ZKFault: Fault Attack Analysis on Zero-Knowledge Based Post-Quantum Digital Signature Schemes

Puja Mondal, Supriya Adhikary, Suparna Kundu, and Angshuman Karmakar

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NIST's Additional Digital Signature

PKE and KEM	Signatures
CRYSTALS-Kyber	CRYSTALS-Dilithium
	FALCON
	SPHINCS+

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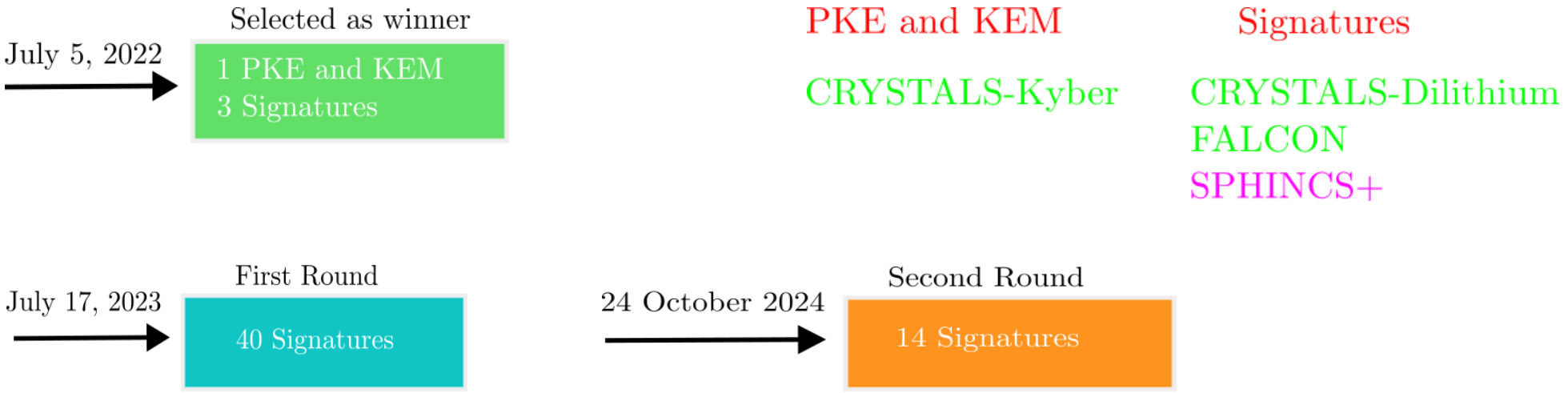
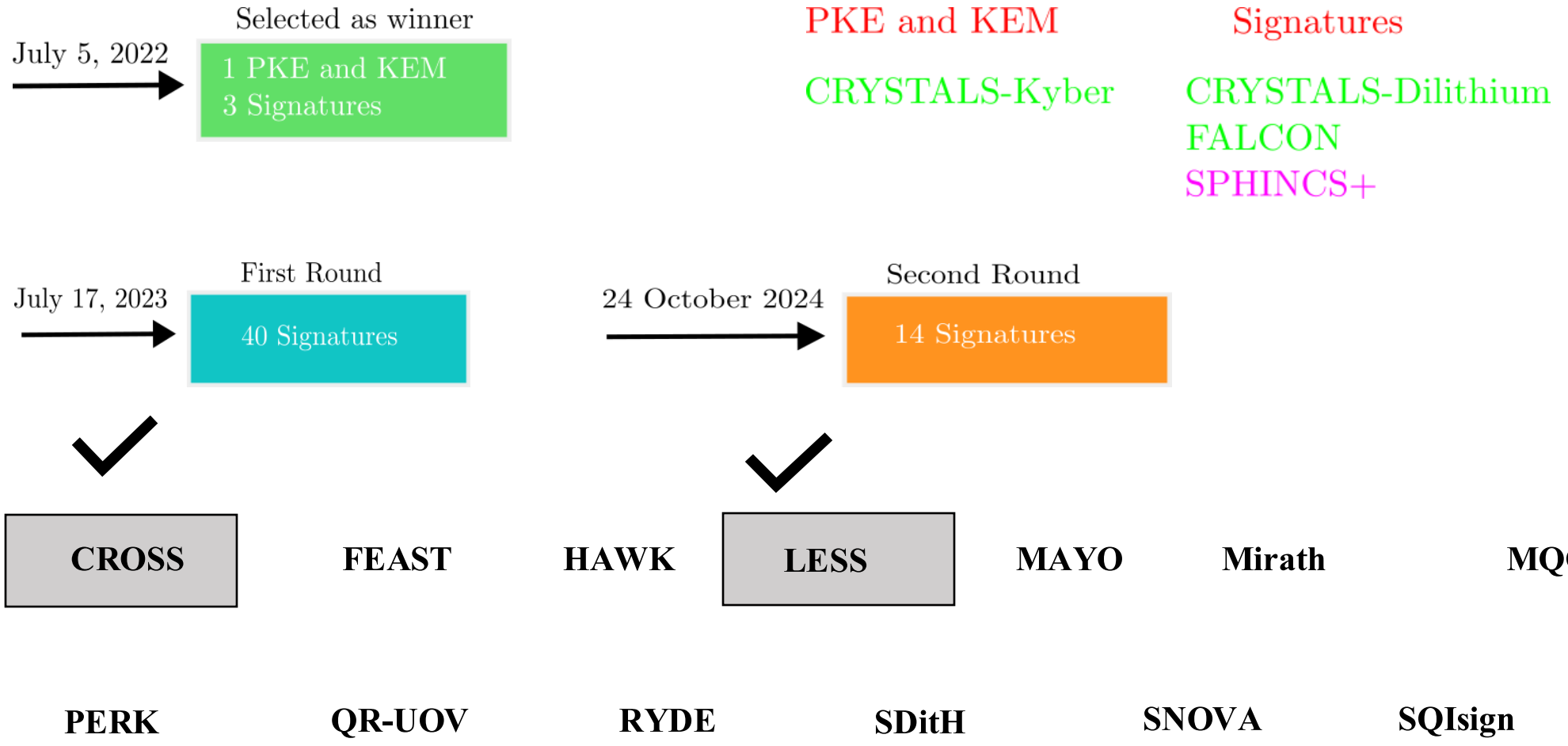


CROSS **FEAST** **HAWK** **LESS** **MAYO** **Mirath** **MQOM**

PERK **QR-UOV** **RYDE** **SDitH** **SNOVA** **SQIsign** **UOV**

NIST's Additional Digital Signature



Interactive-Zero-Knowledge (ZK) Framework

Prover **Verifier**

Interactive-Zero-Knowledge (ZK) Framework

Prover

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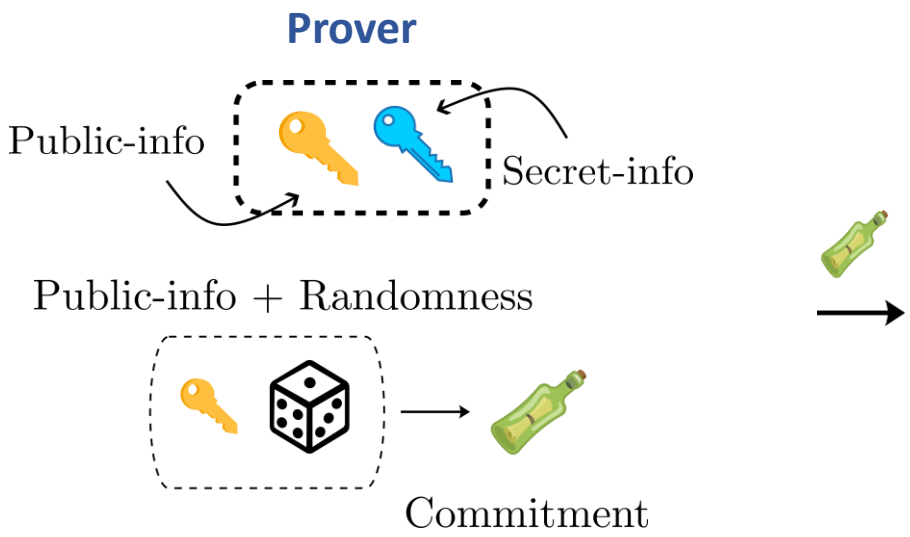

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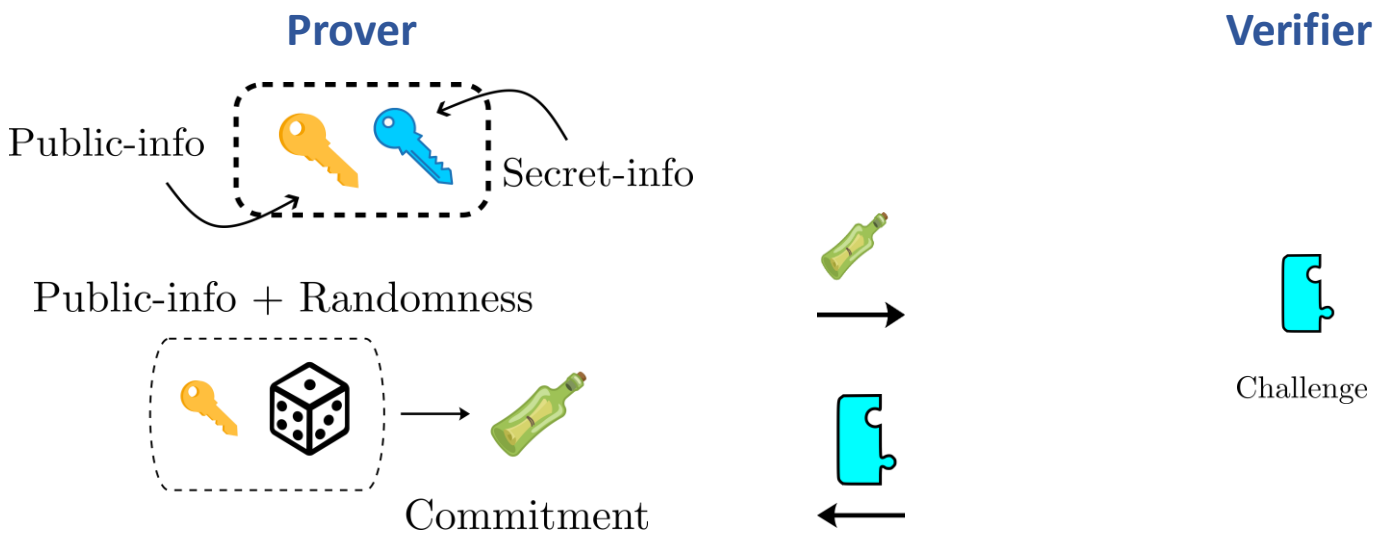

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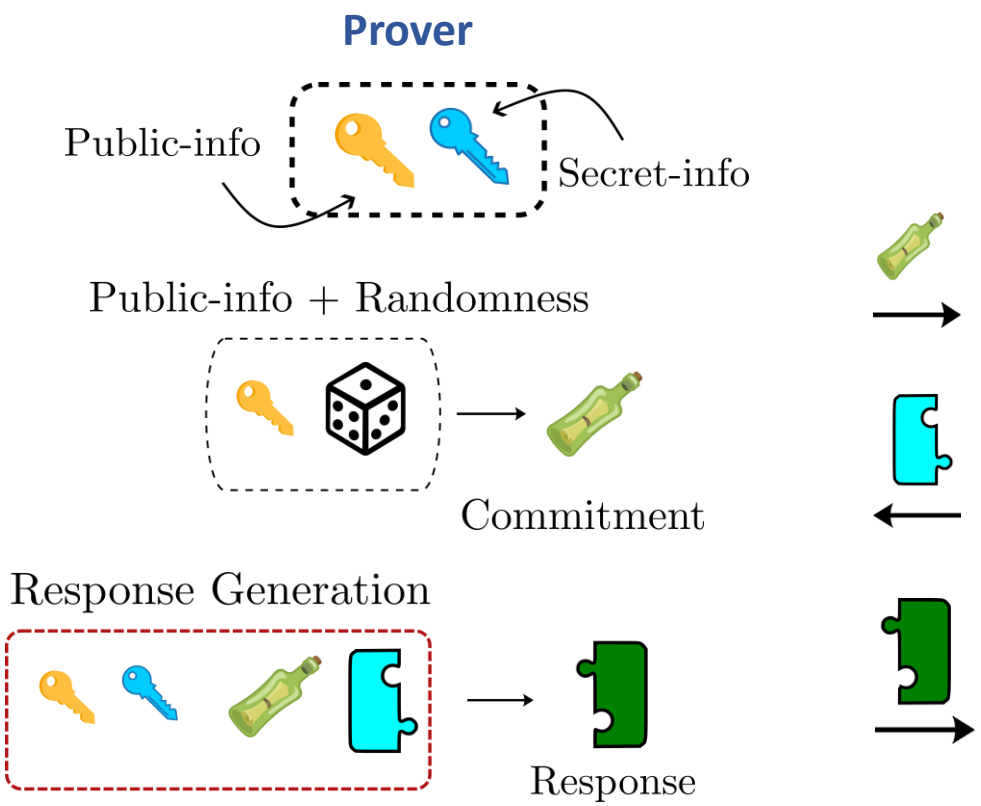

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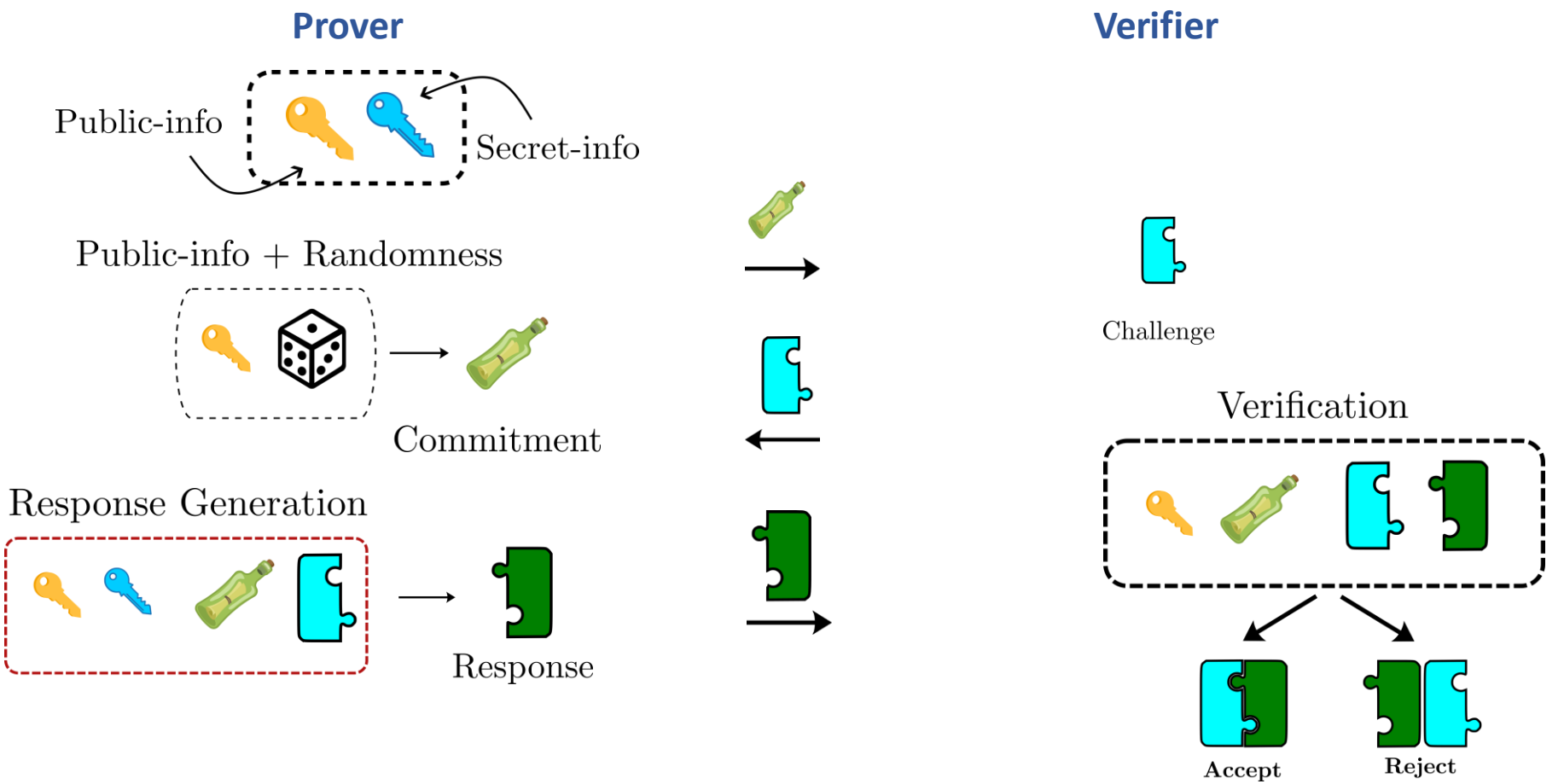
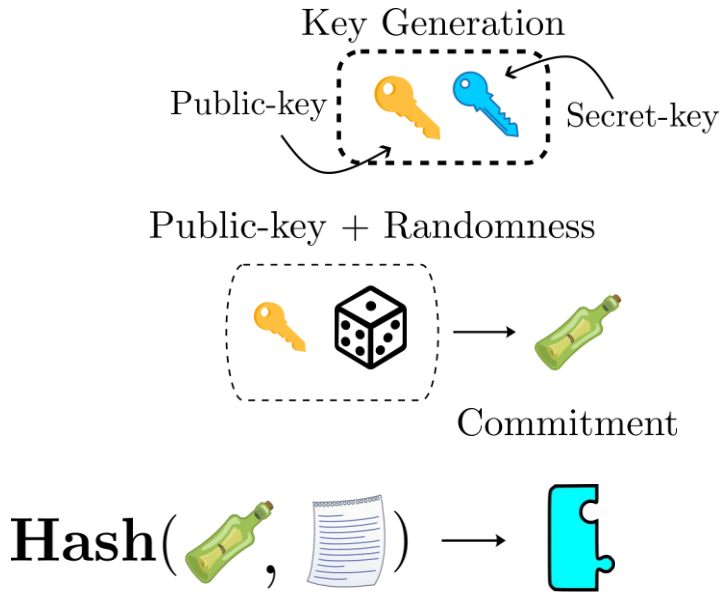


