

# Black-Box (and Fast) Non-Malleable Zero Knowledge

Vincenzo Botta  
Sapienza University

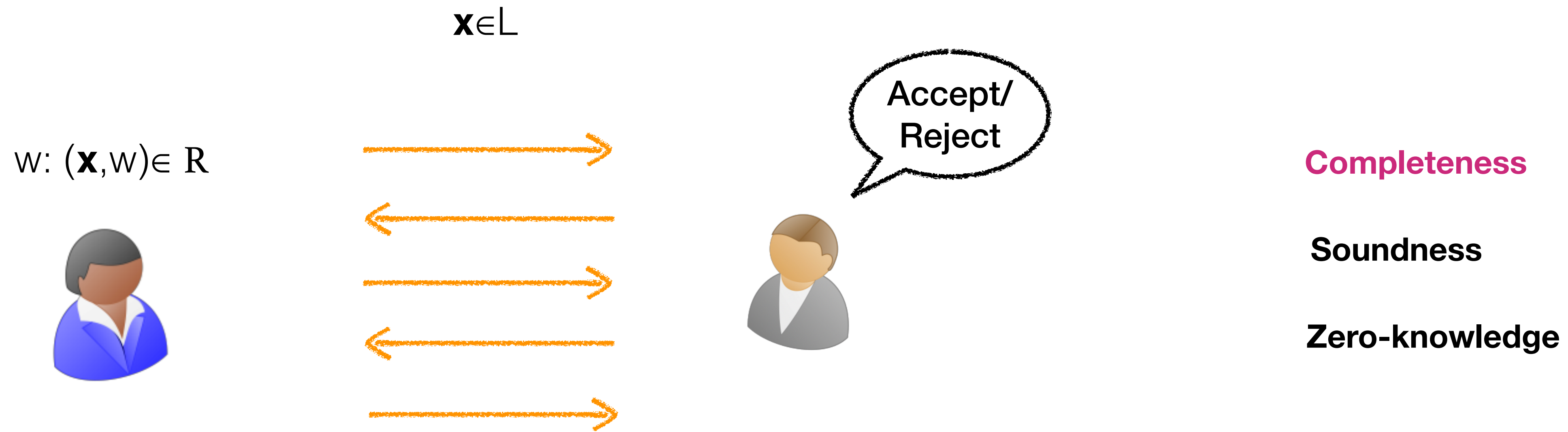
Emmanuela Orsini  
Bocconi University

Ivan Visconti  
University of Salerno

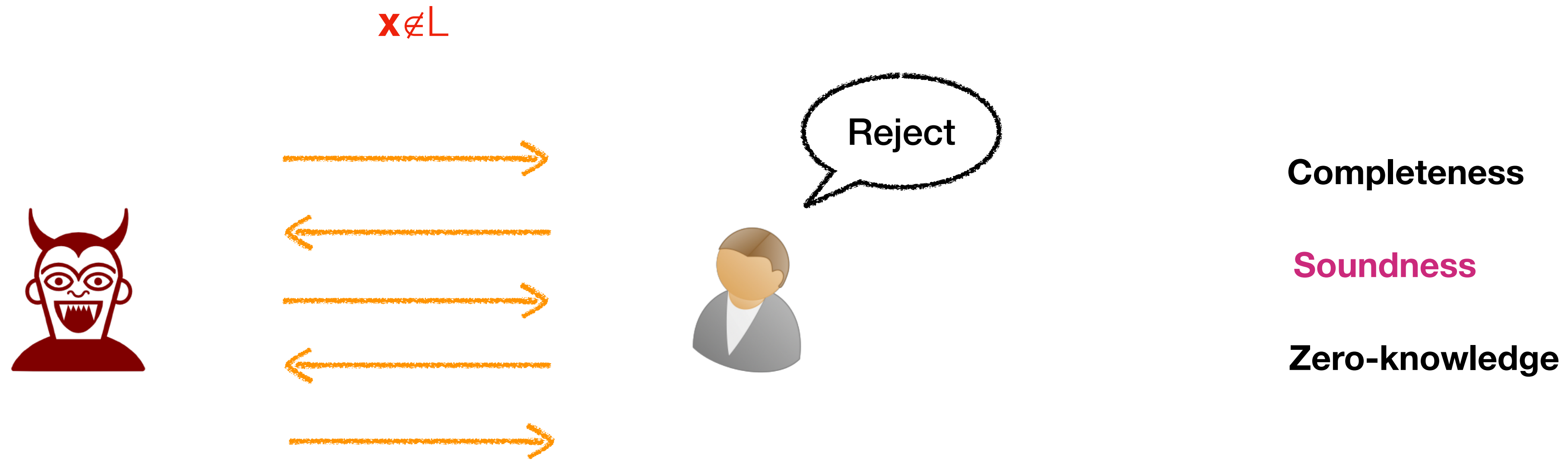
Michele Ciampi  
The University of Edinburgh

Luisa Siniscalchi  
Danish Technical University

# Zero-knowledge proofs



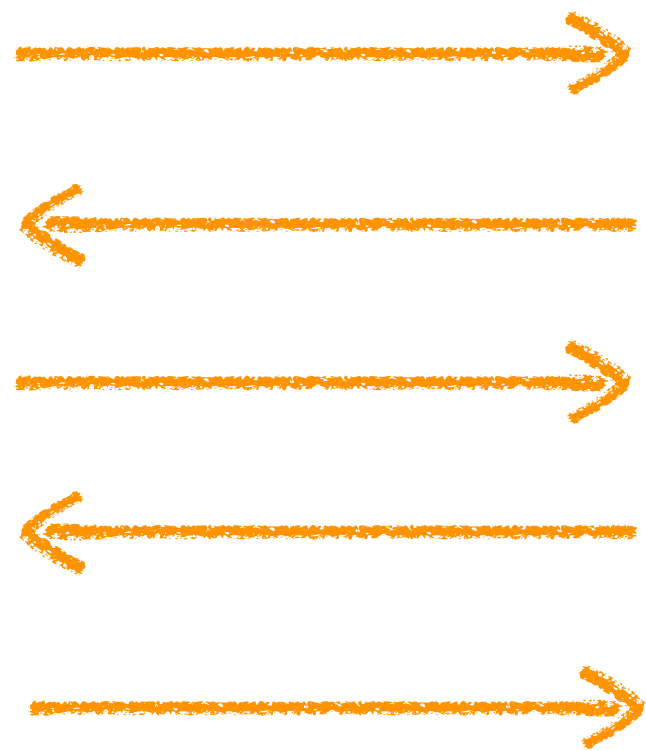
# Zero-knowledge proofs



# Zero-knowledge proofs

$x \in L$

$w: (x, w) \in R$



Output<sup>Real</sup>

**Completeness**

**Soundness**

**Zero-knowledge**



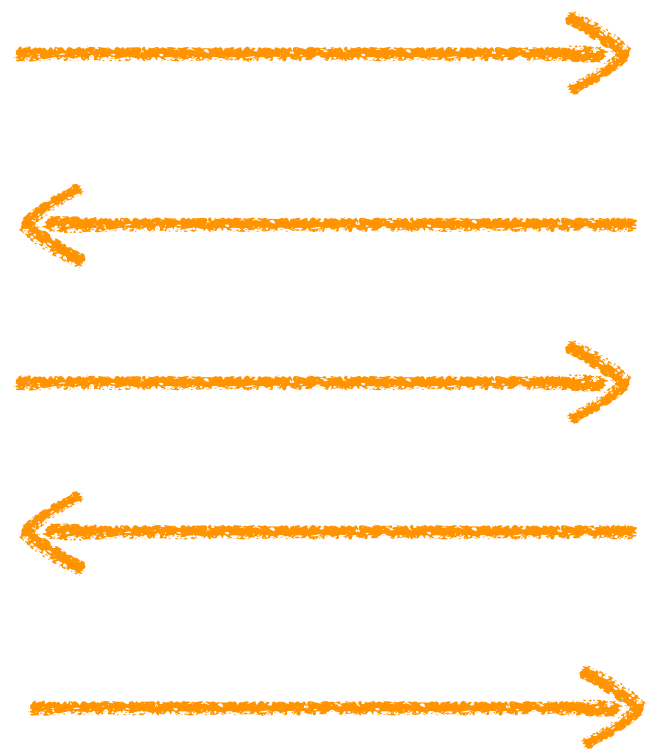
Output<sup>Sim</sup>



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Output<sup>Real</sup>

**Completeness**

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Output<sup>Sim</sup>

# Non-malleable zero-knowledge

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$x' \in L$

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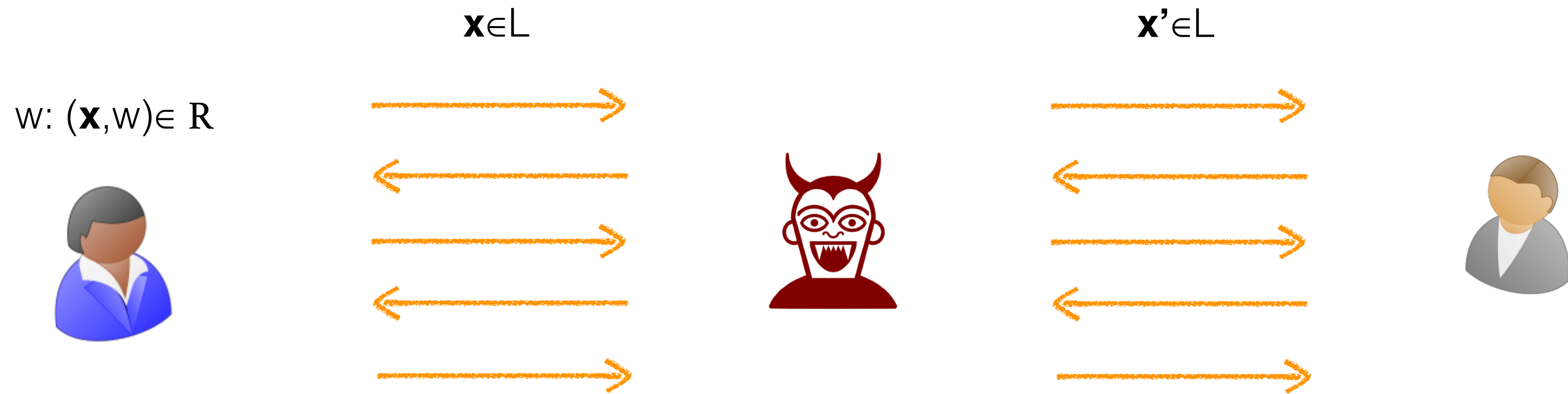
# Non-malleable zero-knowledge



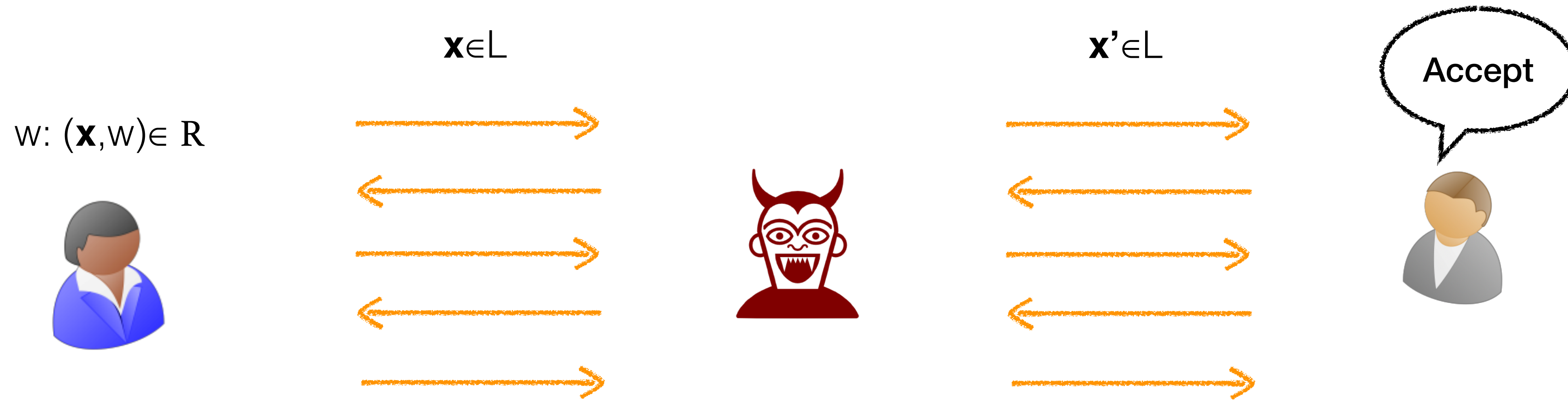
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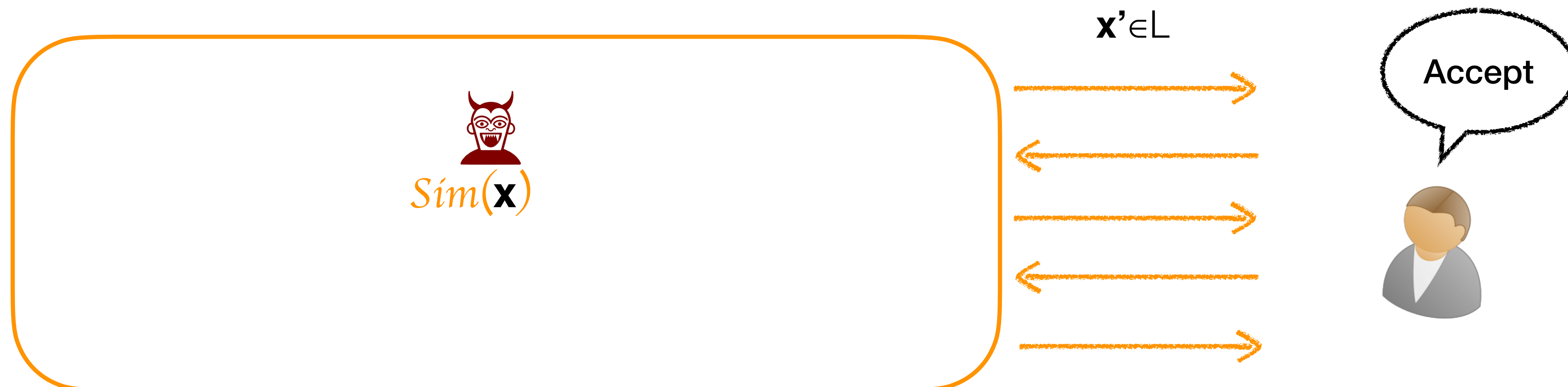
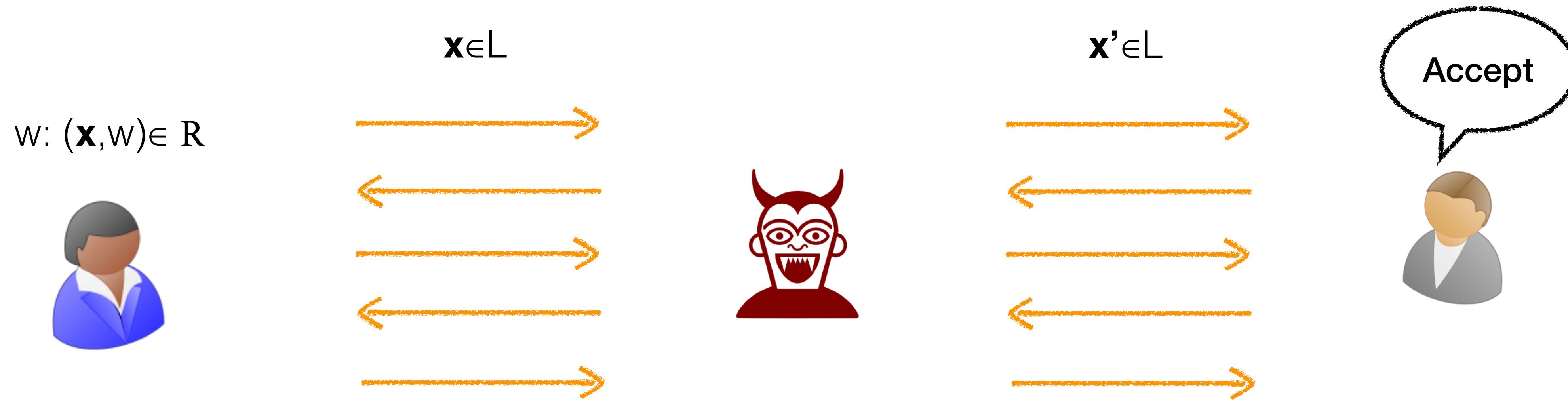
# Non-malleable zero-knowledge



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# Non-malleable zero-knowledge



# State of the art

Black-box simulation  
Plain model (no RO, no setup)  
Minicrypt  
Constant-round  
Black-box use of primitives

Constant round NMZK from one-way functions



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Non-BB protocols

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Non-BB protocols

## Practical

- [KLP22] Allen Kim, Xiao Liang, and Omkant Pandey. A new approach to efficient non-malleable zero-knowledge. CRYPTO 2022

	Rounds	BB use of primitives	SHA-256 preimage	
			Computation	Communication
[KLP22]	>20	non-BB	1680ms	20MB

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The first BB protocol

# Non-malleable commitment

w.r.t. commitment

Exp(0)

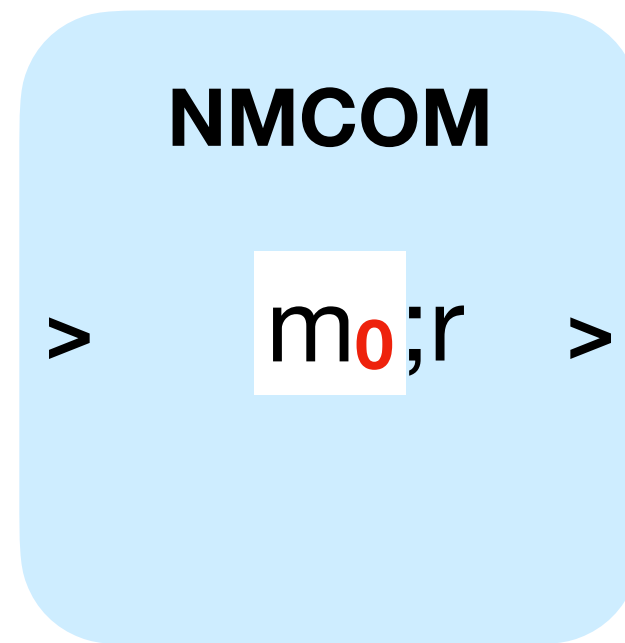


Man In the Middle

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Exp(0)



