

# Maliciously Secure SCALES Protocols

Anasuya Acharya<sup>1</sup>, Carmit Hazay<sup>1</sup>, Vladimir Kolesnikov<sup>2</sup>, Manoj Prabhakaran<sup>3</sup>



<sup>1</sup>Bar-Ilan University

<sup>2</sup>Georgia Institute of Technology

<sup>3</sup>IIT Bombay



**MPC**

# MPC-as-a-Service

# Large Scale MPC-as-a-Service

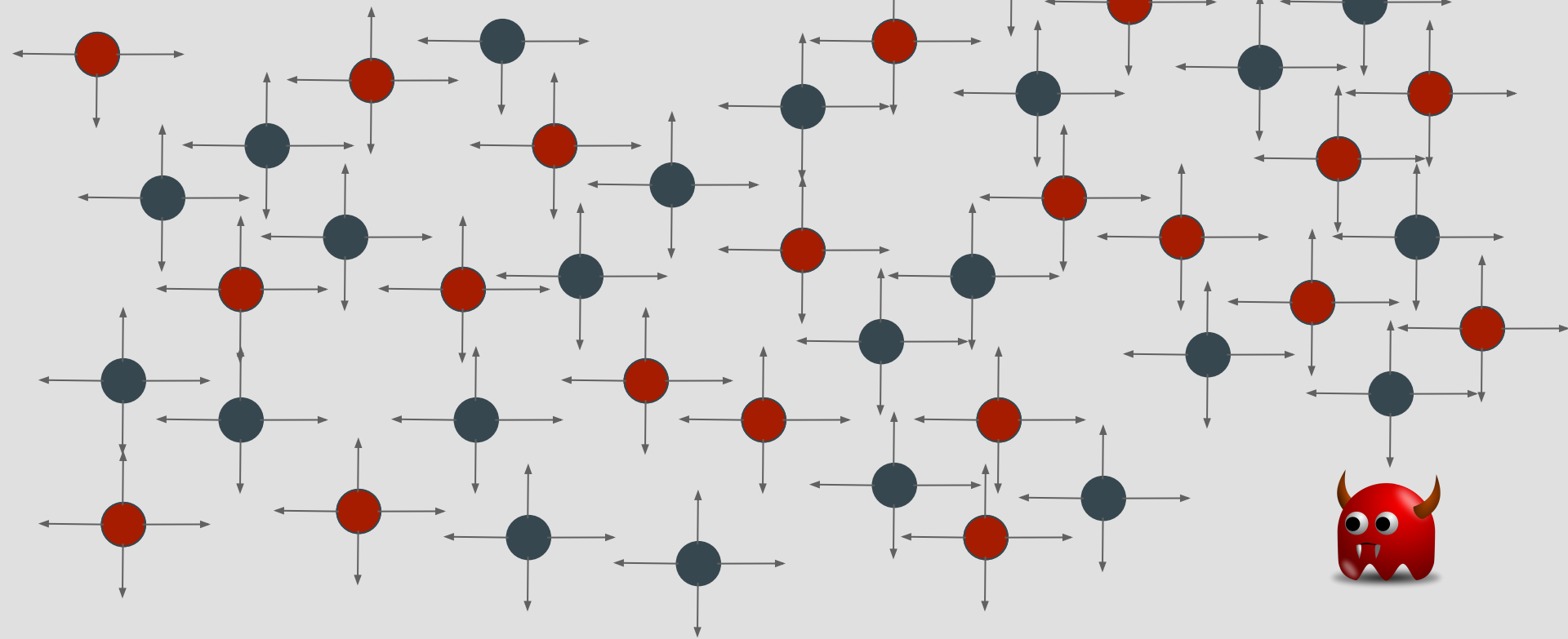


# Large Scale MPC-as-a-Service

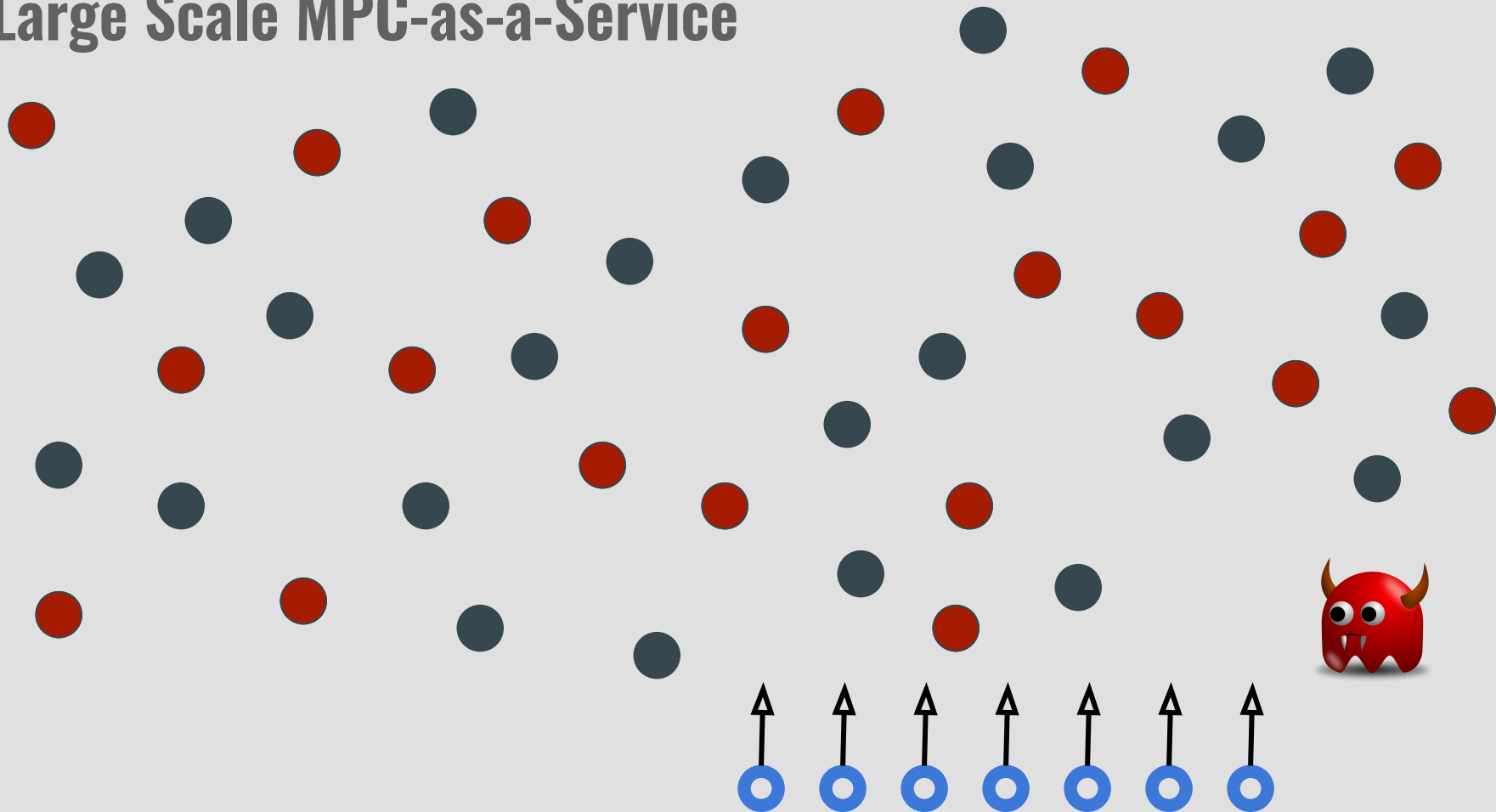




# Large Scale MPC-as-a-Service

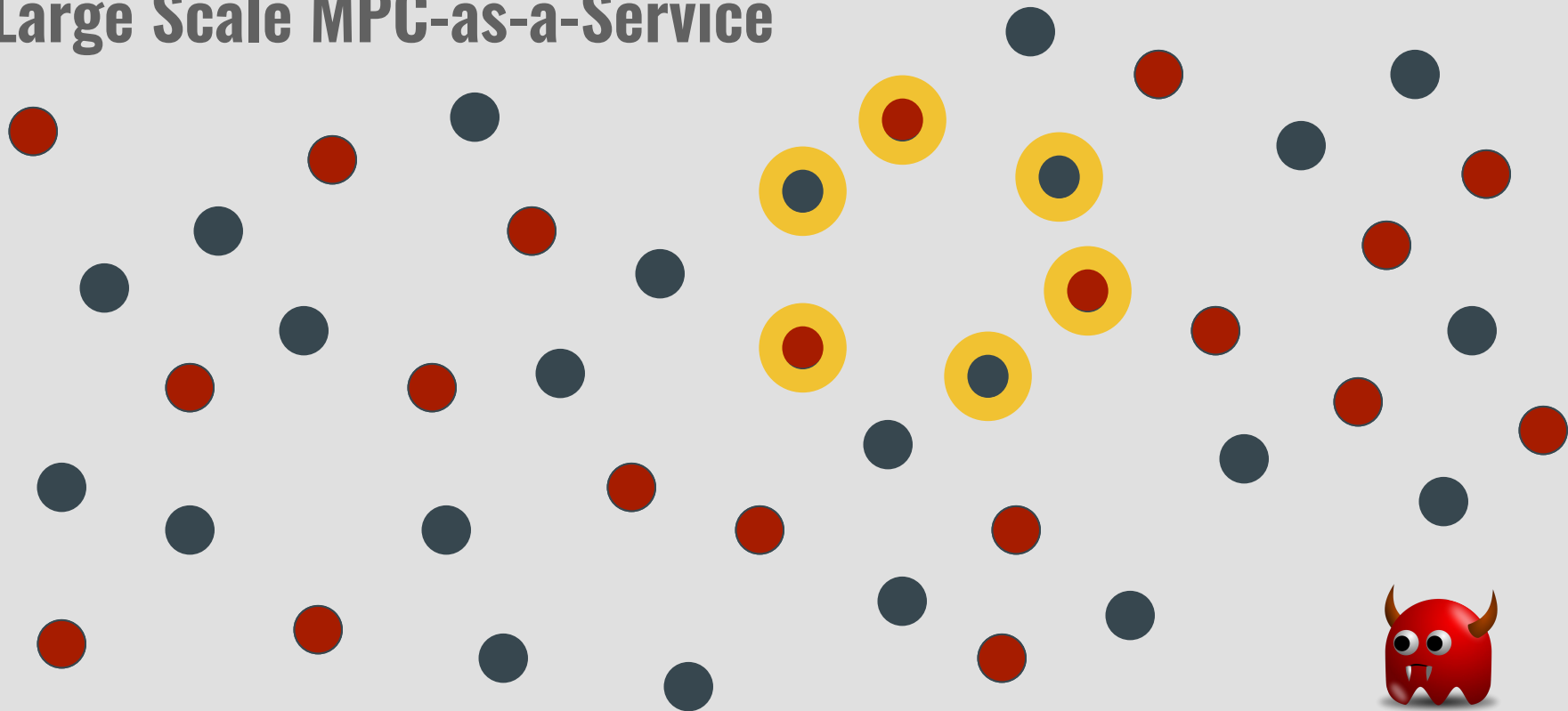


# Large Scale MPC-as-a-Service

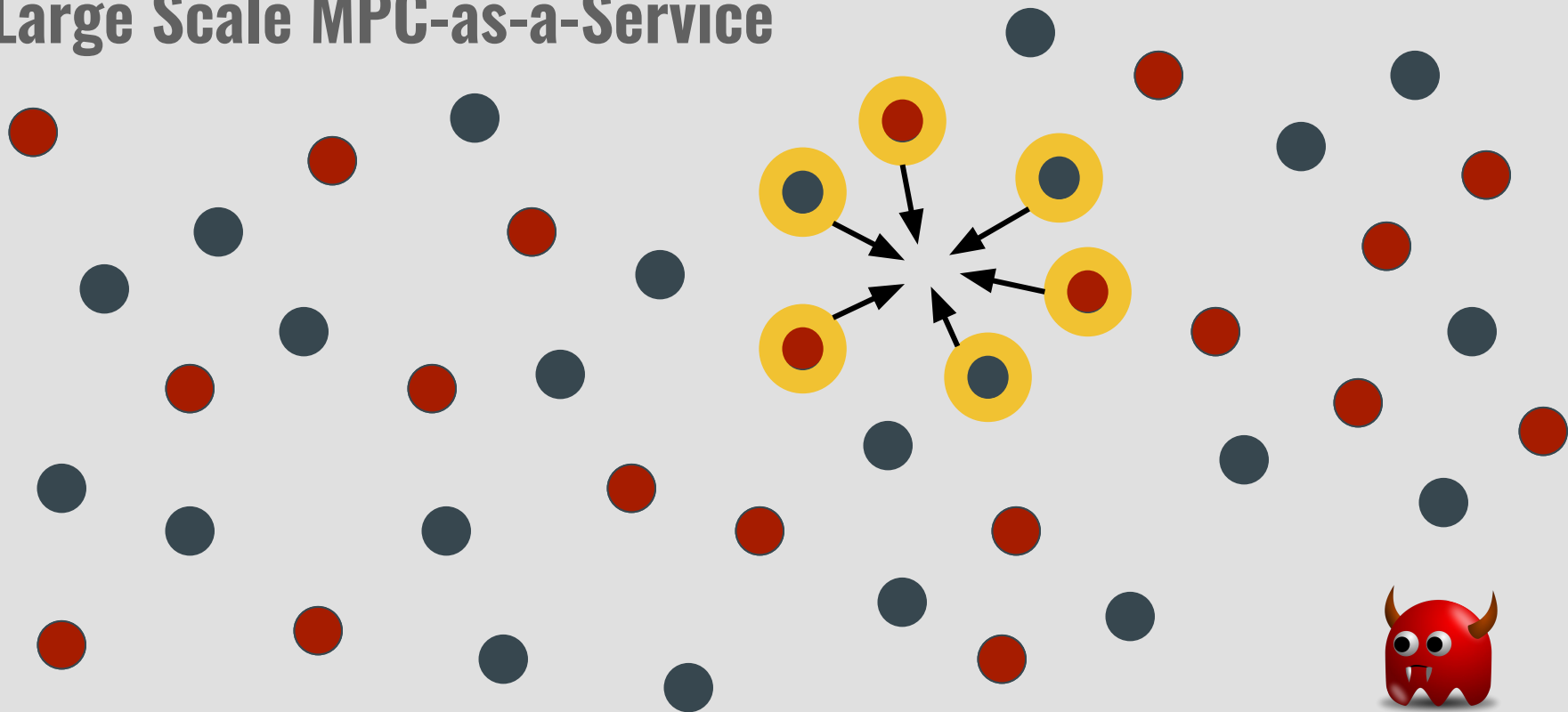




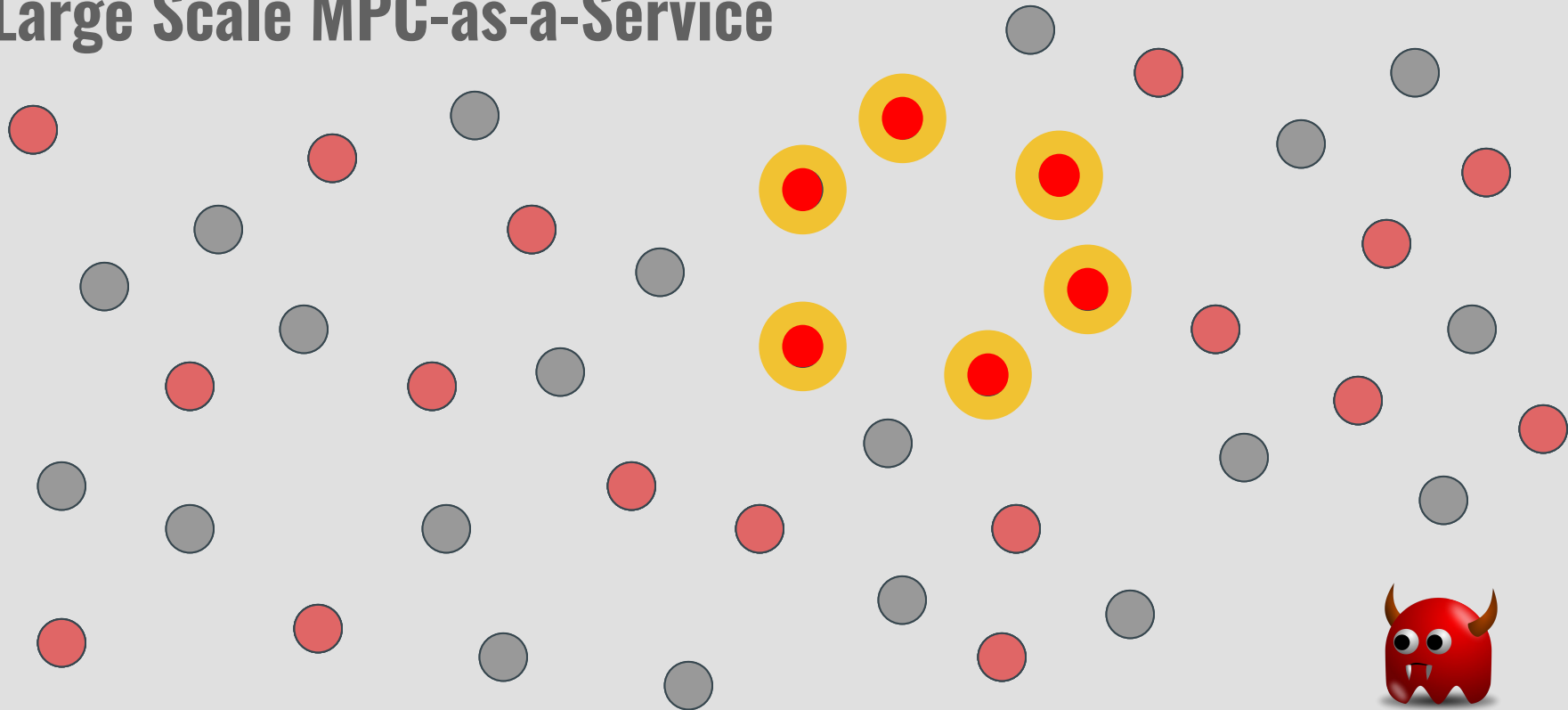
# Large Scale MPC-as-a-Service



# Large Scale MPC-as-a-Service



# Large Scale MPC-as-a-Service



# Overview

SCALES Model

Rerandomizable Garbling Schemes

Semi-Honest SCALES Protocol

Lifting to Malicious Security

# The SCALES Model

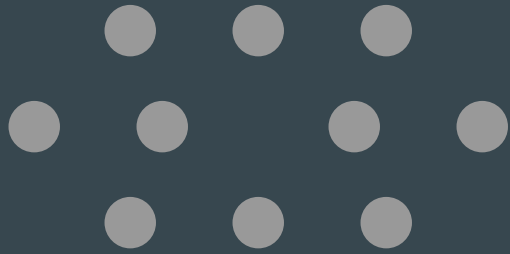
[TCC '22]

# Small Clients And Large Ephemeral Servers

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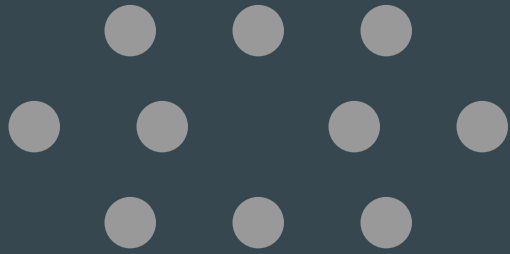




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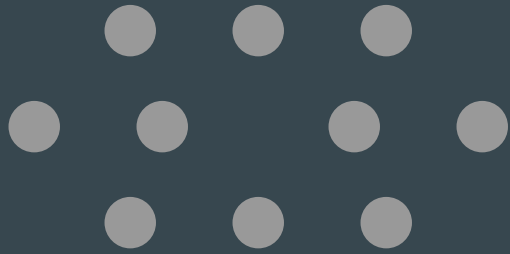


# Small Clients And Large Ephemeral Servers



Bulletin-Board



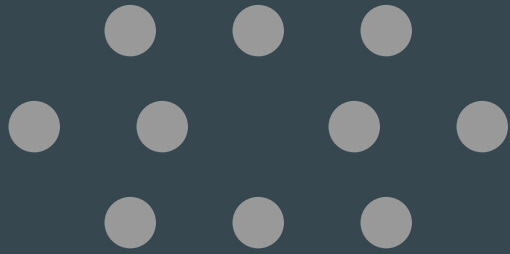


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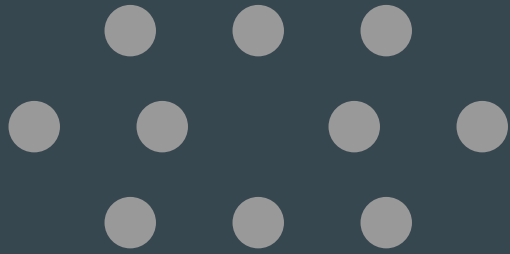