ZK with Fiat-Shamir Transformation

Signer



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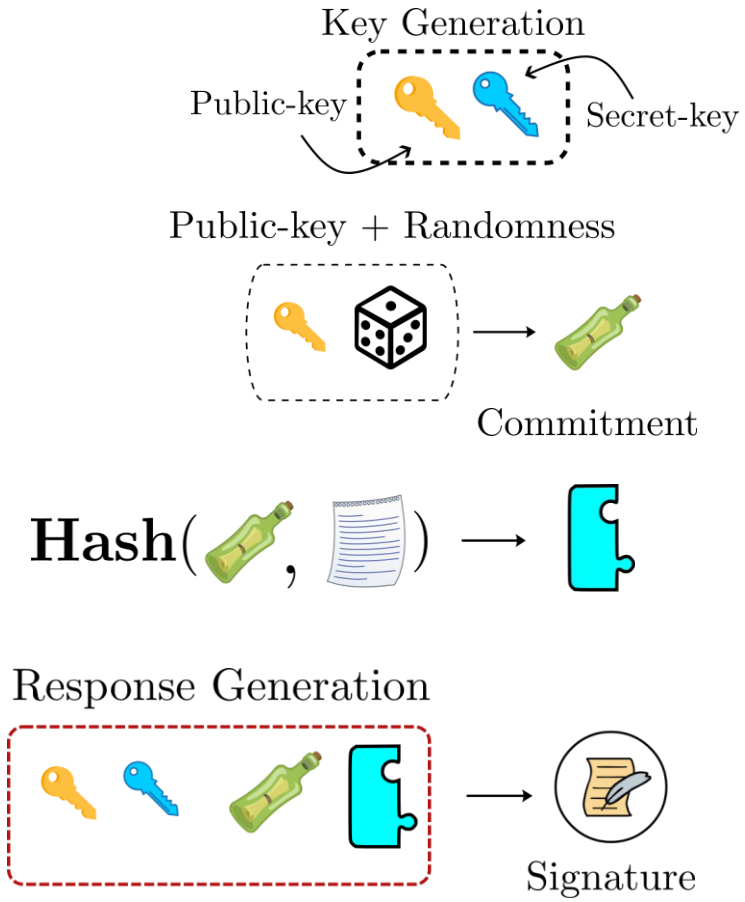

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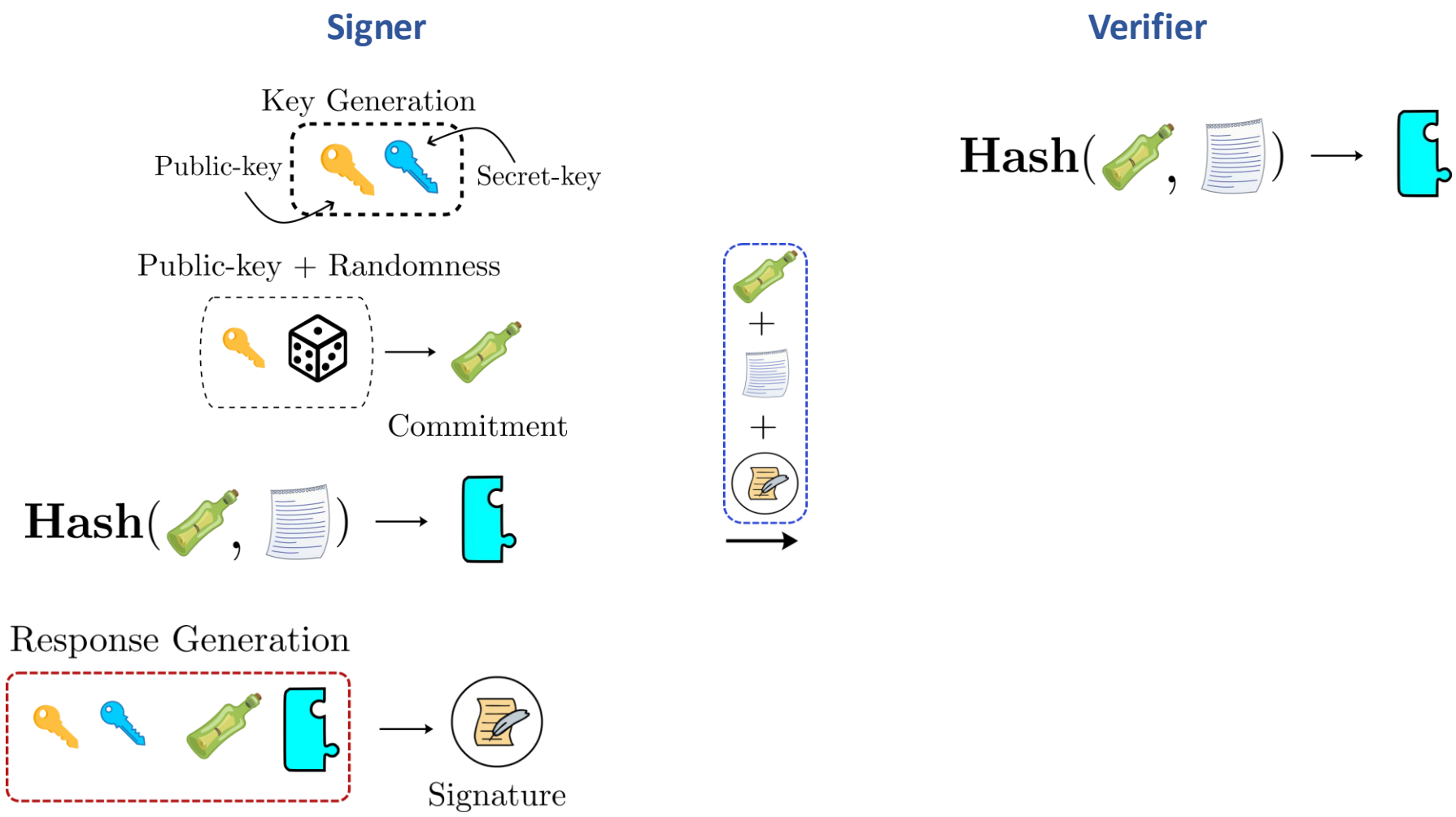

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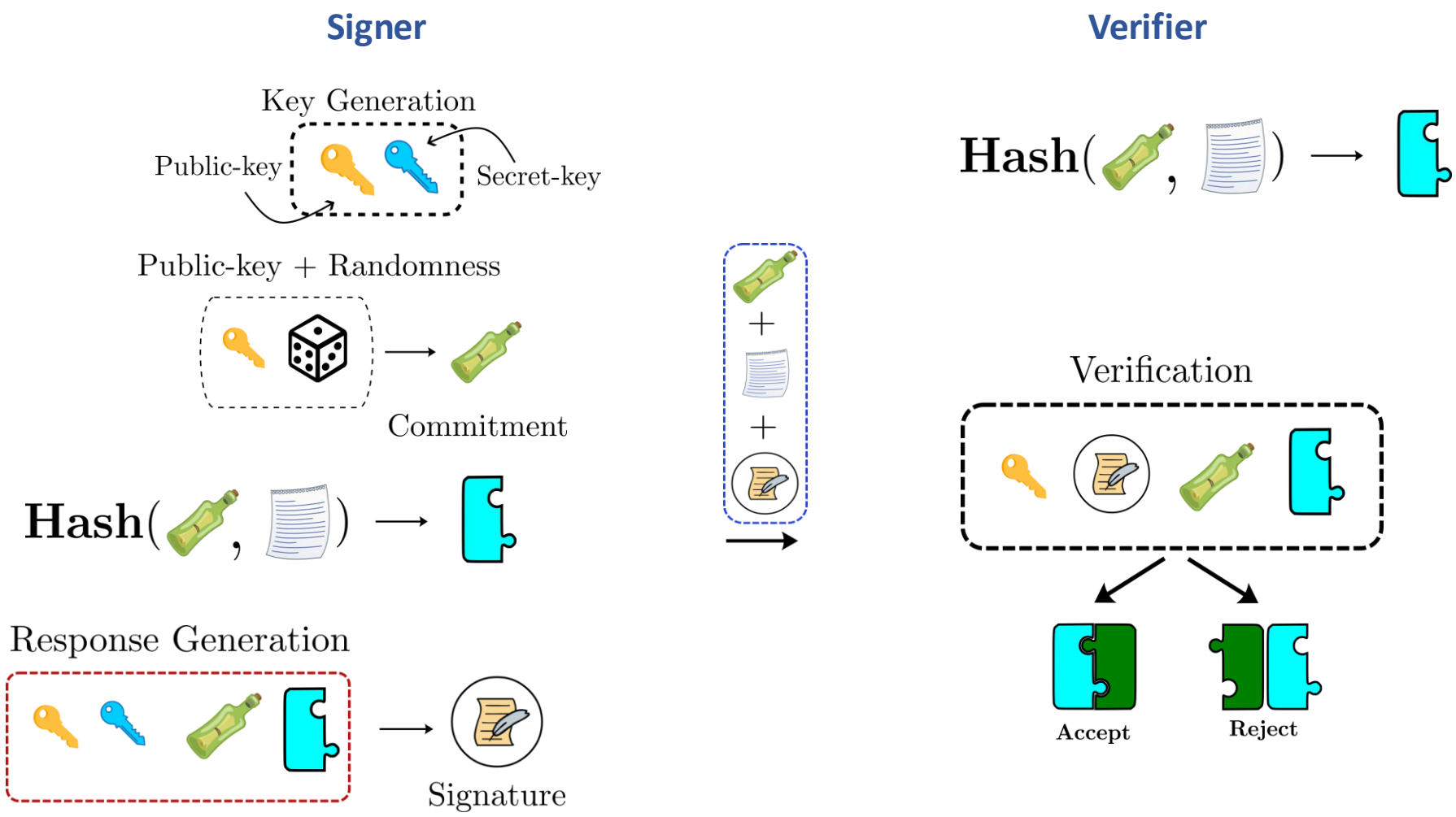

LESS

Signer **Verifier**

🔧 : $\boldsymbol{Q}_1, \boldsymbol{Q}_2, \cdots, \boldsymbol{Q}_s$

🔑 : $\boldsymbol{G}_0, \boldsymbol{G}_1 = S(\boldsymbol{G}_0\boldsymbol{Q}_1), \boldsymbol{G}_2, \cdots, \boldsymbol{G}_s$

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$\textbf{Sample} : \boldsymbol{Q}'_1, \boldsymbol{Q}'_2, \cdots, \boldsymbol{Q}'_t$

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🍾 : $\mathbf{Hash}\left(\boldsymbol{G}'_1, \boldsymbol{G}'_2, \cdots, \boldsymbol{G}'_t\right)$

Commitment

Challenge

$\mathbf{Hash}($ 🍾 , 📄 $) \longrightarrow$ 🧩 : $\mathbf{c_1}, \mathbf{c_2}, \cdots, \mathbf{c_t} \in \{\mathbf{0}, \cdots, \mathbf{s}\}$

LESS

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$: Q_1, Q_2, \cdots, Q_s$

$: G_0, G_1 = S(G_0 Q_1), G_2, \cdots, G_s$

$\textbf{Sample} : Q'_1, Q'_2, \cdots, Q'_t$

$G'_1 = S(G_0 Q'_1), G'_2, \cdots, G'_t$

$: \textbf{Hash}(G'_1, G'_2, \cdots, G'_t)$

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$\mathbf{c}_i \neq \mathbf{0}$: $Q_{\mathbf{c}_i}^{-1} Q'_i$

$: R_i$

$\mathbf{c}_i = \mathbf{0}$: Q'_i

LESS

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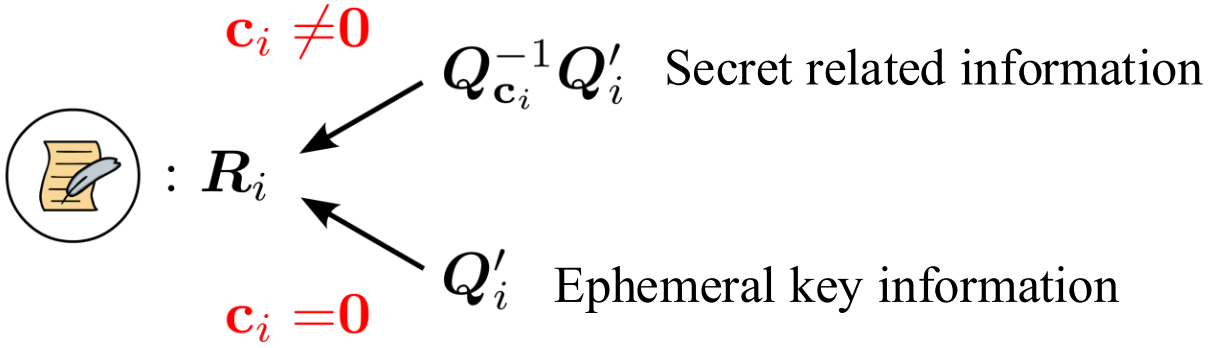
$$\mathbf{Hash}(\text{🍾}, \text{📄}) \longrightarrow \text{🧩}$$

$$G'_i = S(G_{\mathbf{c}_i} R_i)$$

$$\mathbf{Check}:$$

$$\text{🍾} = \mathbf{Hash}(G'_1, G'_2, \cdots, G'_t)$$

Target of Our Fault Attack



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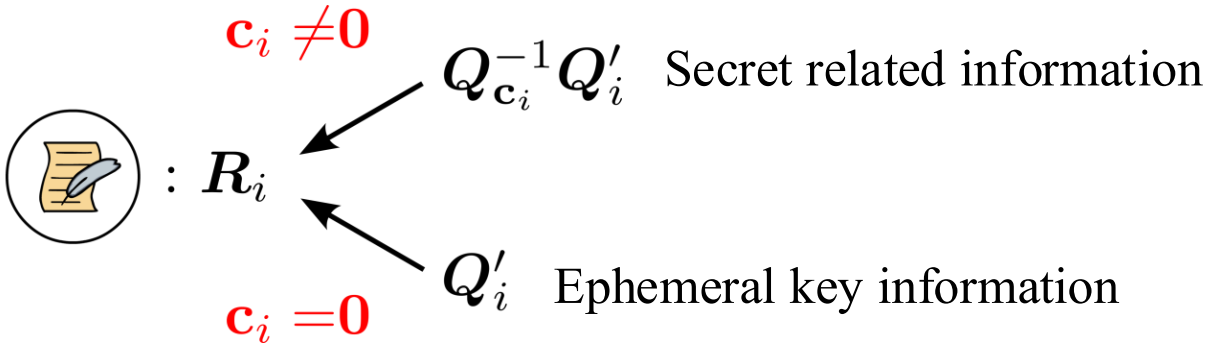