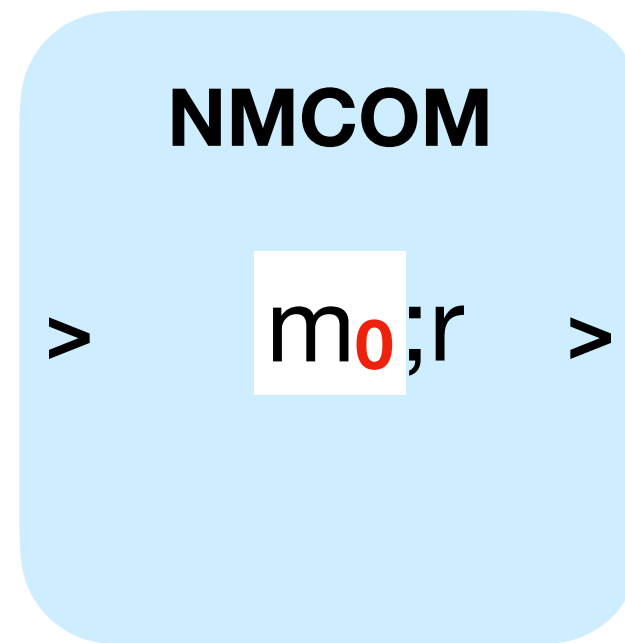
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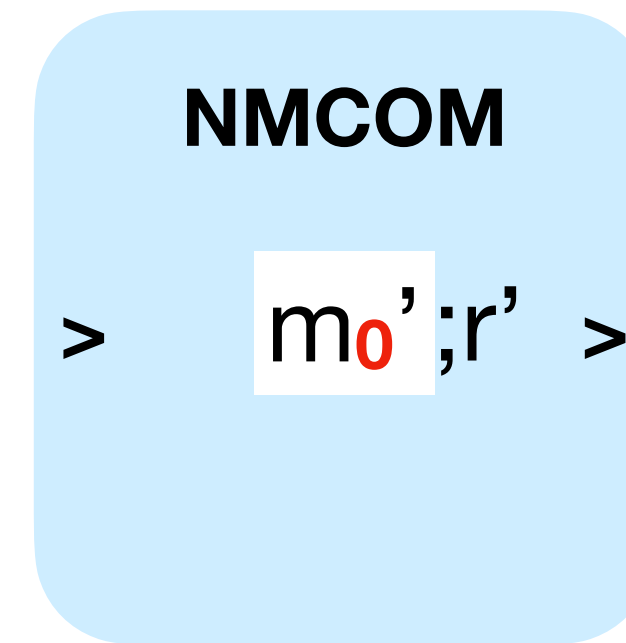
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Man In the Middle

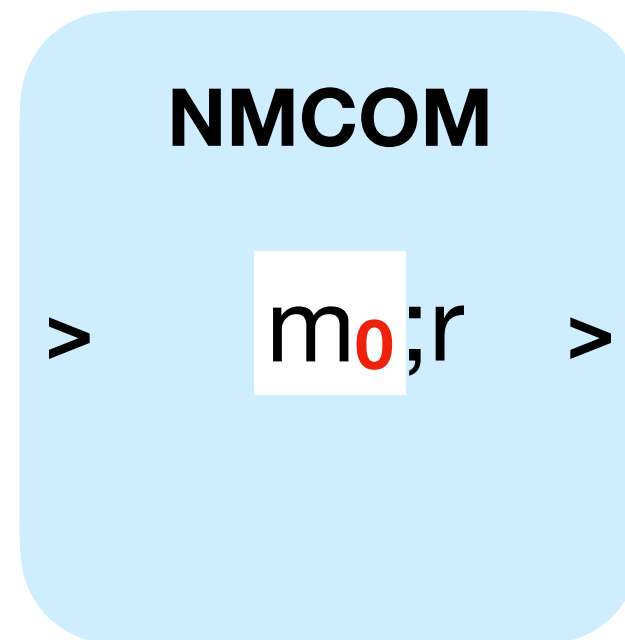




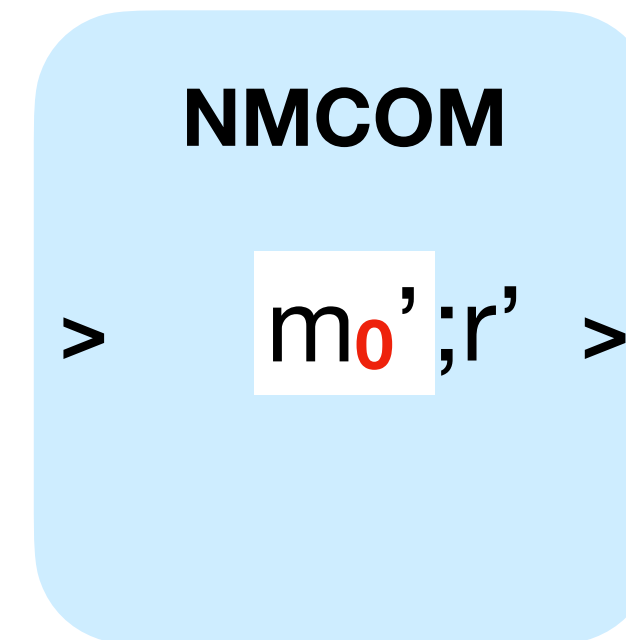
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Man In the Middle



Exp(1)



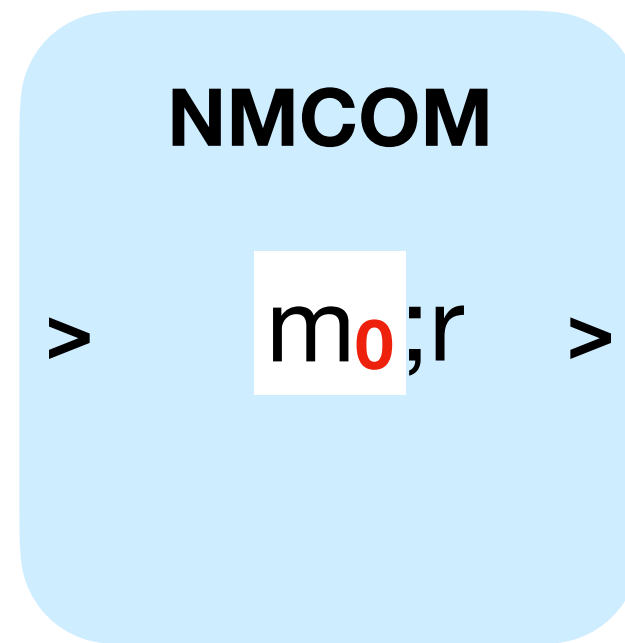
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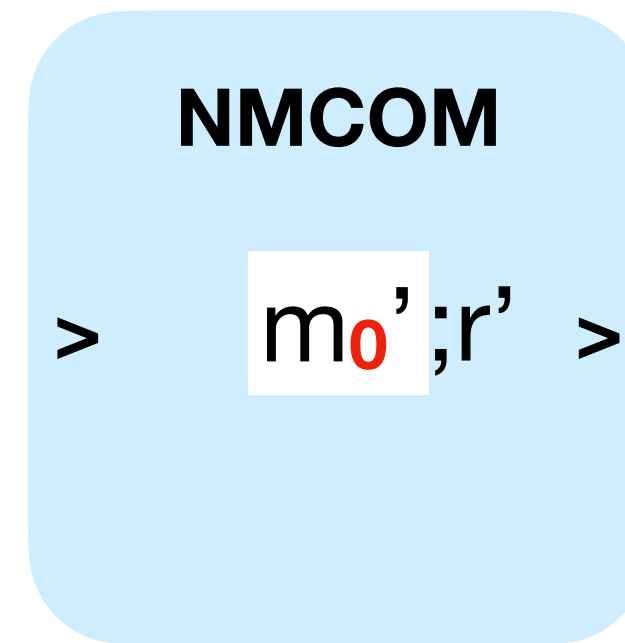
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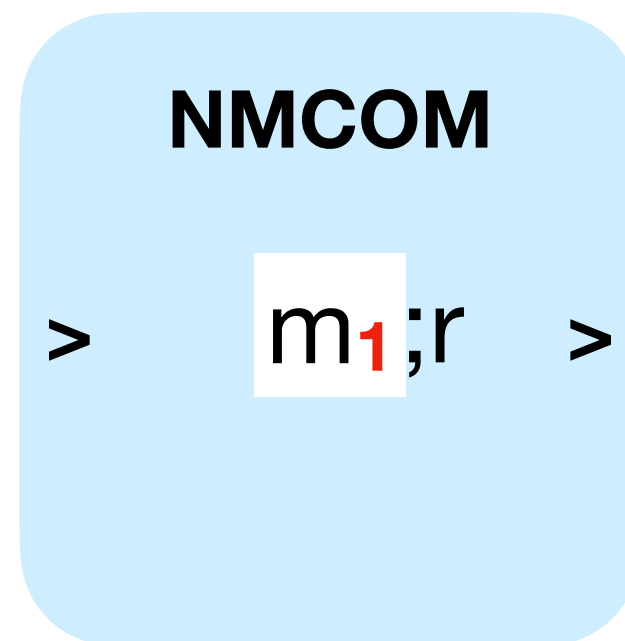
Exp(0)



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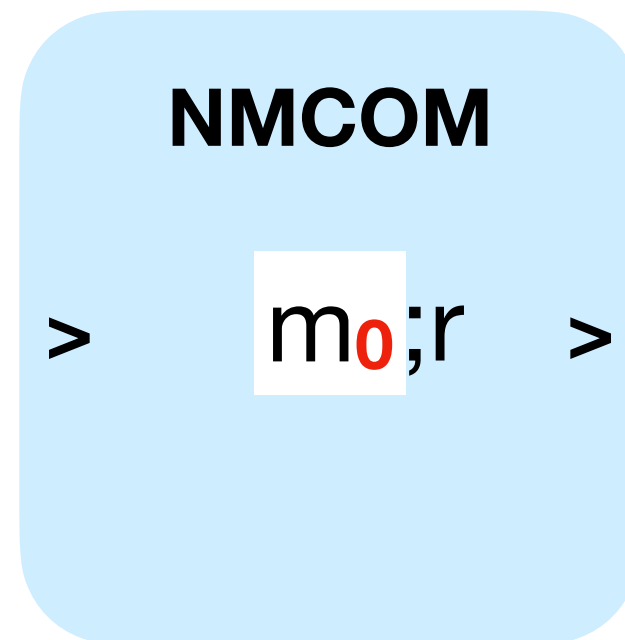
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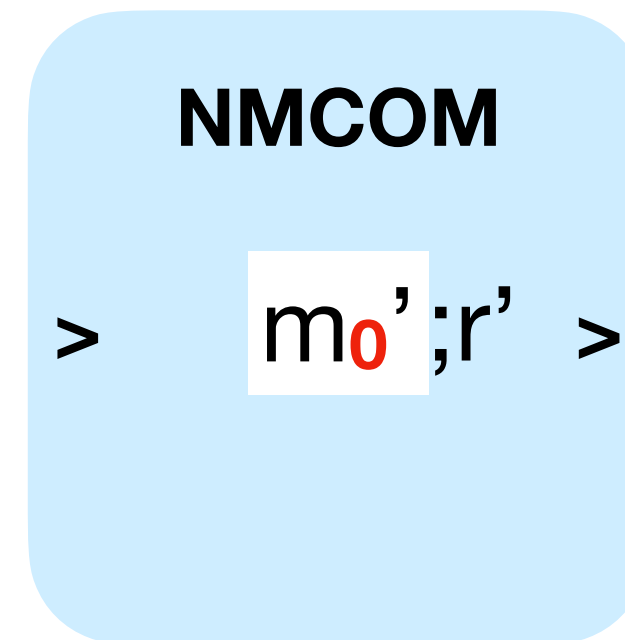
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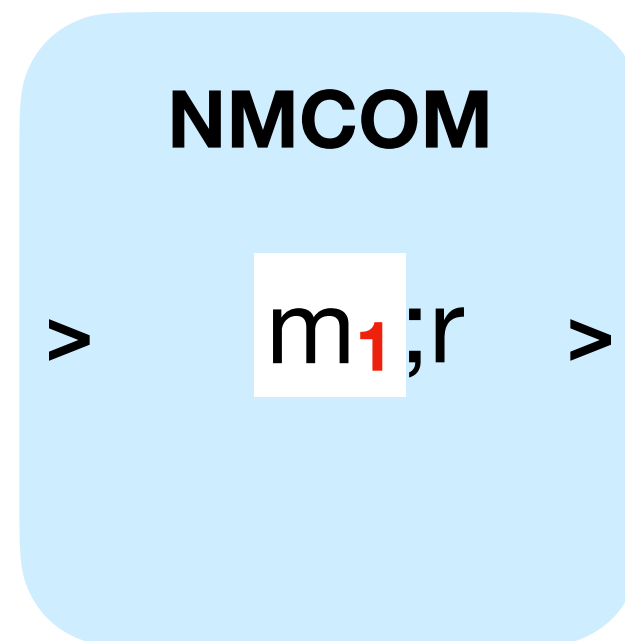
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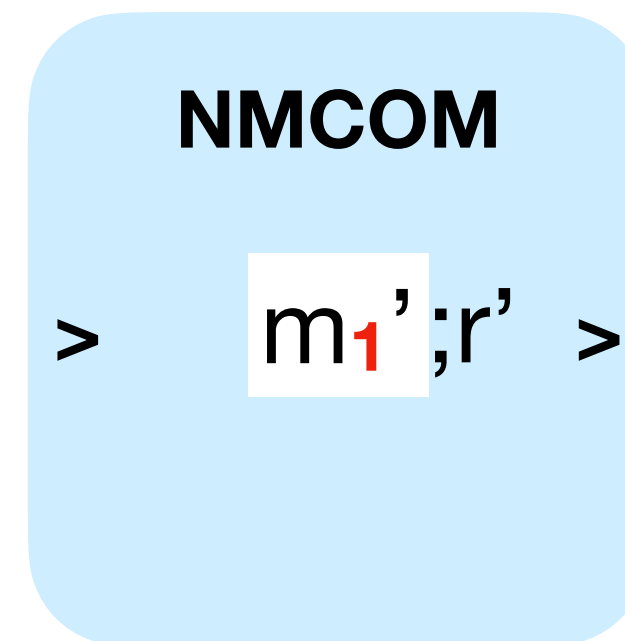
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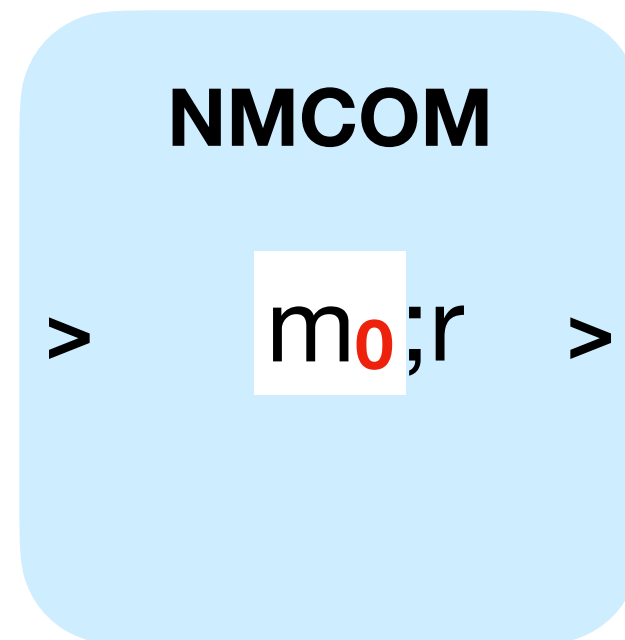
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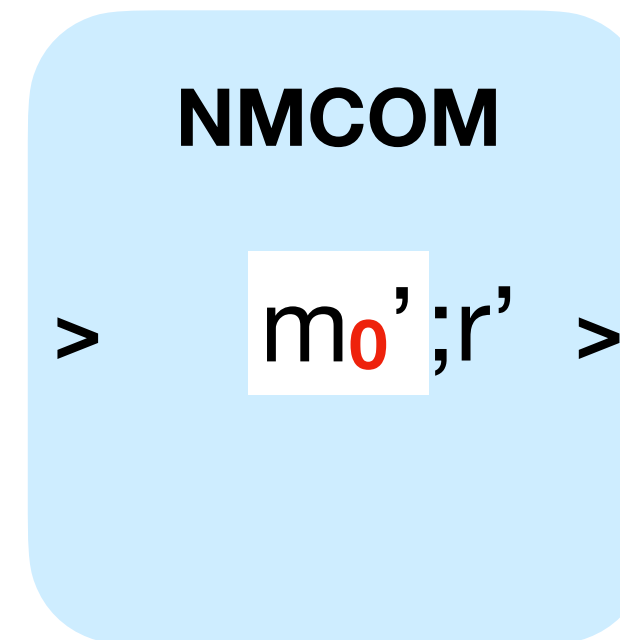
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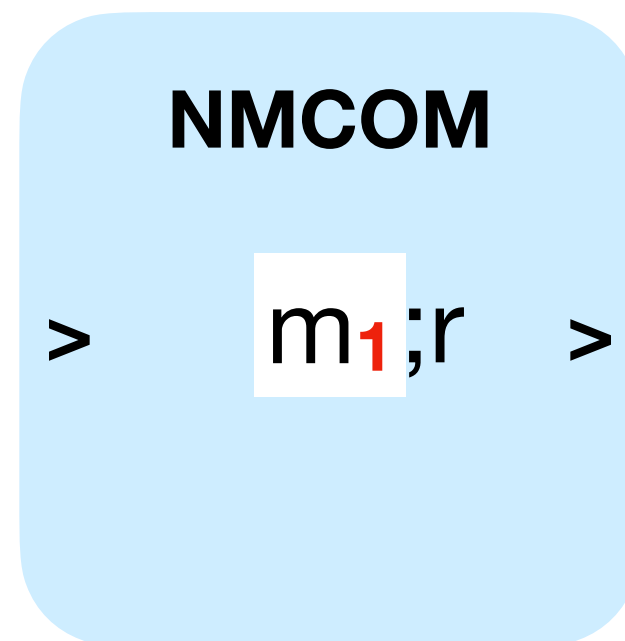


Man In the Middle

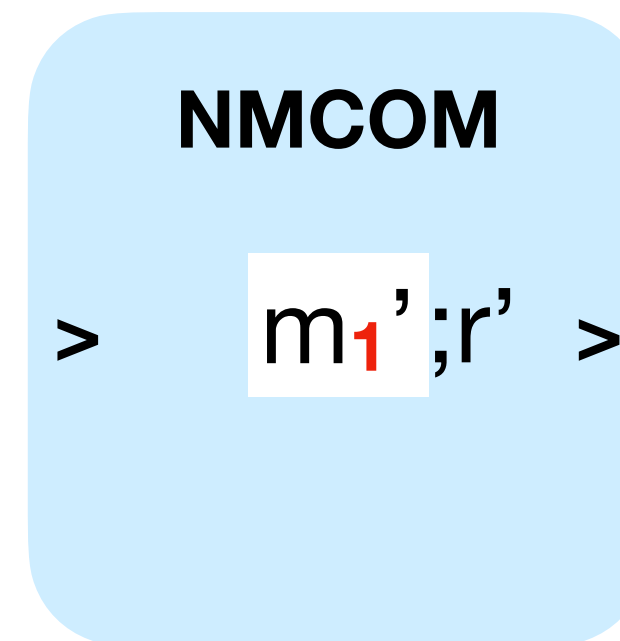


≈

Exp(1)