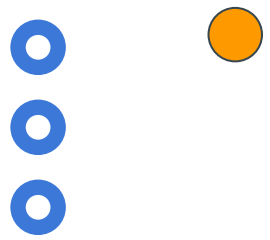
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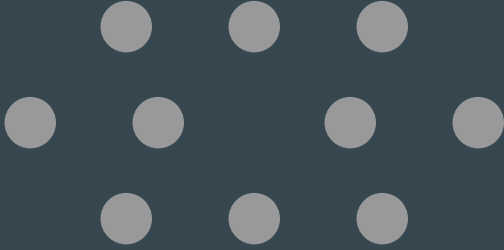
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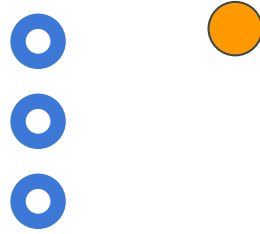
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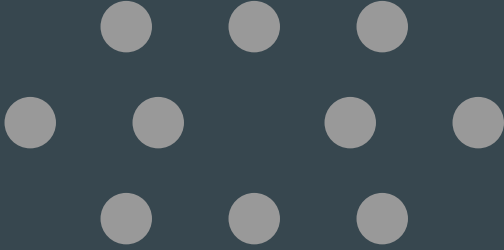
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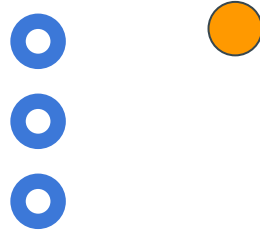
Secretly elected



# Small Clients And Large Ephemeral Servers



Secretly elected  
Silently compute

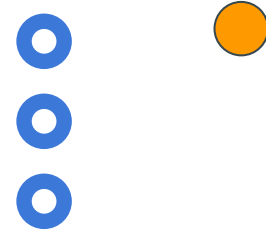


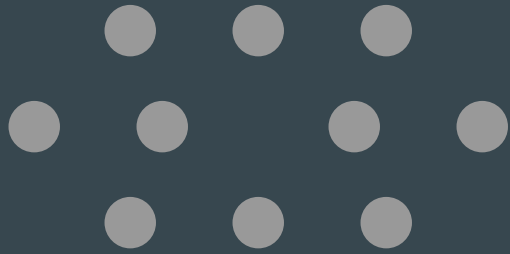


# Small Clients And Large Ephemeral Servers



Secretly elected  
Silently compute  
Erase their state

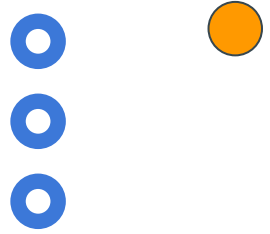




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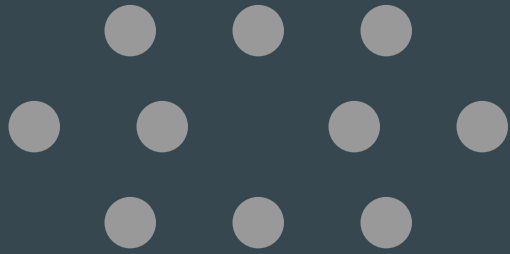


Secretly elected  
Silently compute  
Erase their state  
'Speak Once'



Bulletin-Board

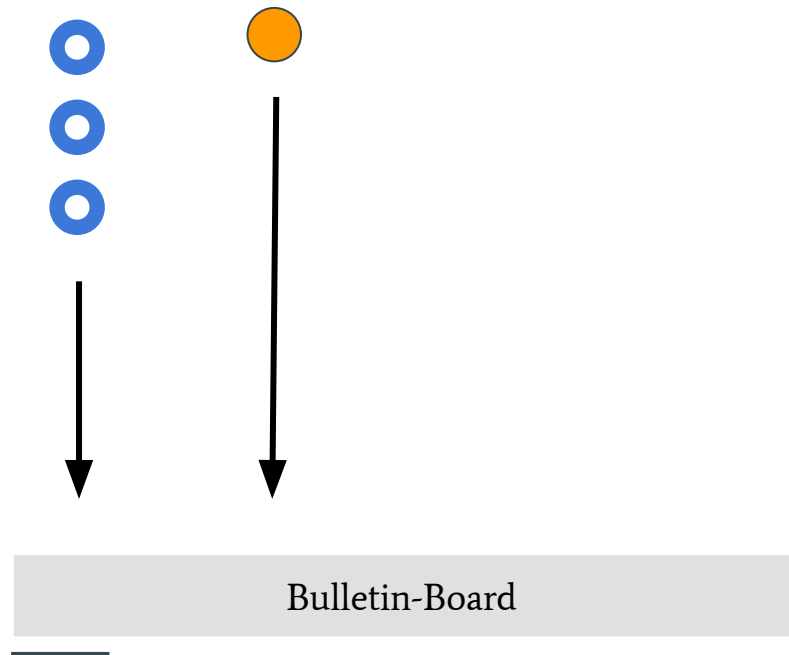


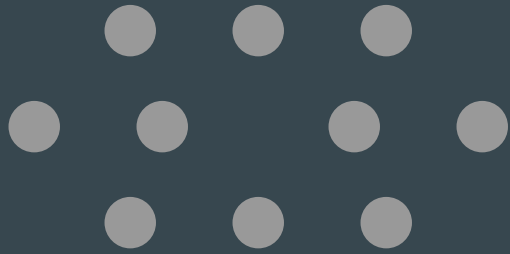


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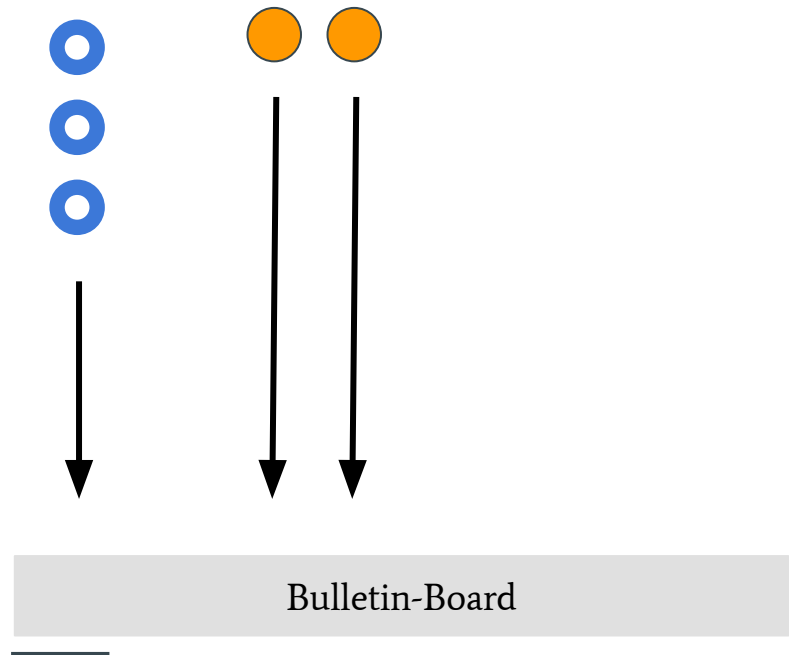


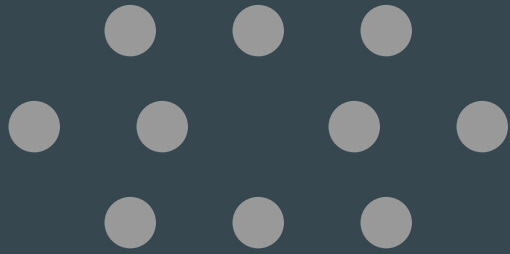


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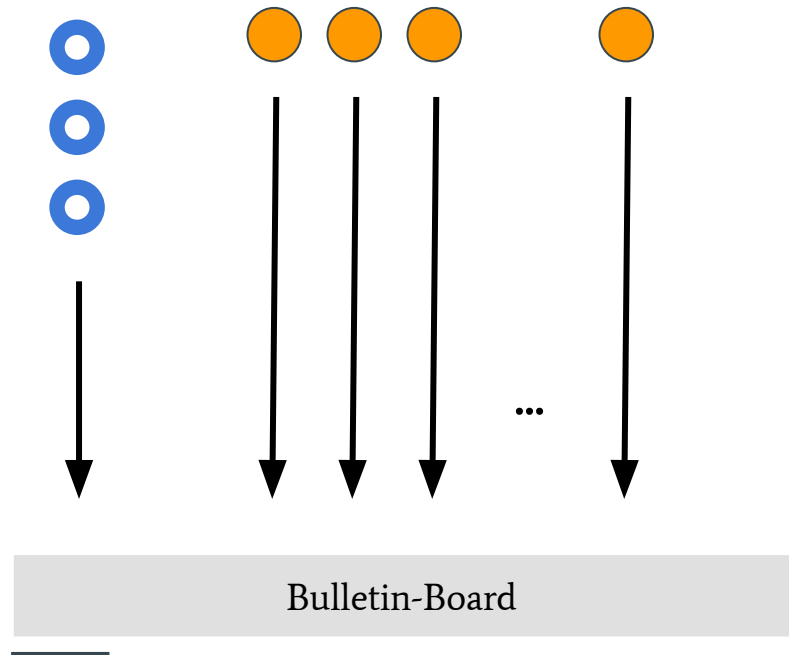


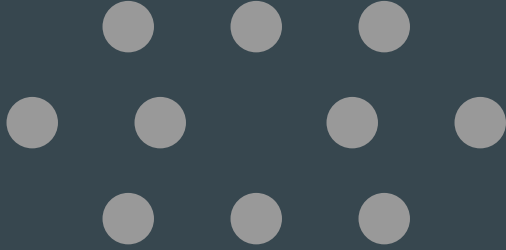


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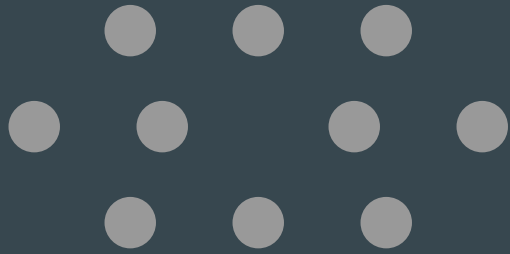