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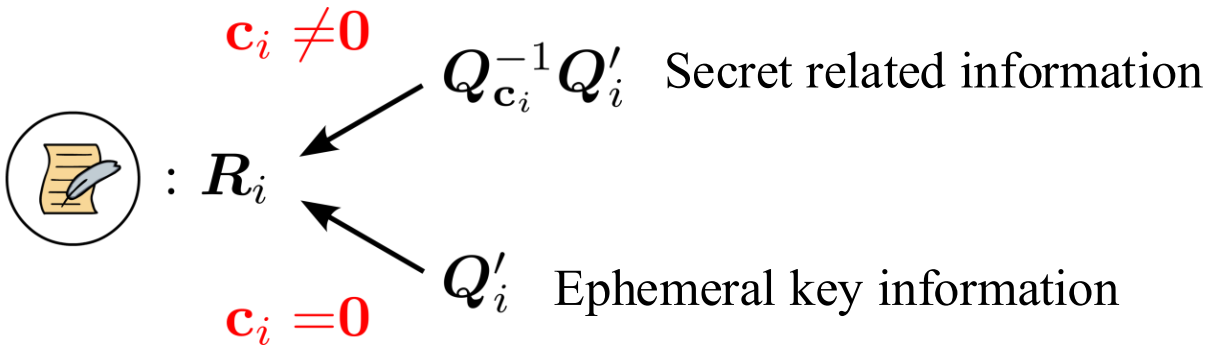

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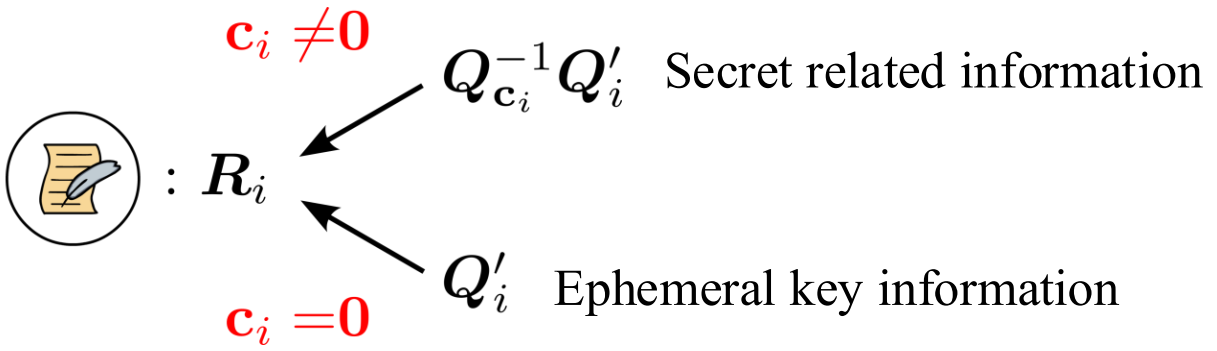

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Target

Get a pair $(\mathbf{Q'_i, Q^{-1}_{ci}Q'_i})$

Fault Assumption and Result

- Our fault assumption is we can change the value of a location from 1 to 0

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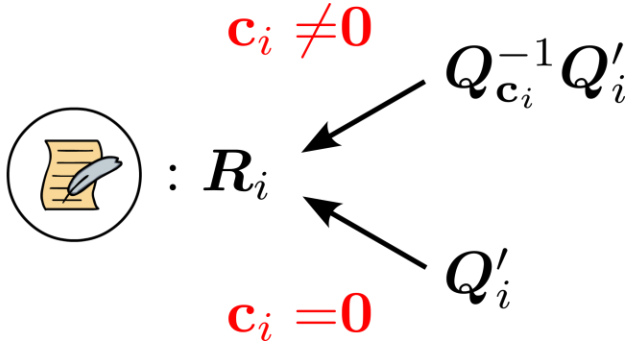
Scheme name	Security level	Parameter set	Required faults for complete secret recovery
LESS	1	Less-1b	**1**
		Less-1i	**1**
		Less-1s	**2**
	3	Less-3b	**1**
		Less-3s	**1**
	5	Less-5b	**1**
		Less-5s	**1**
CROSS	1, 3, 5	CROSS-R-SDP	**1**
		CROSS-R-SDPG	**1**

Overview of LESS



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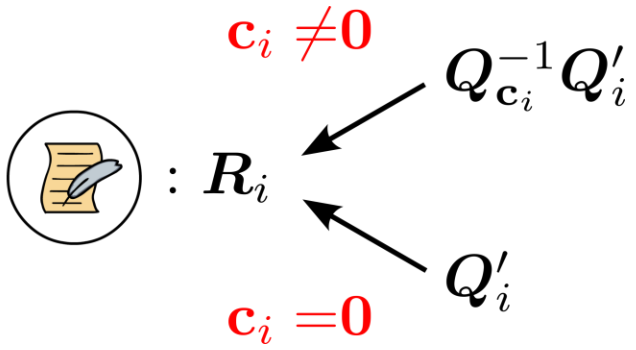
- Each $\mathbf{Q'_i}$ is generated from a random seed $\mathbf{seed_i}$



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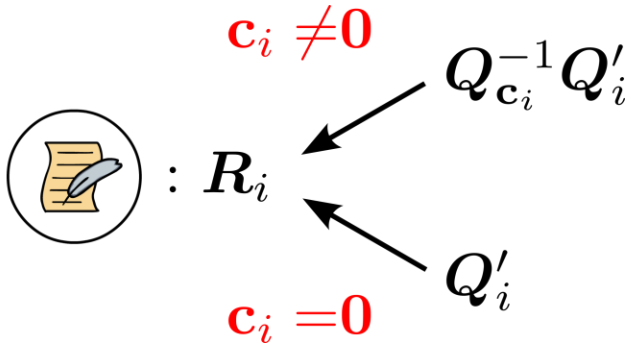

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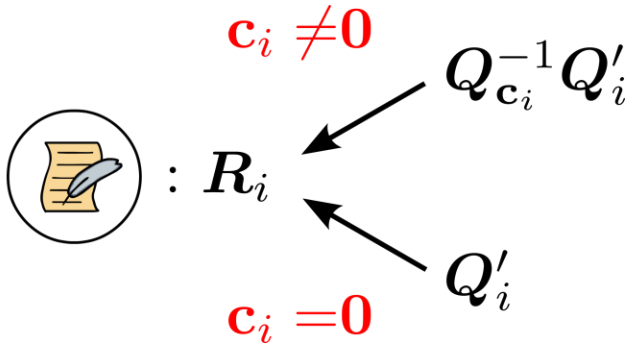

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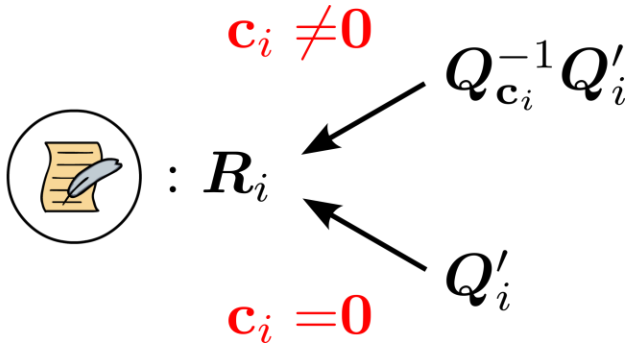
- For parameter, LESS-5b signature size 74960 Bytes



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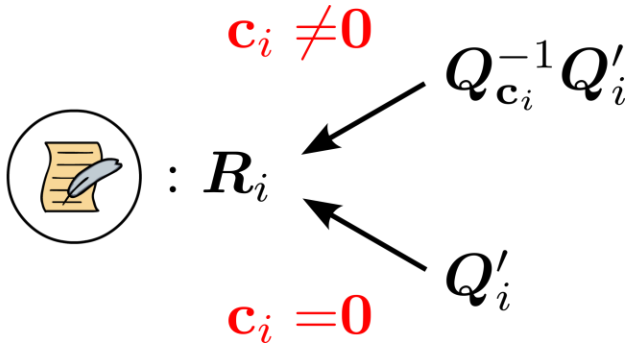

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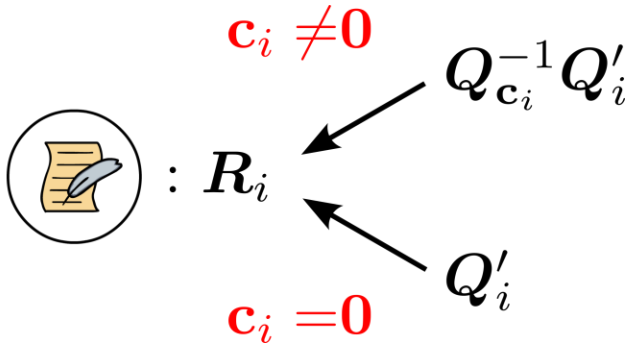
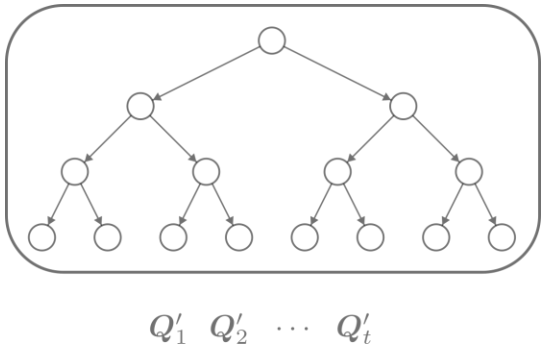
- Compressed signatures size: ~32500 Bytes (~57% reduced)



Summary of Signature Compression

Step 1

Generate a GGM tree (seedtree)
and generate all the ephimeral
keys Q_1', Q_2', … ,Q_t'



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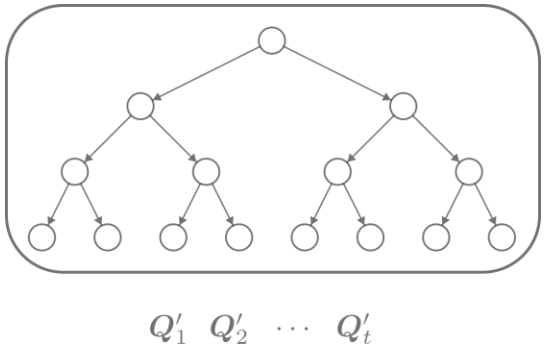
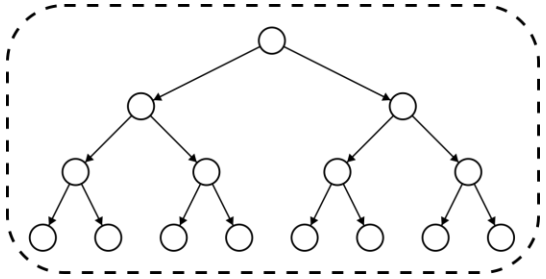


Step 2

Generate a reference tree based on the challenge



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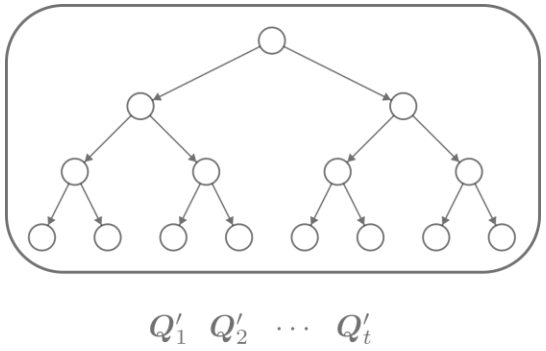

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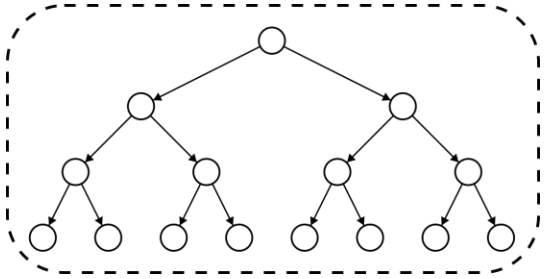
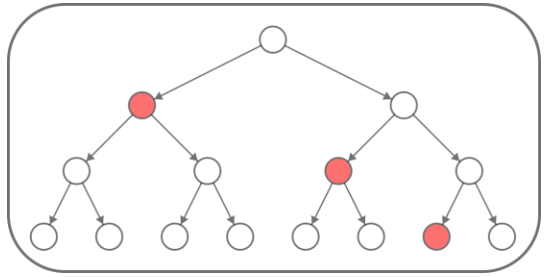


Step 3

Decide the nodes of the seedtree to be published based on reference tree



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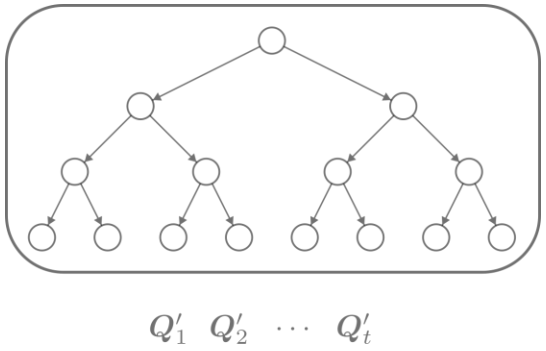

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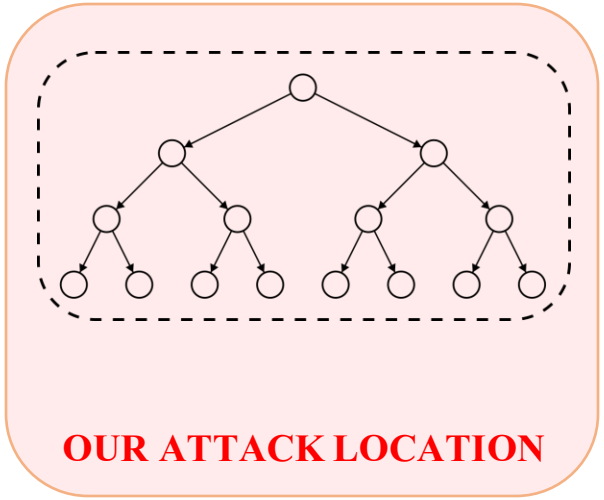

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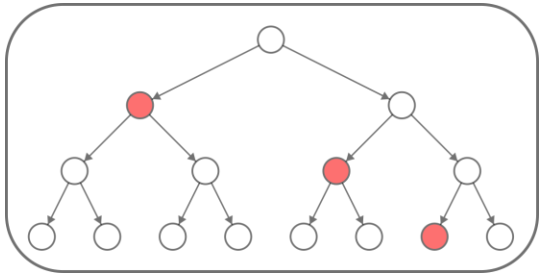

