

Your Reputation's Safe with Me: Framing-Free Distributed Zero-Knowledge Proofs

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Muthuramakrishnan Venkitasubramaniam

Mor Weiss



GEORGETOWN UNIVERSITY



Framing-Free Distributed ZK Proofs

P

V_1

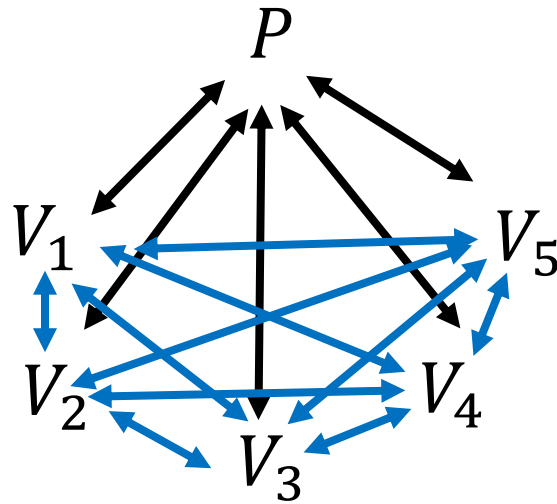
V_5

V_2

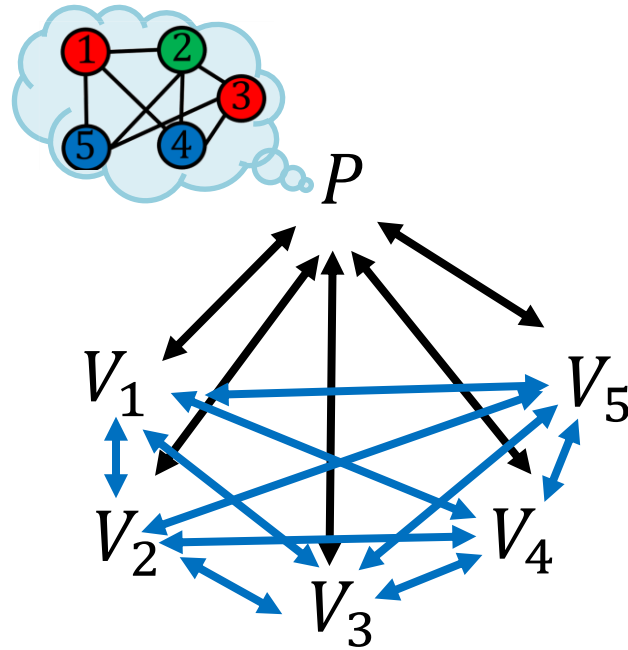
V_4

V_3

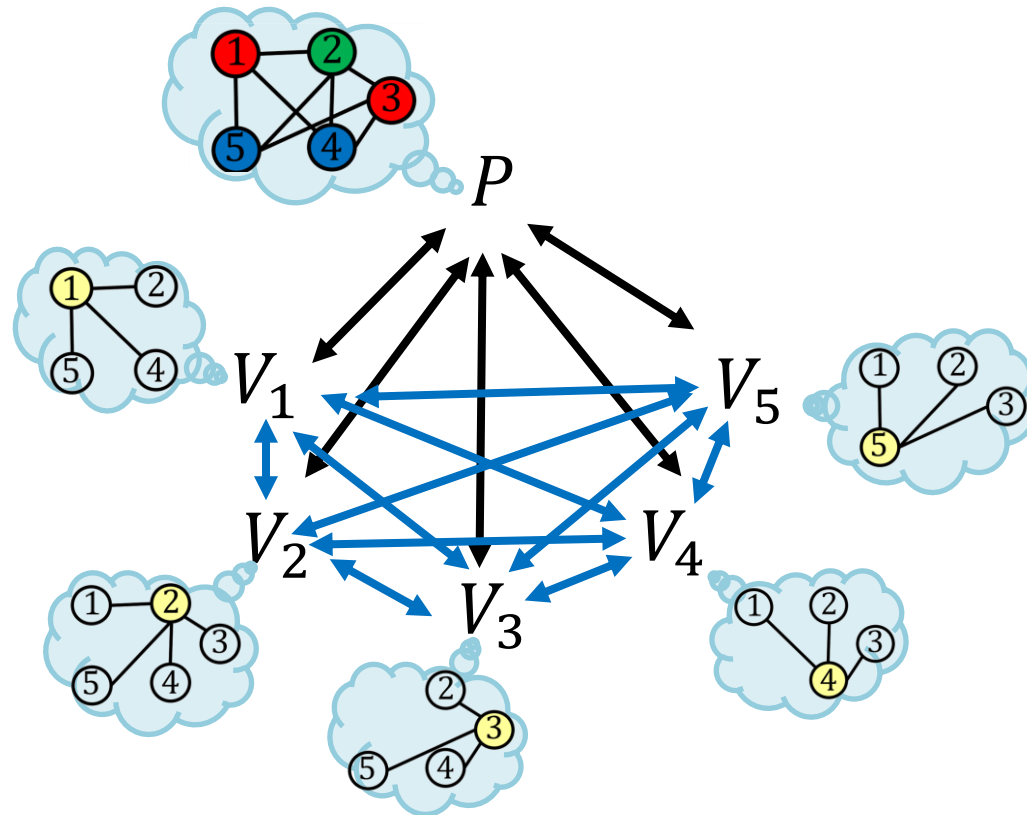
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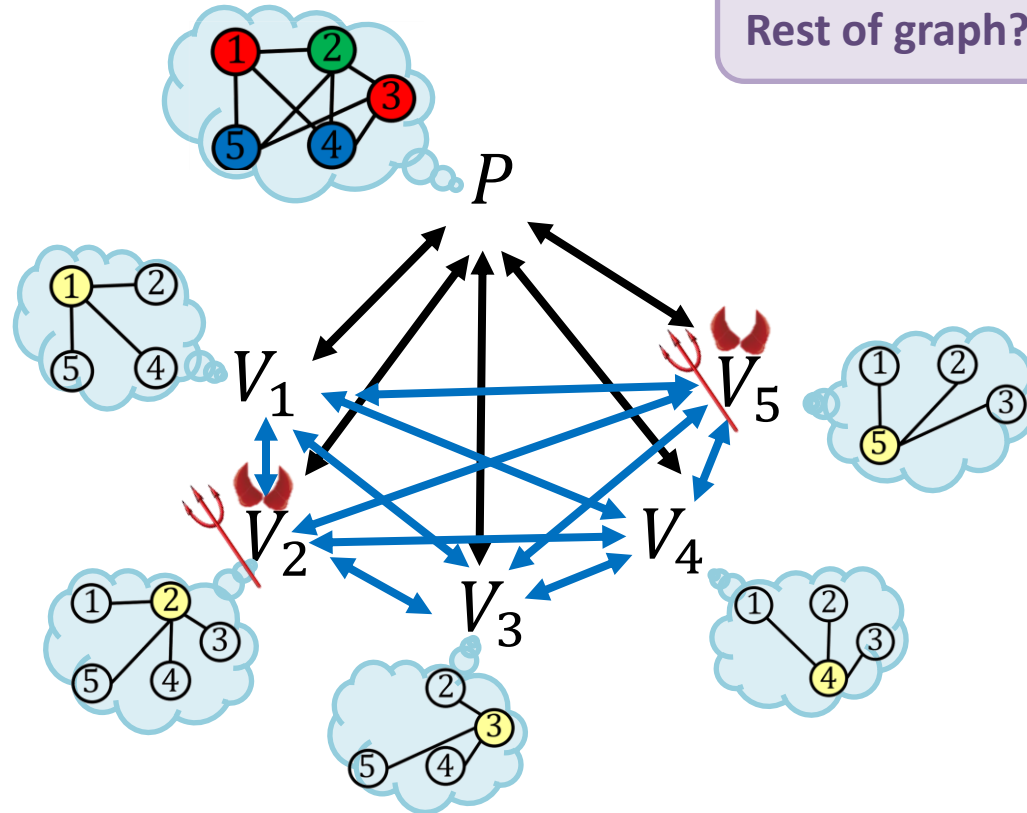


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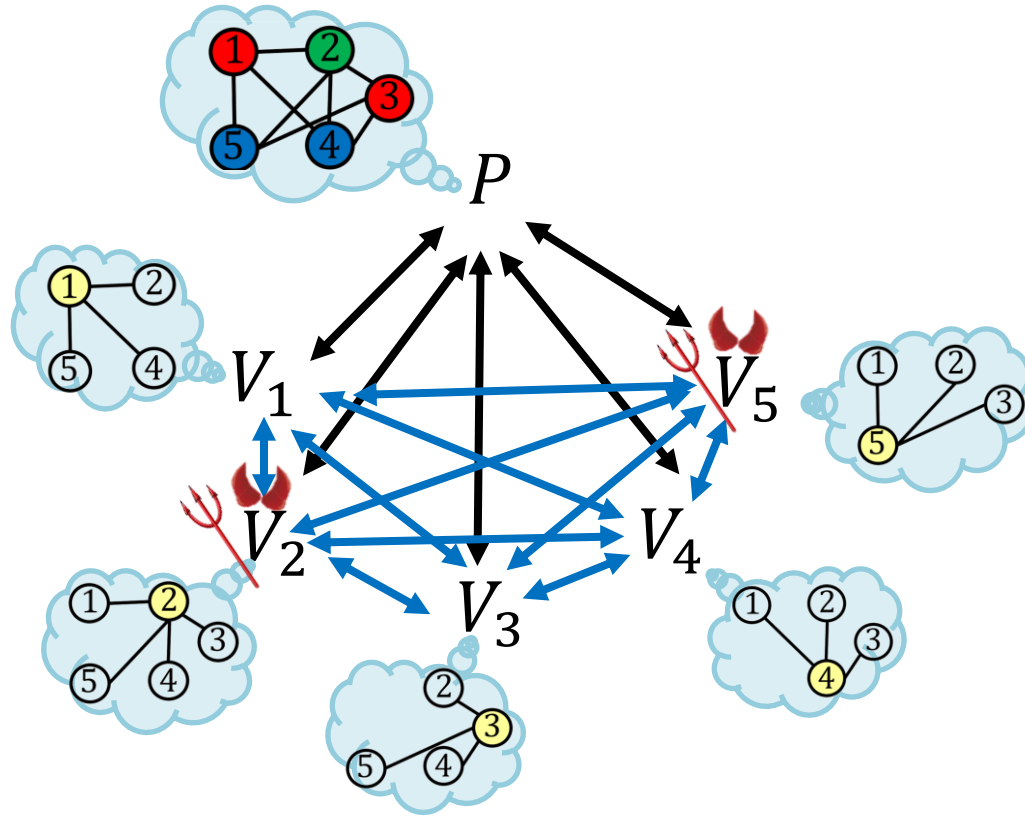
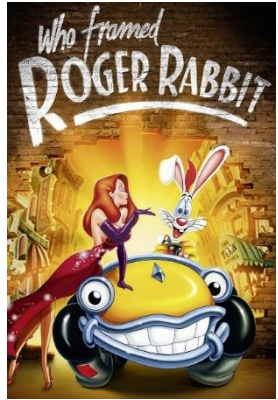


Framing-Free Distributed ZK Proofs

Coloring?
Rest of graph?



Framing-Free Distributed ZK Proofs

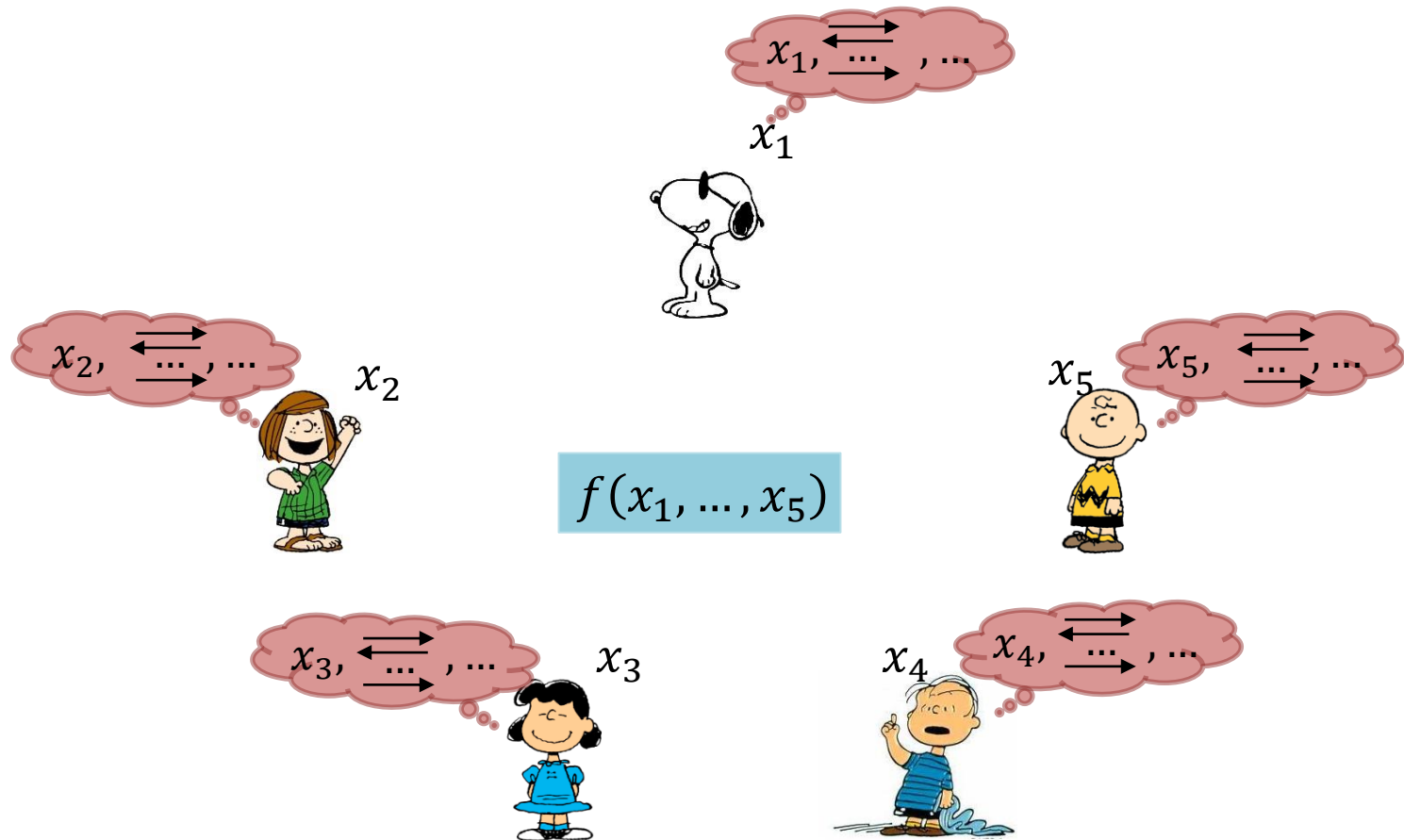


Why **Distributed** ZK (dZK)?

