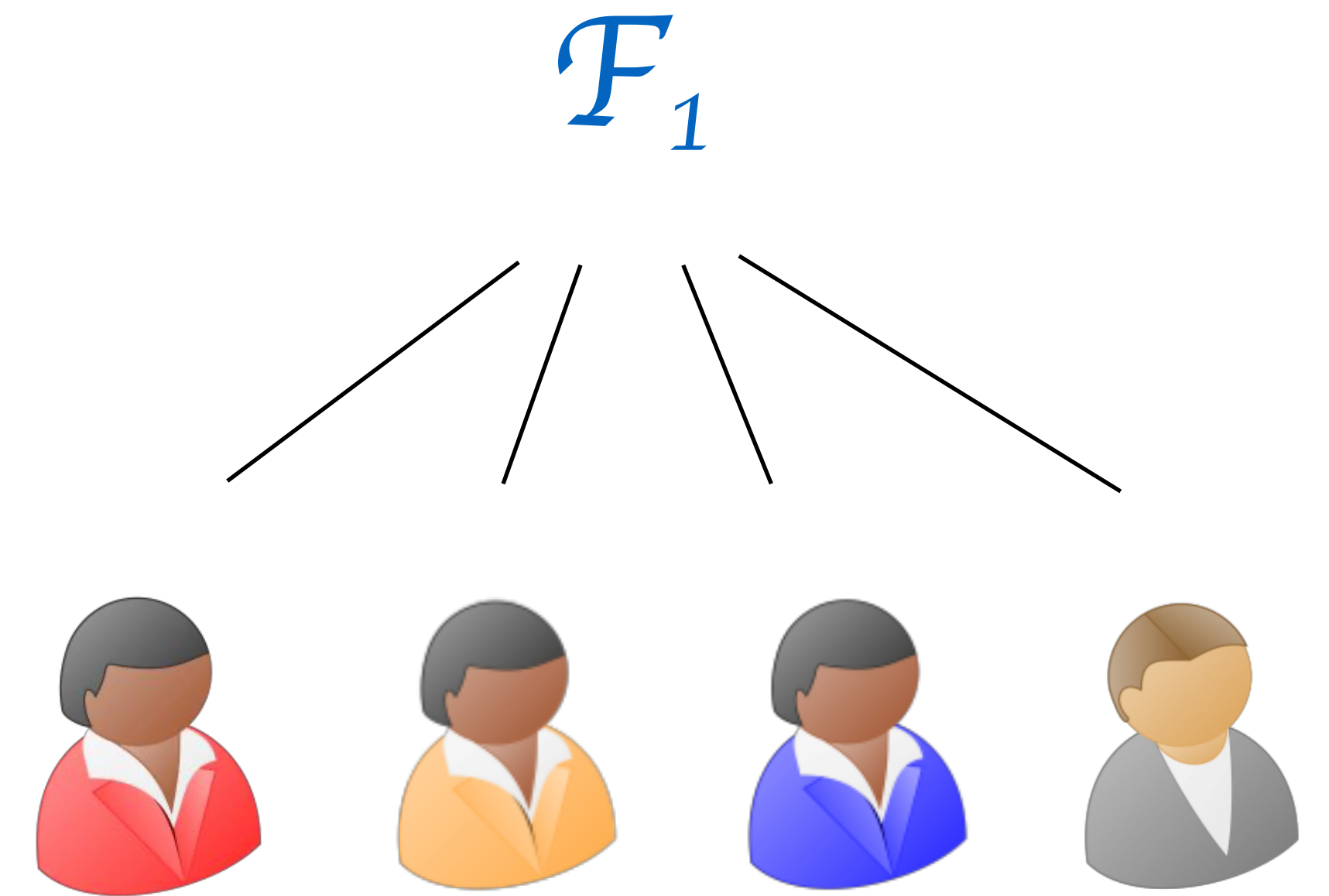
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Real

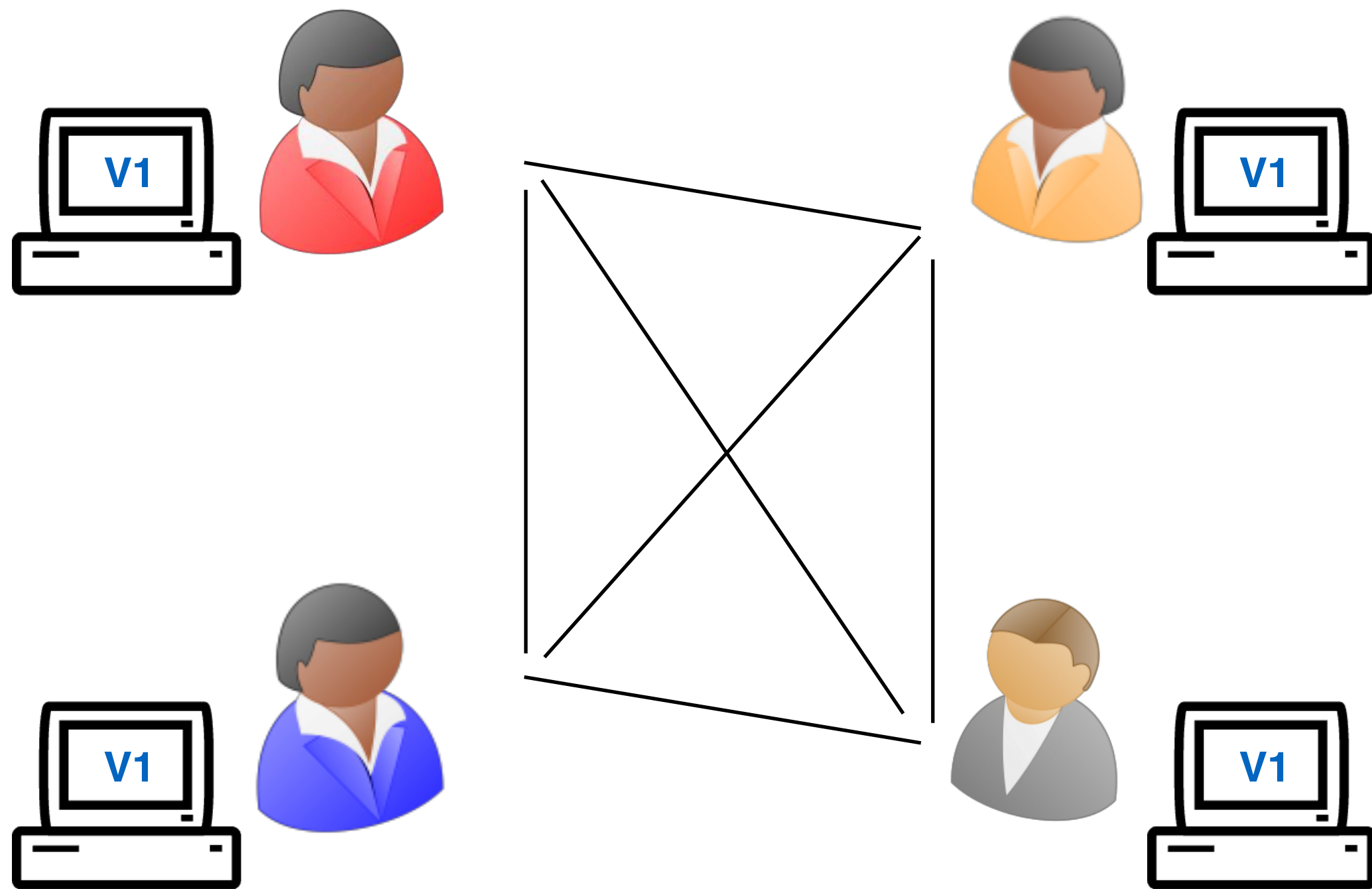


Ideal

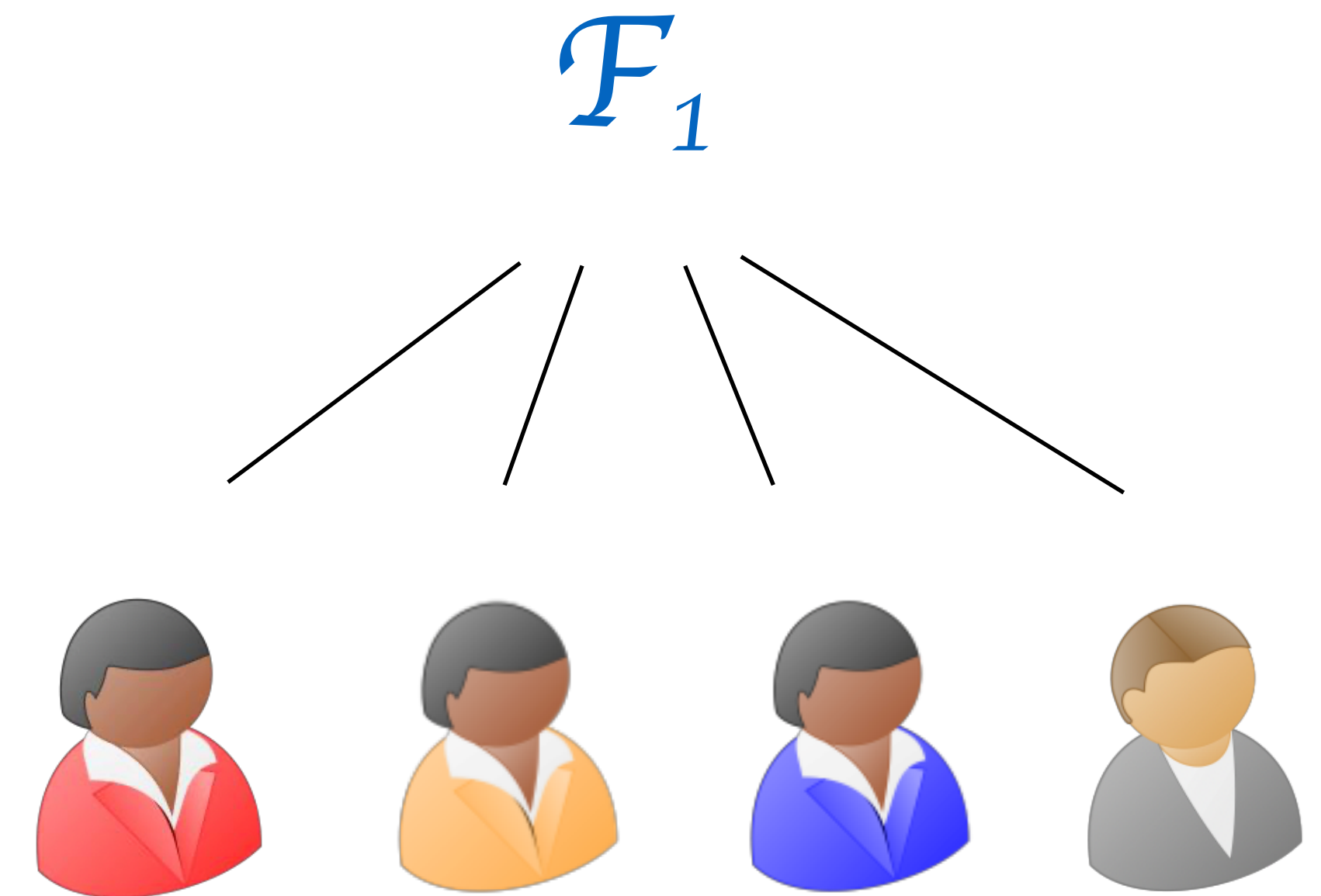


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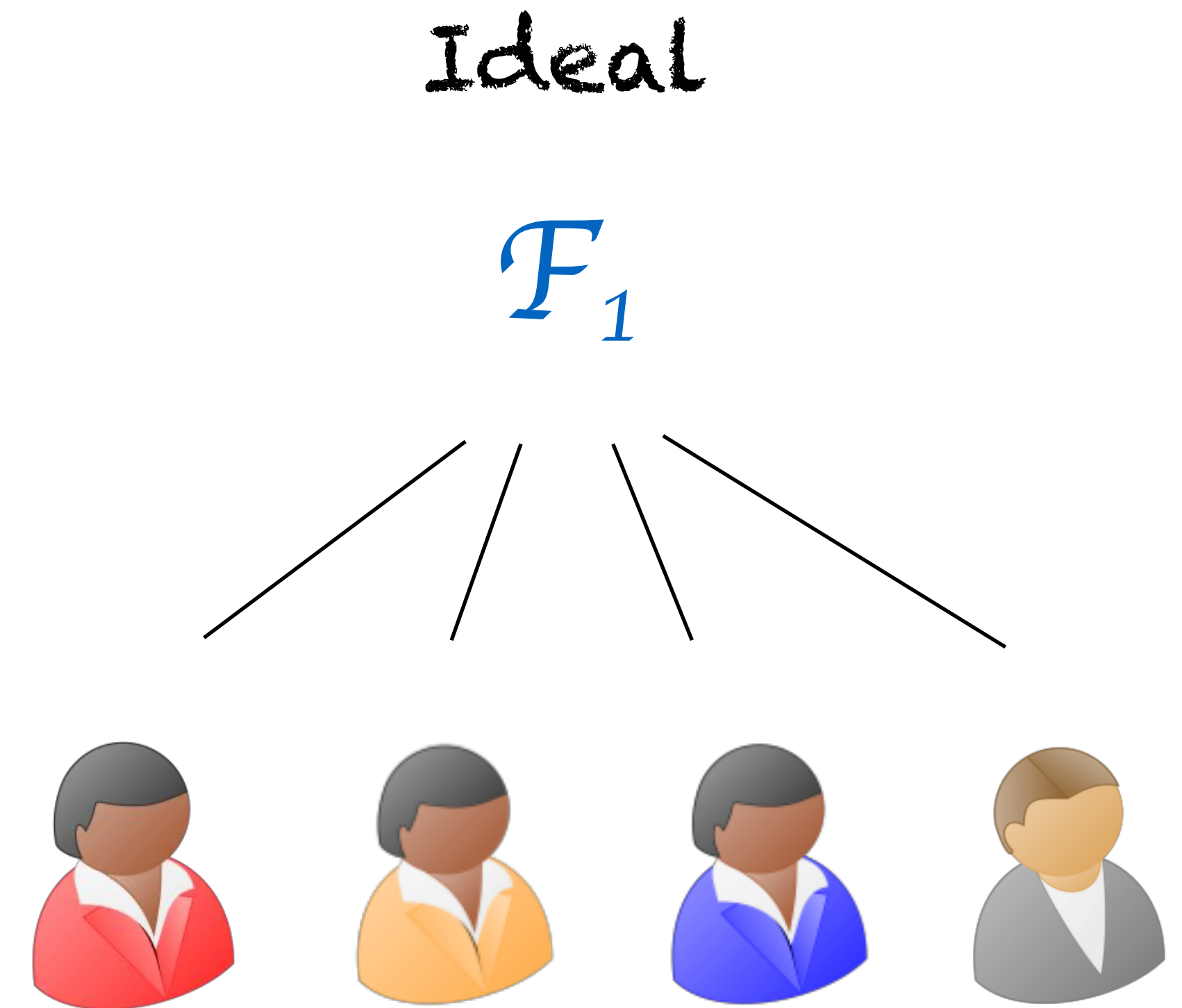
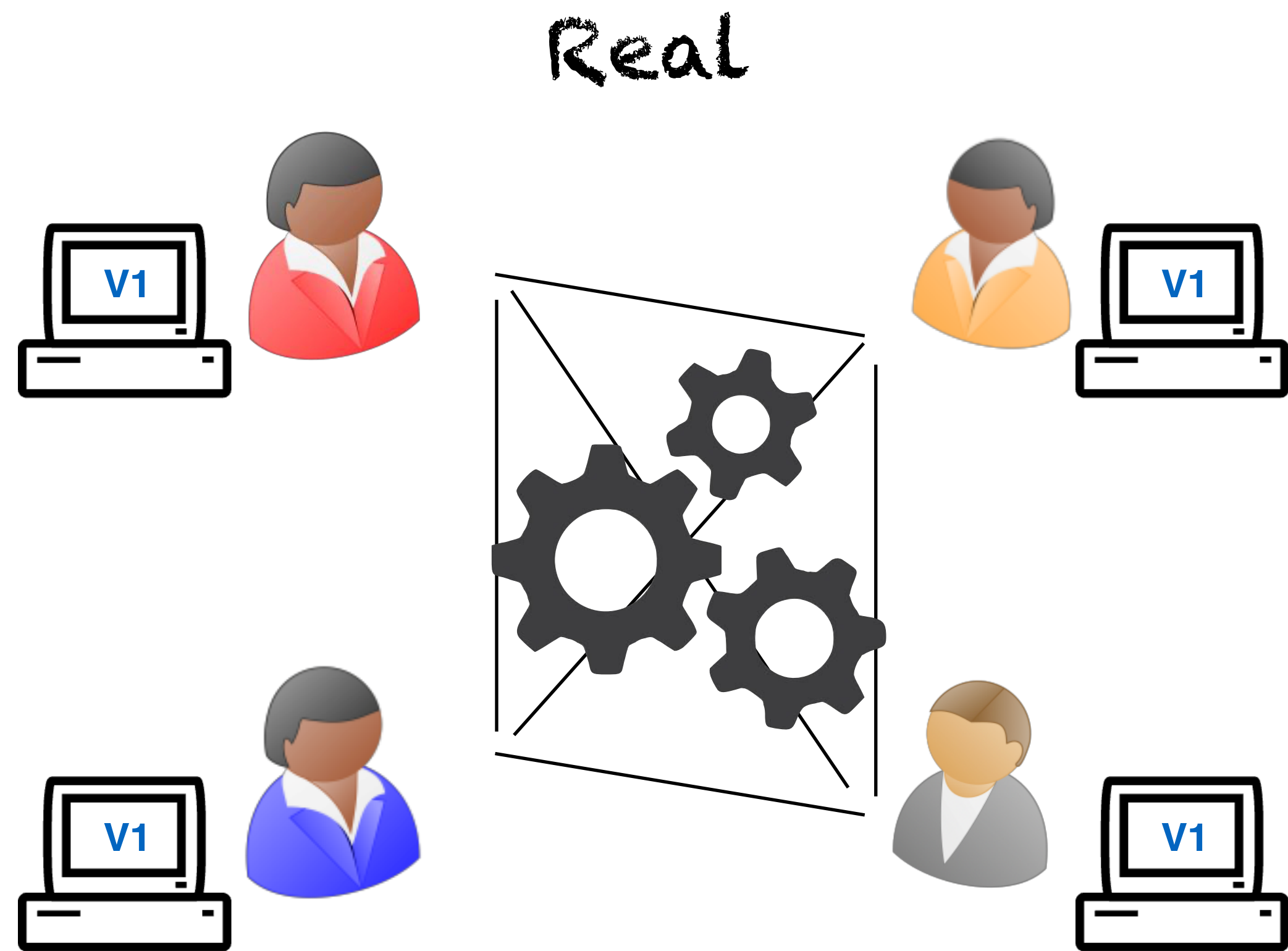


Ideal



- Recover from broken protocols
- Add additional features

# Cryptographic agility

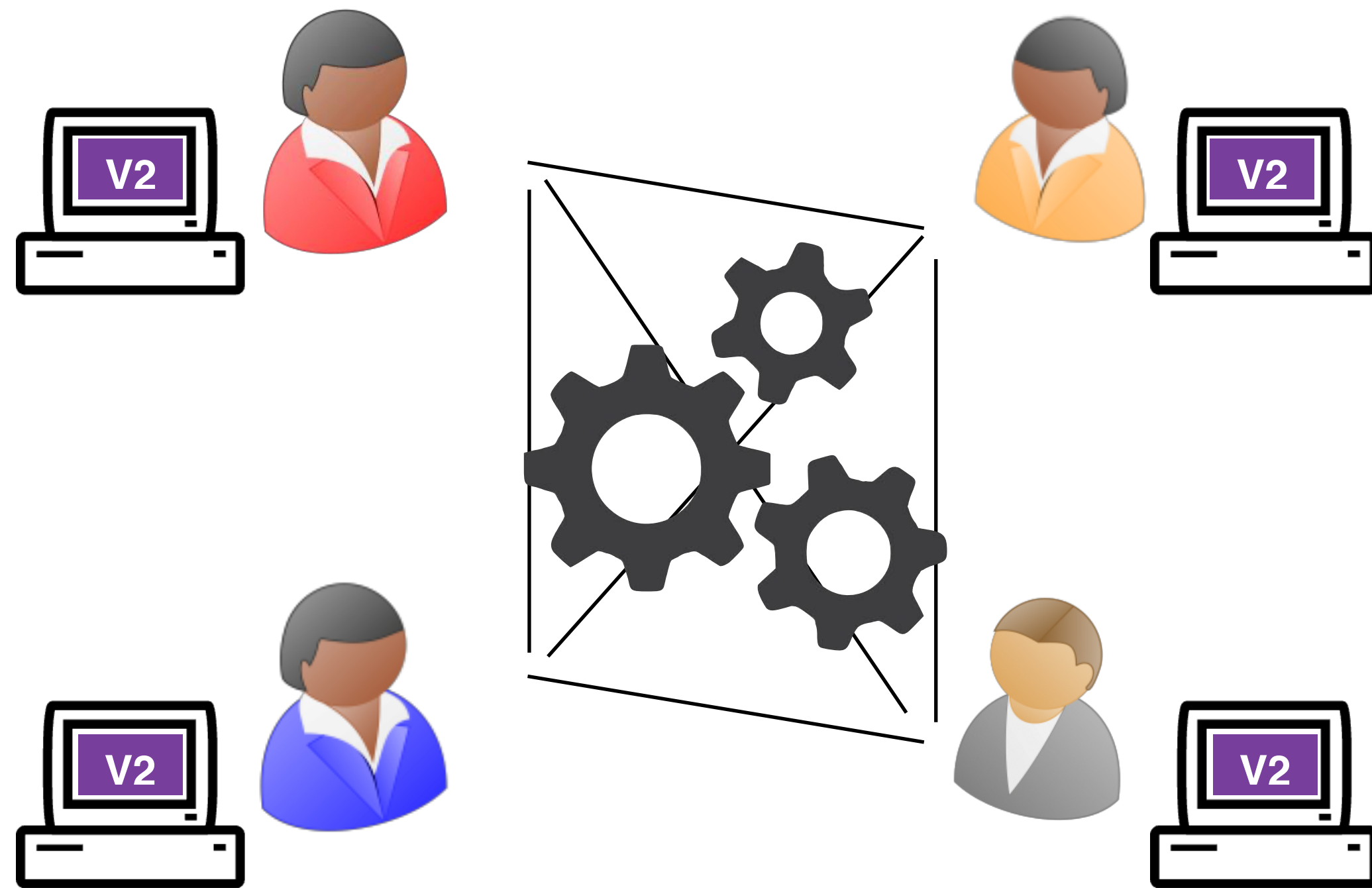


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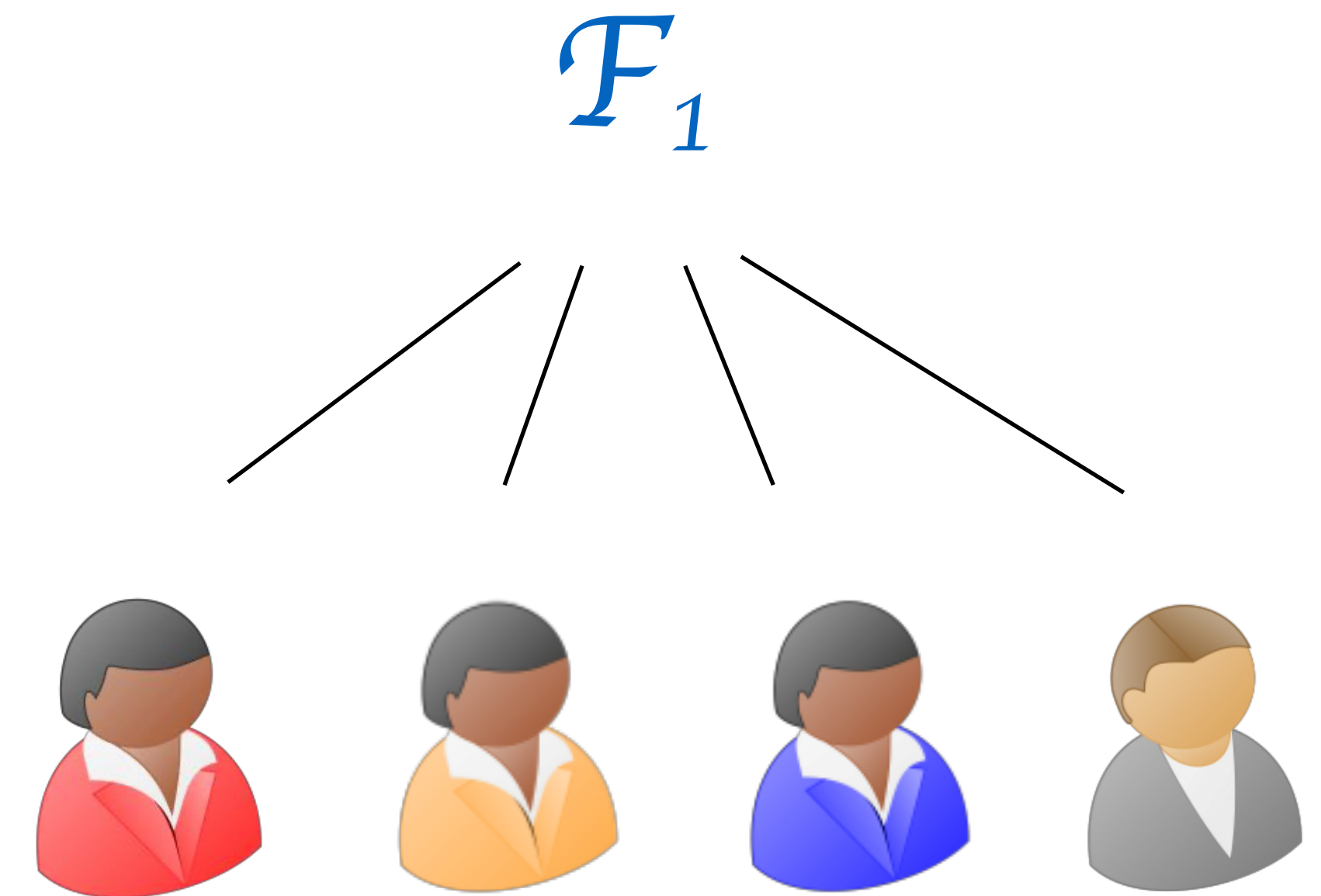


# Cryptographic agility

Real



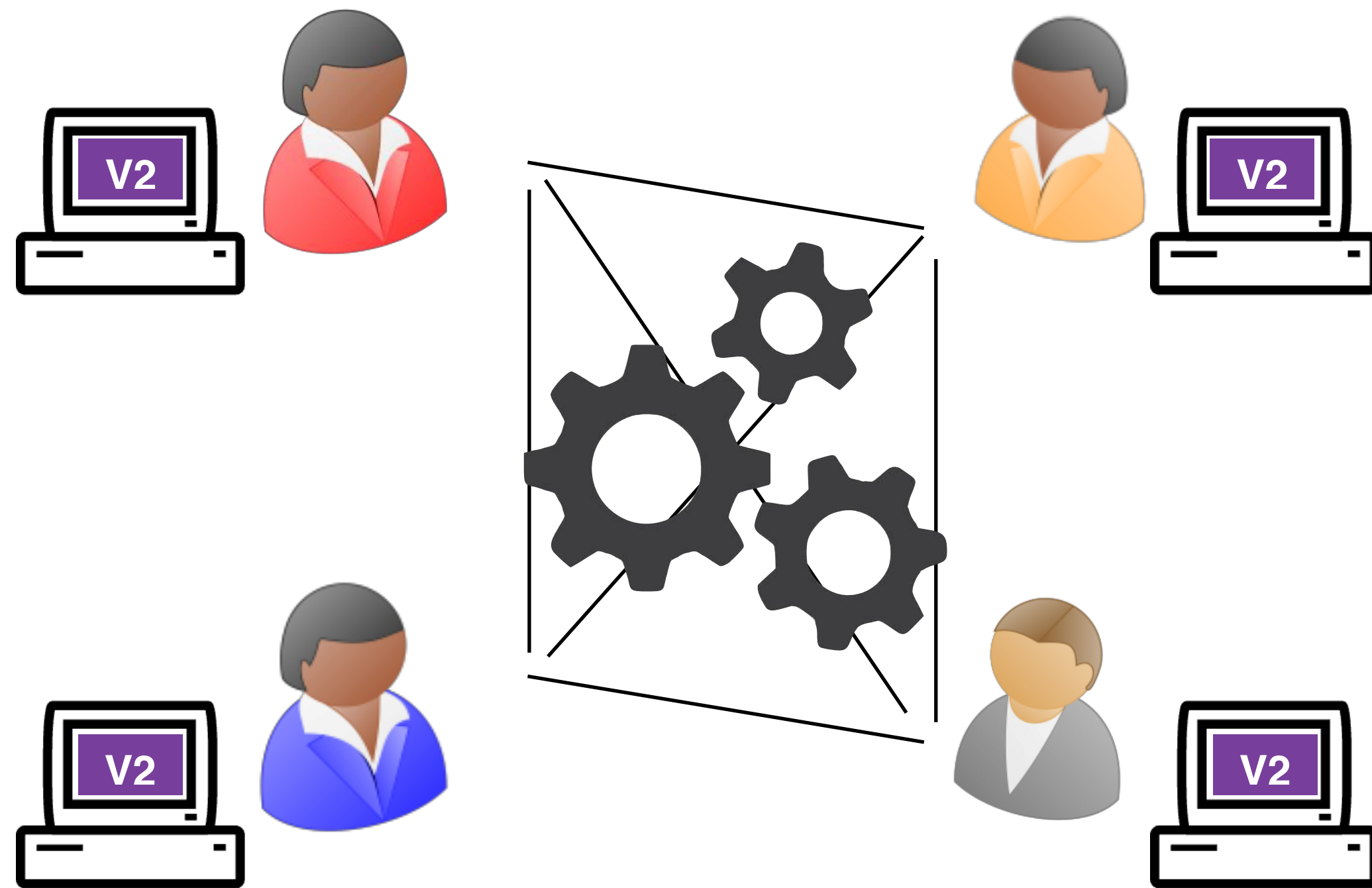
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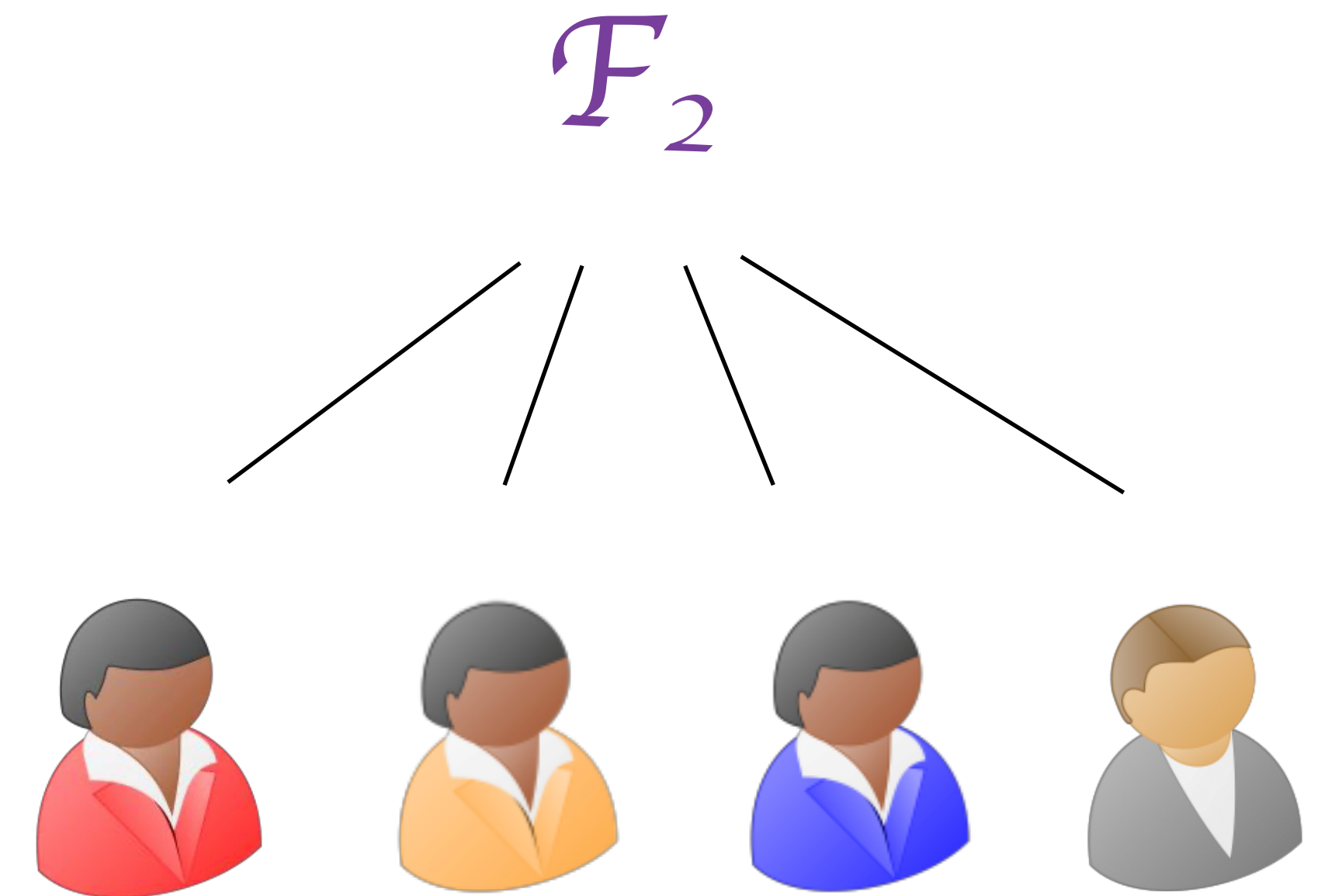
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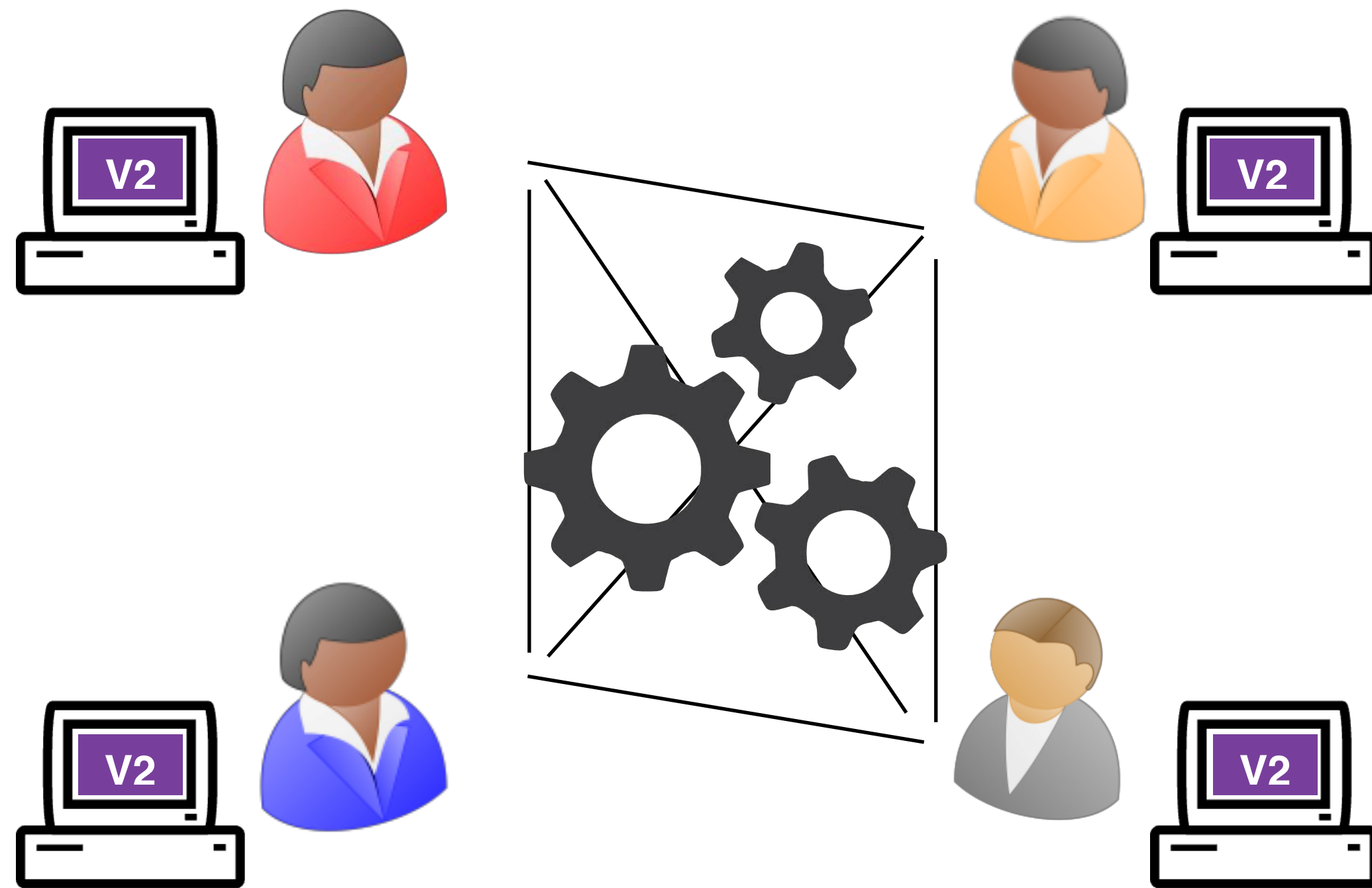
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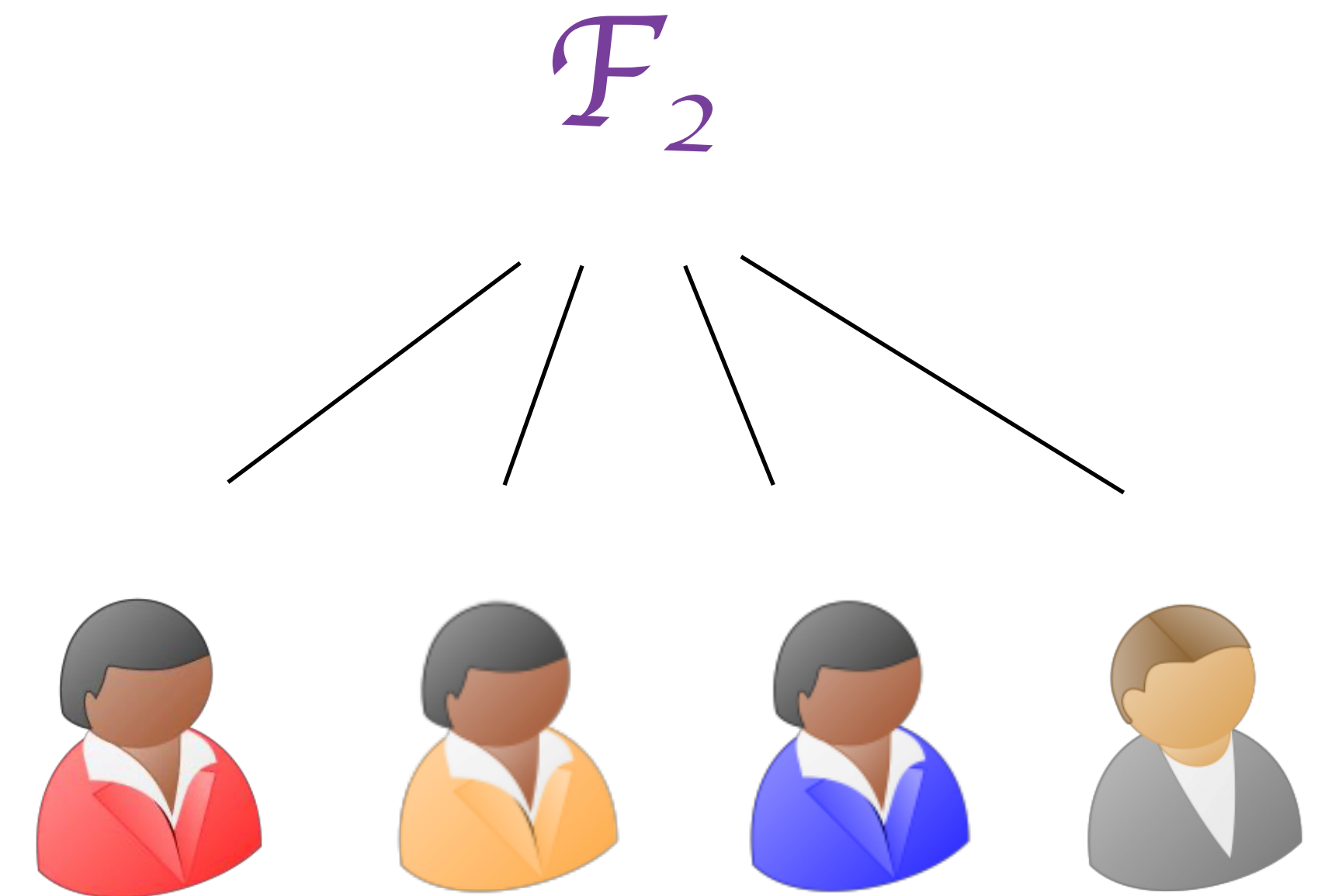
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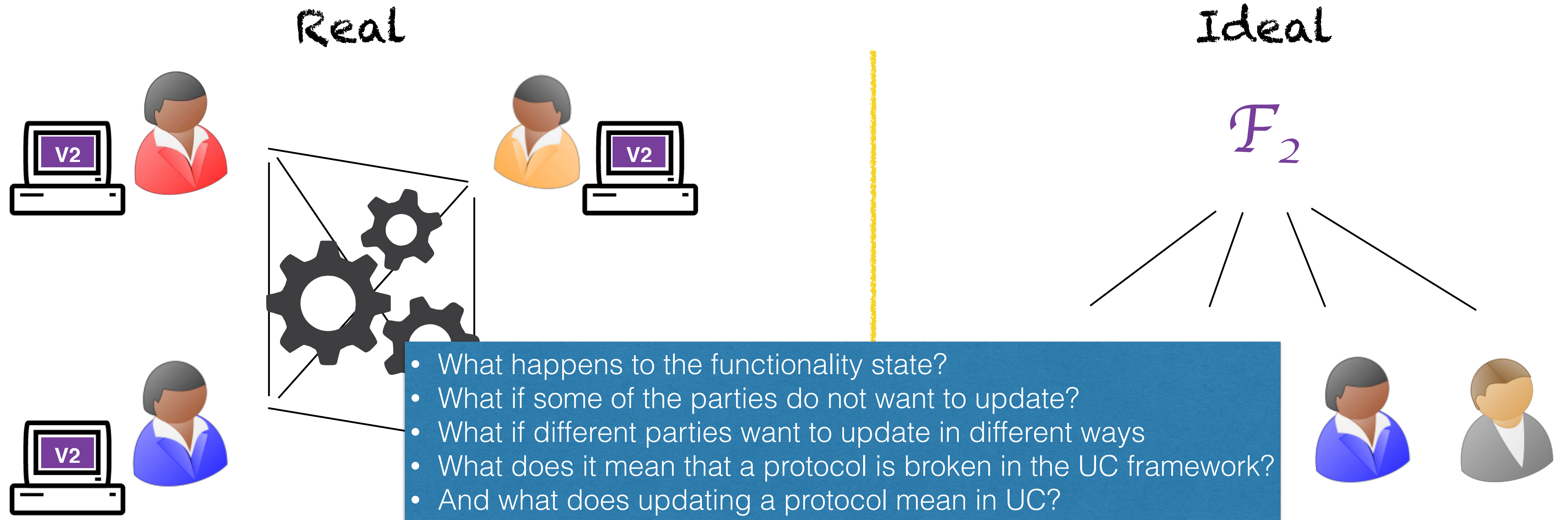
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Just corresponds to parties registering to a different functionality, right?