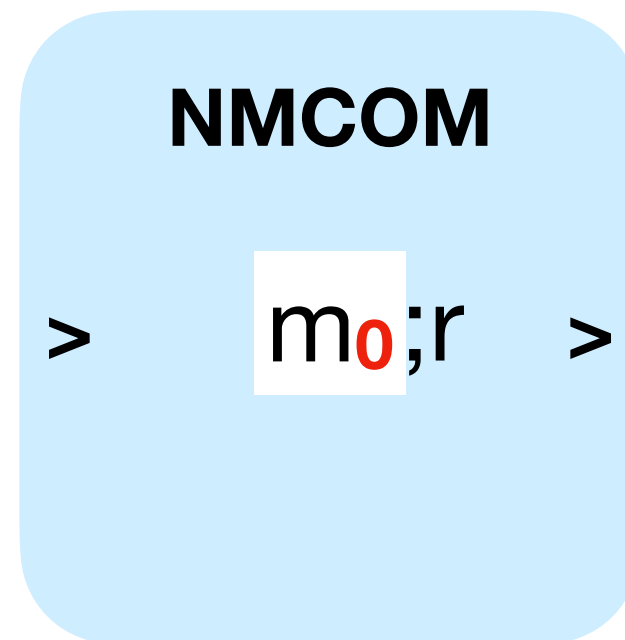
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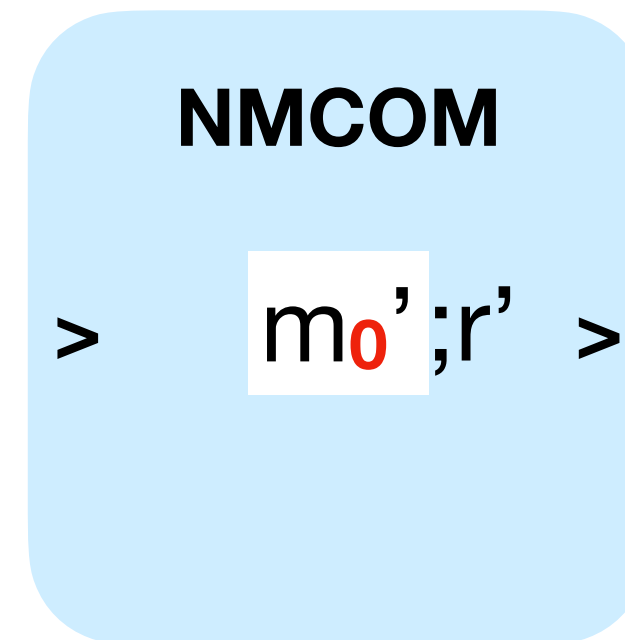
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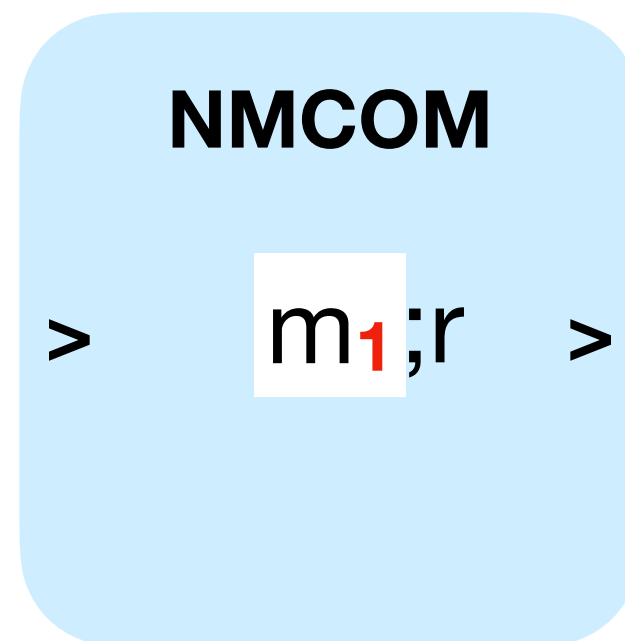
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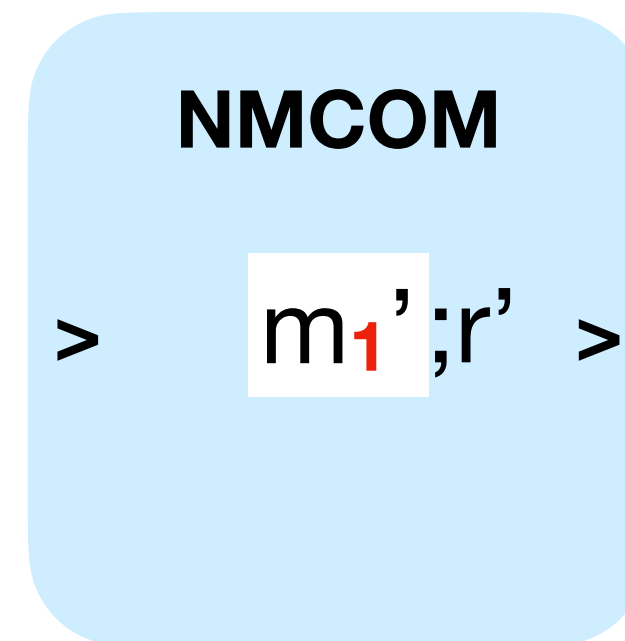
$m_0'$



Exp(1)

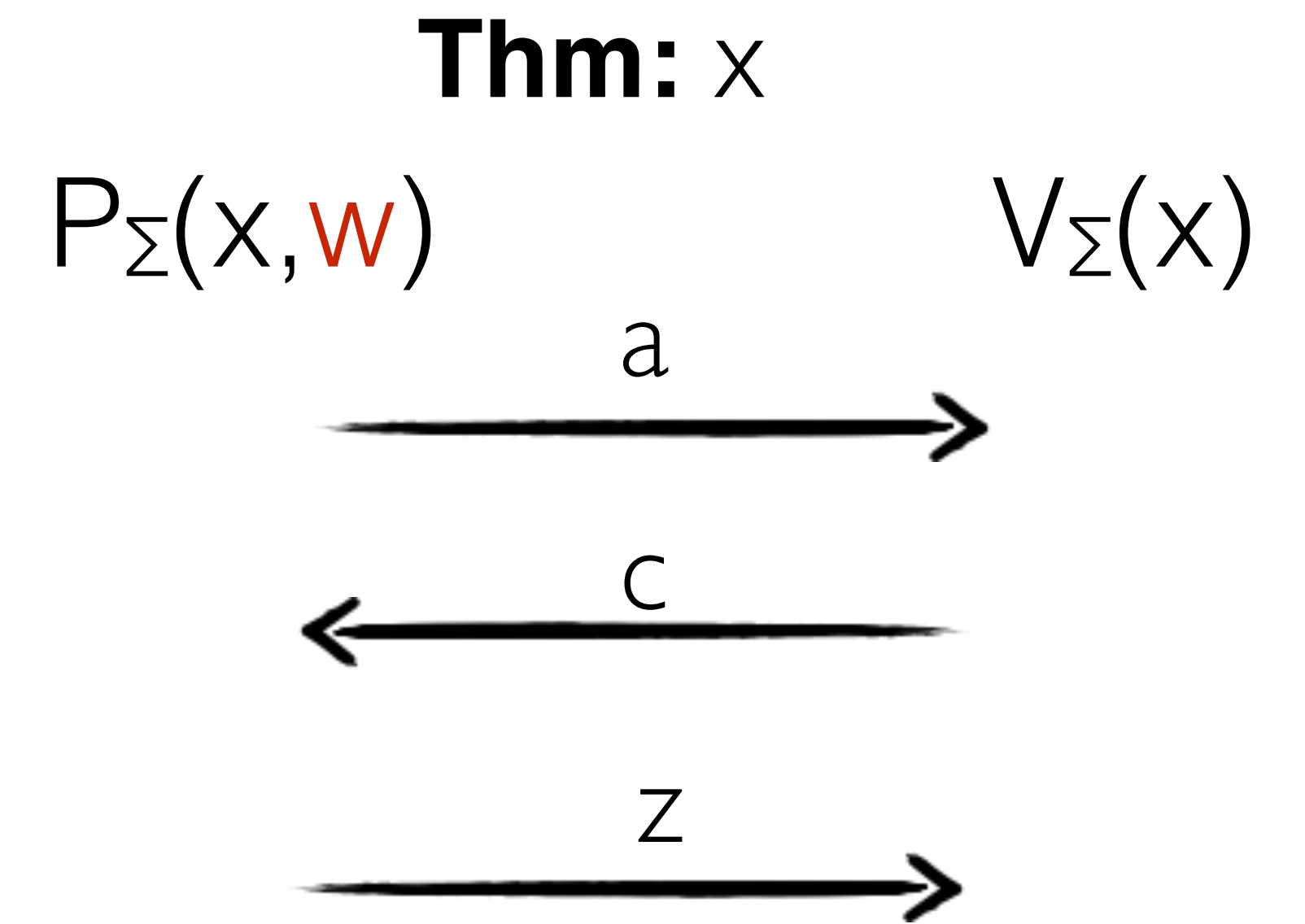


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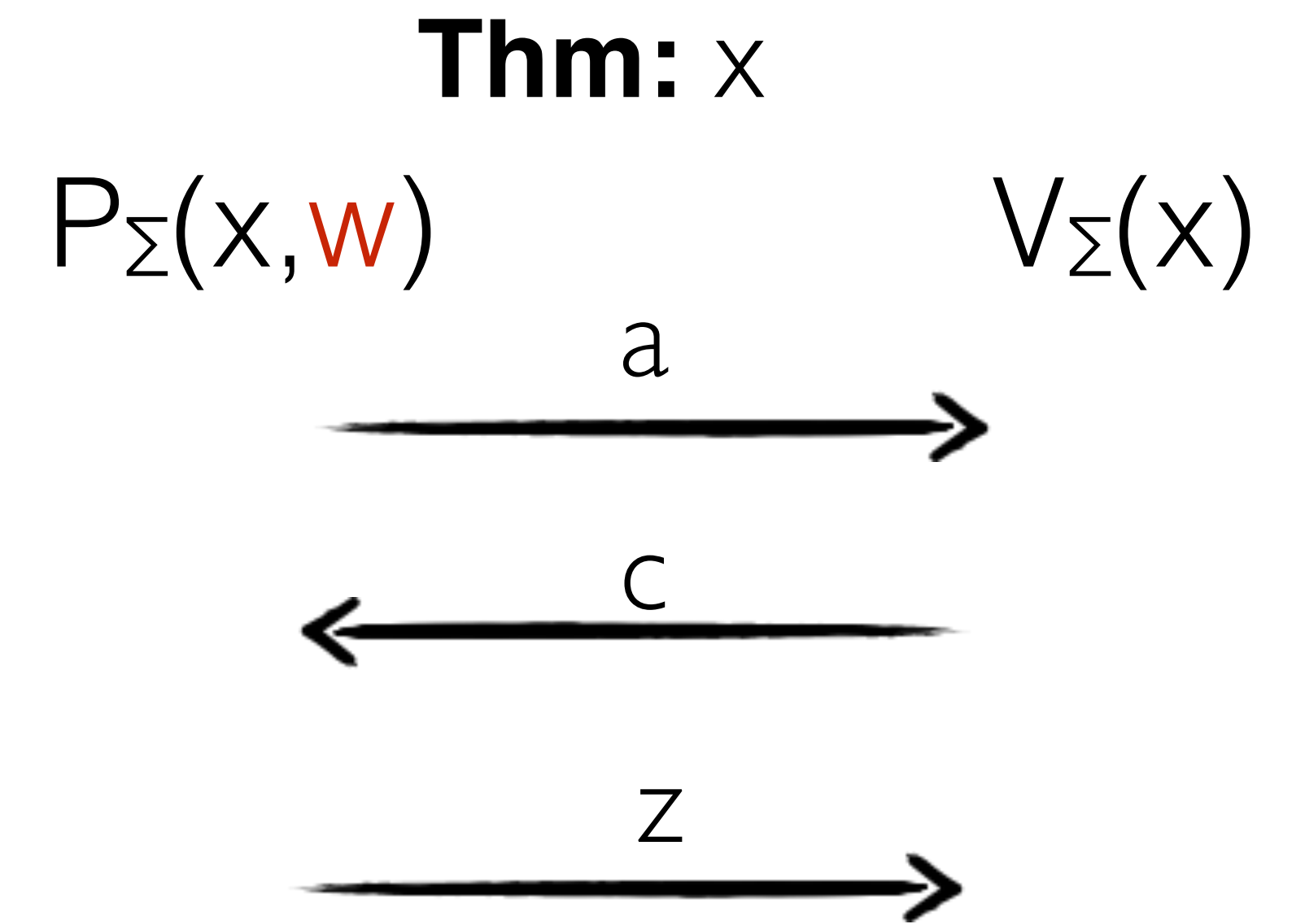
$m_1'$

# Sigma protocols



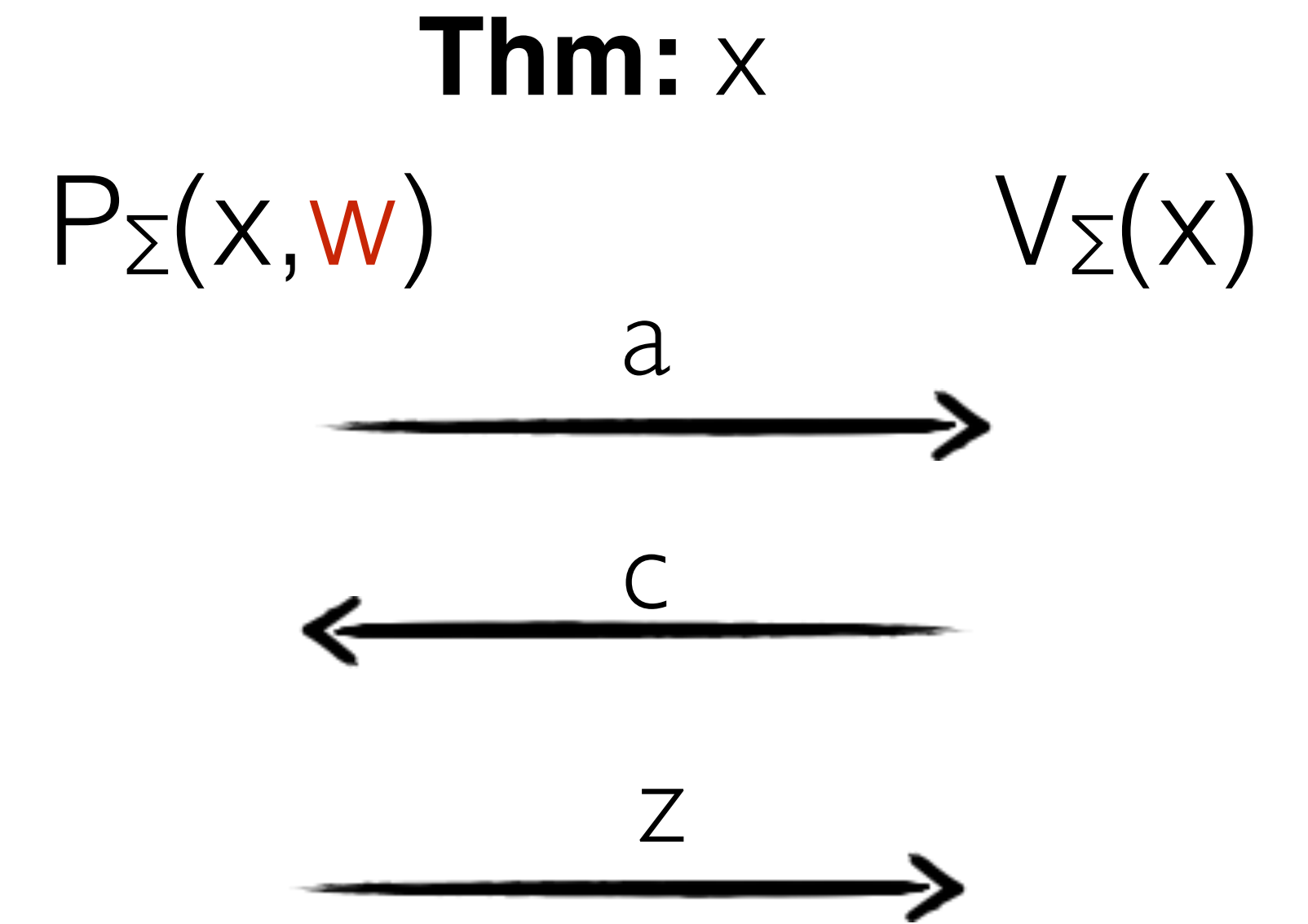
# Sigma protocols

- Completeness



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- Honest Verifier Zero-Knowledge  $\mathcal{HVZK}_{Sim}(x) \Rightarrow$





# Sigma protocols

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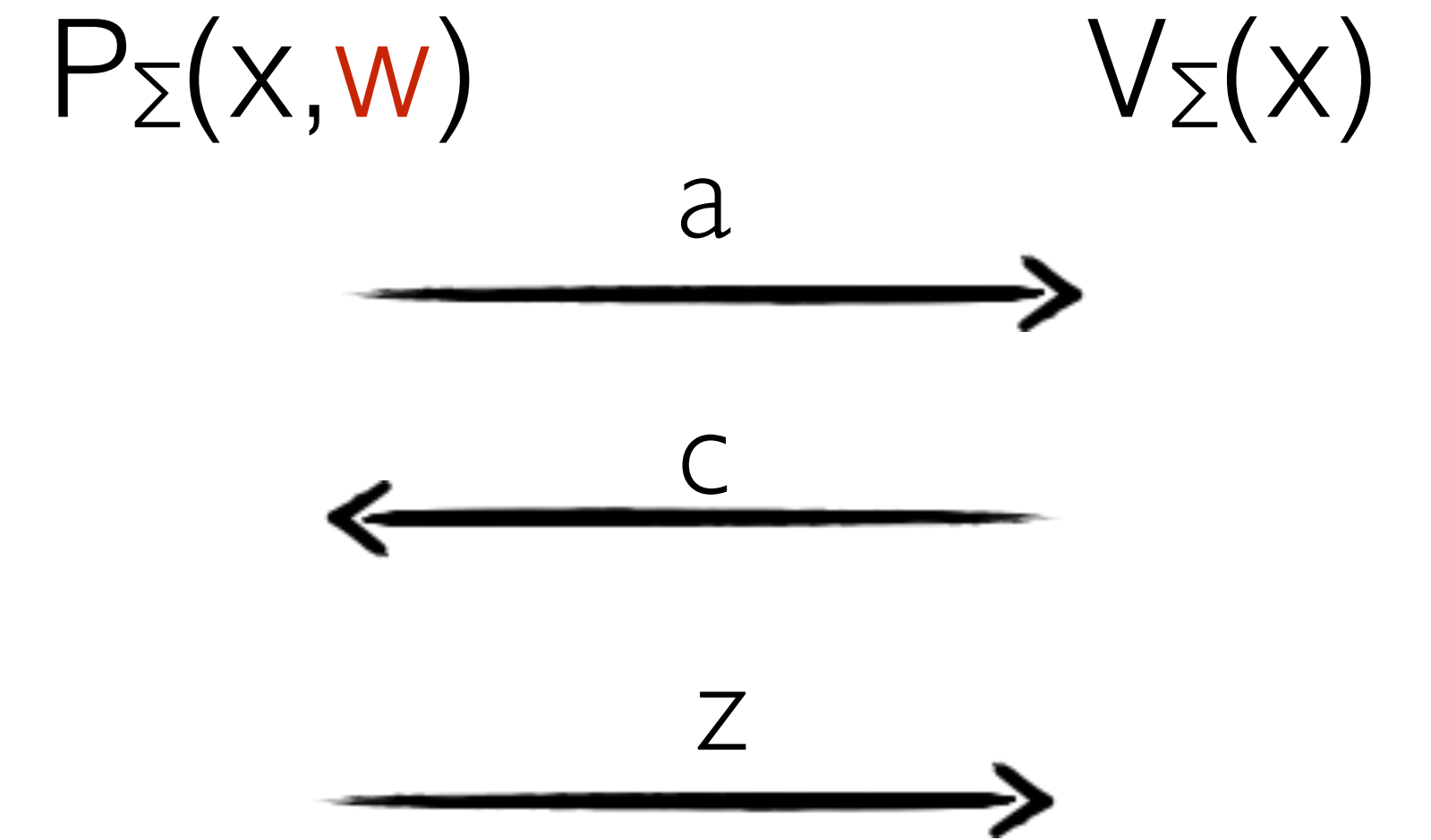
- Honest Verifier Zero-Knowledge  $\mathcal{HVZK}_{Sim}(x) \Rightarrow$