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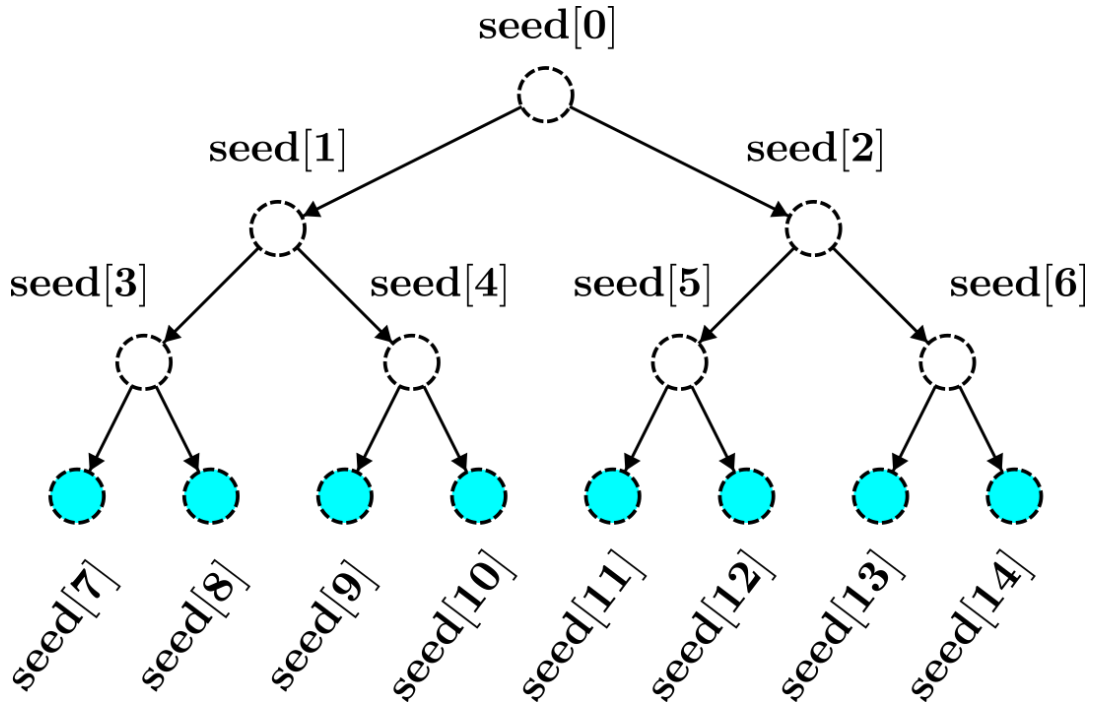

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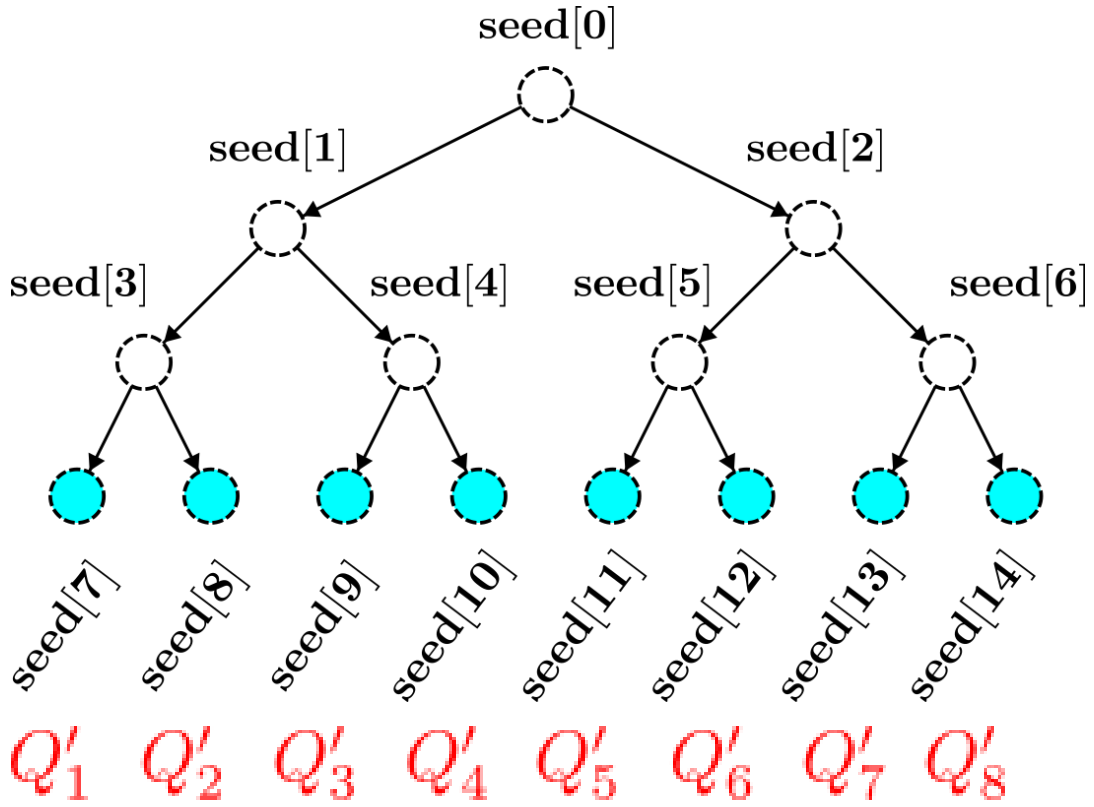
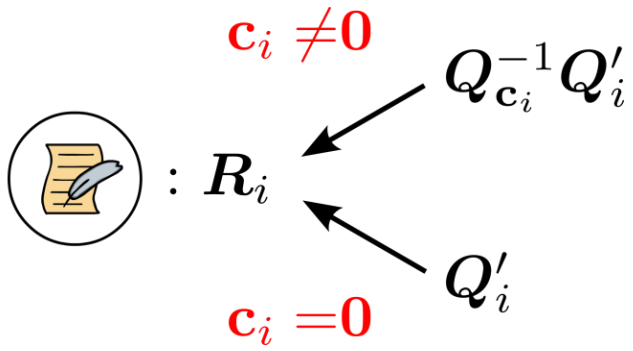


Compression Technique



Suppose **c=(0,0,0,0,1,0,0,2)**

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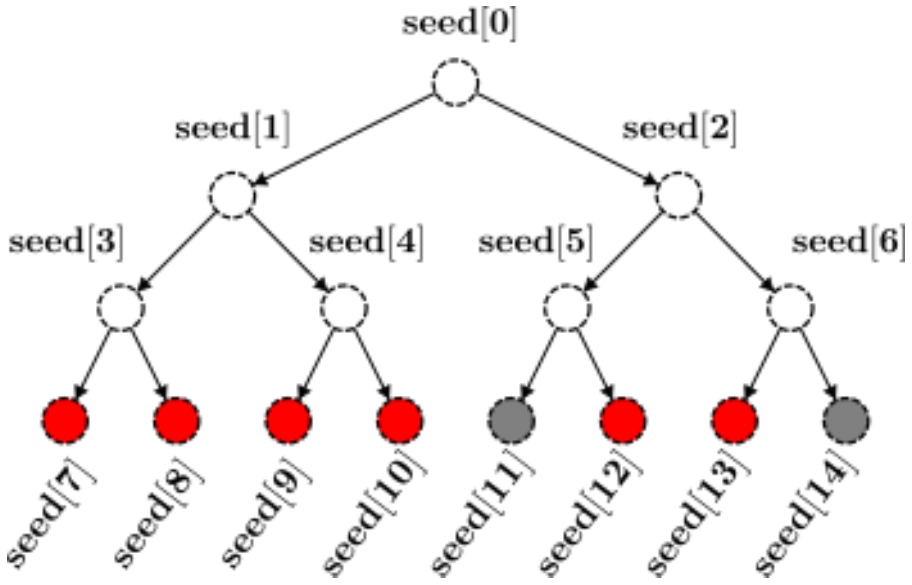

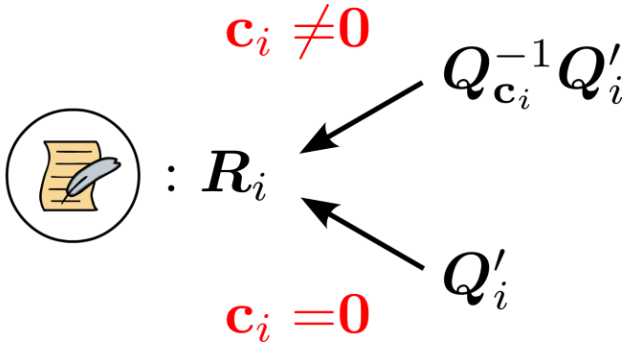

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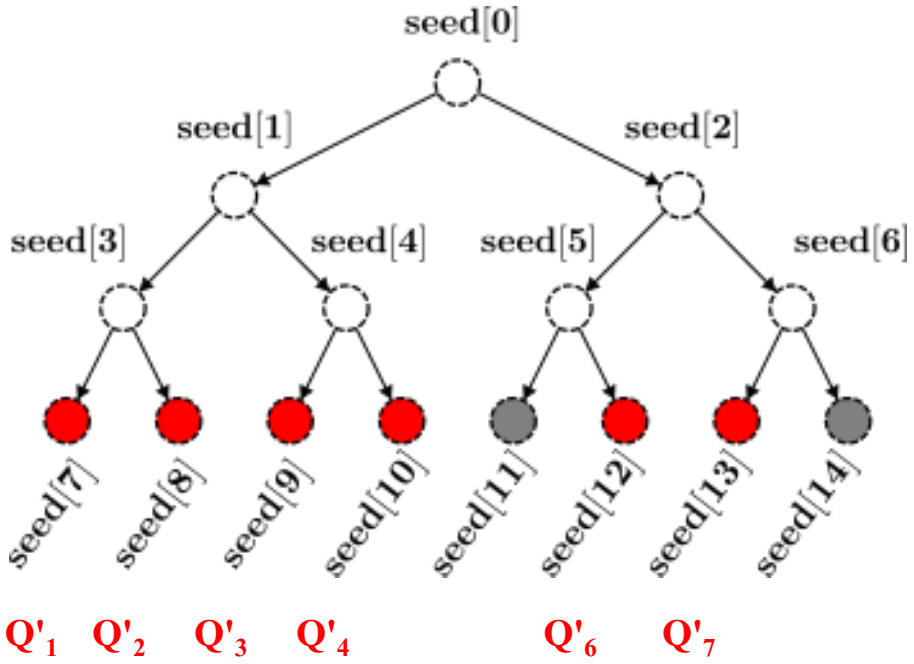

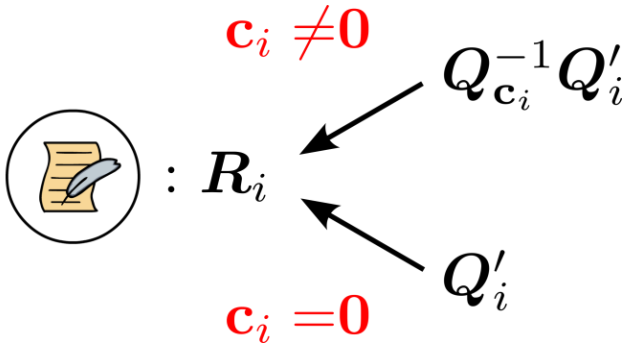

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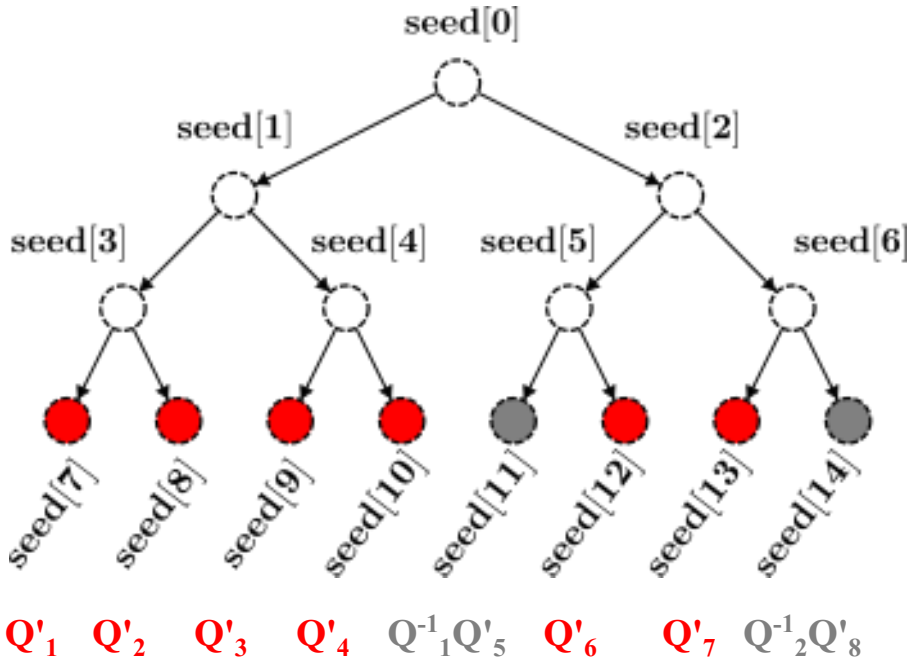

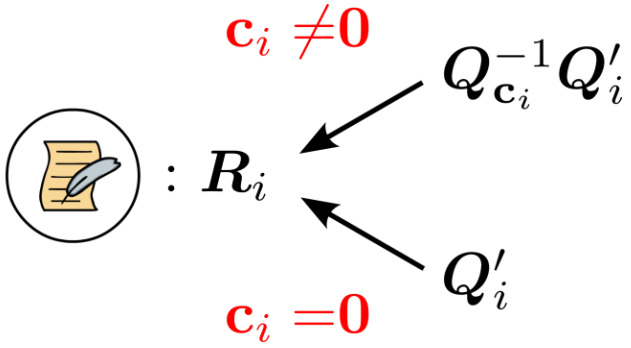

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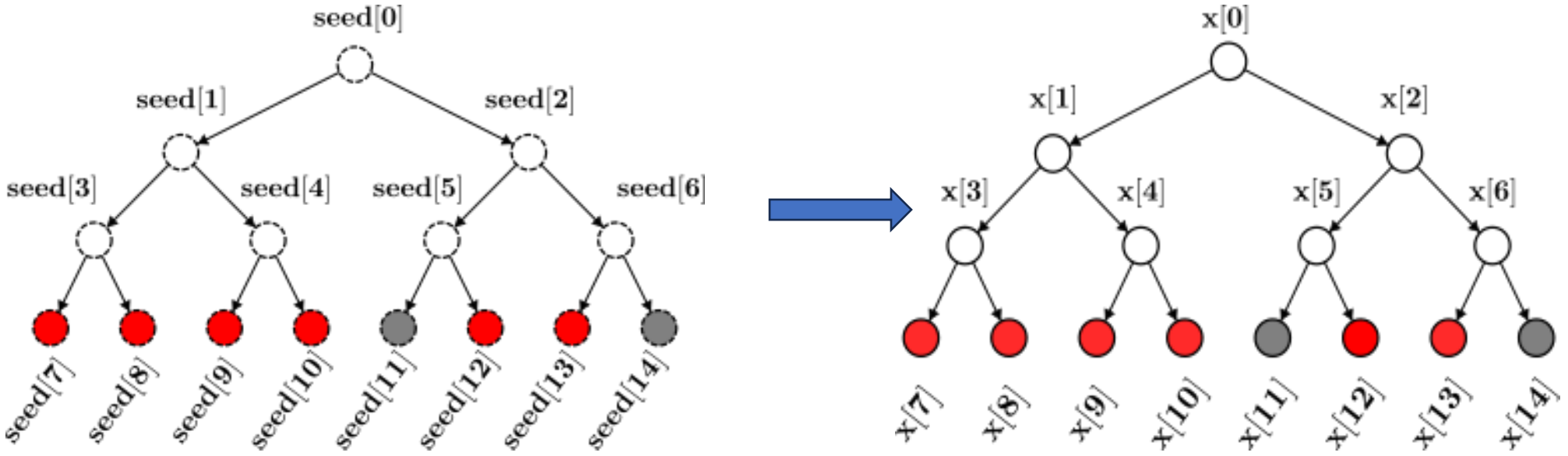
● : to publish **Q'$_i$**, ● : to hide **Q'$_i$**

Compression Technique



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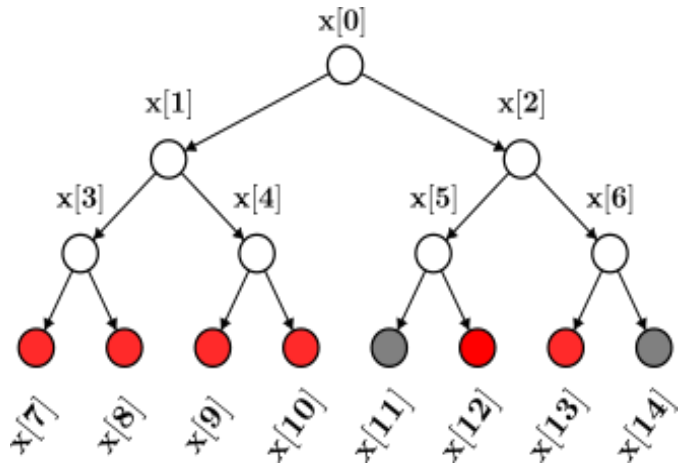