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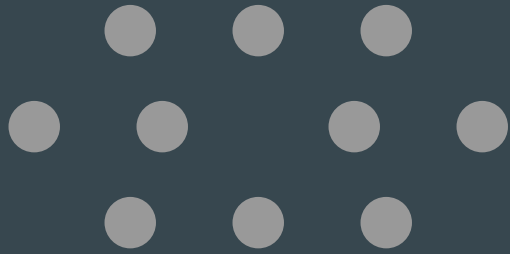


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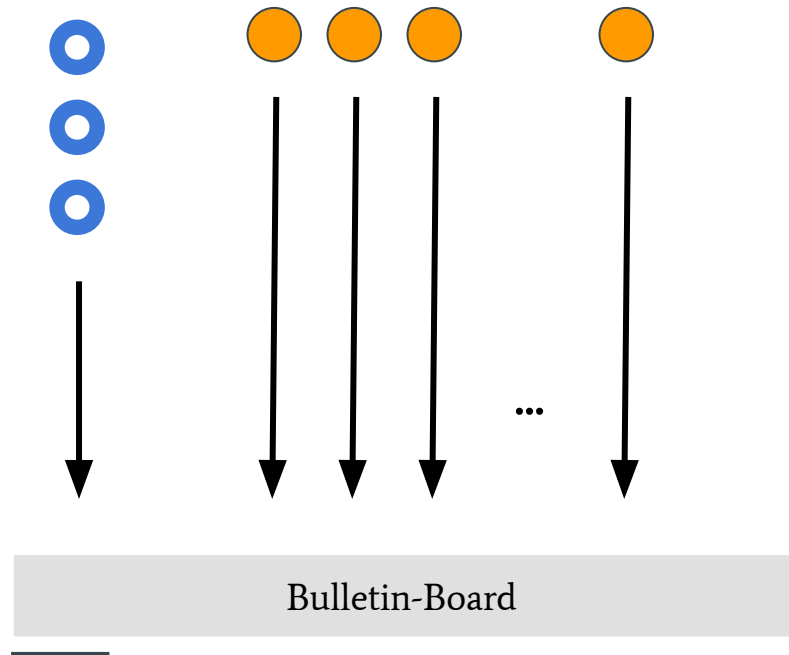


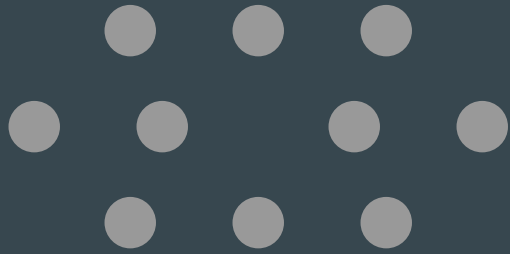


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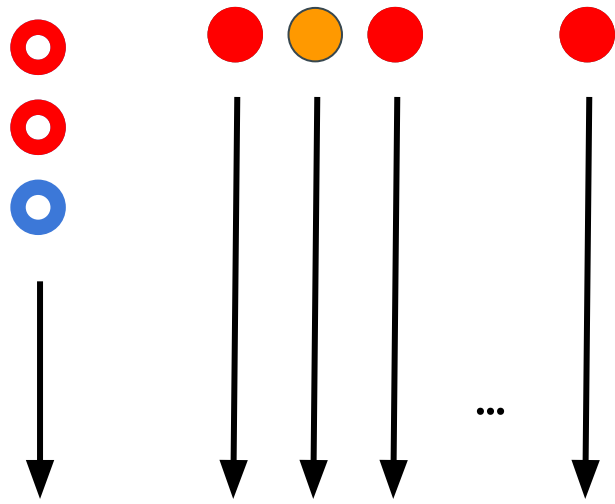
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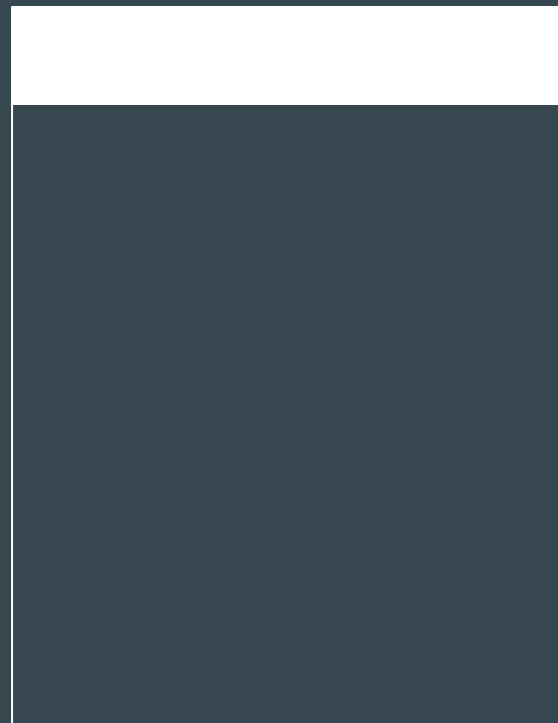
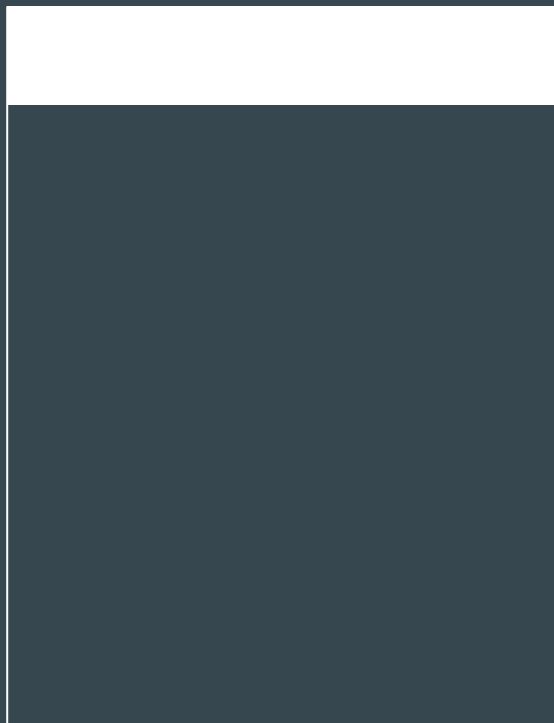
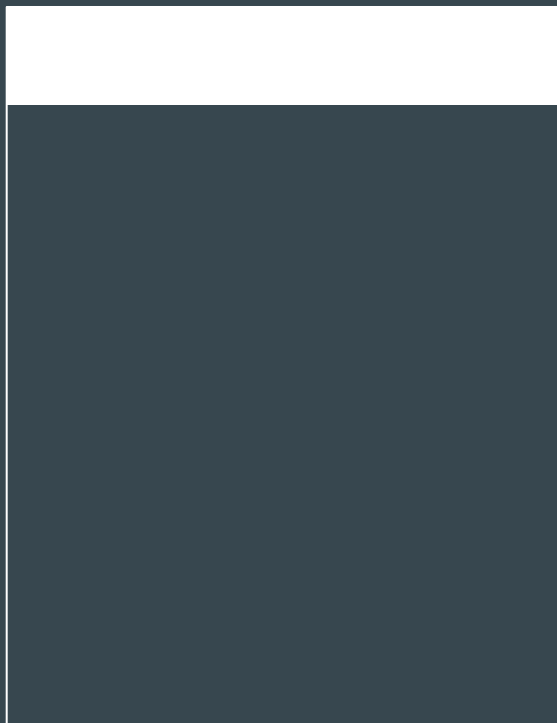


Bulletin-Board

# Semi-Honest SCALES Protocol



# Garbled Circuits



# Garbled Circuits

Garbler

Evaluator

# Garbled Circuits

Garbler

$$f : \{0,1\}^n \rightarrow \{0,1\}^m$$
$$x = (x_1, \dots, x_n)$$

Evaluator

# Garbled Circuits

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Evaluator

# Garbled Circuits

Garbler

$$f : \{0,1\}^n \rightarrow \{0,1\}^m$$
$$x = (x_1, \dots, x_n)$$



$L_0^1$	$L_0^2$	...	$L_0^n$
$L_1^1$	$L_1^2$	...	$L_1^n$

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# Garbled Circuits

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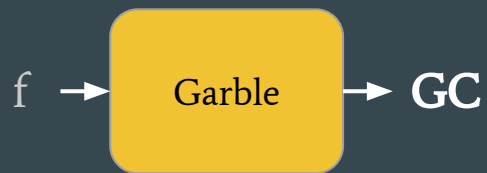
Evaluator

# Garbled Circuits

Garbler

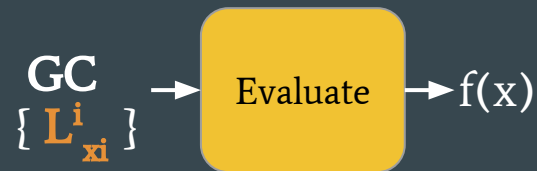
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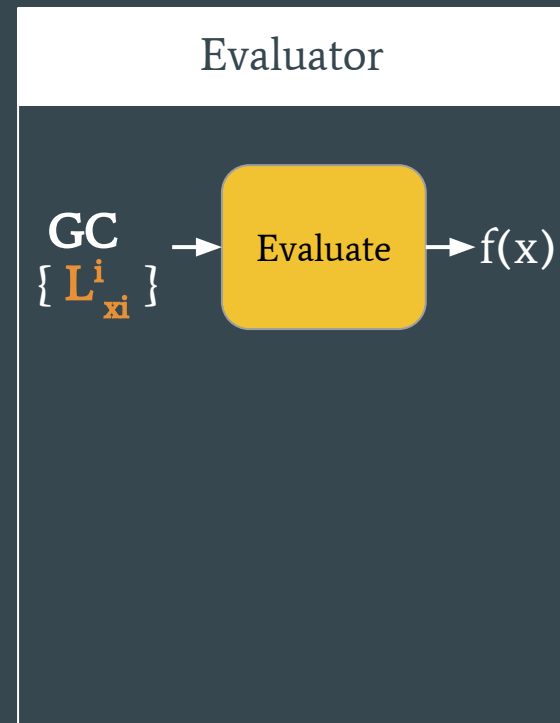
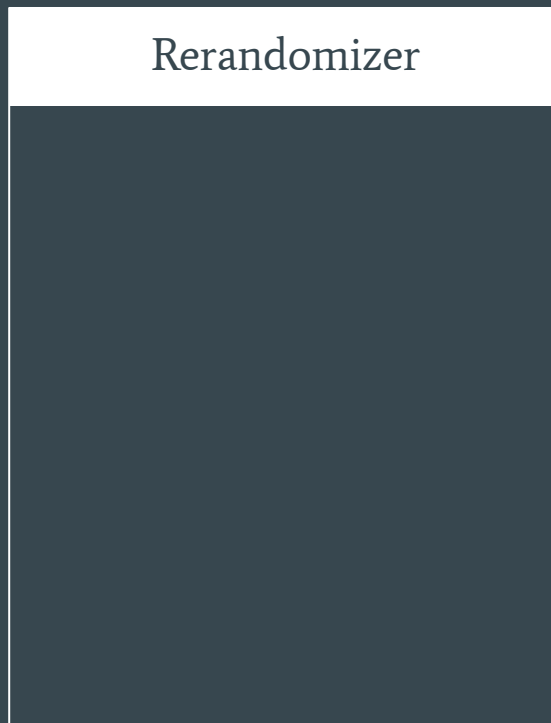
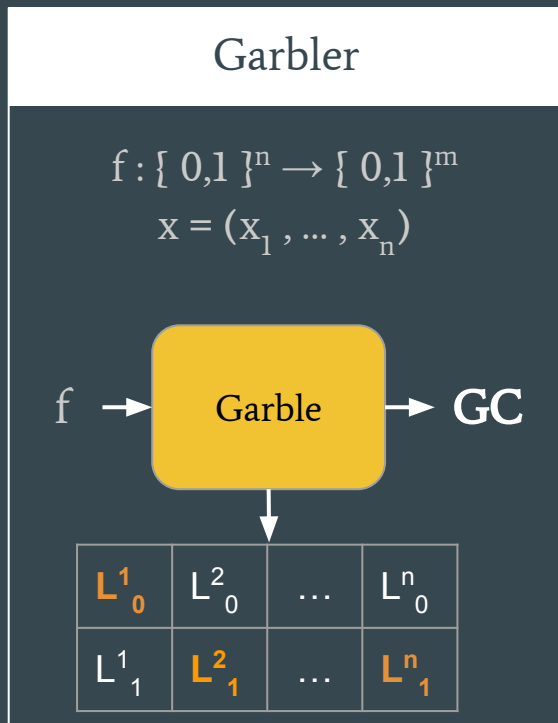


$L_0^1$	$L_0^2$	...	$L_0^n$
$L_1^1$	$L_1^2$	...	$L_1^n$

Evaluator

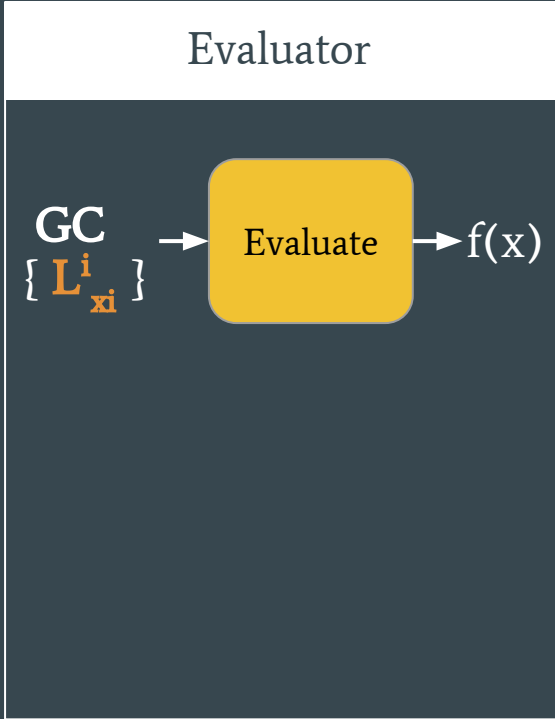
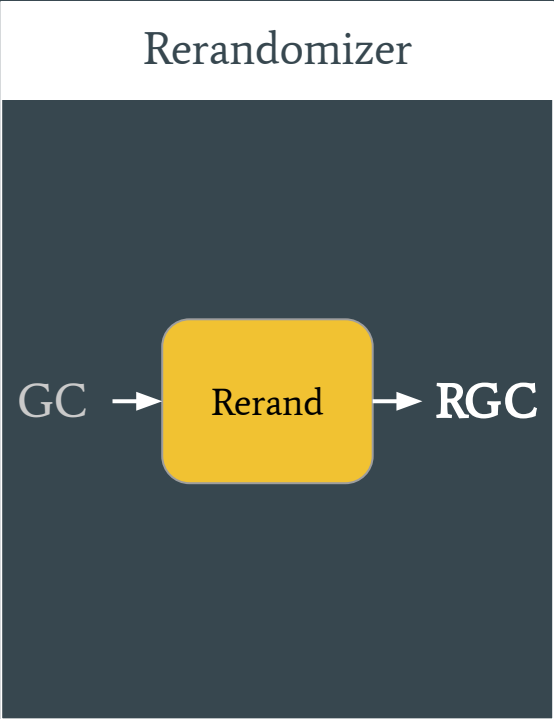
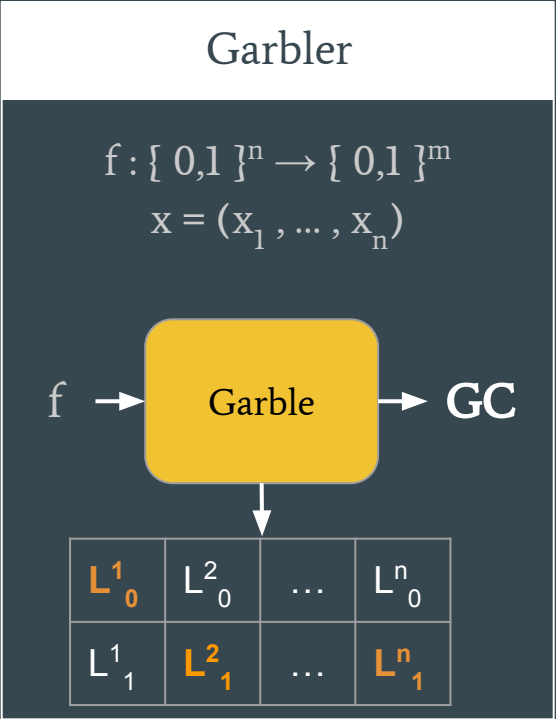