$a'$

$c'$

$z'$

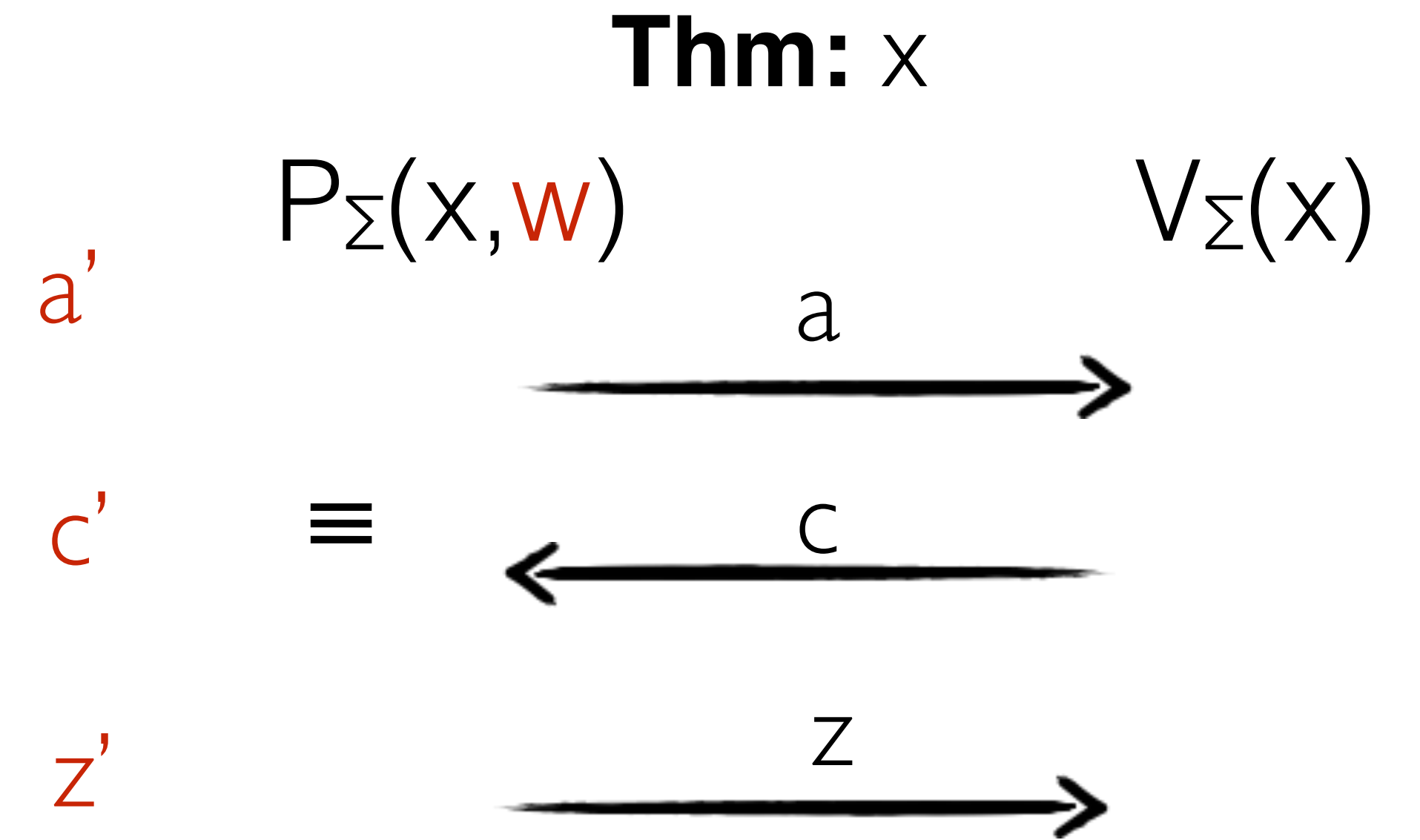
**Thm:**  $x$



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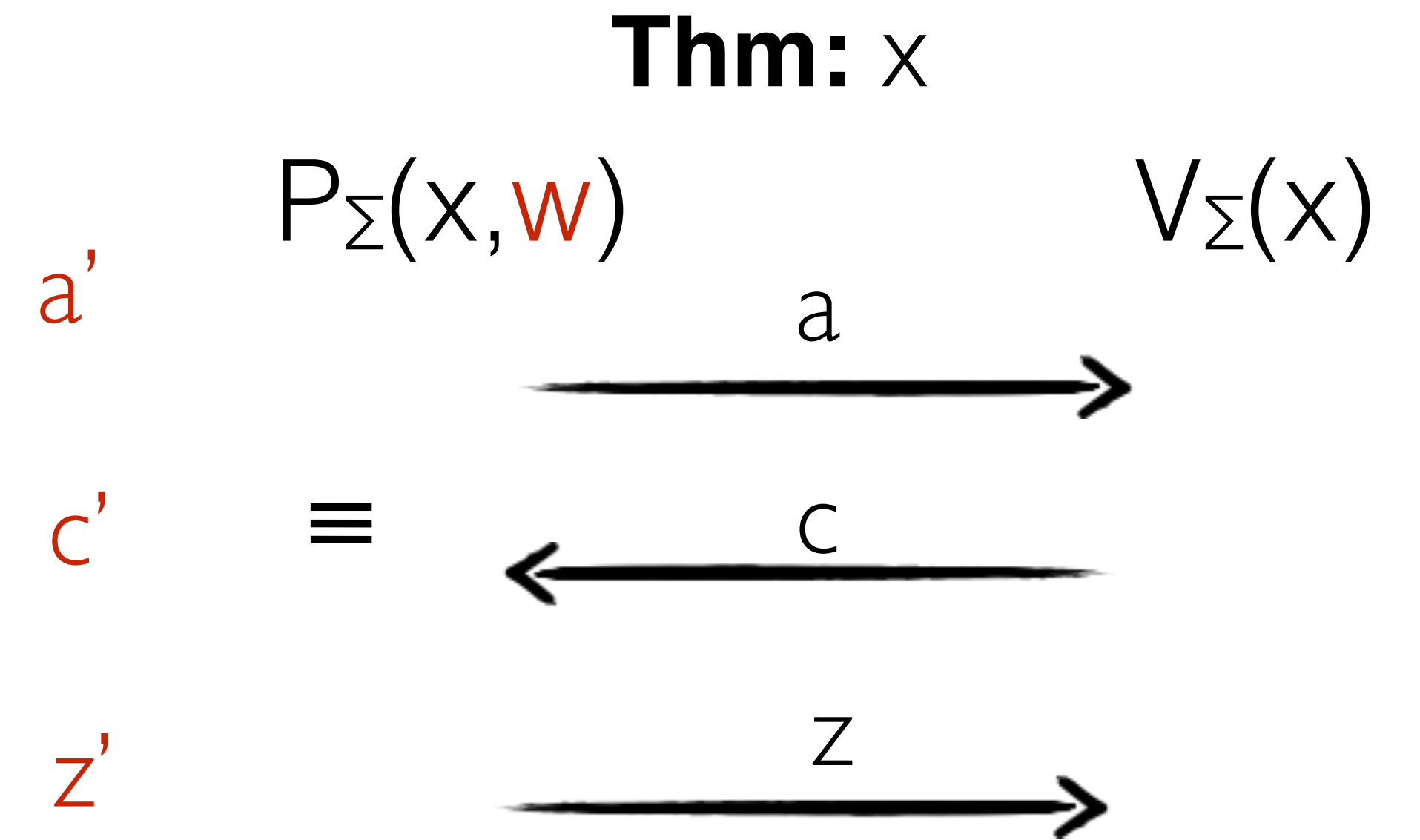
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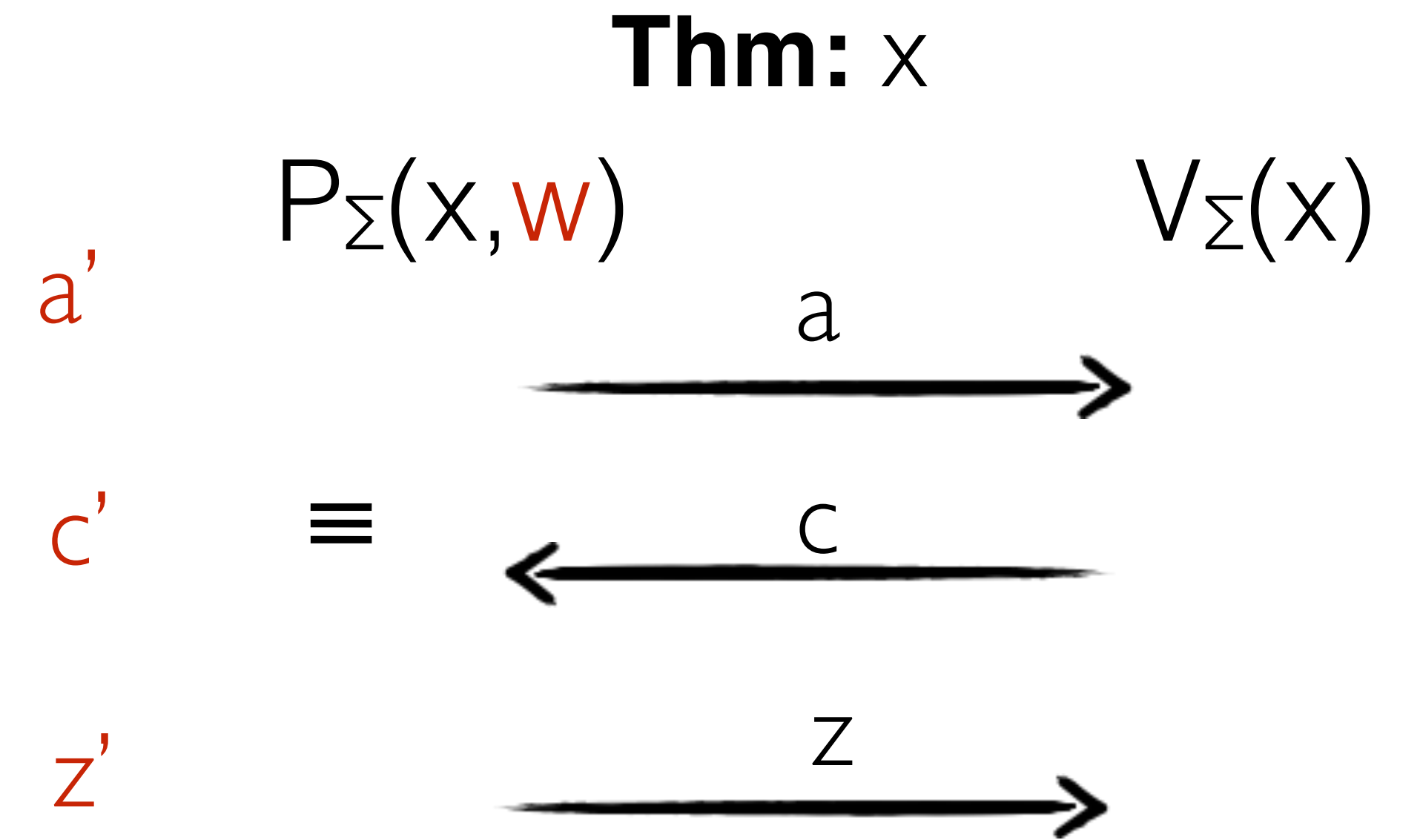
# Sigma protocols

- Completeness
- Honest Verifier Zero-Knowledge  $\mathcal{HVZK}_{\text{Sim}}(x) \Rightarrow$   
*Special* Honest Verifier Zero-Knowledge  $\mathcal{SHVZK}_{\text{Sim}}(x, c) \Rightarrow a', z'$



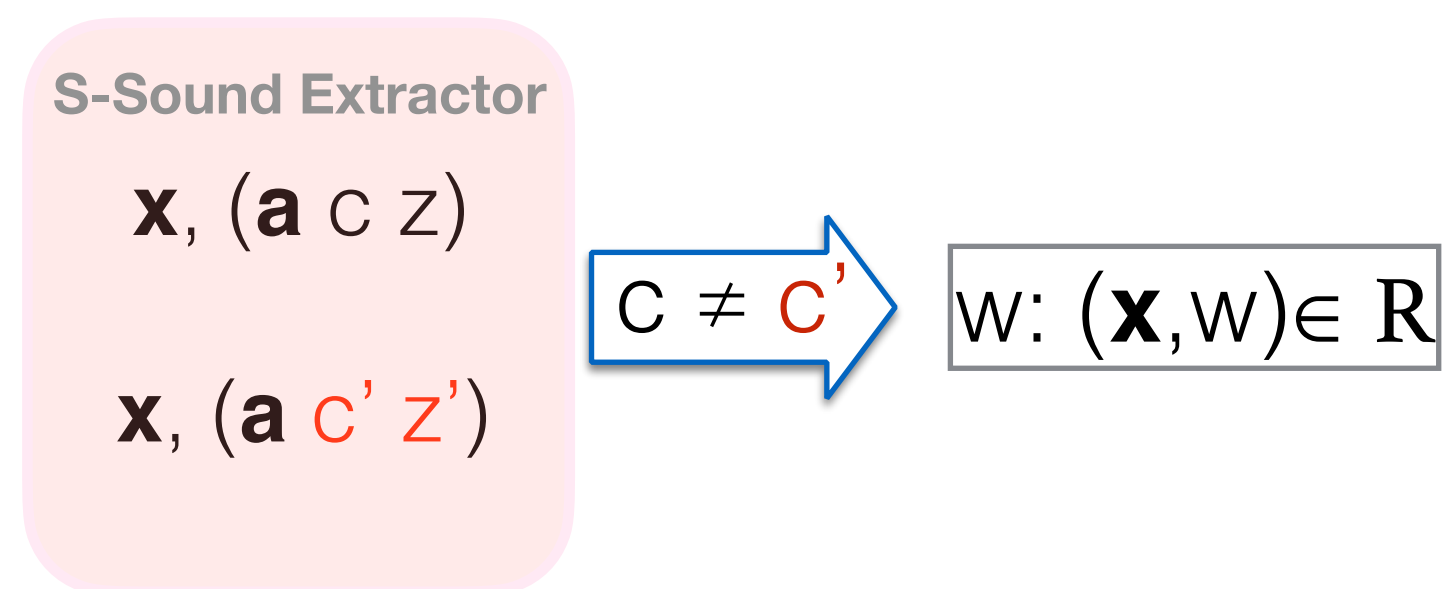
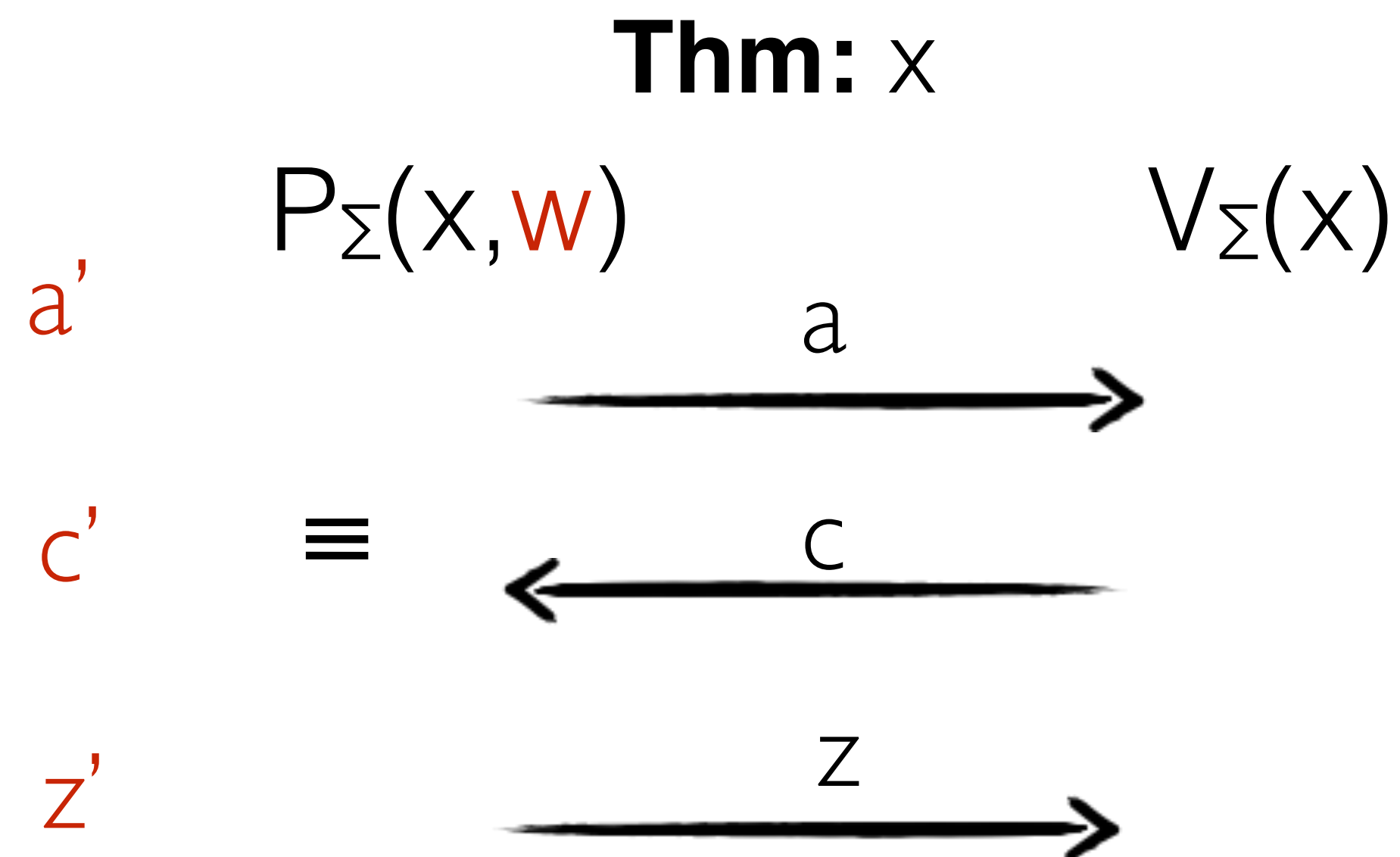
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- Completeness
- Honest Verifier Zero-Knowledge  $\mathcal{HVZK}_{\text{Sim}}(x) \Rightarrow$   
*Special Honest Verifier Zero-Knowledge*  $\mathcal{SHVZK}_{\text{Sim}}(x, c) \Rightarrow a', z'$
- Special Soundness