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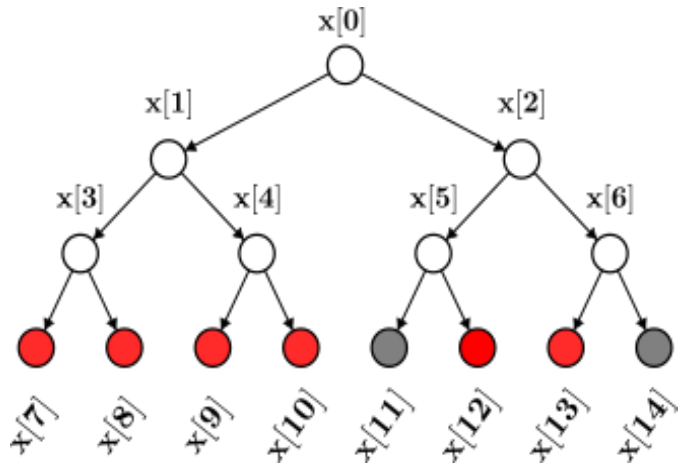

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i-th node: ● if both children are ●

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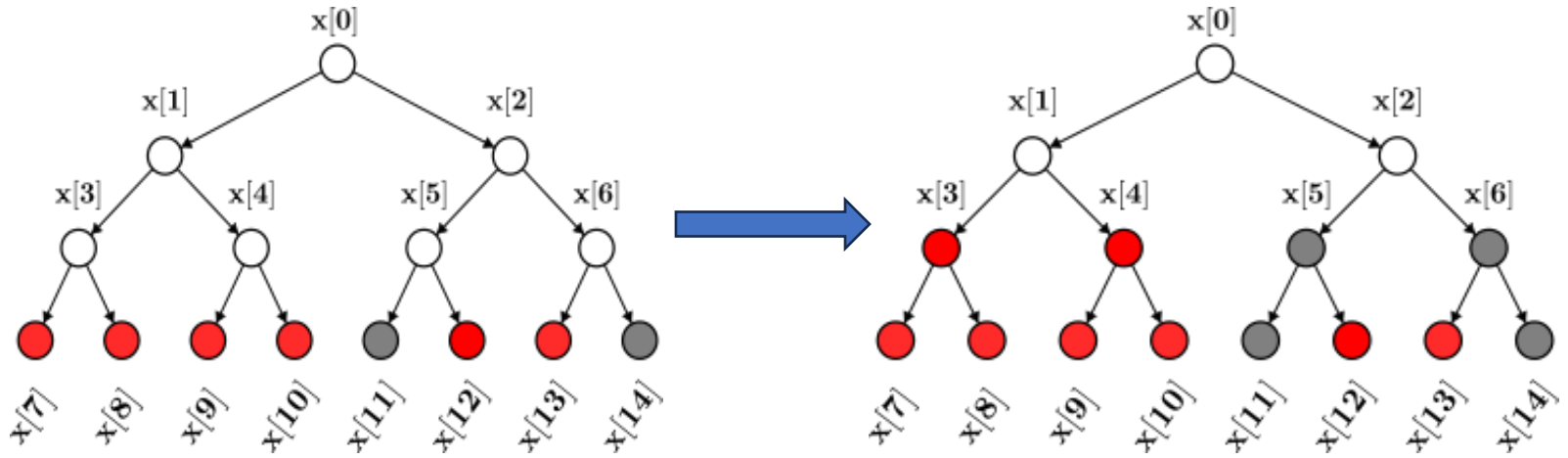

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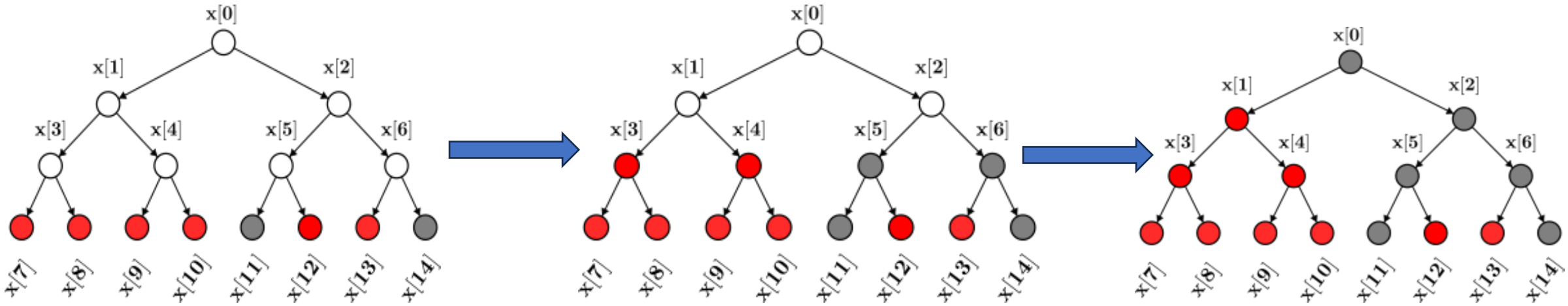

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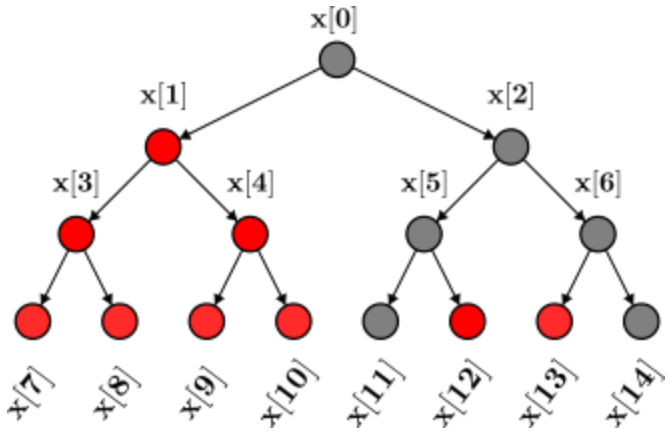

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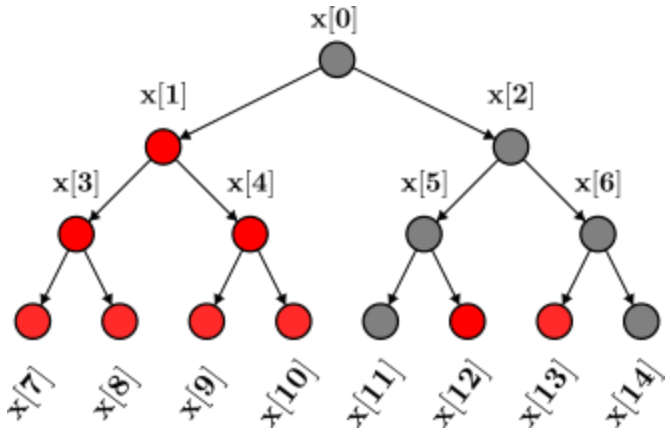

● : to publish $\mathbf{Q'}_i$, ● : to hide $\mathbf{Q'}_i$

Check: i-th node: ● and its parent: ● ?

If yes: publish seed[i]

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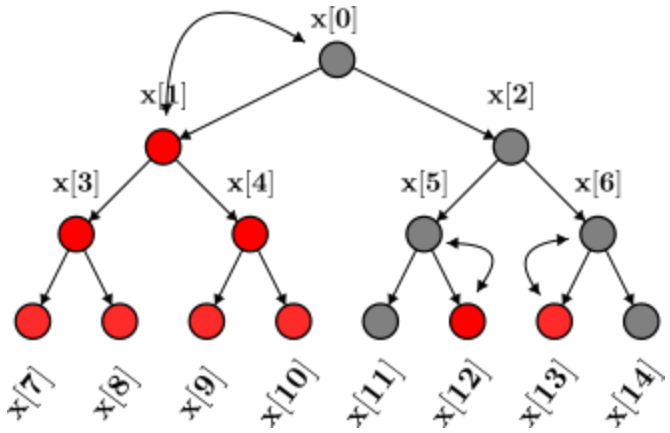

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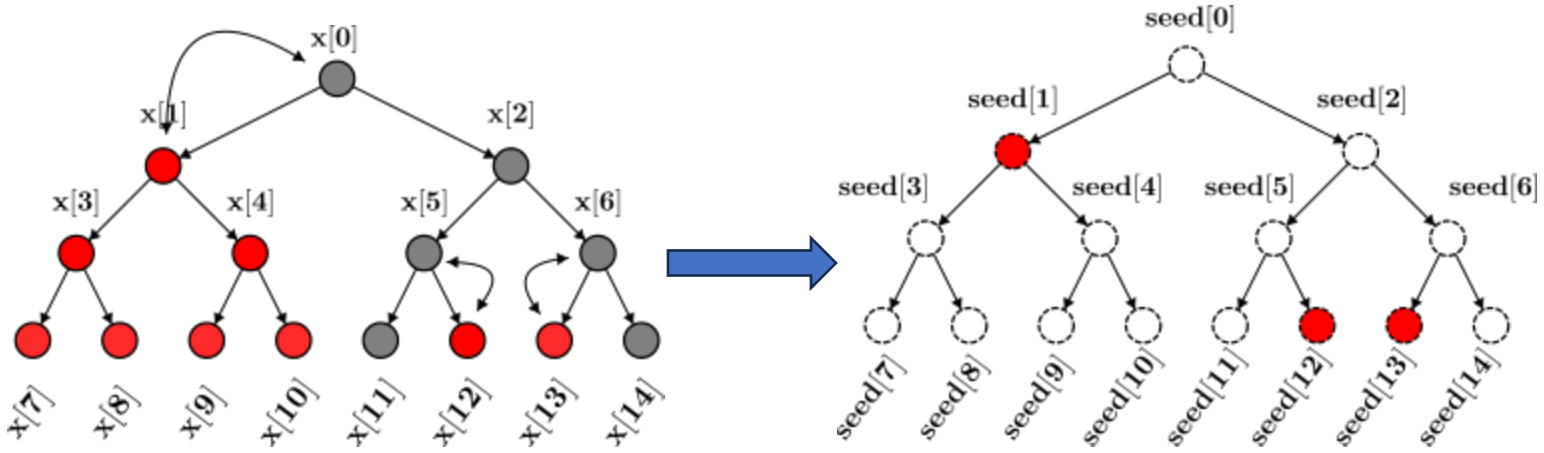

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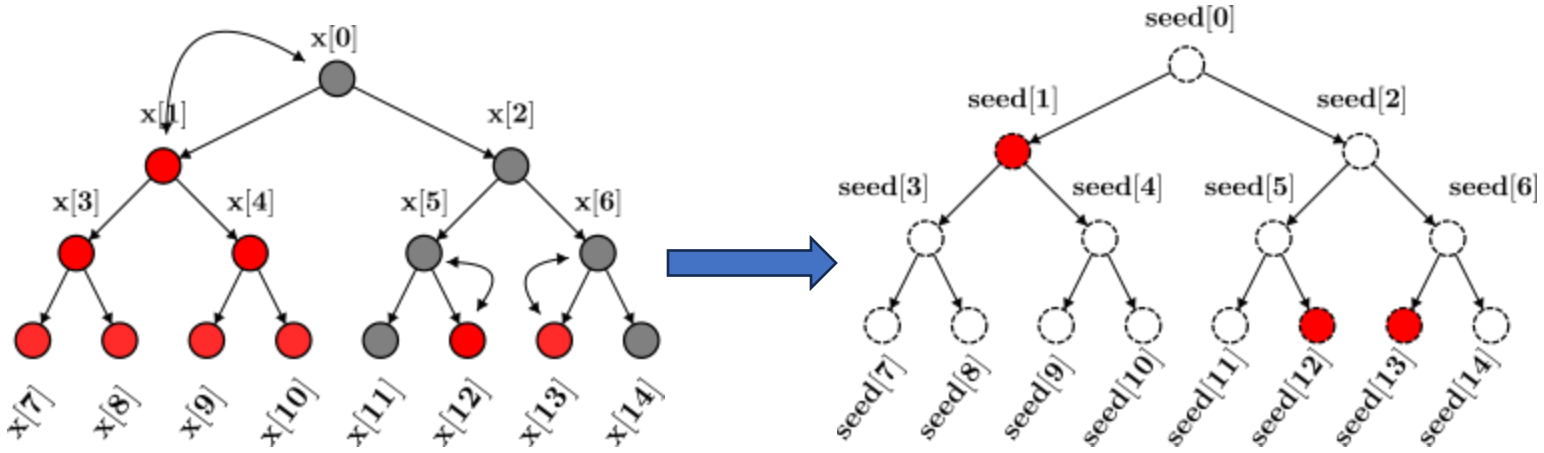

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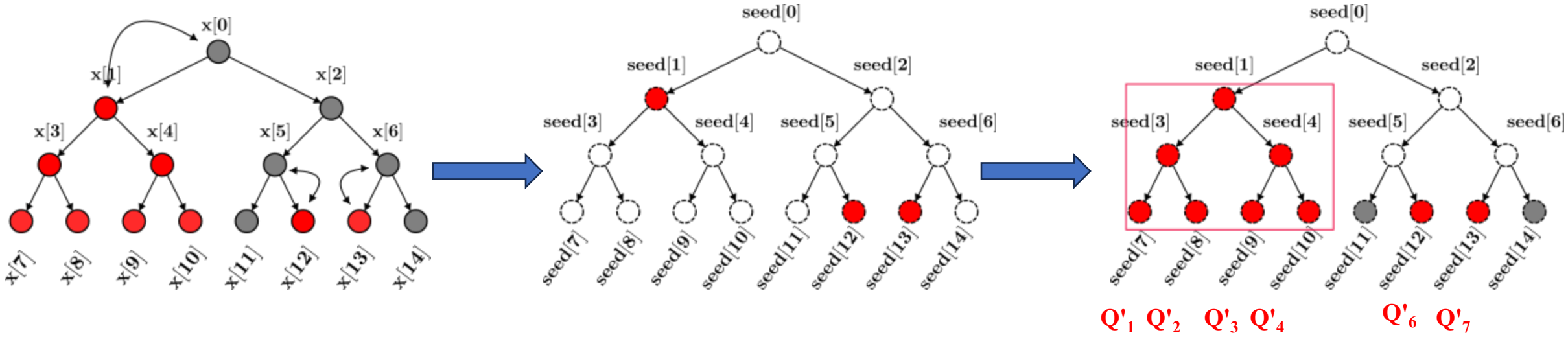

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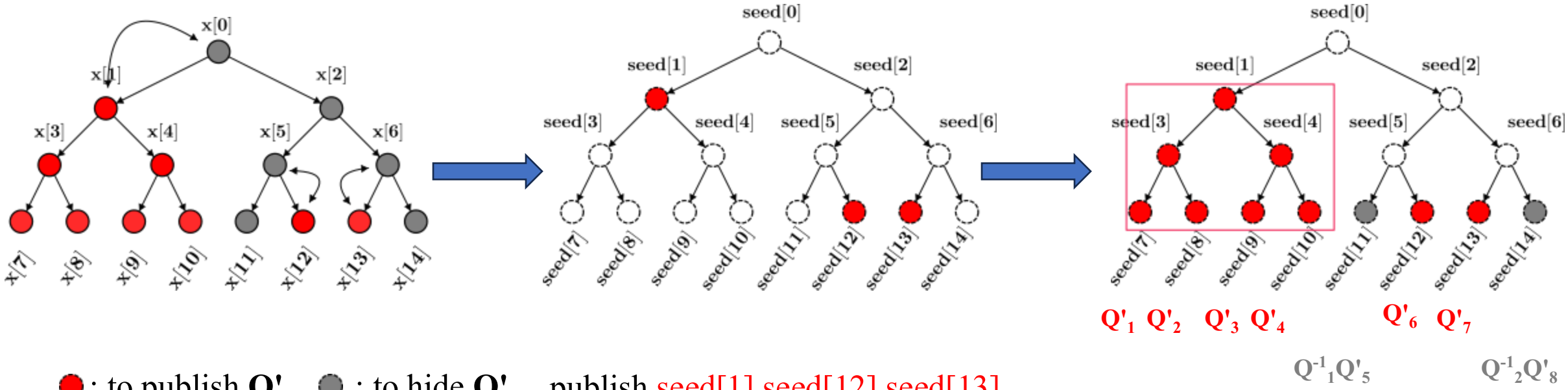