# Rerandomizable Garbled Circuits

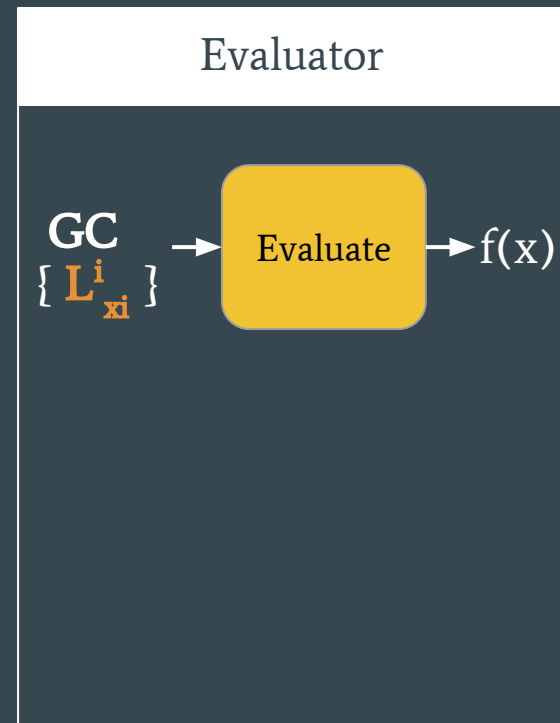
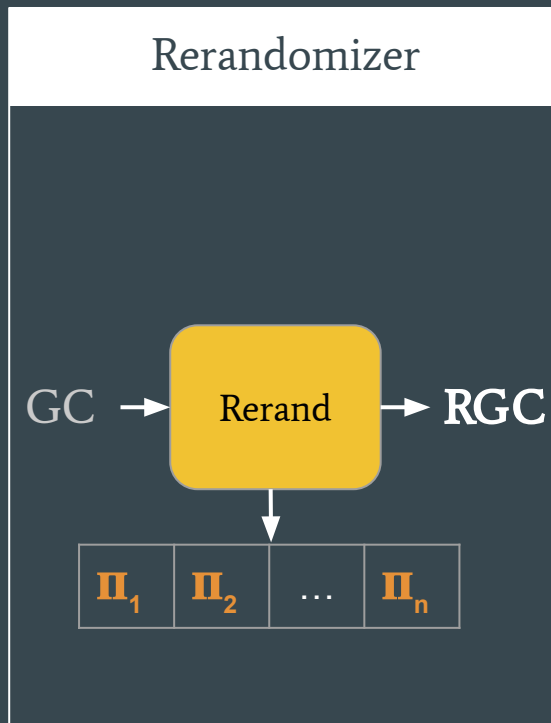
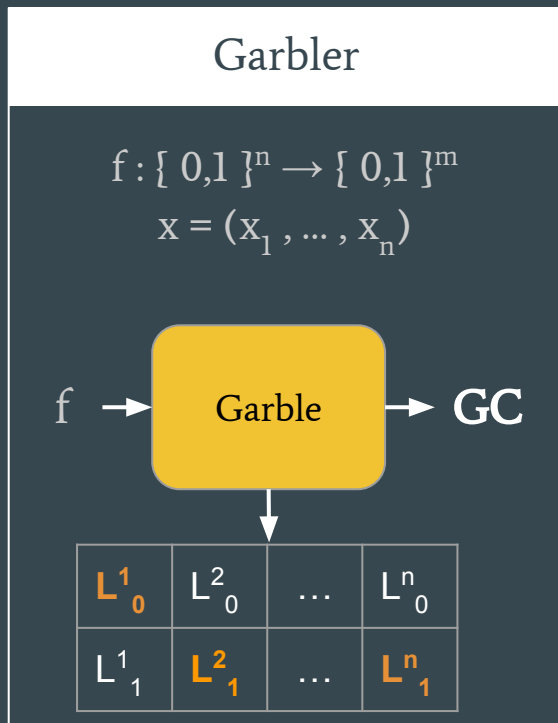




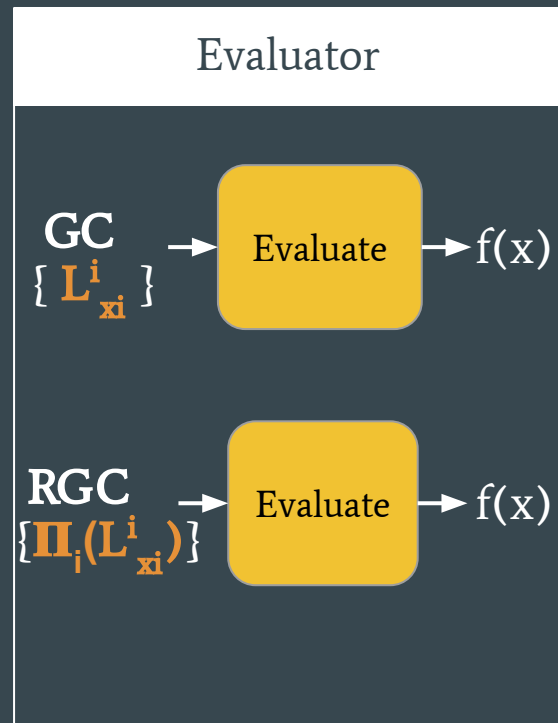
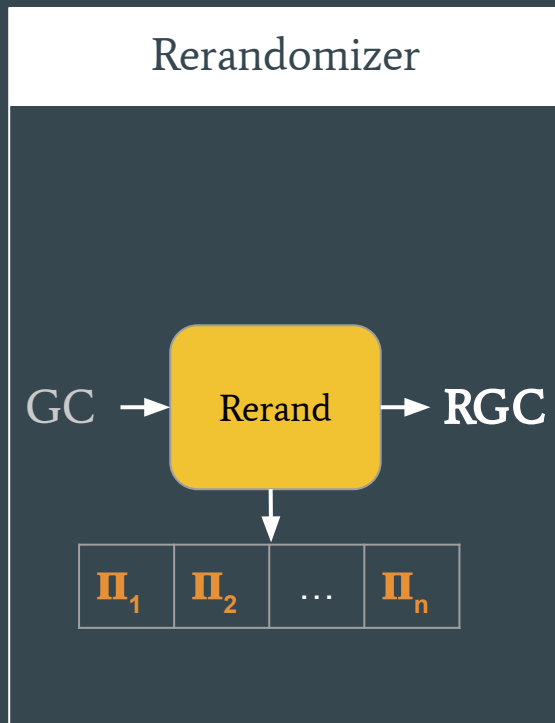
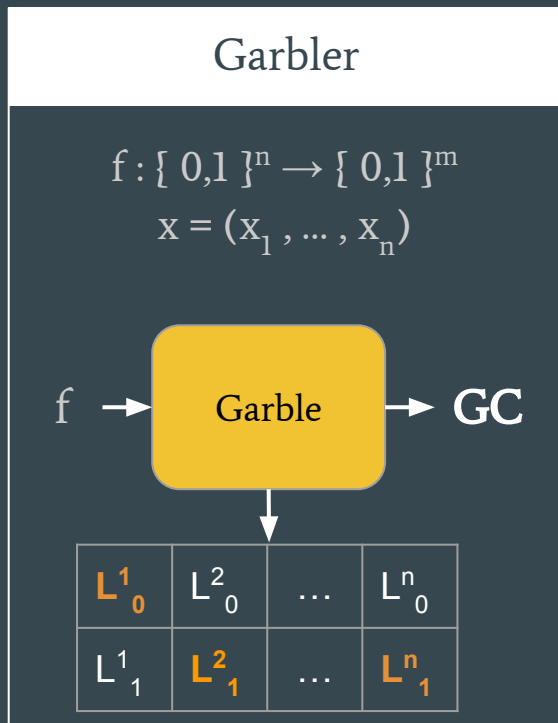
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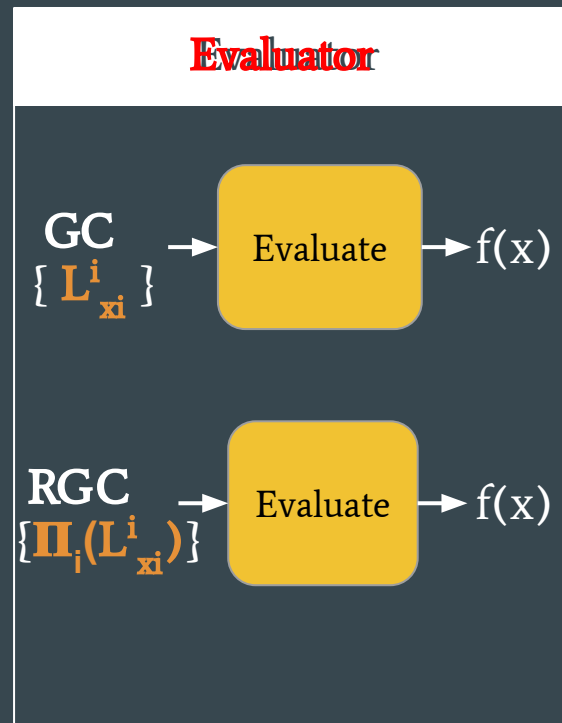
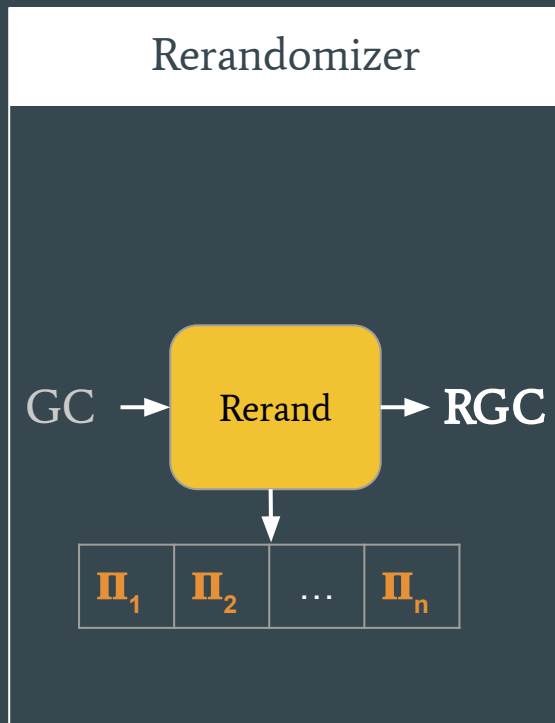
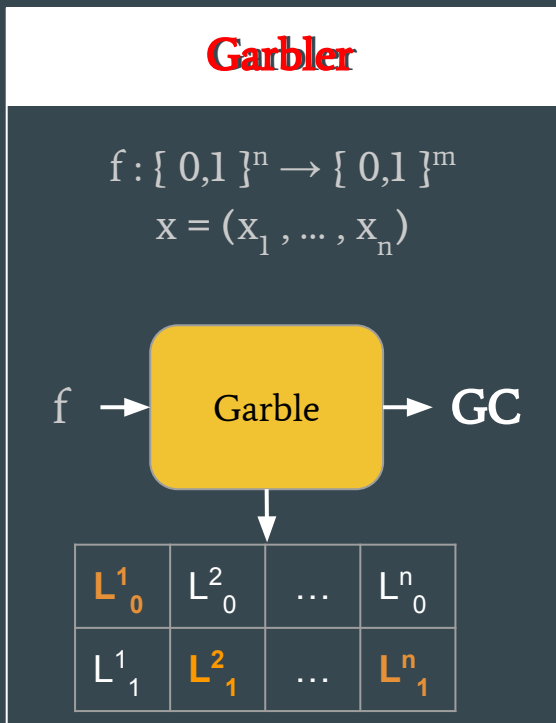
# Rerandomizable Garbled Circuits



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# Semi-Honest Protocol

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## Phase 1

Garble the circuit

## Phase 2

Evaluate the garbling

Bulletin-Board

# Semi-Honest Protocol

## Phase 1

Garble the circuit



## Phase 2

Evaluate the garbling

Bulletin-Board

# Semi-Honest Protocol

## Phase 1

Garble the circuit



UOT 1  
(input)



Bulletin-Board

## Phase 2

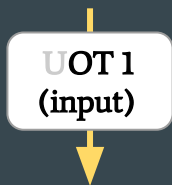
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# Semi-Honest Protocol

## Phase 1

Garble the circuit



## Phase 2

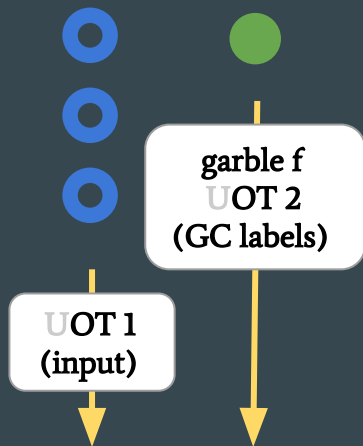
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# Semi-Honest Protocol

## Phase 1

Garble the circuit



## Phase 2

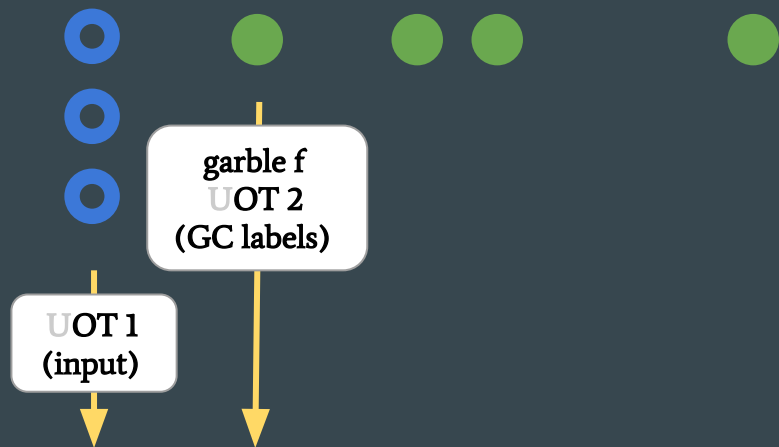
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# Semi-Honest Protocol

## Phase 1

Garble the circuit



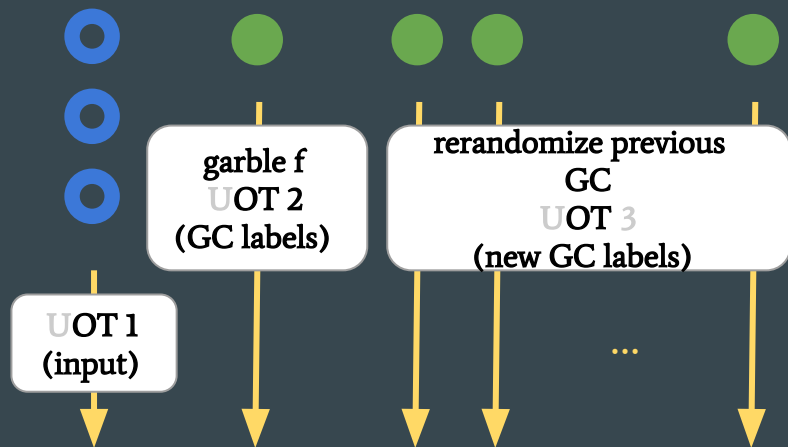
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# Semi-Honest Protocol