# Sigma protocols

- Completeness
- Honest Verifier Zero-Knowledge  $\mathcal{HVZK}_{Sim}(x) \Rightarrow$   
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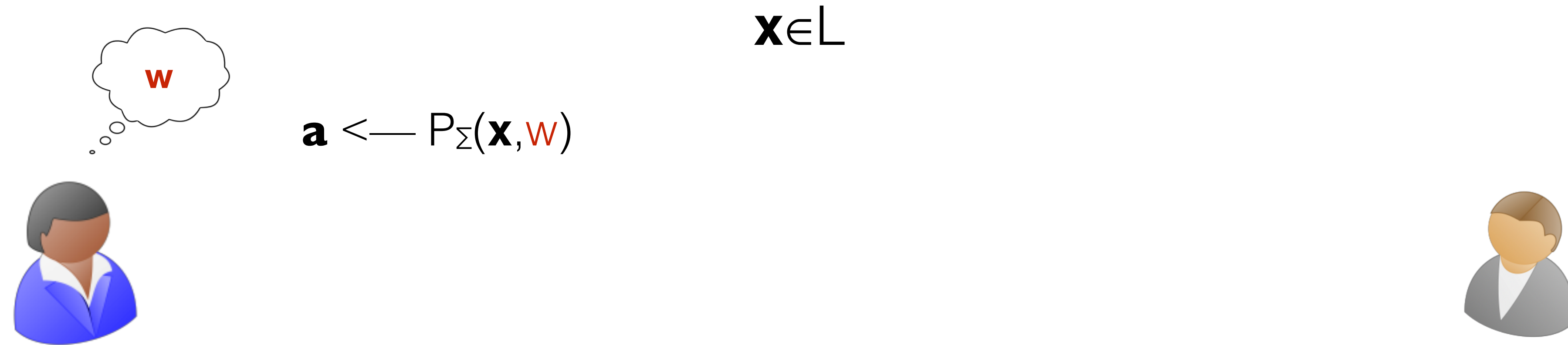
# Our NMZK Scheme\*



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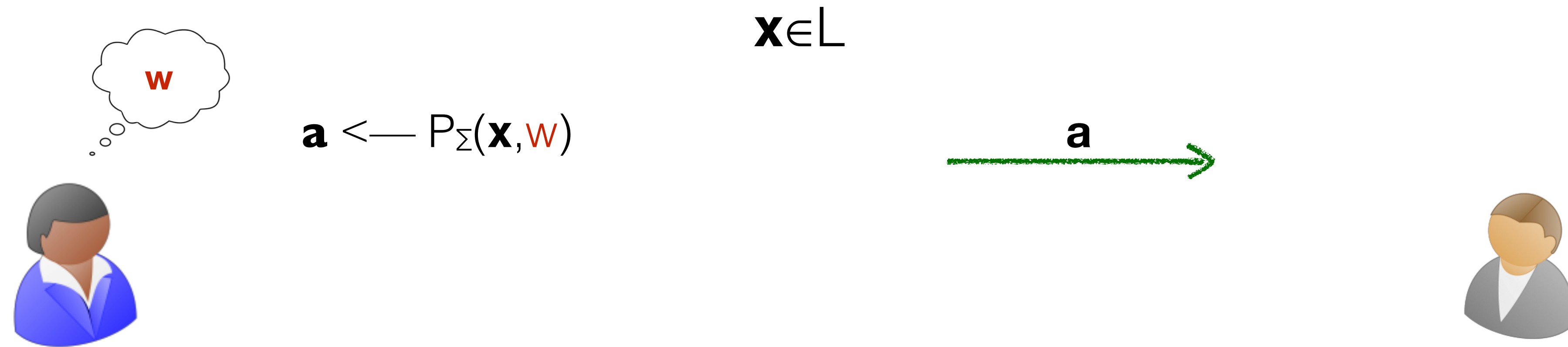


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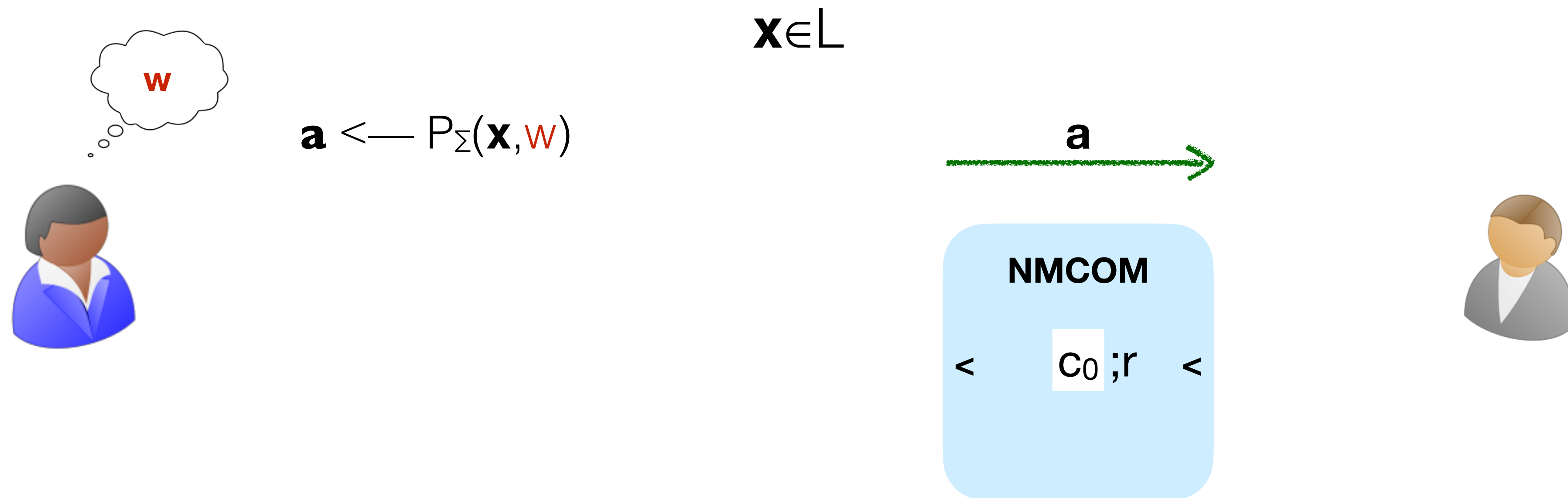
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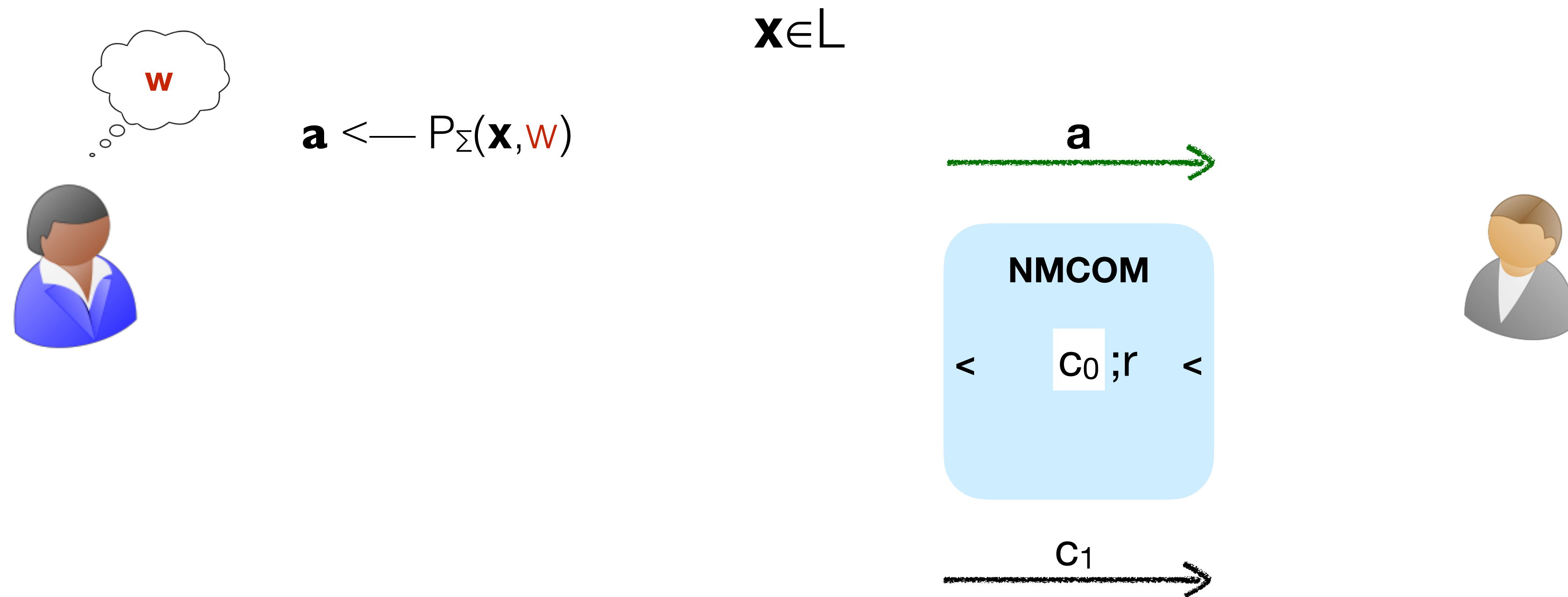