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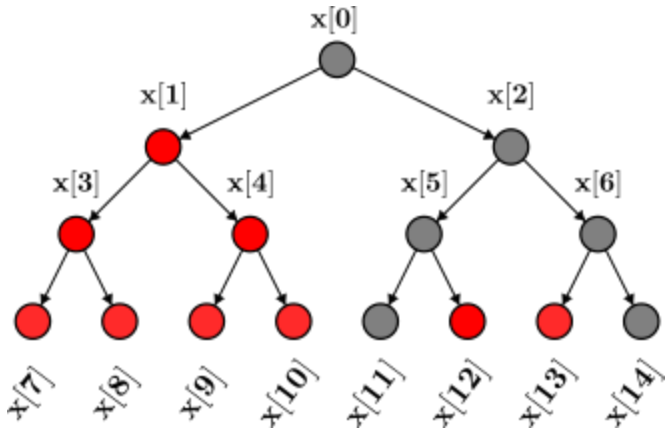

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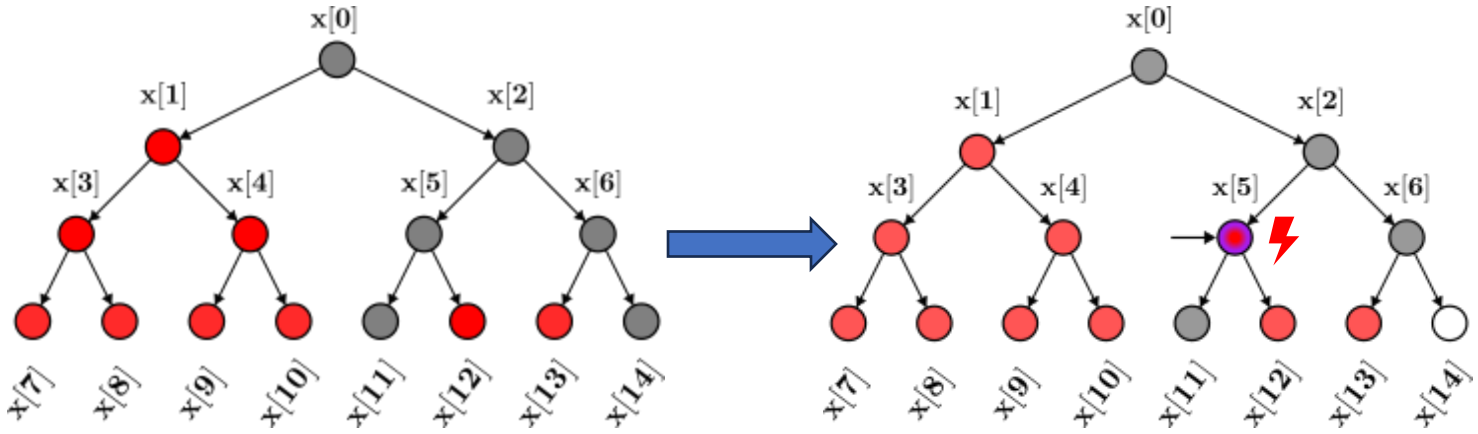

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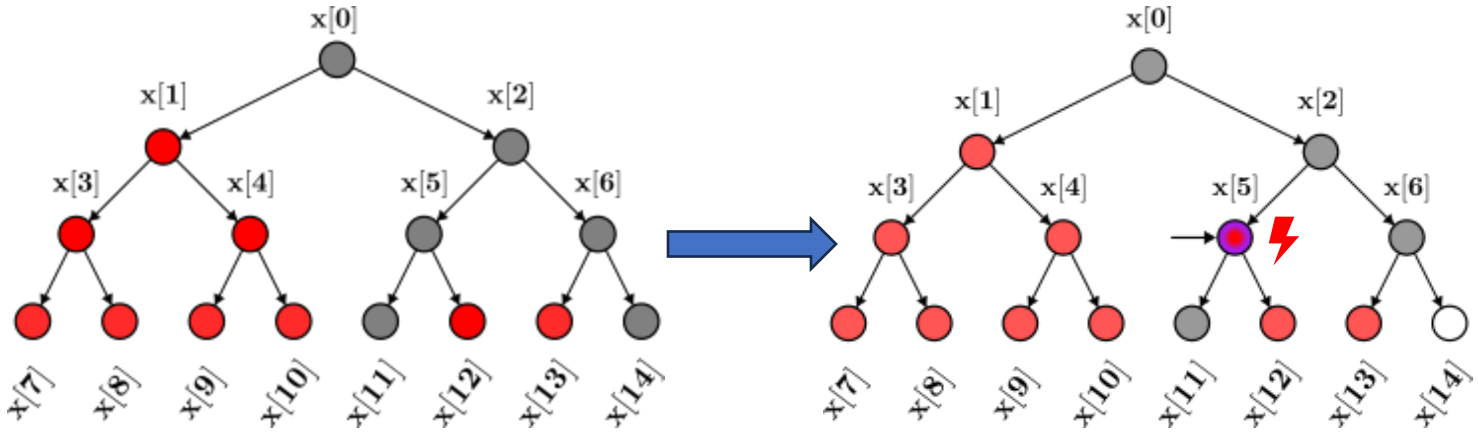

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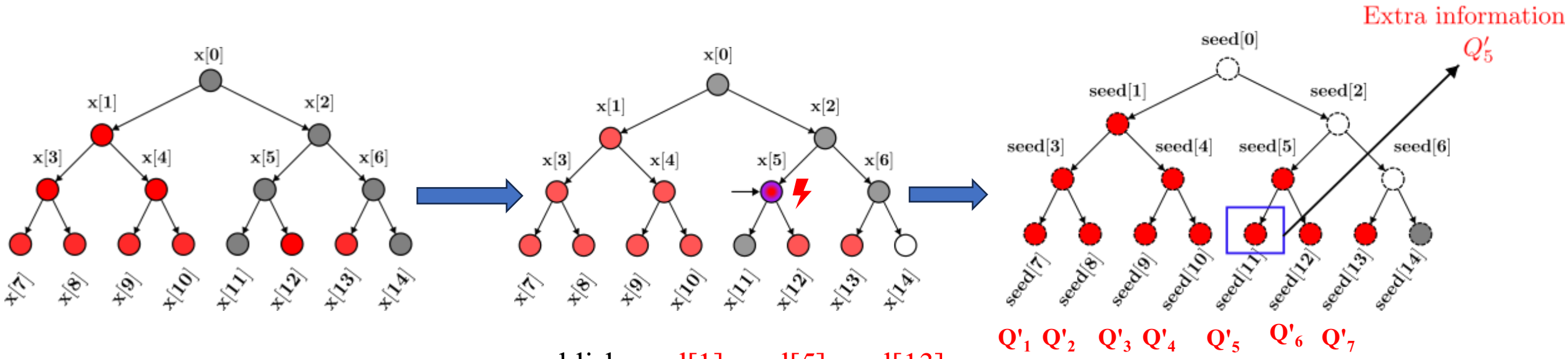

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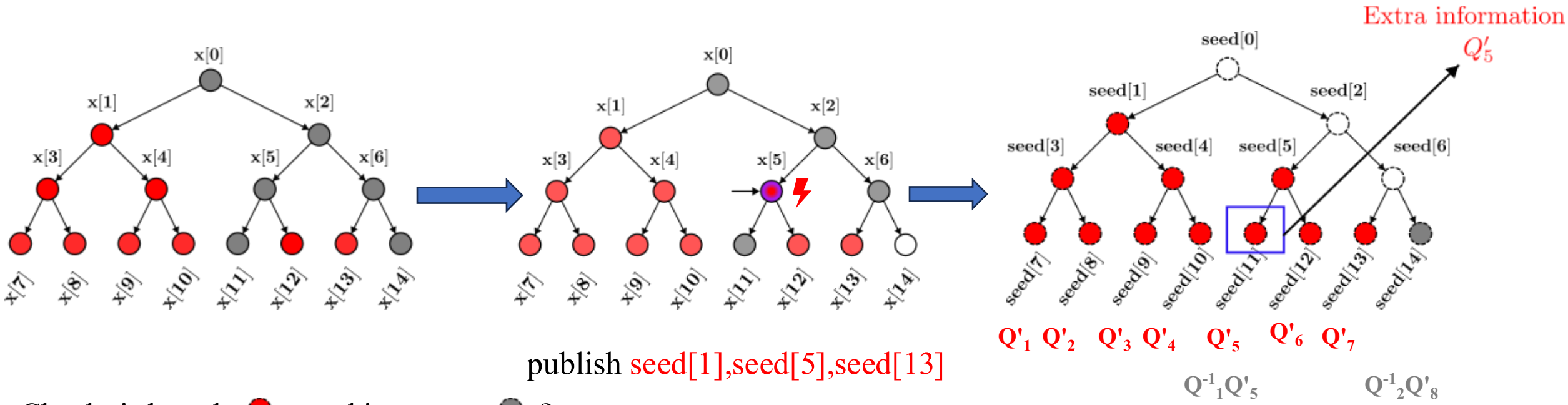

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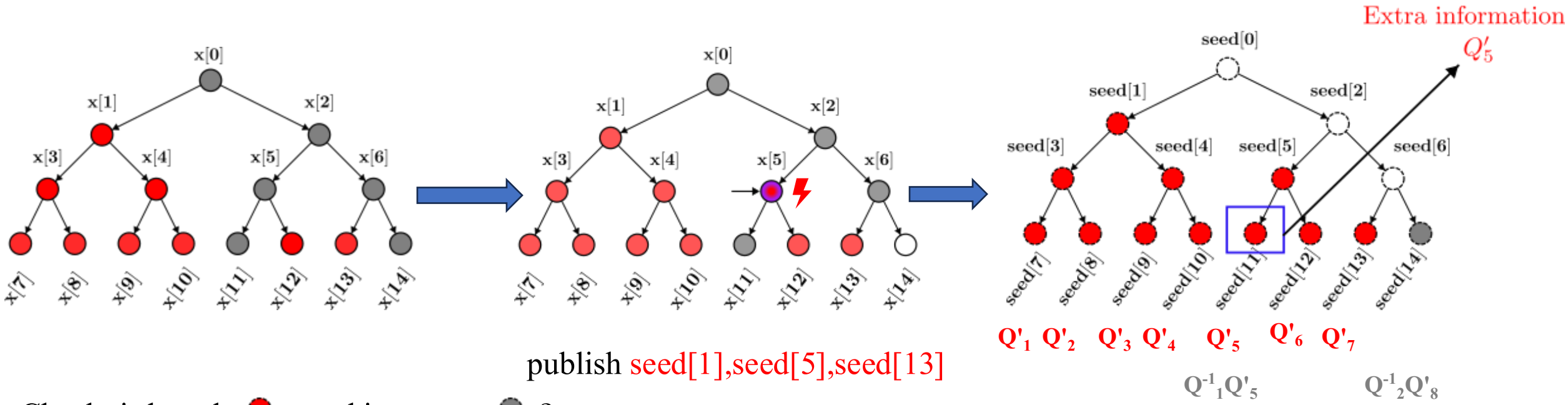

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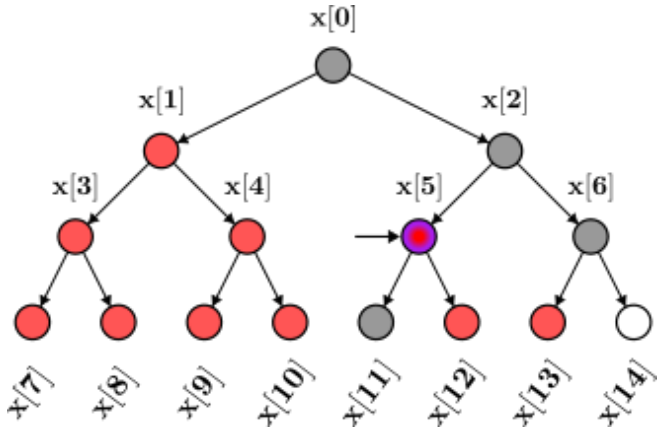
The secret Q_1 can be computed by

$Q_1=Q'_5(Q^{-1}{}_1Q'_5)^{-1}$

Leaks secret information!!!!

Generic Fault Location



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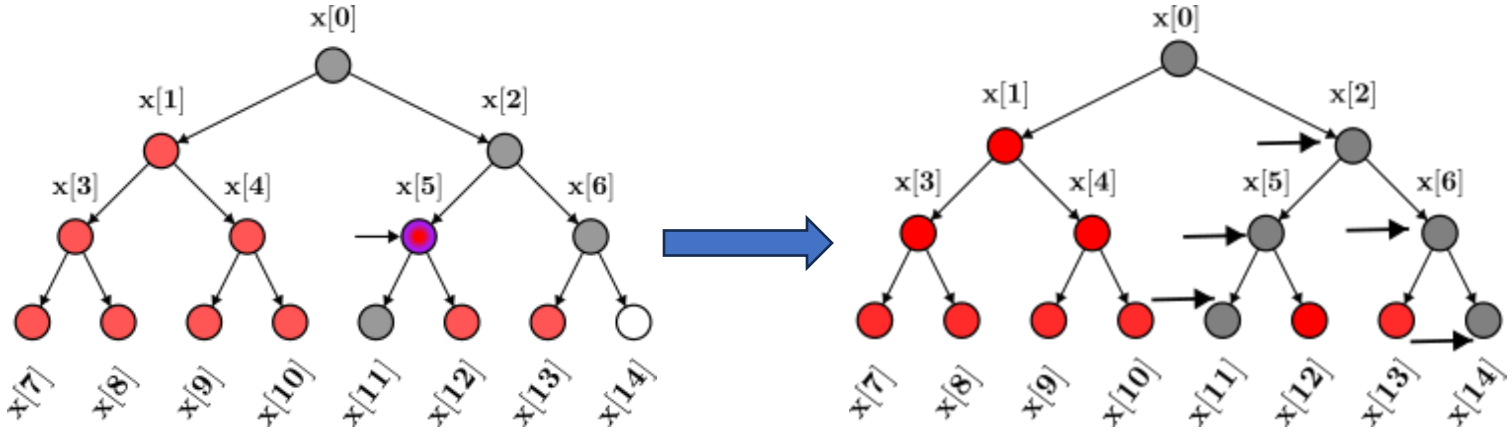

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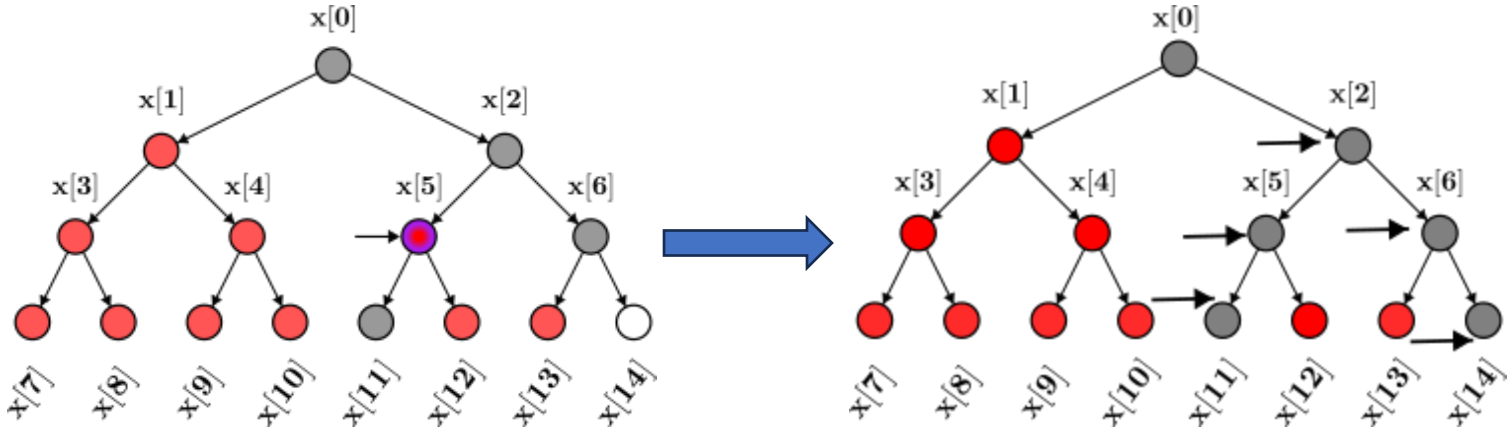