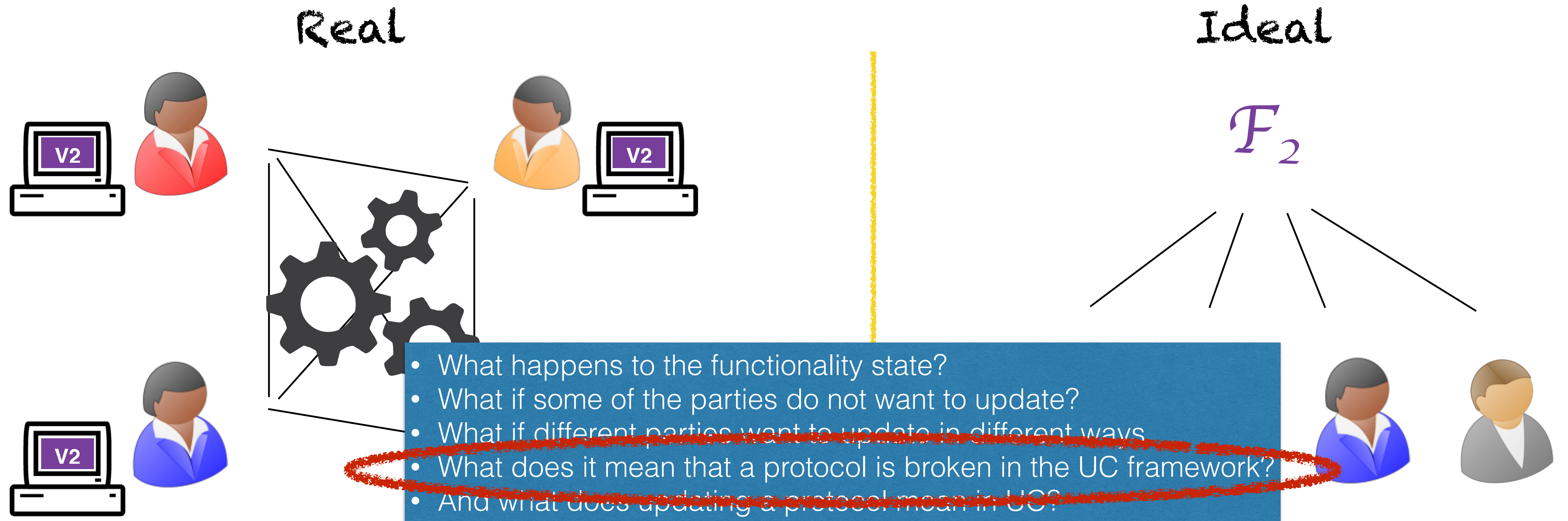
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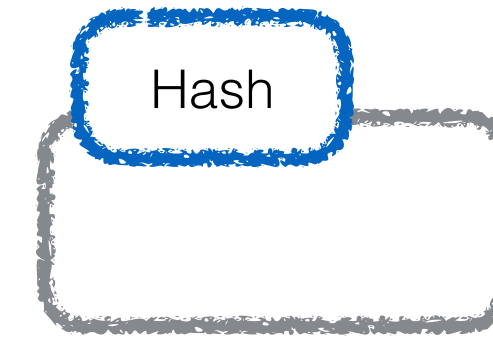
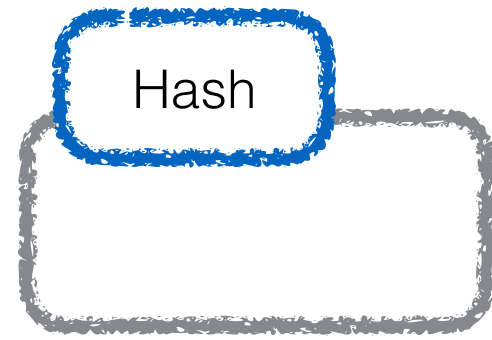
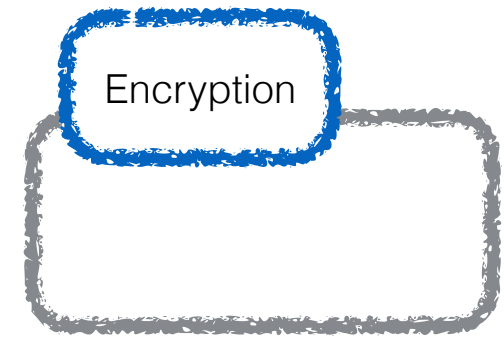
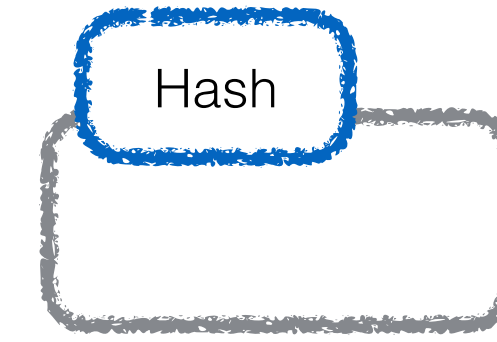
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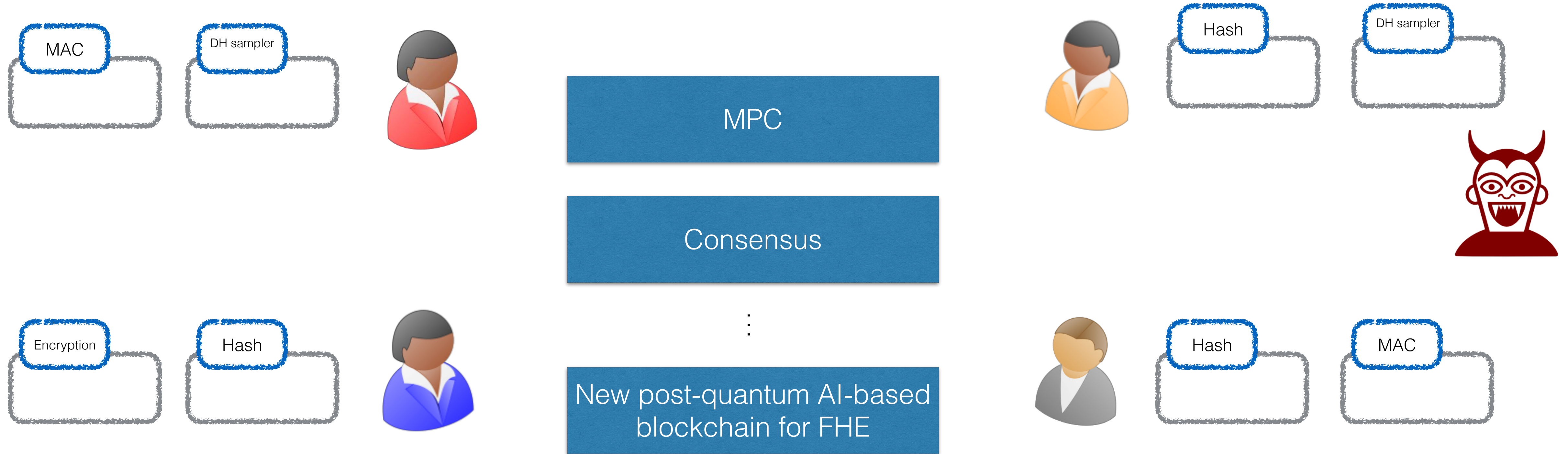
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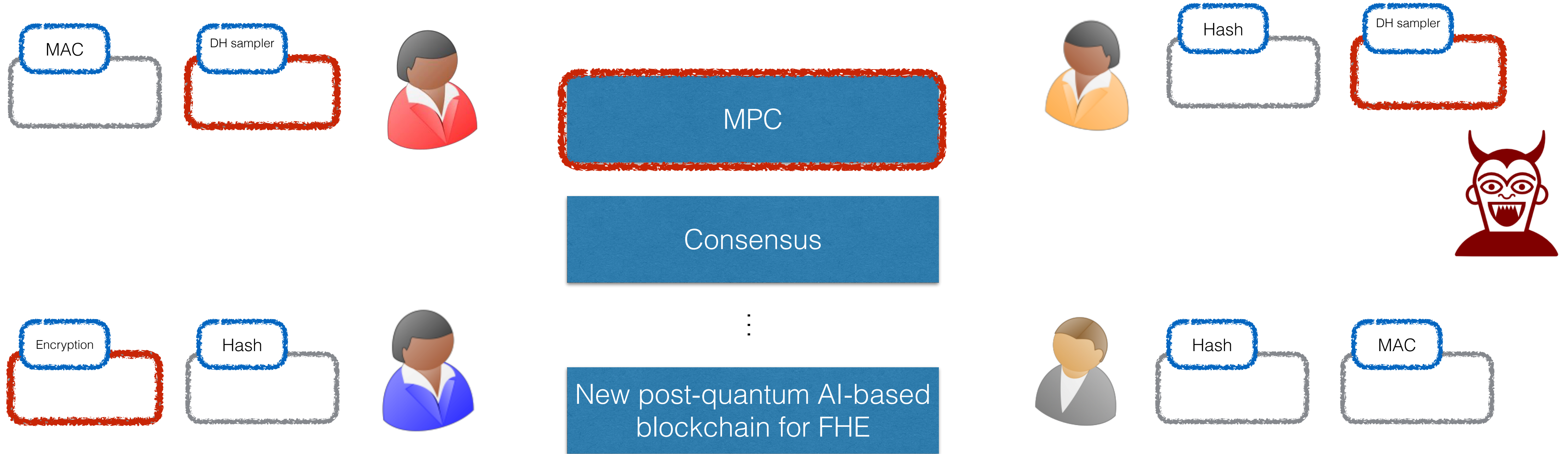
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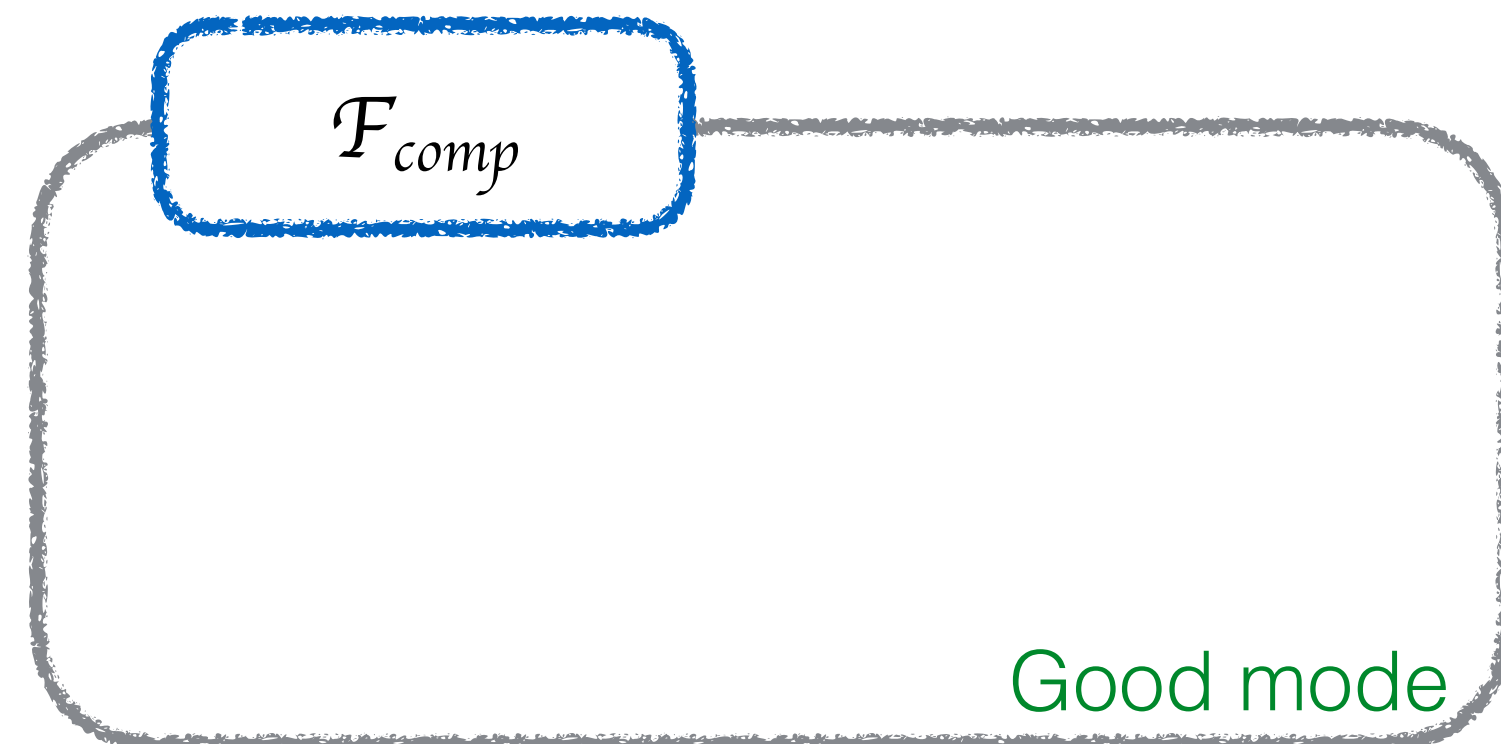
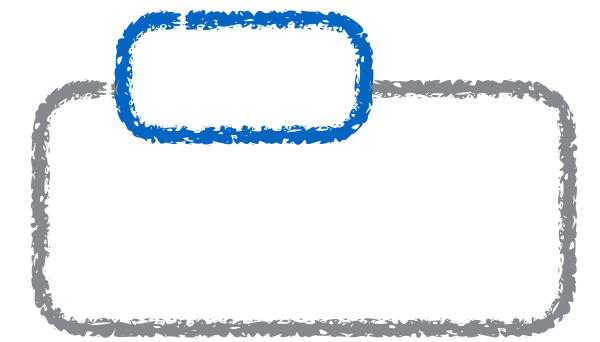
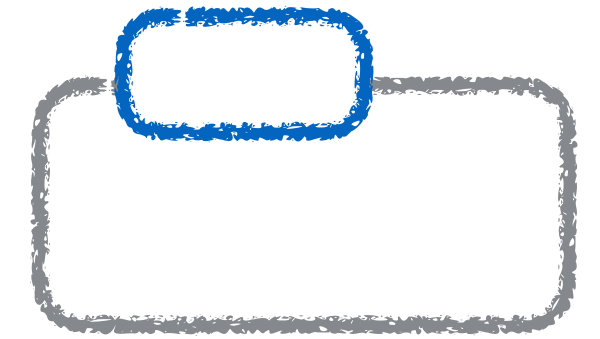
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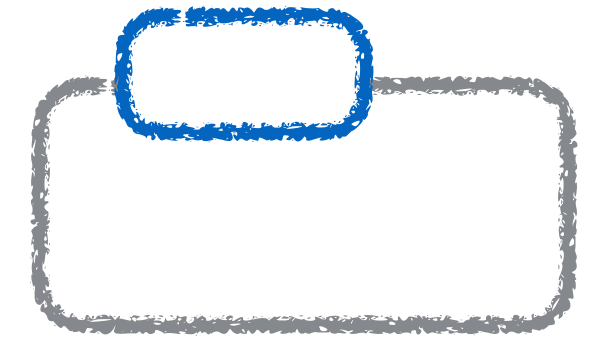
# Modelling broken things

Fist contribution



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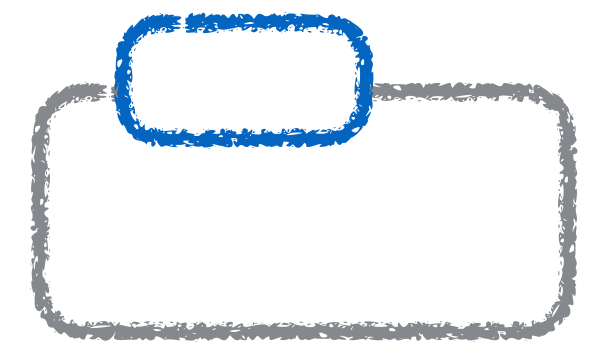
Fist contribution



(INIT, alg)



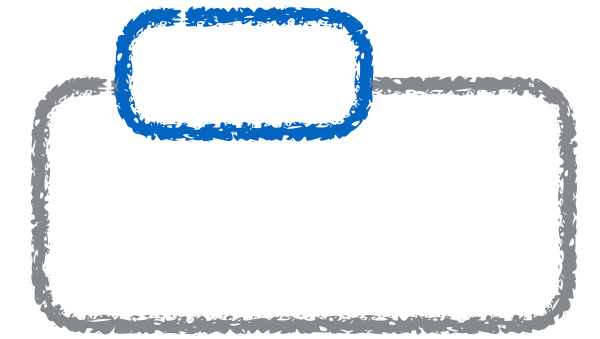
$\mathcal{F}_{comp}$



Good mode

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Fist contribution



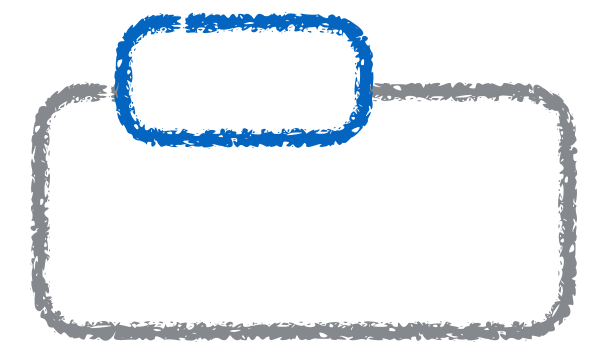
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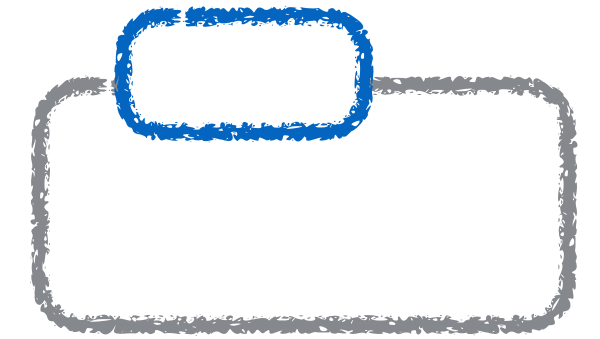
alg

Good mode



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Fist contribution



(QUERY,  $x_1$ )

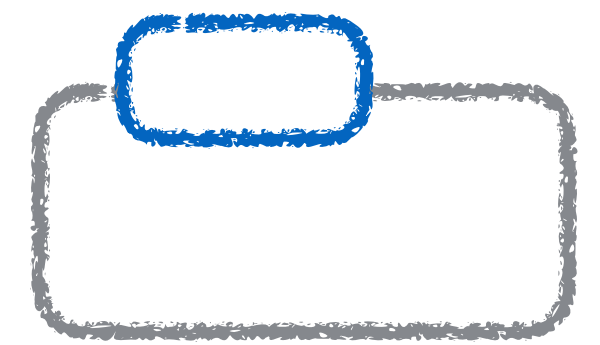


$\mathcal{F}_{comp}$

( $x_1, y_1$ )

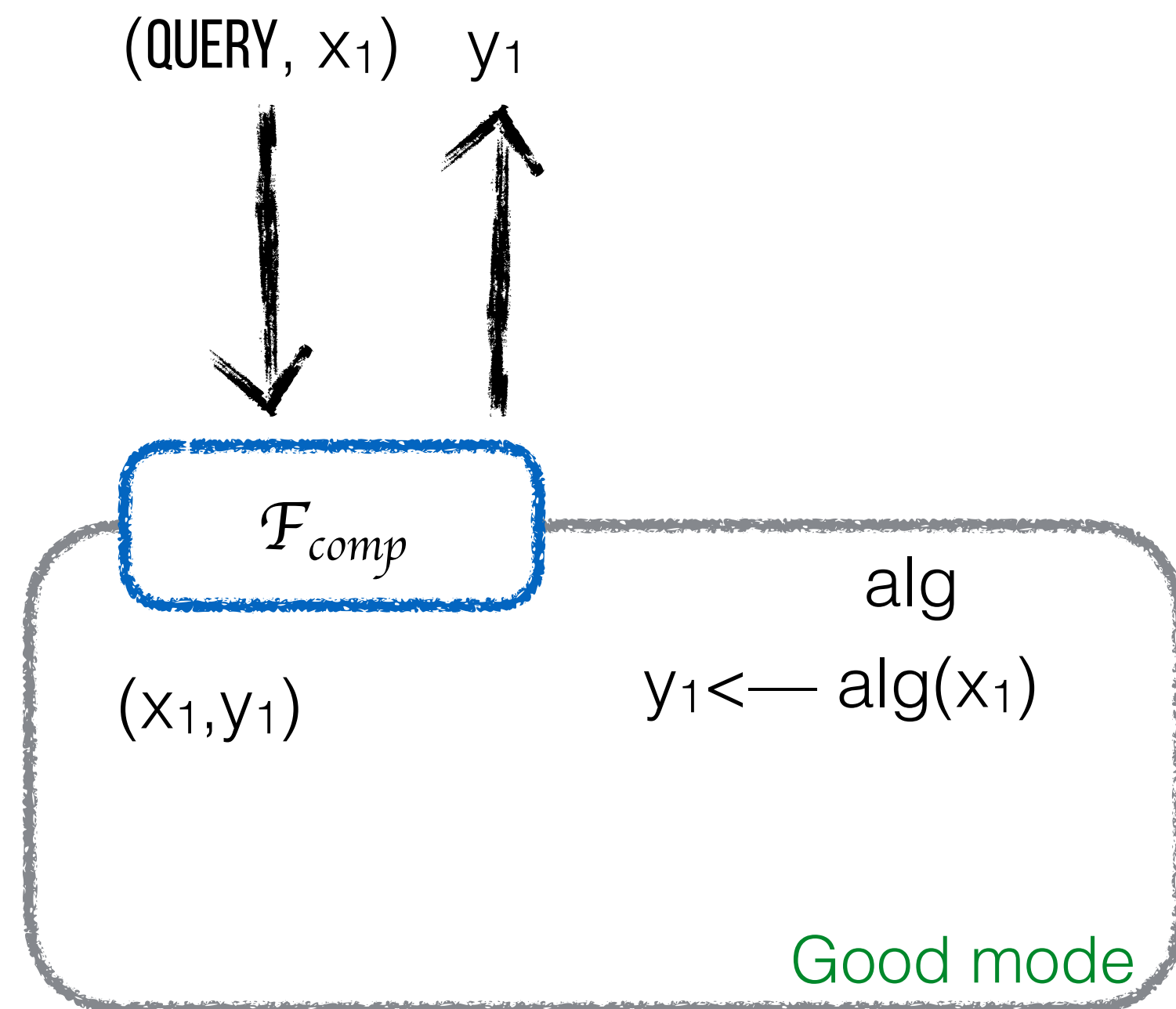
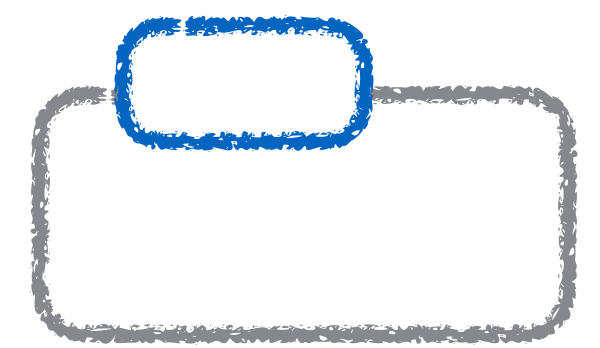
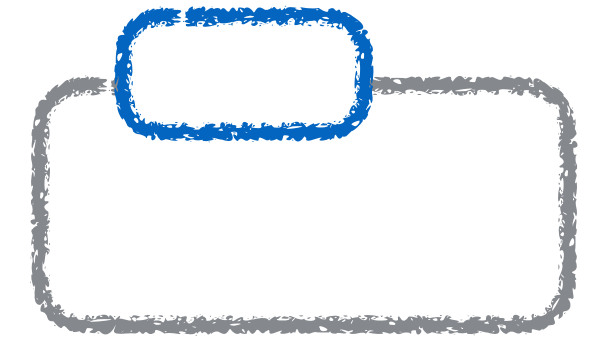
alg  
 $y_1 \leftarrow \text{alg}(x_1)$

Good mode



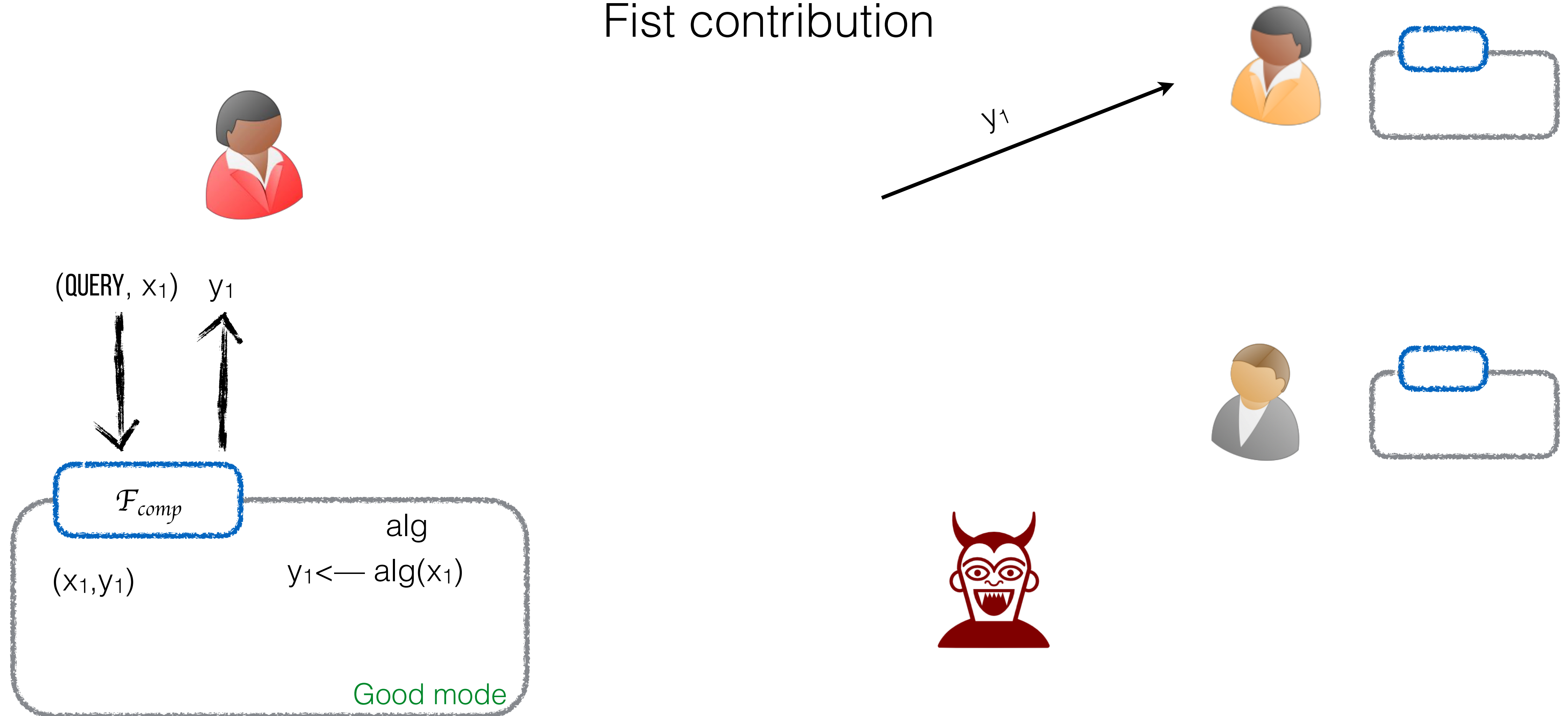
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Fist contribution



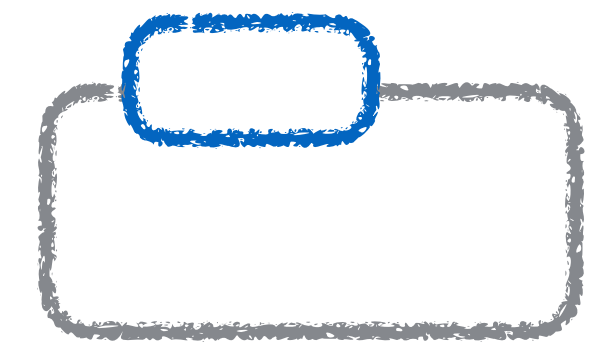
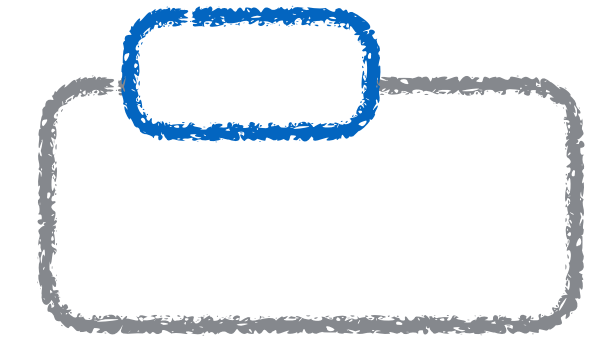
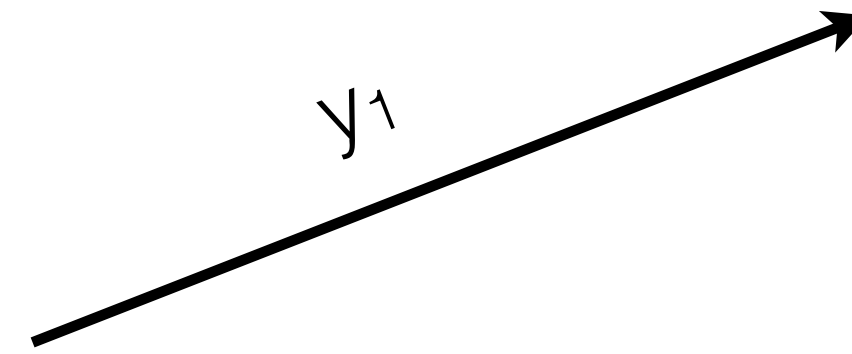
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Fist contribution



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$\mathcal{F}_{comp}$

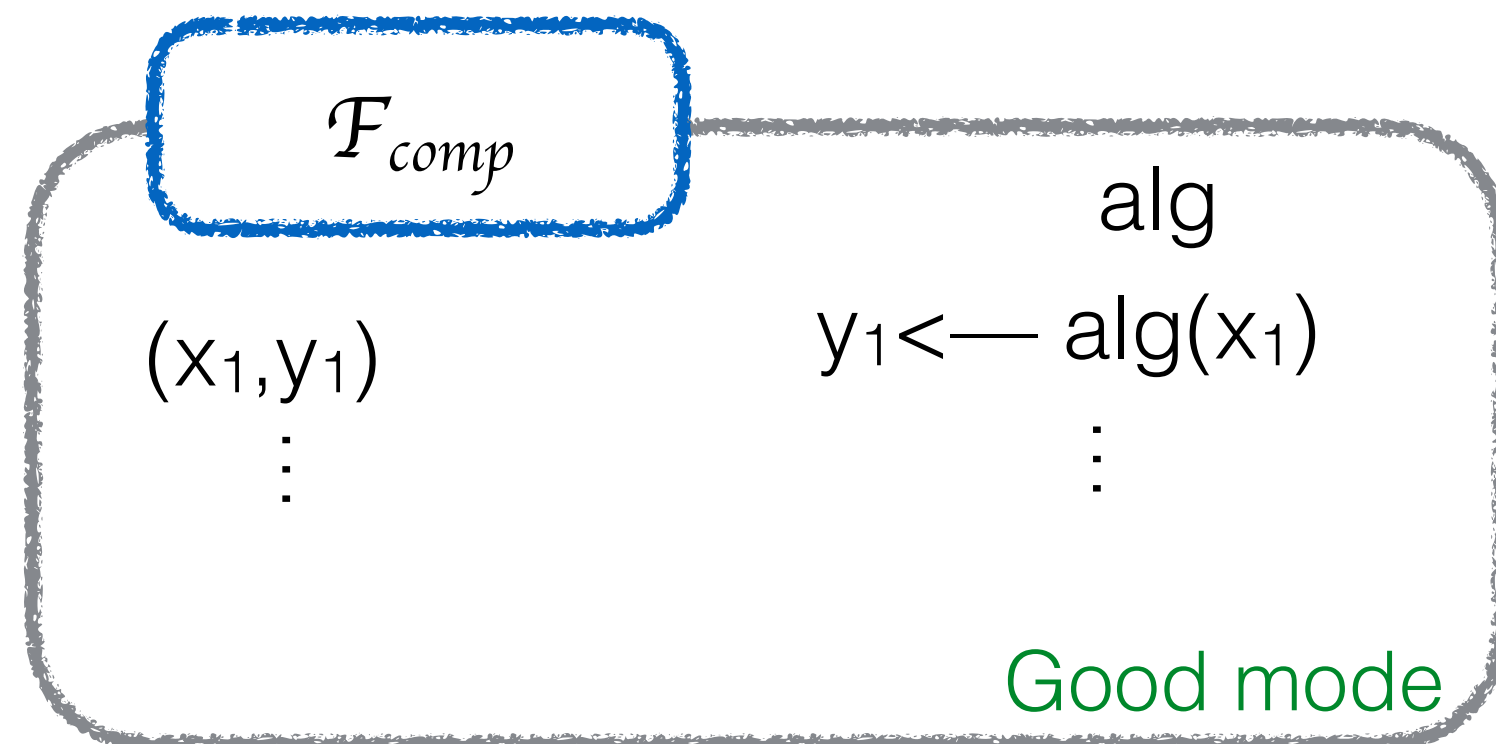
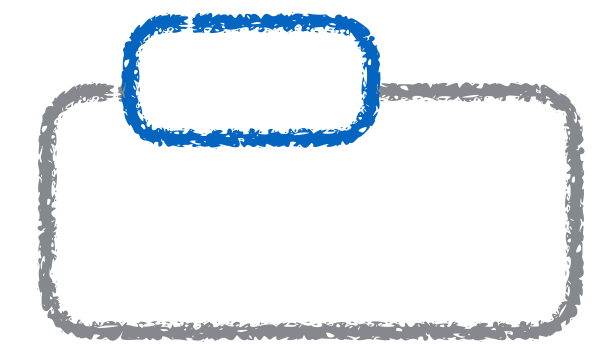
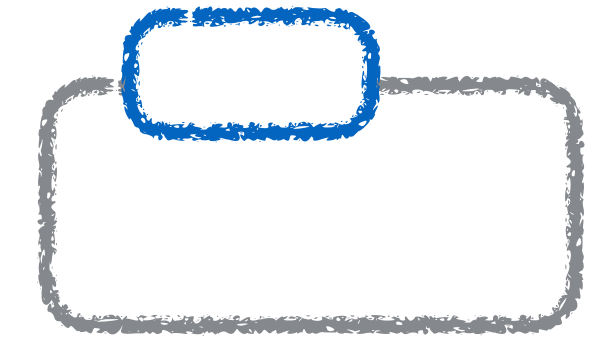
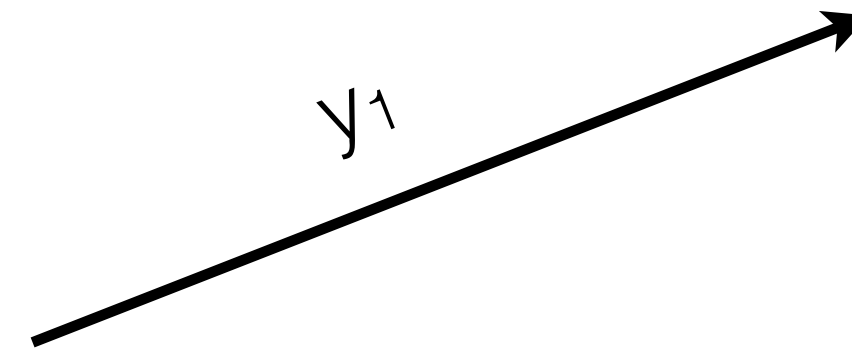
$(x_1, y_1)$

alg  
 $y_1 \leftarrow \text{alg}(x_1)$

Good mode

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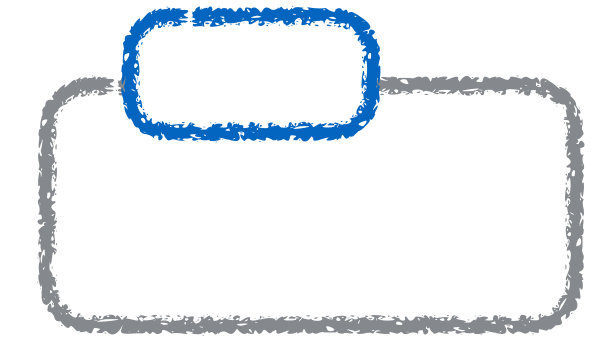
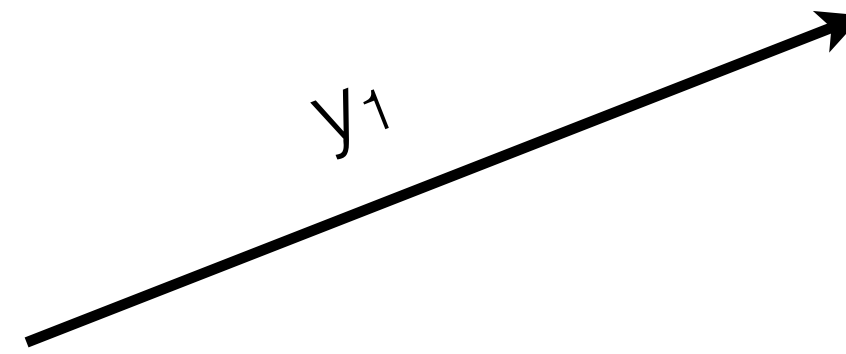
Fist contribution





# Modelling broken things

Fist contribution



(QUERY,  $x_k$ )

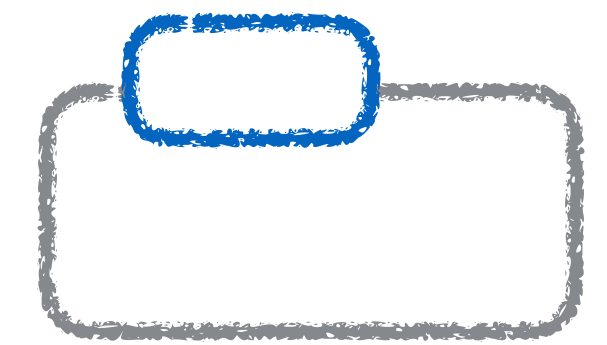


$\mathcal{F}_{comp}$

$(x_1, y_1)$   
 $\vdots$   
 $(x_k, y_k)$

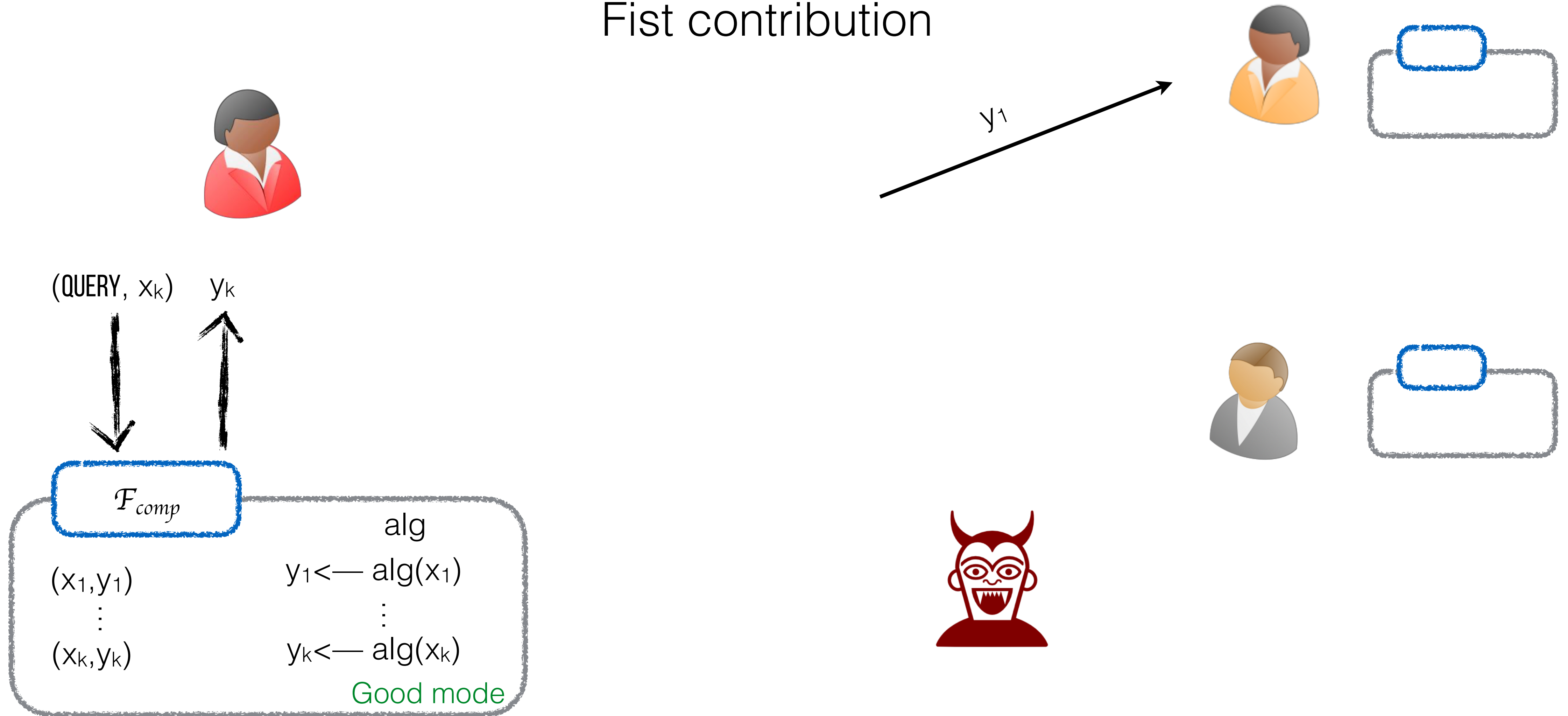
alg  
 $y_1 \leftarrow \text{alg}(x_1)$   
 $\vdots$   
 $y_k \leftarrow \text{alg}(x_k)$

Good mode



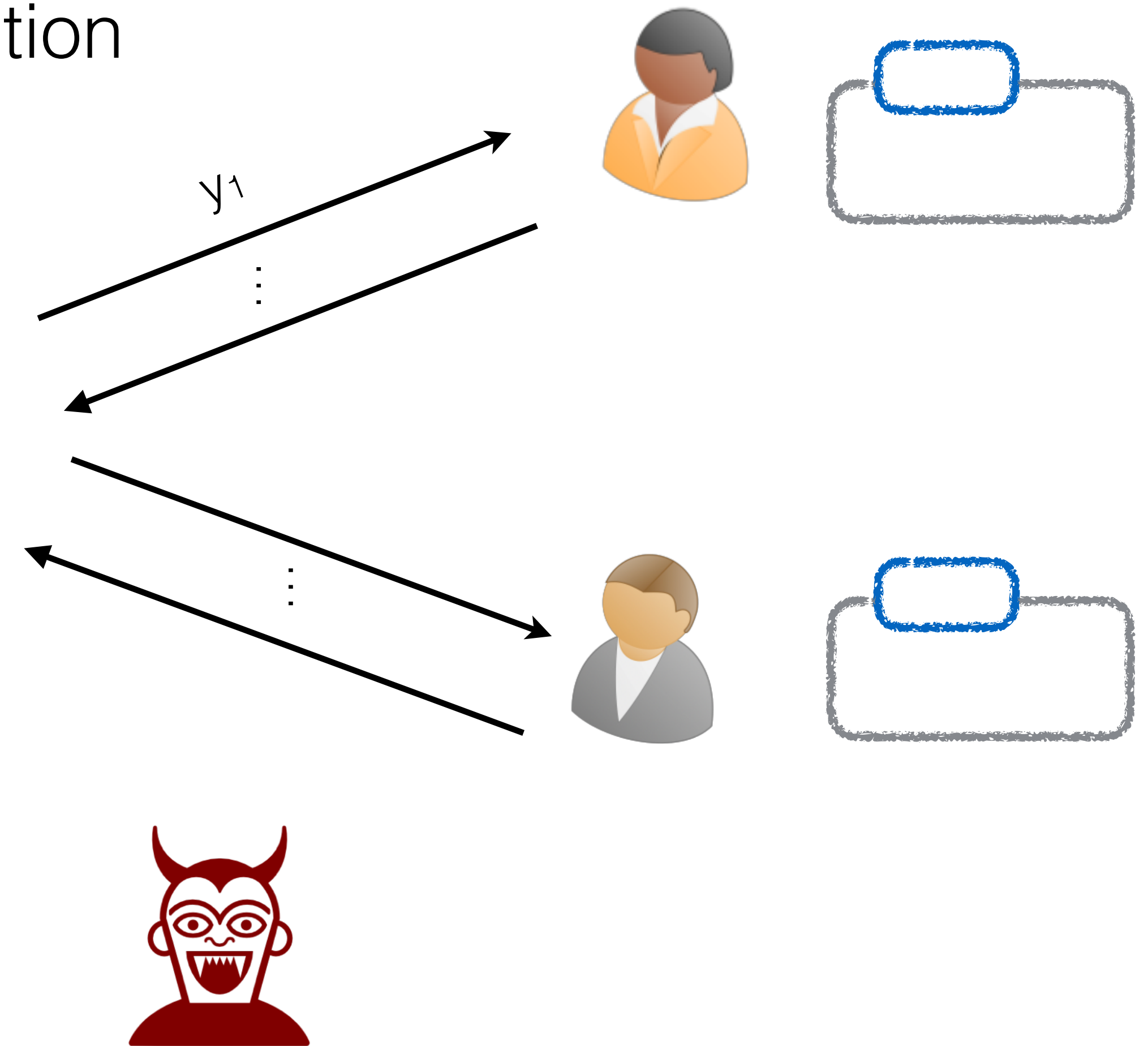
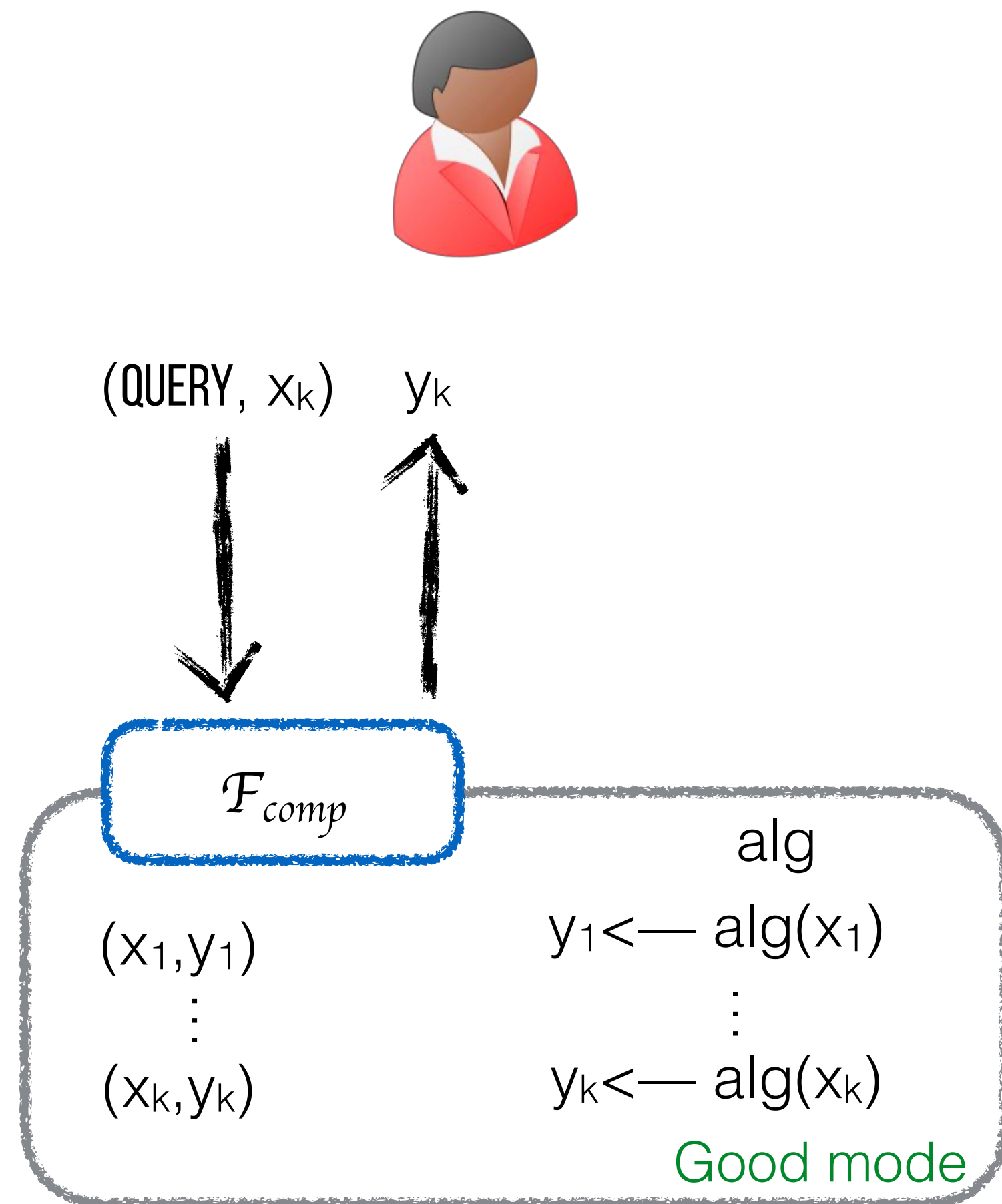
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Fist contribution