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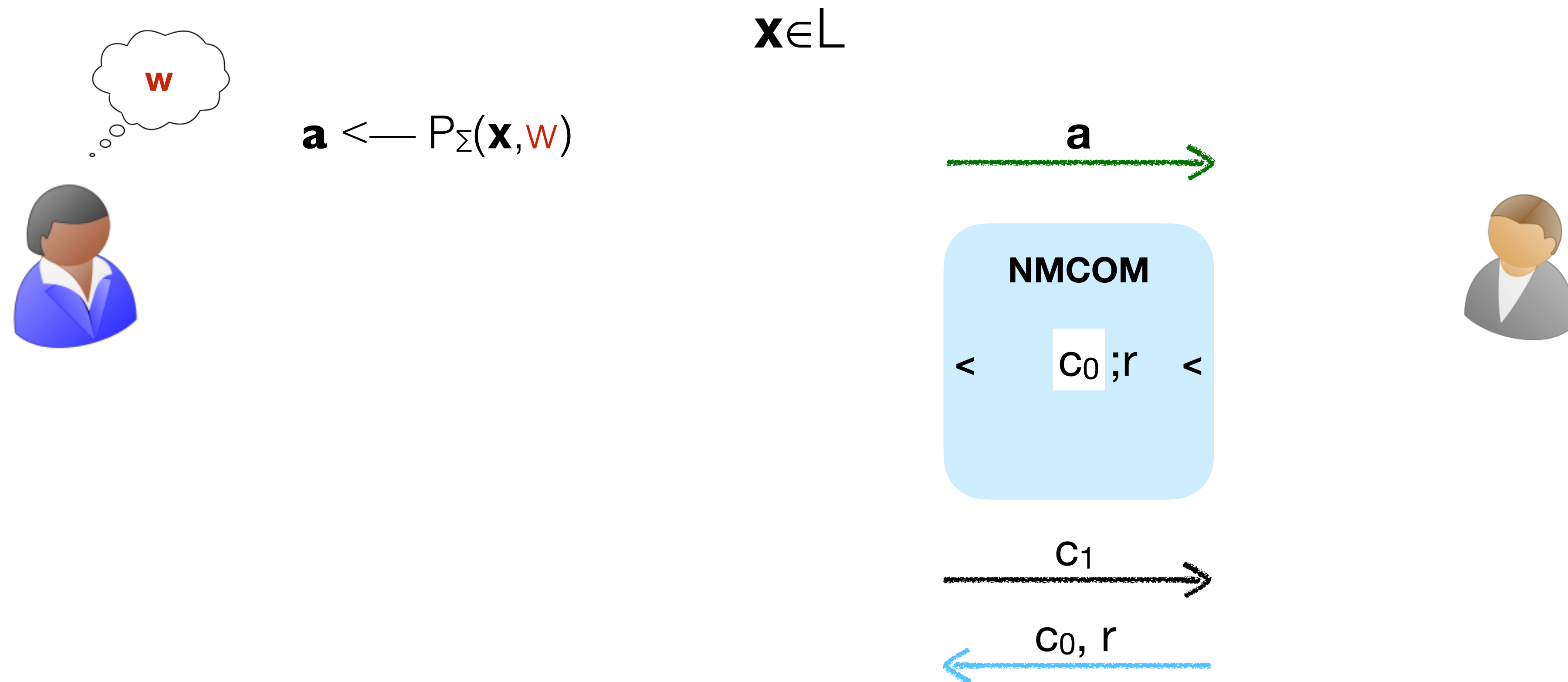
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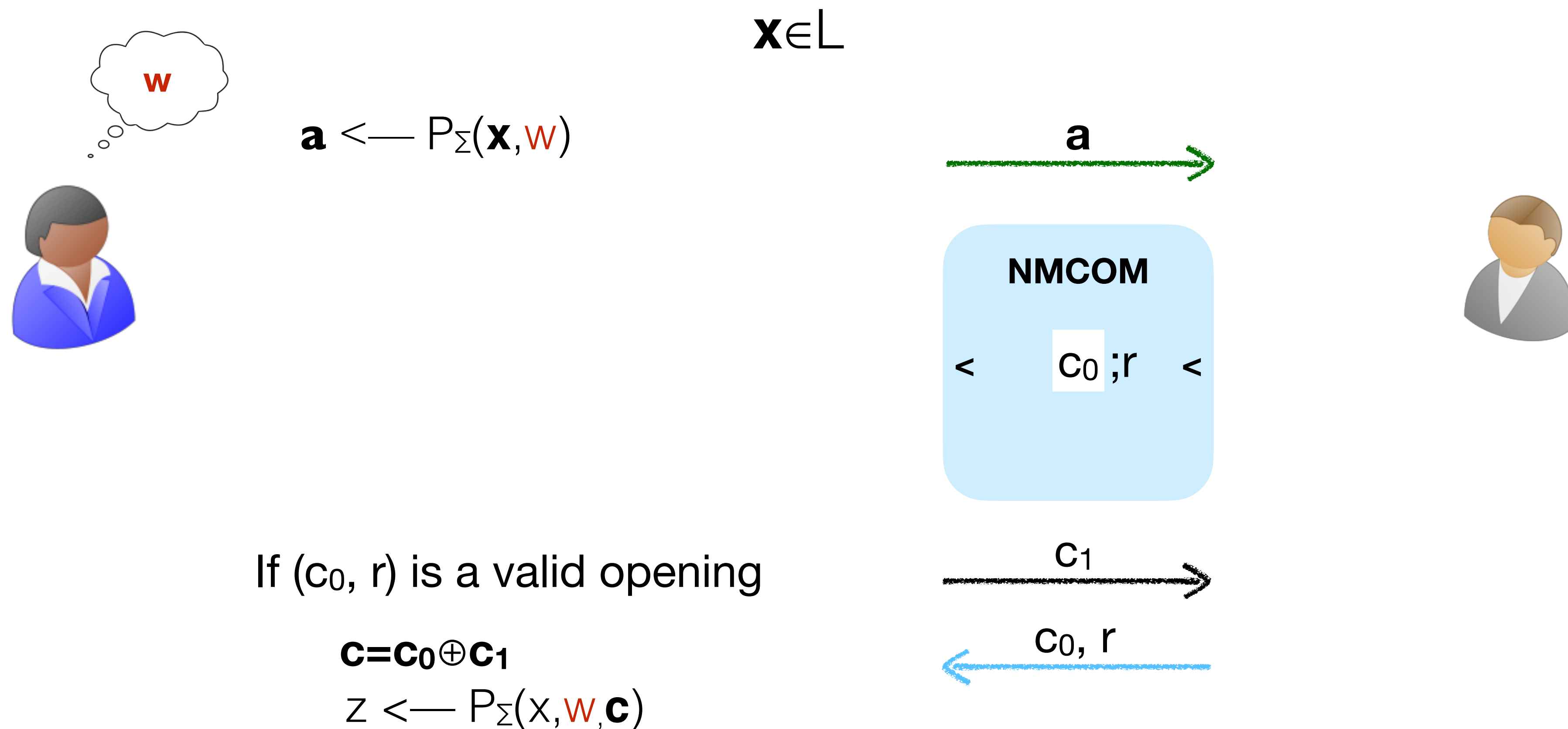
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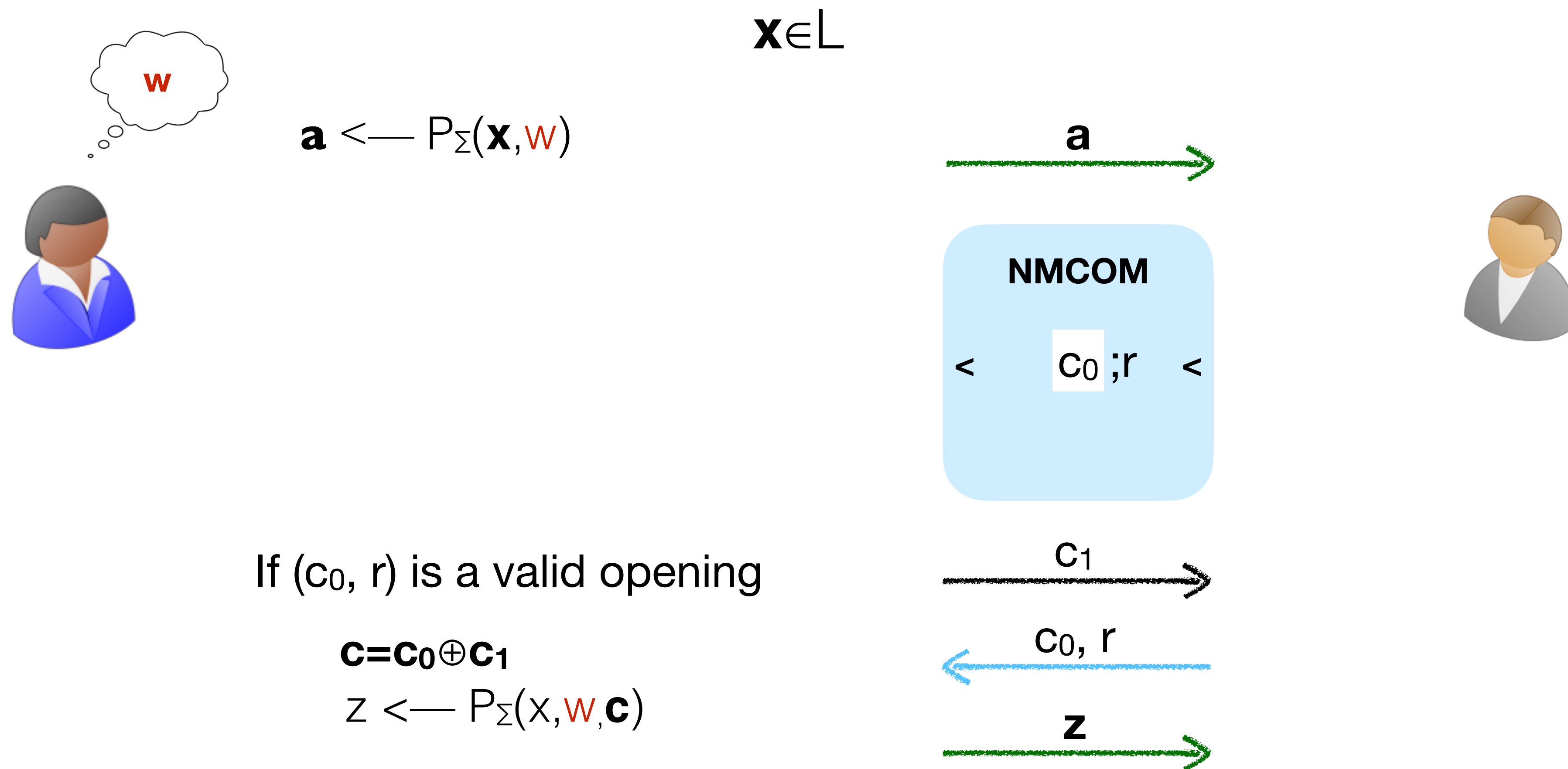
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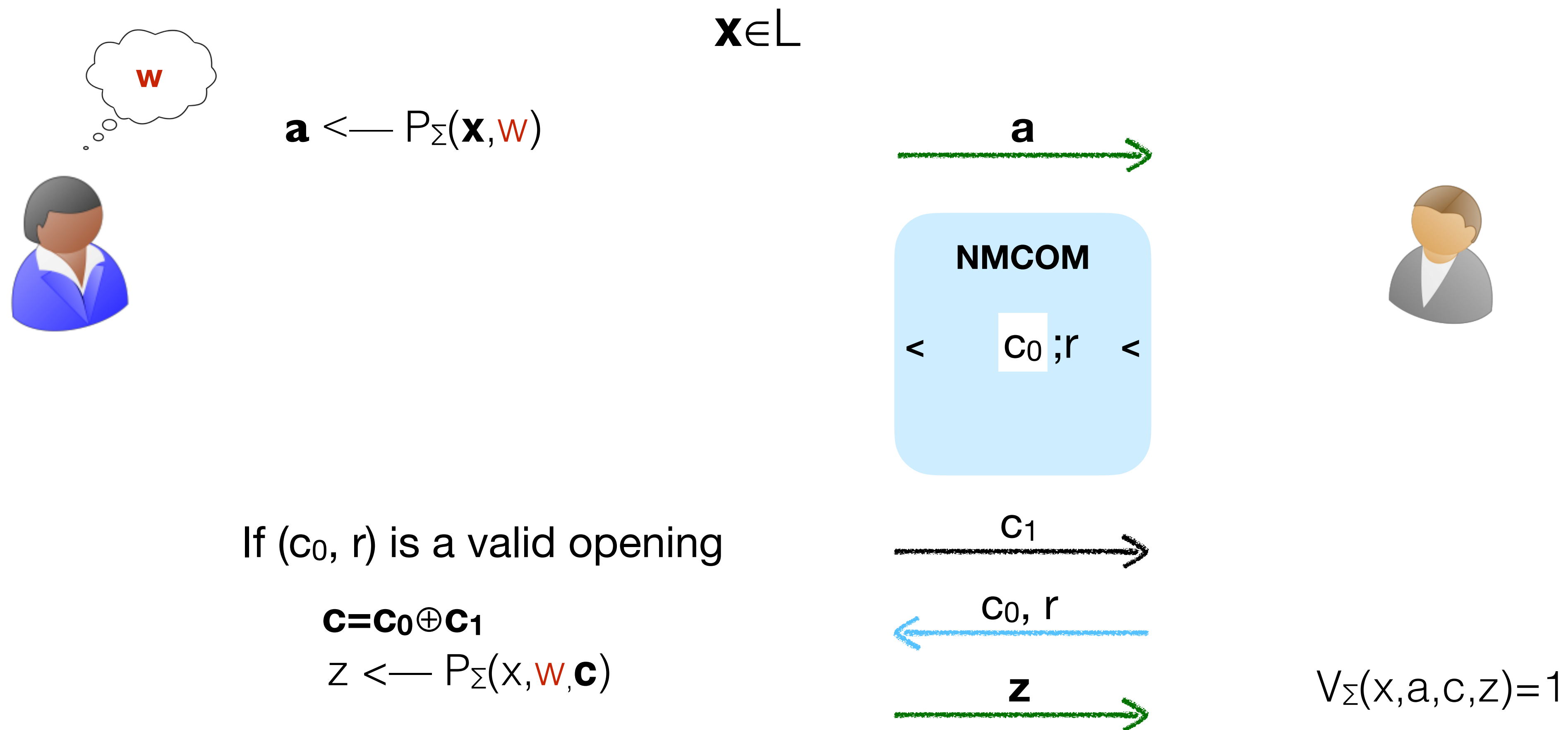
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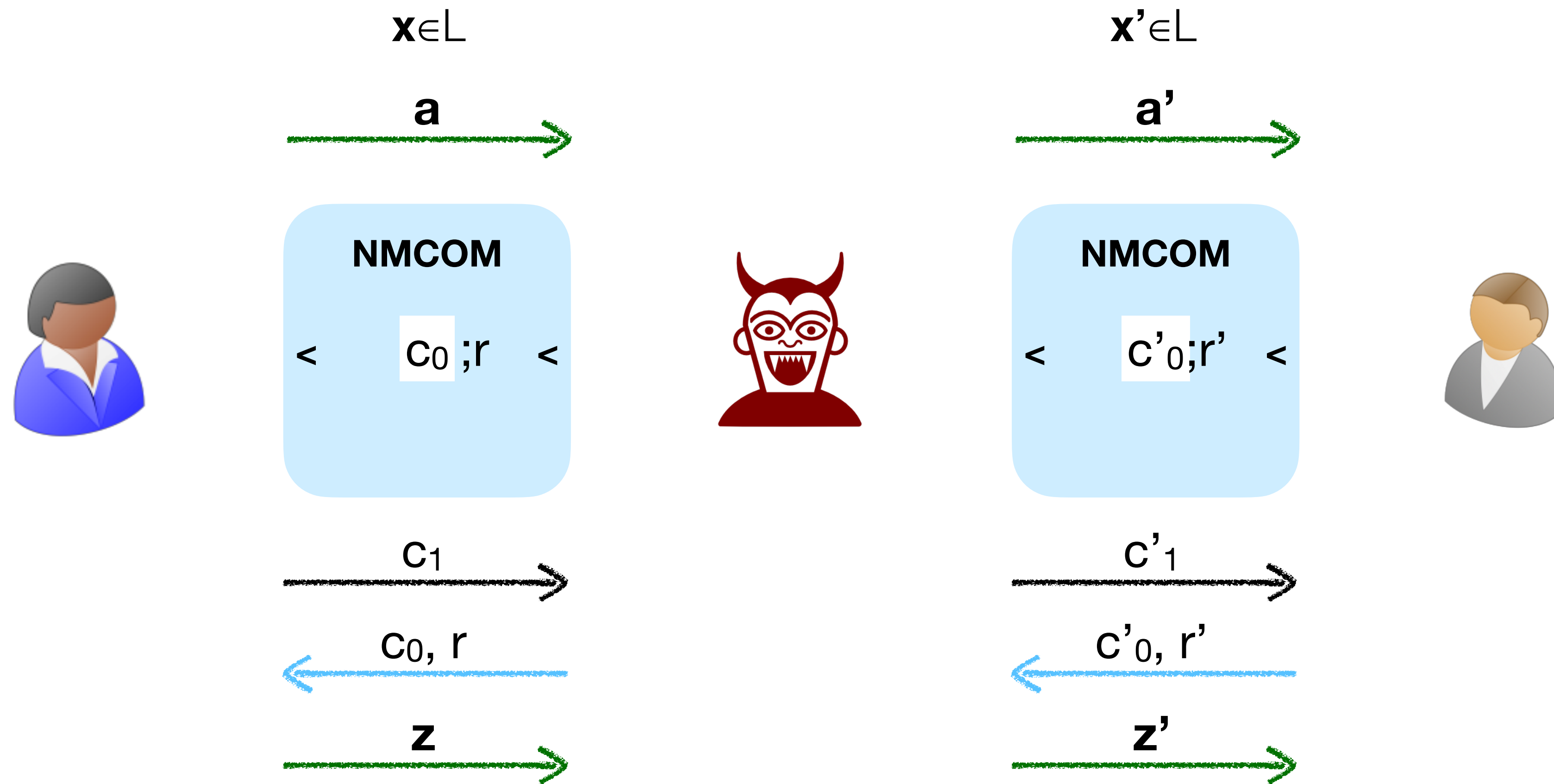
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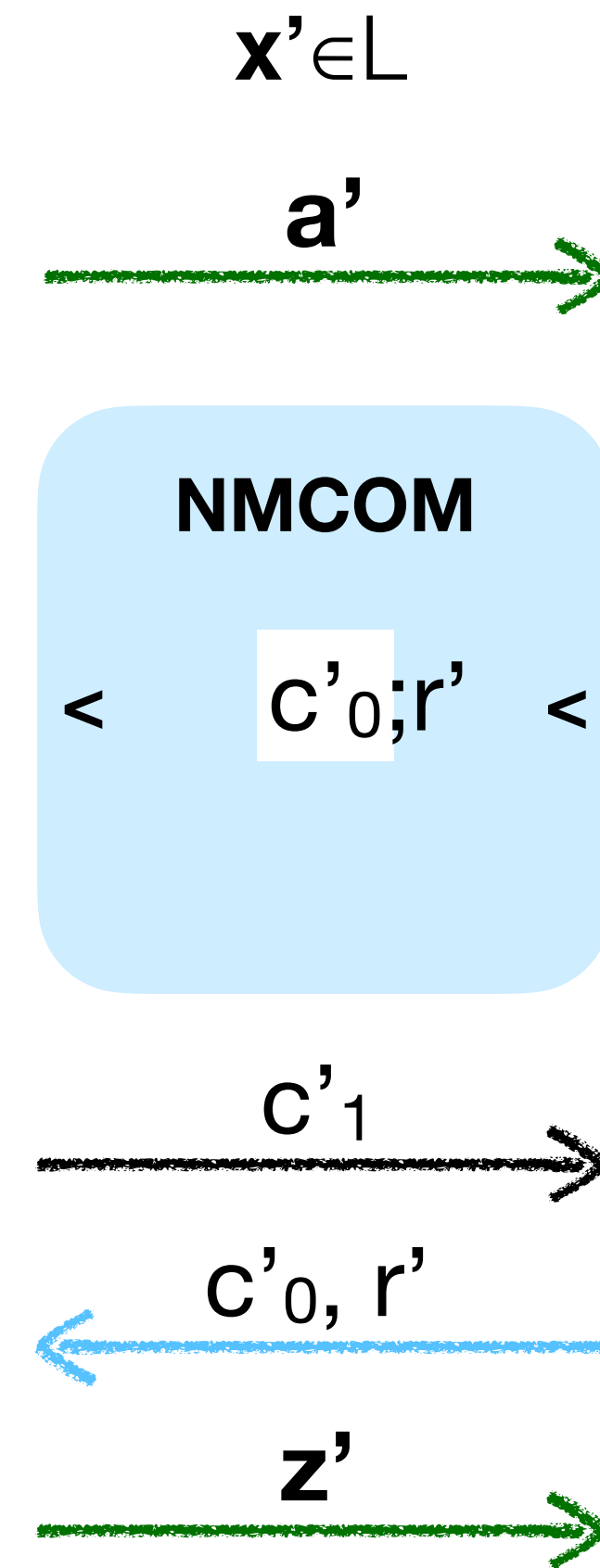
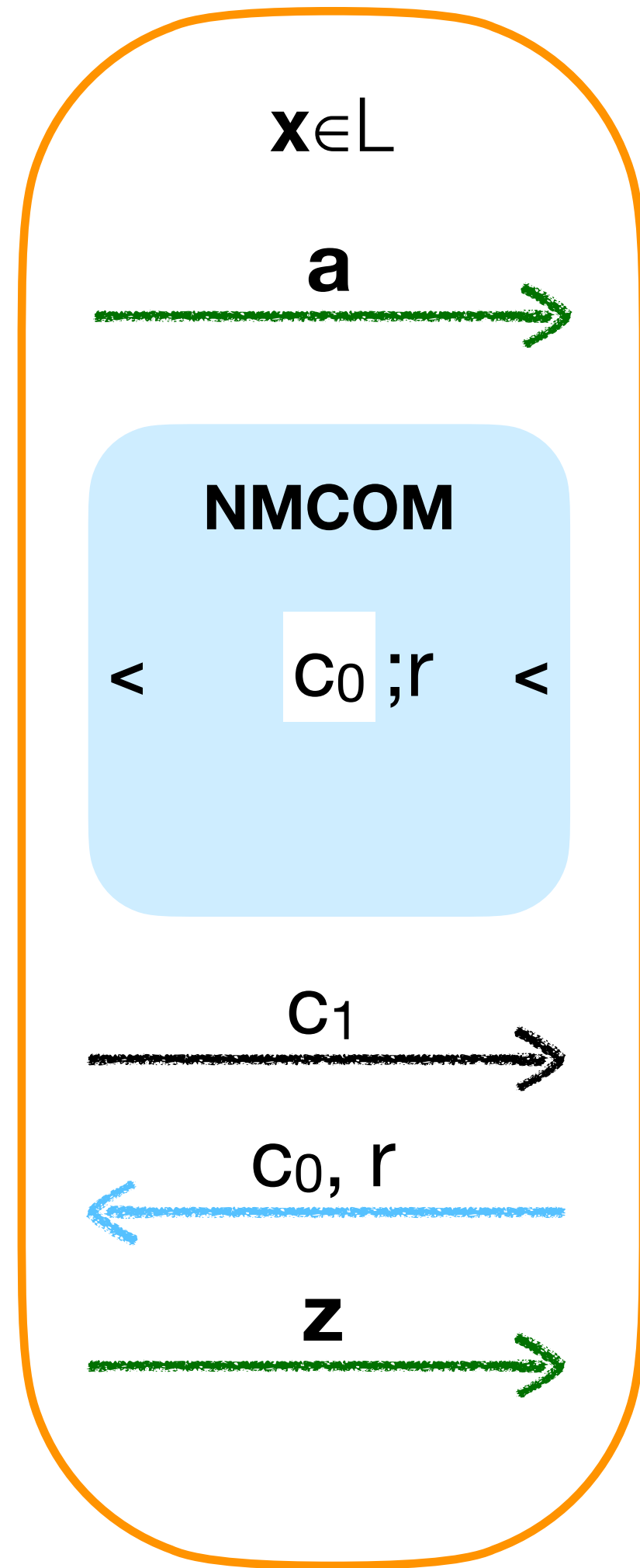
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# Proof approach



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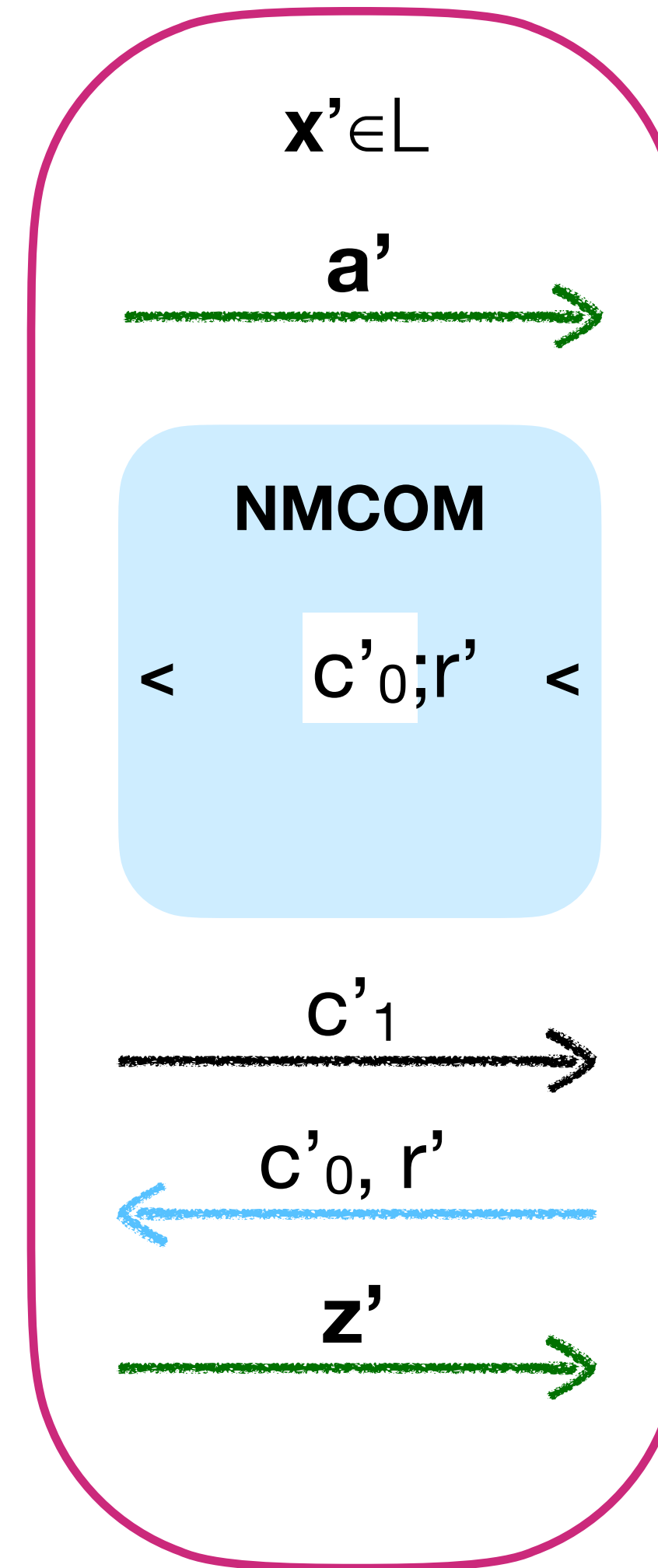
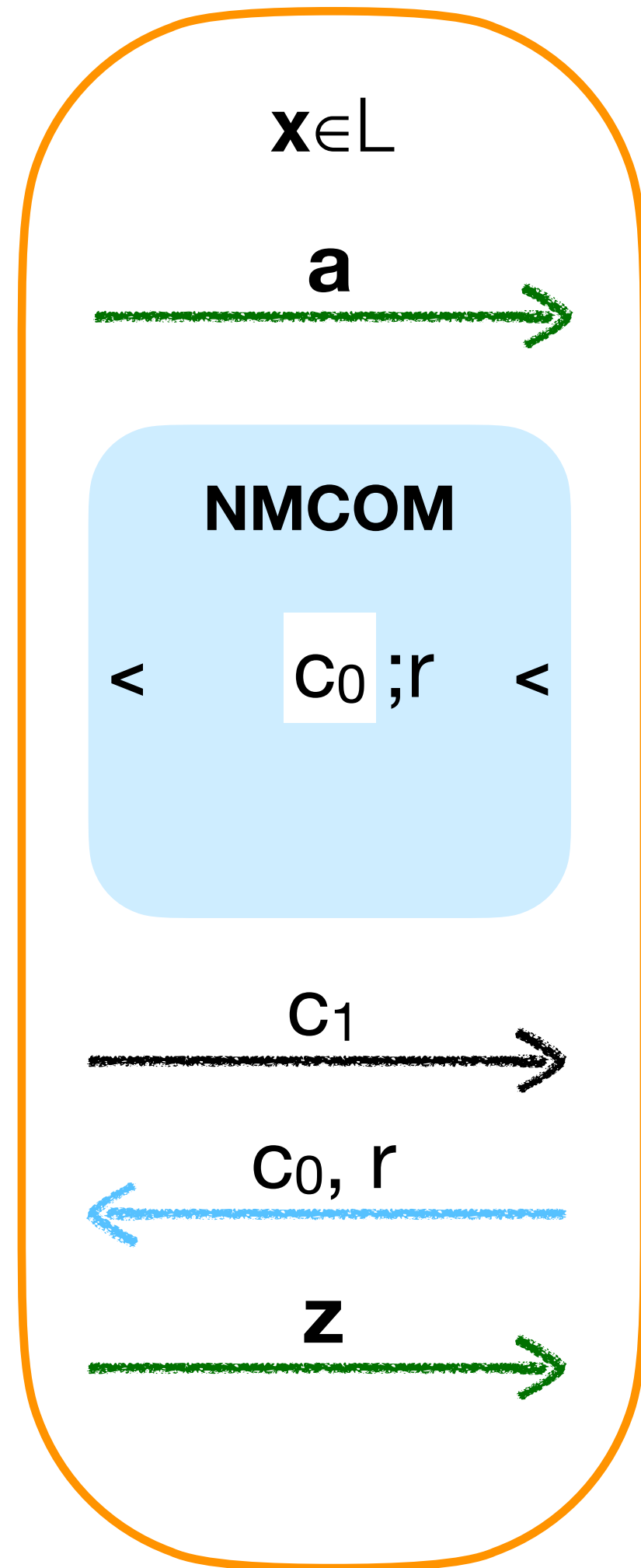
*Sim*(**x**)