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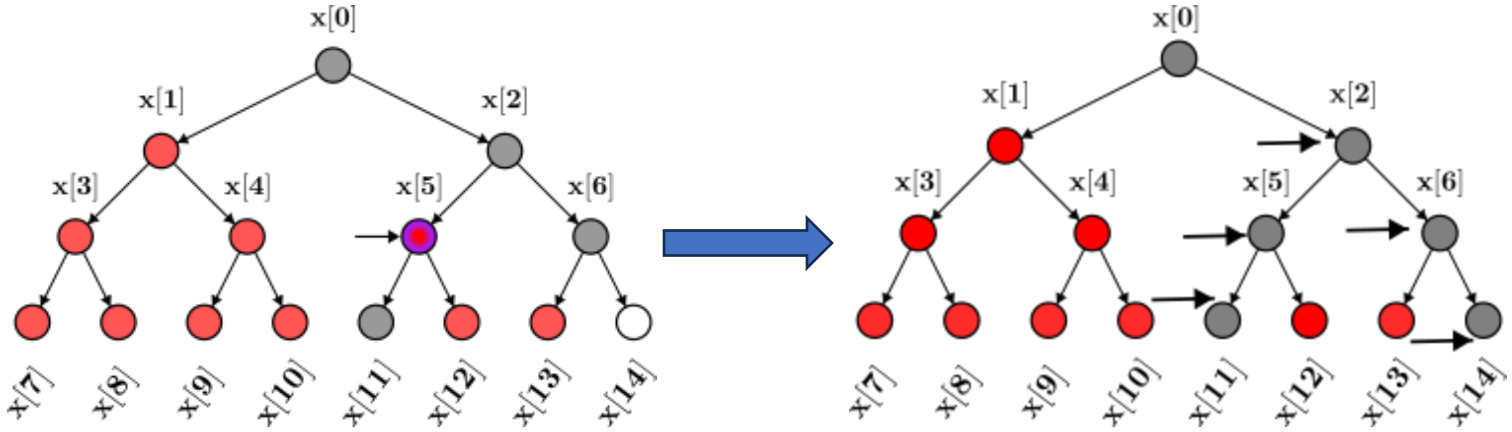

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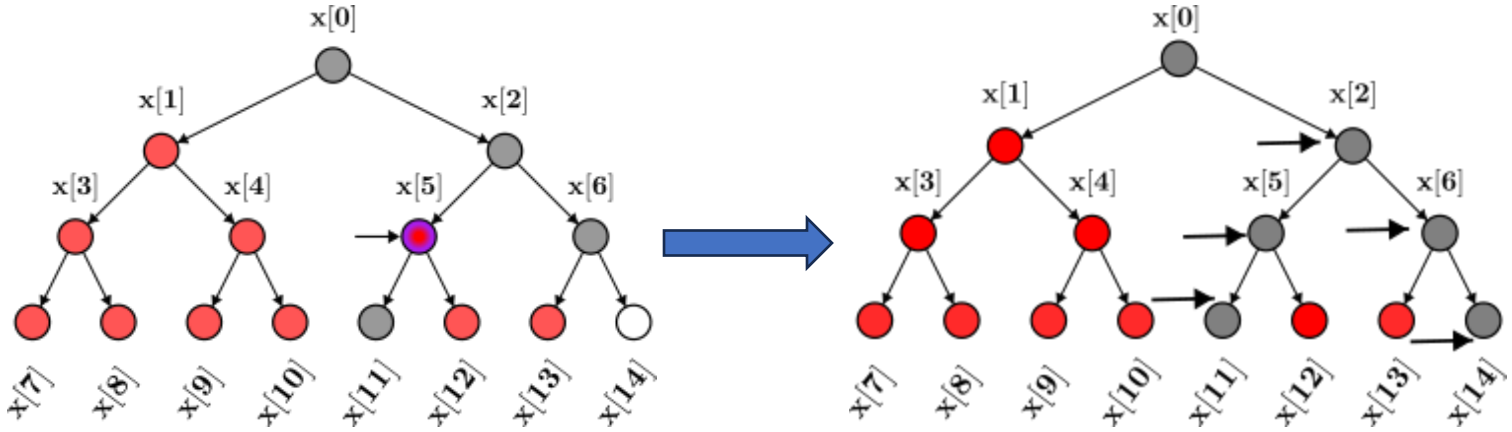

- Change of any grey node by injecting fault will leak the information of the secret
- The nodes with higher heights would always give more informations about secret
- For our result, we have targeted the location x[1]/x[2]

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  - Is the fault injected exactly at i-th location?
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  - Is the fault injection successful?
- In our work, the fault detection method answers both of the above questions.

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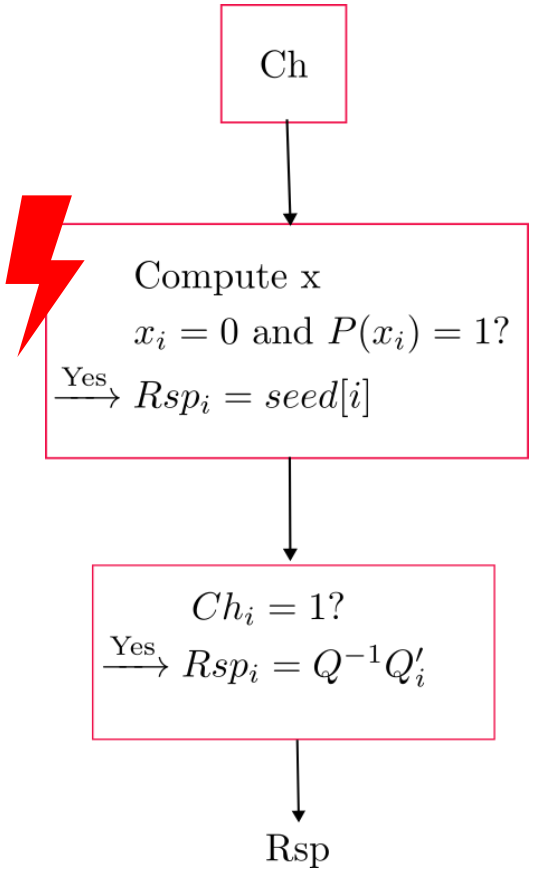

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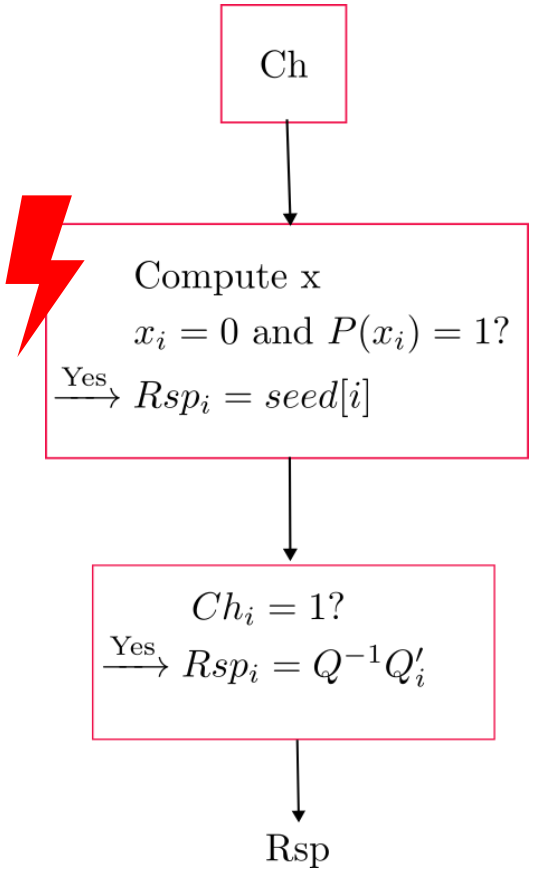

- By injecting fault in the first part to get the value seed[i'] corresponding to Ch_i=1, which will not hamper the second part.

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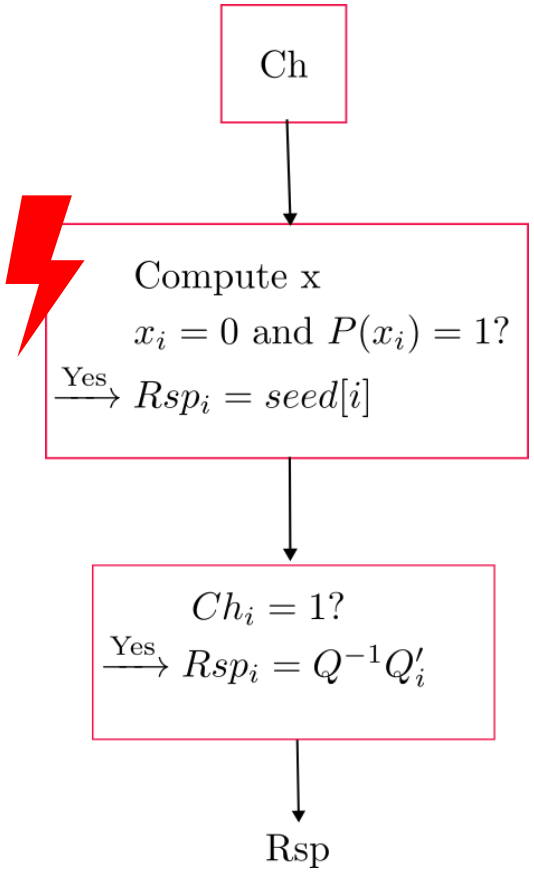

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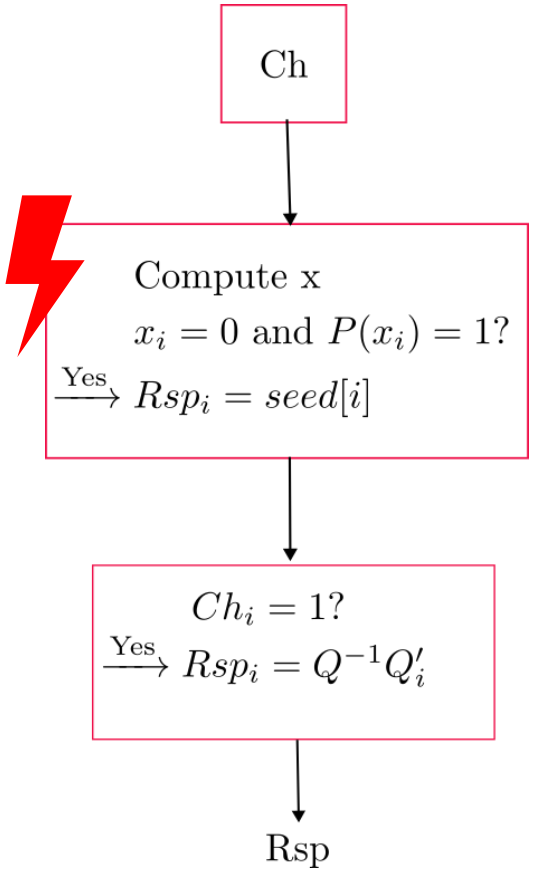

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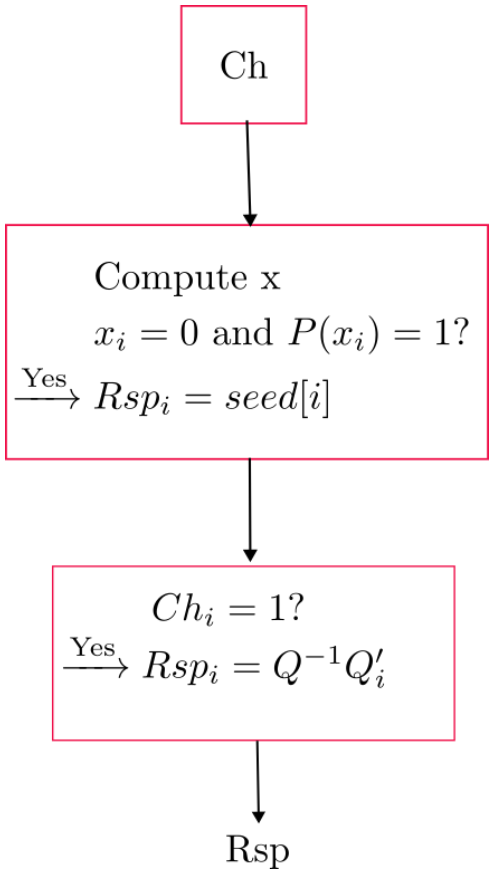
- So, we are getting both values seed[i'] (=Q'_i) and $Q^{-1}Q'_i$ for a non-zero Ch_i.
- The attack successfully done.

First Countermeasure



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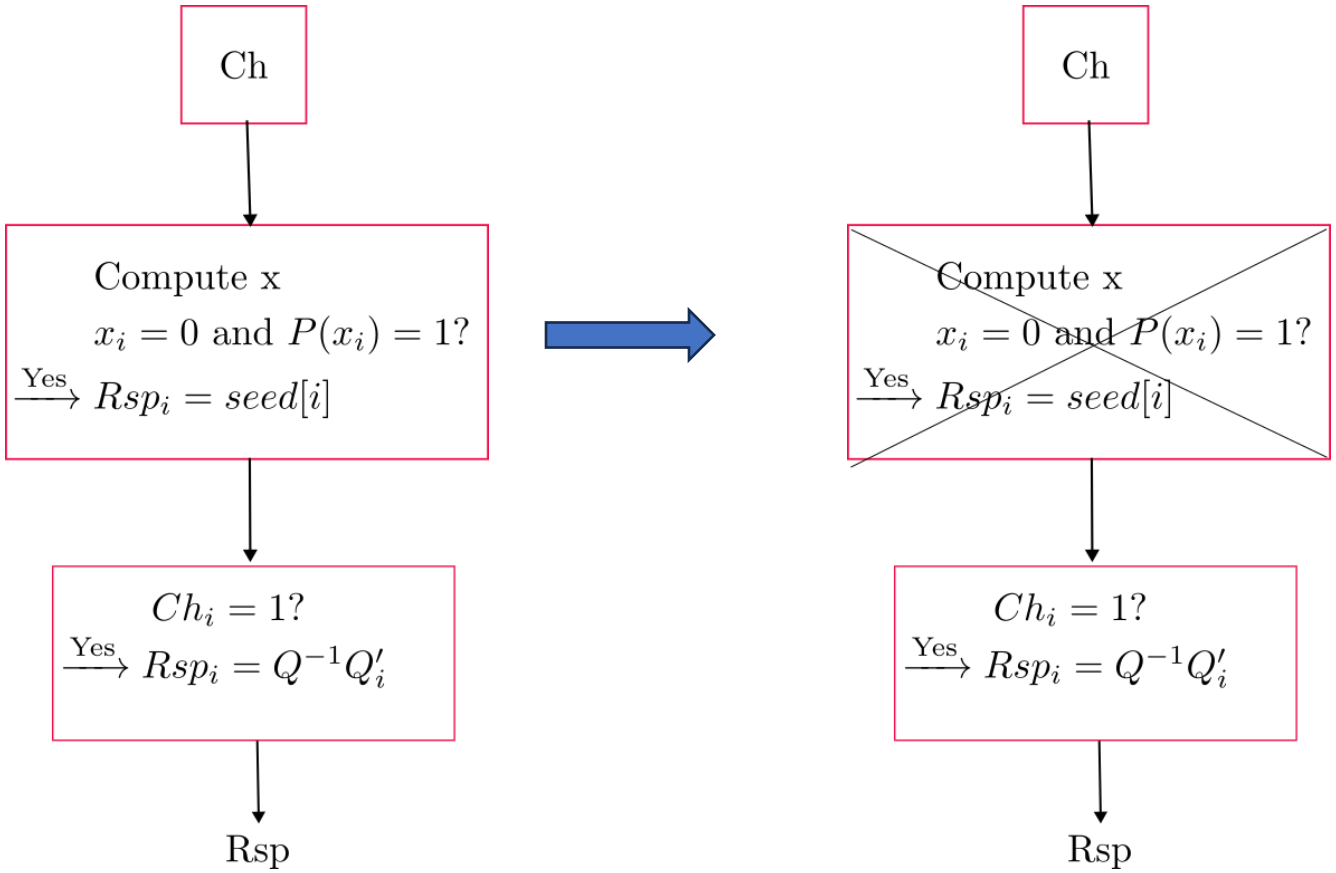