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Garble the circuit



## Phase 2

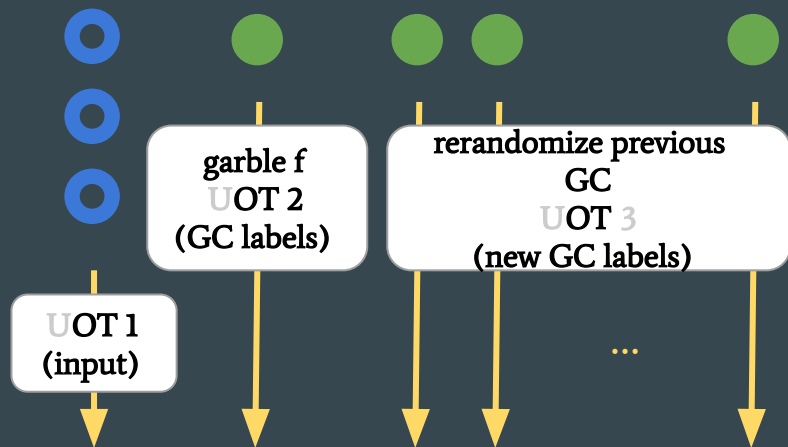
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Bulletin-Board

# Semi-Honest Protocol

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Garble the circuit



## Phase 2

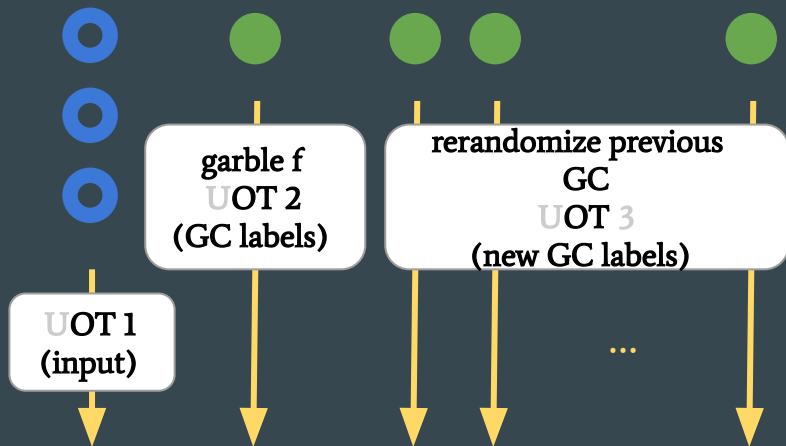
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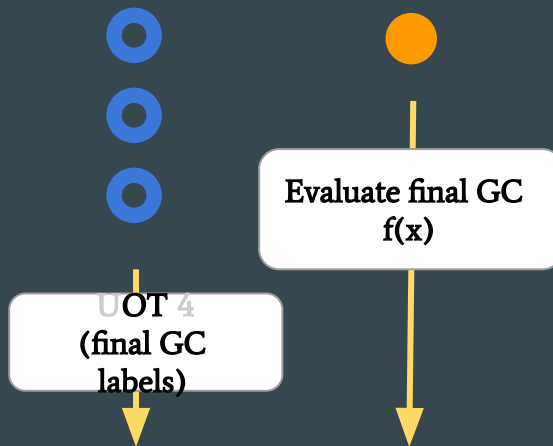
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Garble the circuit



## Phase 2

Evaluate the garbling

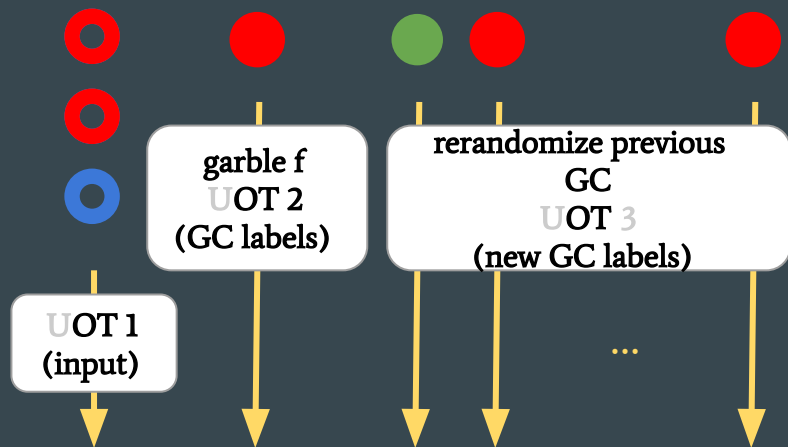


# Semi-Honest Protocol



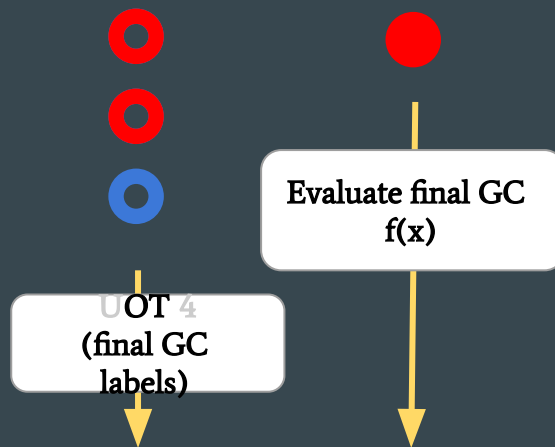
## Phase 1

Garble the circuit



## Phase 2

Evaluate the garbling



# Lifting to Malicious Security



# Lifting to Malicious Security

Security with Abort

# Lifting to Malicious Security

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Semi-honest secure UOT  $\rightarrow$  Maliciously secure UOT

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**Semi-honest secure UOT**  $\rightarrow$  **Maliciously secure UOT**

2-round OT (with special structure) : CRS model

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**Semi-honest secure UOT**  $\rightarrow$  **Maliciously secure UOT**

2-round OT (with special structure) : CRS model

**Forcing Semi-honest behaviour**

# Lifting to Malicious Security

**Semi-honest secure UOT** → **Maliciously secure UOT**

2-round OT (with special structure) : CRS model

## **Forcing Semi-honest behaviour**

Approach 1: Generic SNARKs (CRS/RO model)

# Lifting to Malicious Security

Semi-honest secure UOT  $\rightarrow$  Maliciously secure UOT

2-round OT (with special structure) : CRS model

## Forcing Semi-honest behaviour

Approach 1: Generic SNARKs (CRS/RO model)

**Expensive Prover  
Computation**

# Custom Made ZK Proofs



Black-Box in RGS



# ZK Proof for Correct Garbling

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# ZK Proof for Correct Garbling

Prover

Verifier

---

# ZK Proof for Correct Garbling

**Prover**

Witness: randomness  $r$

**Verifier**

Public:  $f$ ,  $GC$

---

# ZK Proof for Correct Garbling

**Prover**

Witness: randomness  $\mathbf{r}$

**Verifier**

Public:  $\mathbf{f}$ ,  $\mathbf{GC}$

compute  $\mathbf{RGC} = \text{Rerand}(\mathbf{GC}; \mathbf{r}') \longrightarrow \mathbf{RGC}$

---

# ZK Proof for Correct Garbling

**Prover**

Witness: randomness  $r$

**Verifier**

Public:  $f$ ,  $GC$

compute  $RGC = \text{Rerand}(GC; r') \longrightarrow RGC$

$\longleftarrow b \leftarrow \{0,1\}$

---

# ZK Proof for Correct Garbling

**Prover**

Witness: randomness  $r$

compute  $\mathbf{RGC} = \text{Rerand}(\mathbf{GC}; r') \longrightarrow \mathbf{RGC}$

$\longleftarrow b \leftarrow \{0,1\}$

**Verifier**

Public:  $f, \mathbf{GC}$

**Case 0:** check if  $\mathbf{RGC}$  correctly rerandomized from  $\mathbf{GC}$

# ZK Proof for Correct Garbling

**Prover**

Witness: randomness  $r$

compute  $\mathbf{RGC} = \text{Rerand}(\mathbf{GC}; r') \longrightarrow \mathbf{RGC}$

$\longleftarrow b \leftarrow \{0,1\}$

**Verifier**

Public:  $f, \mathbf{GC}$

**Case 0:** check if  $\mathbf{RGC}$  correctly rerandomized from  $\mathbf{GC}$

**Case 1:** check if  $\mathbf{RGC}$  correctly garbled from  $f$

# ZK Proof for Correct Garbling

**Prover**

Witness: randomness  $r$

compute  $\mathbf{RGC} = \text{Rerand}(\mathbf{GC}; r) \longrightarrow \mathbf{RGC}$

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**Case 0:** check if  $\mathbf{RGC}$  correctly rerandomized from  $\mathbf{GC}$

**Case 1:** check if  $\mathbf{RGC}$  correctly garbled from  $f$

—

soundness  $\frac{1}{2}$   
amplify by parallel repetition

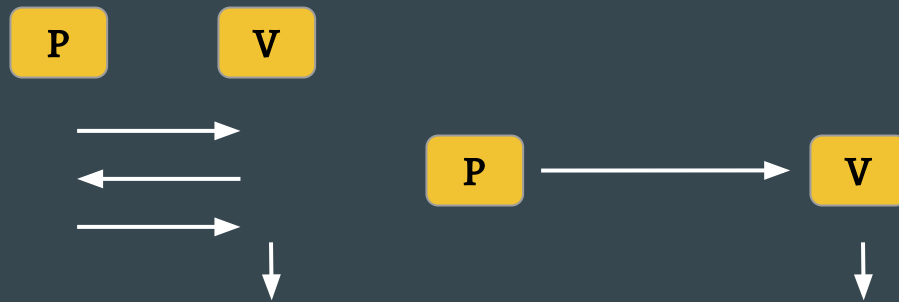


# Approach 2: Ephemeral Prover Zero-Knowledge

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## Option 1

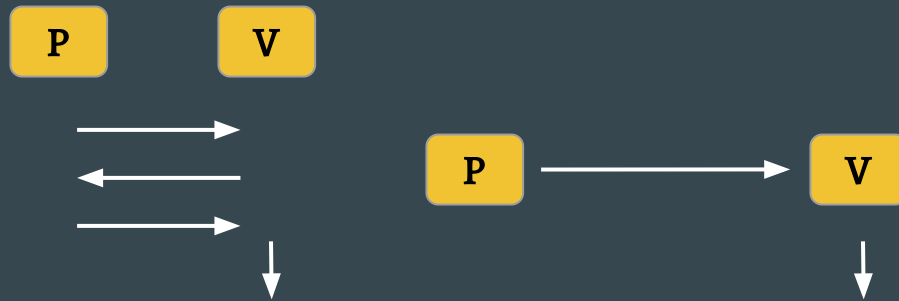
RO Model – Fiat-Shamir transform



# Approach 2: Ephemeral Prover Zero-Knowledge

## Option 1

RO Model – Fiat-Shamir transform



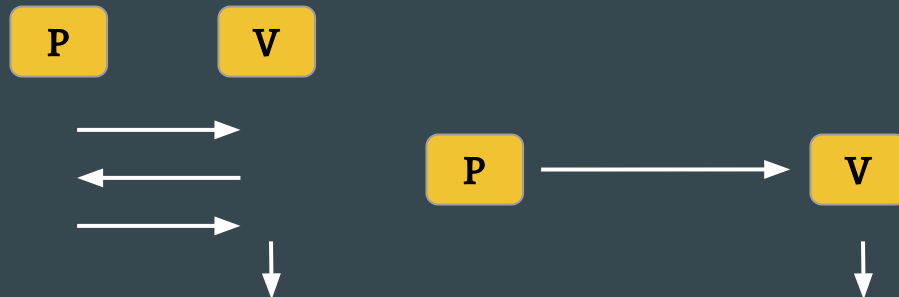
## Option 2

CRS Model – Distributed Committed-Index OT

# Approach 2: Ephemeral Prover Zero-Knowledge

## Option 1

RO Model – Fiat-Shamir transform



## Option 2

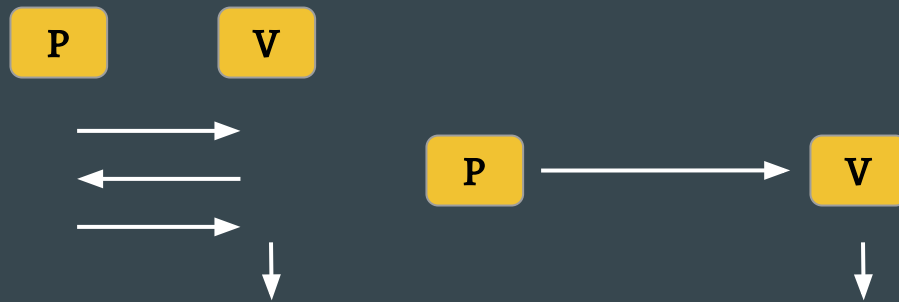
CRS Model – Distributed Committed-Index OT

multi-receiver OT Protocol:

# Approach 2: Ephemeral Prover Zero-Knowledge

## Option 1

RO Model – Fiat-Shamir transform



## Option 2

CRS Model – Distributed Committed-Index OT

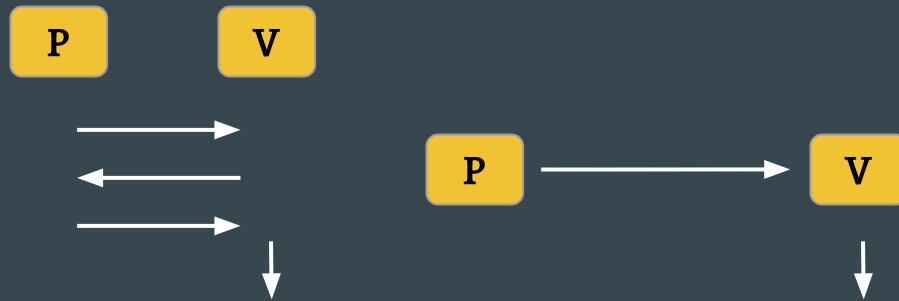
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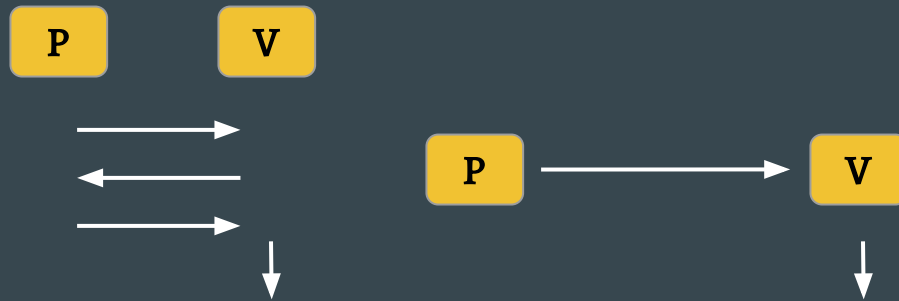
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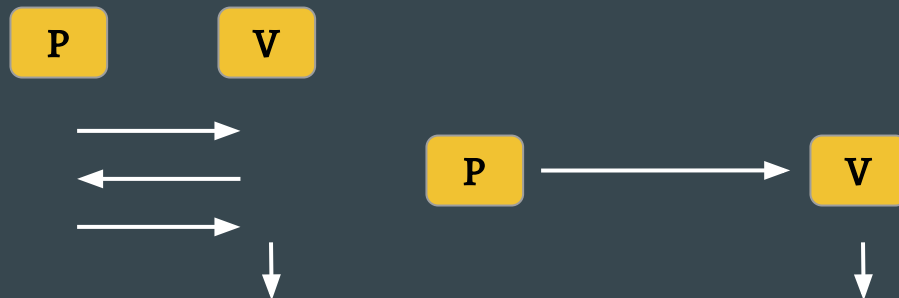
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- server sends **first** proof message and OTs the **third** proof message