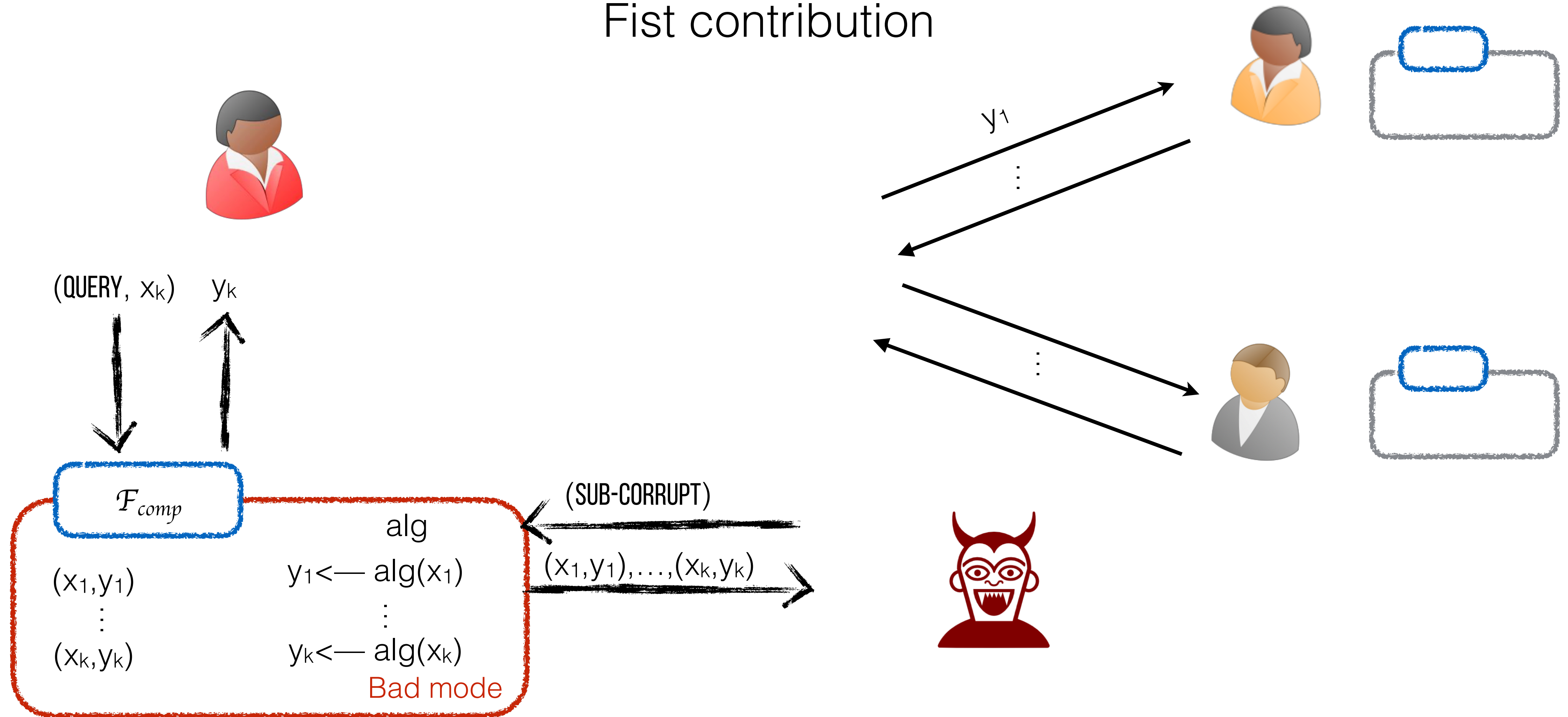
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Fist contribution



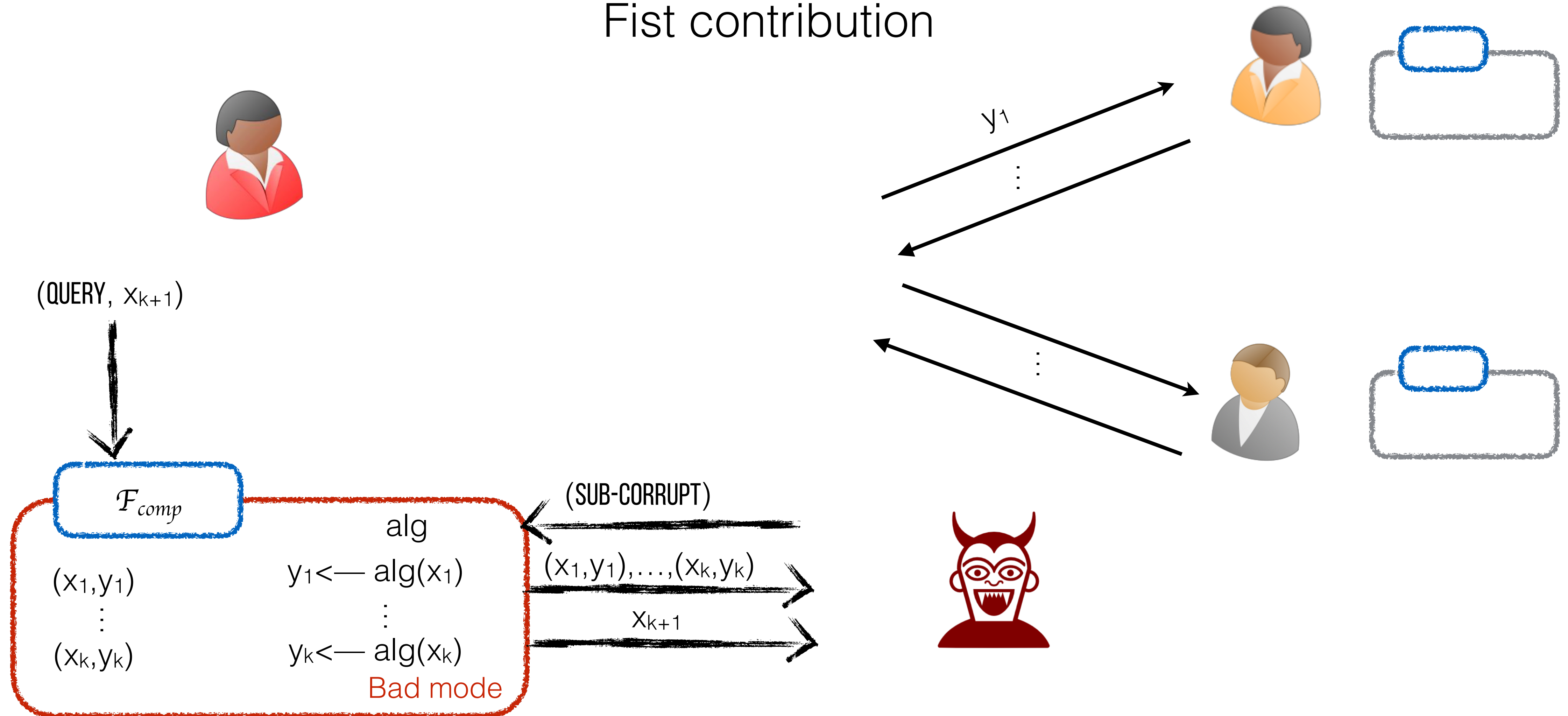
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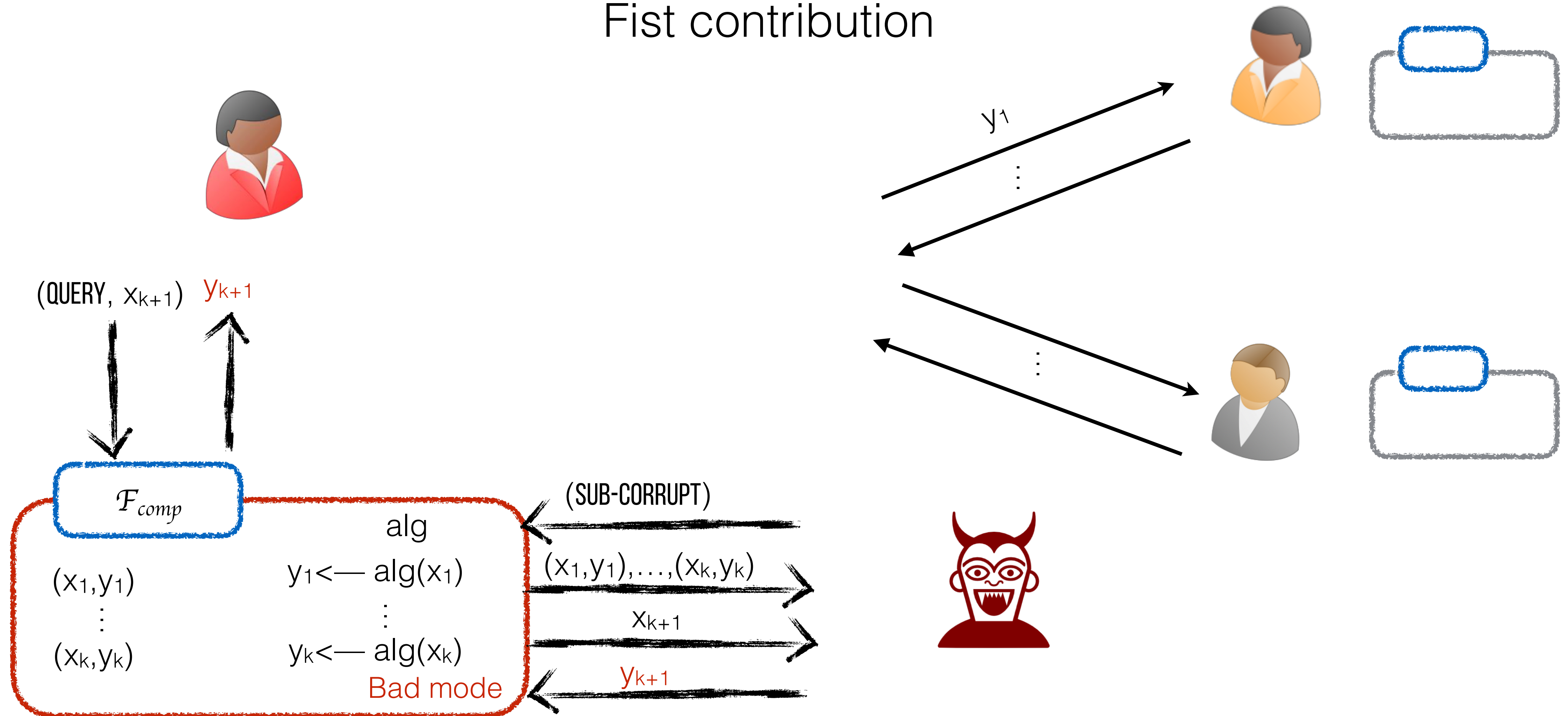
# Modelling broken things

Fist contribution



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# Modelling broken things

Assumptions



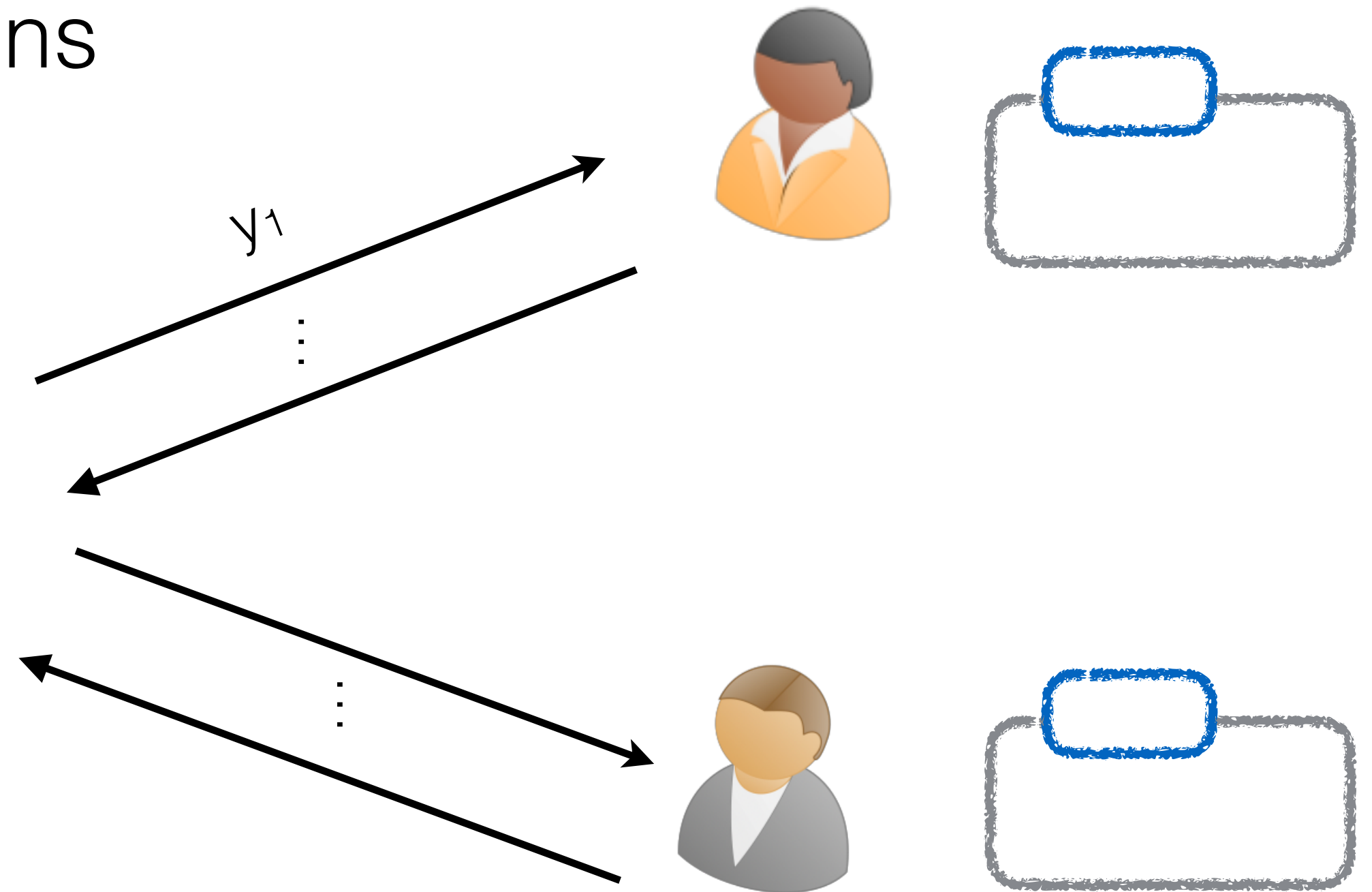
(INIT, DH\_sampler)



DH\_Sampler

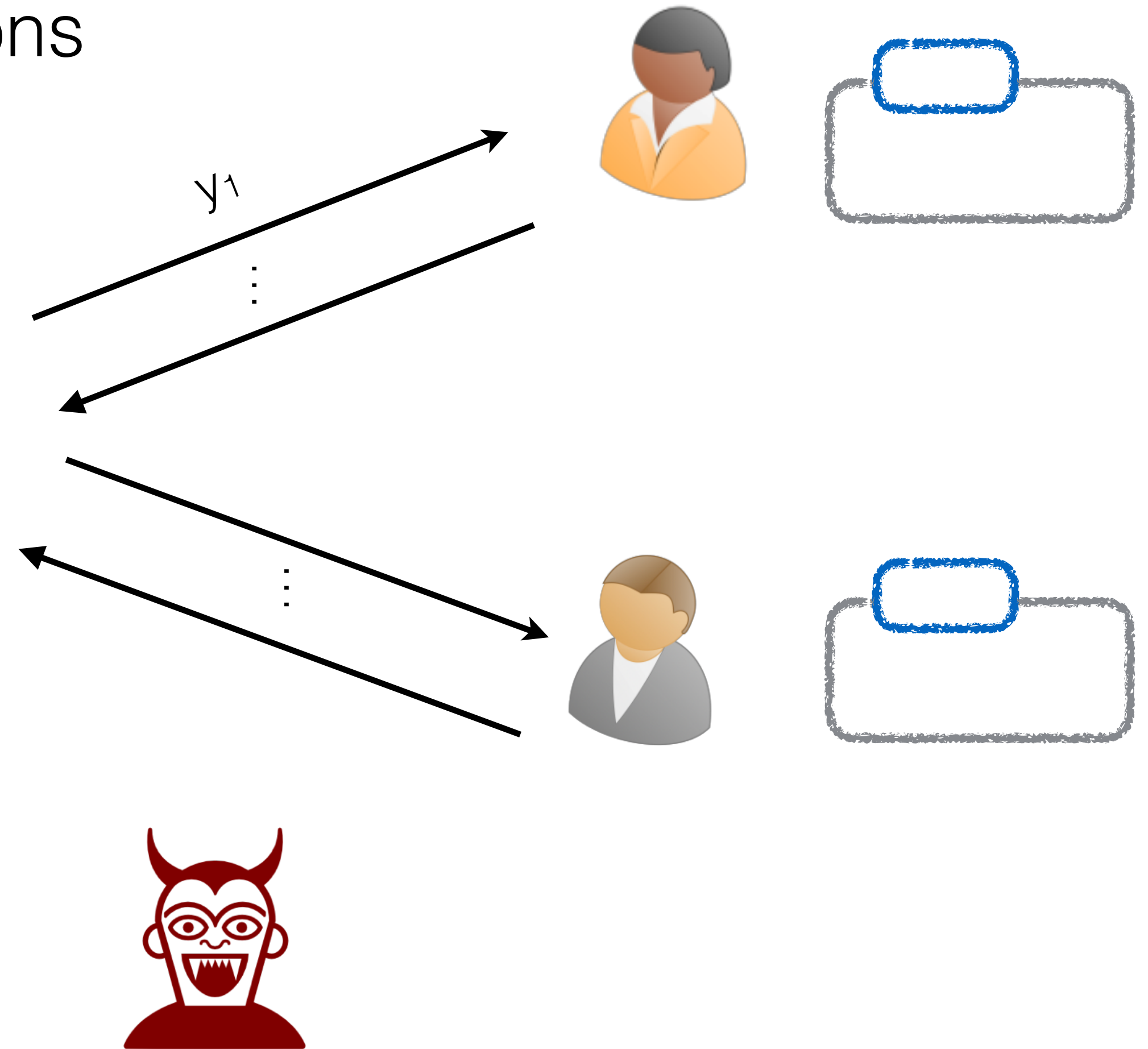
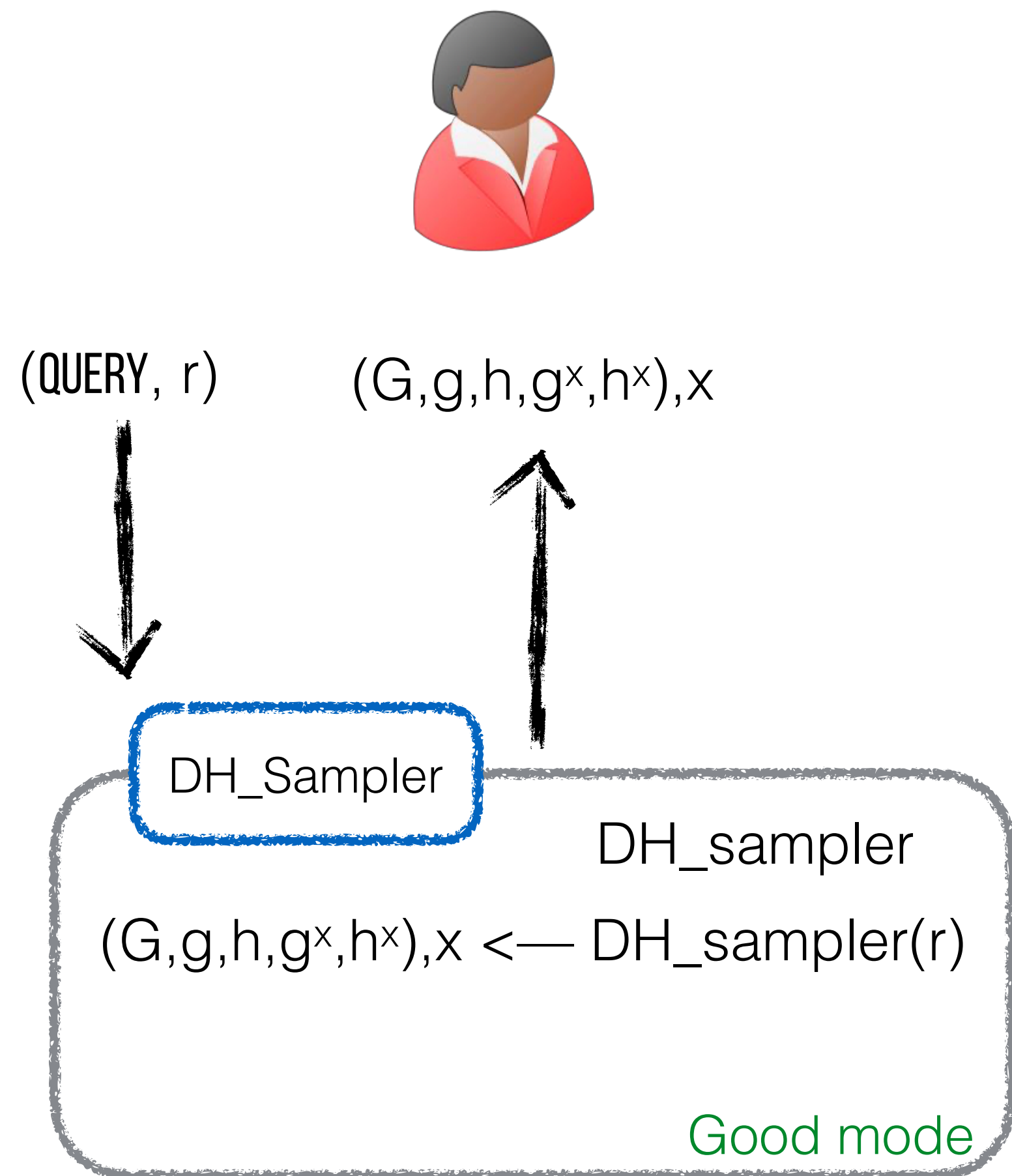
DH\_sampler

Good mode



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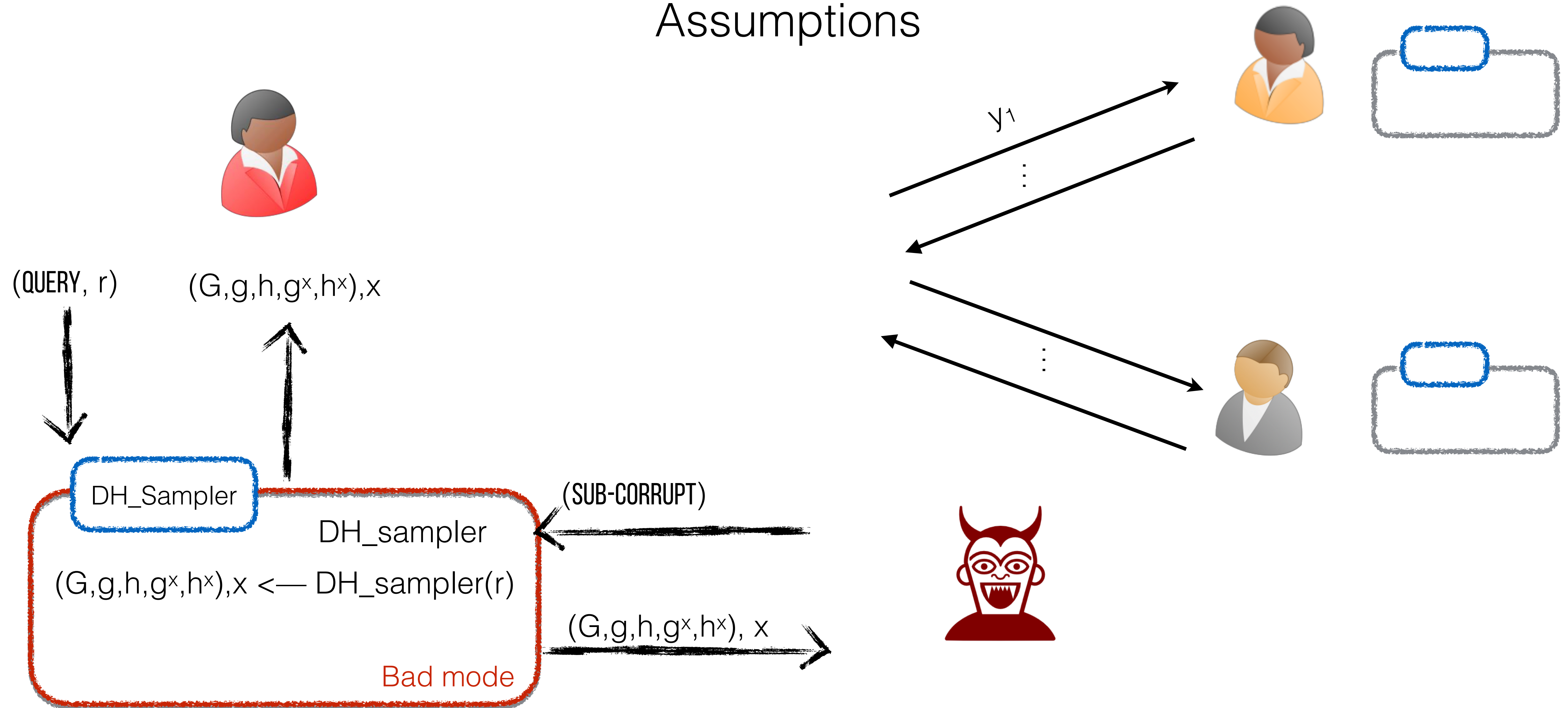
Assumptions



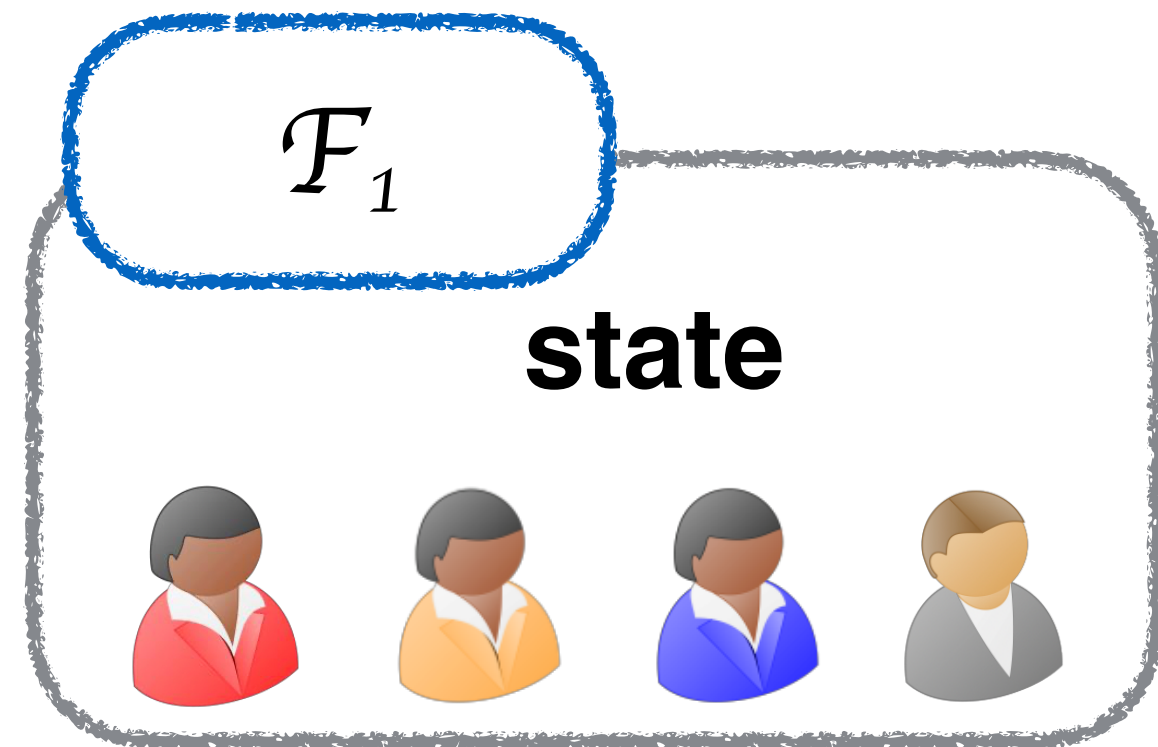


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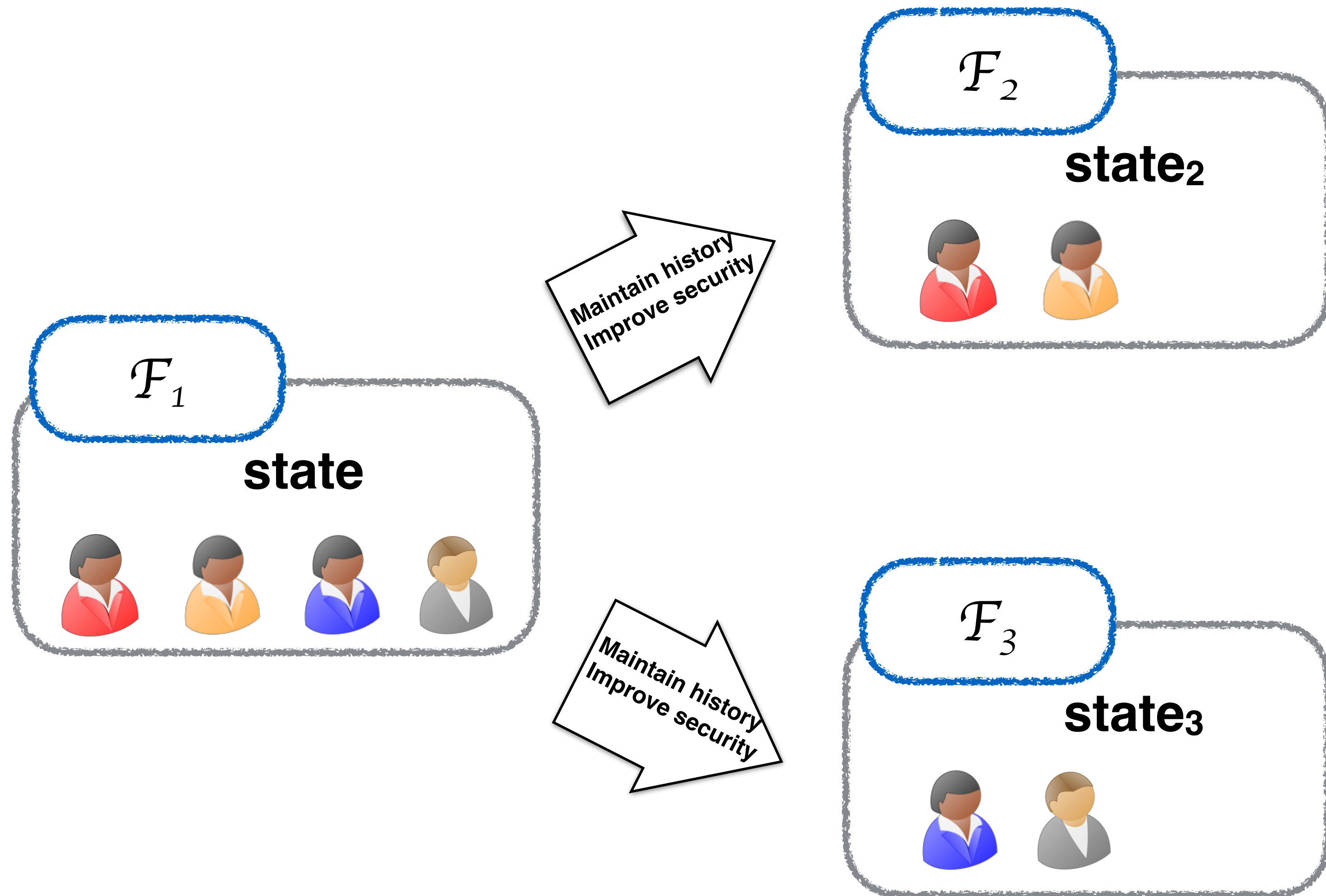
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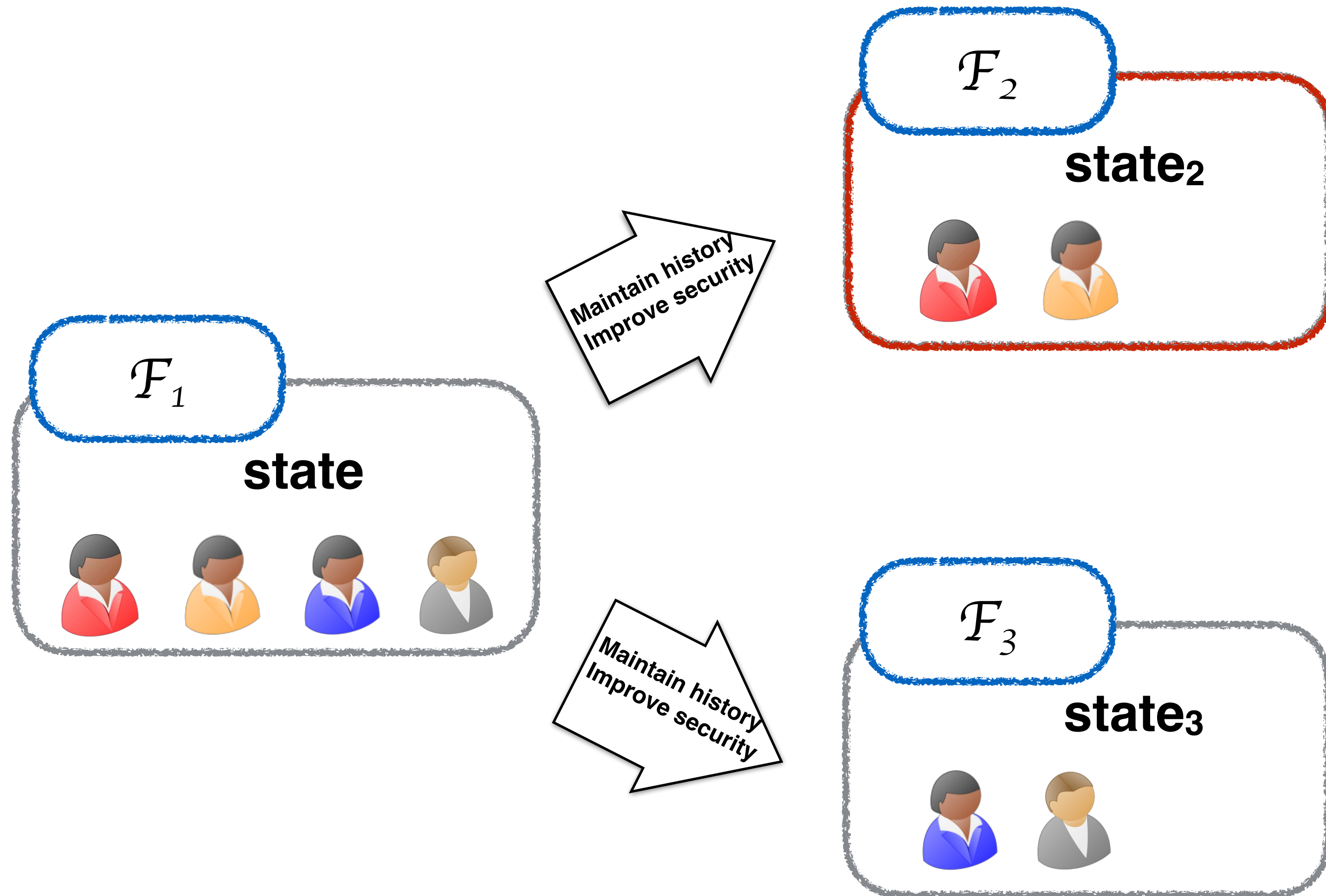
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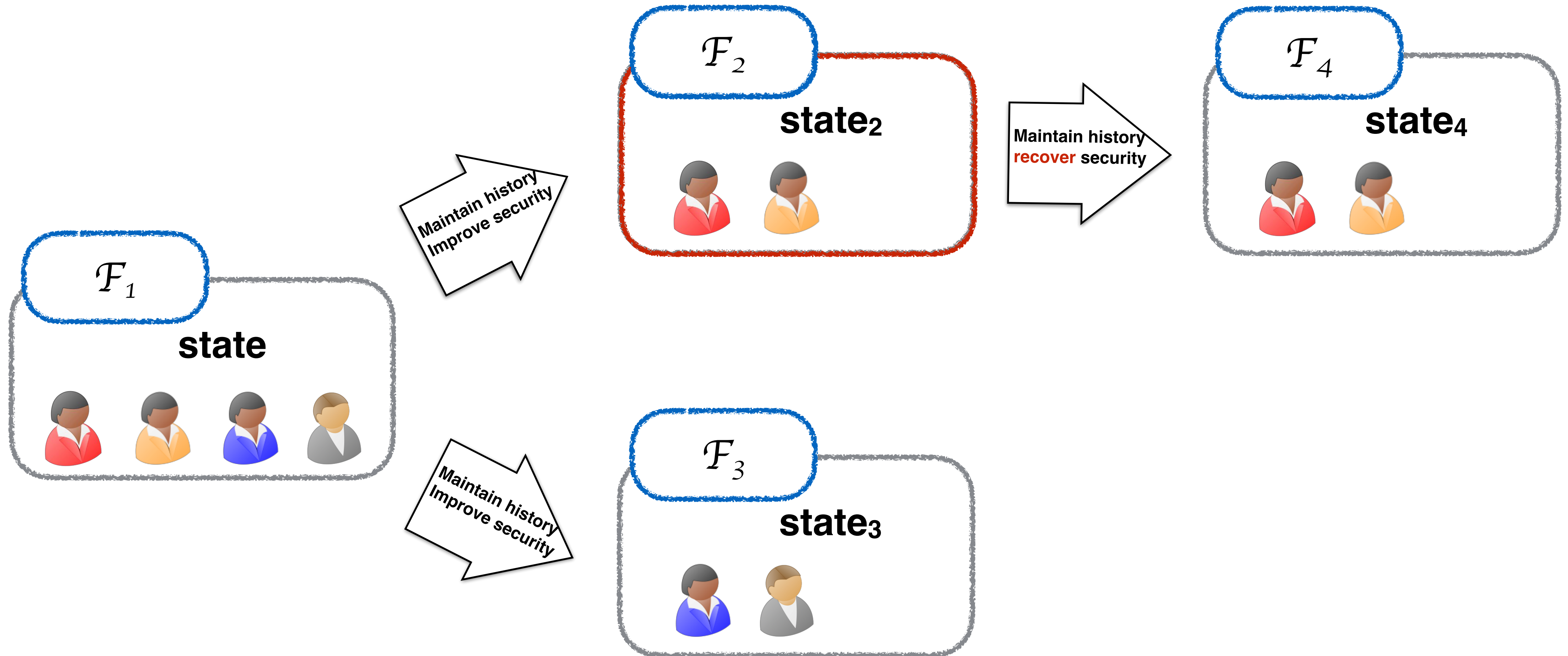
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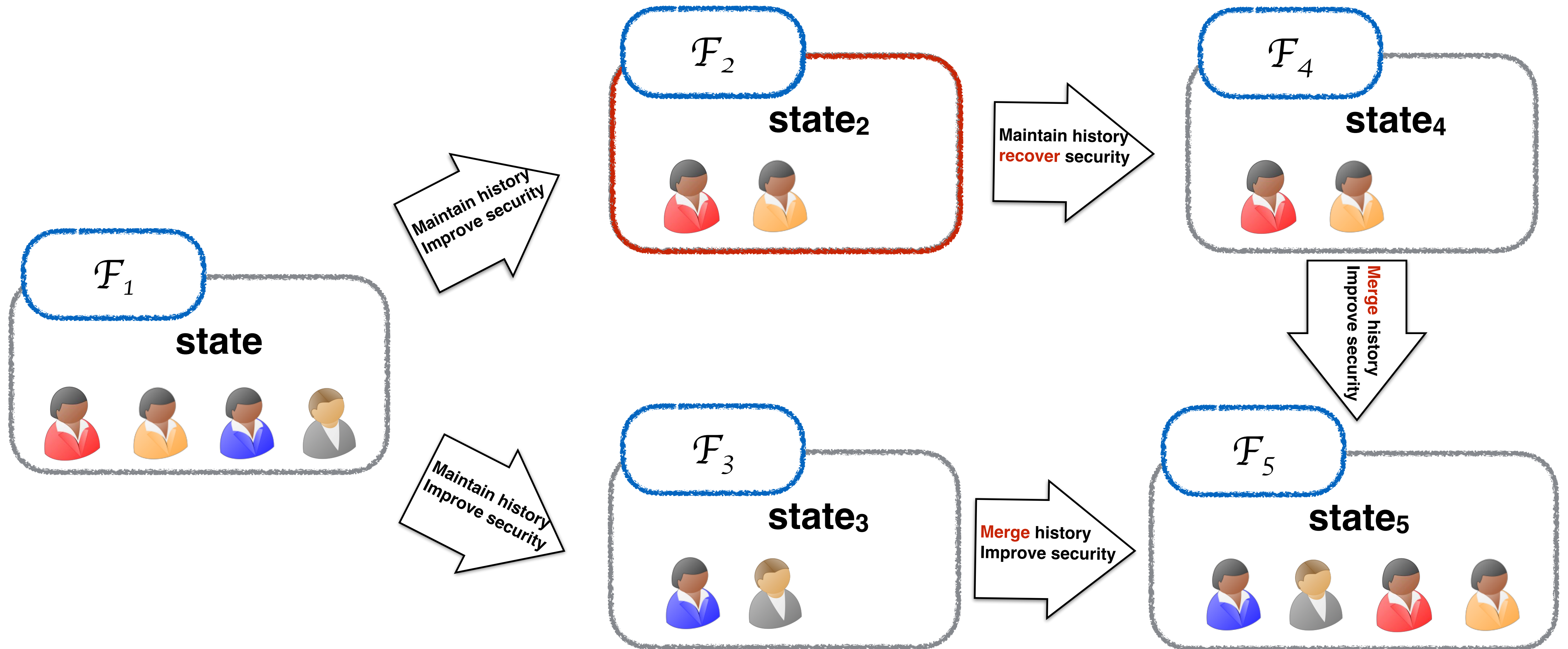
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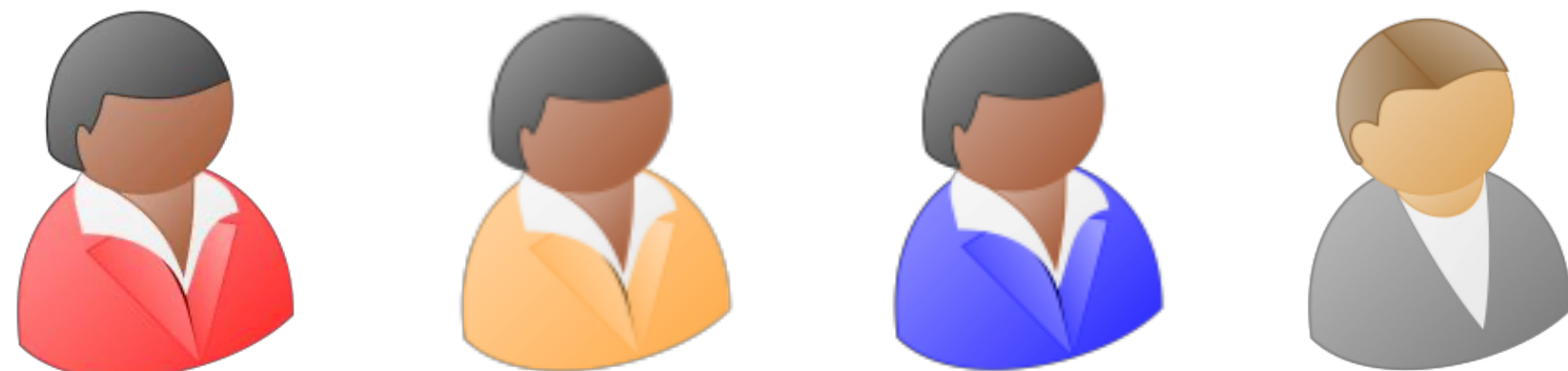
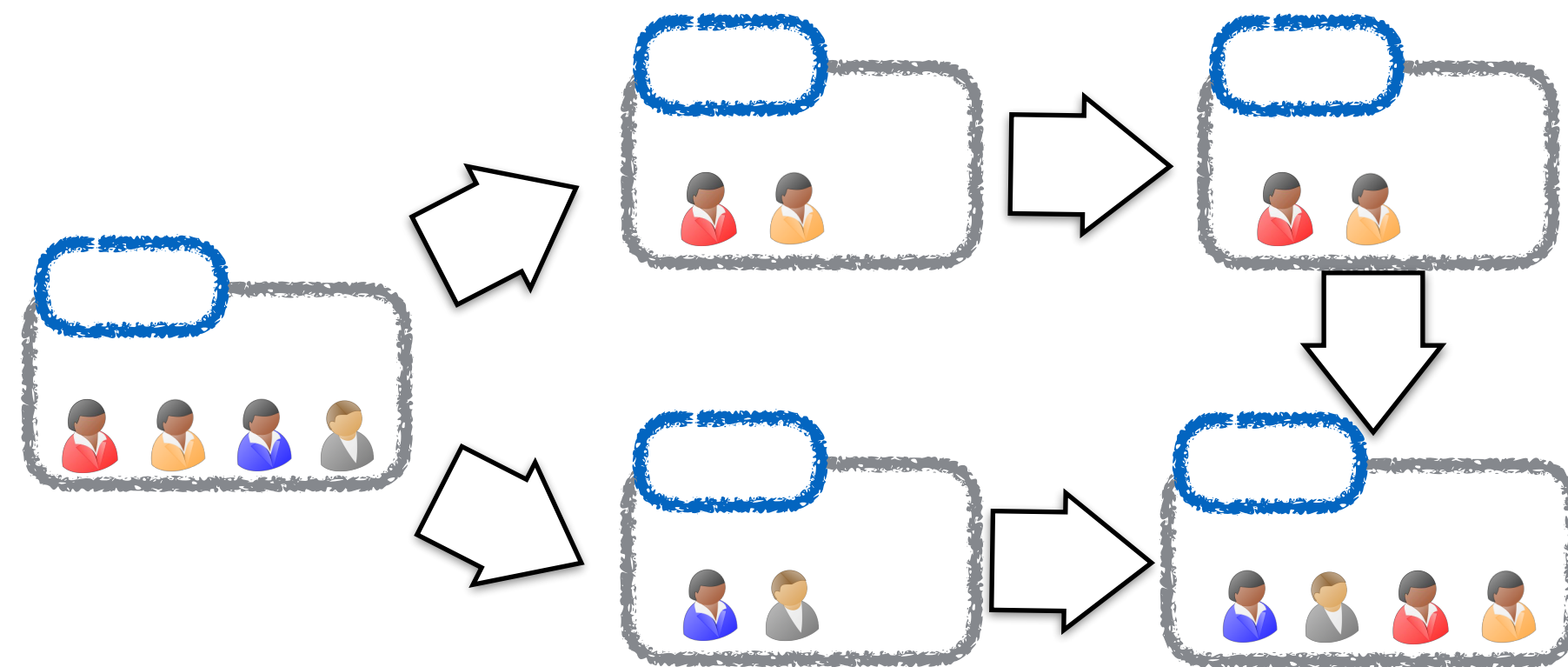
# Cryptographic agility

Second contribution

$\mathcal{F}_{update}$

Parameters

- Class of supported functionalities  $\mathcal{C}_{\mathcal{F}}$
- UpdatePredicate()
- StateUpdate()