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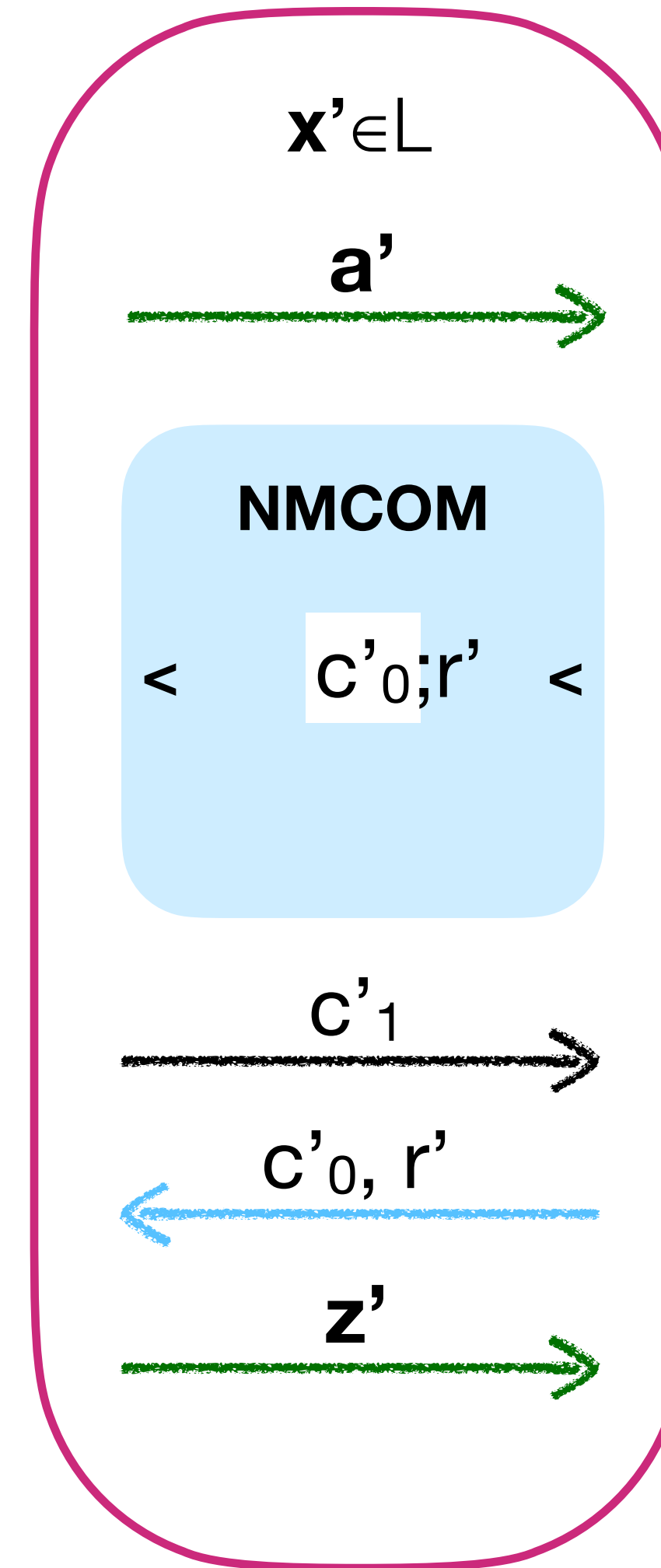
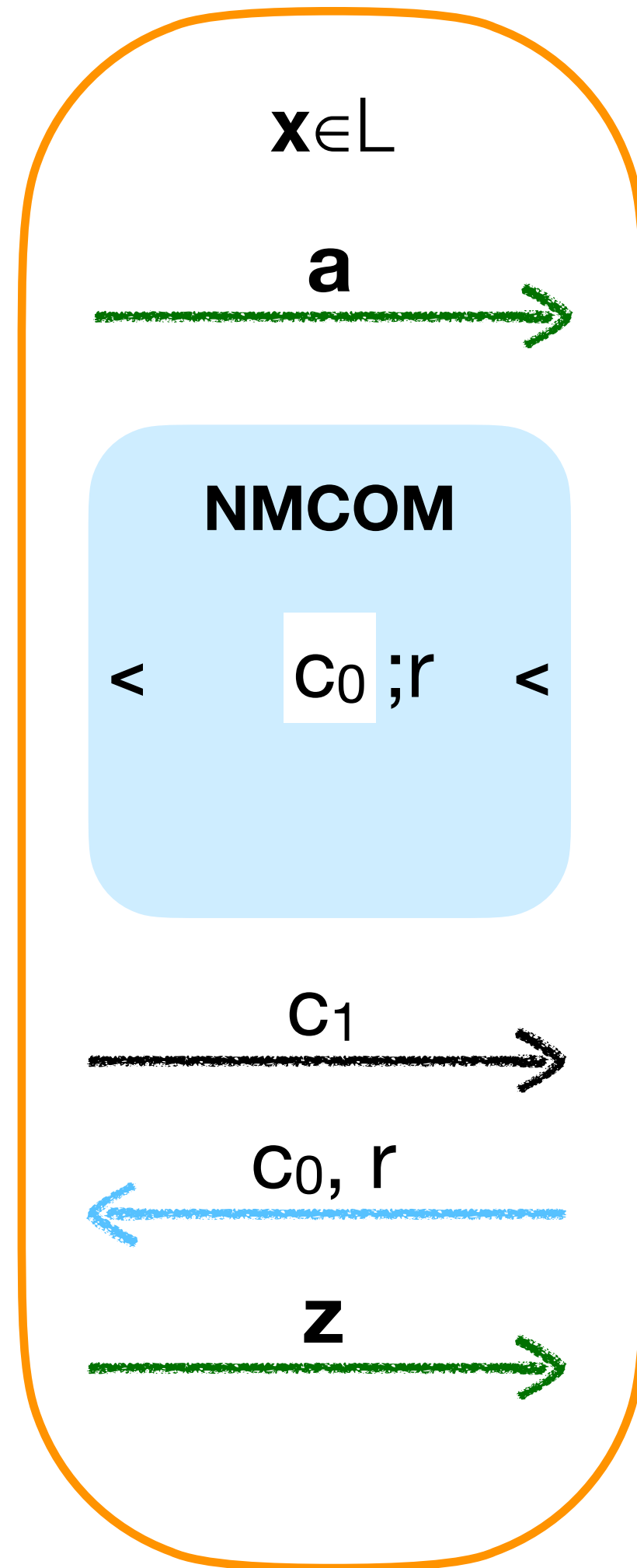
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**PoKExtractor**

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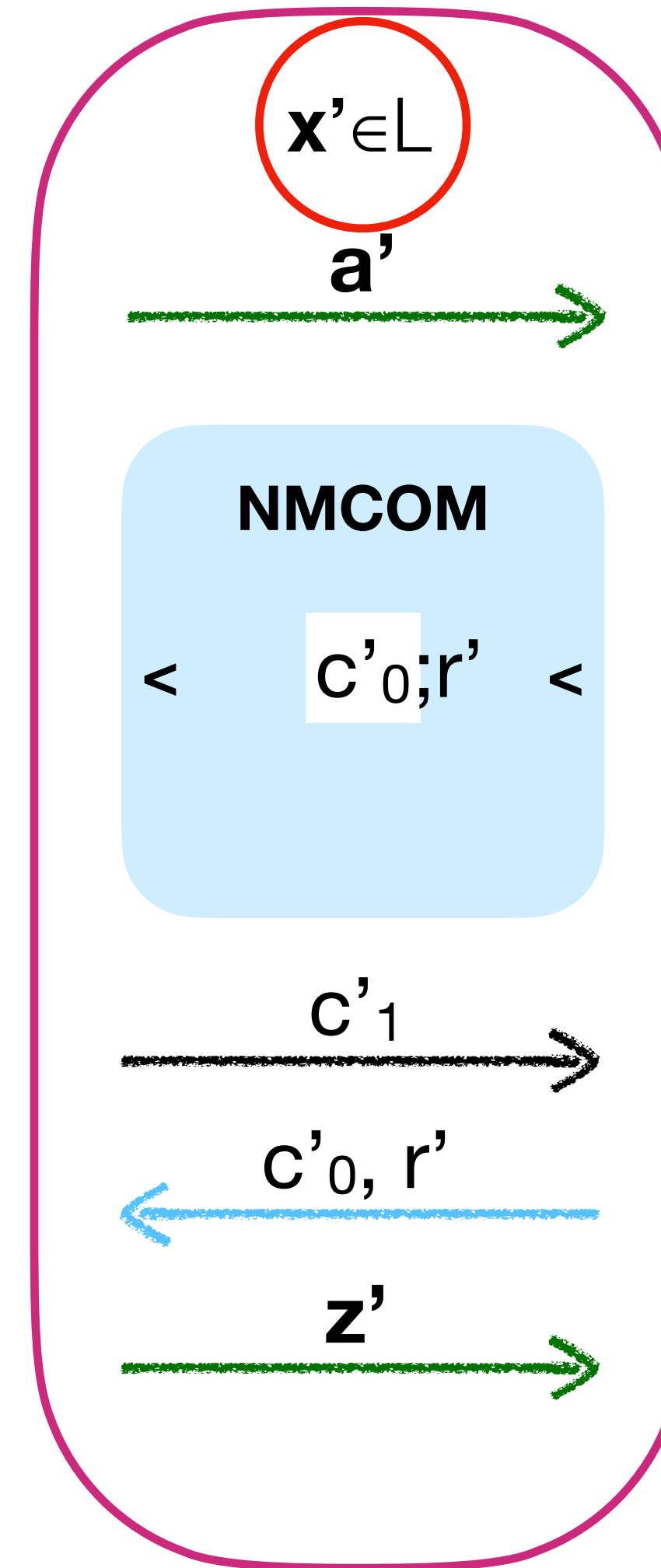
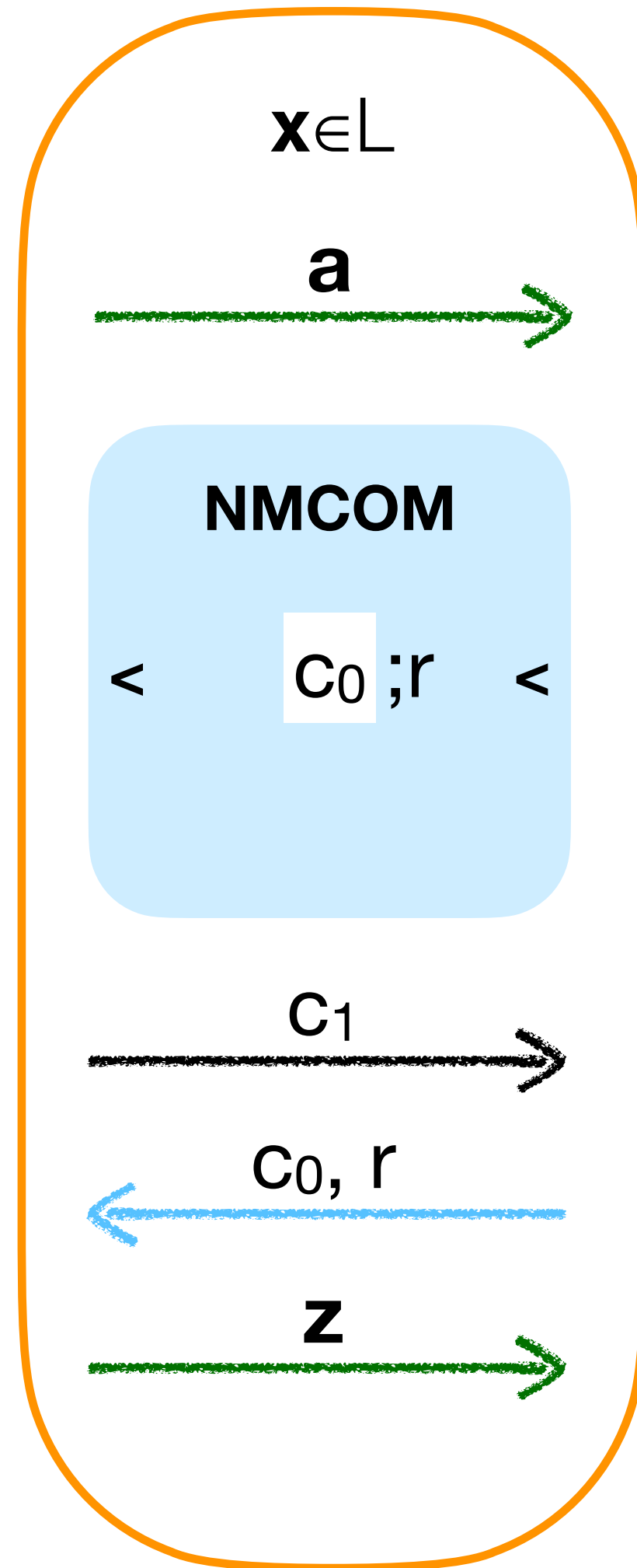
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**PoKExtractor**  $\rightarrow w': (x', w') \in R$

# Proof approach

*Sim*(**x**)



PoKExtractor  $\rightarrow w' : (x', w') \in R$

# Zero-Knowledge

*Sim*(**x**)



# Zero-Knowledge

*Sim*(**x**)

**a, c, z**  $\leftarrow$  HVZK $_{\Sigma}$ (**x**)



# Zero-Knowledge

*Sim*(**x**)

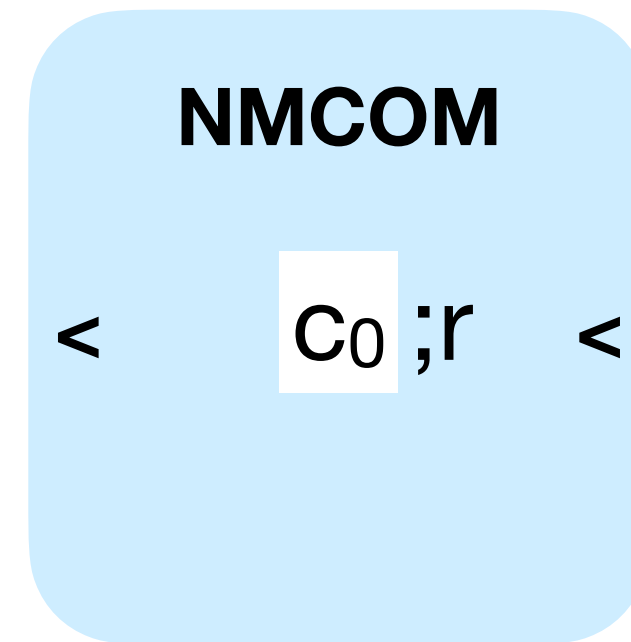
**a, c, z**  $\leftarrow$  HVZK $_{\Sigma}$ (**x**)



# Zero-Knowledge

*Sim*(**x**)

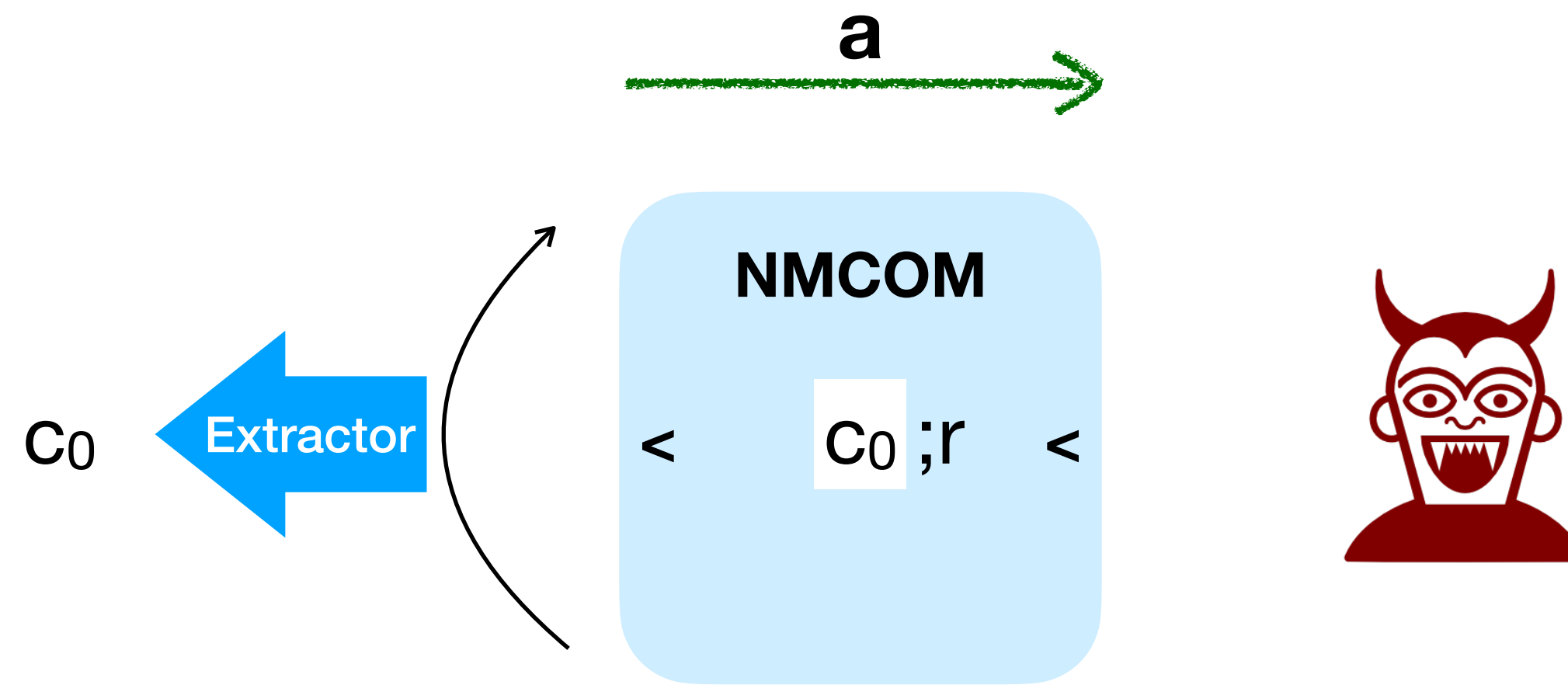
**a, c, z**  $\leftarrow$  HVZK $_{\Sigma}$ (**x**)



# Zero-Knowledge

*Sim*(**x**)