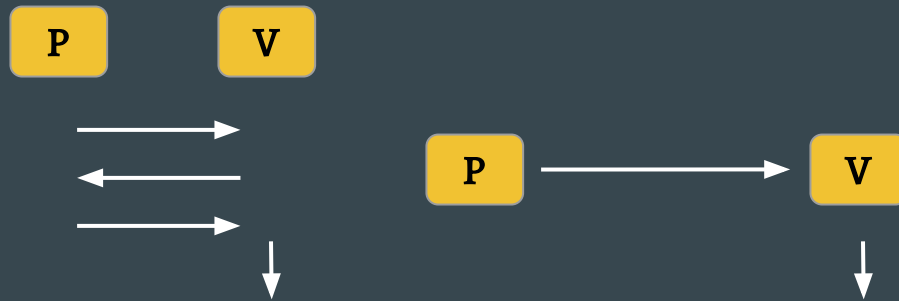




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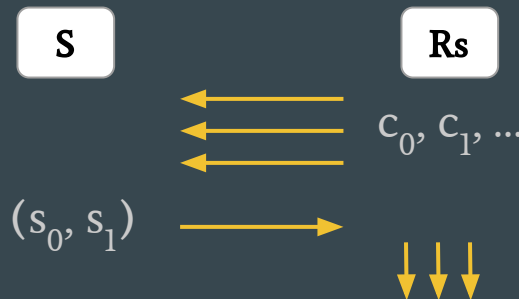


## Option 2

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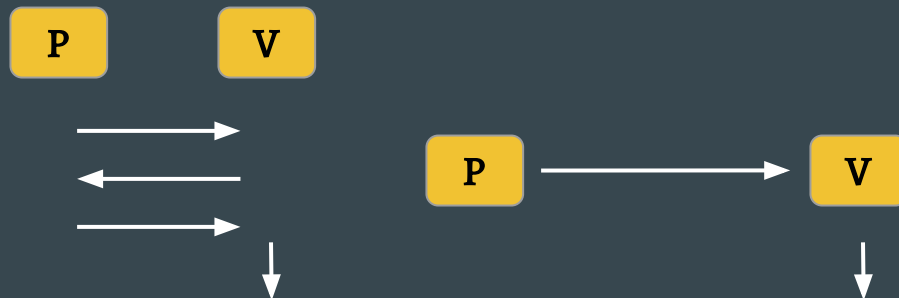
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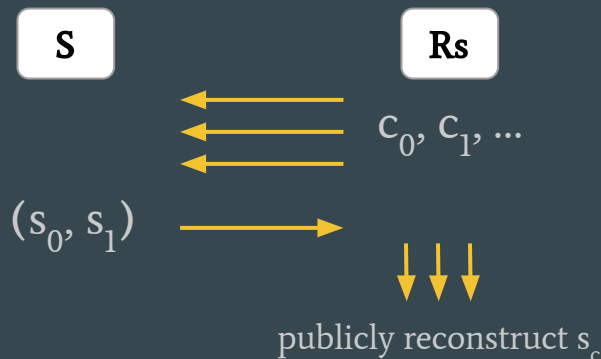


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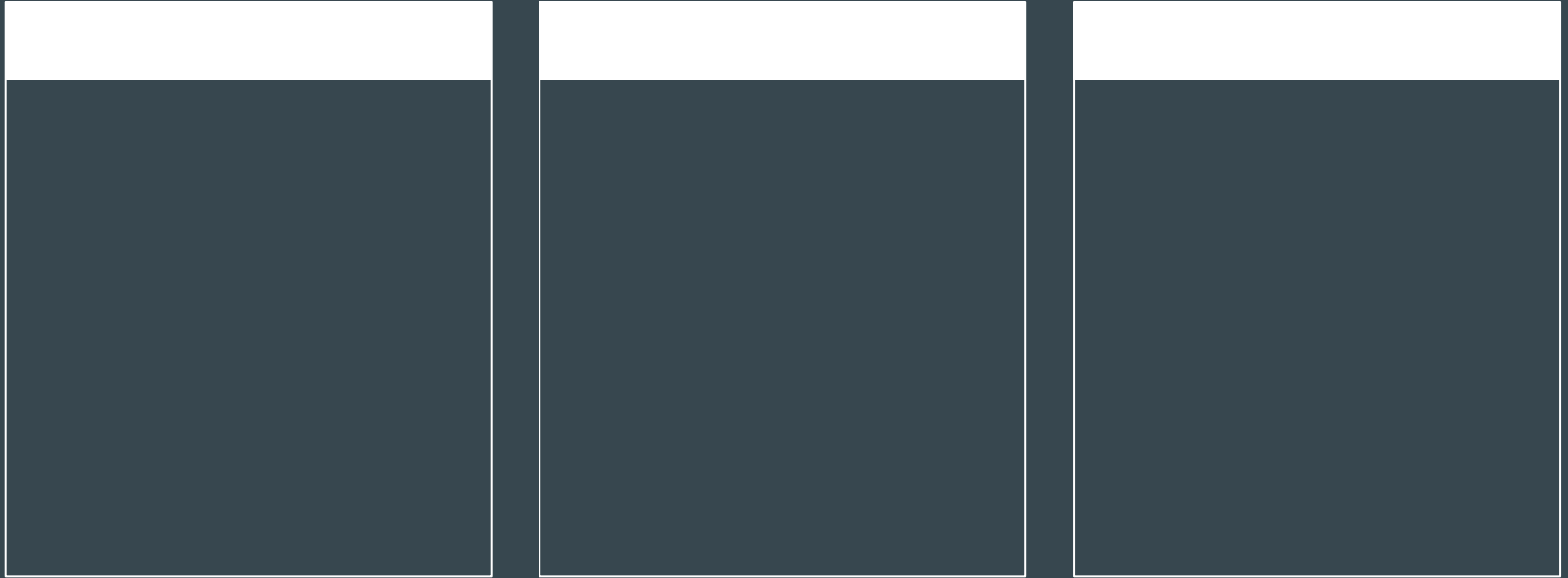
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# Maliciously Secure SCALES Protocol



Bulletin-Board

# Maliciously Secure SCALES Protocol

Encoding Phase

Bulletin-Board

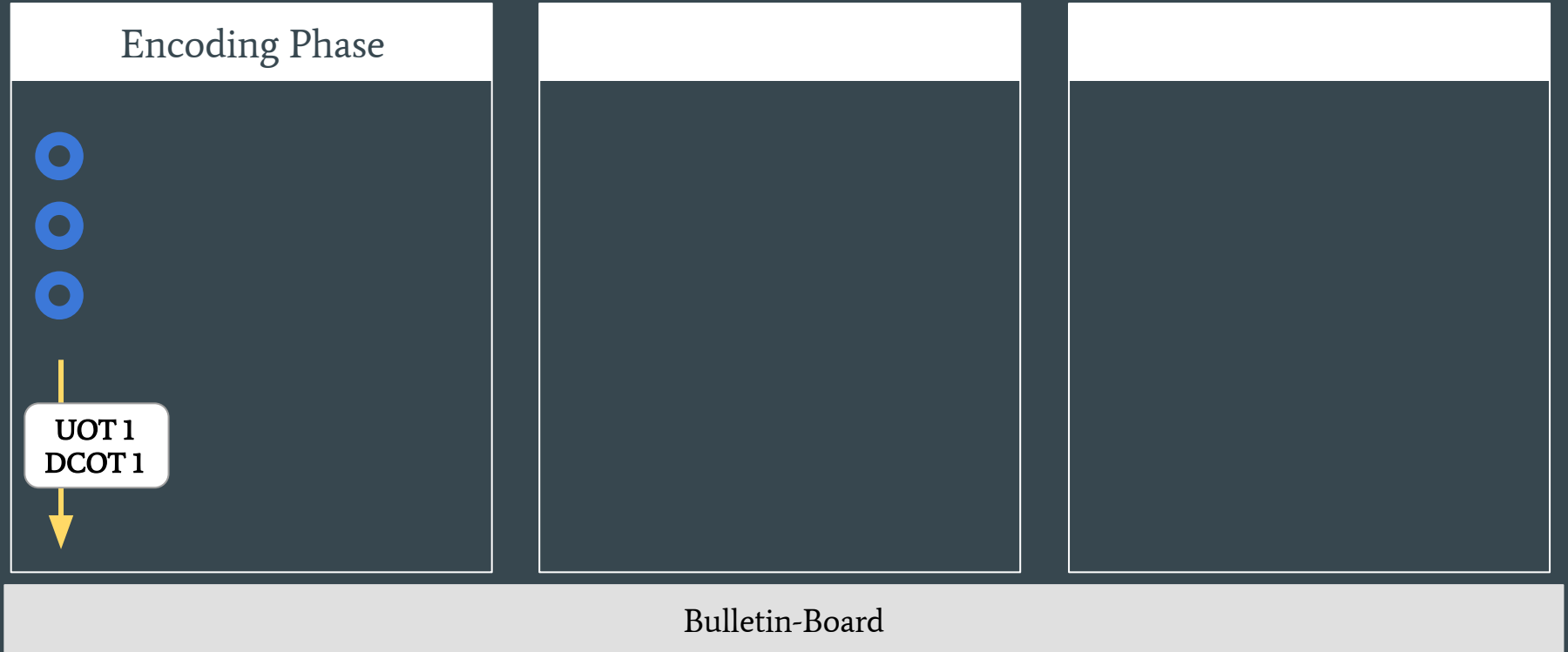
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Encoding Phase