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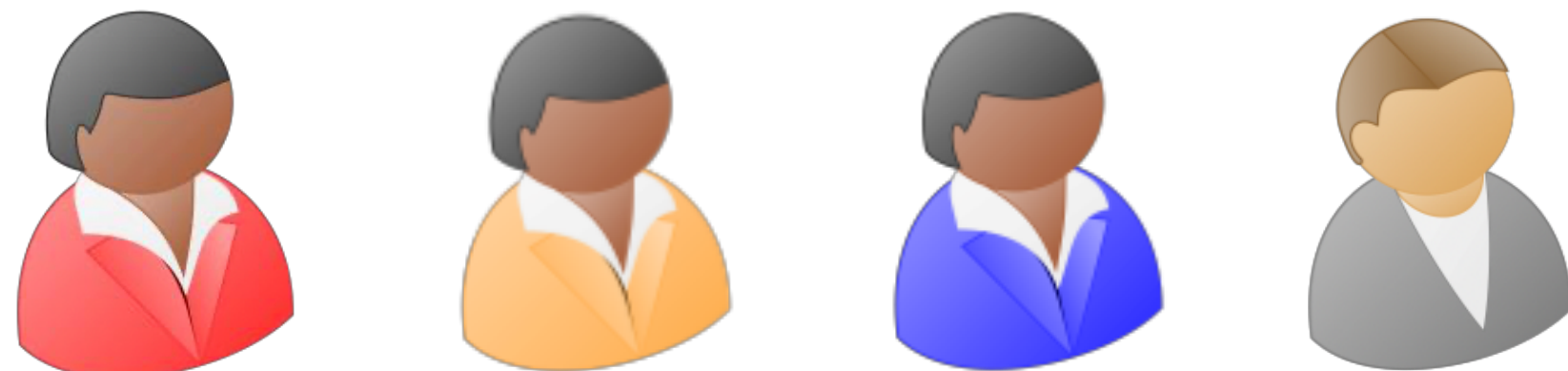
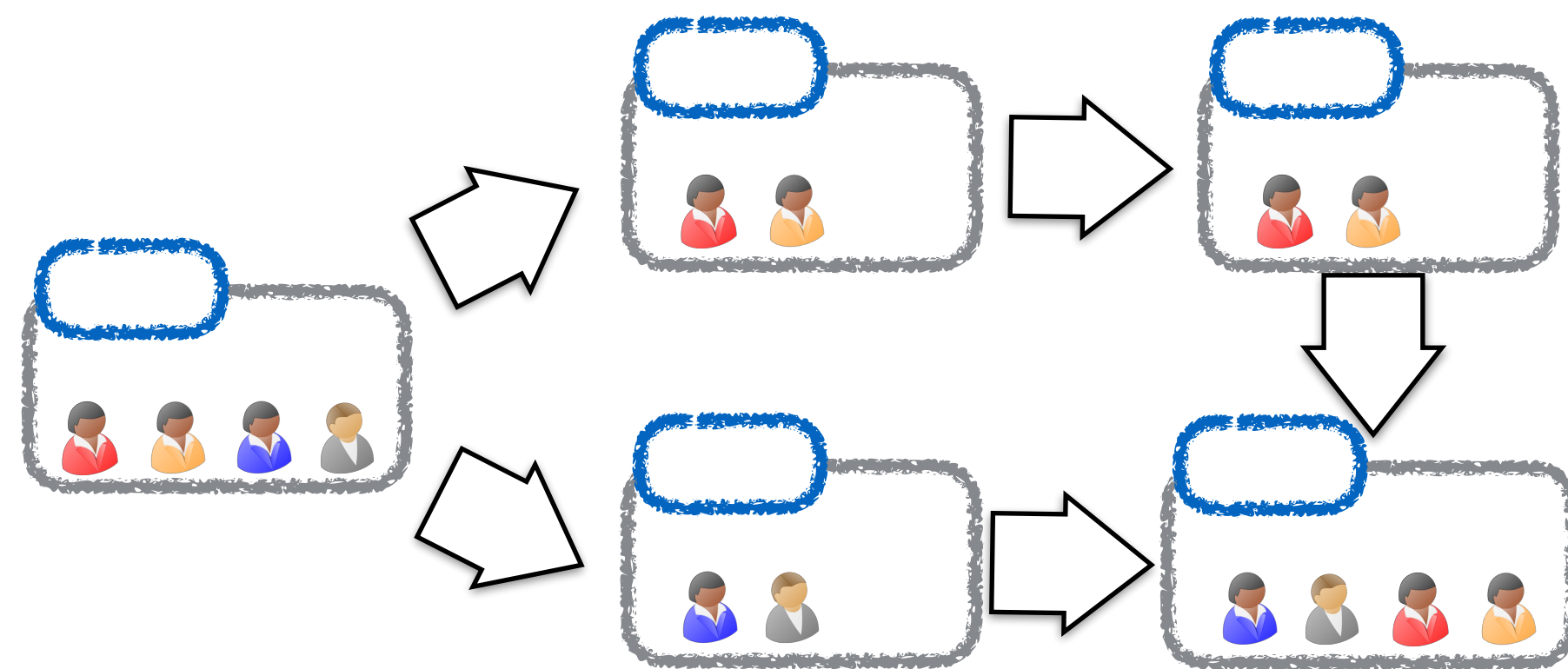
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e.g., functionalities for which such that **state**  $\in \mathcal{L}$  or which have the same interface





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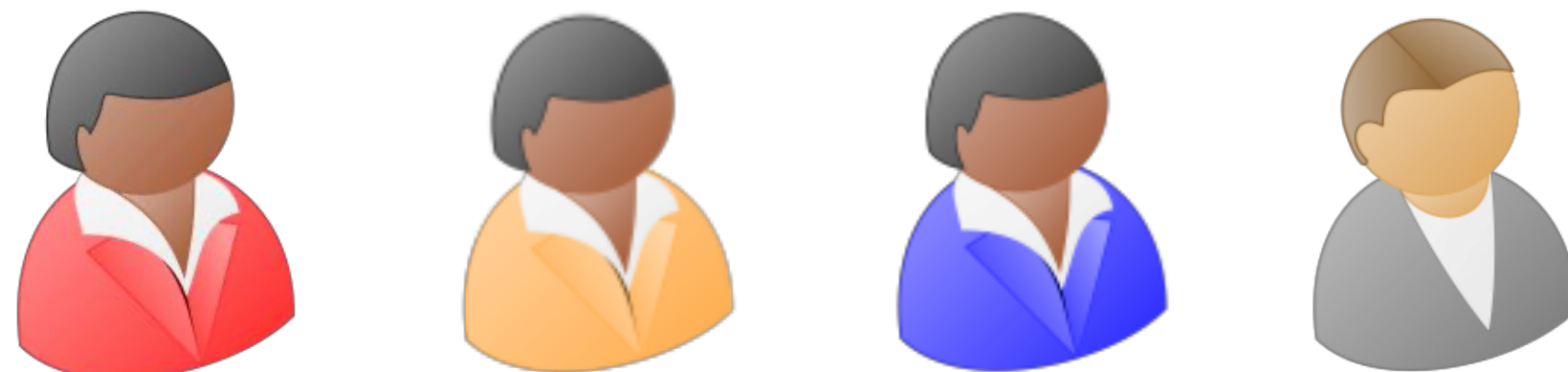
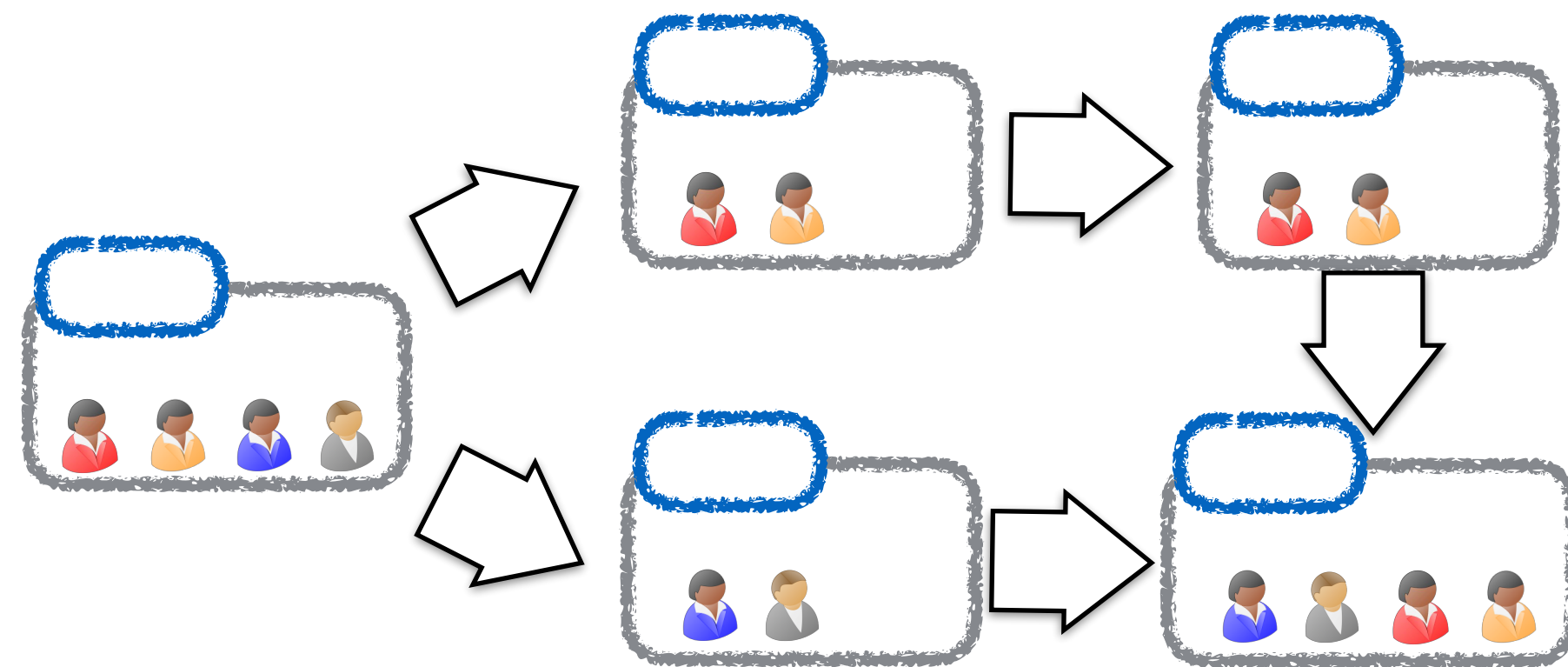
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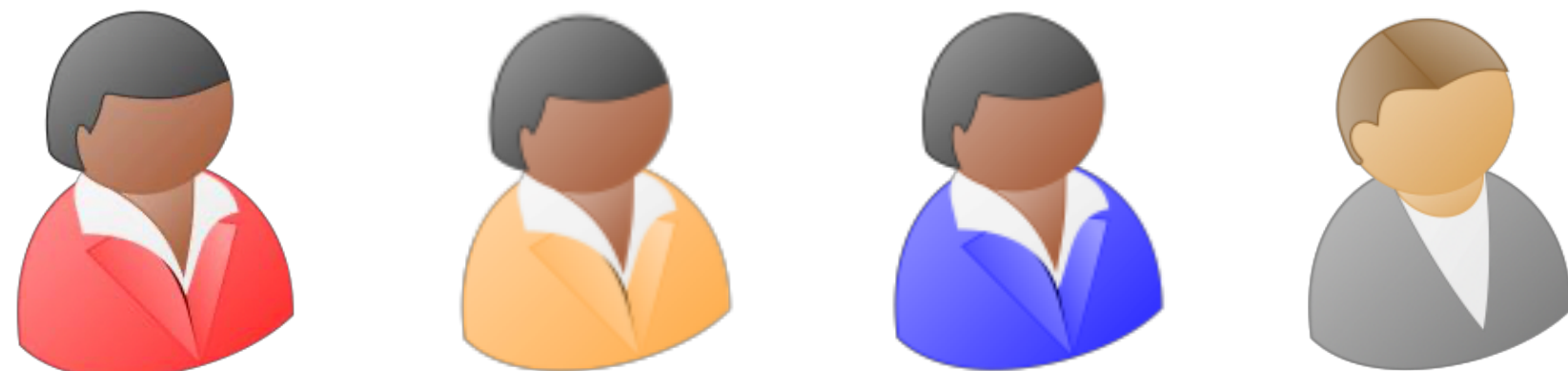
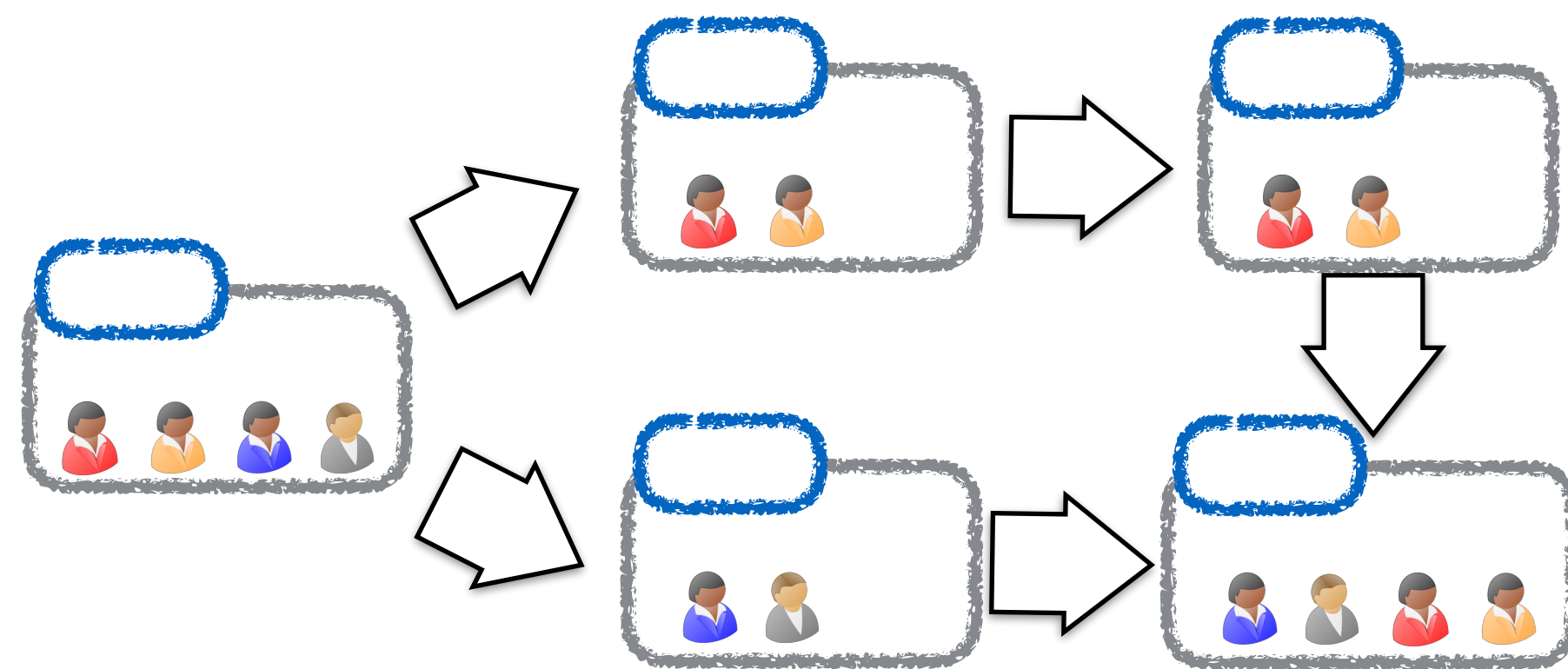
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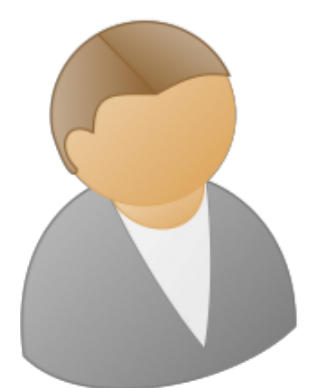
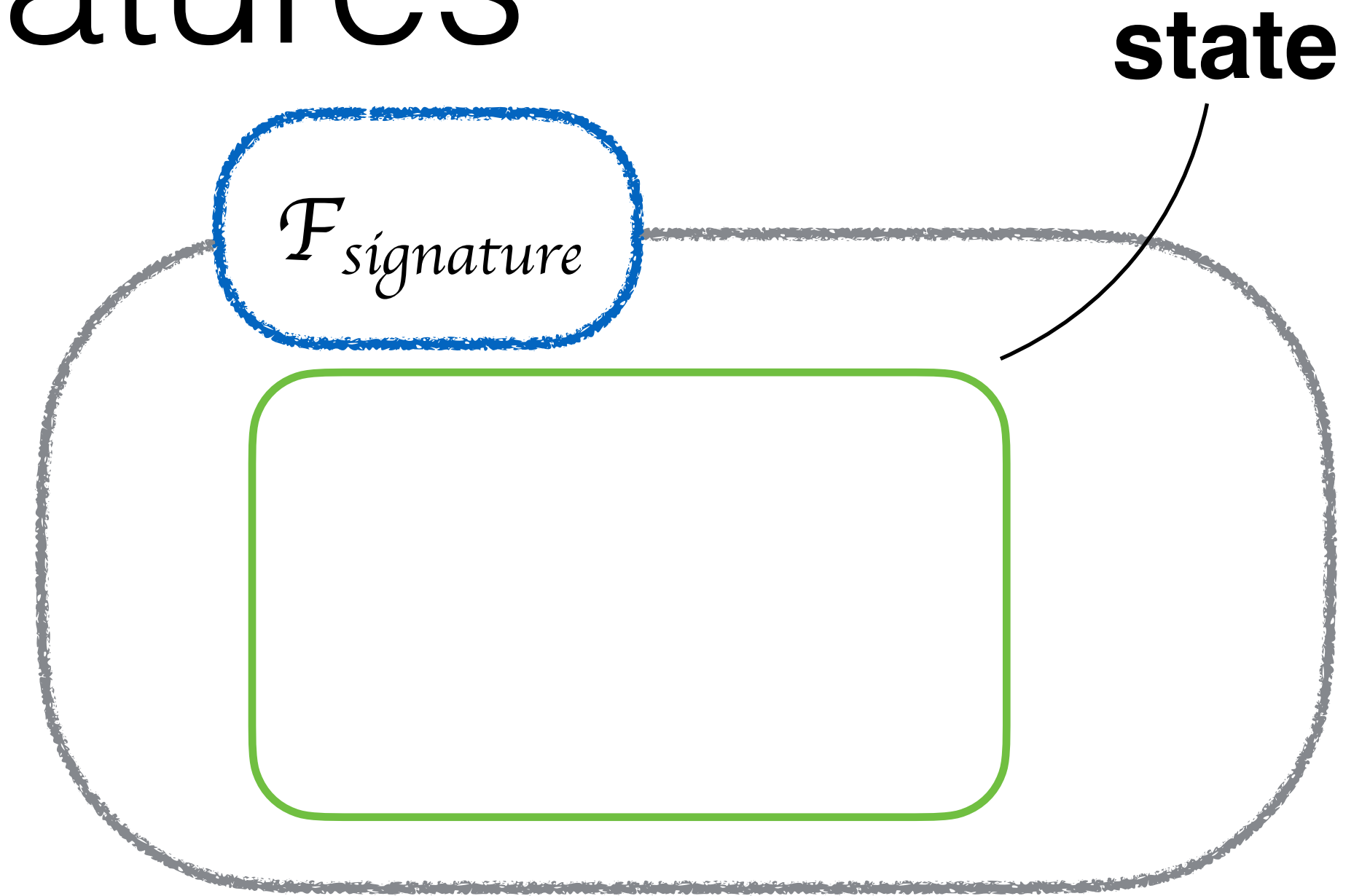
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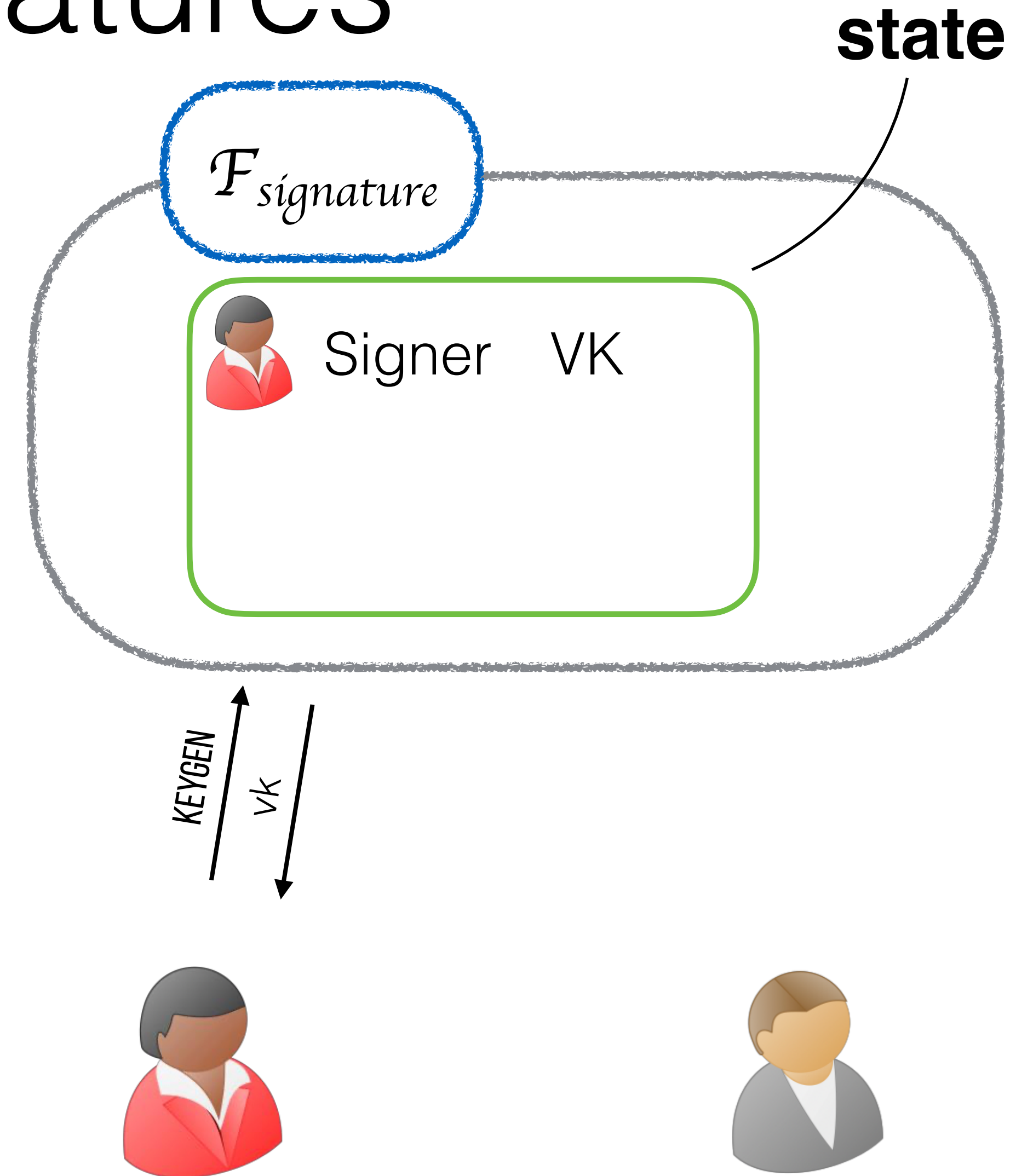
e.g., what part of the state should be preserved



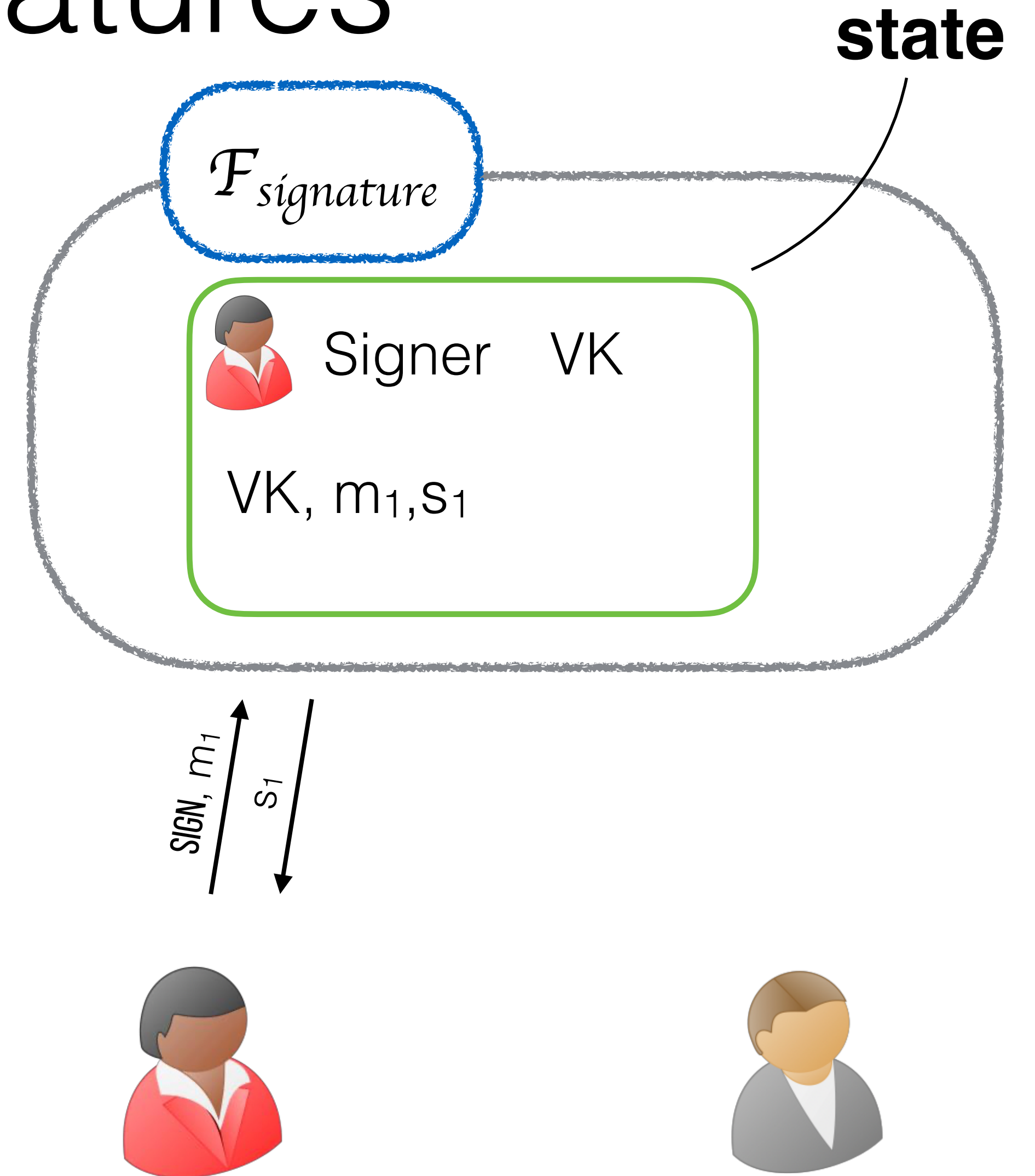
# Updatable signatures



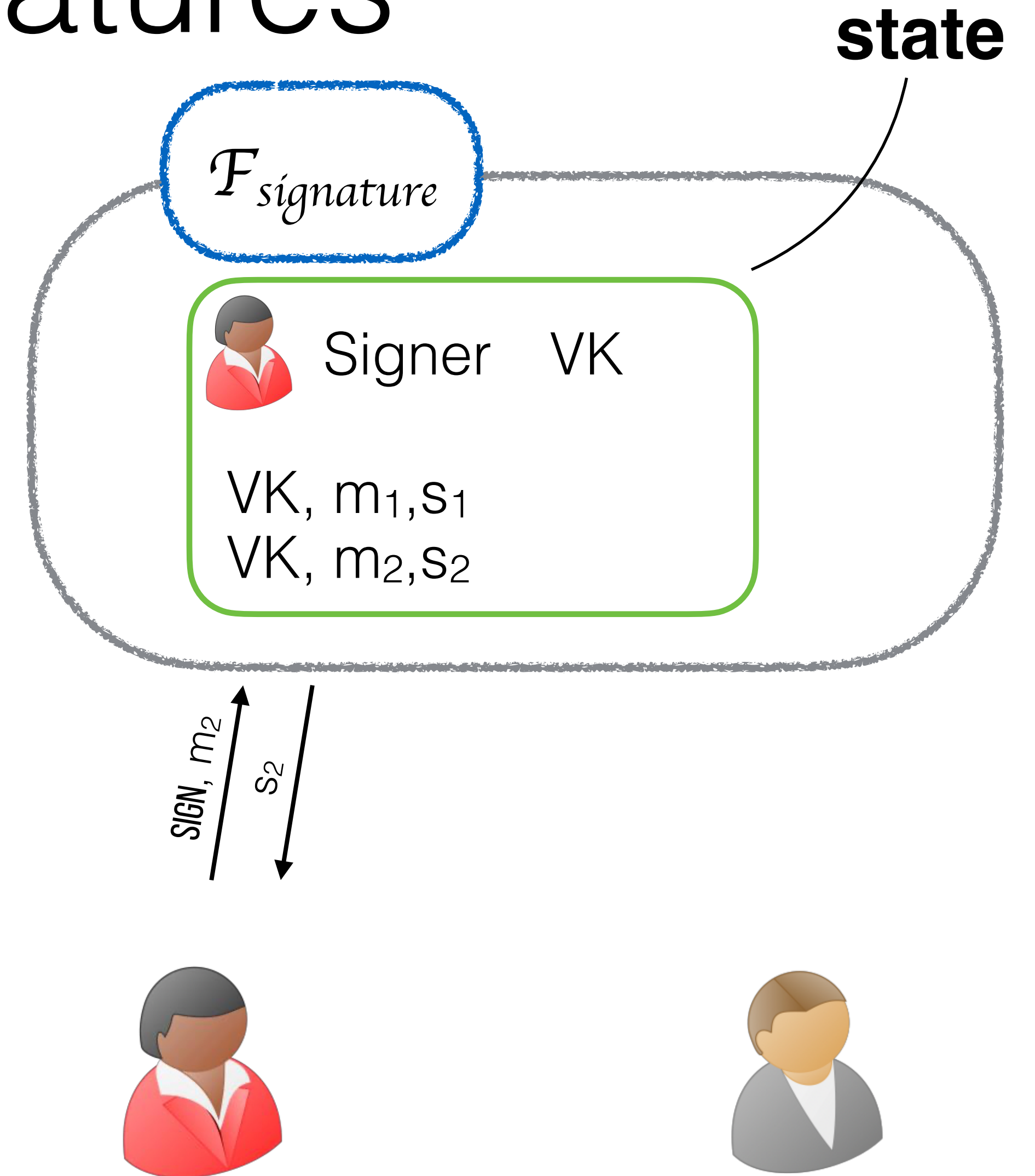
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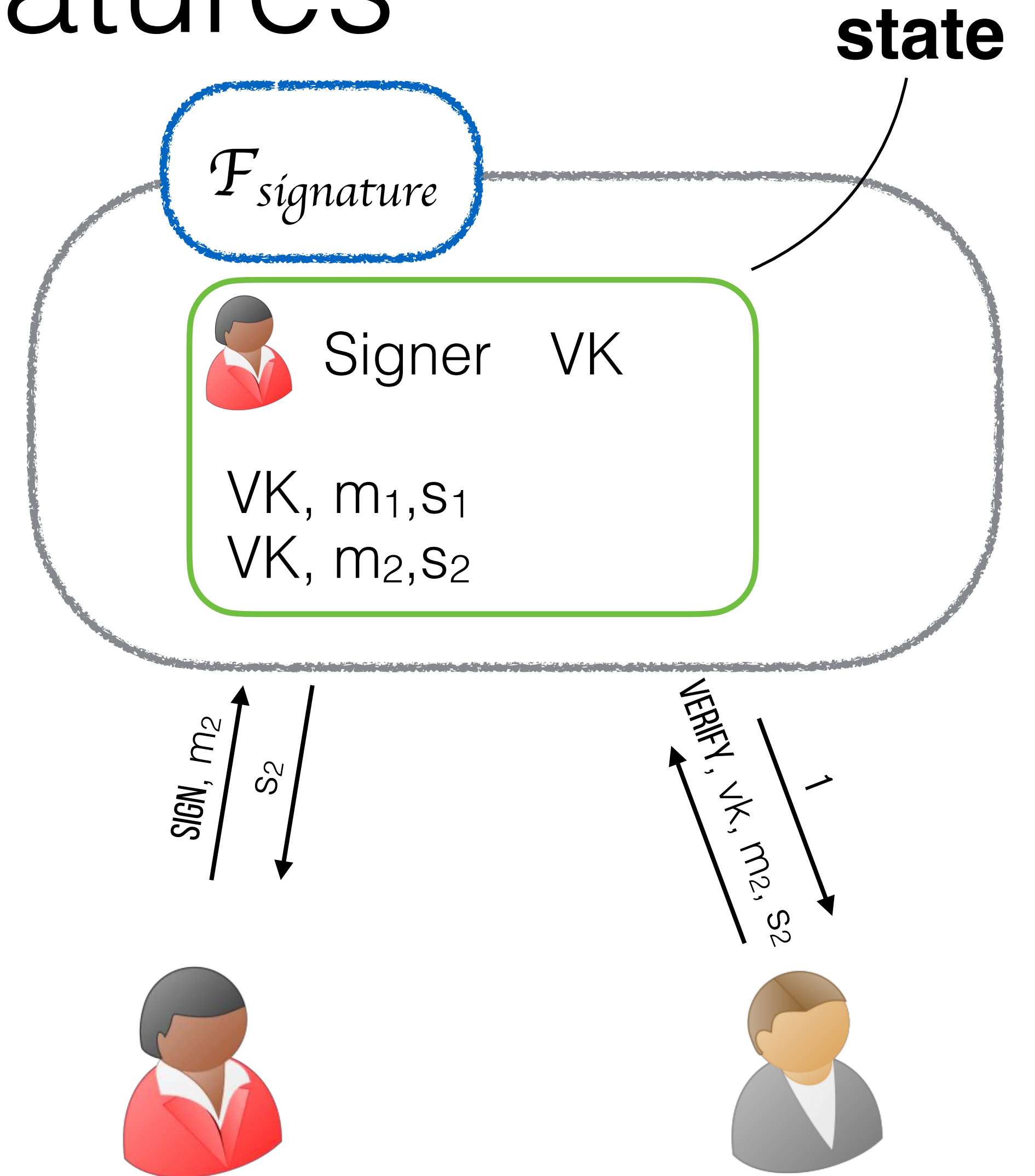
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# Updatable signatures


$\mathcal{F}_{update}$

- $C_{\mathcal{F}}$  = Signature functionalities
- Update when the signer decides that
- Copy the state in the new functionality

$\mathcal{F}_1$

 Signer VK  
VK,  $m_1, s_1$

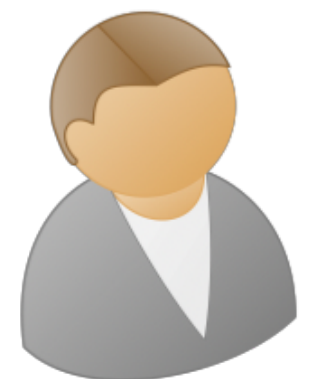
$\mathcal{F}_{signature}$

 Signer VK  
VK,  $m_1, s_1$   
VK,  $m_2, s_2$

state

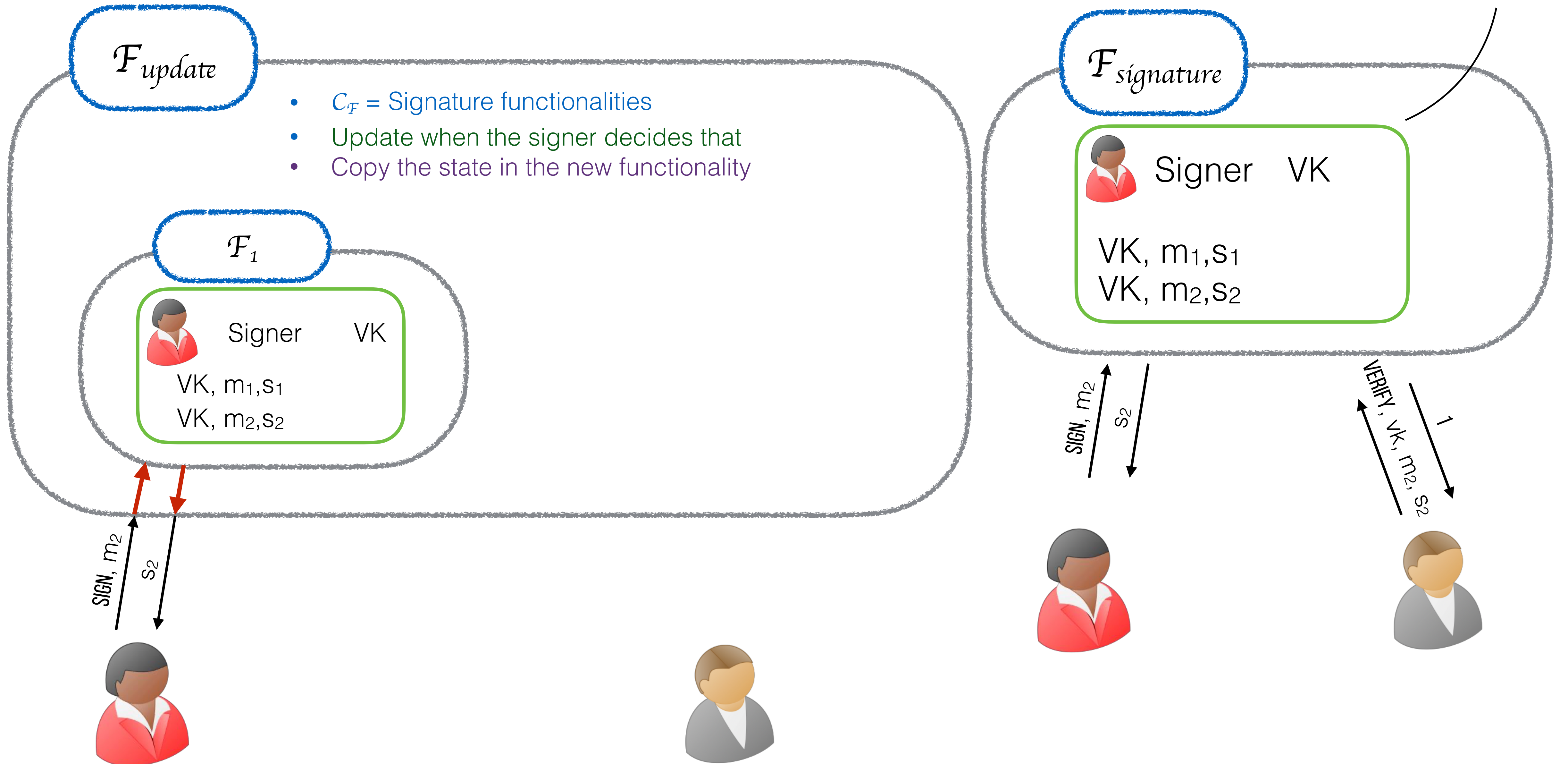
SIGN,  $m_2$   
 $s_2$

VERIFY, VK,  $m_2, s_2$   
1





# Updatable signatures



# Updatable signatures

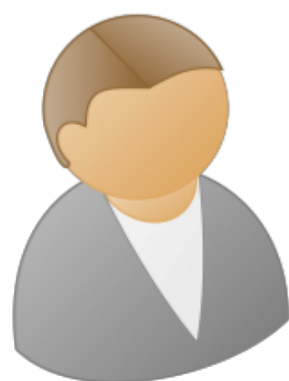
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$\mathcal{F}_1$

 Signer VK  
VK,  $m_1, s_1$   
VK,  $m_2, s_2$

UPDATE,  $\mathcal{F}_2$



$\mathcal{F}_{signature}$

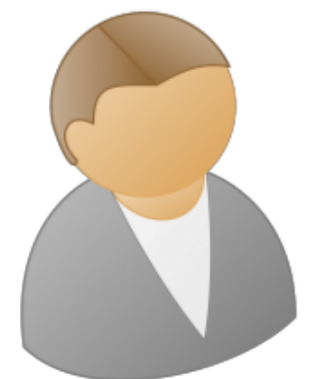
 Signer VK  
VK,  $m_1, s_1$   
VK,  $m_2, s_2$