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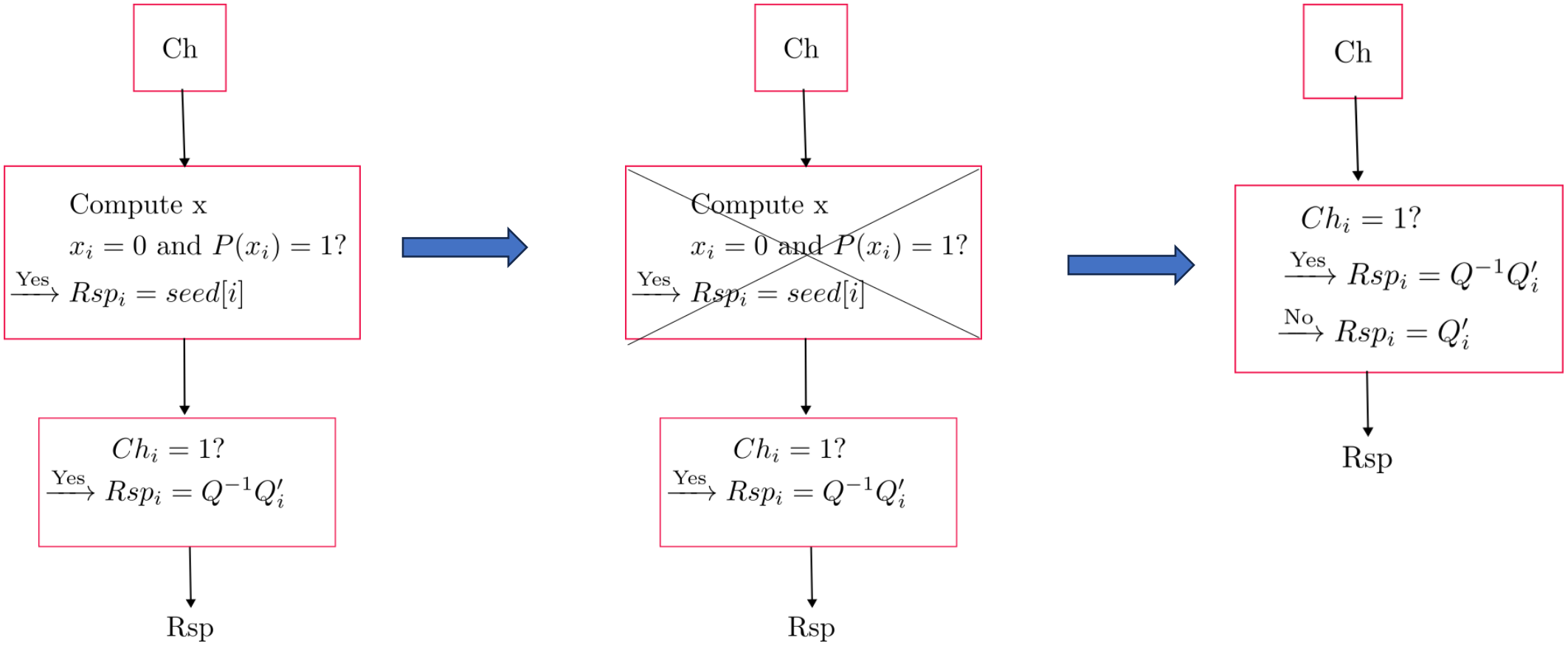

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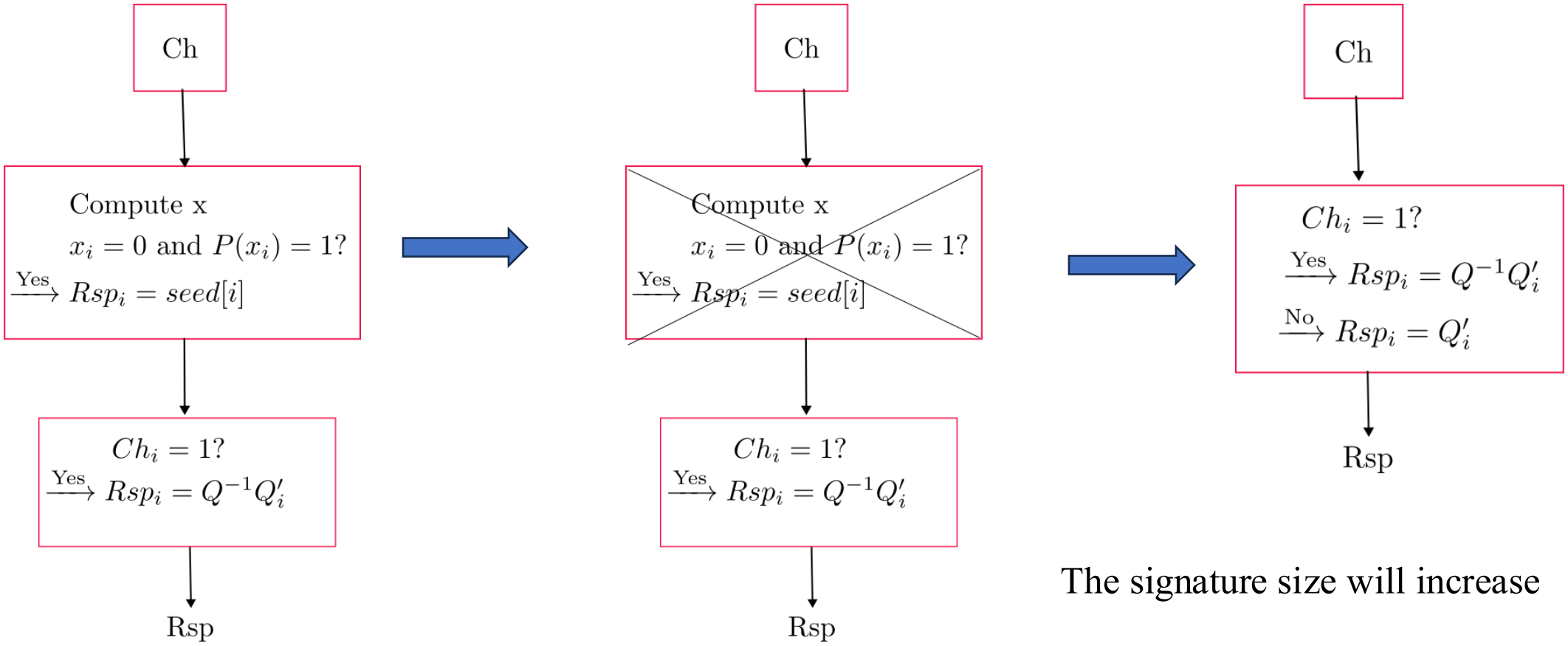
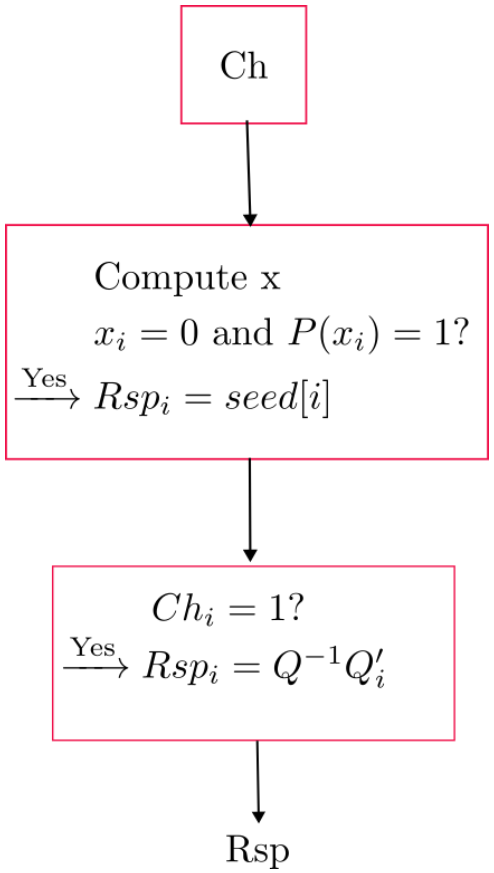


The signature size will increase

Second Countermeasure



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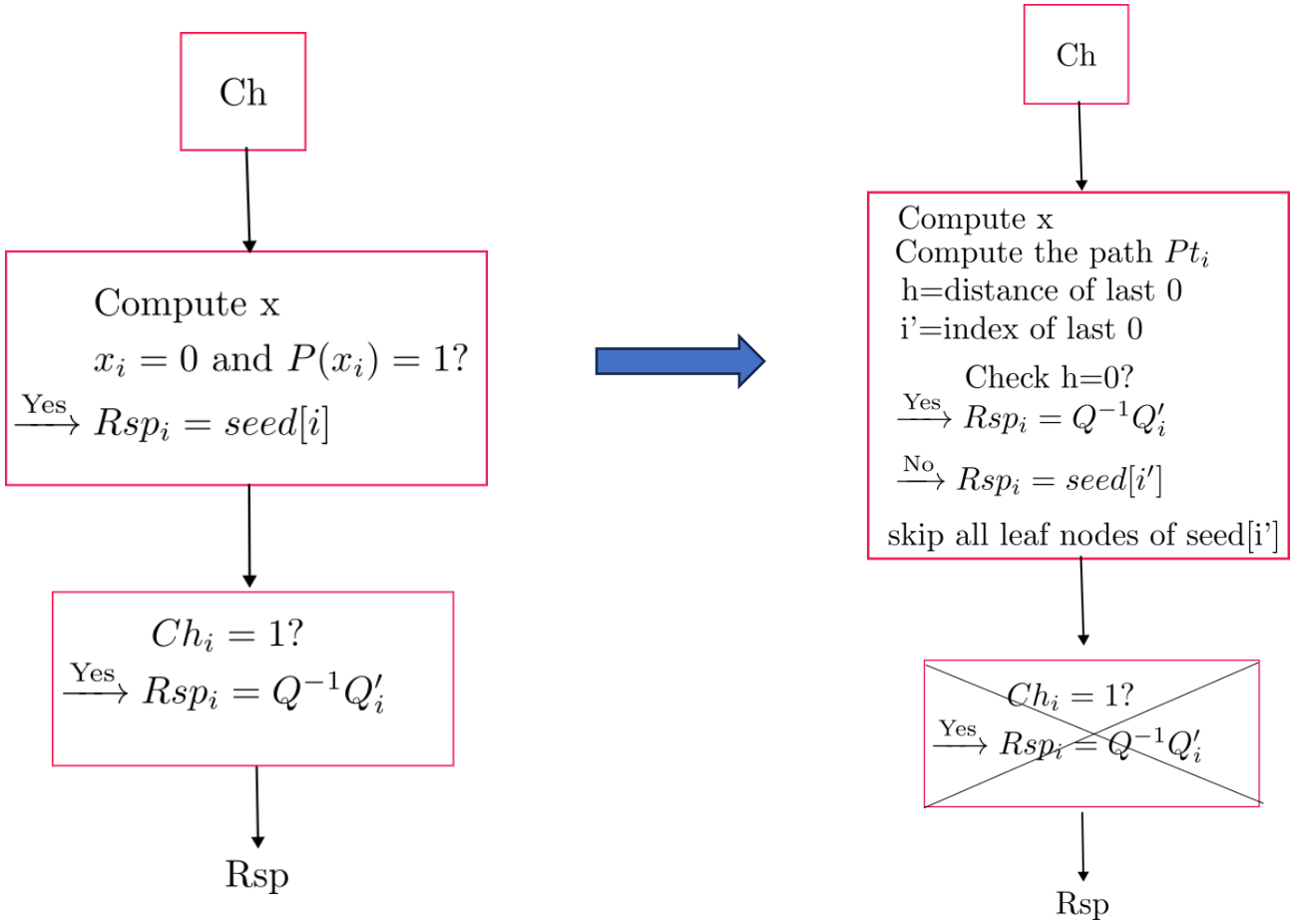

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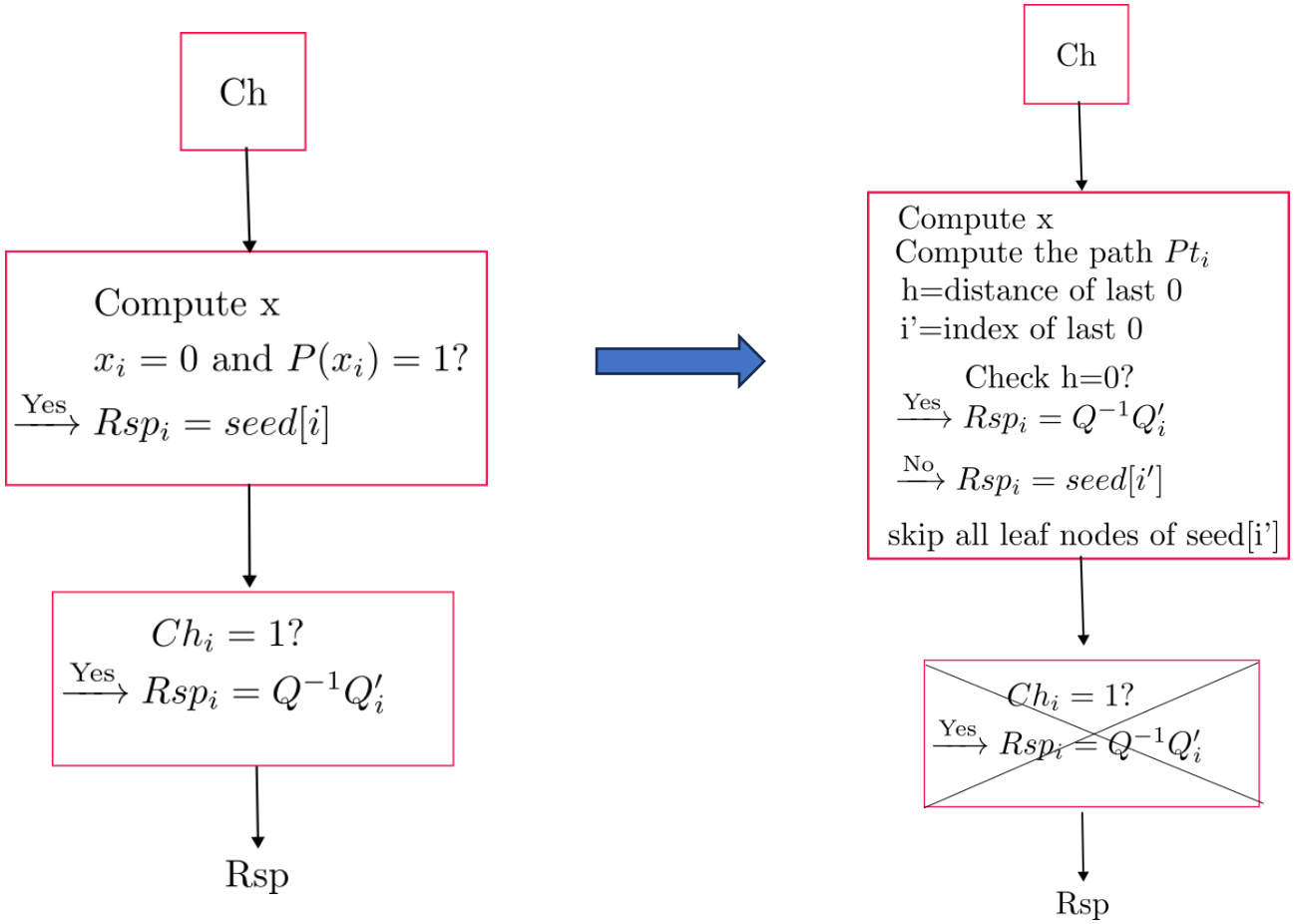

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- We have proposed two countermeasures that prevent the fault

Questions?

Thank you!