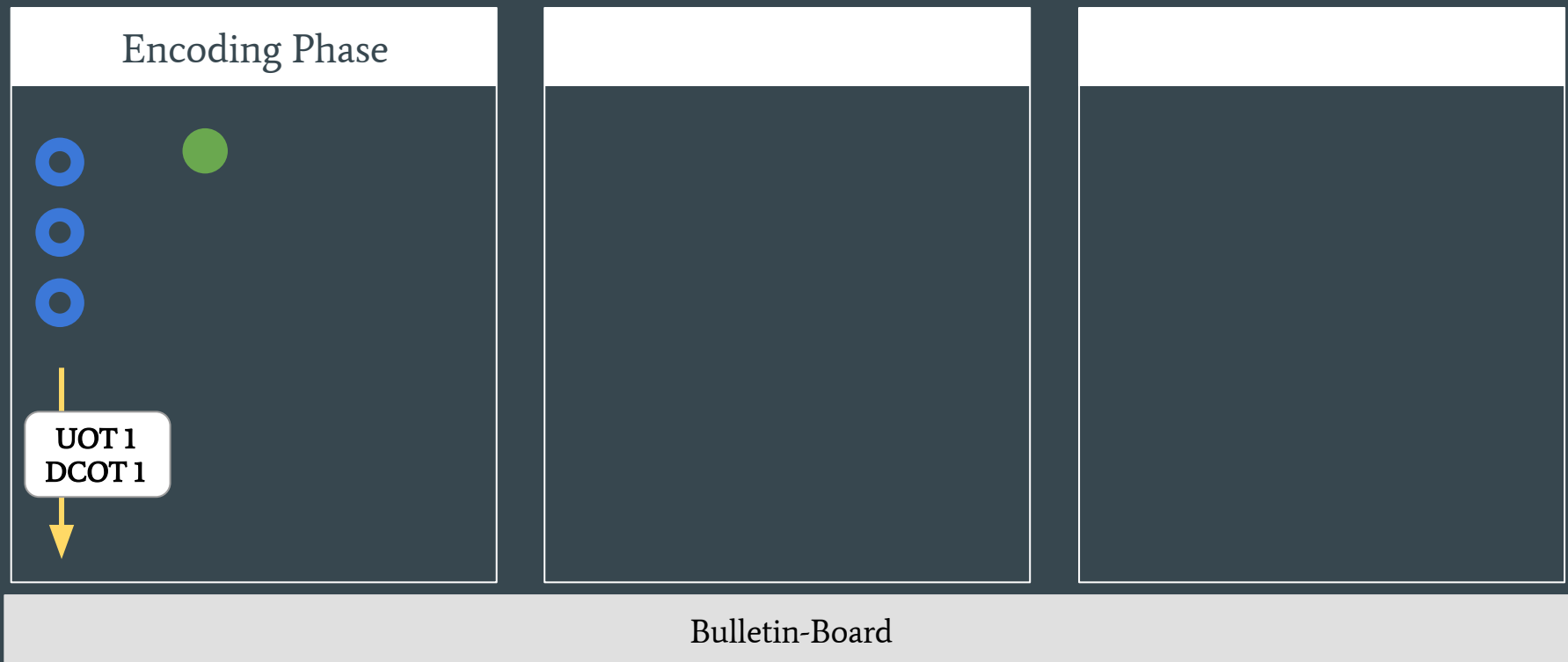


Bulletin-Board

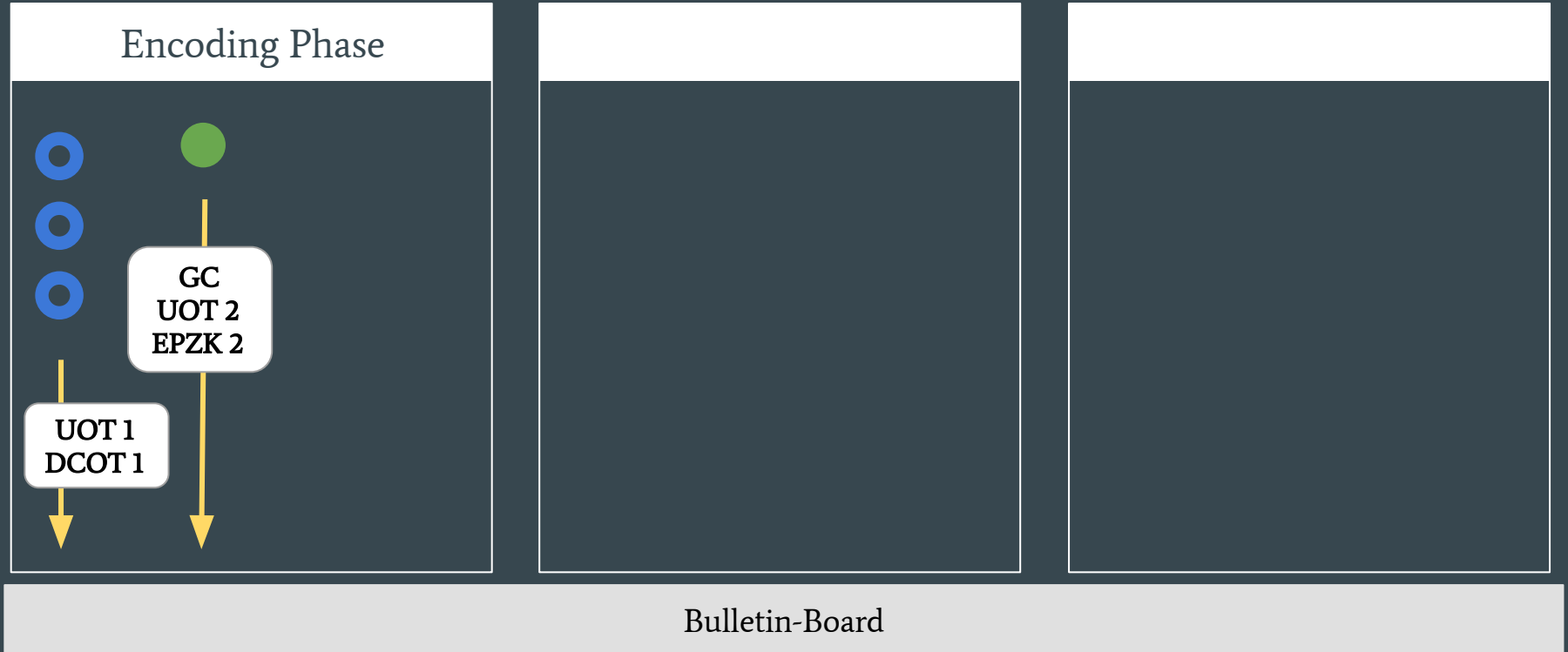
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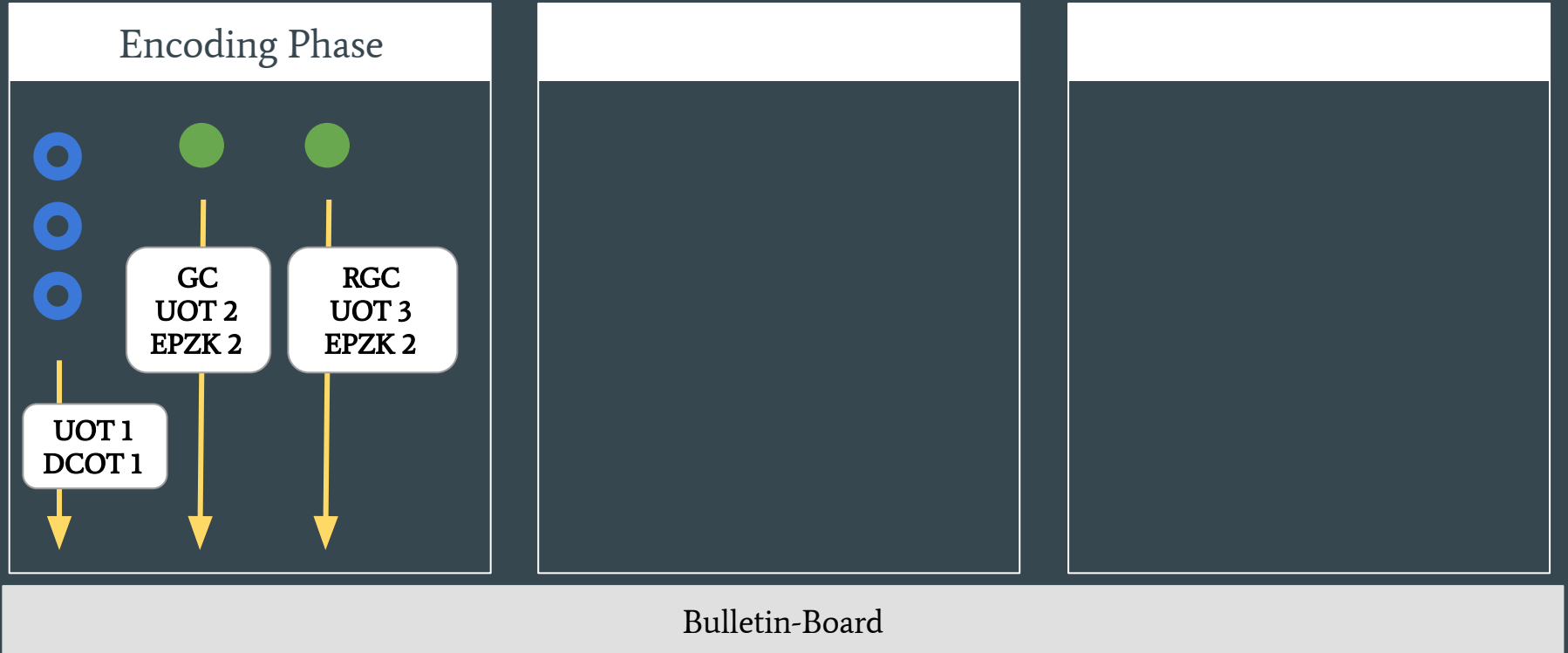


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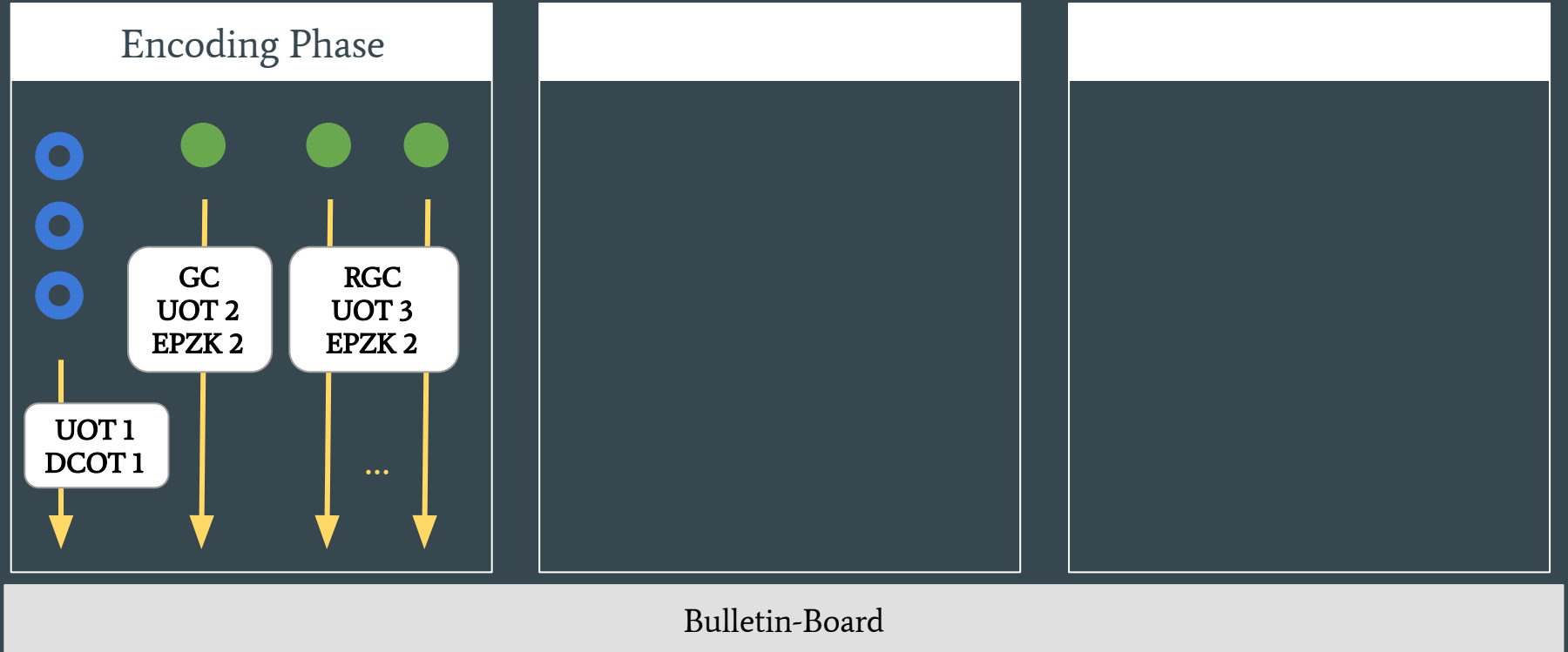