state

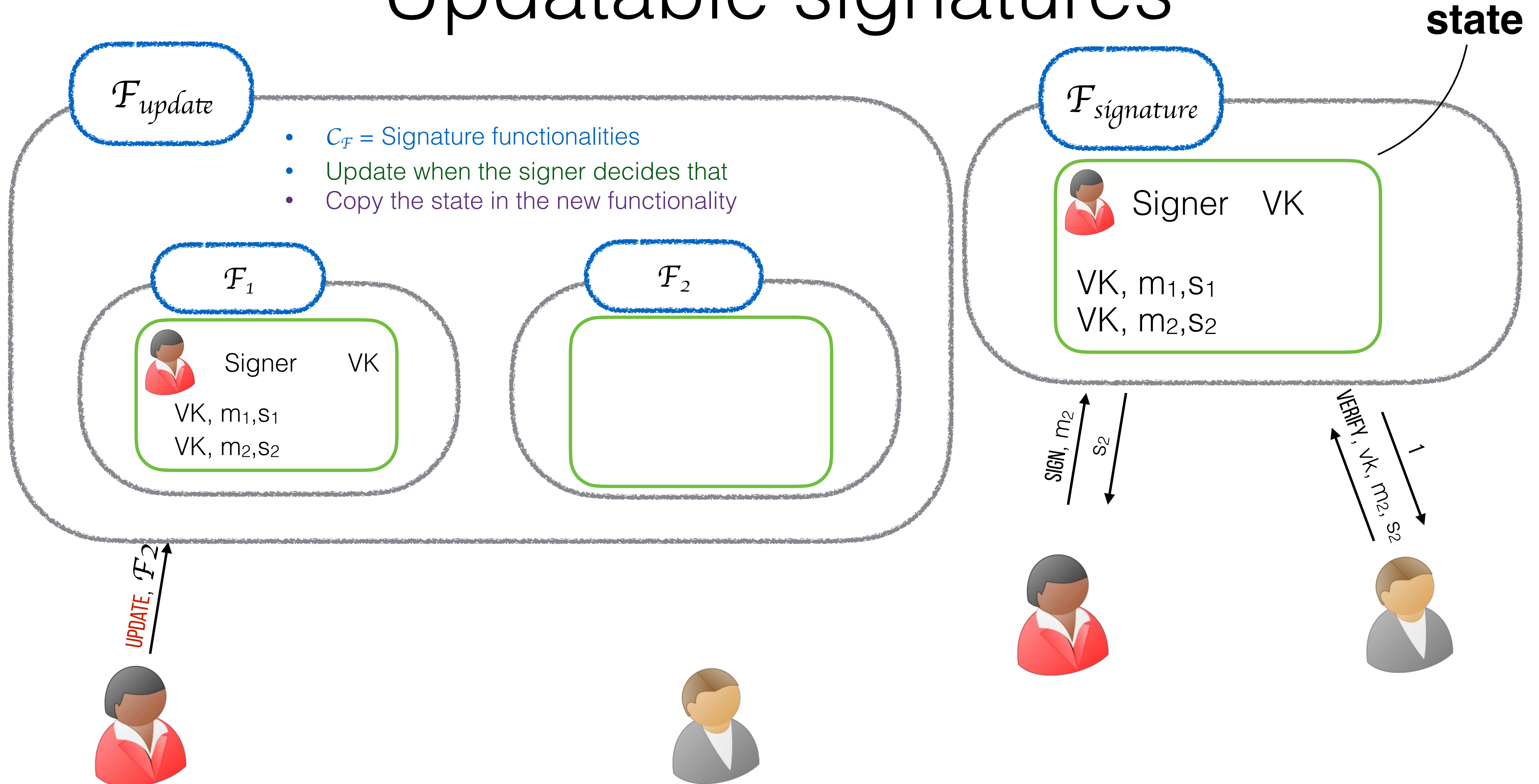
SIGN,  $m_2$   
 $s_2$



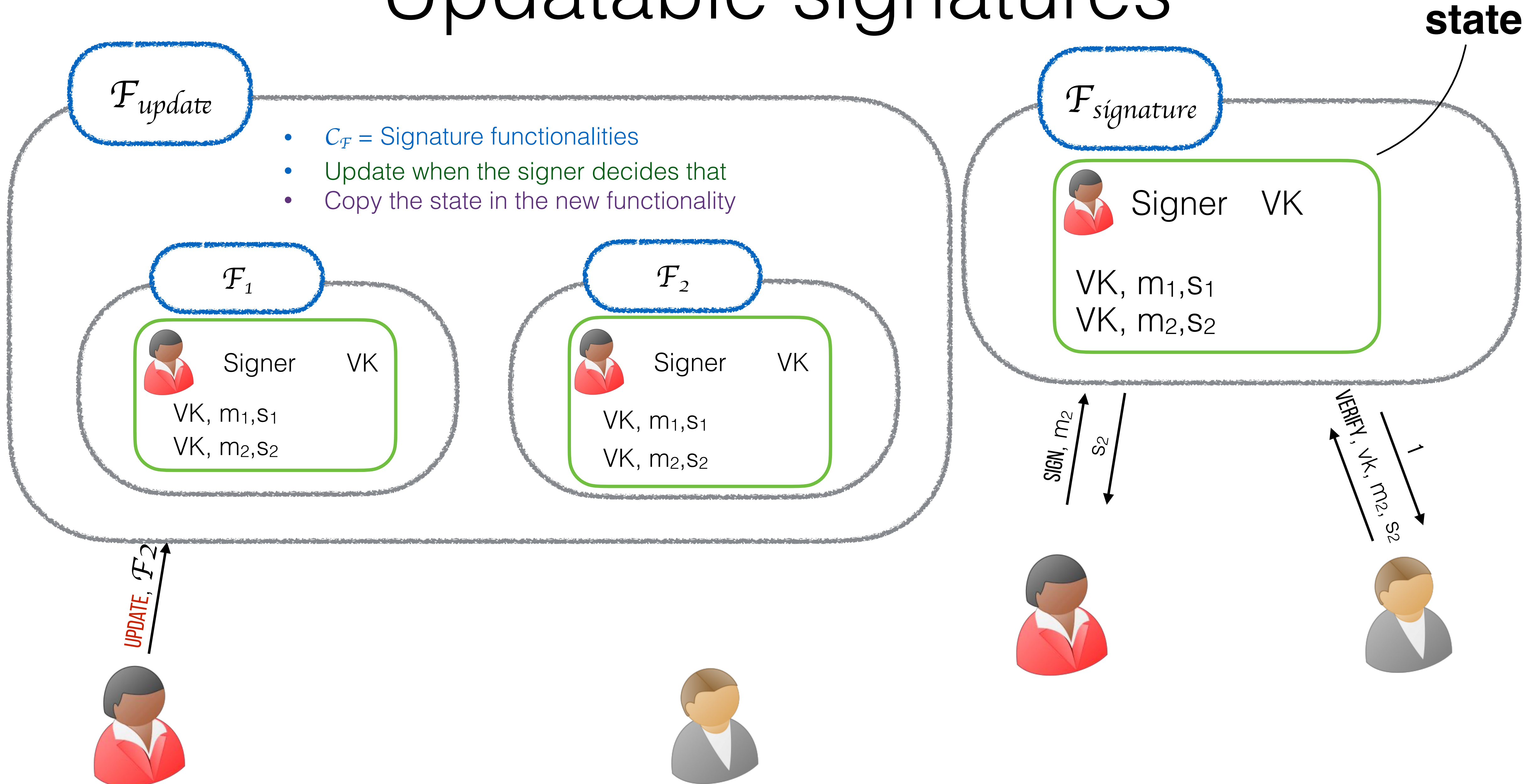
VERIFY, VK,  $m_2, s_2$   
1



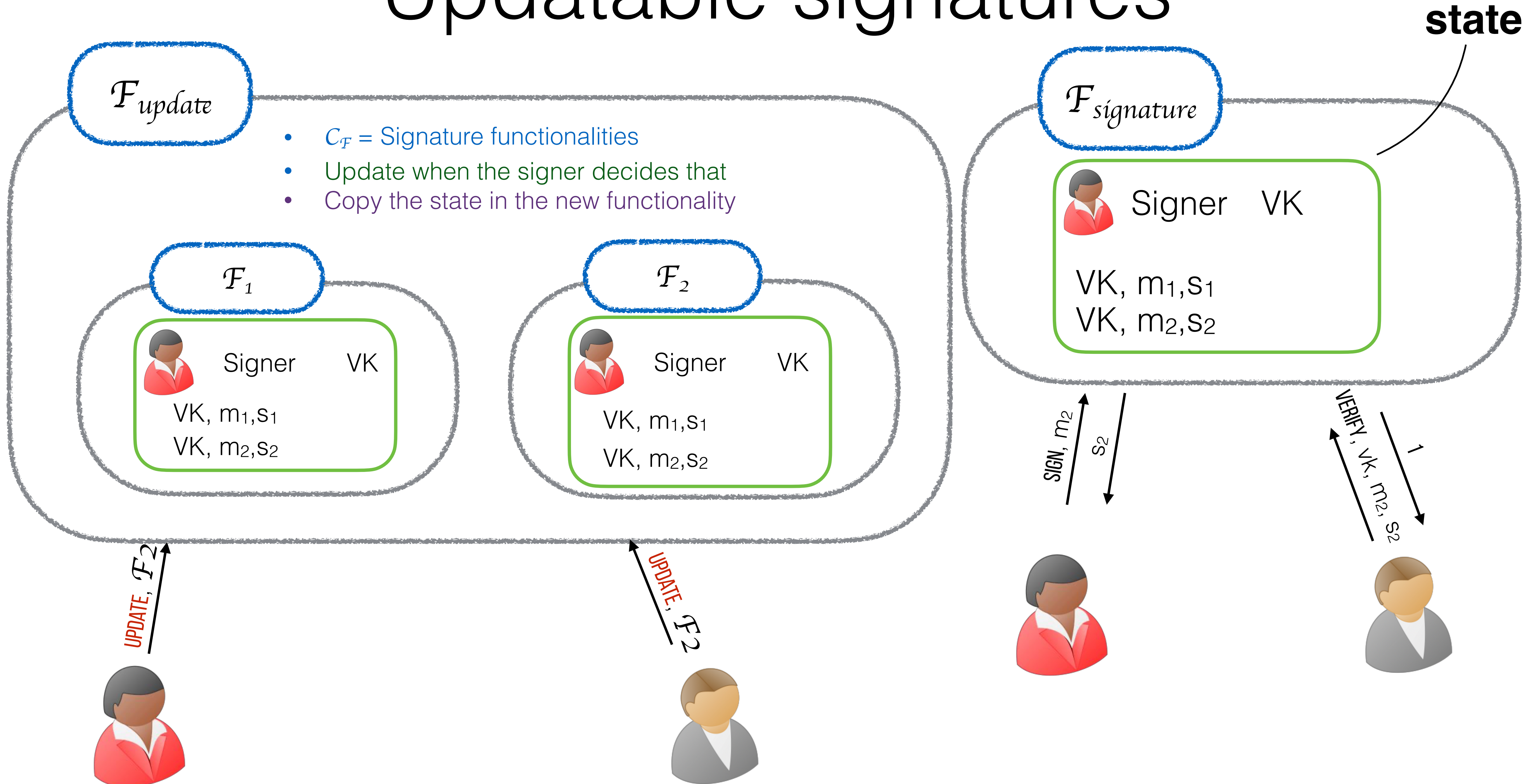
# Updatable signatures



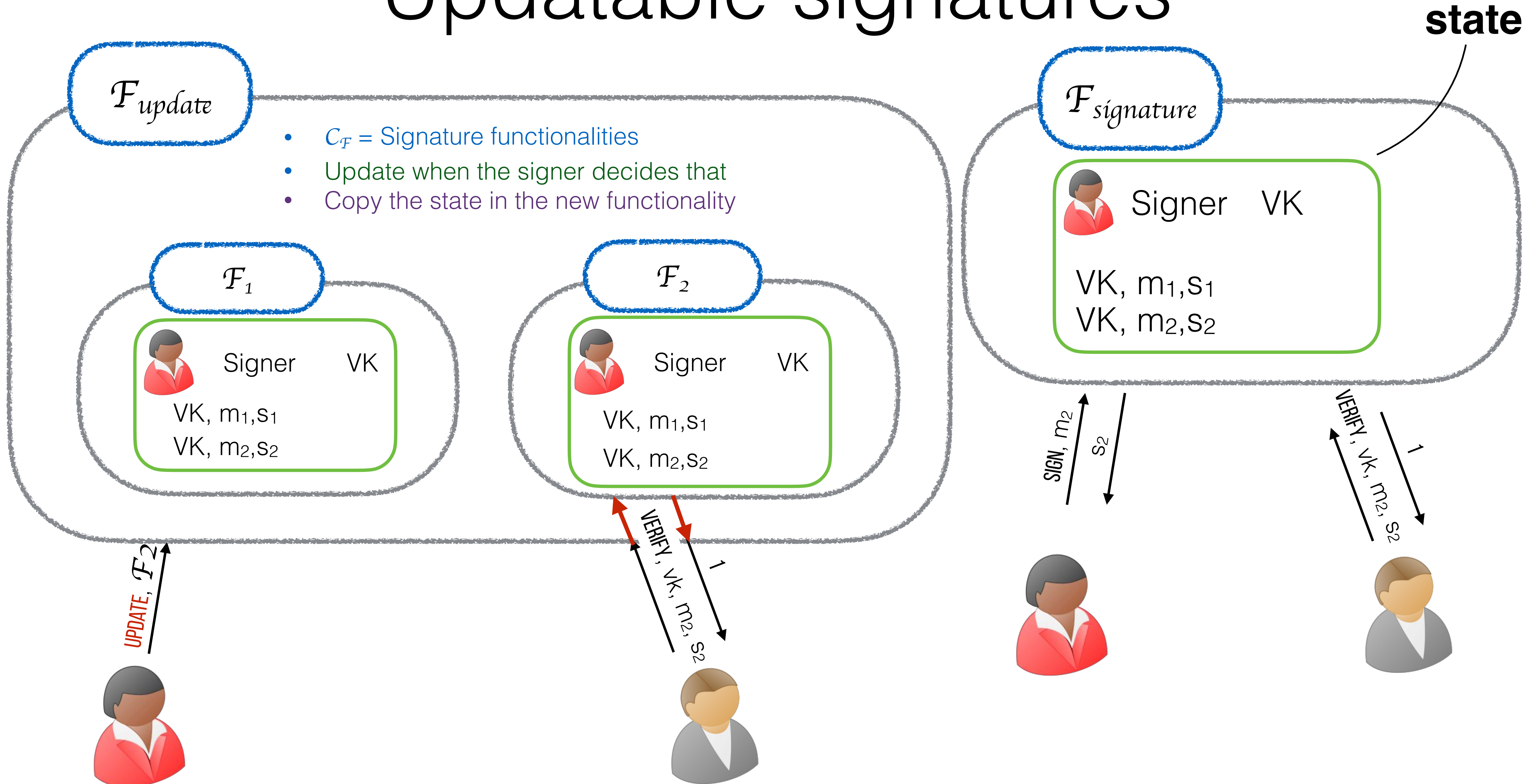
# Updatable signatures



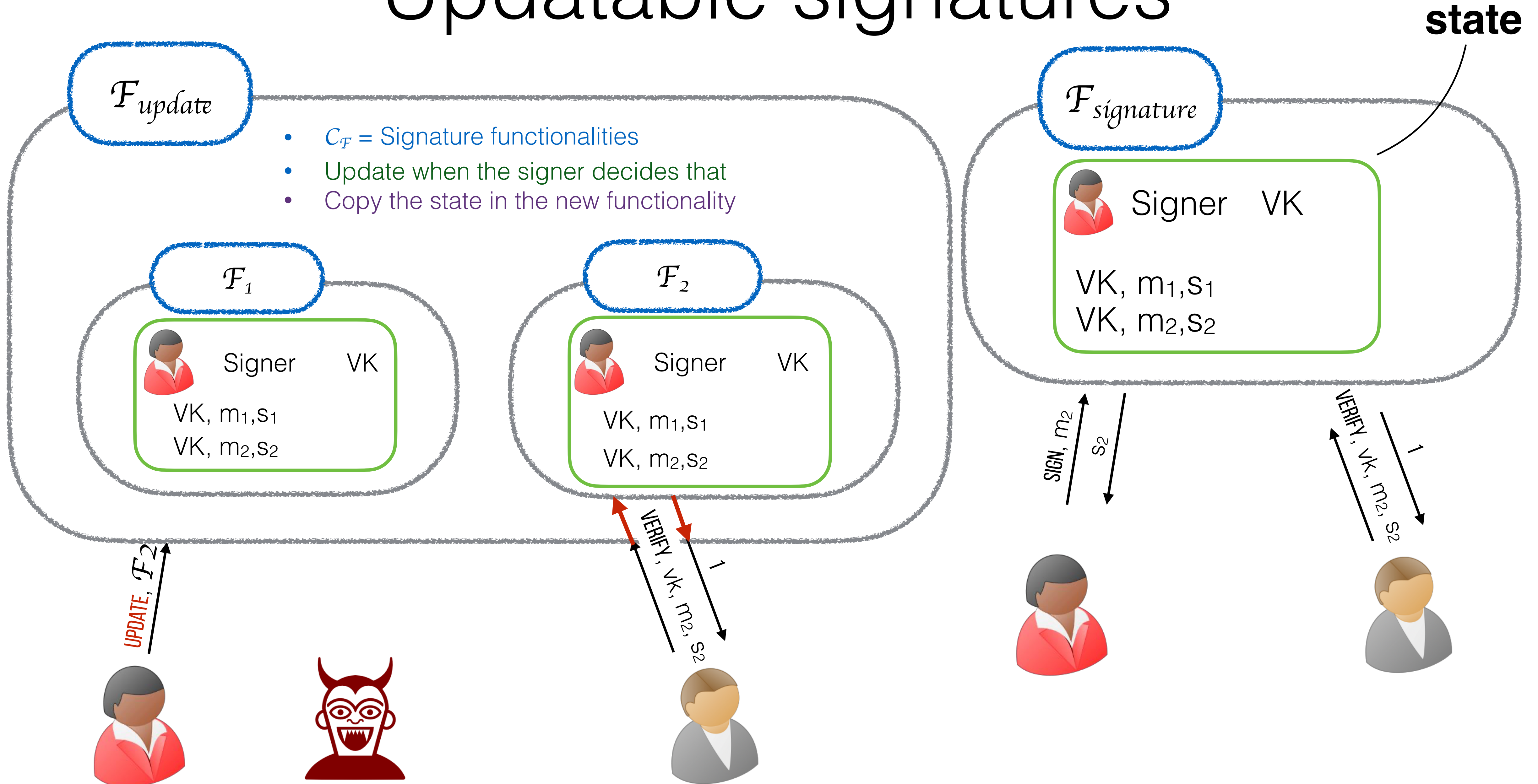
# Updatable signatures



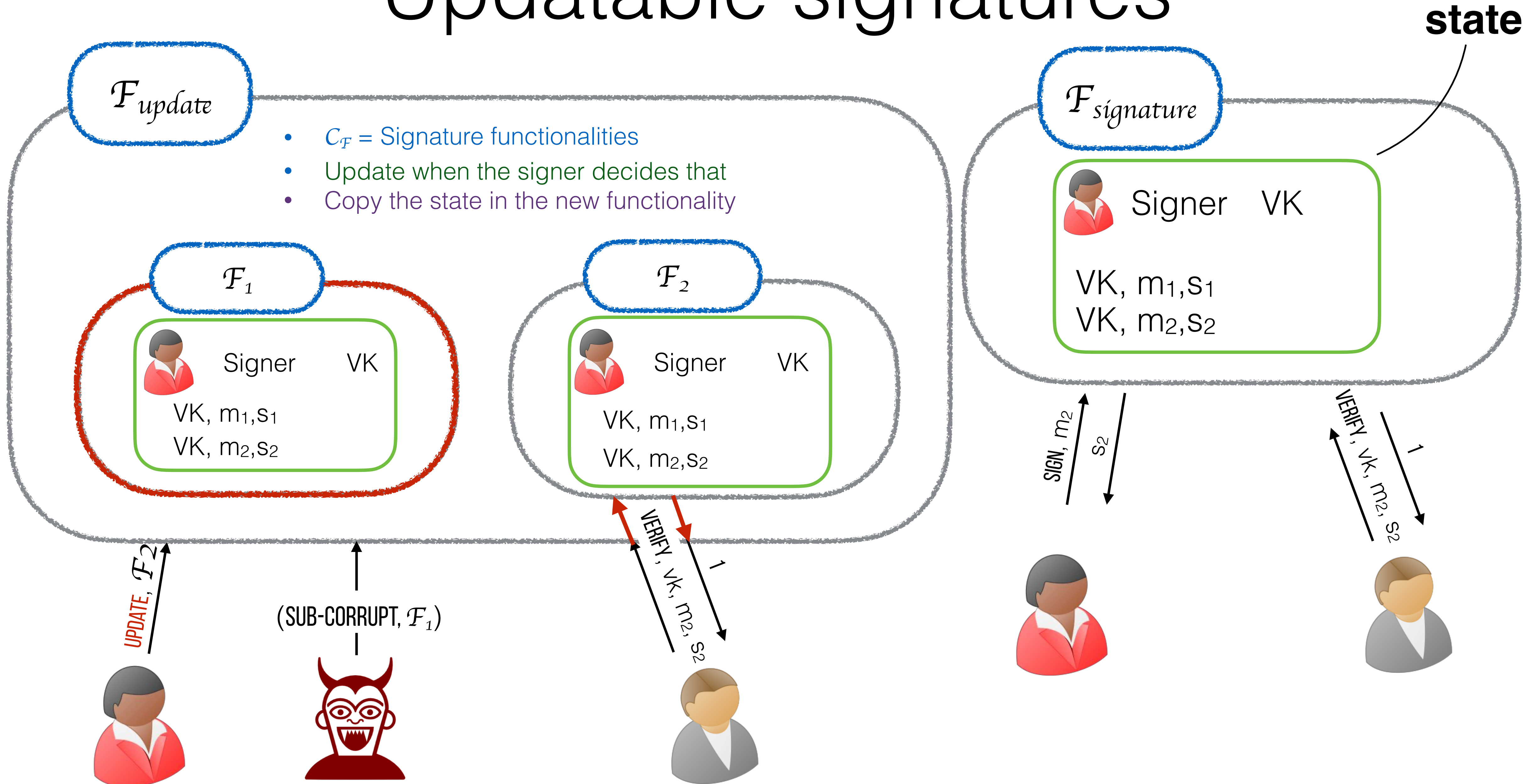
# Updatable signatures



# Updatable signatures

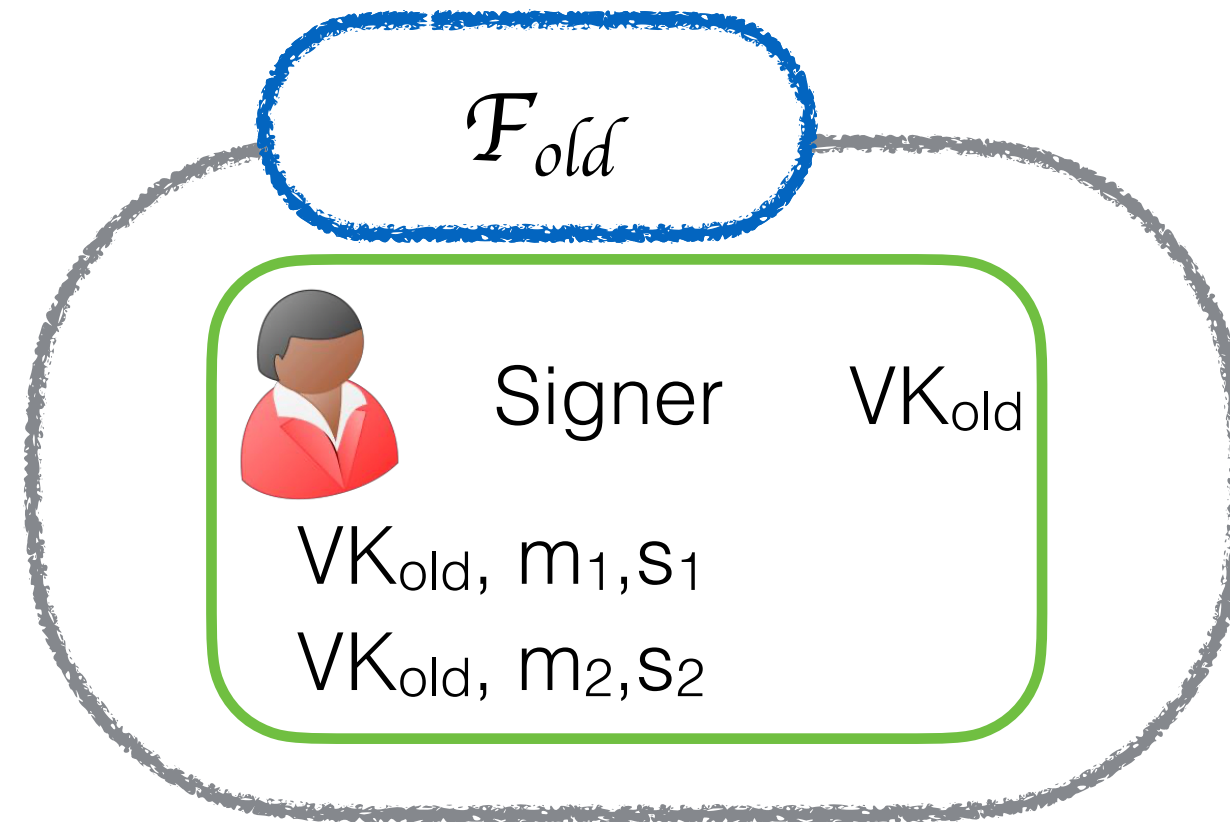


# Updatable signatures





# Updatable signatures

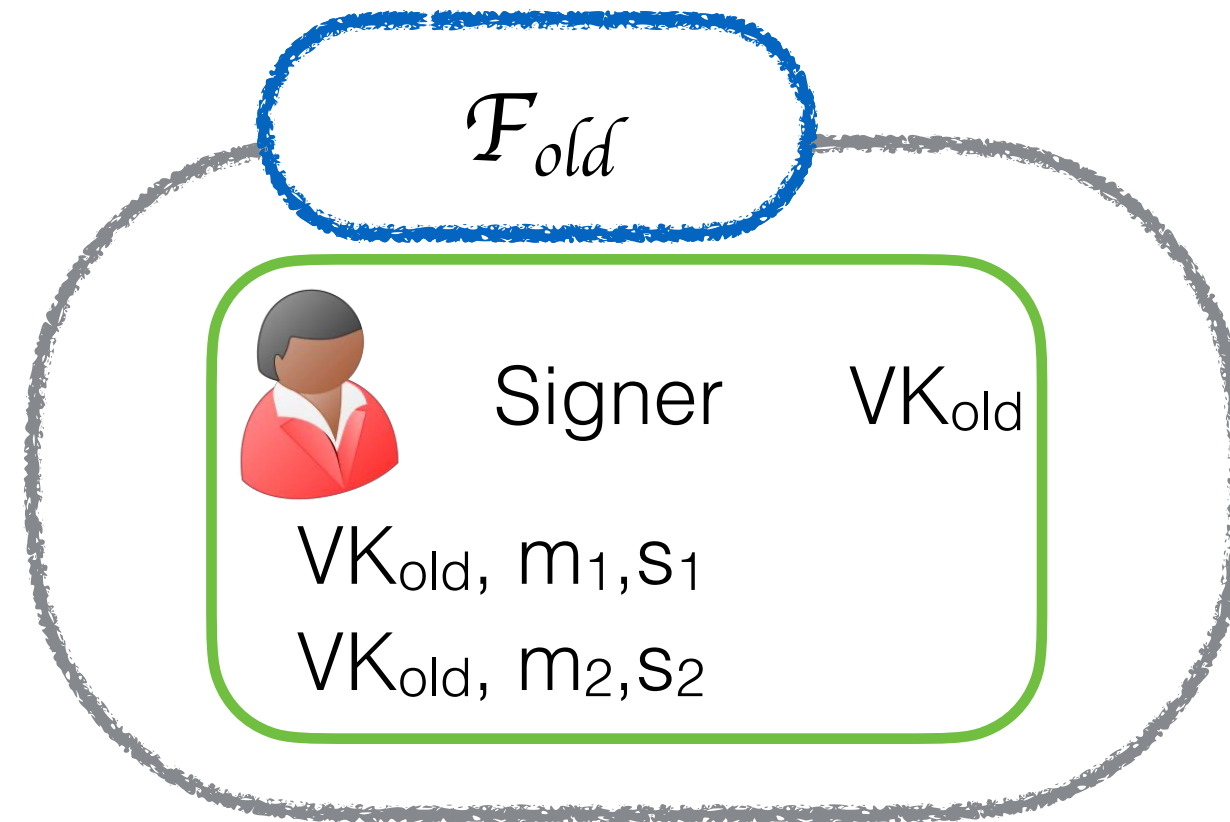


$VK_c$

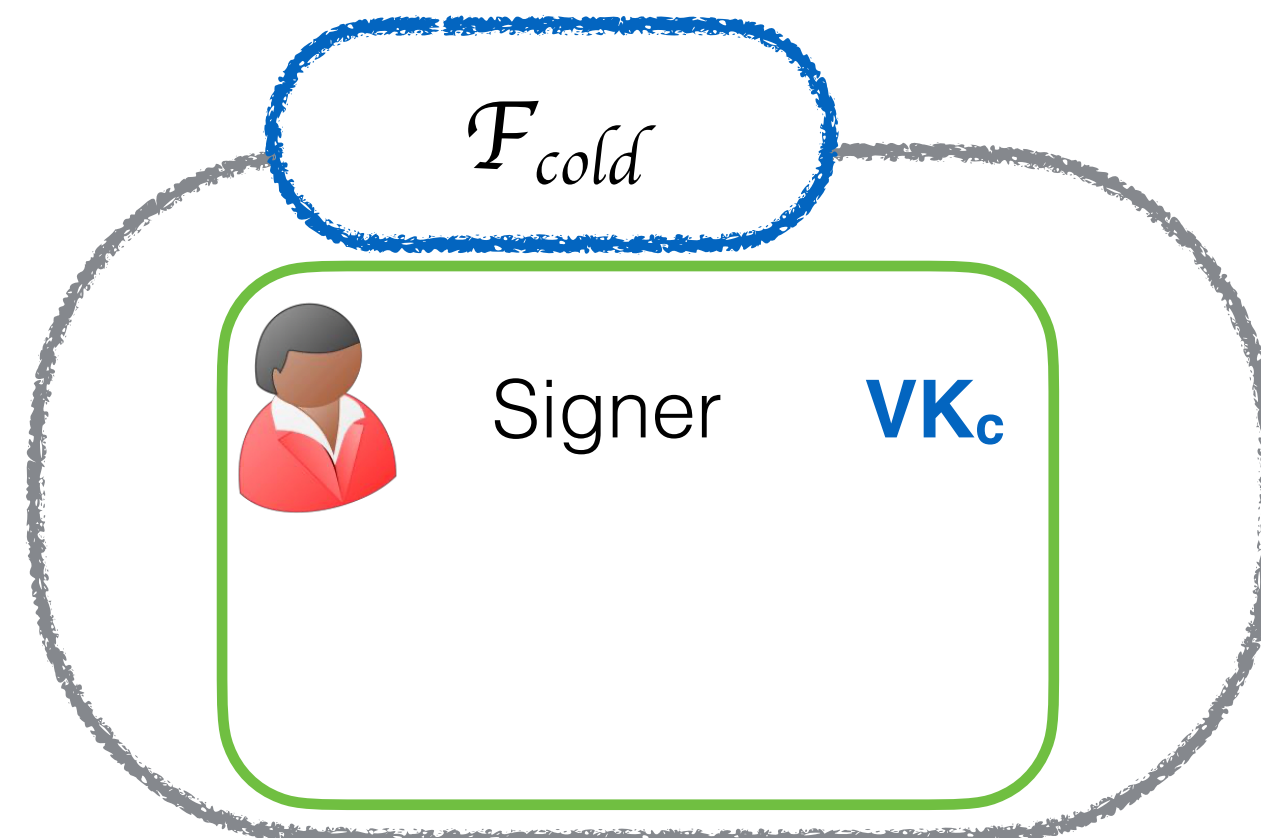


$VK_c$

# Updatable signatures



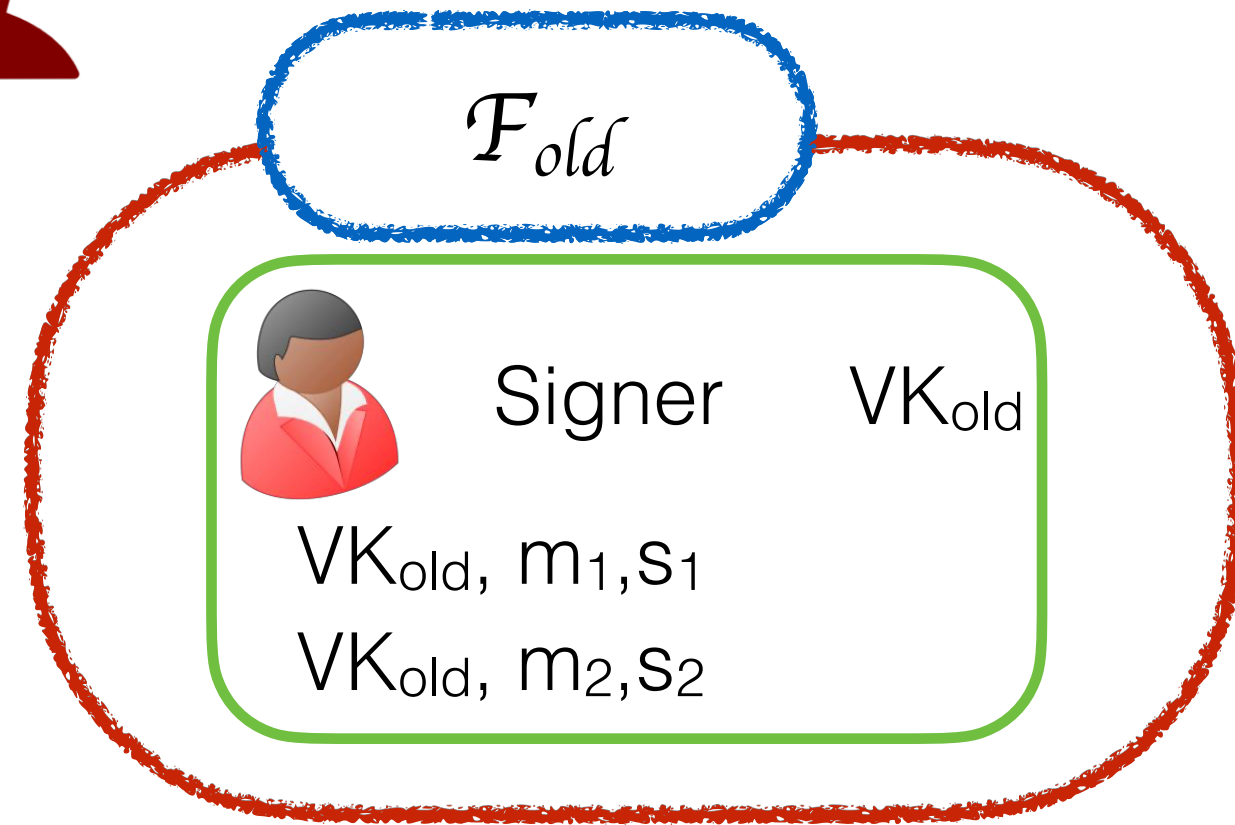
$VK_c$



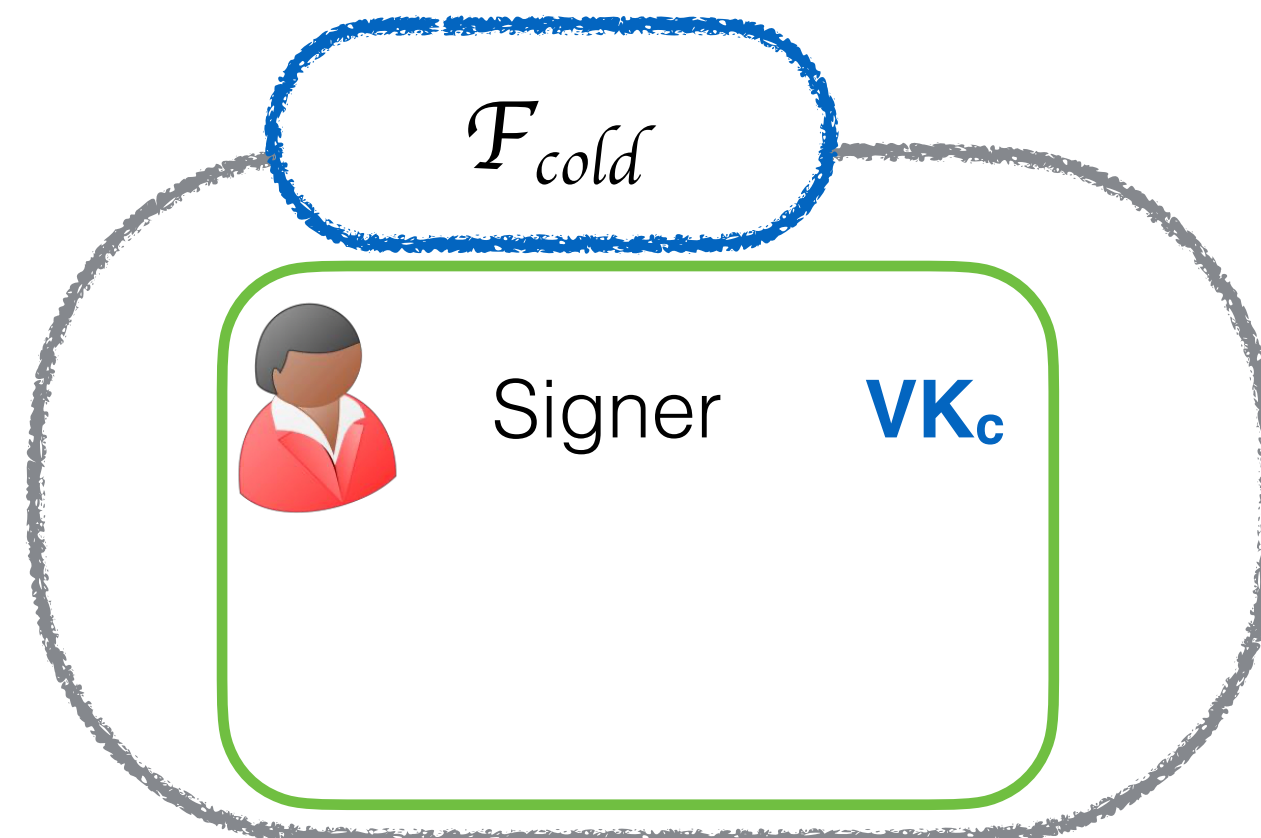
$VK_c$



# Updatable signatures



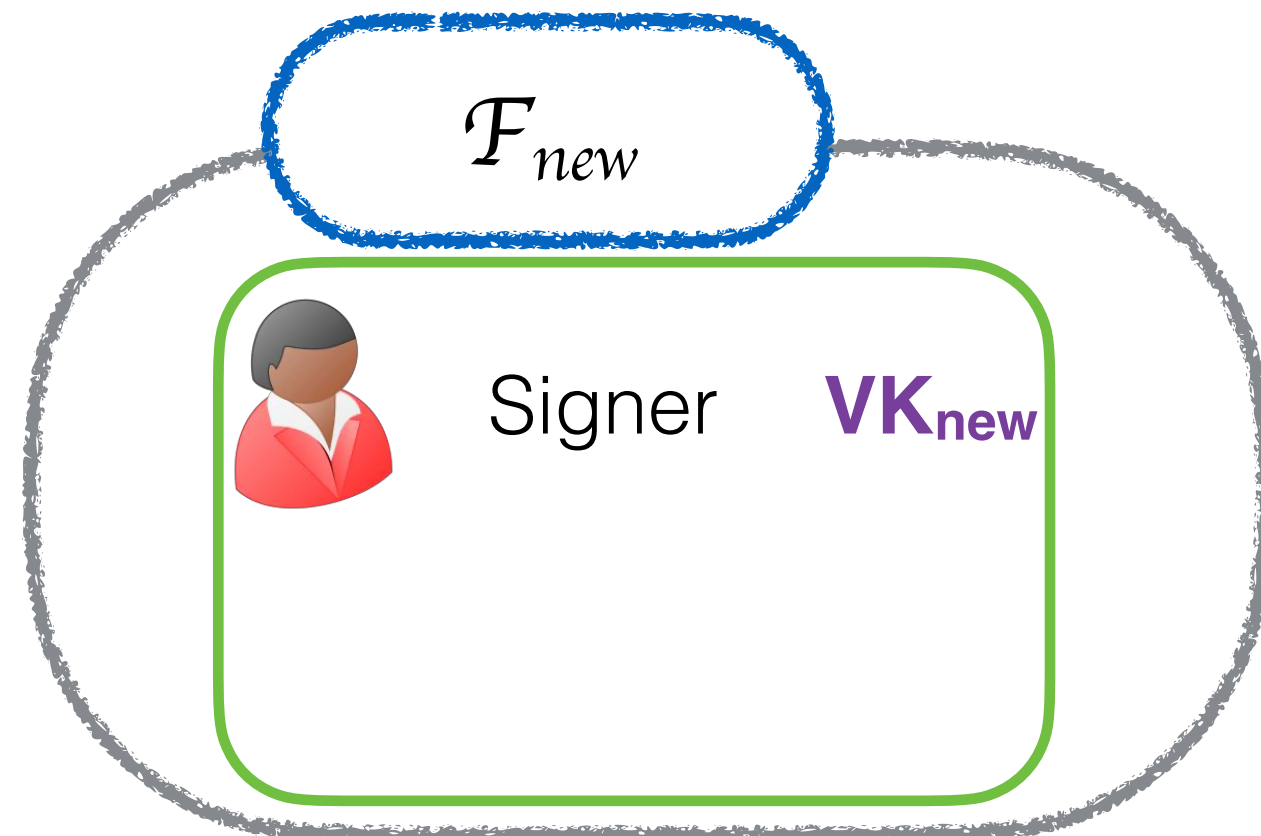
$VK_c$



$VK_c$



# Updatable signatures

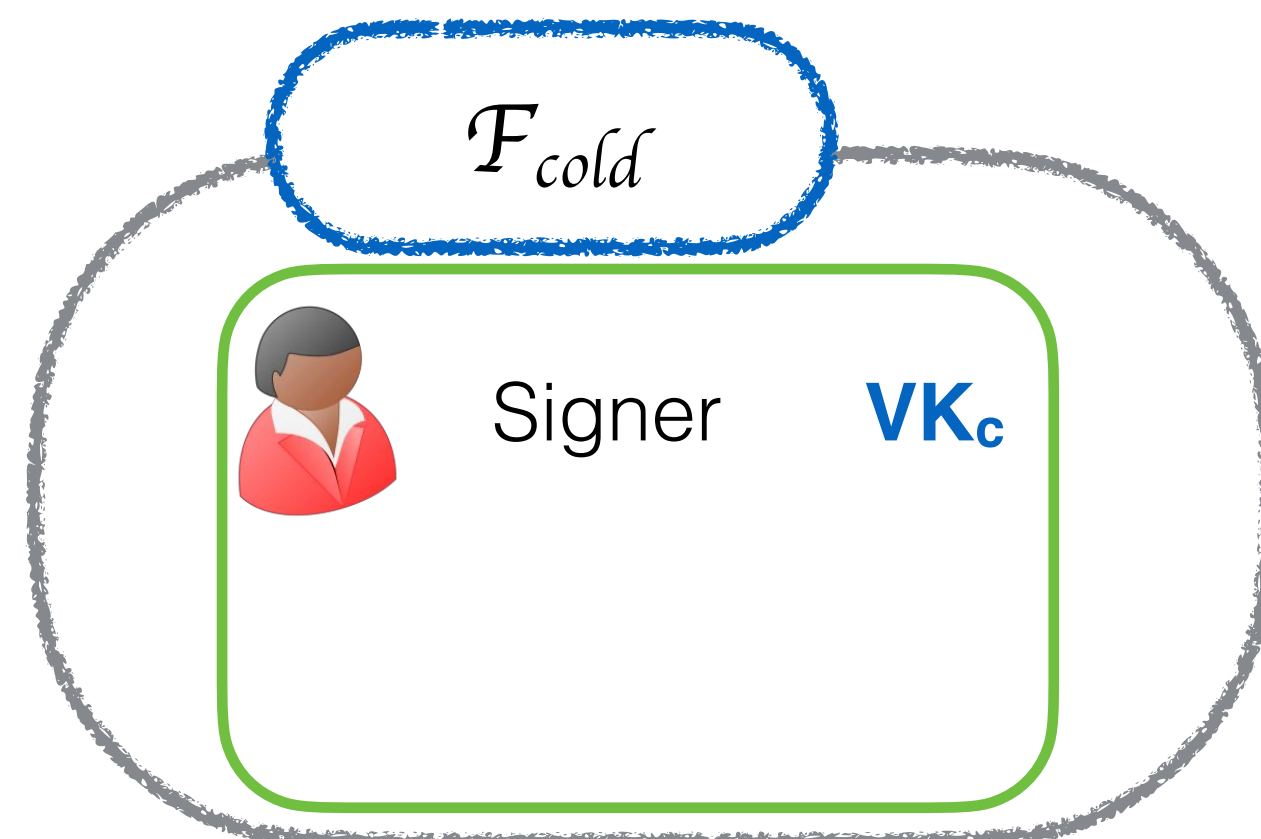


UPDATE,  $\mathcal{F}_{new}$



$VK_c$

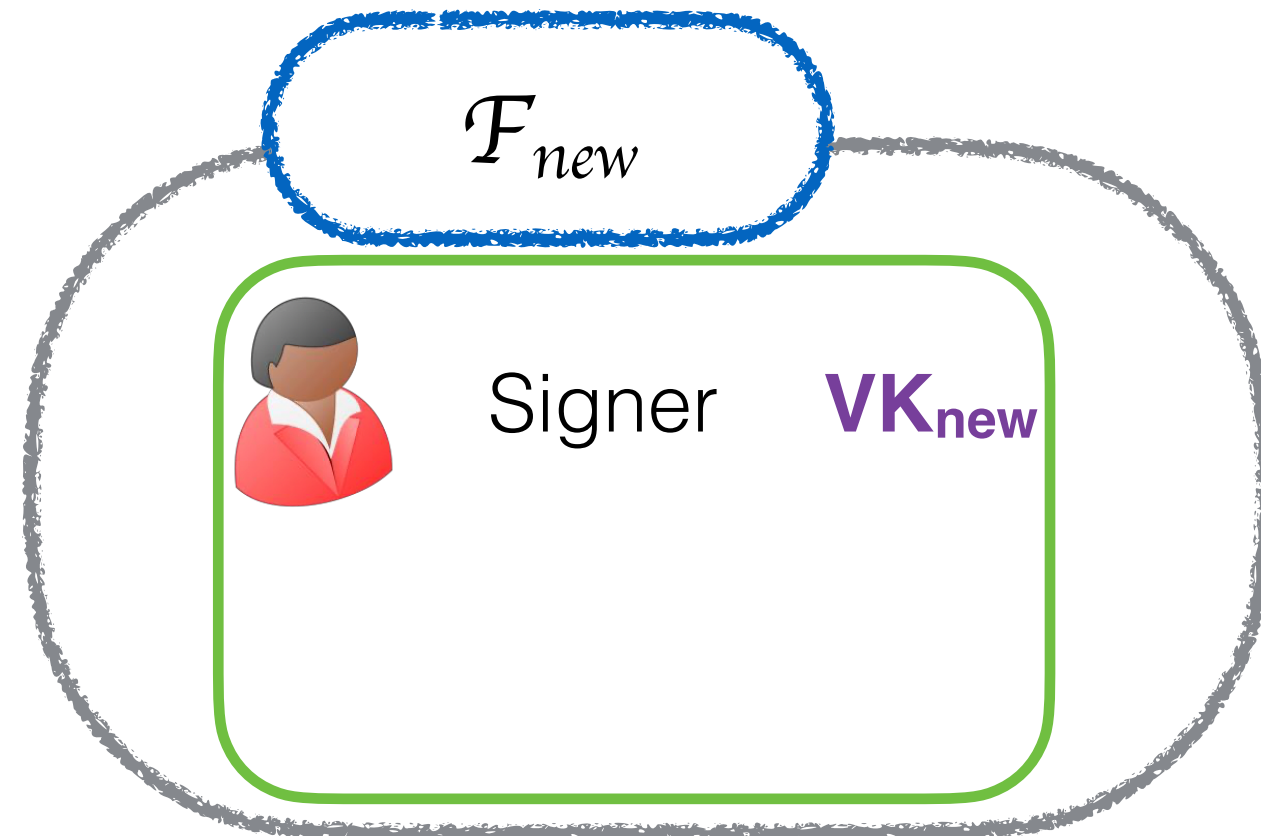
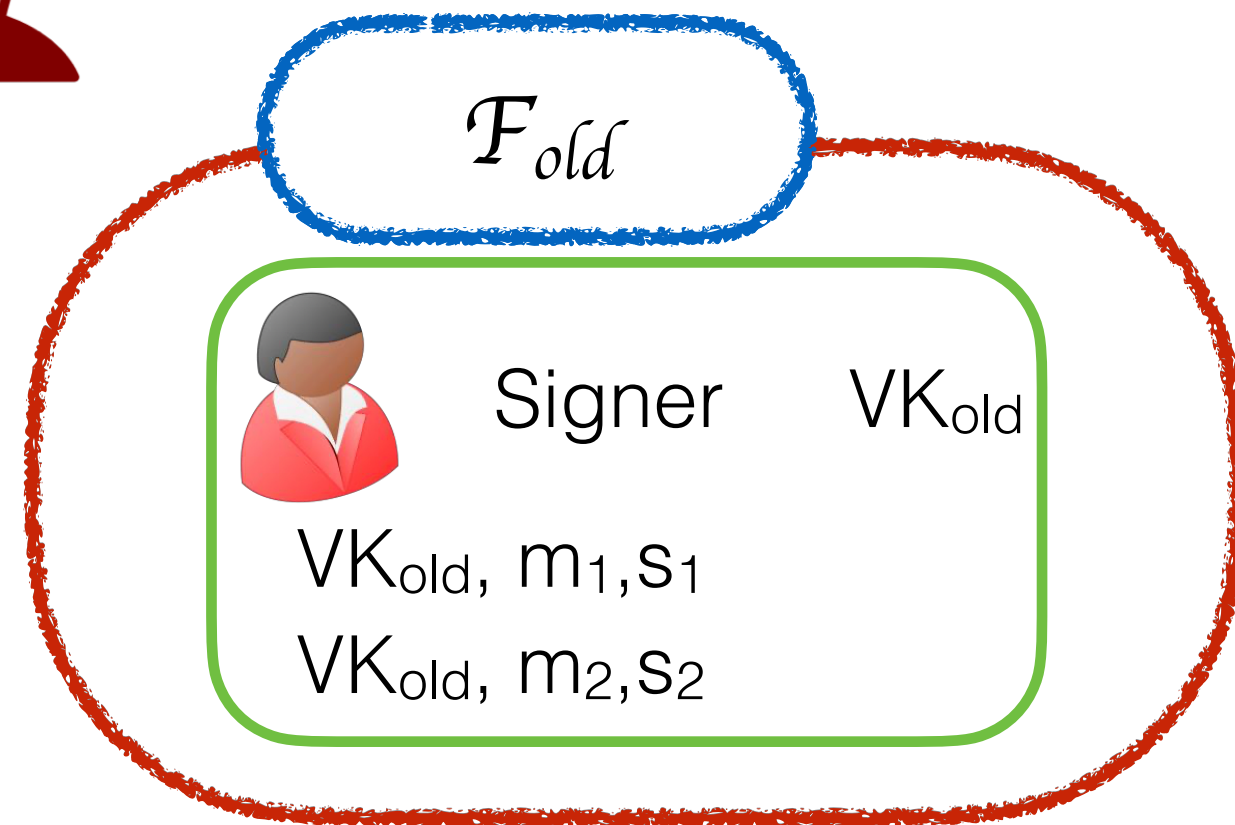
$VK_{new}$