- Many scenarios involve single prover and many verifiers
- Each verifier has only local view of statement

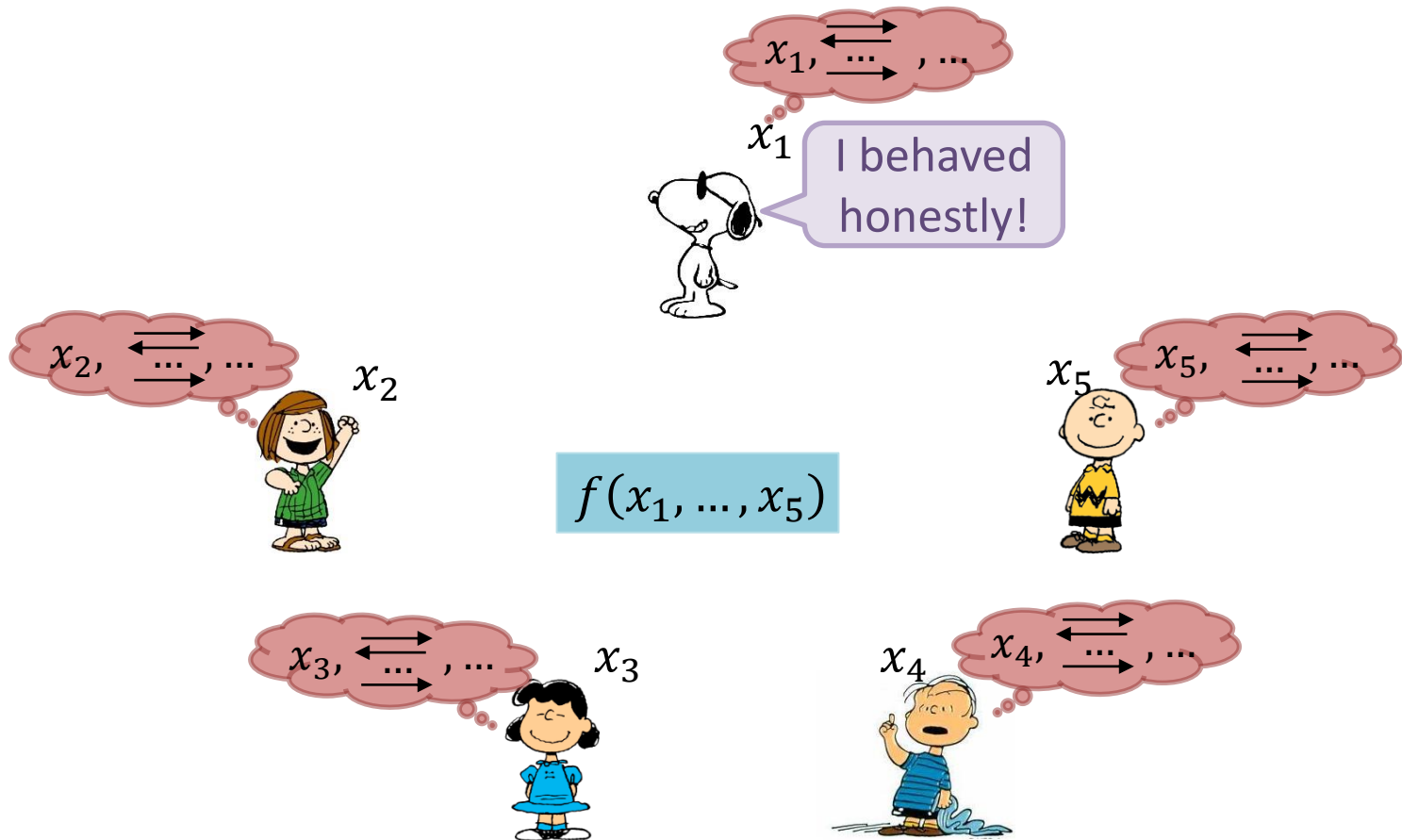
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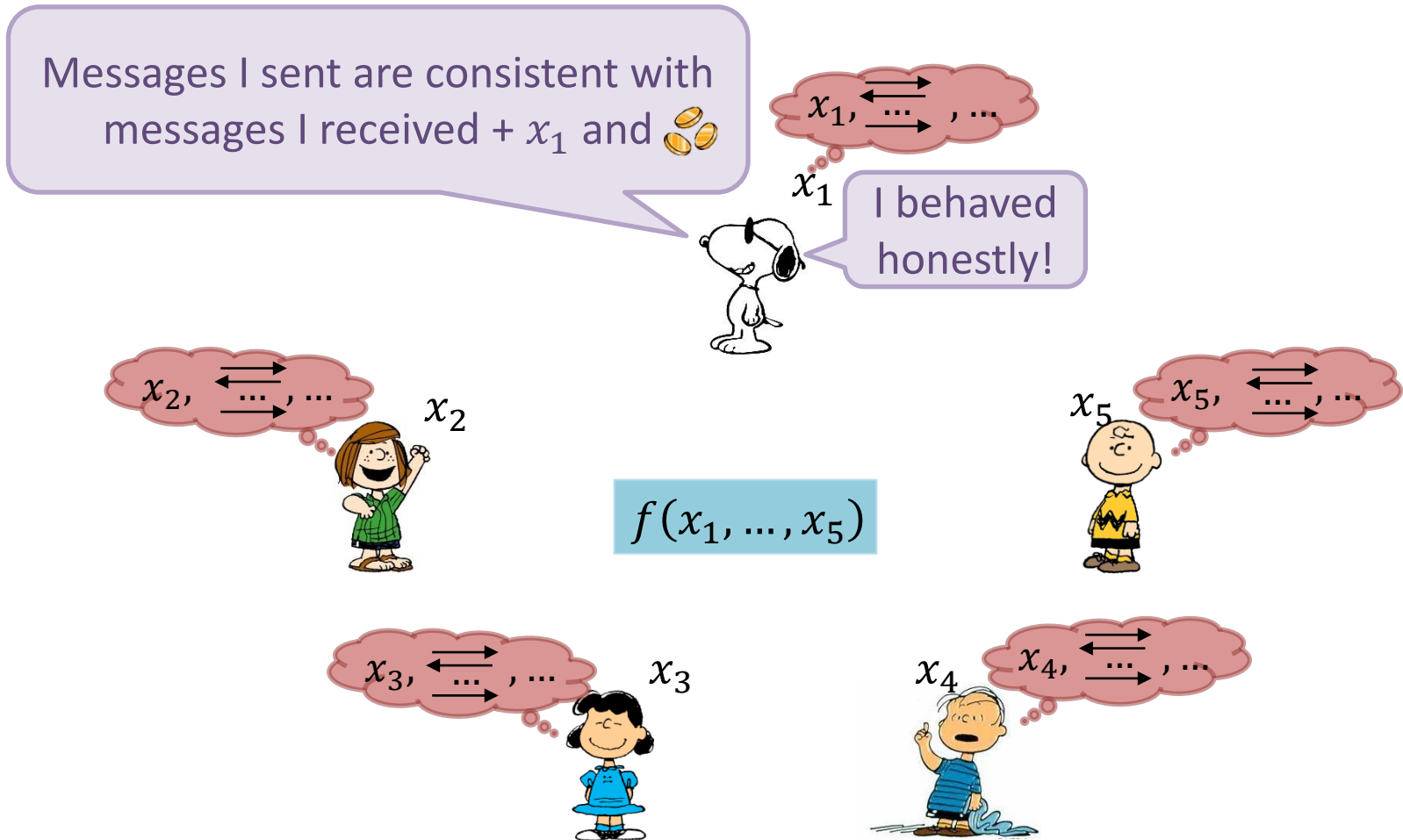
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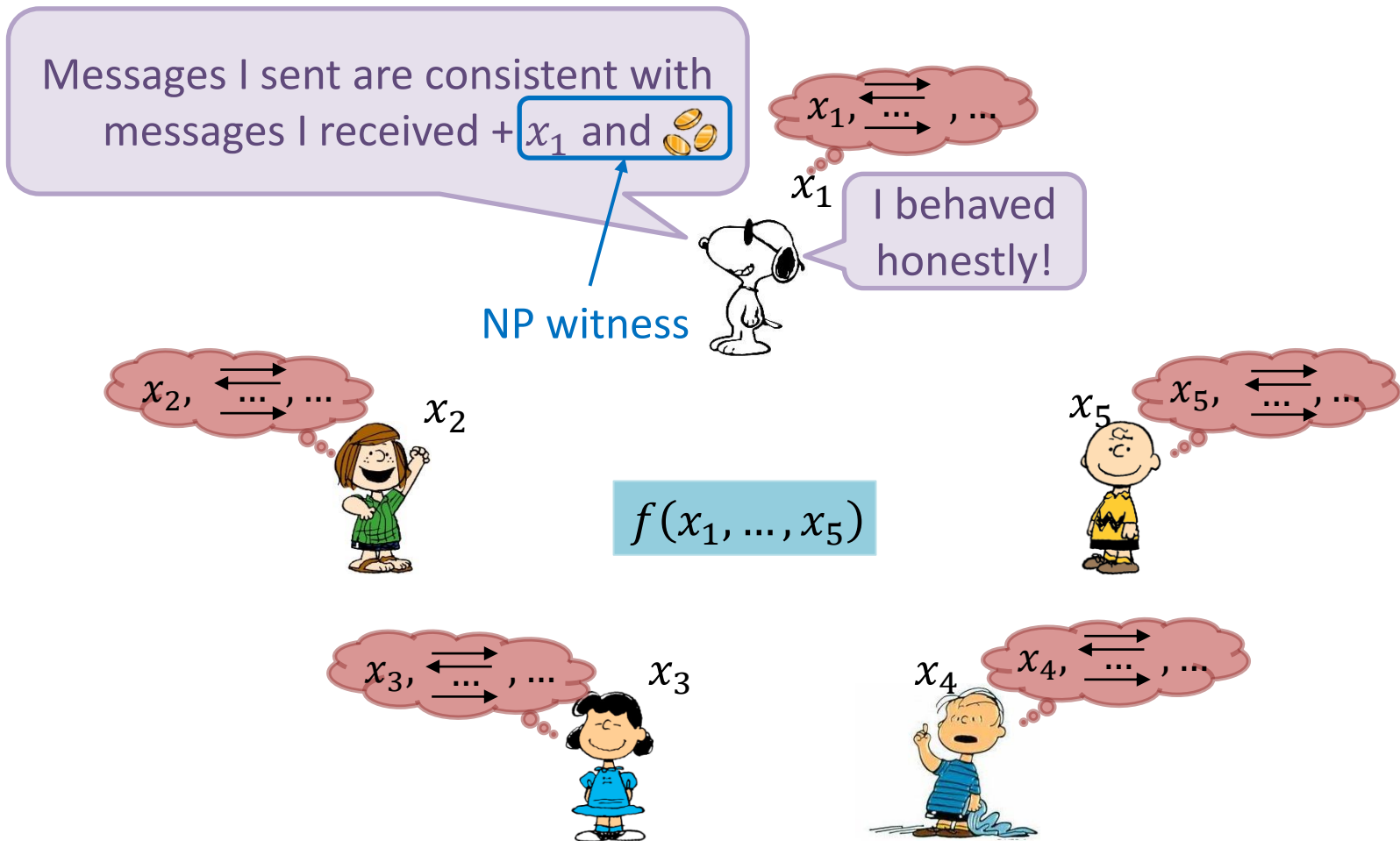
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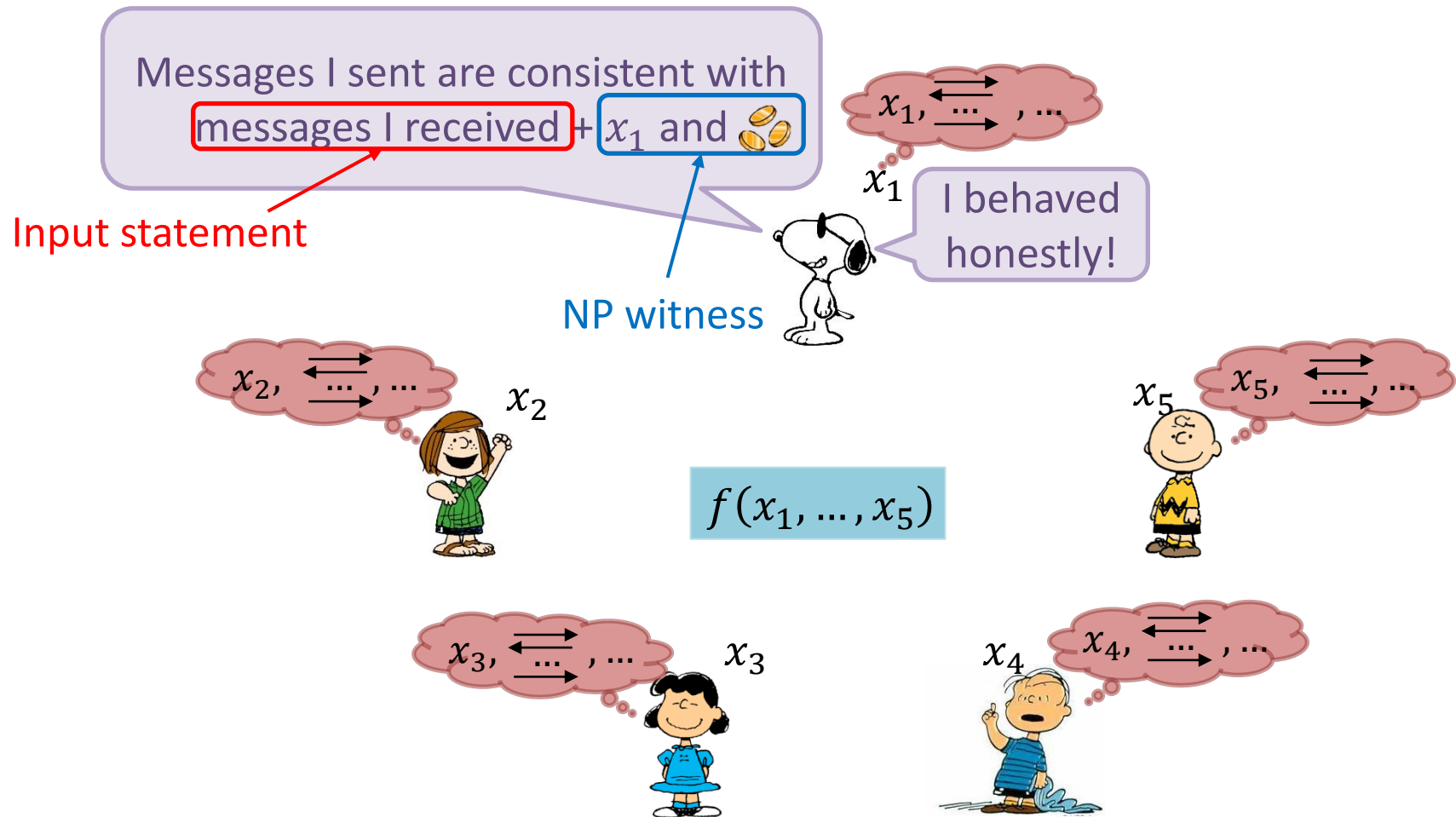
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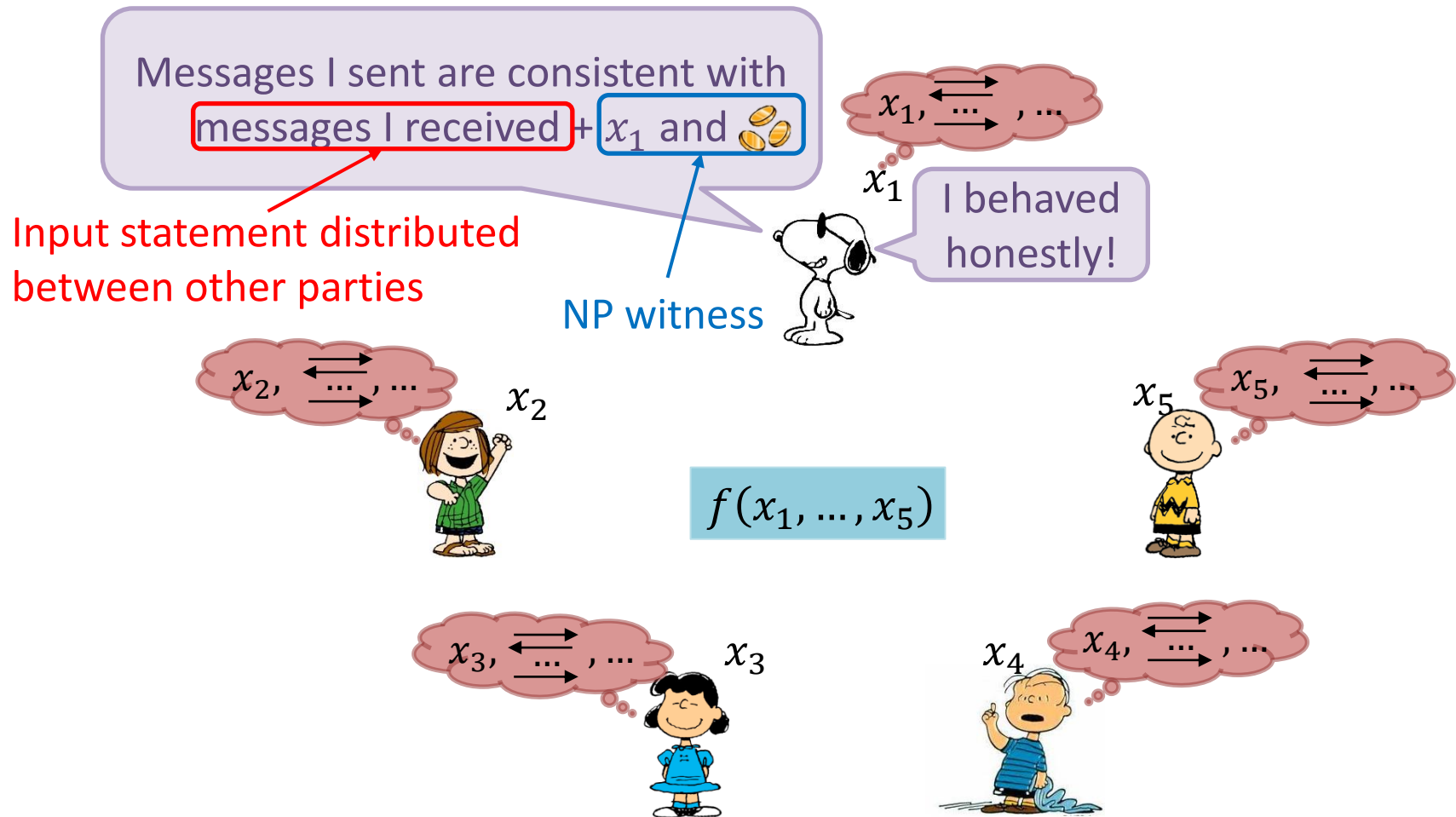
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 - Aggregate statistics (proofs on secret-shared data)
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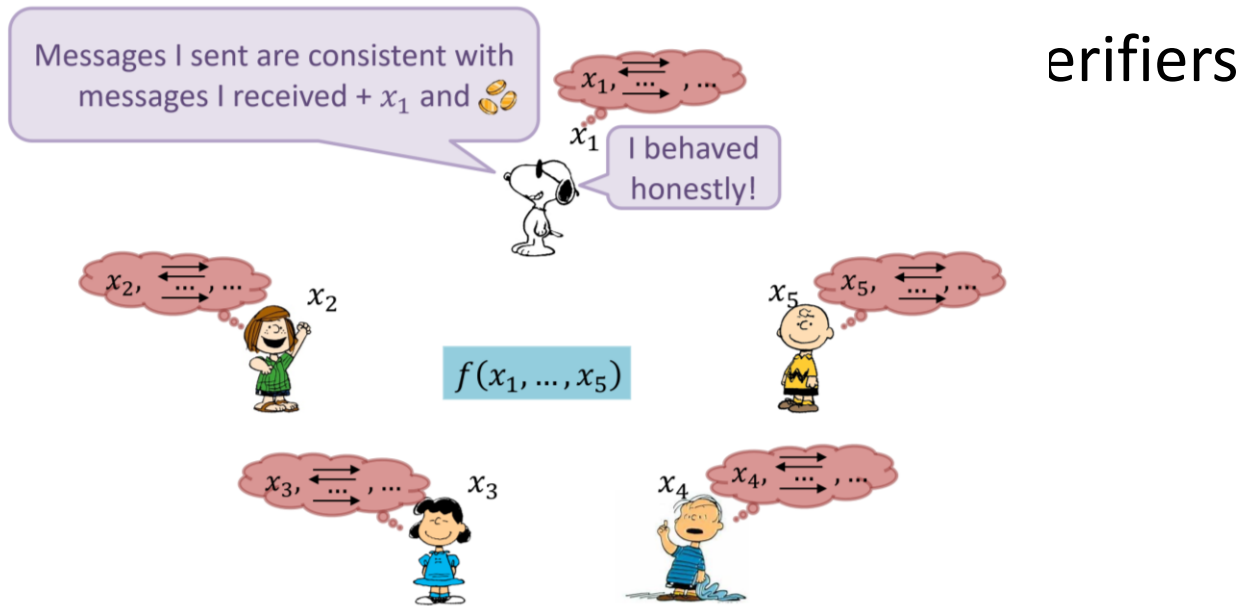
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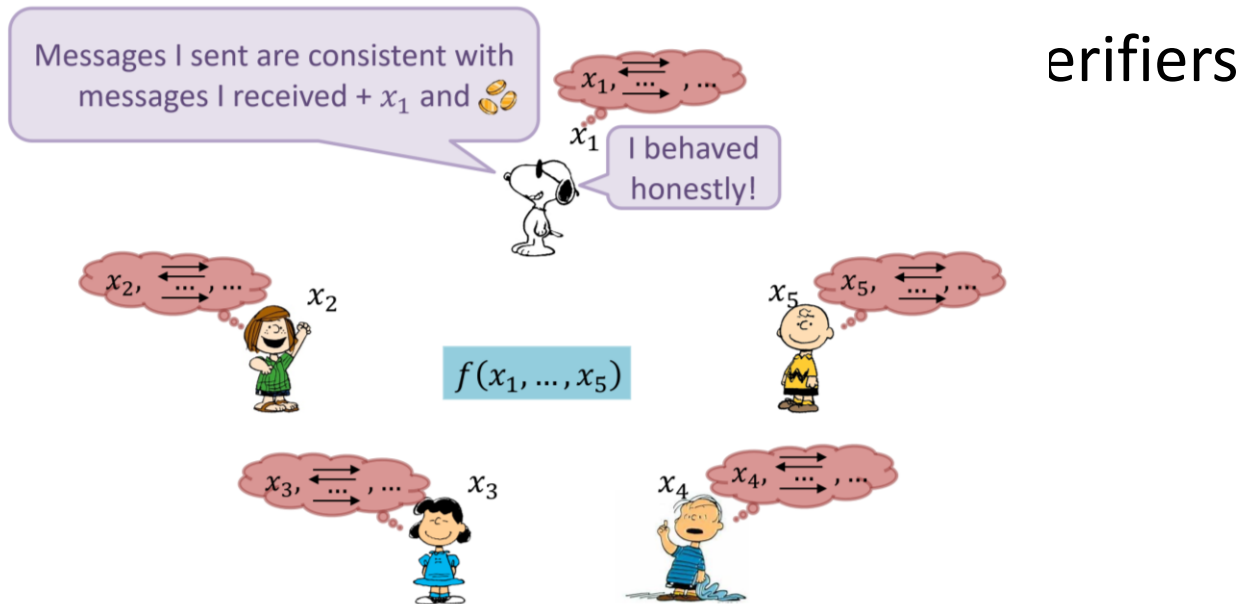
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- poly(k, log|x|)* Total CC during verification phase