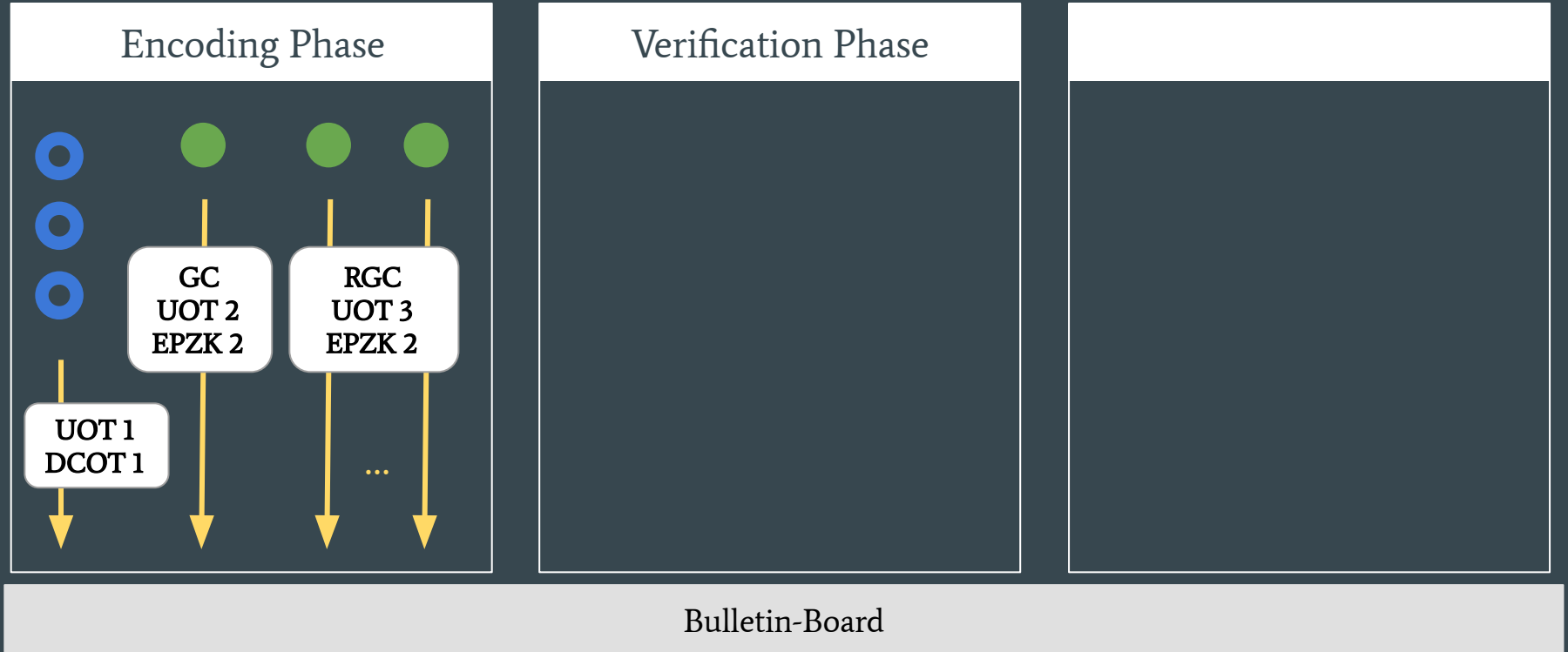
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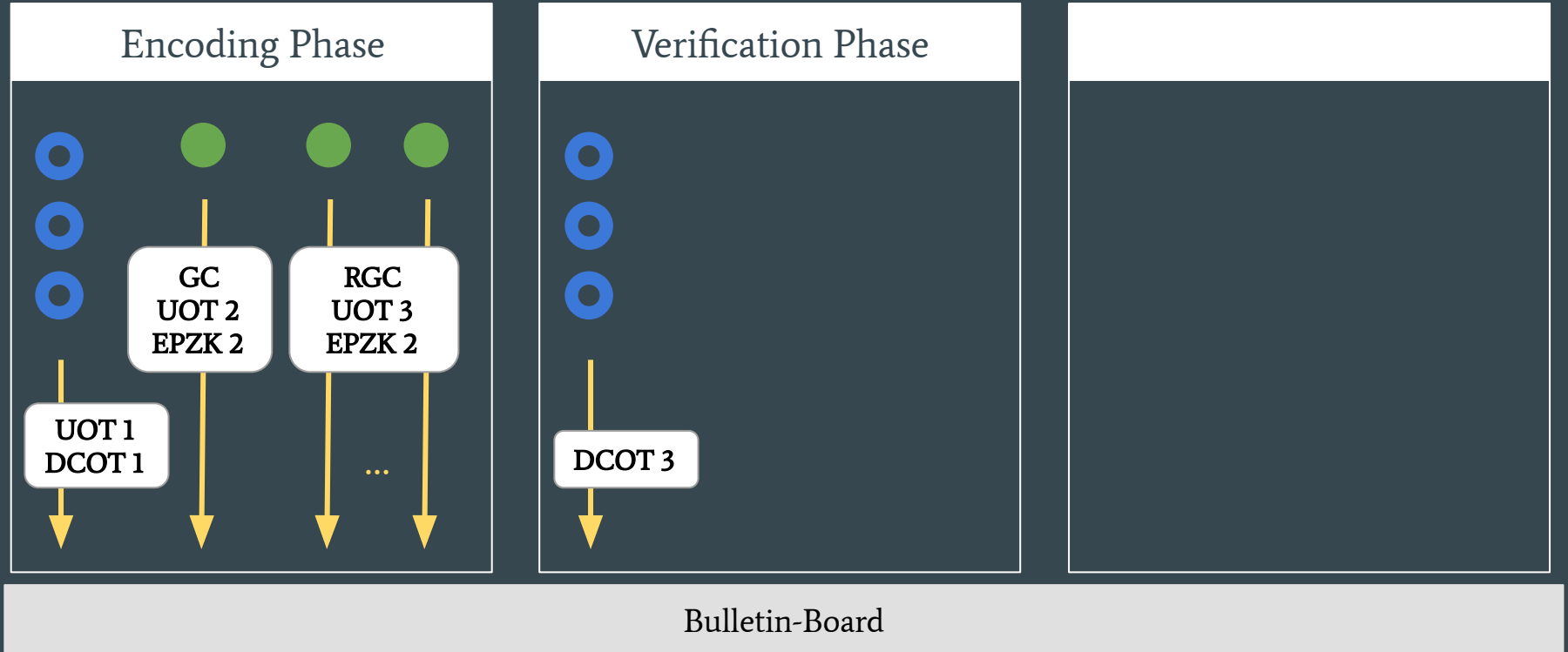
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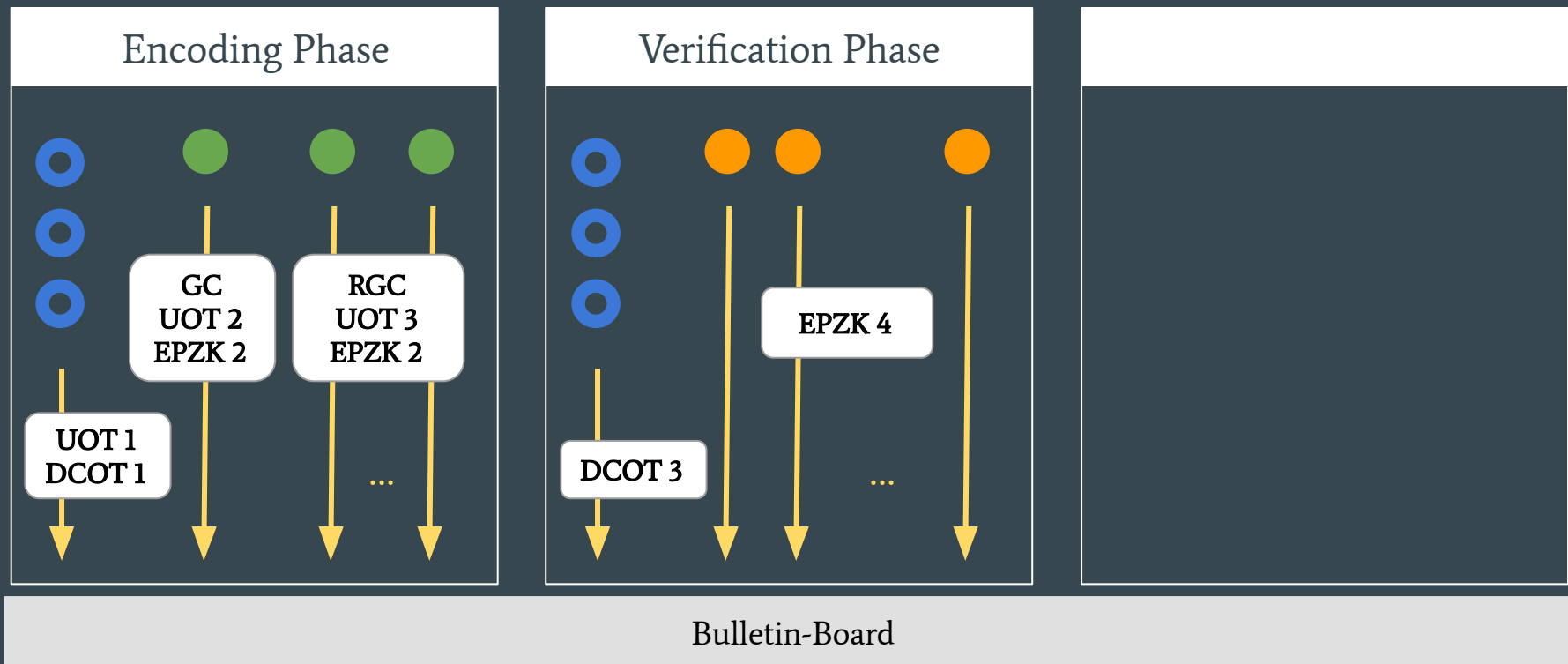
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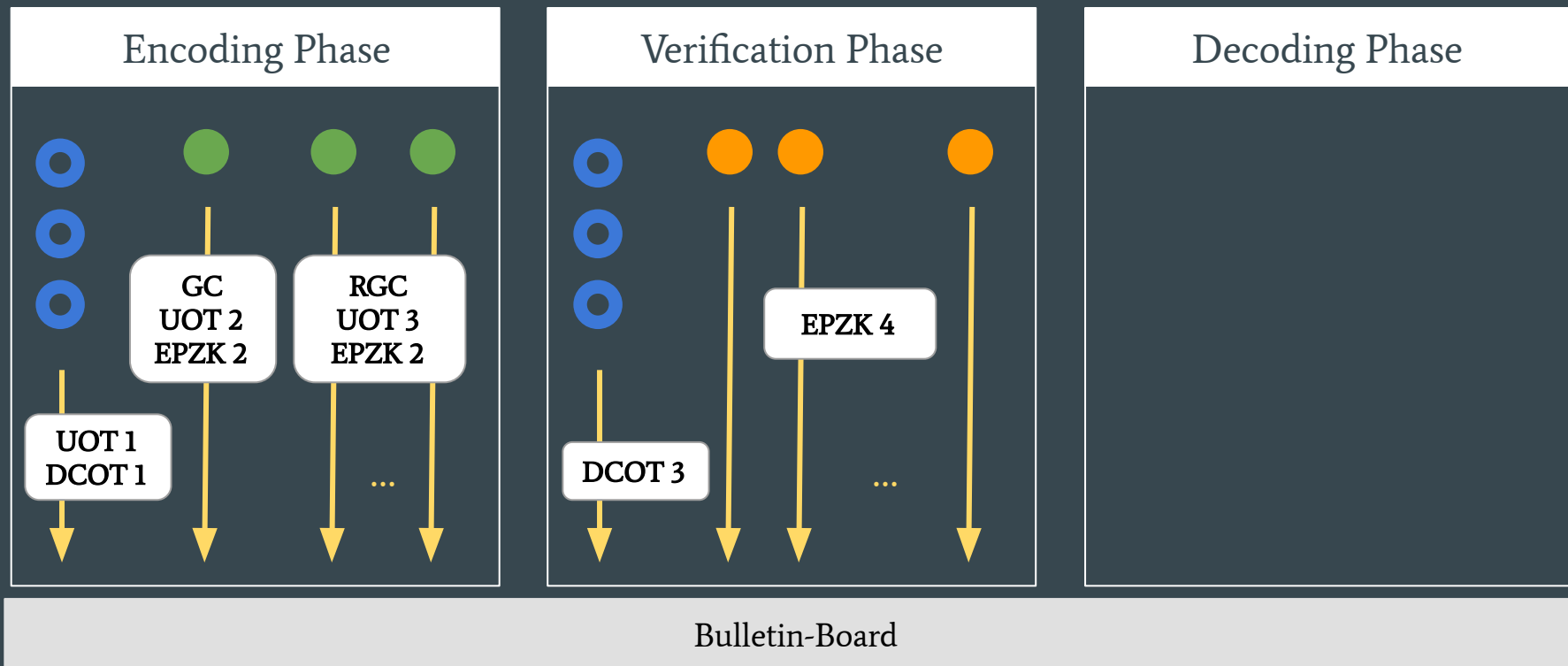
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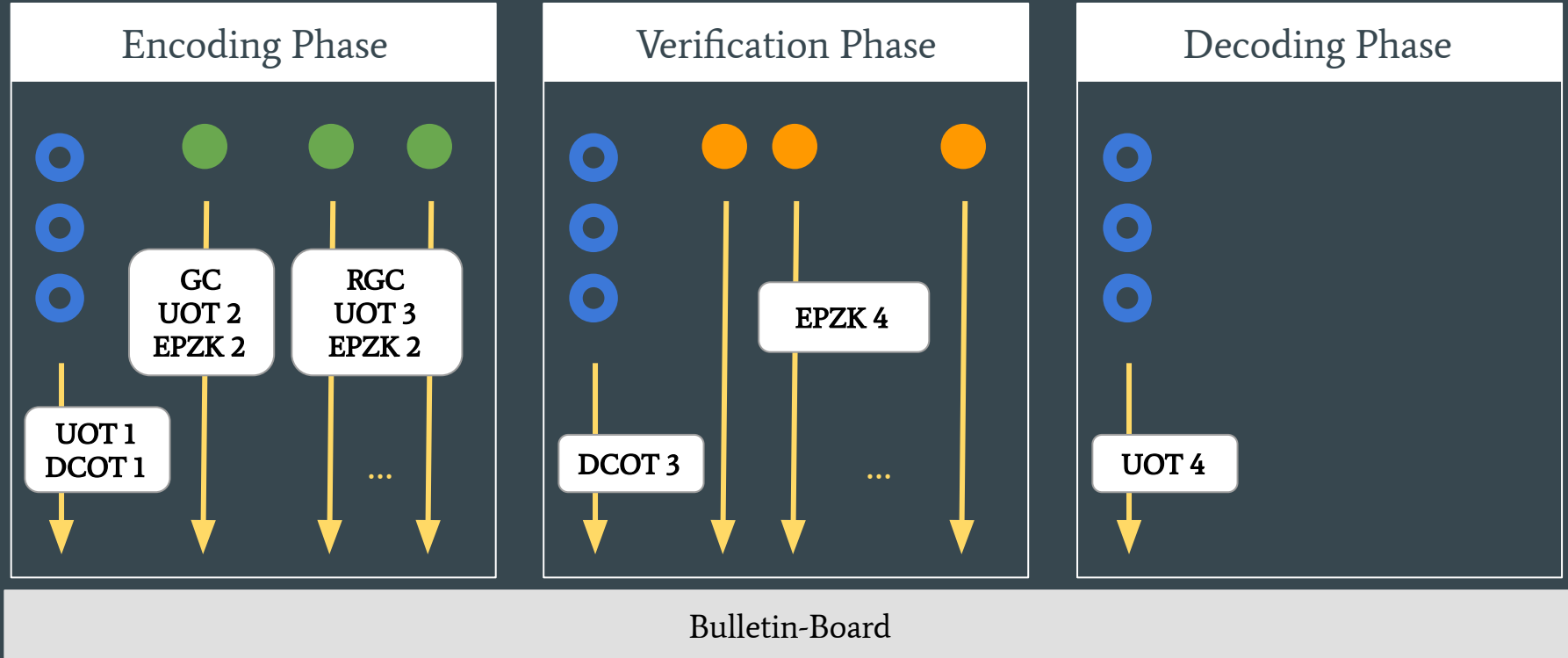
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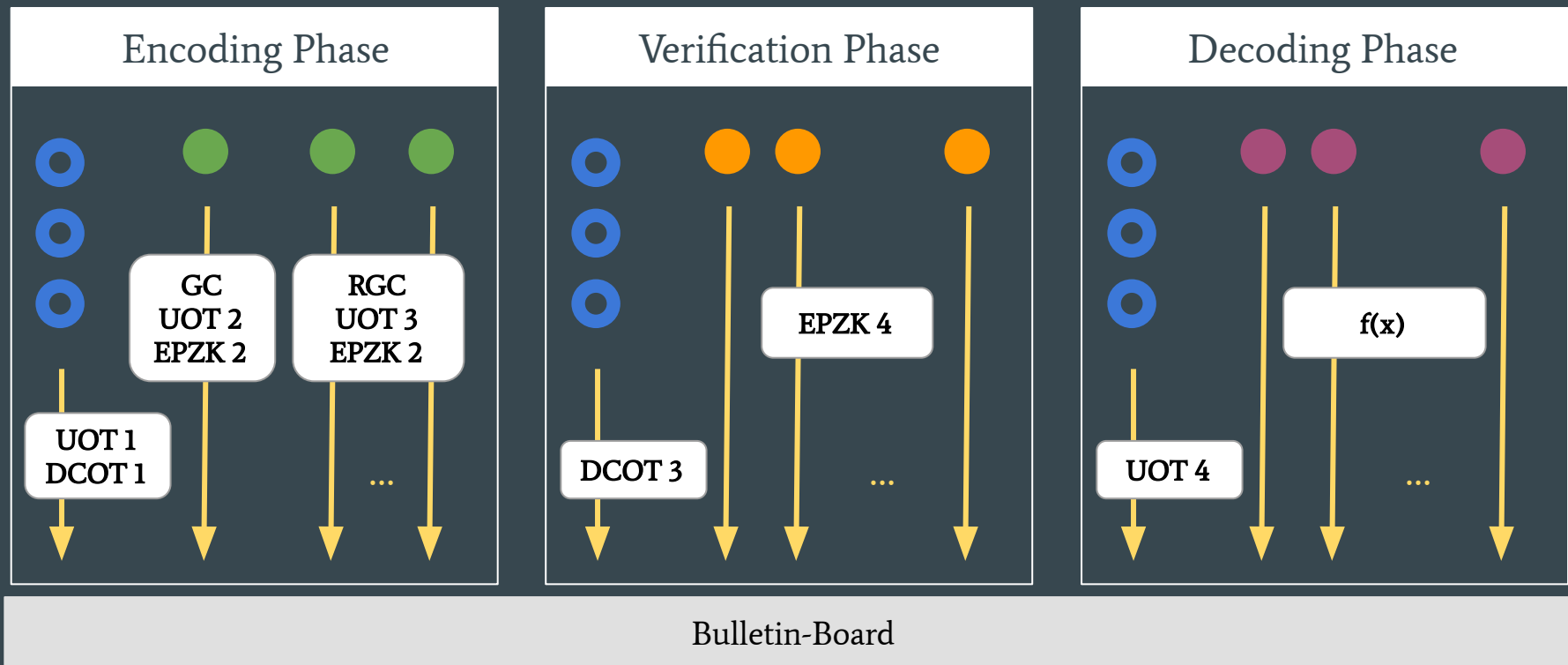
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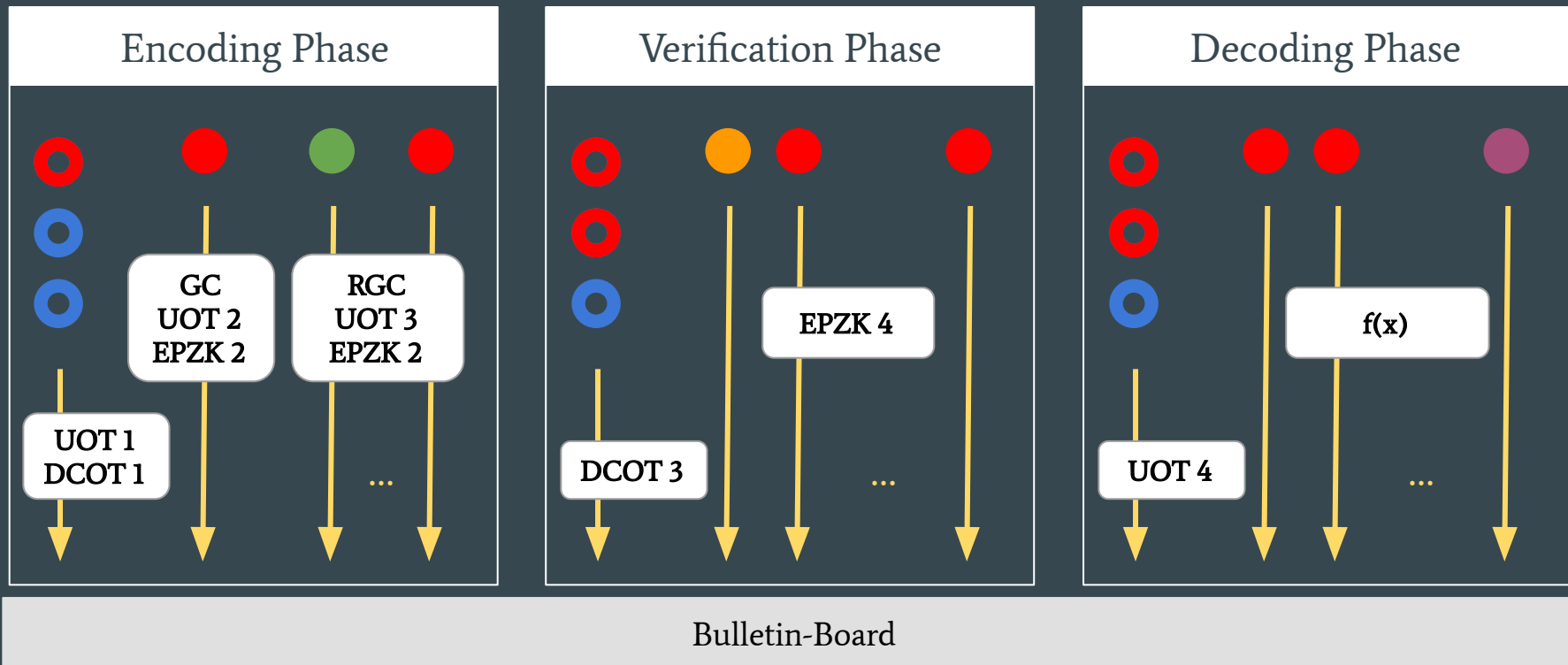


# Maliciously Secure SCALES Protocol





# Maliciously Secure SCALES Protocol



# Summary

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Maliciously Secure SCALES Protocols –

**Assuming DDH**

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- using Custom ZK proofs      2 phases – CRS + RO model

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**Universally Composable**

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Maliciously Secure SCALES Protocols –

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Open Problems –

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Maliciously Secure SCALES Protocols –

- using Custom ZK proofs      2 phases – CRS + RO model  
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Open Problems –

- SCALES protocols with Guaranteed Output Delivery

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# Summary

Maliciously Secure SCALES Protocols –

- using Custom ZK proofs      2 phases – CRS + RO model  
3 phases – CRS model

Open Problems –

- SCALES protocols with Guaranteed Output Delivery
- SCALES protocols in the RO model only (or in the plain model)
- SCALES from other hardness assumptions

**Assuming DDH**

**Universally Composable**

# Thank You!



<https://eprint.iacr.org/2024/383>