$VK_c$



# Updatable signatures



UPDATE,  $\mathcal{F}_{new}$

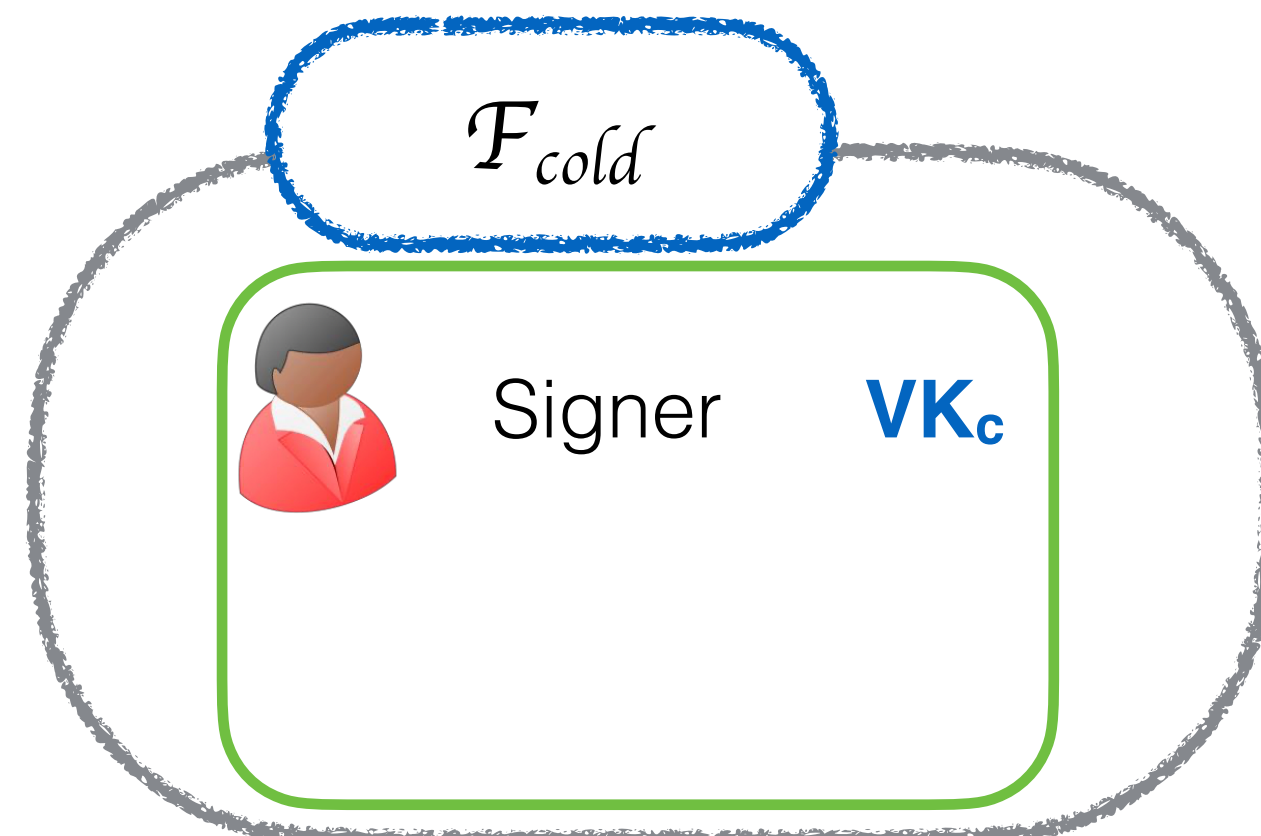


$VK_c$

$VK_{new}$

$M \leftarrow \{m_1, m_2\}$

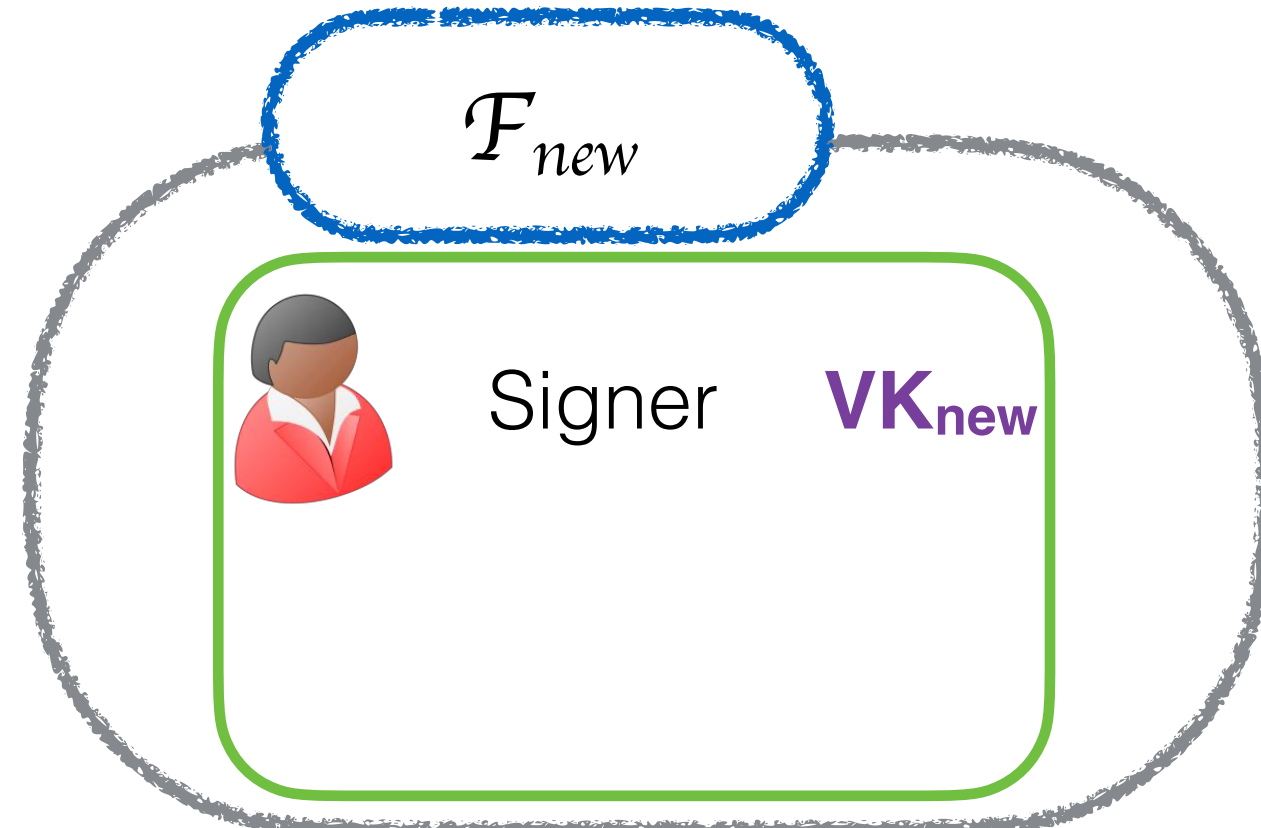
$h \leftarrow H(m_1 || m_2)$



$VK_c$



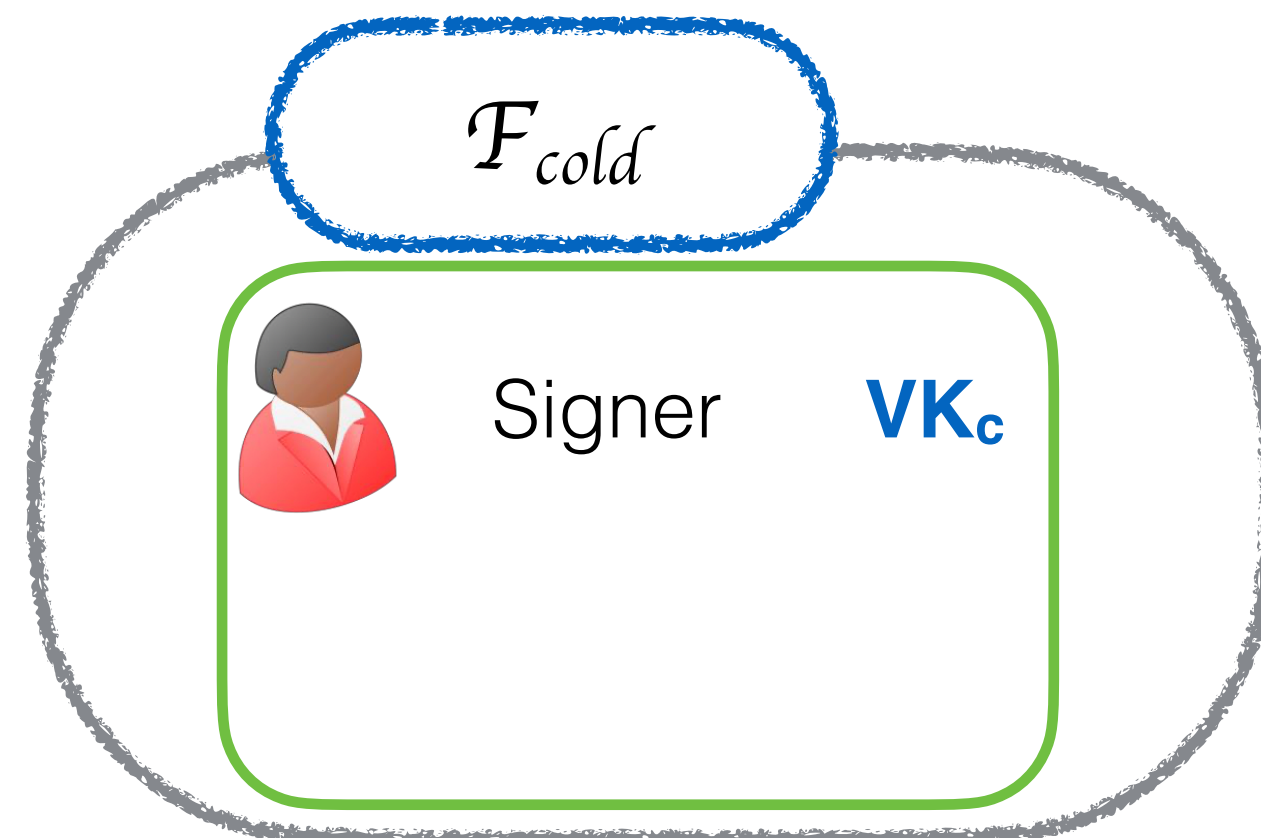
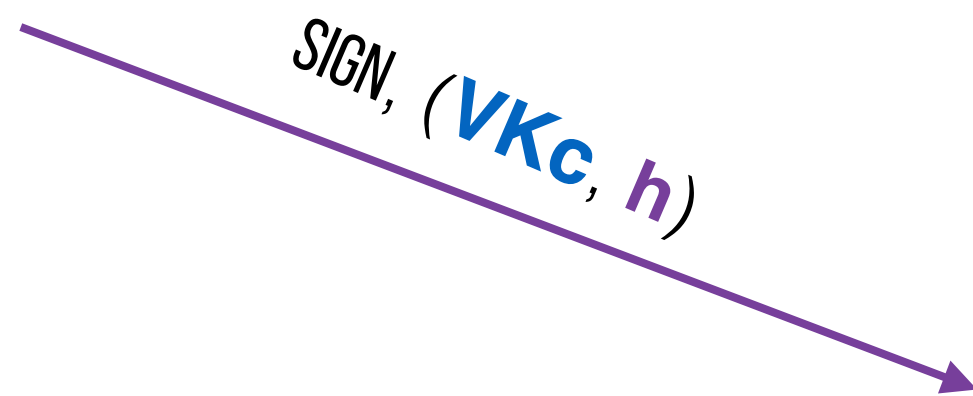
# Updatable signatures



UPDATE,  $F_{new}$



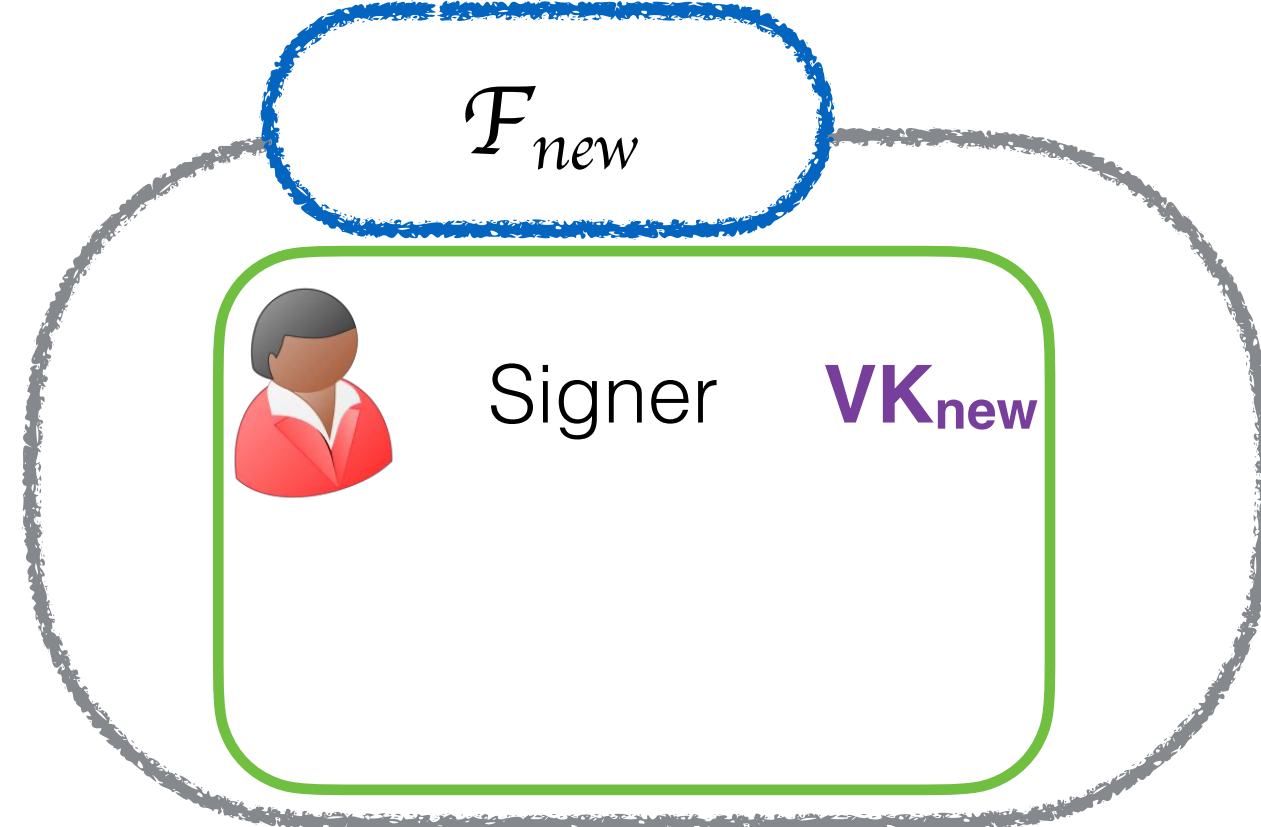
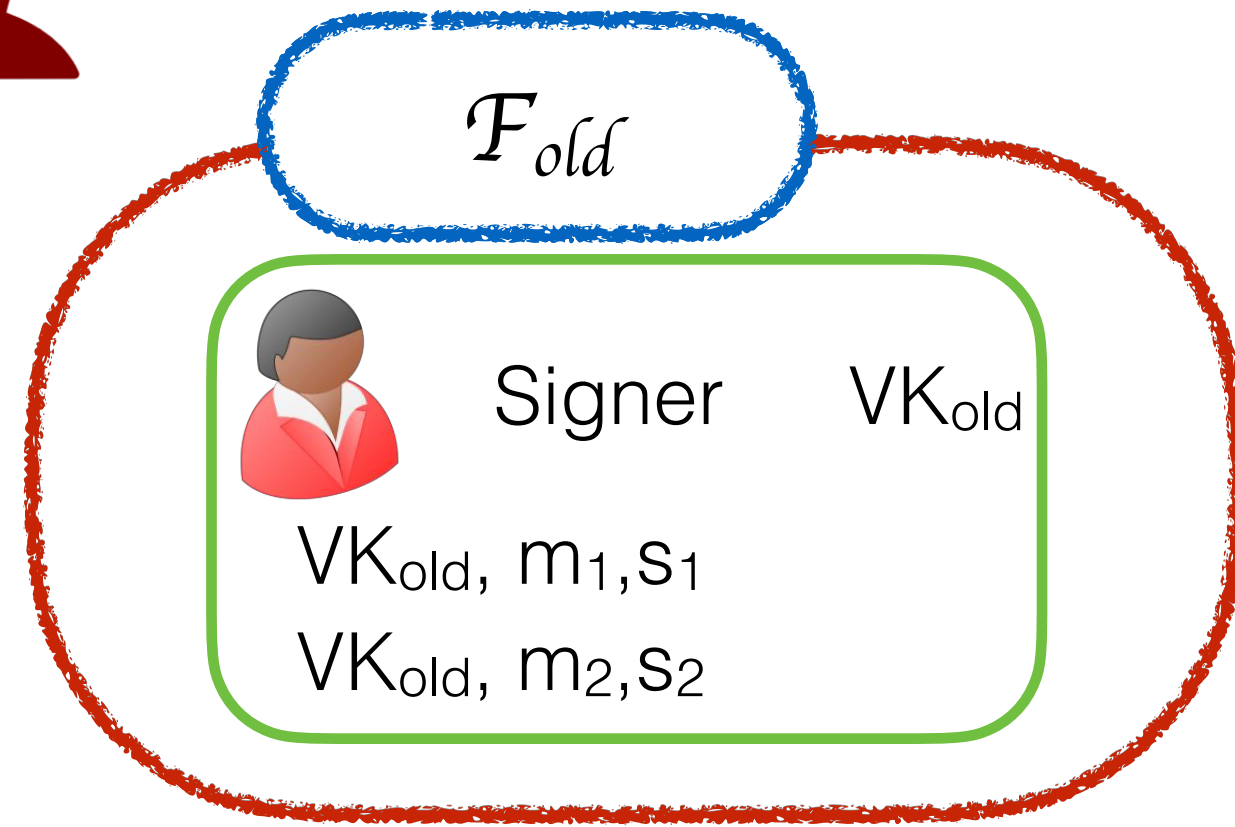
$VK_c$   
 $VK_{new}$   
 $M \leftarrow \{m_1, m_2\}$   
 $h \leftarrow H(m_1 || m_2)$



$VK_c$



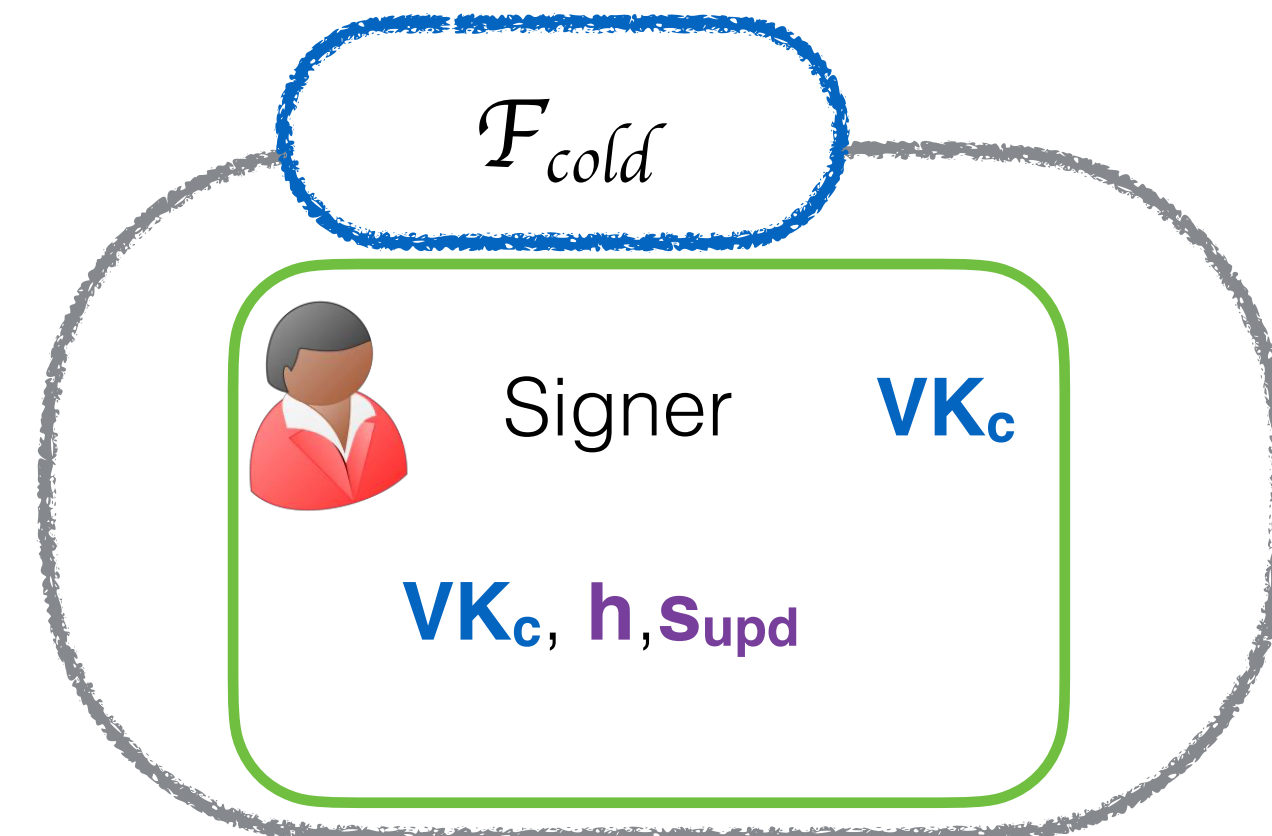
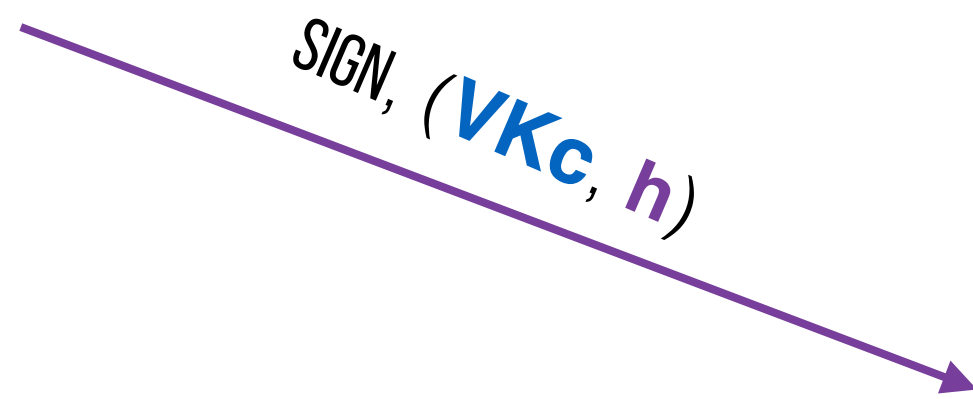
# Updatable signatures



UPDATE,  $F_{new}$



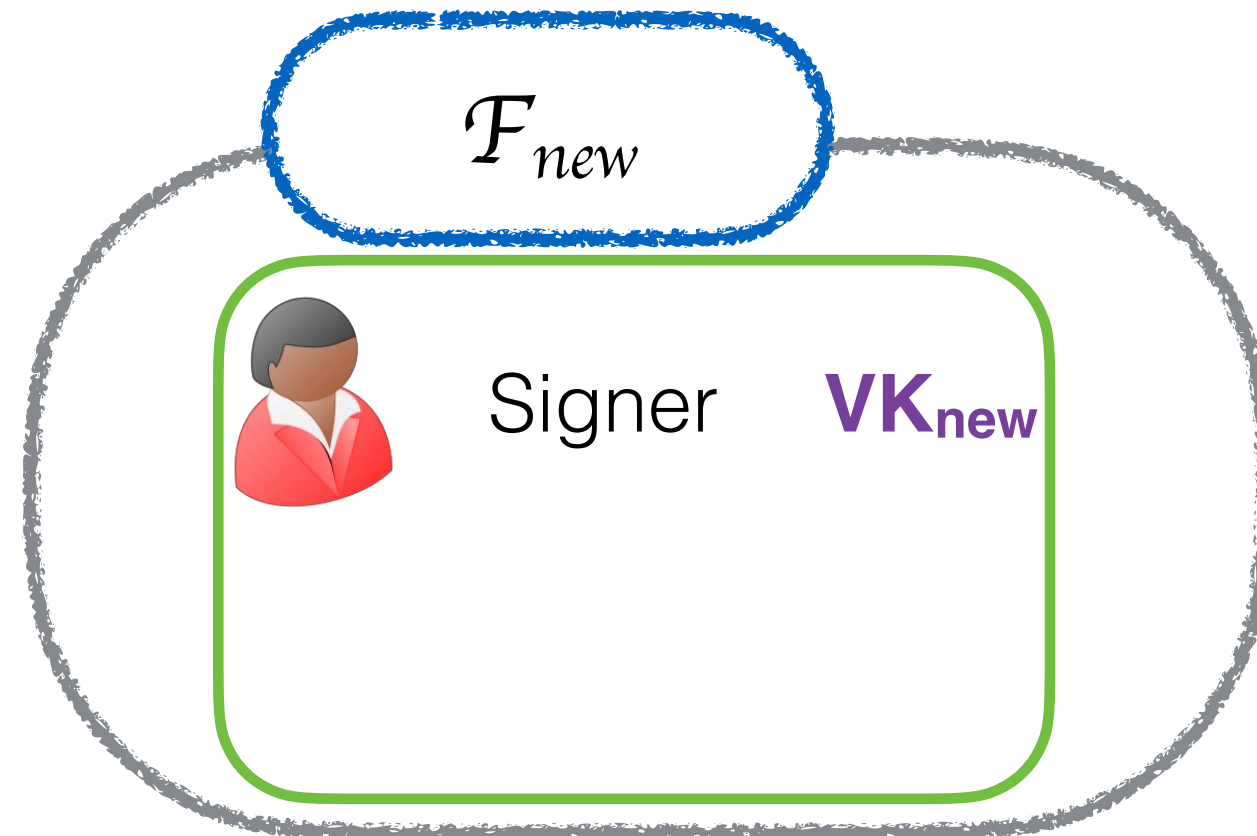
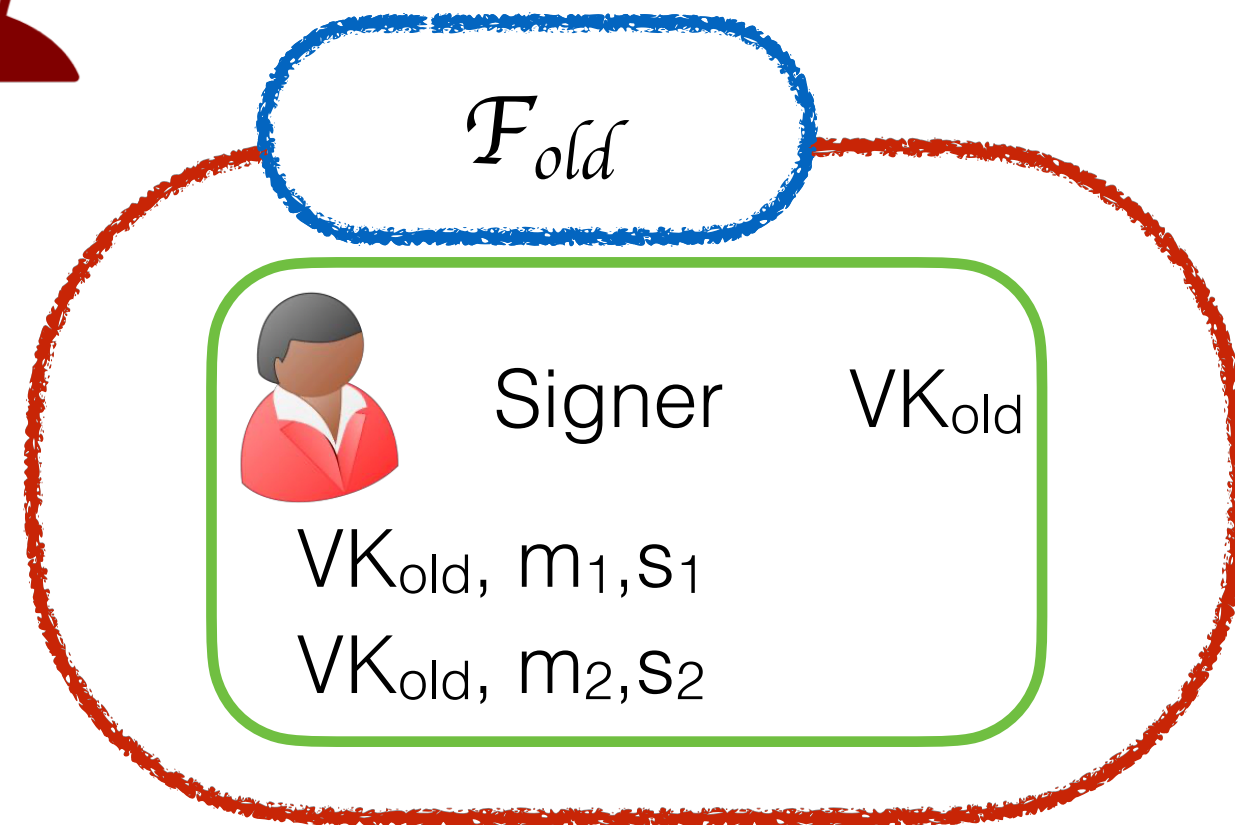
$VK_c$   
 $VK_{new}$   
 $M \leftarrow \{m_1, m_2\}$   
 $h \leftarrow H(m_1 || m_2)$



$VK_c$

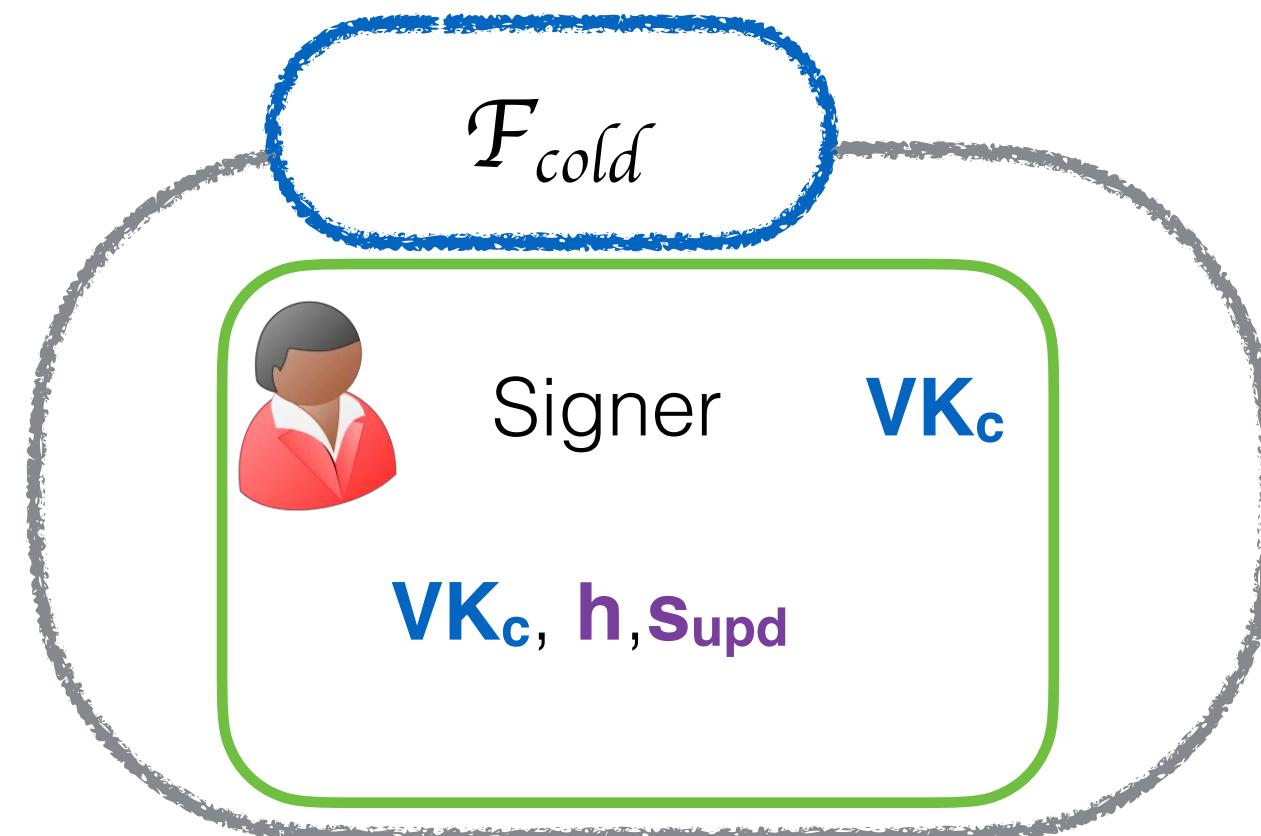
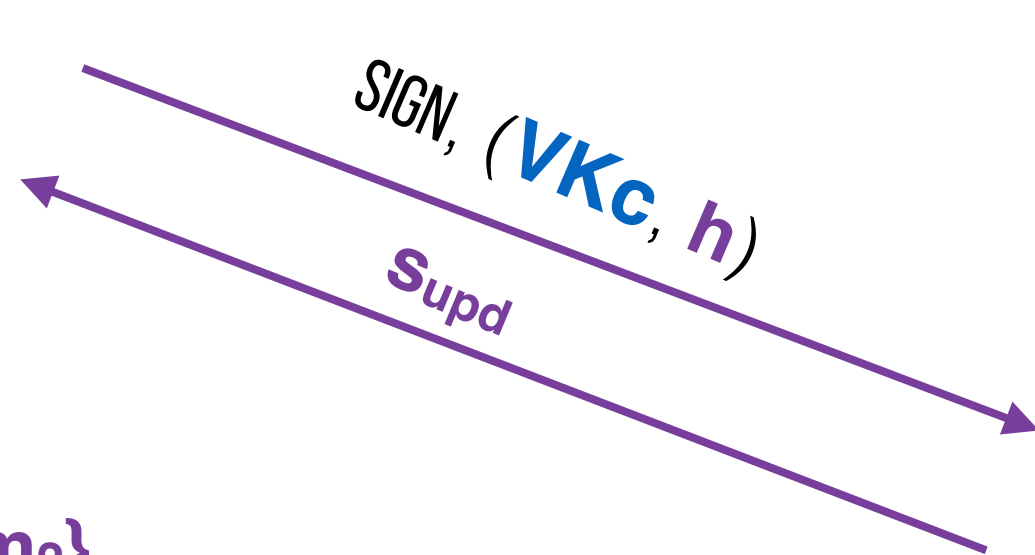


# Updatable signatures



UPDATE,  $\mathcal{F}_{new}$

  
 $VK_c$   
 $VK_{new}$   
 $M \leftarrow \{m_1, m_2\}$   
 $h \leftarrow H(m_1 || m_2)$

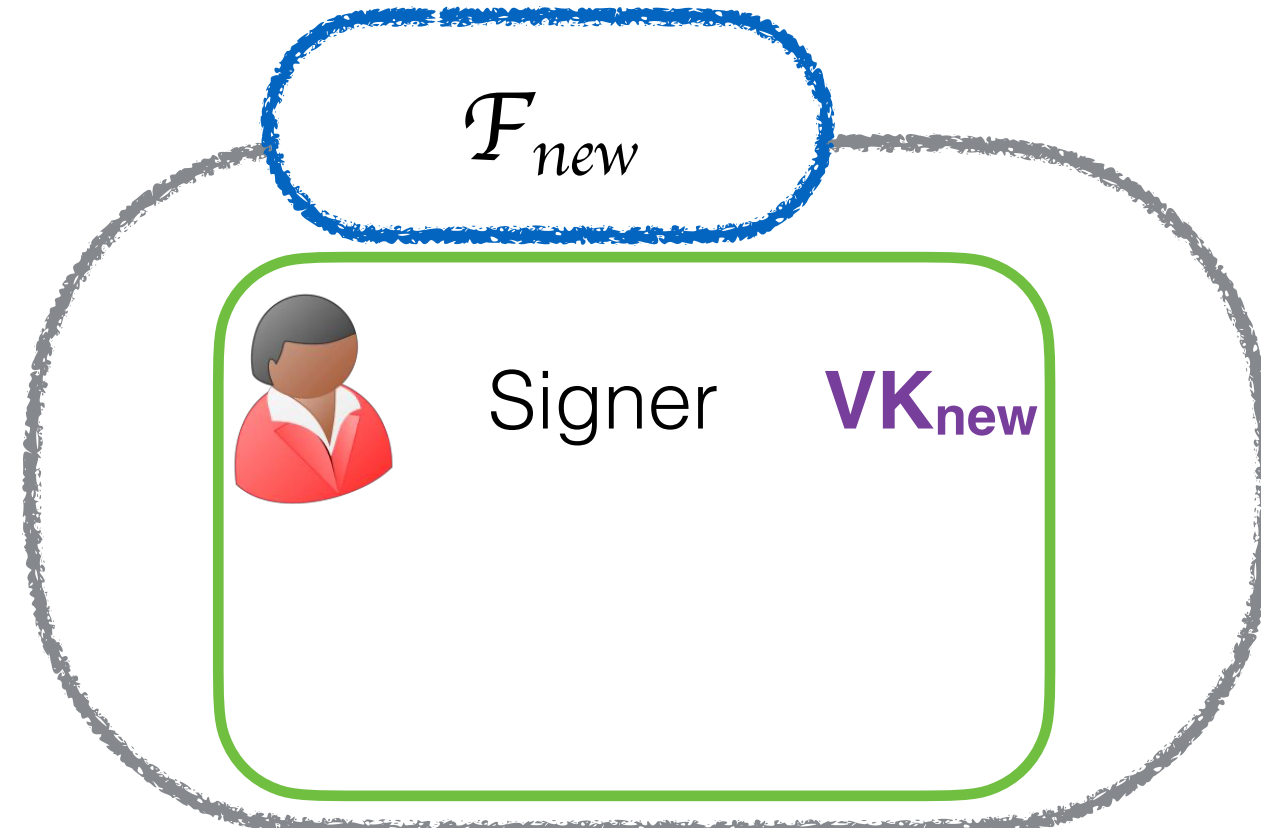


  
 $VK_c$






# Updatable signatures



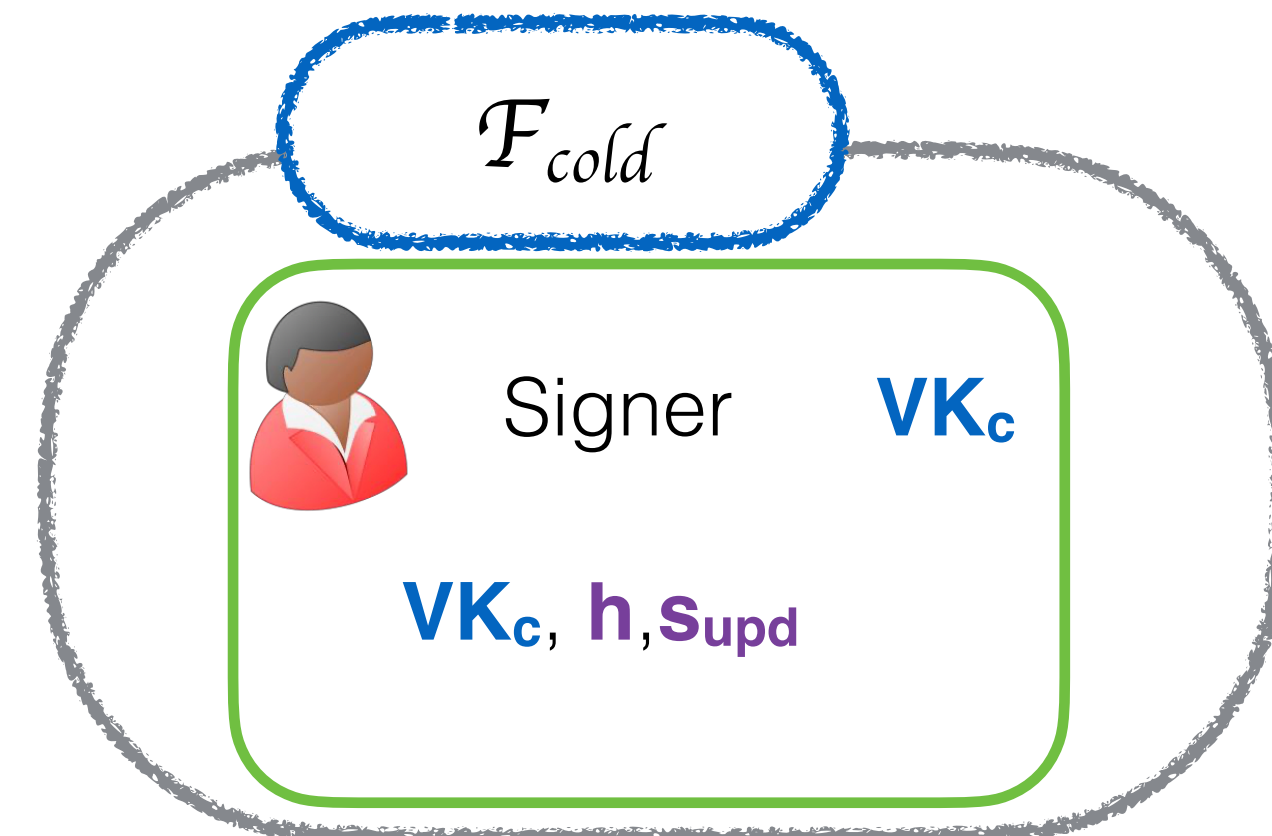
UPDATE,  $F_{new}$

  
 $VK_c$   
 $VK_{new}$   
 $M \leftarrow \{m_1, m_2\}$   
 $h \leftarrow H(m_1 || m_2)$

$VK_{new}, M, Supd$

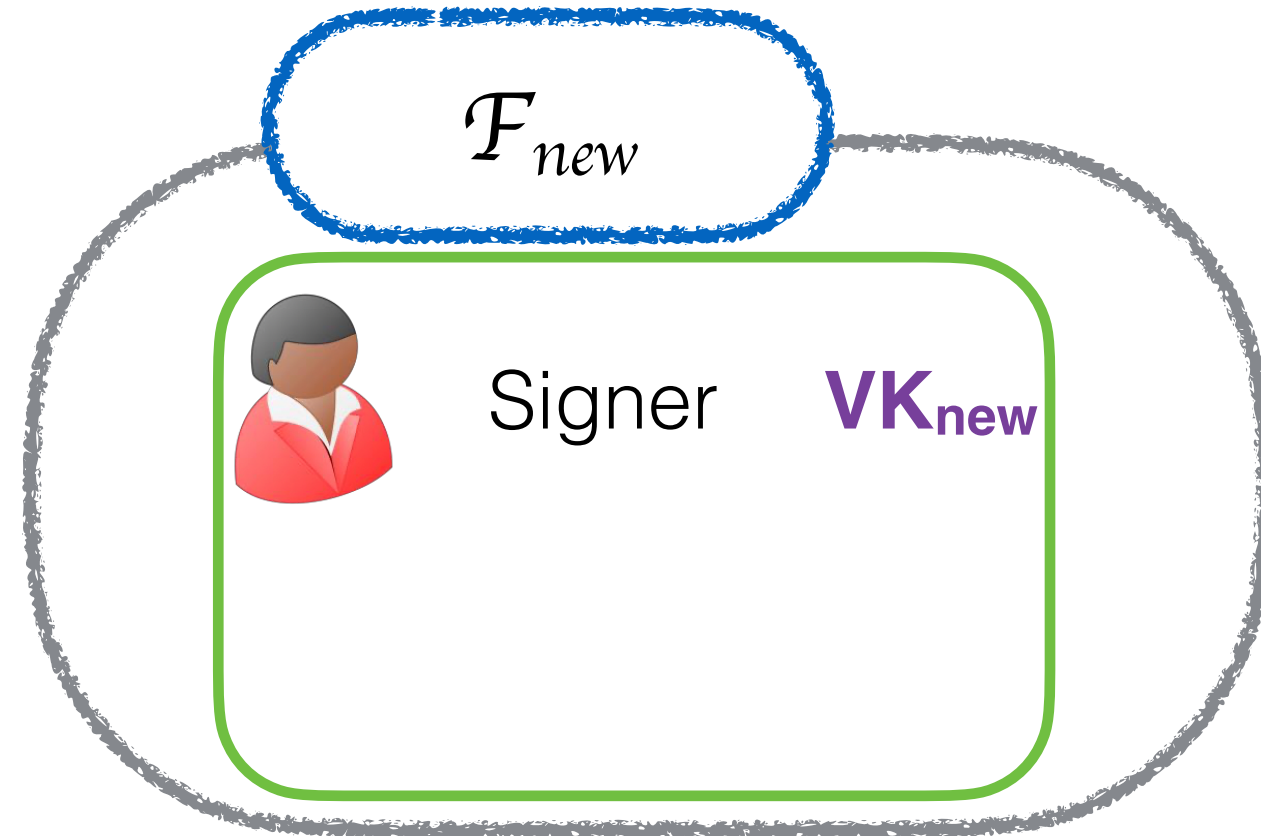
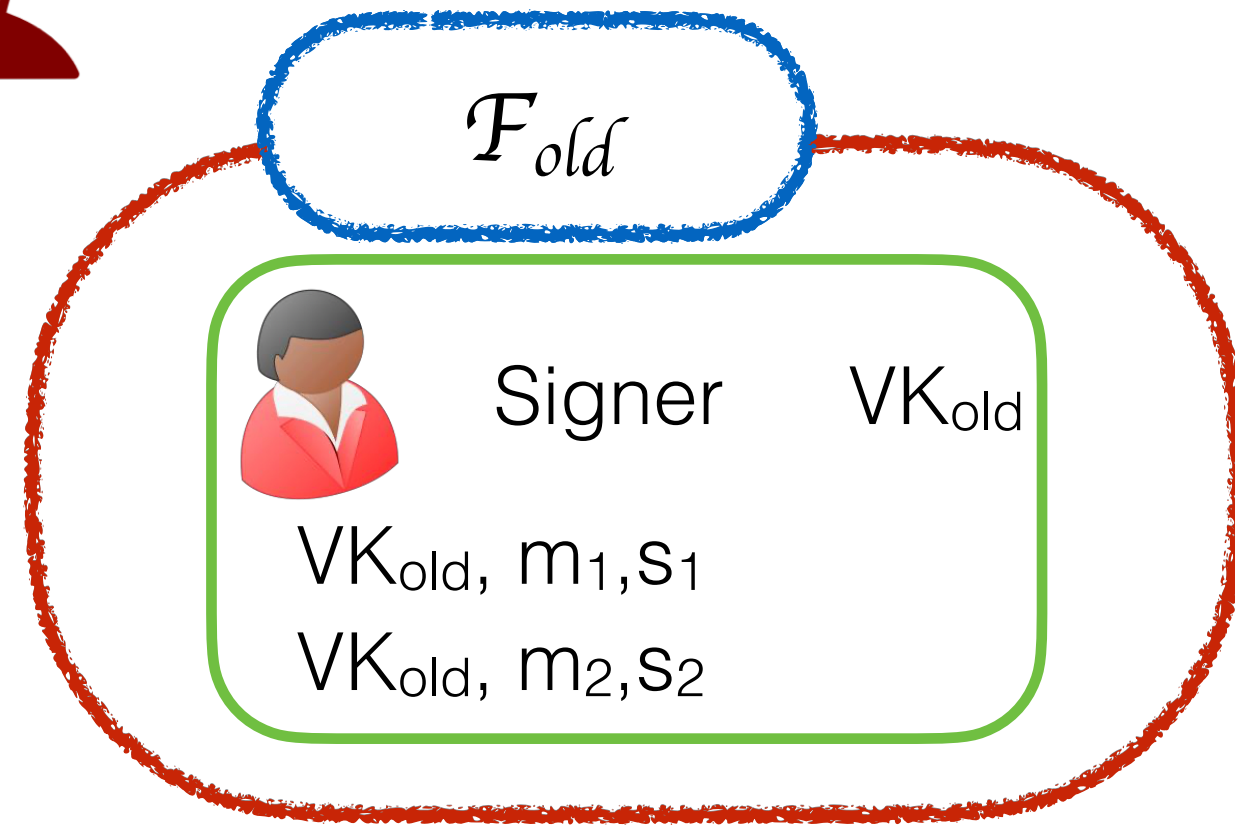
  