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- **Our goal:** verification-efficient framing free dZKs

Distributed ZK Proofs: Previous Works

- **Many different models**

- Verifiers colluding with prover, computational powers of corrupted parties, who knows input statement, ... [ABD91,CF02,GIKR02,GO07,CBM15,CB17,BBCGI19,AKP20a,BBGIN20,BGIN21,BJOSS22,WY22, AKP22]

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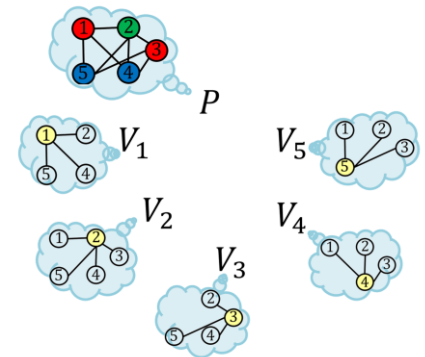
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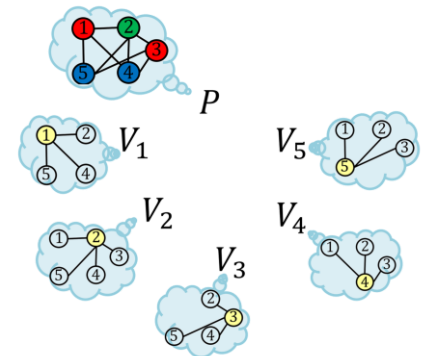
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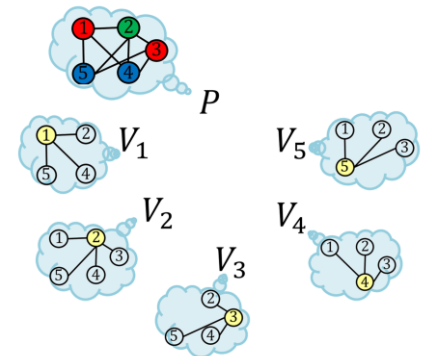
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- **Generic MPC protocols [BGW88,CCD88] give dZK**

- Even with $O(1)$ rounds [IK02,ABT19,ACGJ18,ACGJ19] and tight thresholds and round complexities [AKP20a,AKP20b]

- **Not verification-efficient!**



Our Contribution

- First **verification-efficient** **“framing-free”** dZK for NP
 - k verifiers, $t < \frac{k-2}{6}$ corruptions
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 - Based on “MPC in the head”
 - Using new analysis for “MPC in the head” in distributed setting (fundamentally different from the analysis in [AKP22])
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- **Instantiations** (assuming ideal coin tossing, $\Omega(k)$ corruptions):

# Rounds	Total proof length	Verification CC
3	$O(\log k \cdot \log C \cdot C)$	$O(k^2)$
4	$O(C)$	$O(k^2 + s)$ (s statistical security param)

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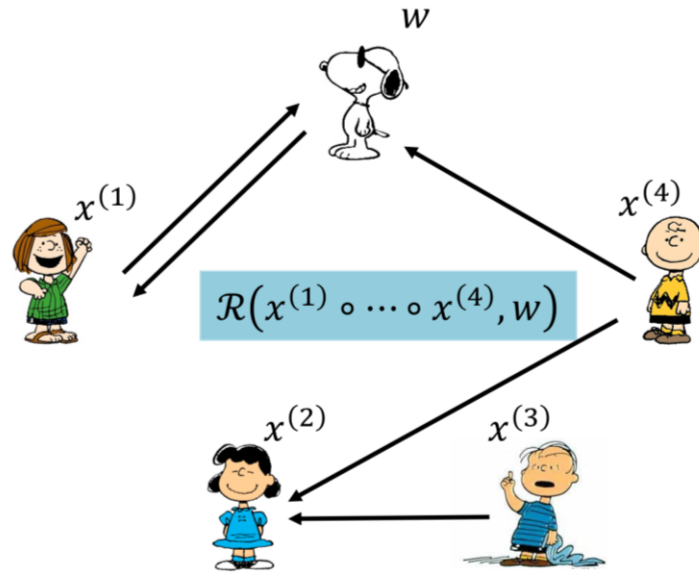
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- **Applications:** aggregate statistics, VSS, (reusable) certifiable VSS, proving honest behavior

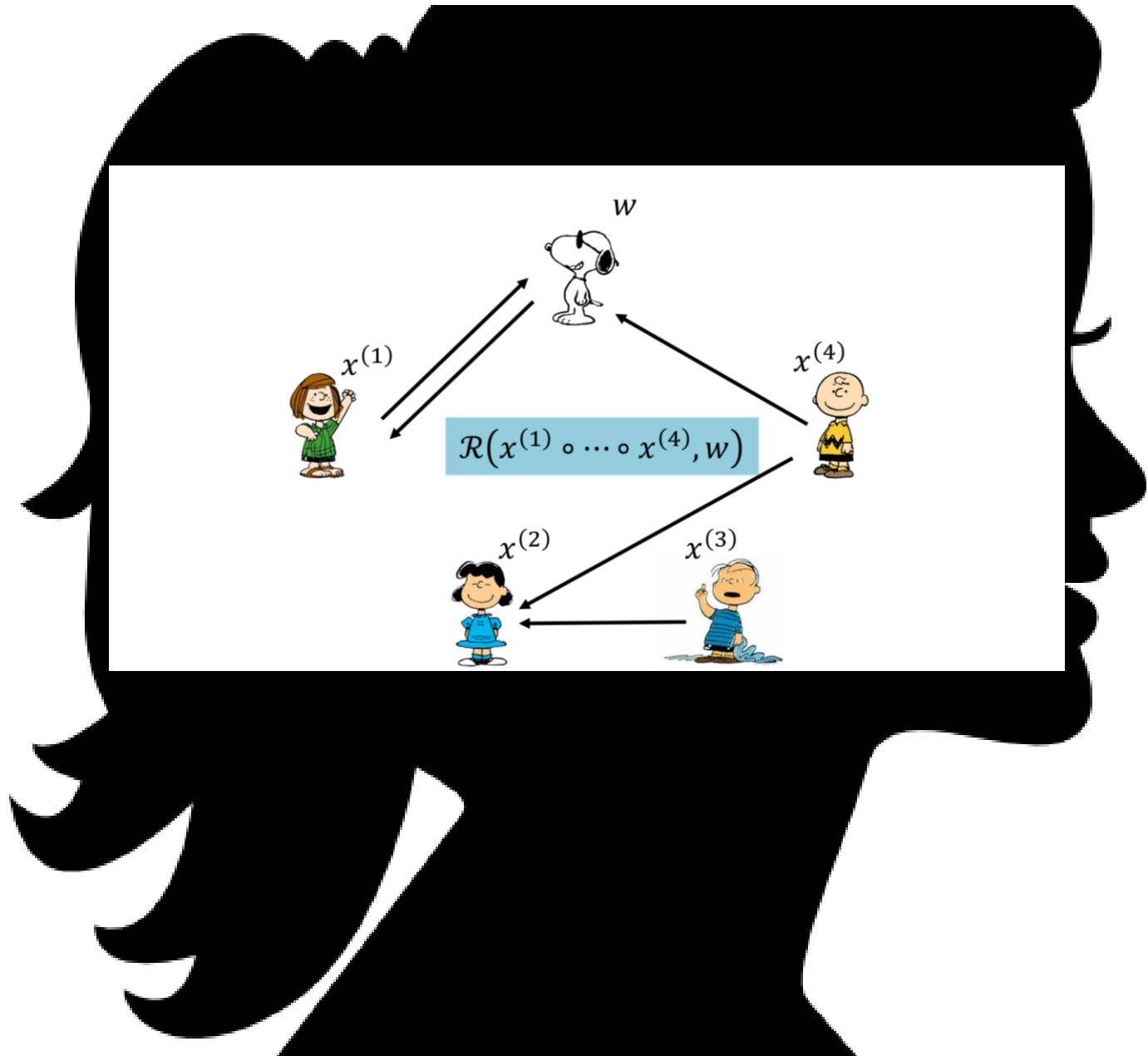
Highlights of Our dZK Construction



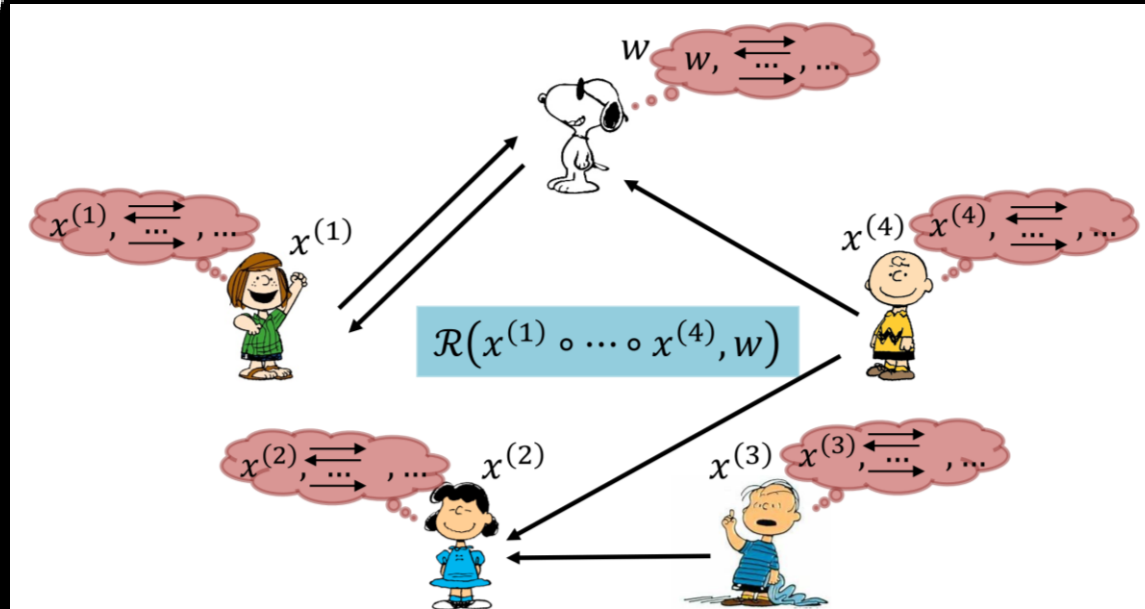
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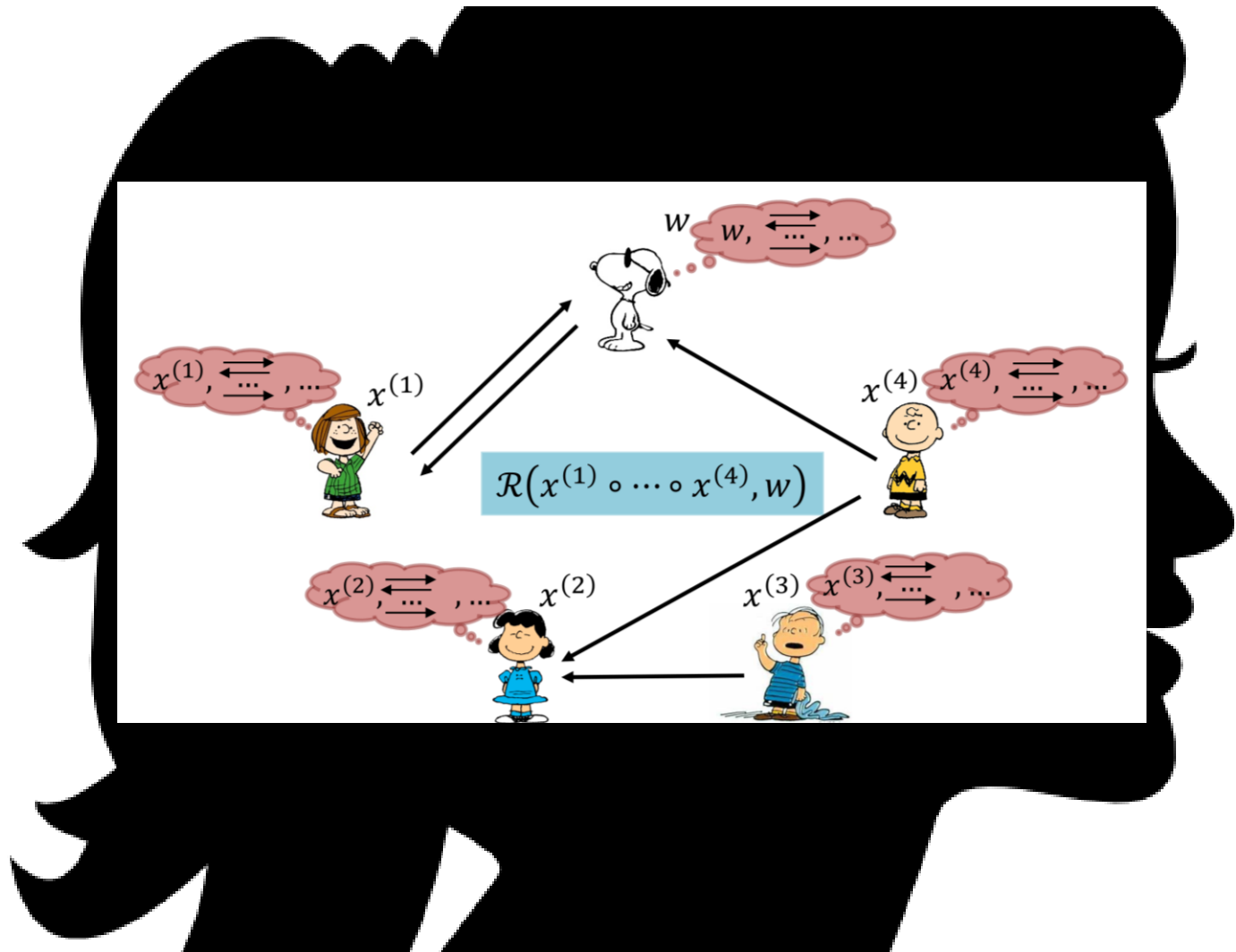
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Proofs from “MPC in the Head”



Proofs from “MPC in the Head”



Pairwise consistency \Rightarrow global consistency \Rightarrow soundness [IKOS07]

dZK from “MPC in the Head” (Warmup)