 $VK_c$

$SIGN, (VK_c, h)$   
 $Supd$





# Updatable signatures



UPDATE,  $\mathcal{F}_{new}$



$VK_c$

$VK_{new}$

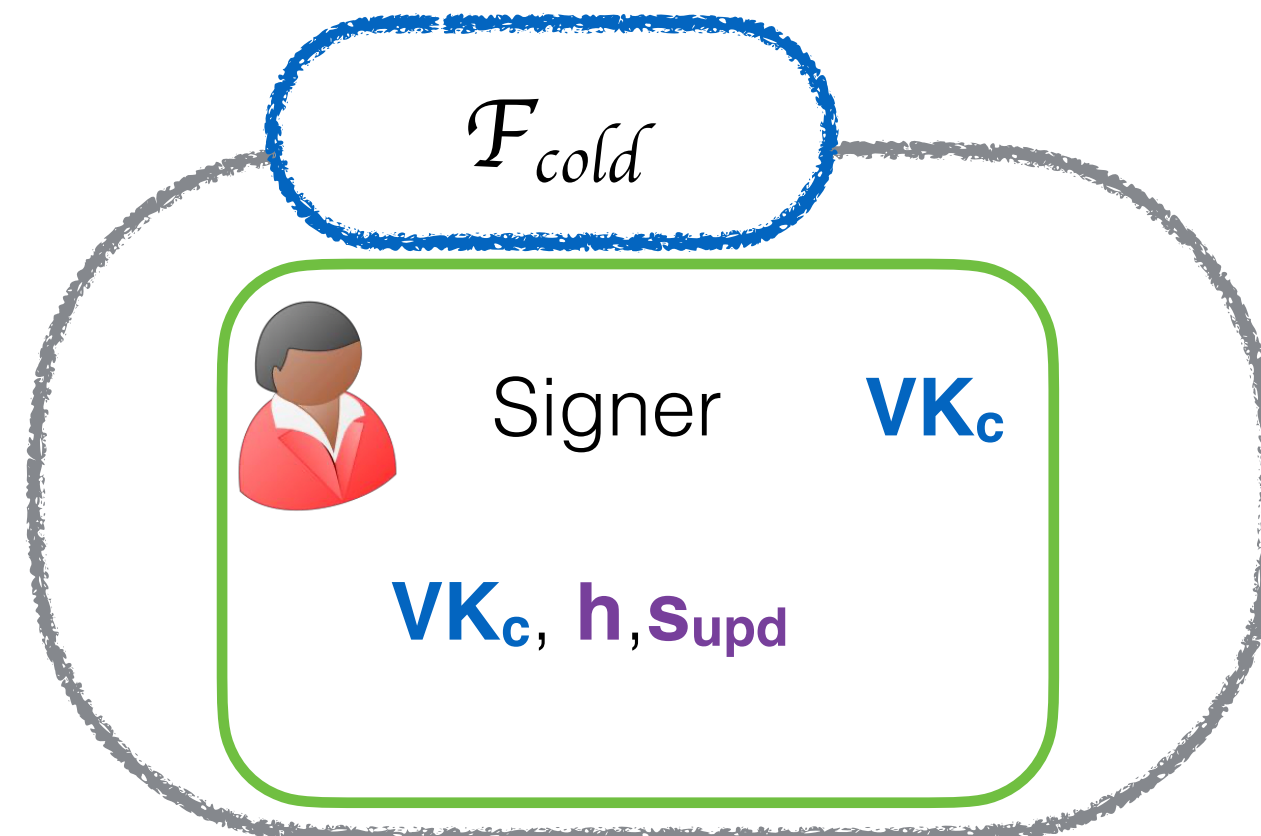
$M \leftarrow \{m_1, m_2\}$

$h \leftarrow H(m_1 || m_2)$

$VK_{new}, M, Supd$

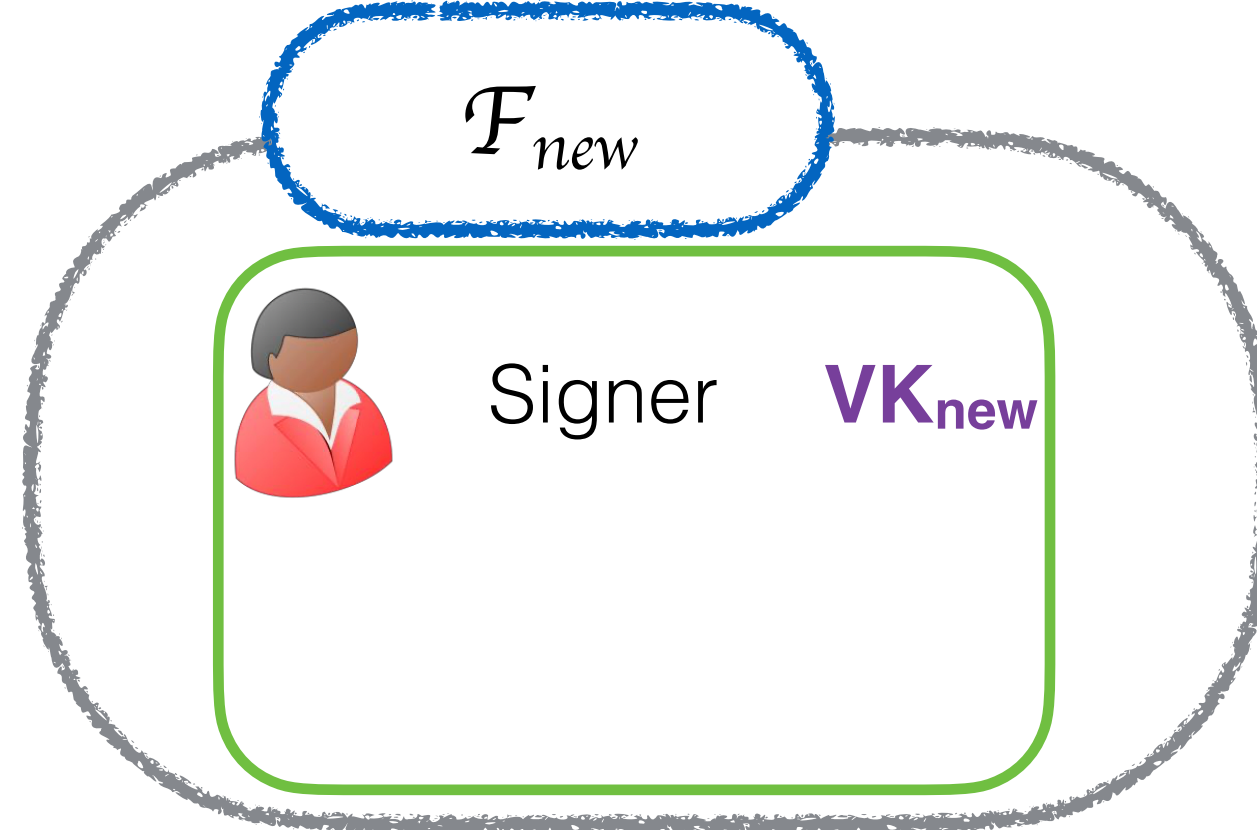
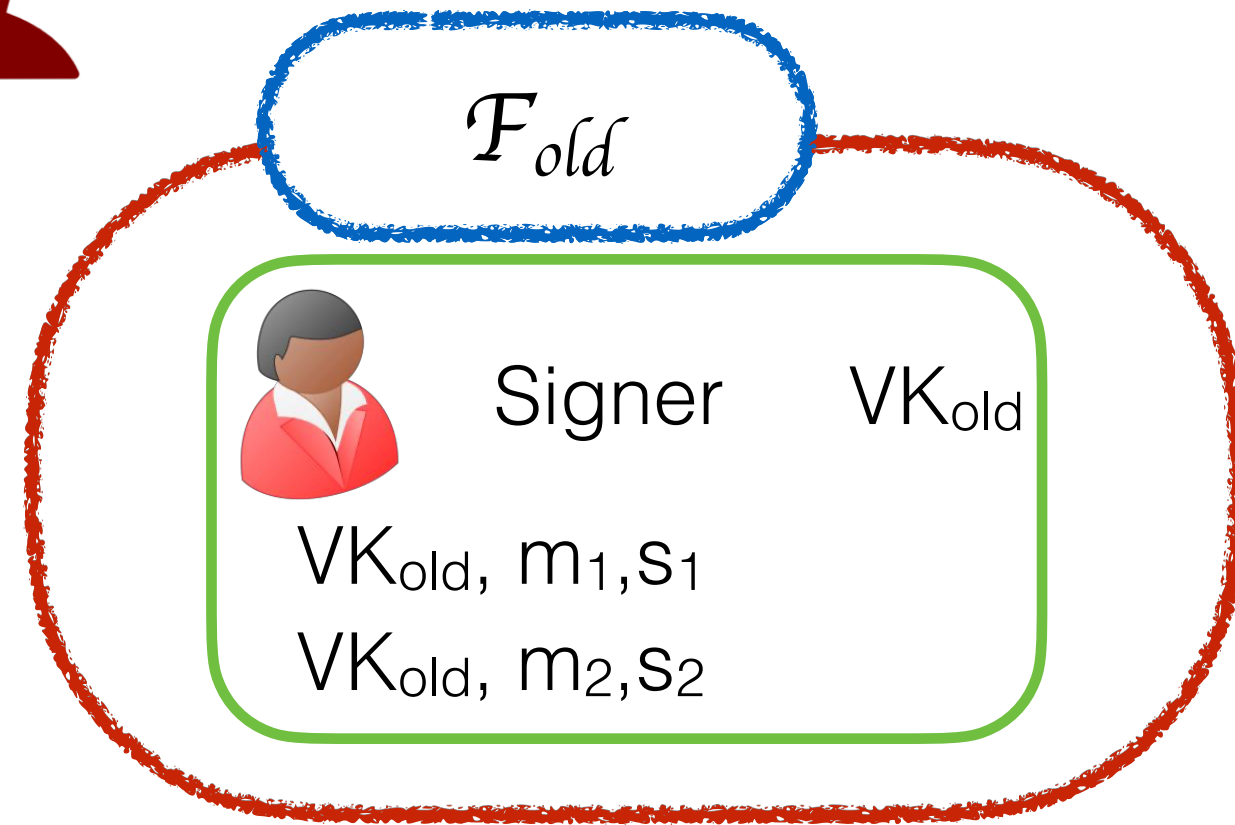


$VK_c$





# Updatable signatures



SIGN,  $m_3$



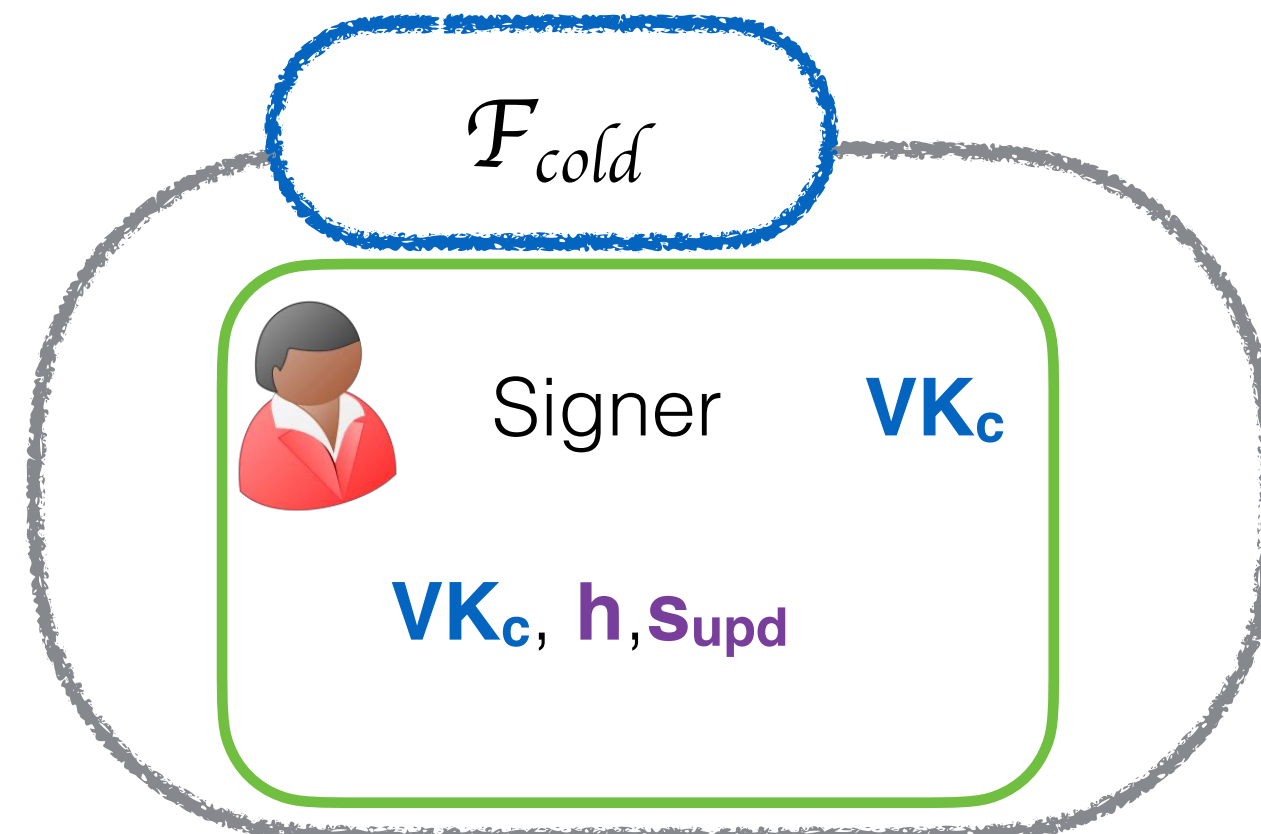
$VK_c$

$VK_{new}$

$M \leftarrow \{m_1, m_2\}$

$h \leftarrow H(m_1 || m_2)$

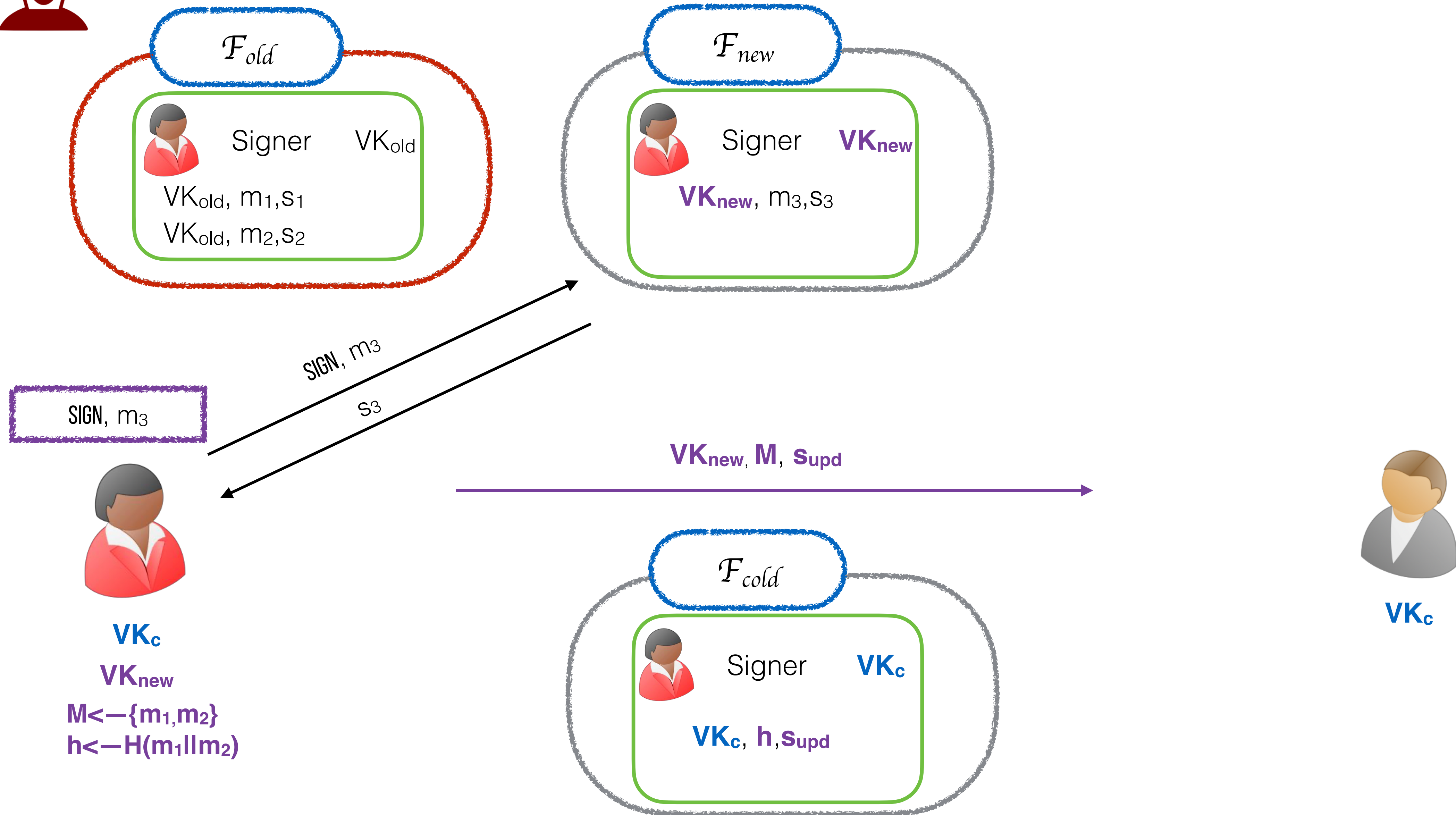
$VK_{new}, M, Supd$



$VK_c$

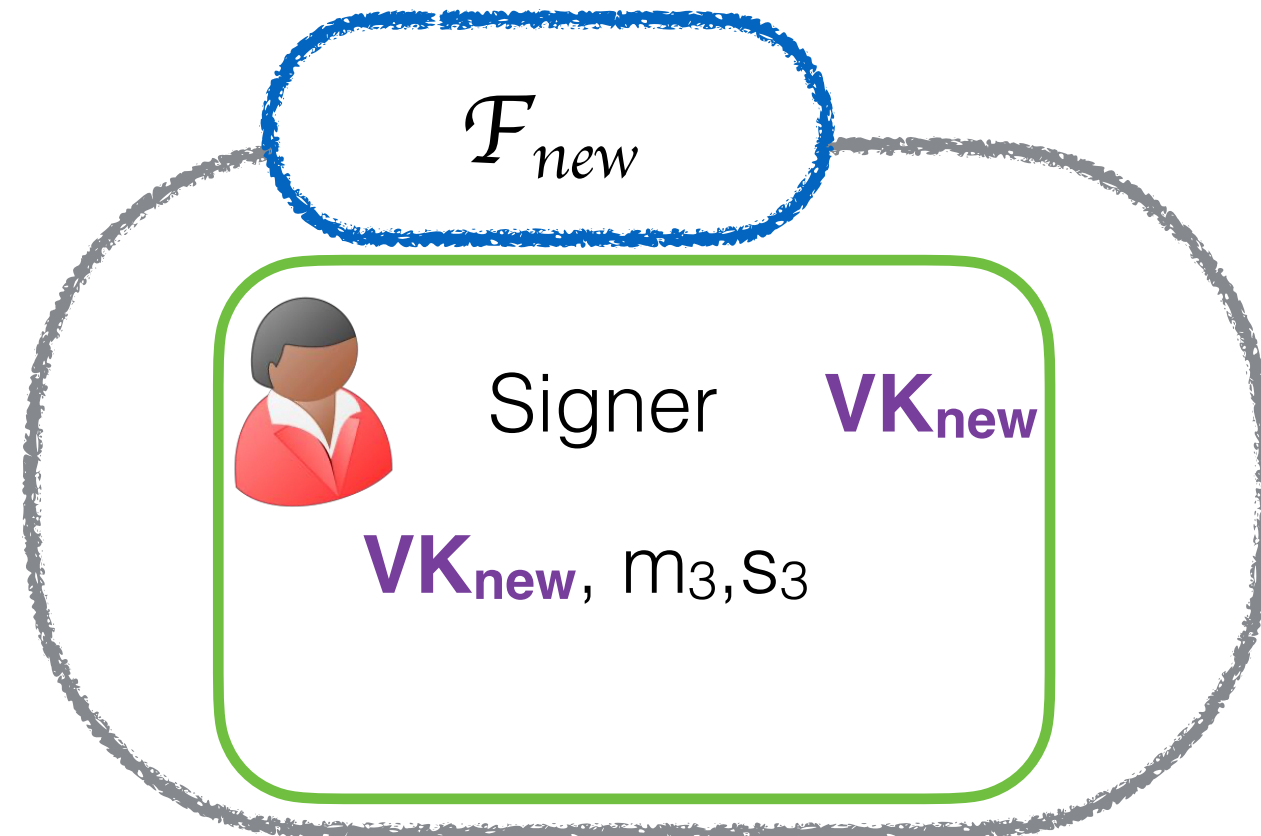
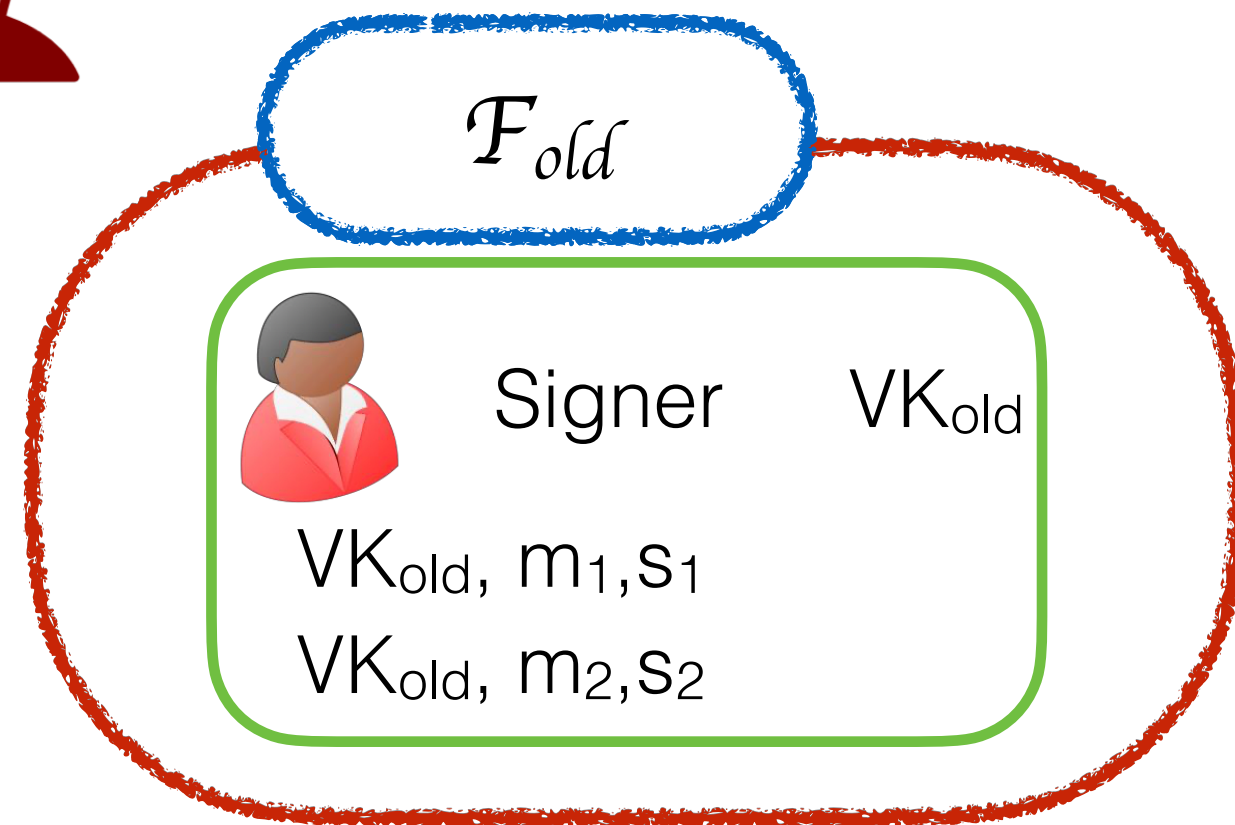


# Updatable signatures





# Updatable signatures



SIGN,  $m_3$



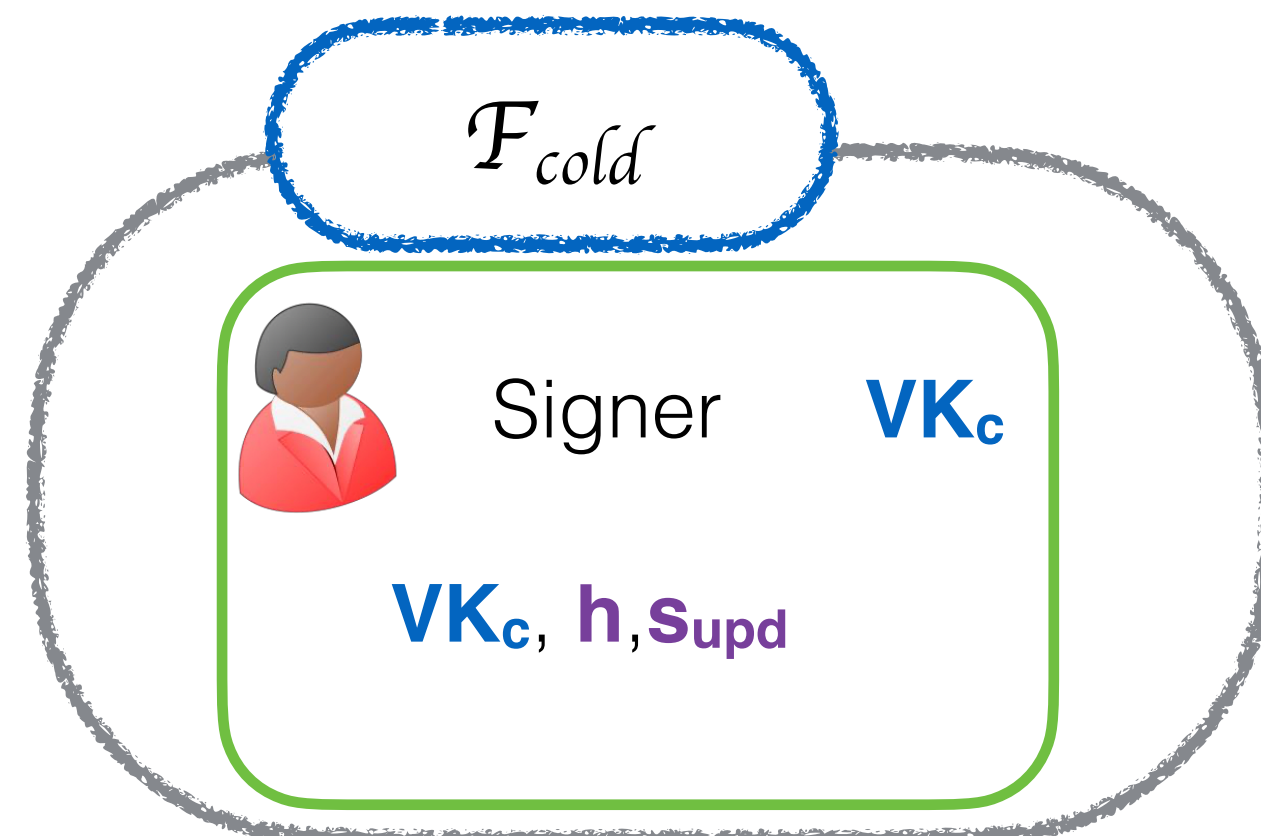
$VK_c$

$VK_{new}$

$M \leftarrow \{m_1, m_2\}$

$h \leftarrow H(m_1 || m_2)$

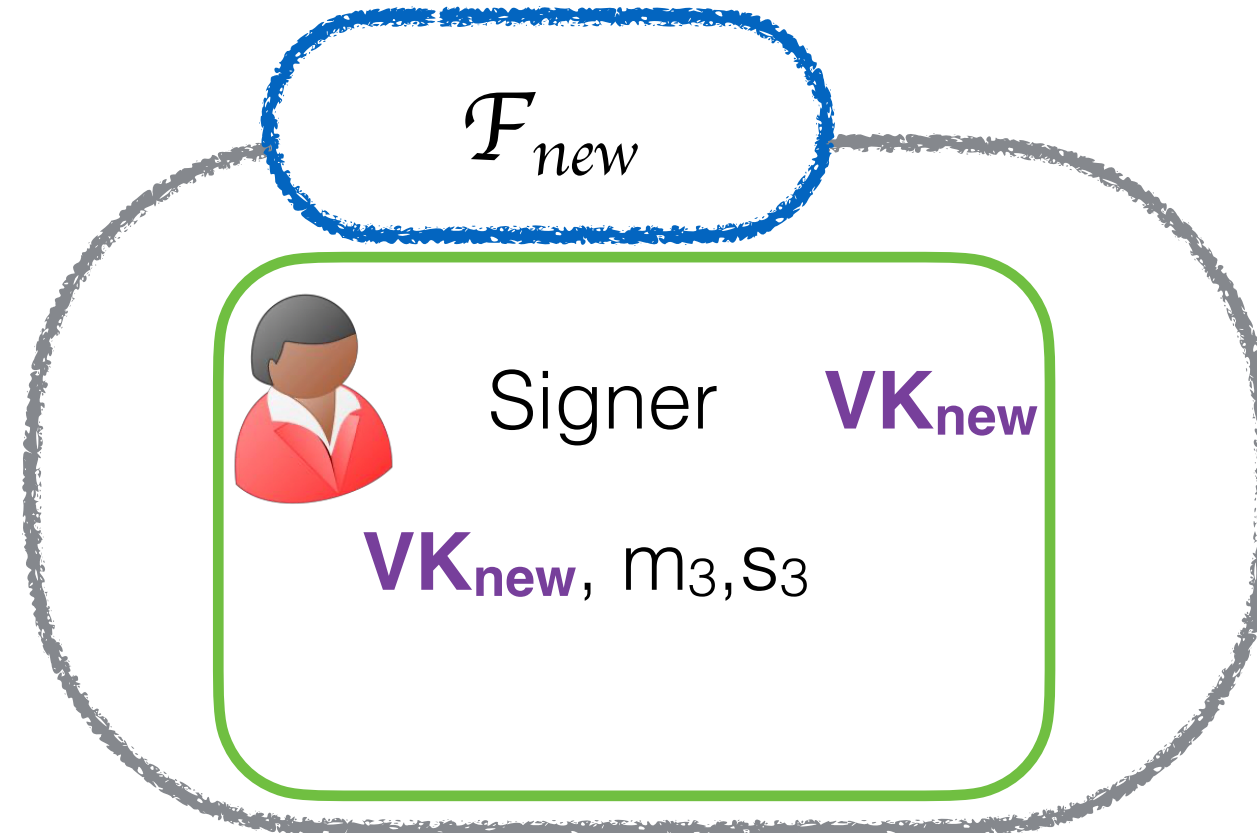
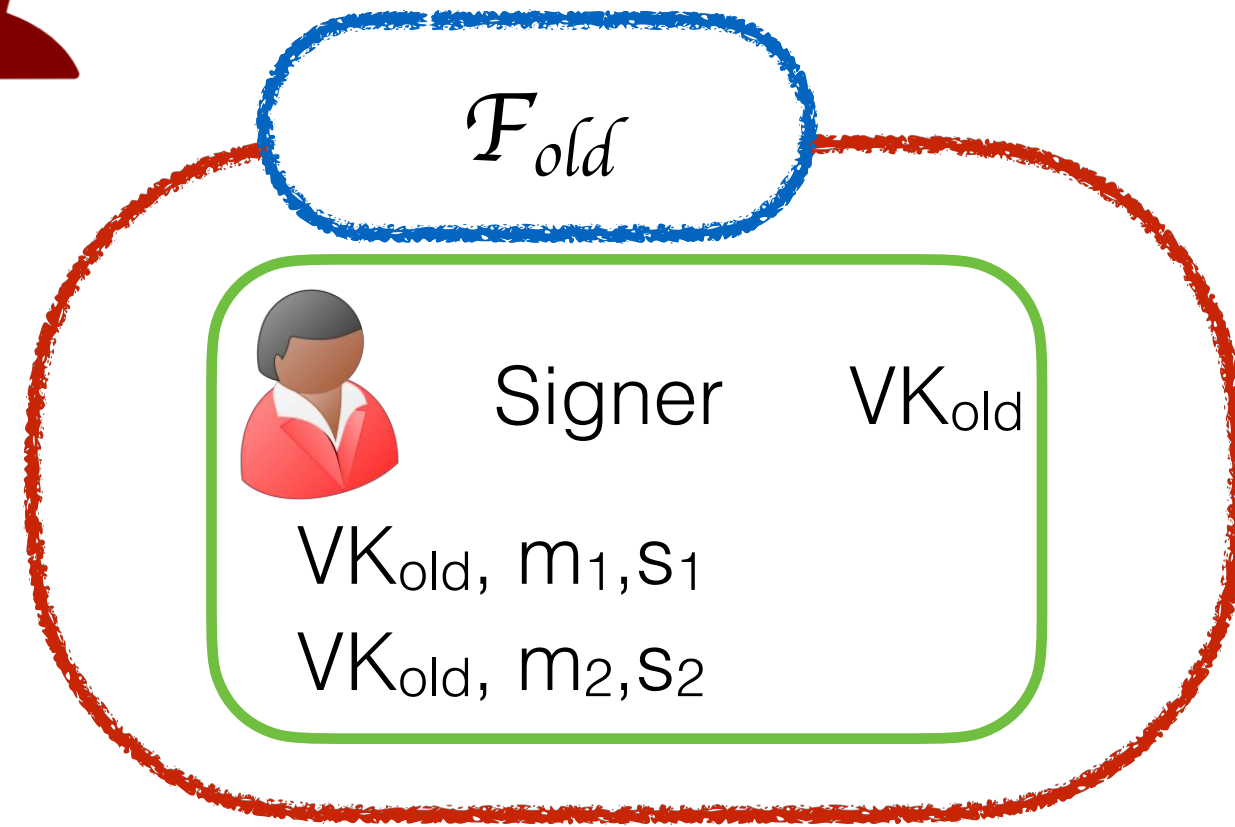
$VK_{new}, M, Supd$



$VK_c$



# Updatable signatures



SIGN,  $m_3$



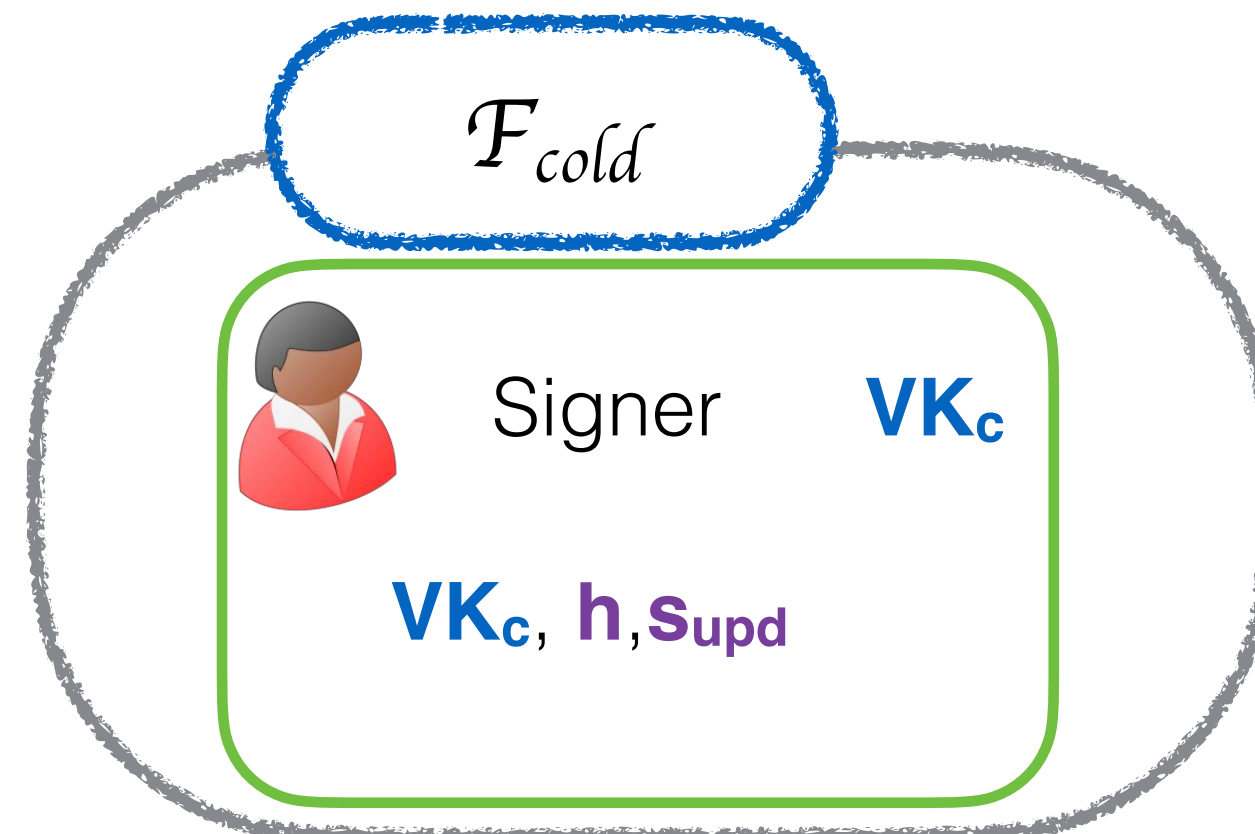
$VK_c$

$VK_{new}$

$M \leftarrow \{m_1, m_2\}$

$h \leftarrow H(m_1 || m_2)$

$VK_{new}, M, Supd$



UPDATE,  $\mathcal{F}_{new}$

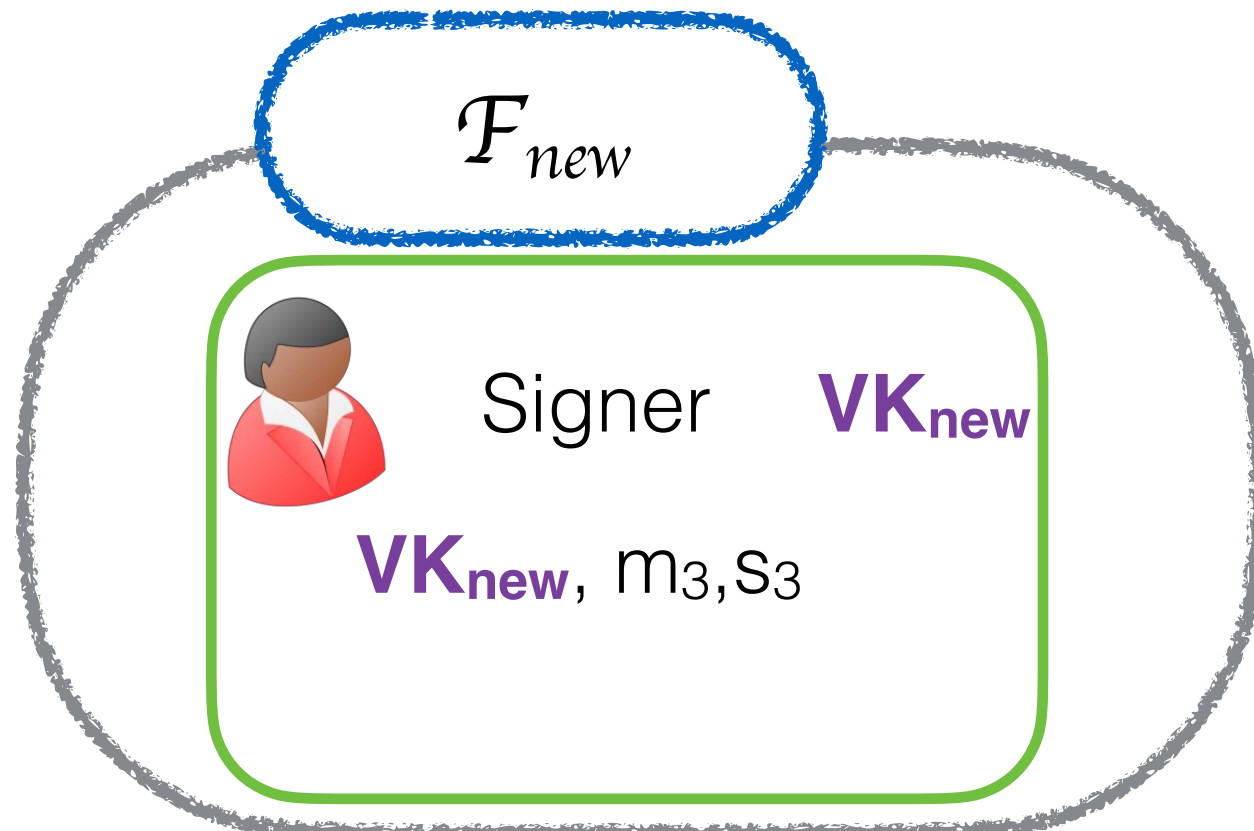
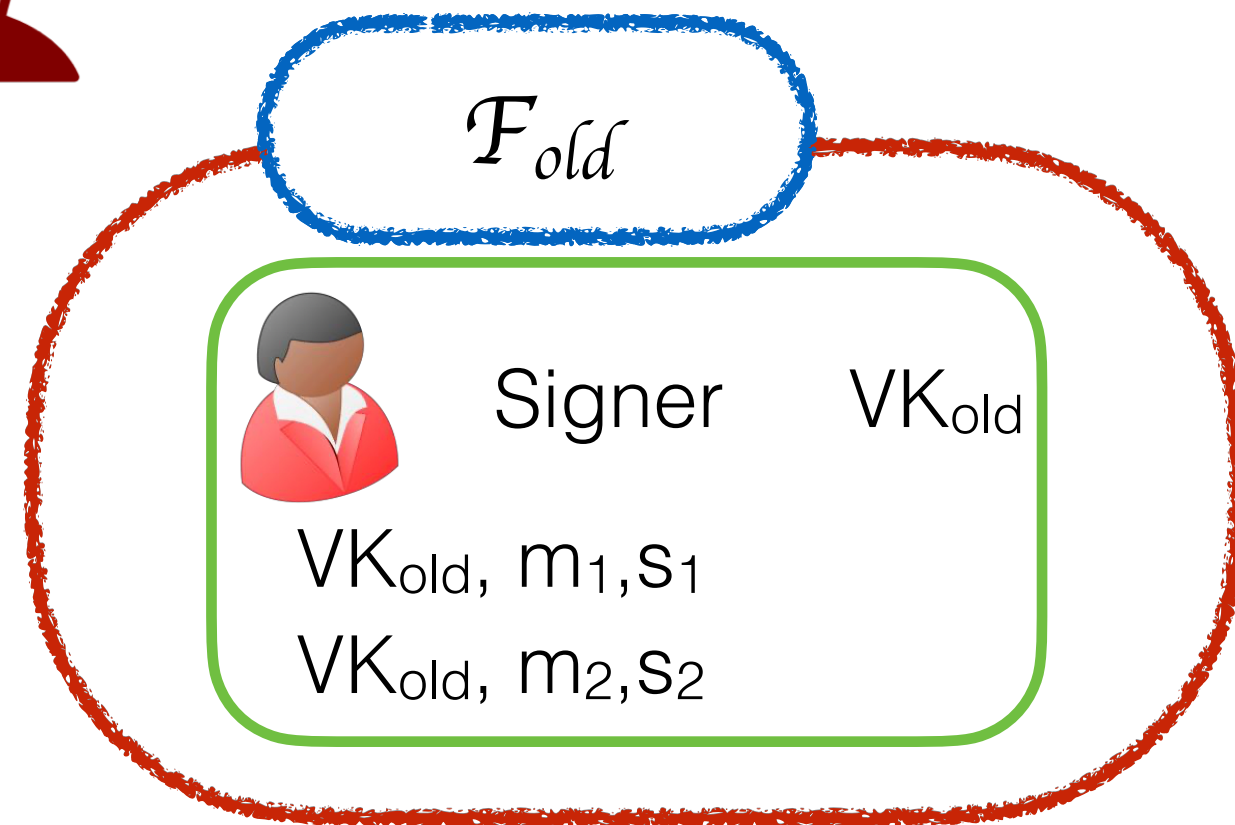


$VK_c$

$VK_{new}, M, Supd$




# Updatable signatures



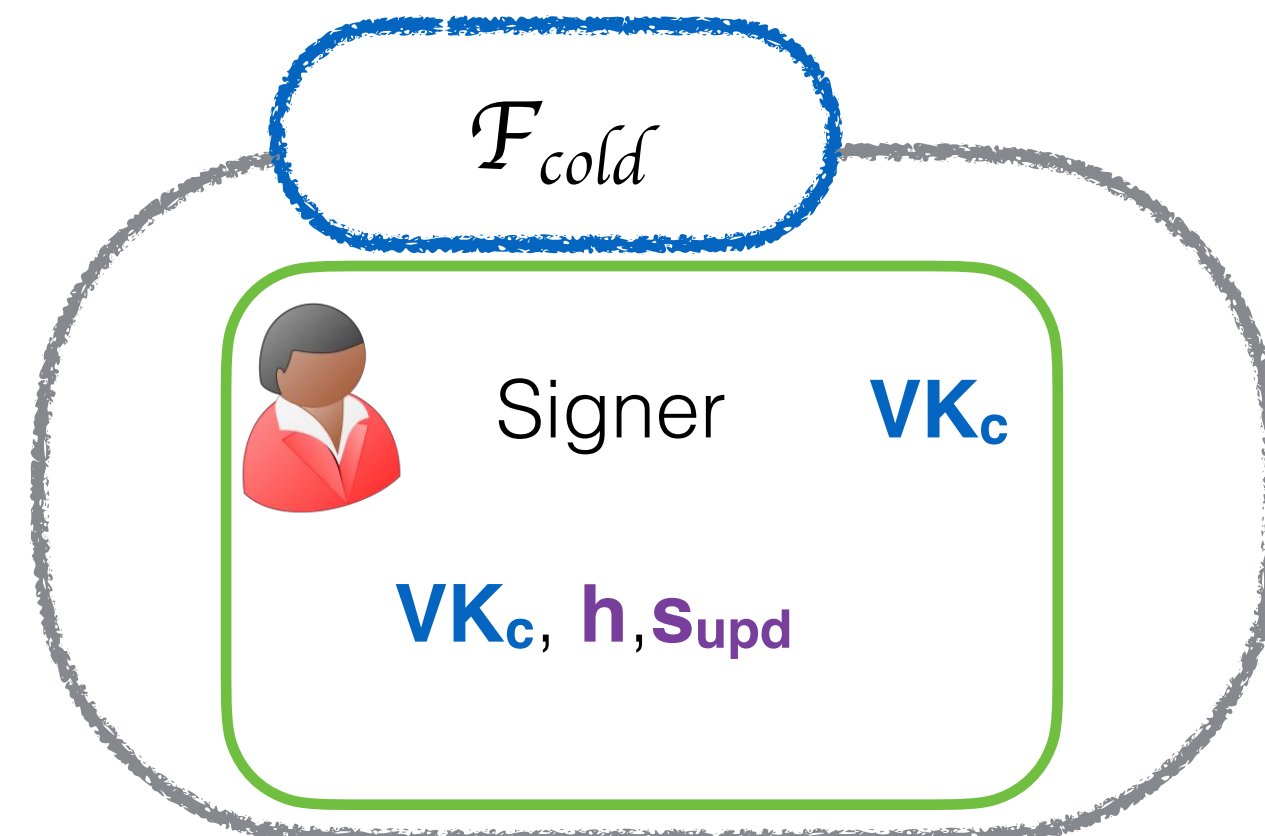
SIGN,  $m_3$

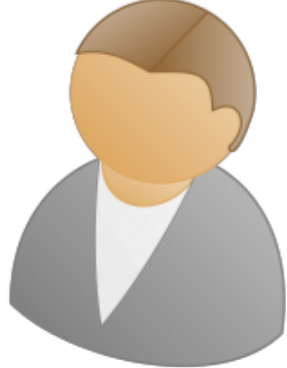
UPDATE,  $\mathcal{F}_{new}$



$VK_c$   
 $VK_{new}$   
 $M \leftarrow \{m_1, m_2\}$   
 $h \leftarrow H(m_1 || m_2)$