Prover Zone



$V_1^{x^{(1)}}$

$V_2^{x^{(2)}}$

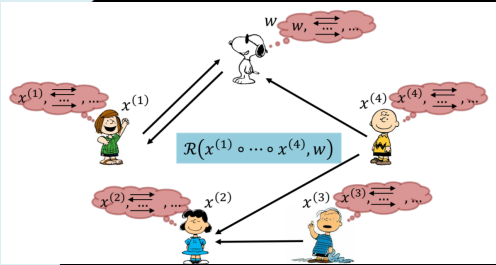
$V_3^{x^{(3)}}$

$V_4^{x^{(4)}}$

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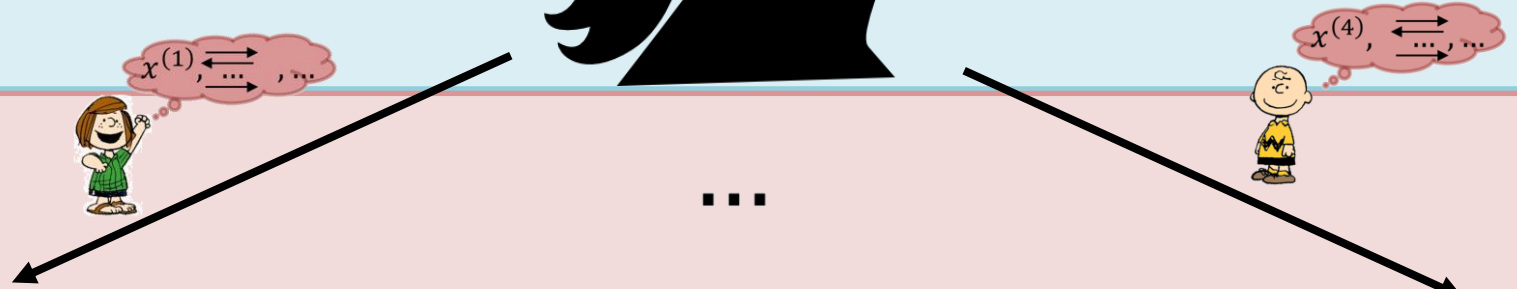
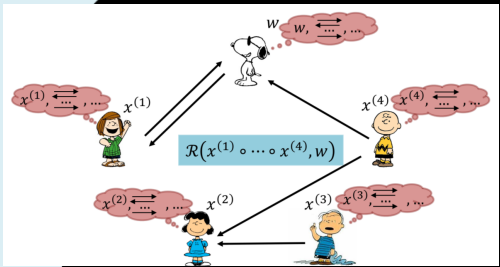
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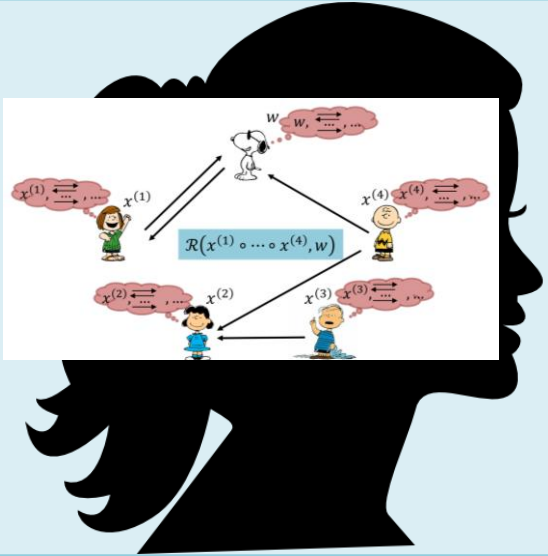


V_1 $x^{(1)}$ V_2 $x^{(2)}$ V_3 $x^{(3)}$ V_4 $x^{(4)}$

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 V_1

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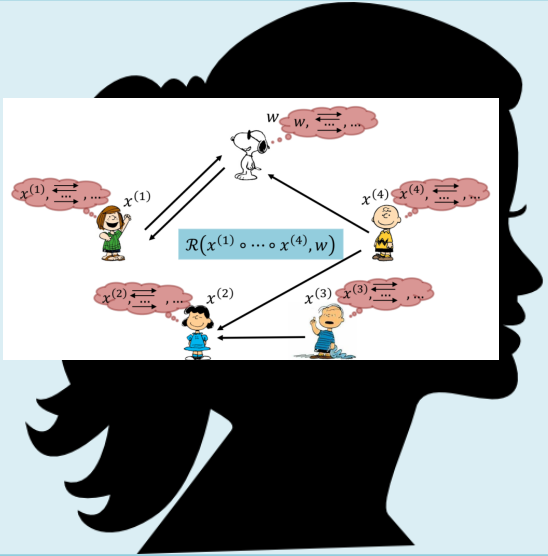
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 V_3

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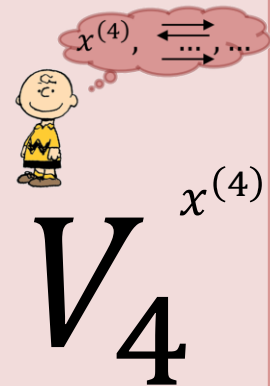
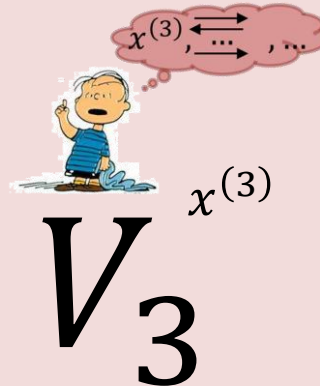
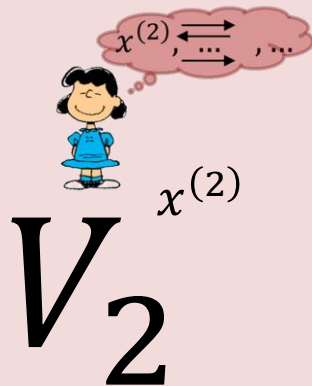
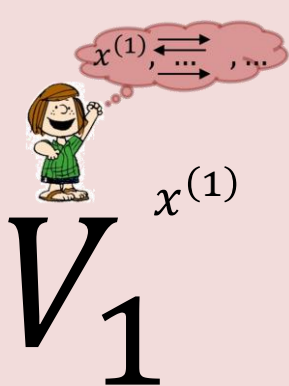
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- Pairwise consistency with every V_j

Accept if no verifier broadcasts complaint

Verification Zone

Getting Verification Efficiency



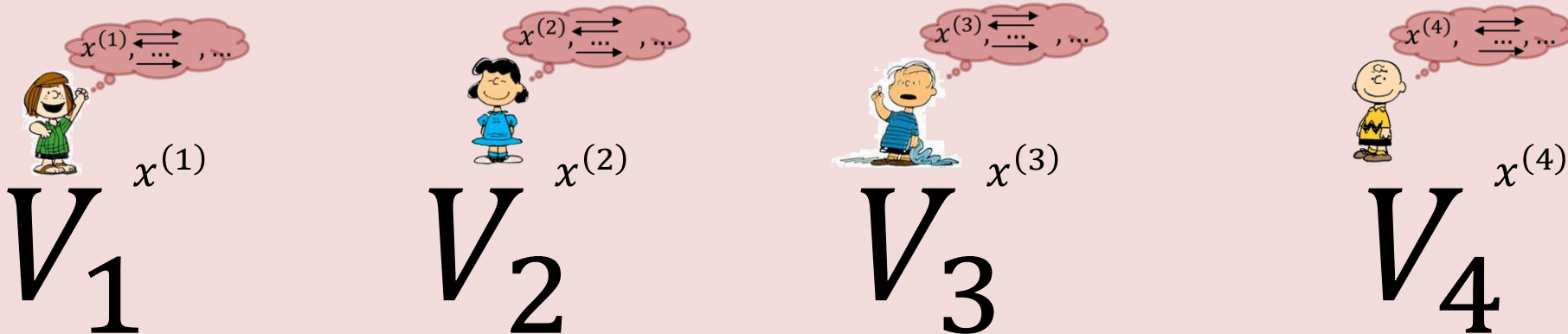
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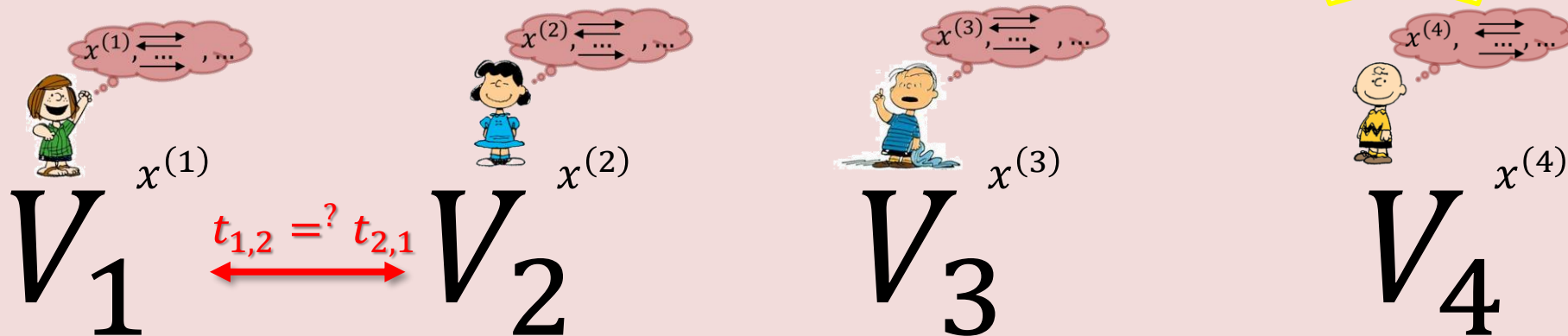
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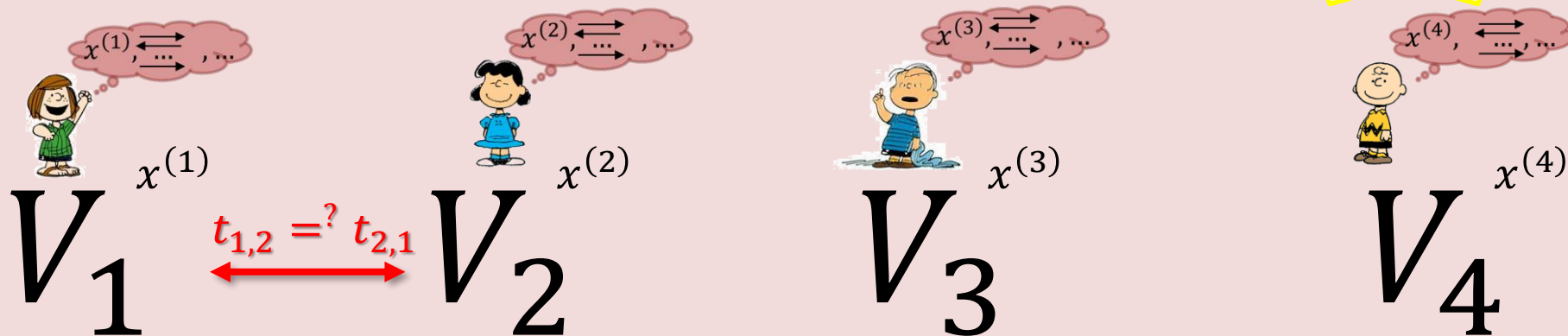
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- Matches dZK of [\[BBCGI19\]](#)

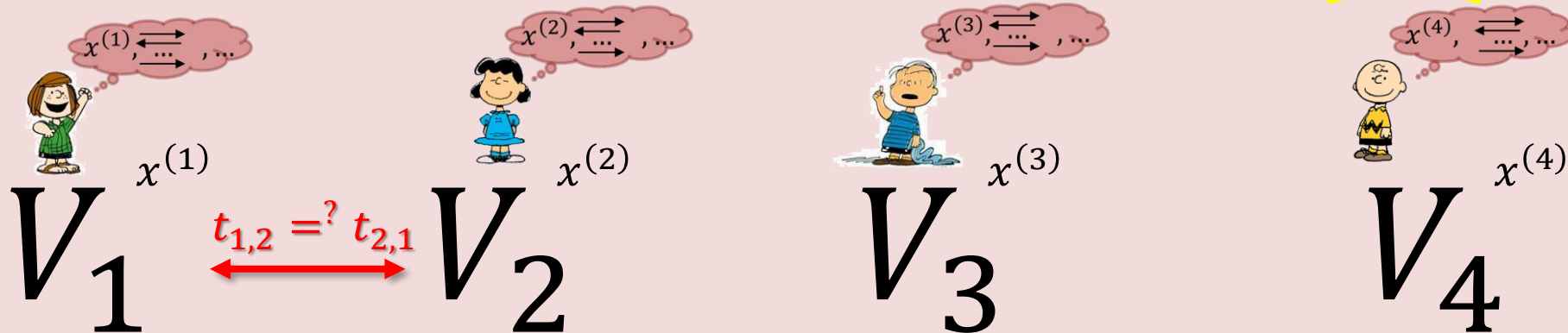


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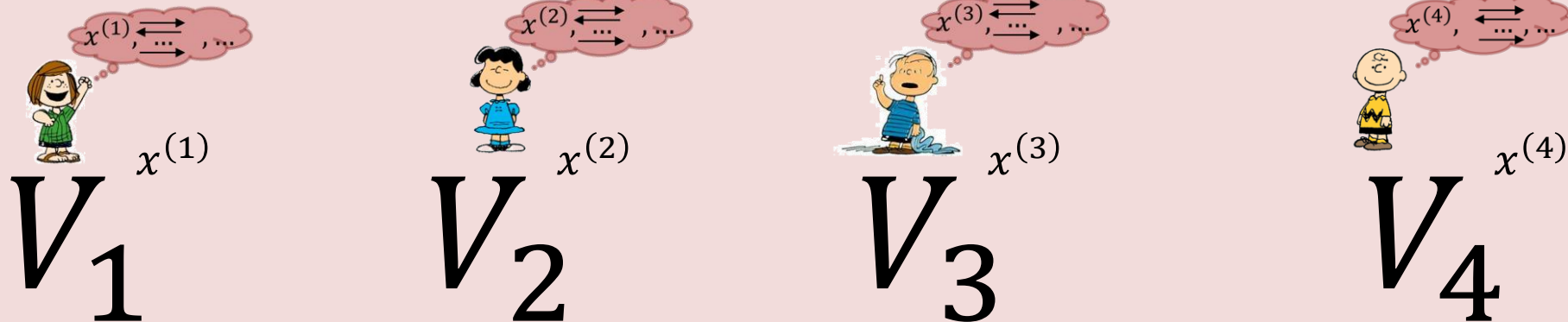
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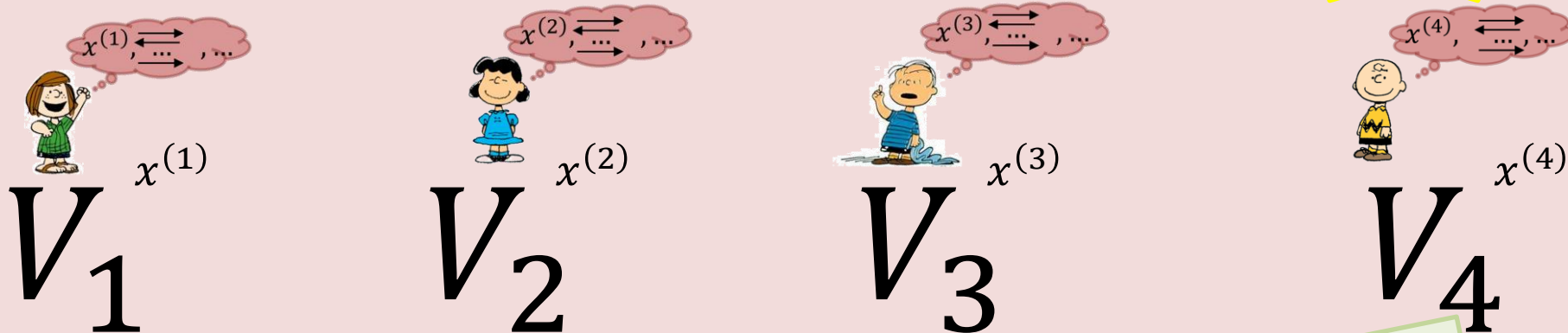
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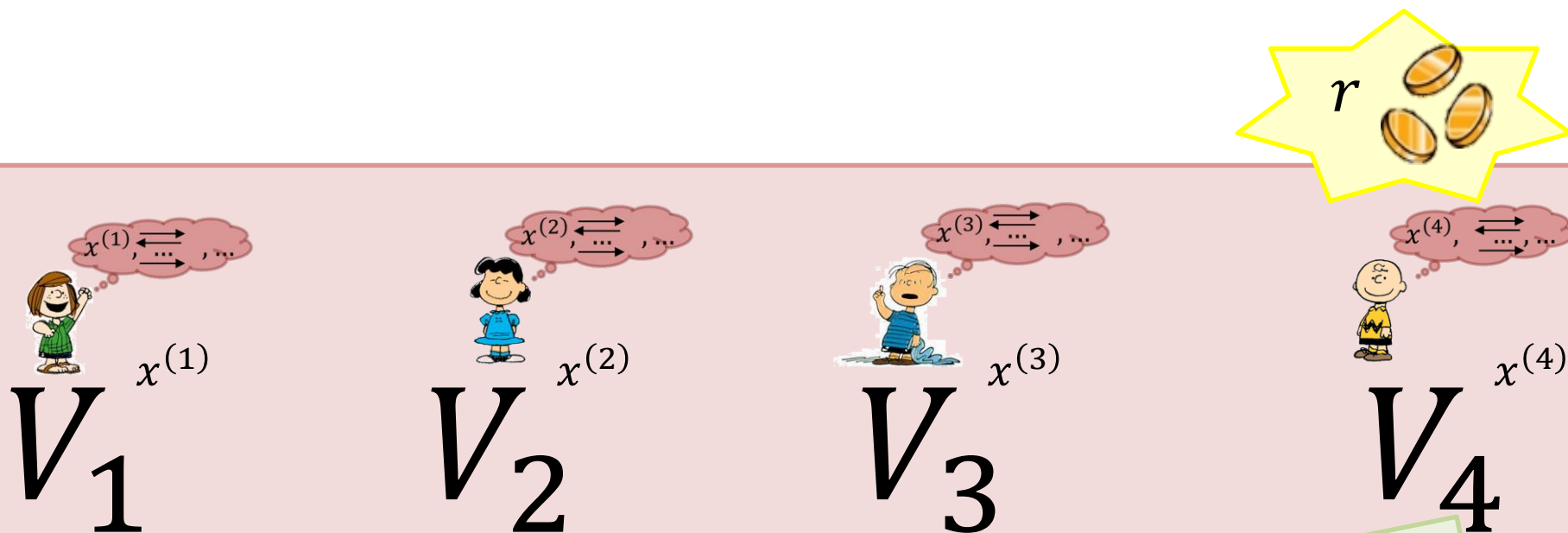
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$t_{1,2}, t_{1,3}, t_{1,4}$
 $view_4$ consistent?

Getting Framing Free

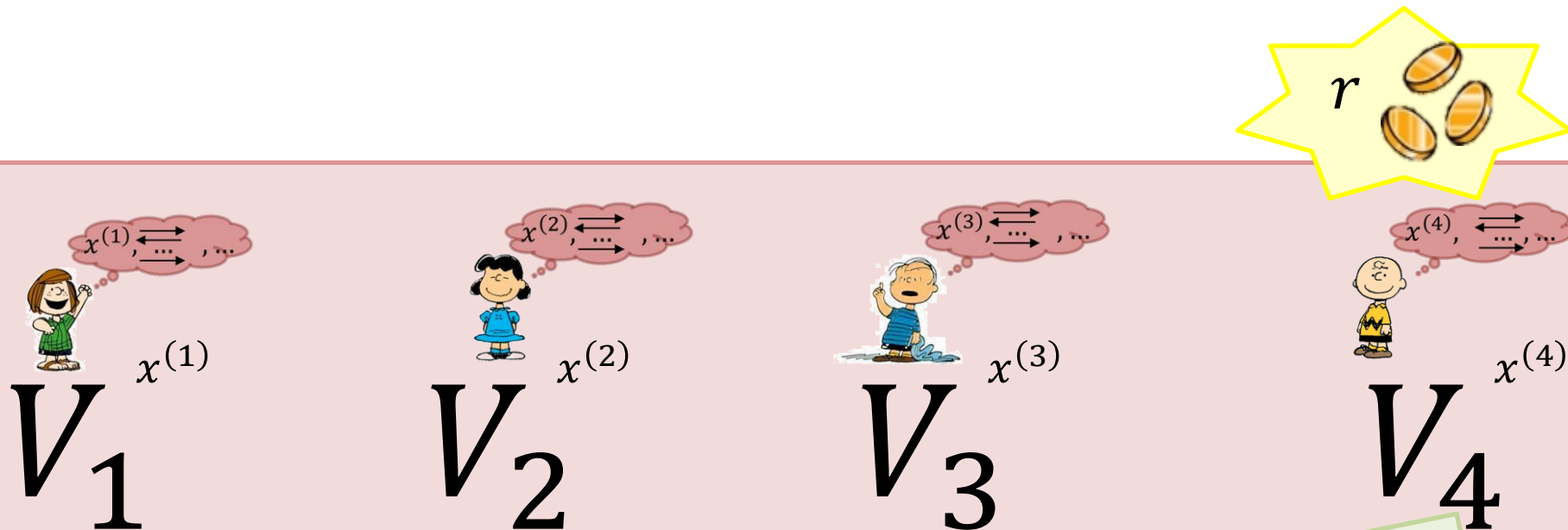
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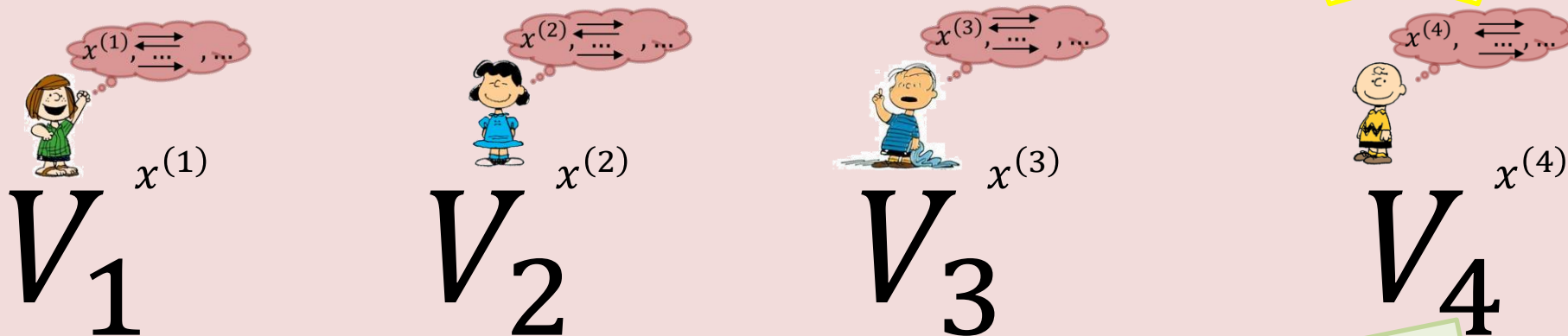
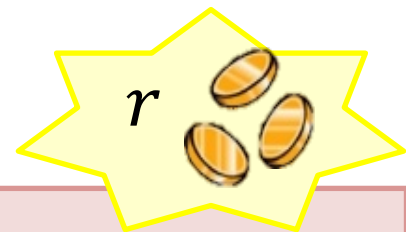
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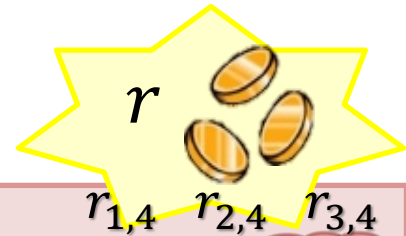
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$r_{1,2} \ r_{1,3} \ r_{1,4}$

$x^{(1)}, \dots, \dots$



$x^{(1)}$

V_1

$r_{1,2} \ r_{2,3} \ r_{2,4}$

$x^{(2)}, \dots, \dots$



$x^{(2)}$

V_2

$r_{1,3} \ r_{2,3} \ r_{3,4}$

$x^{(3)}, \dots, \dots$



$x^{(3)}$

V_3

$r_{1,4} \ r_{2,4} \ r_{3,4}$

$x^{(4)}, \dots, \dots$



$x^{(4)}$

V_4

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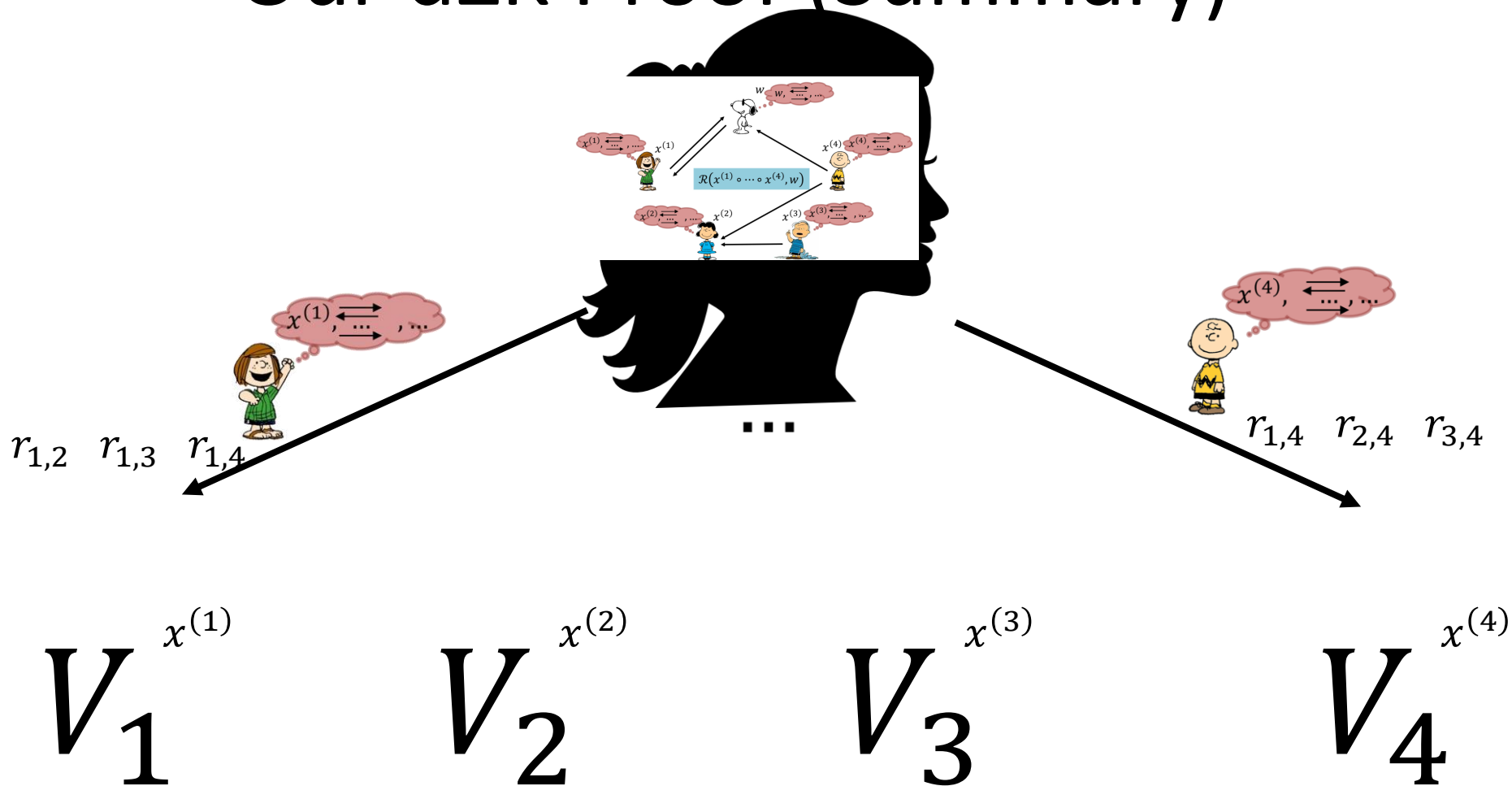
$t_{1,2} + r_{1,2}, t_{1,3} + r_{1,3}, t_{1,4} + r_{1,4}$
 $view_4$ consistent?