$VK_{new}, M, Supd$



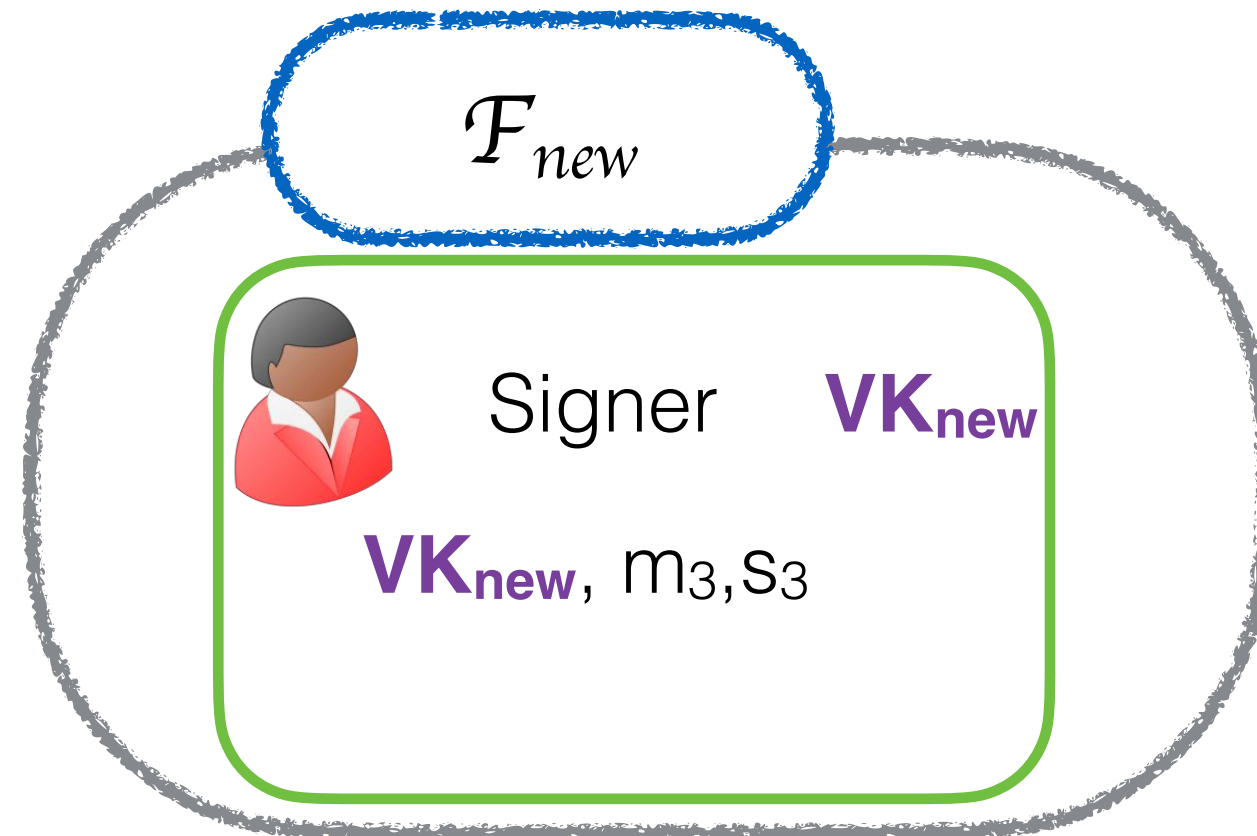
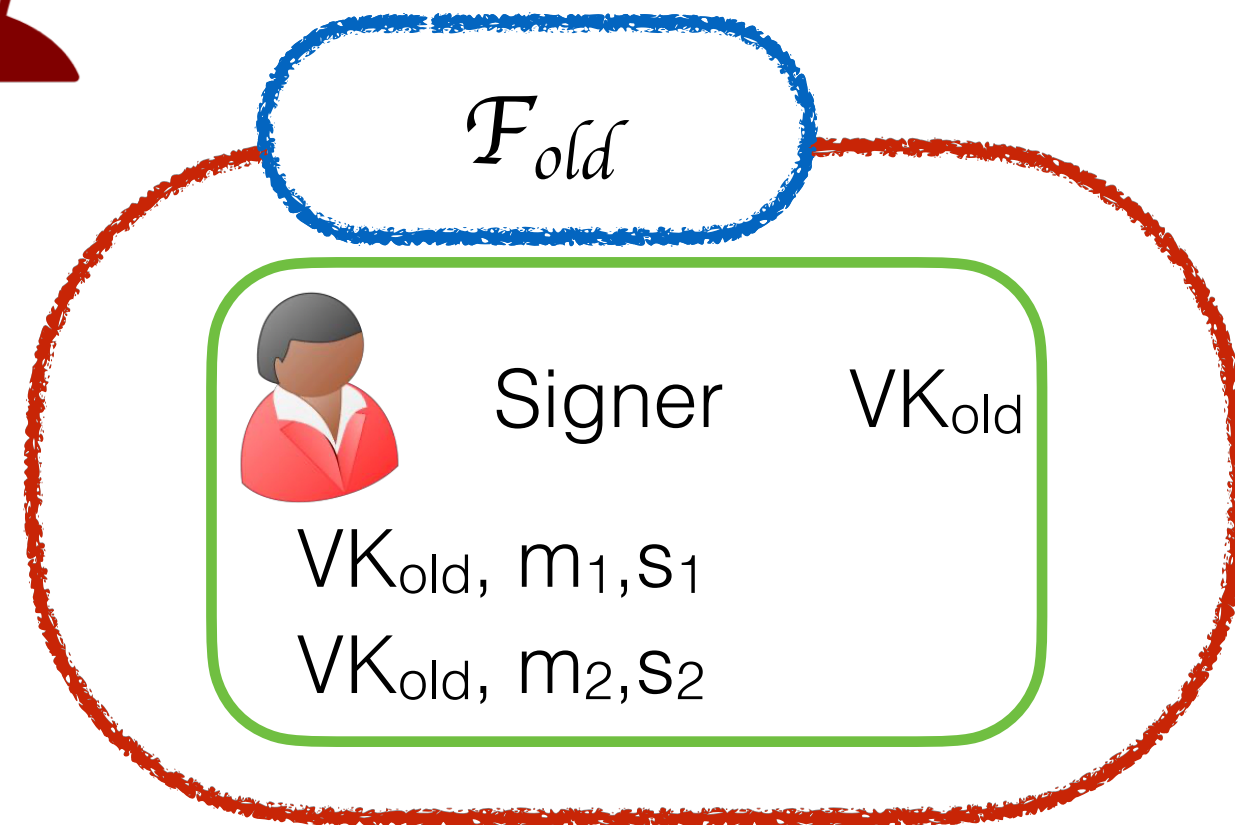


$VK_c$   
 $VK_{new}, M, Supd$

VERIFY,  $VK_c, H(M), Supd$



# Updatable signatures



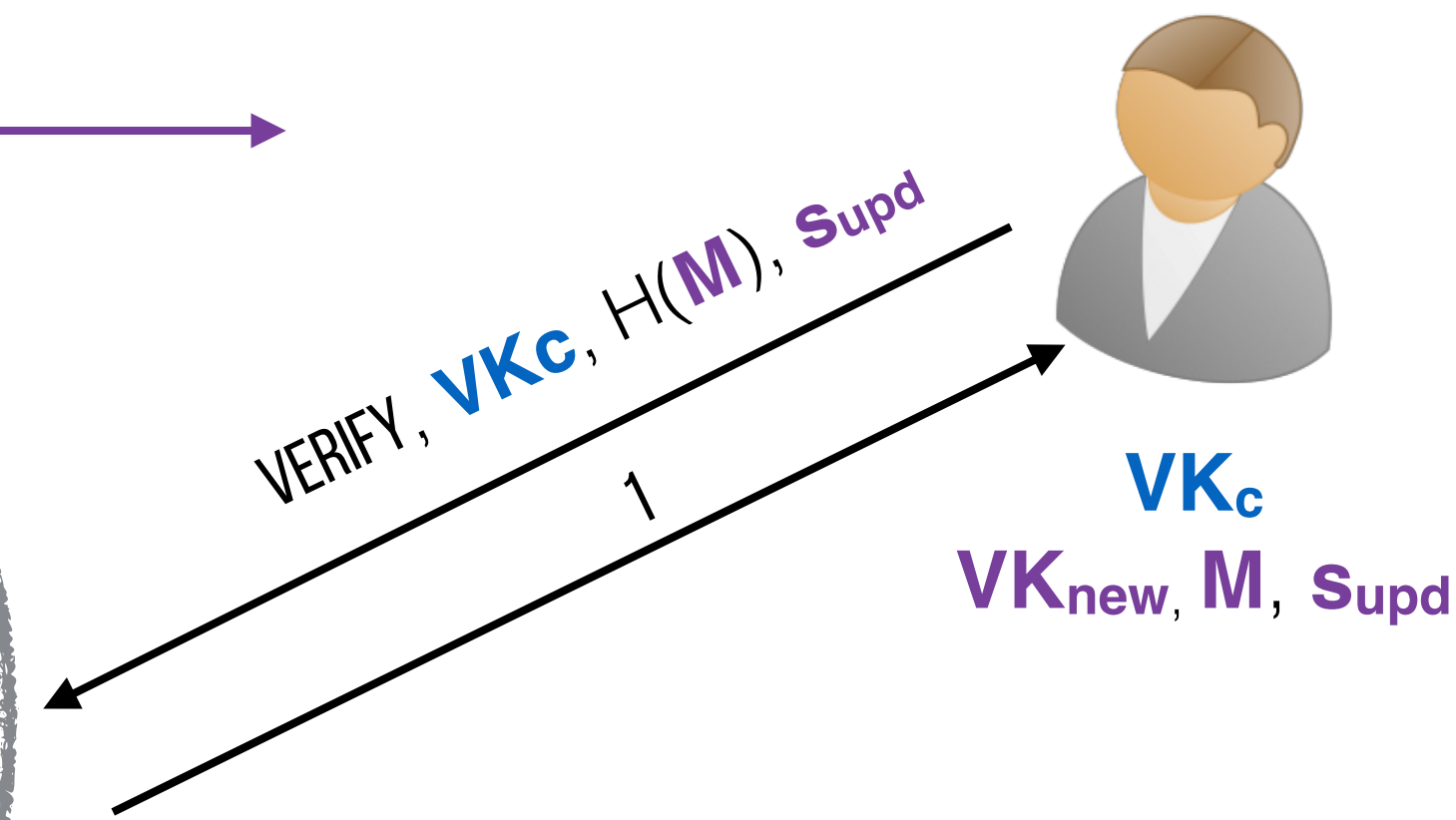
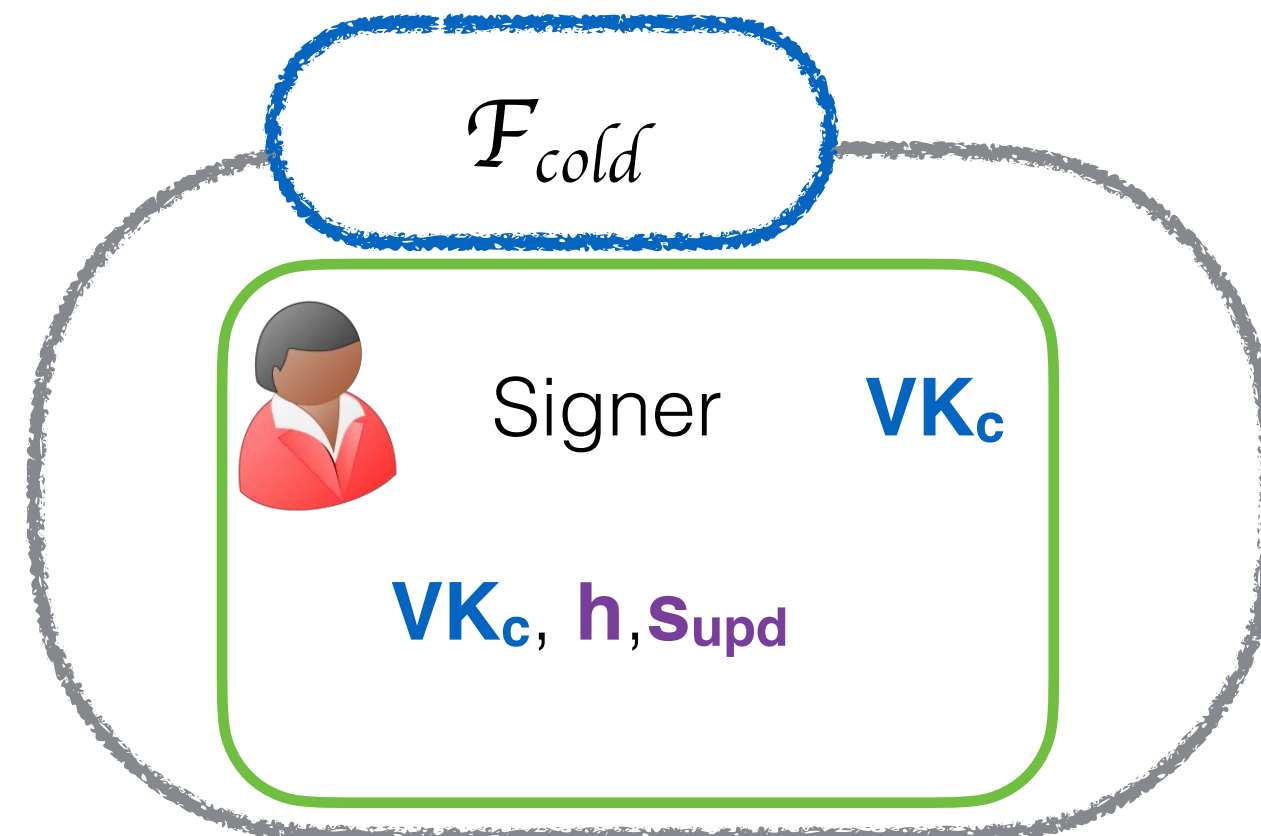
SIGN,  $m_3$

UPDATE,  $\mathcal{F}_{new}$



$VK_c$   
 $VK_{new}$   
 $M \leftarrow \{m_1, m_2\}$   
 $h \leftarrow H(m_1 || m_2)$

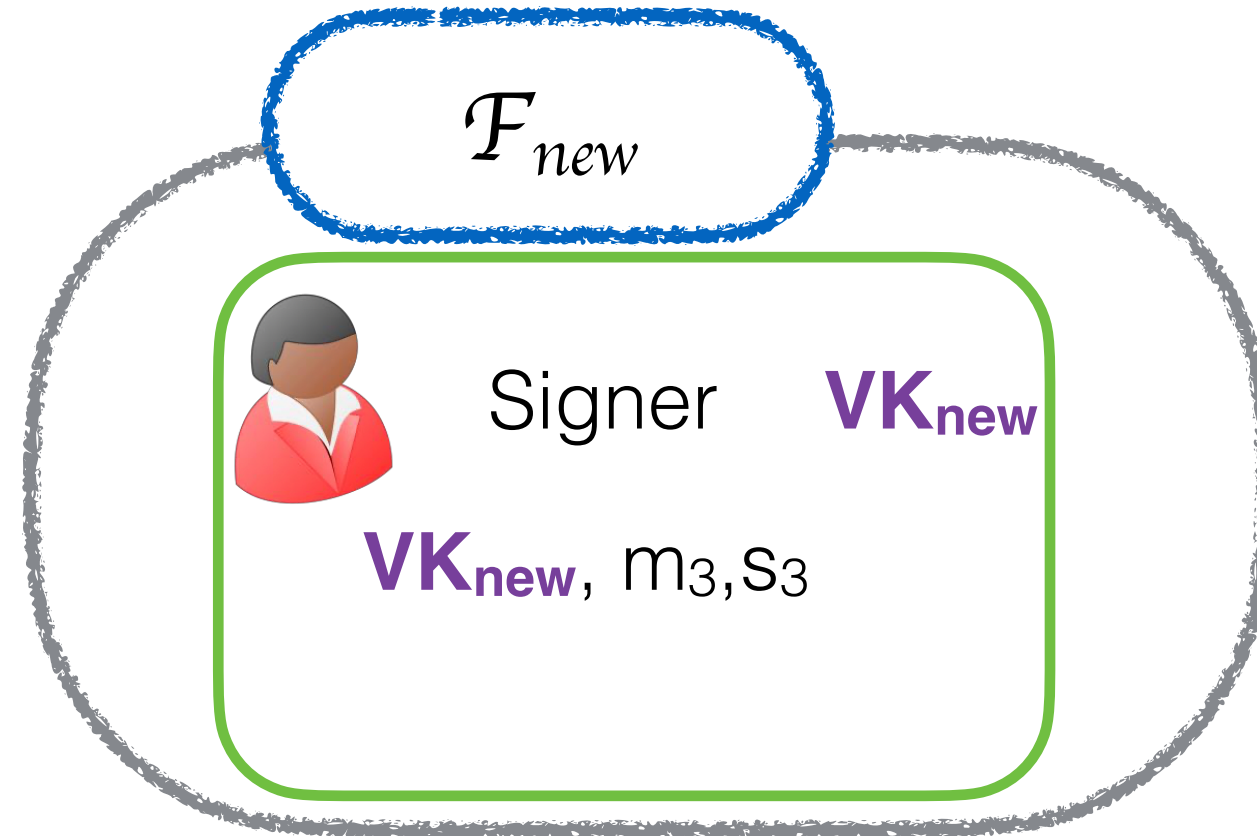
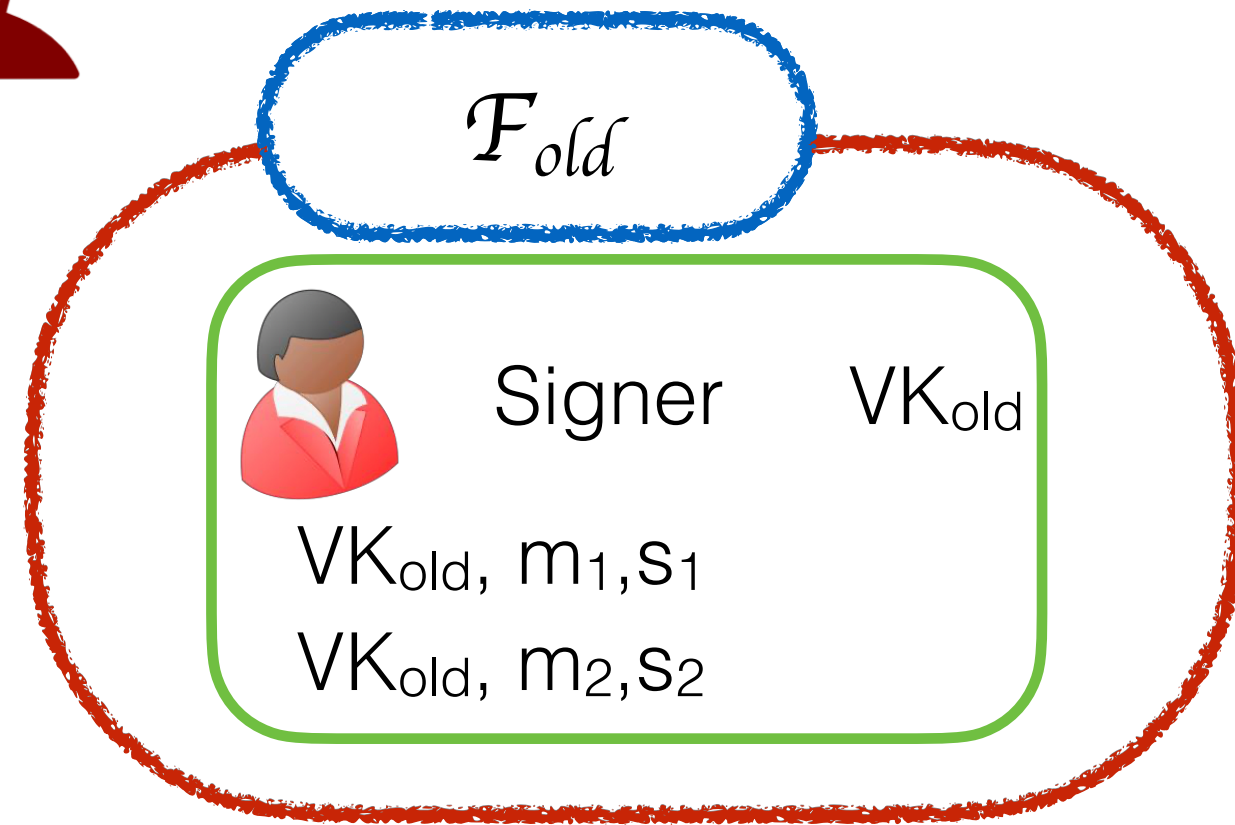
$VK_{new}, M, Supd$







# Updatable signatures

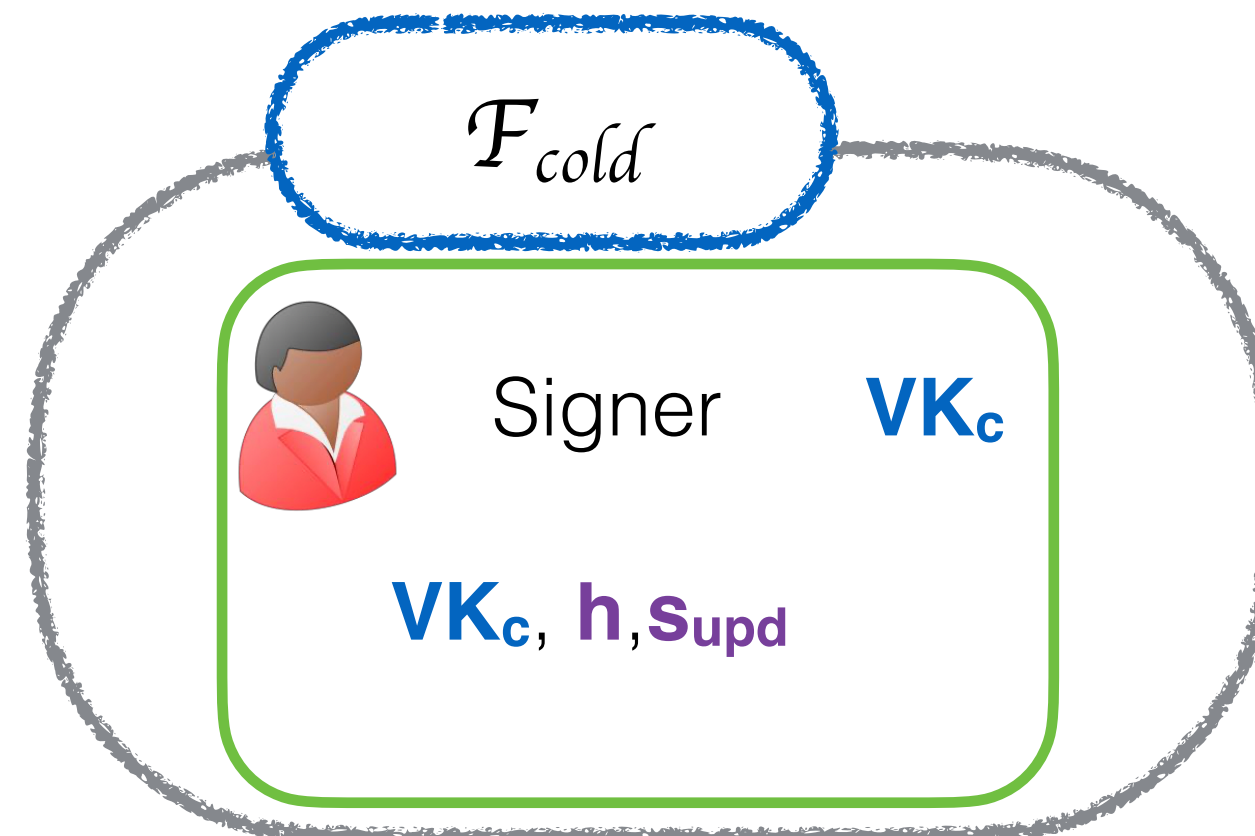


SIGN,  $m_3$



$VK_c$   
 $VK_{new}$   
 $M \leftarrow \{m_1, m_2\}$   
 $h \leftarrow H(m_1 || m_2)$

$VK_{new}, M, Supd$



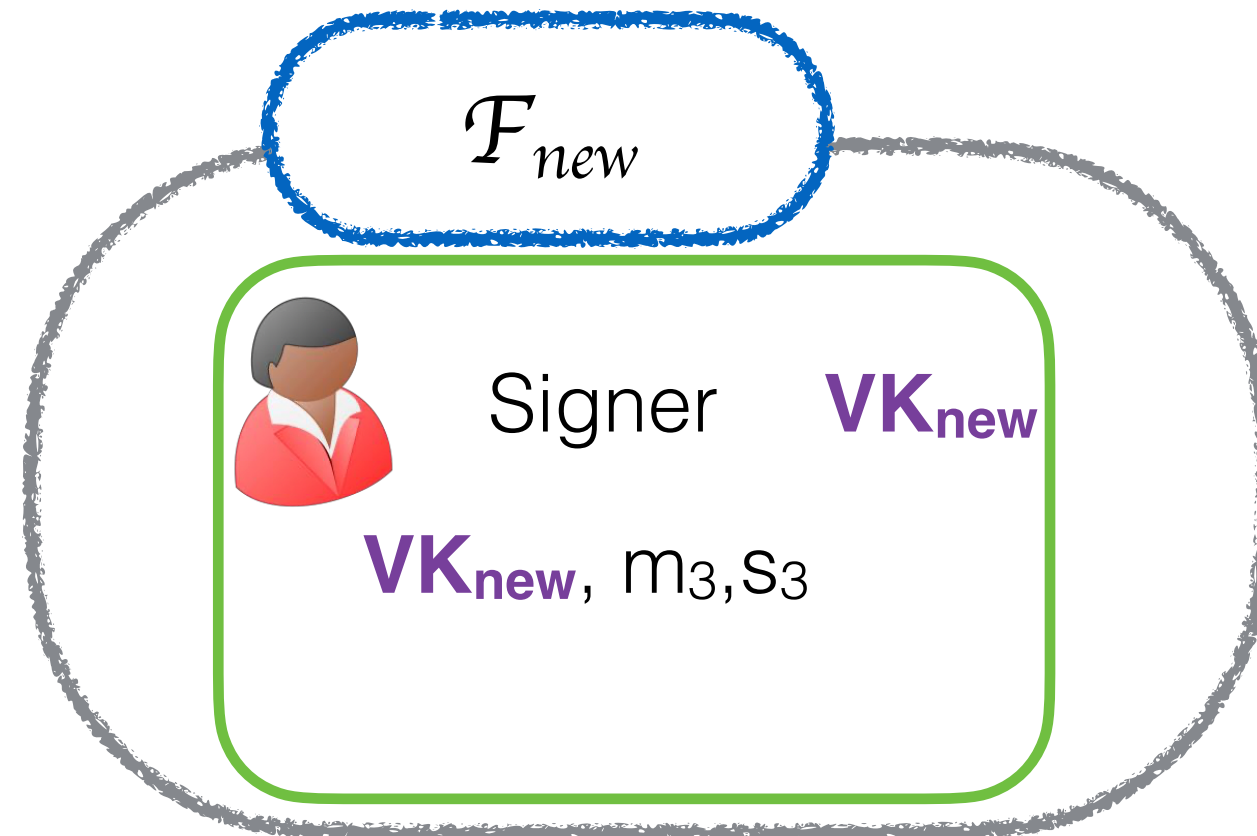
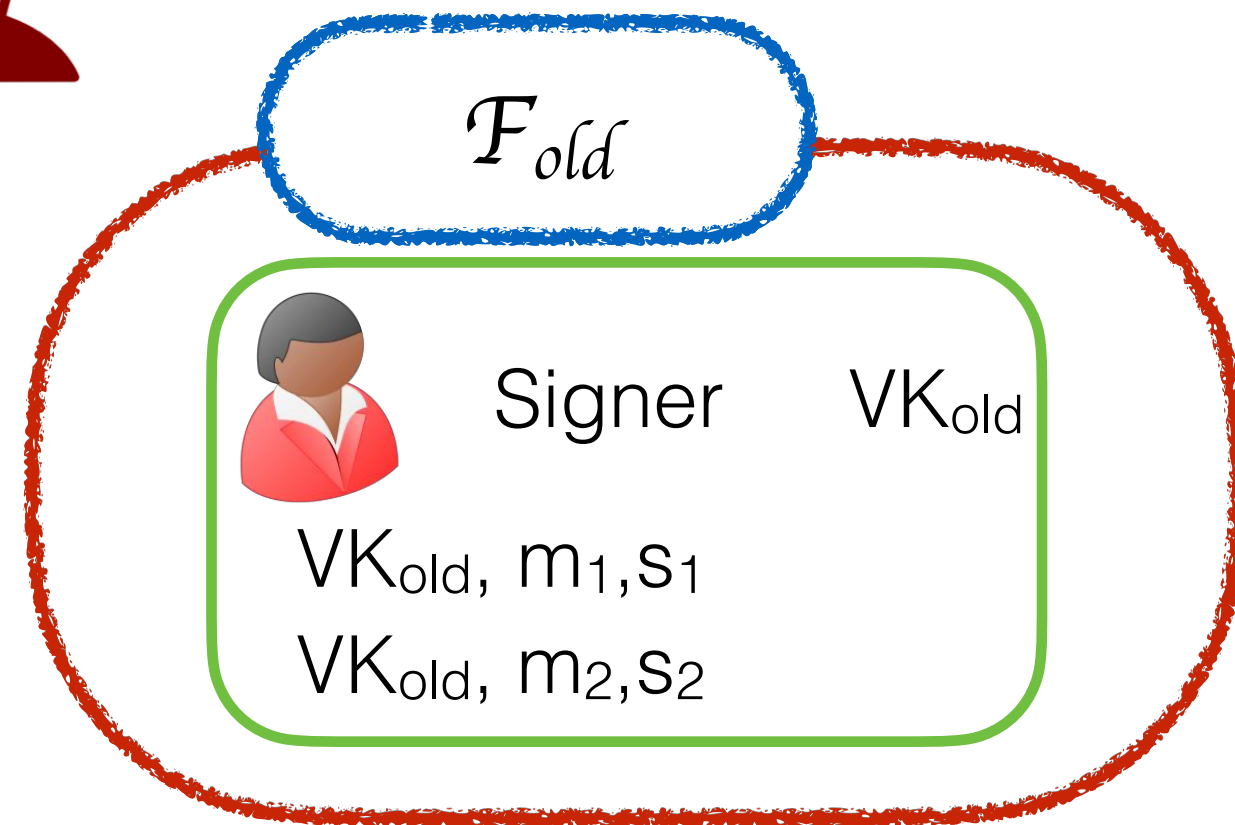
UPDATE,  $\mathcal{F}_{new}$



$VK_c$   
 $VK_{new}, M, Supd$



# Updatable signatures



SIGN,  $m_3$

VERIFY,  $vk_{old}, m_2, s_2$



$VK_c$

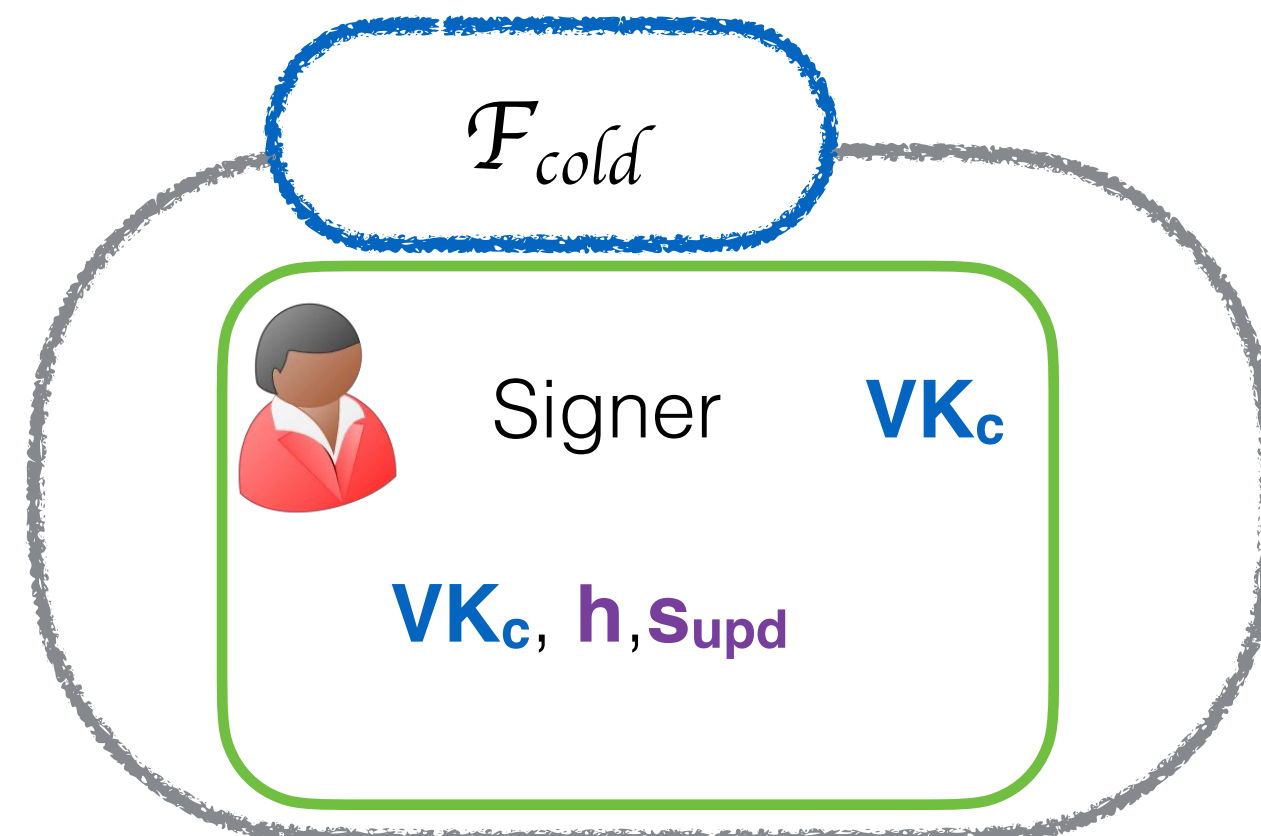
$VK_{new}$

$M \leftarrow \{m_1, m_2\}$

$h \leftarrow H(m_1 || m_2)$

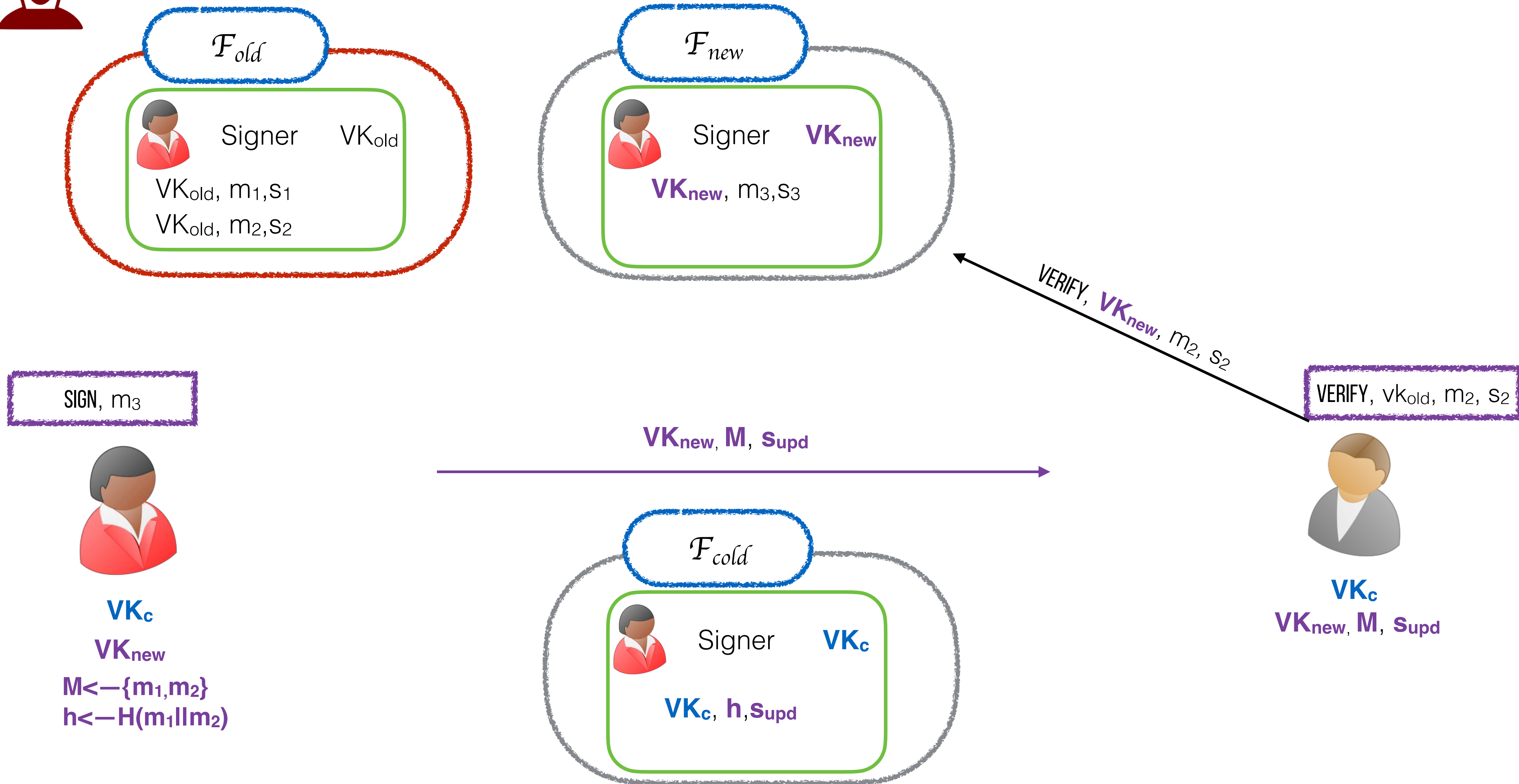
$VK_c$

$VK_{new}, M, Supd$



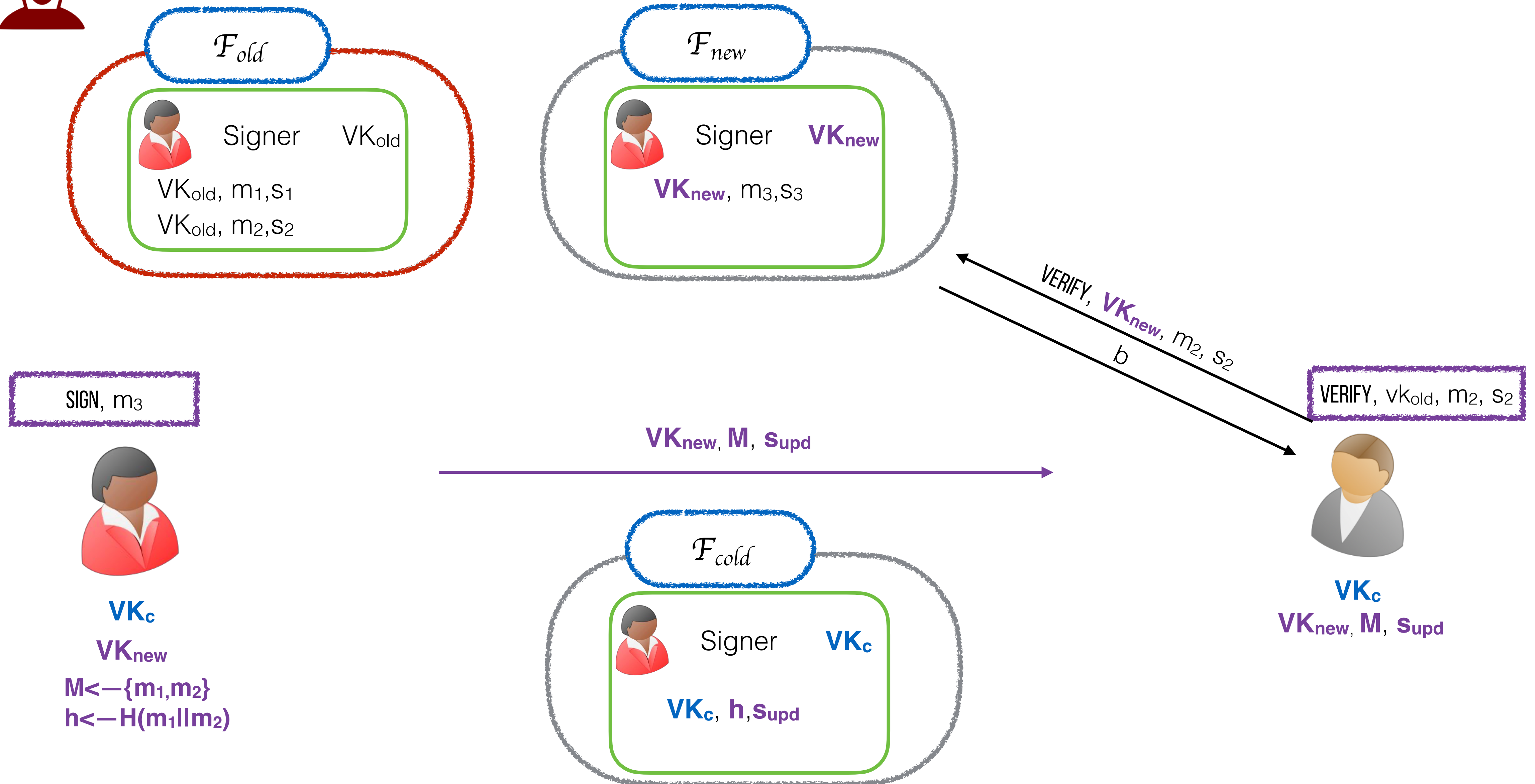


# Updatable signatures



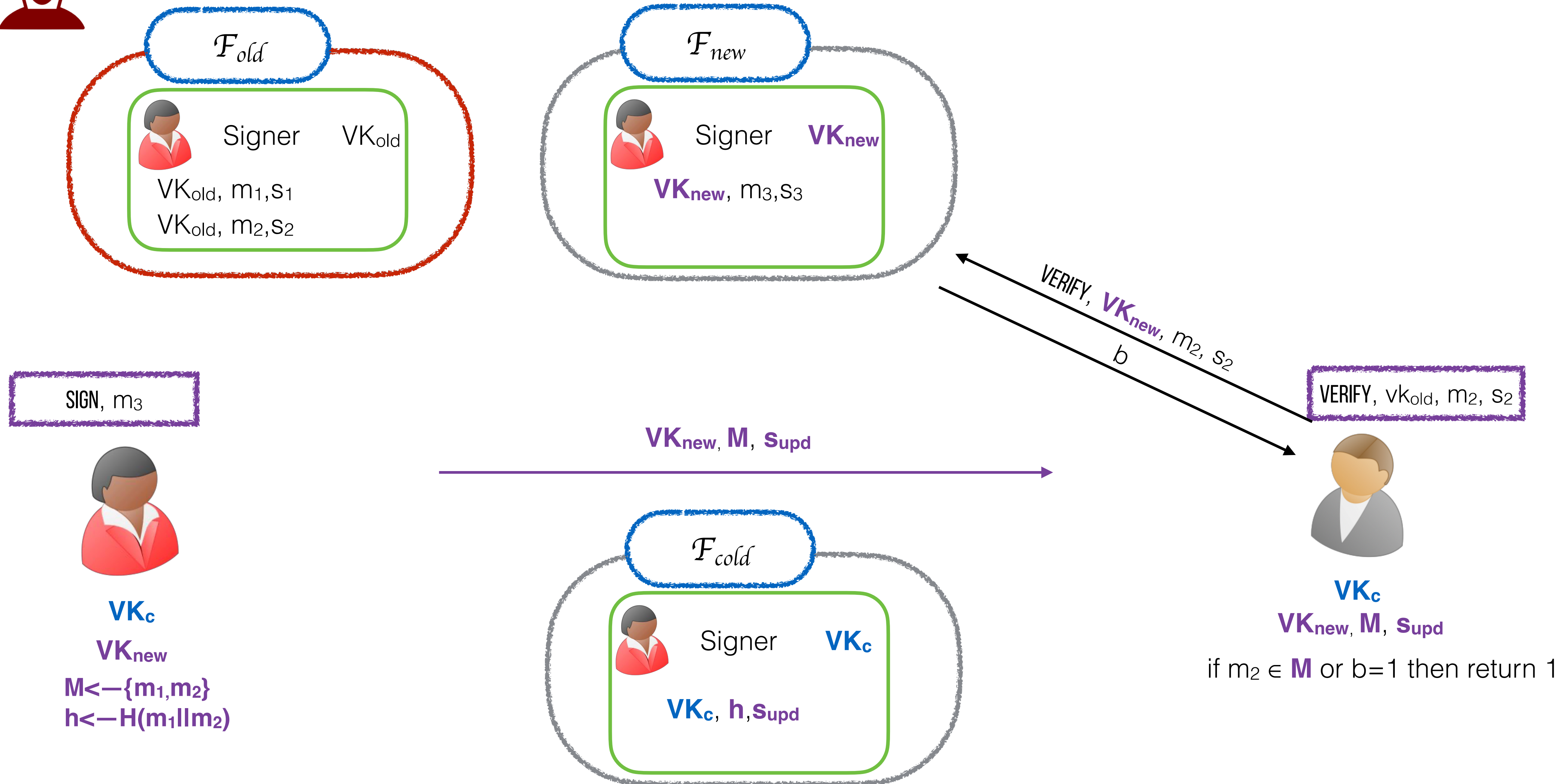


# Updatable signatures



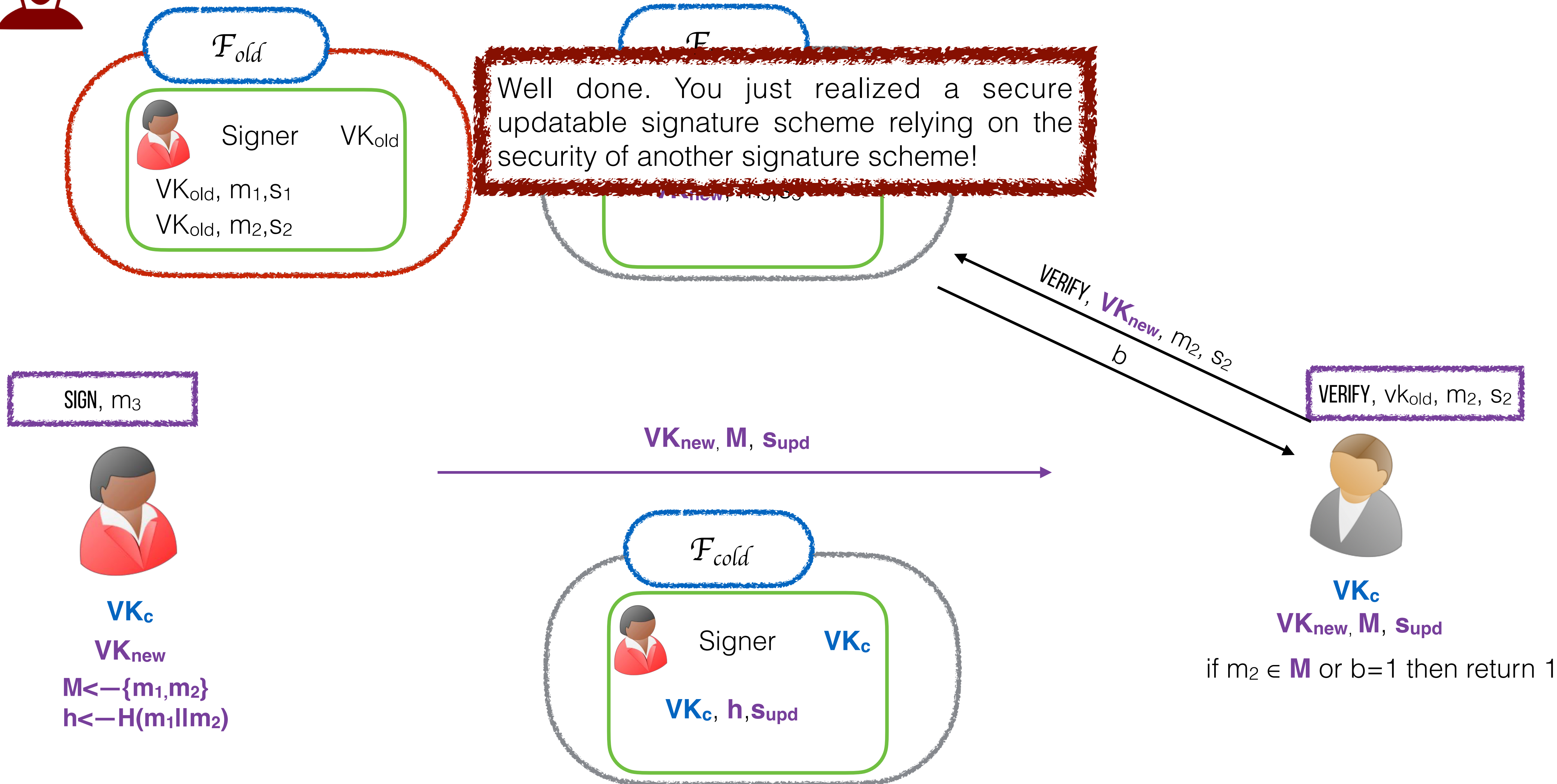


# Updatable signatures





# Updatable signatures





# Updatable signatures

$\mathcal{F}_{old}$



Signer

$VK_{old}$

$VK_{old}, m_1, s_1$

$VK_{old}, m_2, s_2$

$\mathcal{F}$

Well done. You just realized a secure updatable signature scheme relying on the security of another signature scheme!

- $\mathcal{F}_{cold}$  could be a post-quantum secure, **inefficient** scheme used only for the updates
- The support of  $\mathcal{F}_{cold}$  is needed only if  $\mathcal{F}_{old}$  is believed to be compromised

SIGN,  $m_3$



$VK_c$

$VK_{new}$

$M \leftarrow \{m_1, m_2\}$

$h \leftarrow H(m_1 || m_2)$

$\mathcal{F}_{cold}$



Signer

$VK_c$

$VK_c, h, Supd$

$VK_{new}, m_2, s_2$

$b$

VERIFY,  $vk_{old}, m_2, s_2$



$VK_c$

$VK_{new}, M, Supd$

if  $m_2 \in M$  or  $b=1$  then return 1

# Conclusions

- Cryptographic protocols need to be updated. This should be considered when designing the protocol
- Propose a framework to capture updates
- Model compromised protocols via the corruption of hybrid functionalities
- Extend our result to the case of non-interactive zero-knowledge and PRF



Willing to do a postdoc in multi-party computation at  
The University of Edinburgh? **Reach me out**



**No hot summers!**

**Thank you**