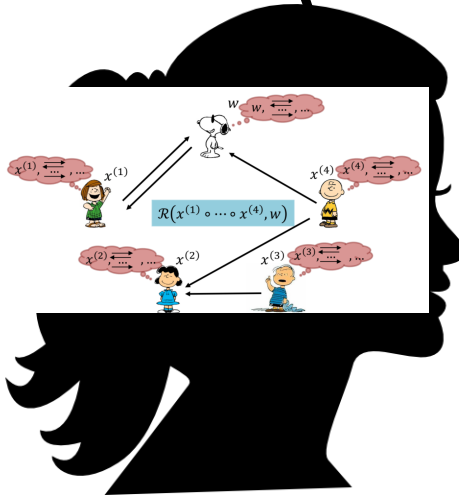
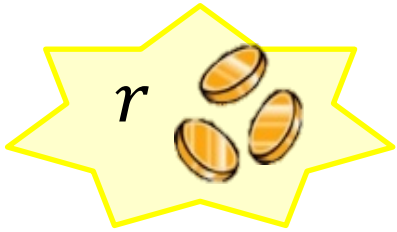
Our dZK Proof (Summary)

 $V_1^{x^{(1)}}$ $V_2^{x^{(2)}}$ $V_3^{x^{(3)}}$ $V_4^{x^{(4)}}$

Our dZK Proof (Summary)



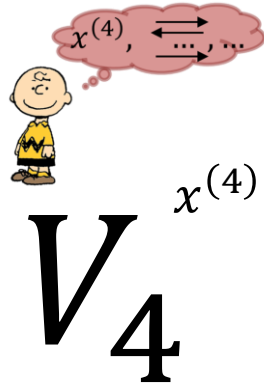
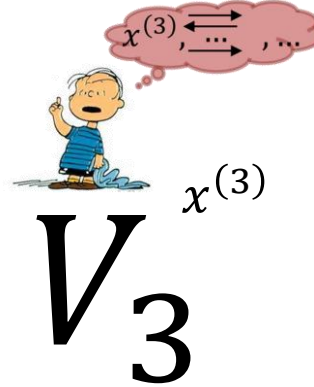
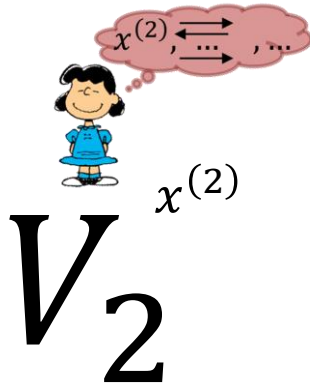
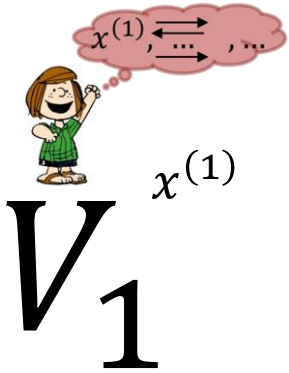
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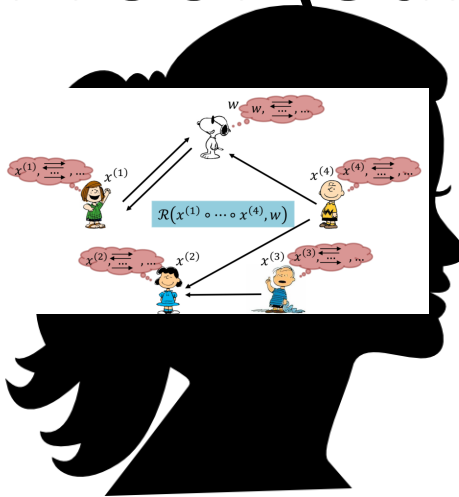
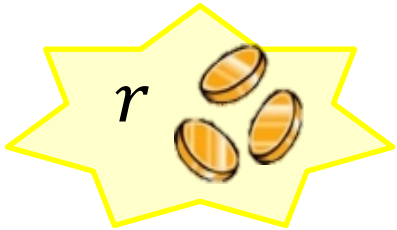
...

$r_{1,2}$ $r_{1,3}$ $r_{1,4}$

$r_{1,4}$ $r_{2,4}$ $r_{3,4}$

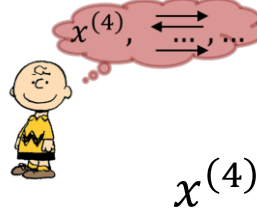
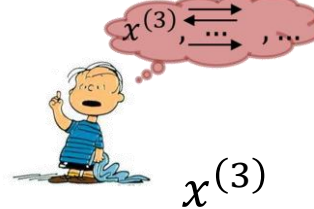
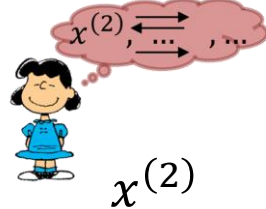
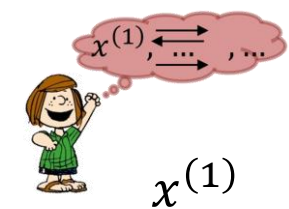


Our dZK Proof (Summary)



$r_{1,2}$ $r_{1,3}$ $r_{1,4}$

$r_{1,4}$ $r_{2,4}$ $r_{3,4}$



V₁

V₂

V₃

V₄



$$t_{1,2} + r_{1,2}$$

$$t_{1,3} + r_{1,3}$$

$$t_{1,4} + r_{1,4}$$

view₁ consistent?

$$t_{2,1} + r_{1,2}$$

$$t_{2,3} + r_{2,3}$$

$$t_{2,4} + r_{2,4}$$

view₂ consistent?

$$t_{3,1} + r_{1,3}$$

$$t_{3,2} + r_{2,3}$$

$$t_{3,4} + r_{3,4}$$

view₃ consistent?

$$t_{4,1} + r_{1,4}$$

$$t_{4,2} + r_{2,4}$$

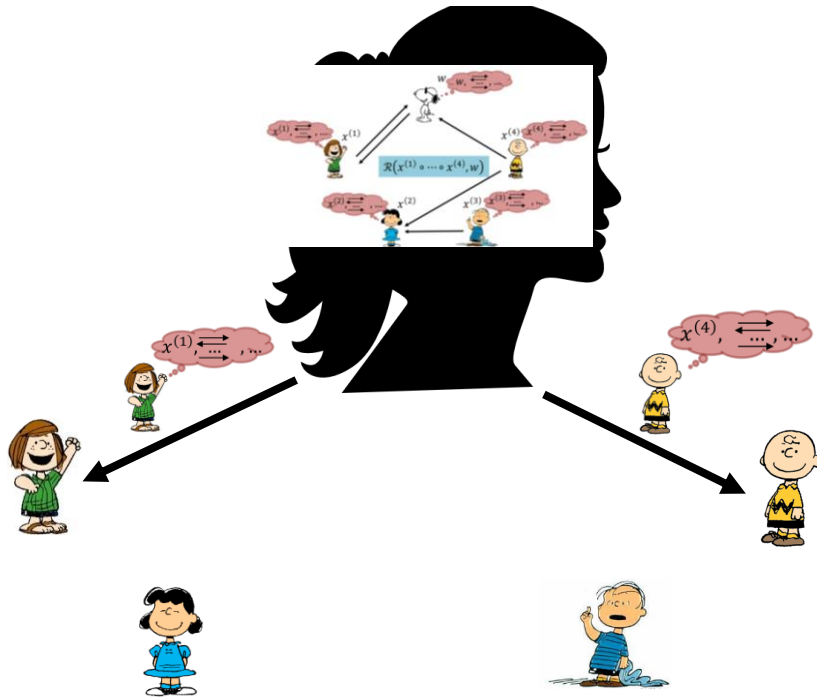
$$t_{4,3} + r_{3,4}$$

view₄ consistent?

MPC in the Head: Distributed vs. 2-Party

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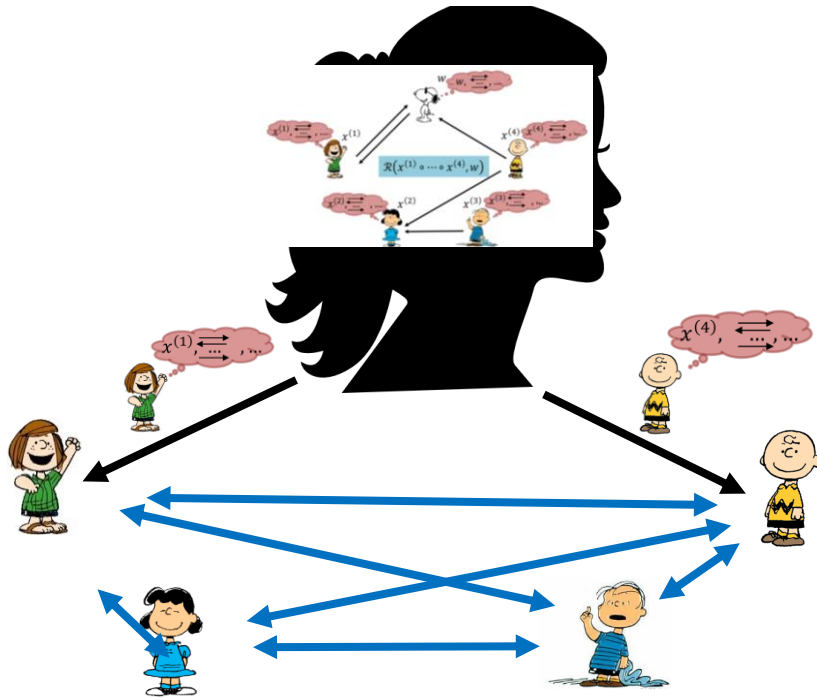
Distributed



MPC parties correspond to verifiers

MPC in the Head: Distributed vs. 2-Party

Distributed

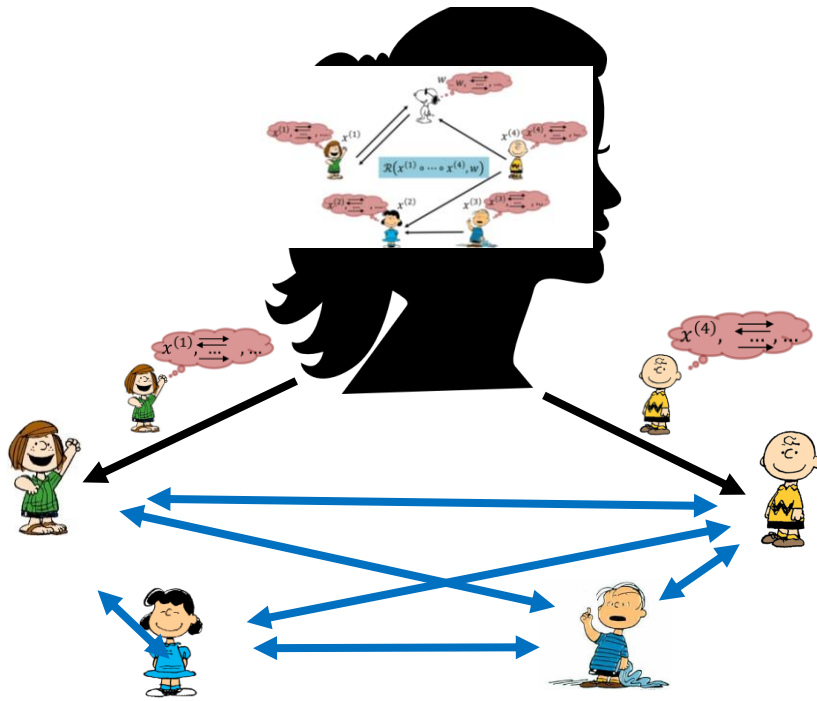


MPC parties correspond to verifiers

Entire execution trace checked

MPC in the Head: Distributed vs. 2-Party

Distributed



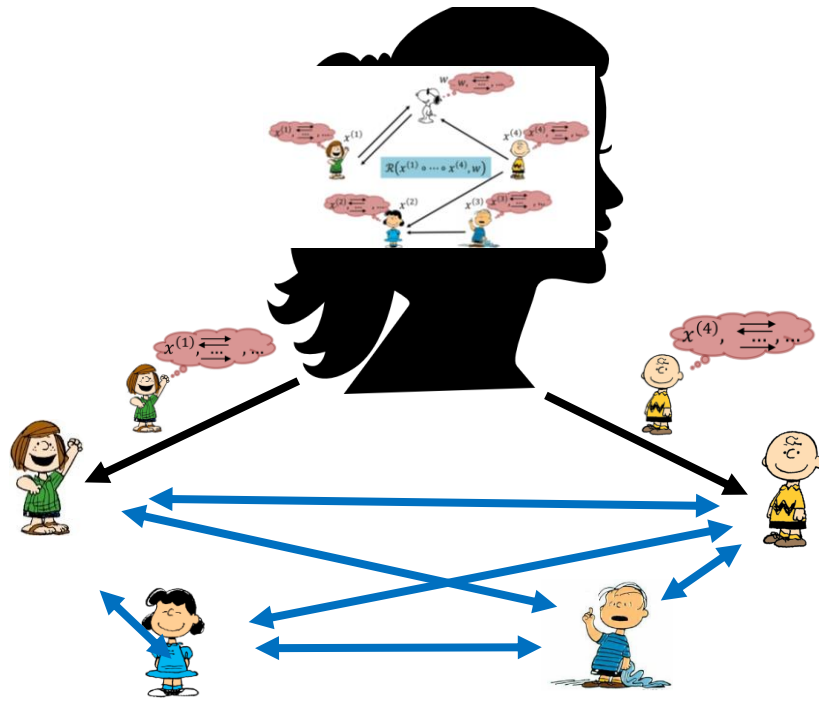
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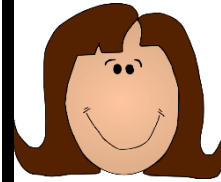
$negl(s)$ error, independent of
MPC parties

MPC in the Head: Distributed vs. 2-Party

Distributed



2-Party [IKOS07]



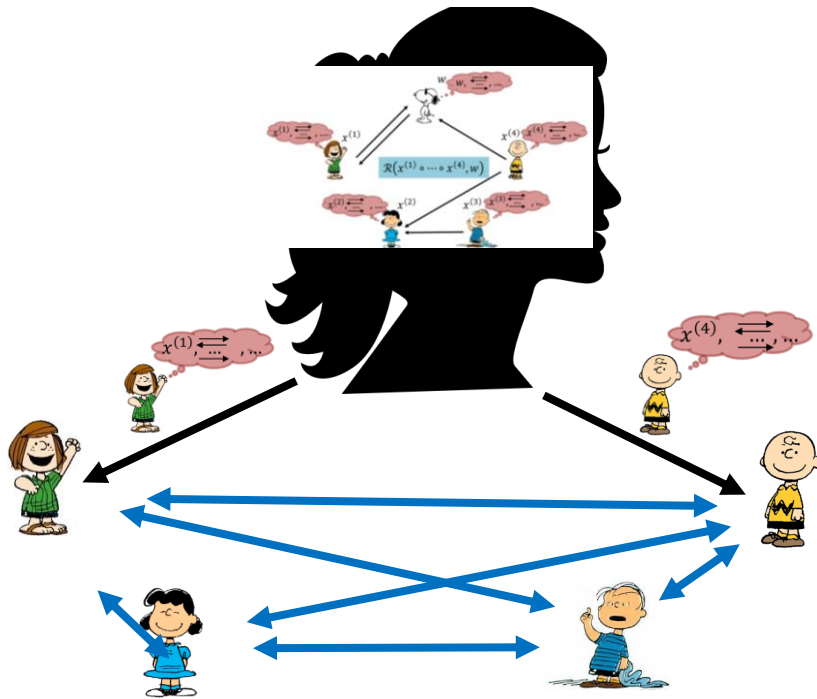
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Entire execution trace checked

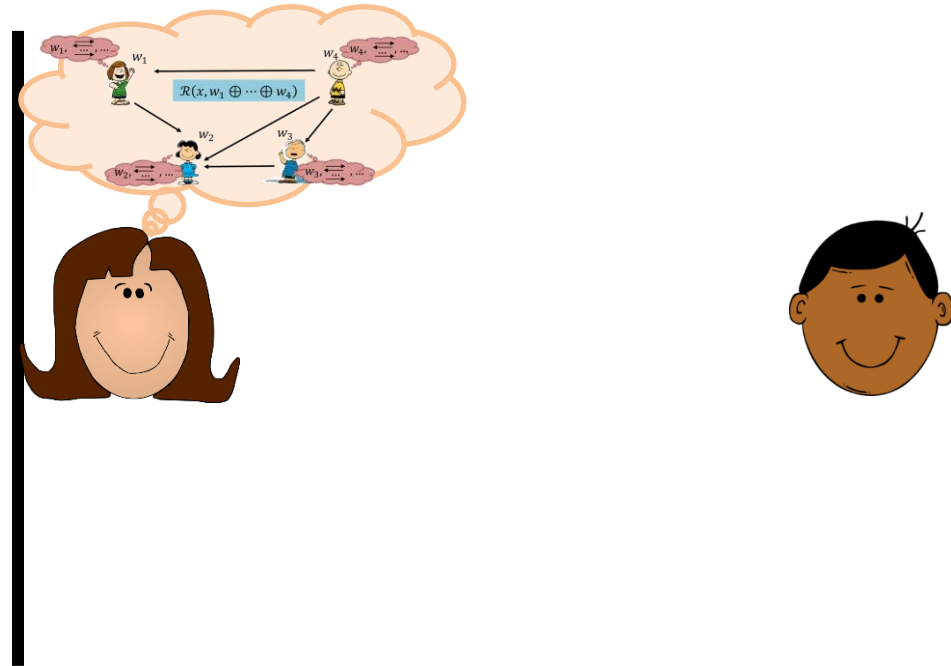
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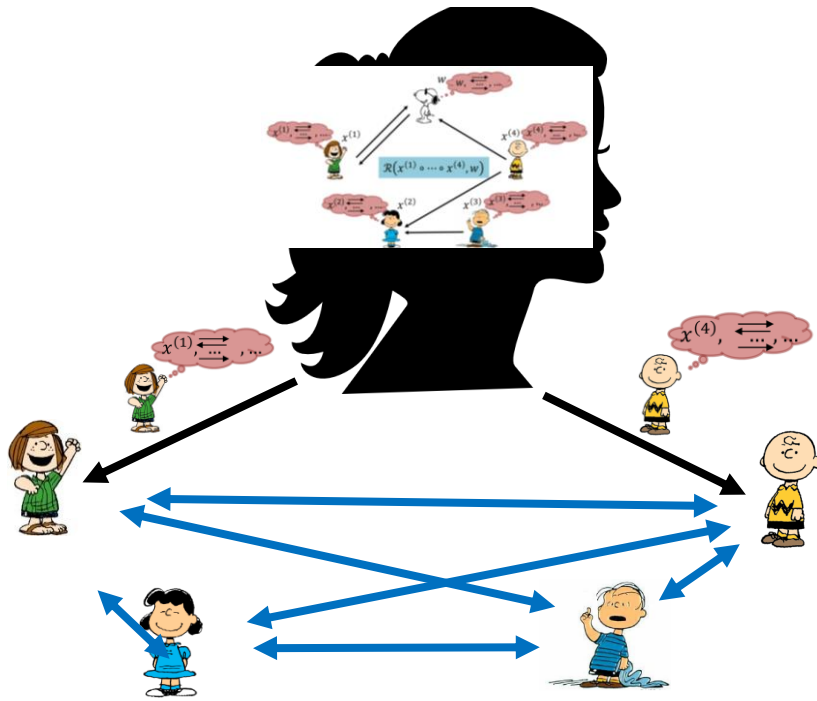
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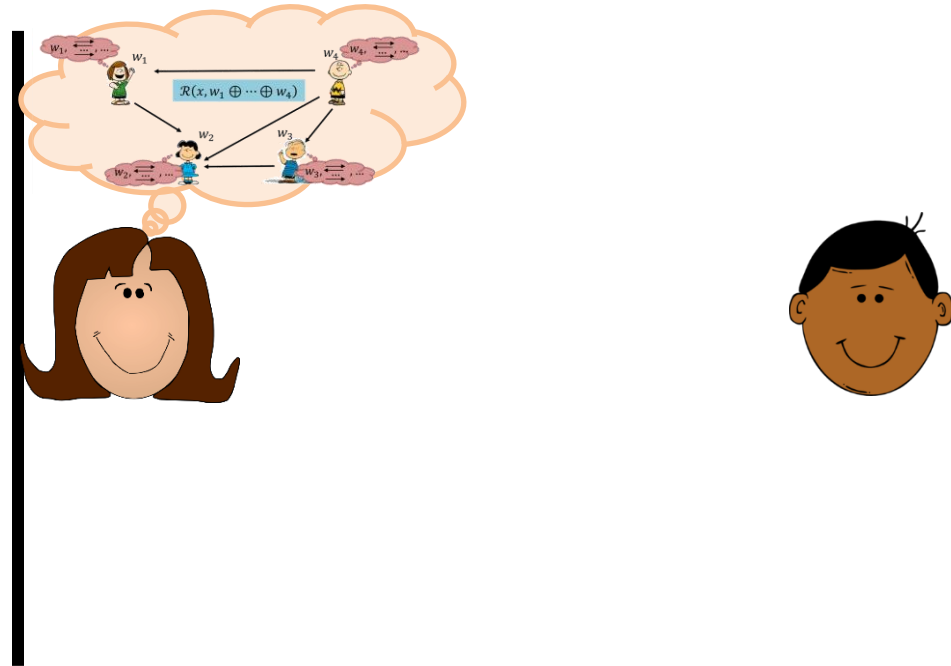
MPC parties are virtual

MPC in the Head: Distributed vs. 2-Party

Distributed



2-Party [IKOS07]



MPC parties correspond to verifiers

Entire execution trace checked

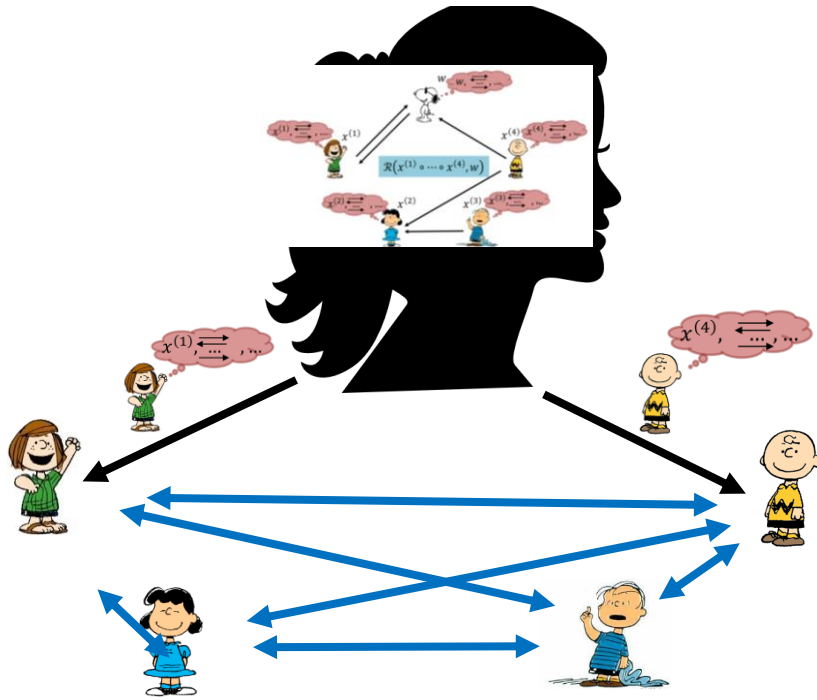
$negl(s)$ error, independent of
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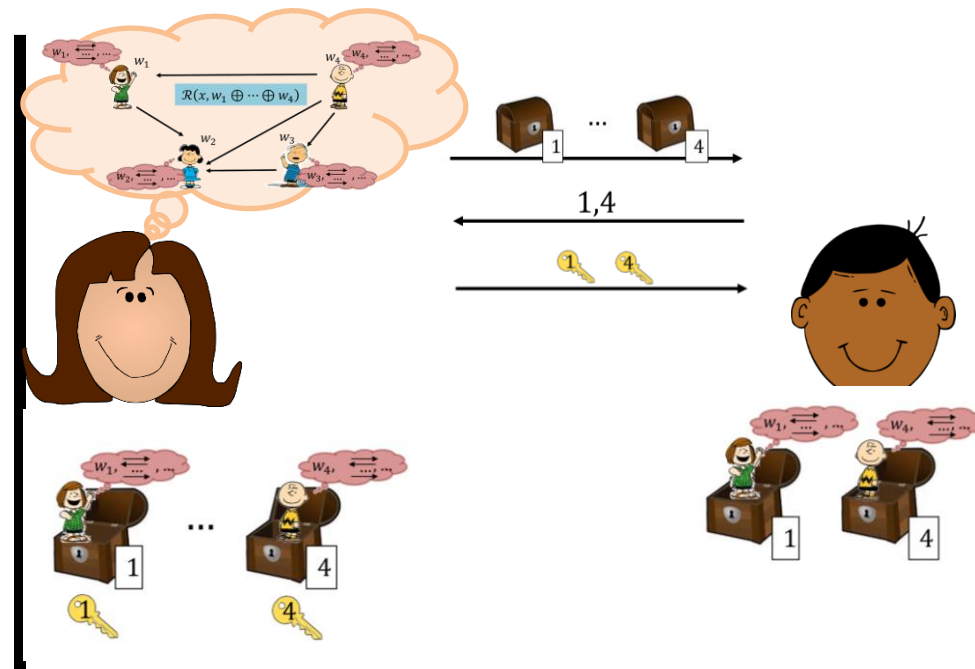
$negl(s)$ error with s MPC parties

MPC in the Head: Distributed vs. 2-Party

Distributed



2-Party [IKOS07]



MPC parties correspond to verifiers

Entire execution trace checked

$negl(s)$ error, independent of
MPC parties

MPC parties are virtual

Partial execution trace checked

$negl(s)$ error with s MPC parties

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# Rounds	Total proof length	Verification CC
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Thank you!