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$

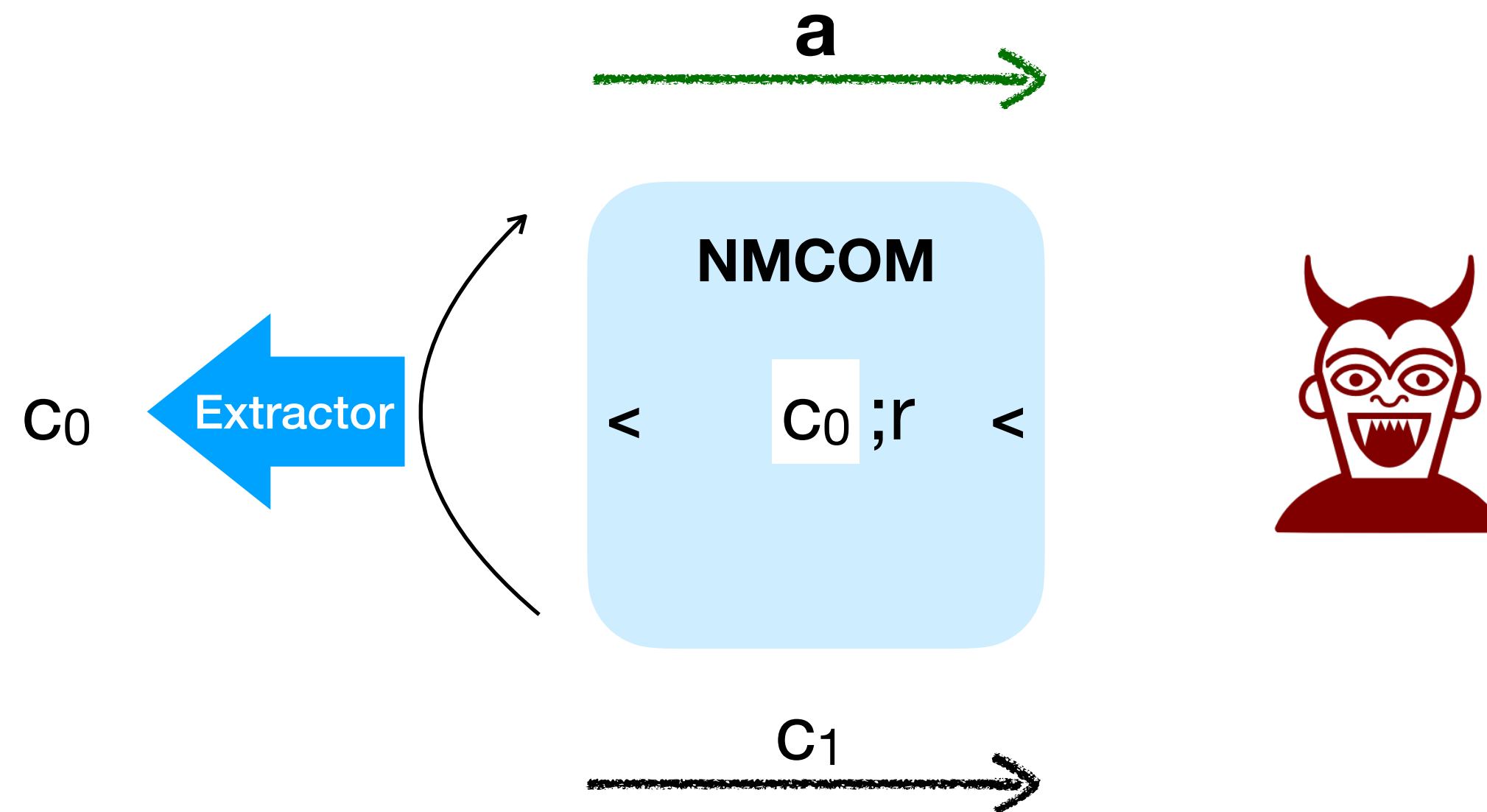




# Zero-Knowledge

*Sim*(**x**)

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$

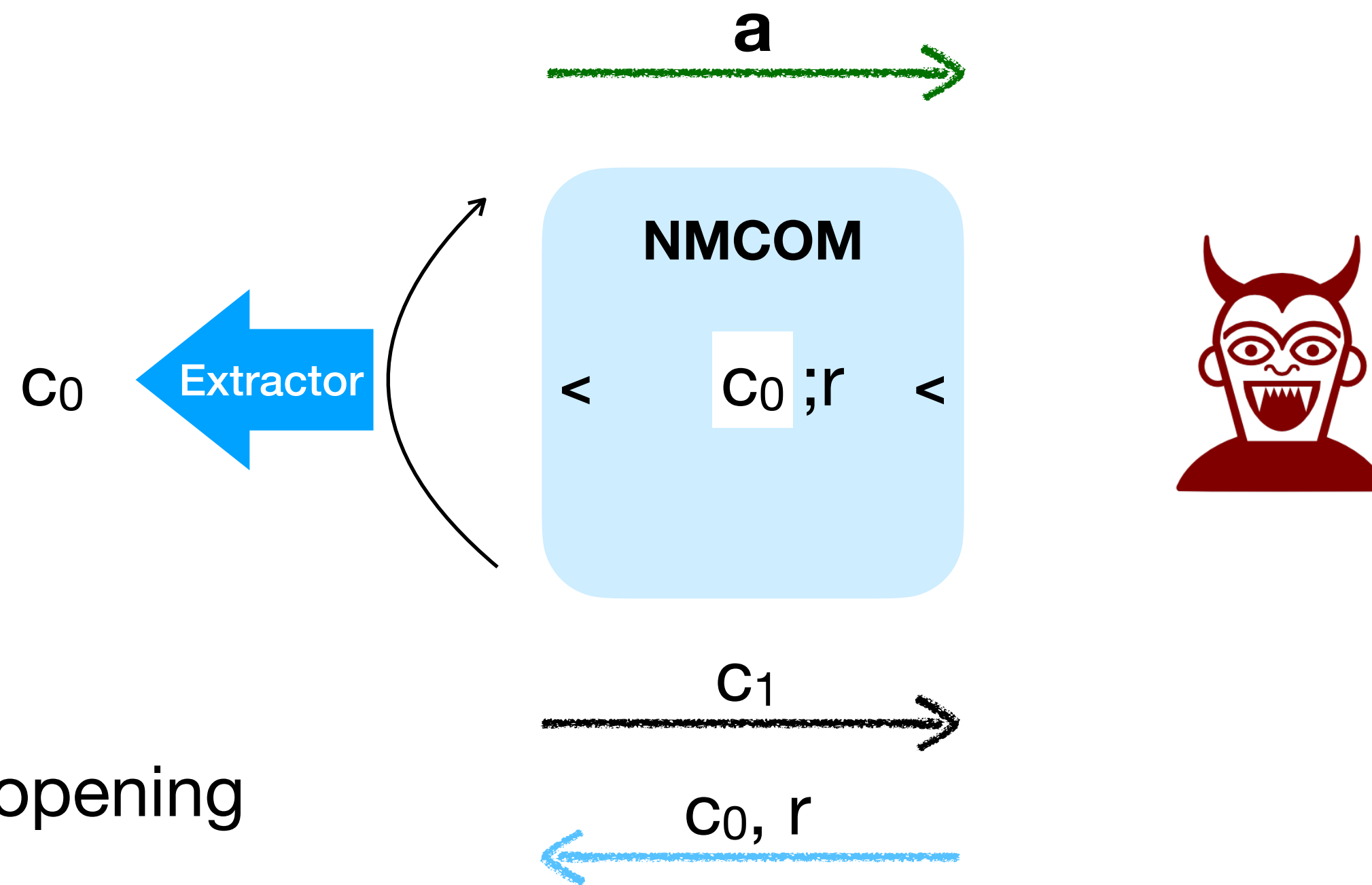


$\mathbf{C}_1 = \mathbf{C}_0 \oplus \mathbf{C}$

# Zero-Knowledge

*Sim*(**x**)

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$



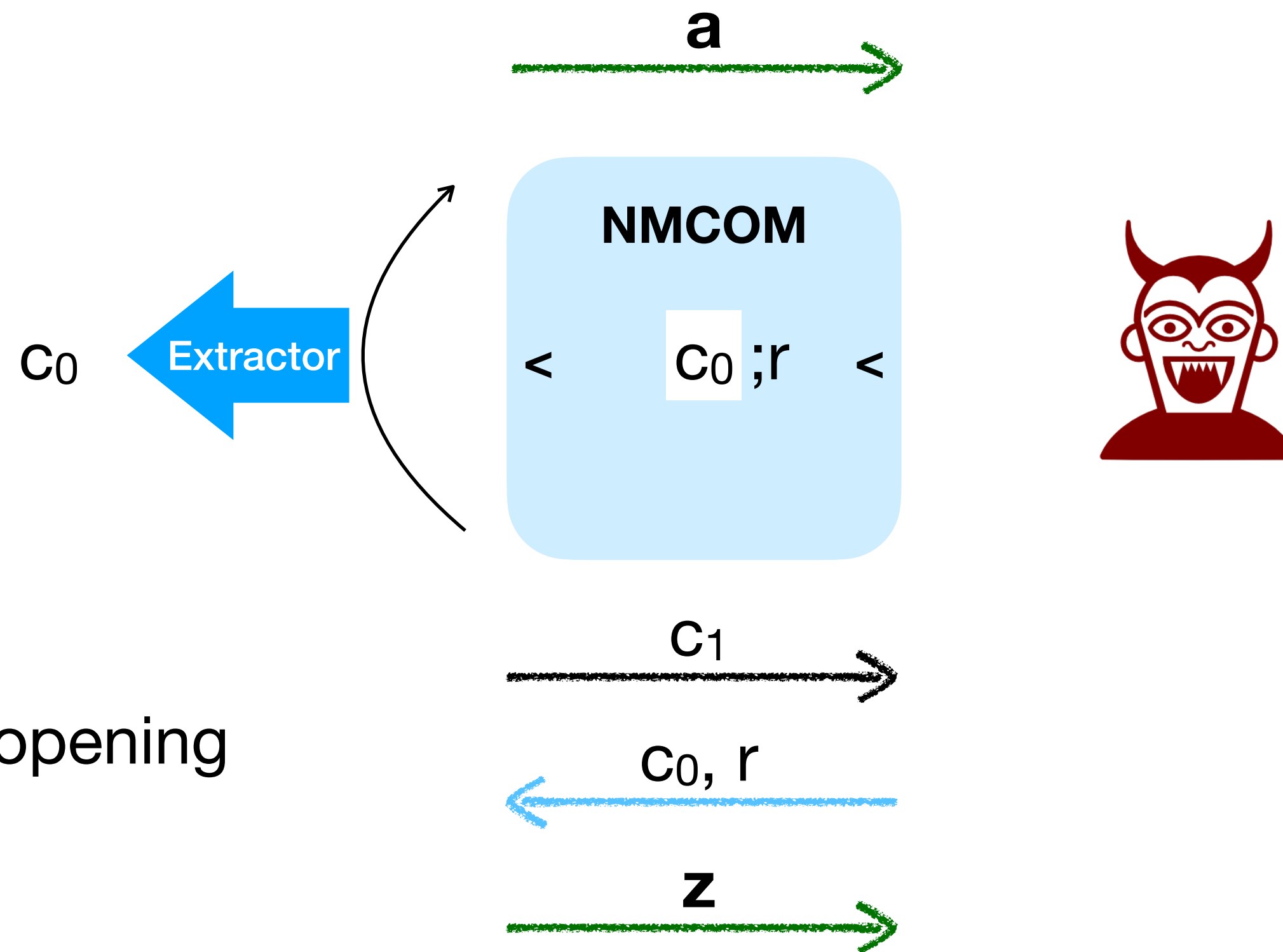
$\mathbf{C}_1 = \mathbf{C}_0 \oplus \mathbf{C}$

If  $(c_0, r)$  is a valid opening

# Zero-Knowledge

*Sim*(**x**)

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$

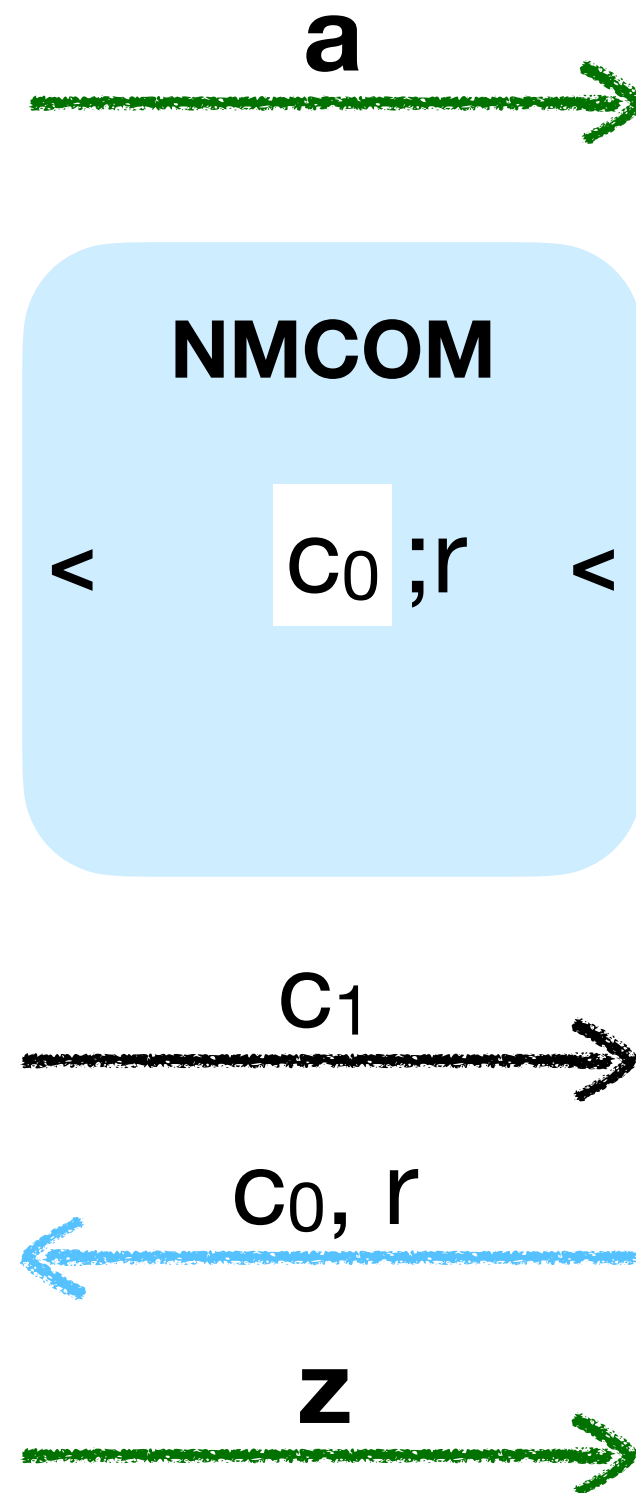


$\mathbf{C}_1 = \mathbf{C}_0 \oplus \mathbf{C}$

If  $(c_0, r)$  is a valid opening

# Soundness (Via Extraction)

PoKExtractor(x)



$$\mathbf{c} = \mathbf{c}_0 \oplus \mathbf{c}_1$$

$$V_{\Sigma}(x, \mathbf{a}, \mathbf{c}, \mathbf{z}) = 1$$

$x, \mathbf{a}, \mathbf{c}, \mathbf{z}$

# Soundness (Via Extraction)

PoKExtractor(**x**)

**a**



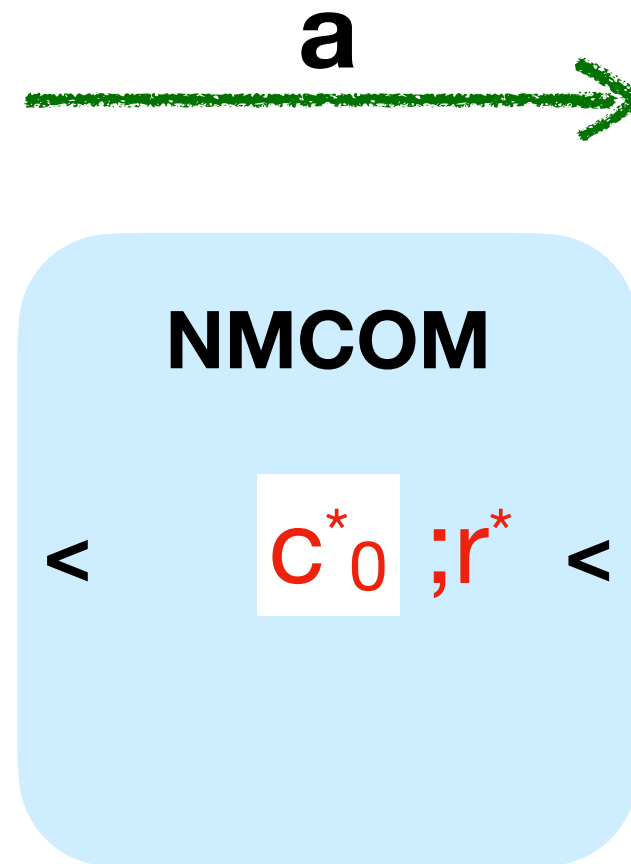
$$\mathbf{c} = \mathbf{c}_0 \oplus \mathbf{c}_1$$

$$V_{\Sigma}(\mathbf{x}, \mathbf{a}, \mathbf{c}, \mathbf{z}) = 1$$

**x, a, c, z**

# Soundness (Via Extraction)

PoKExtractor(x)



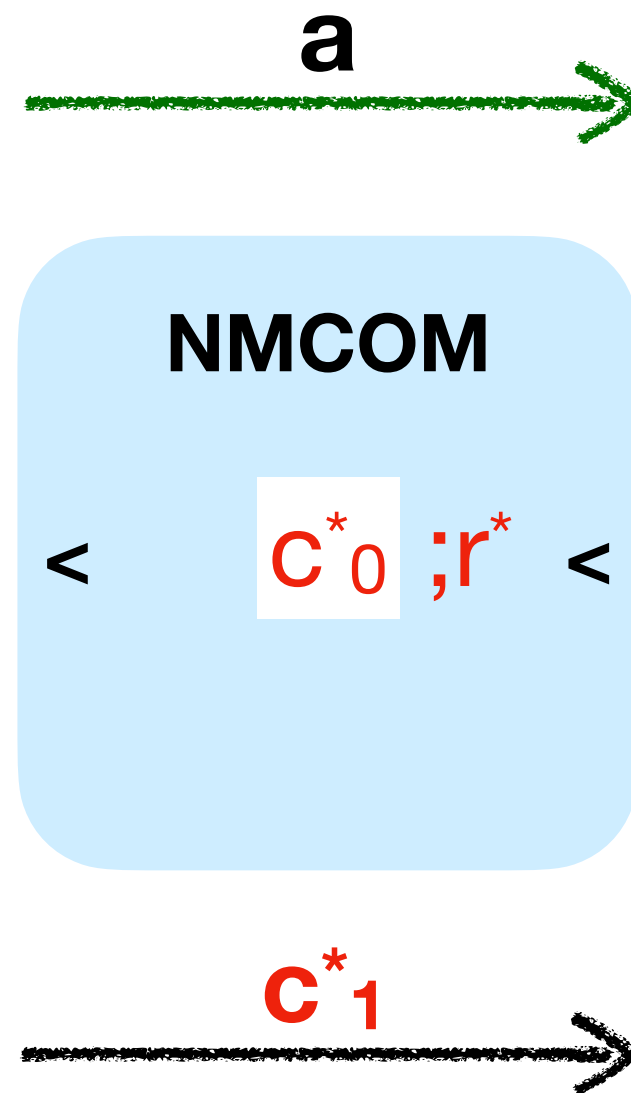
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**x, a, c, z**

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$$\mathbf{c} = \mathbf{c}_0 \oplus \mathbf{c}_1$$

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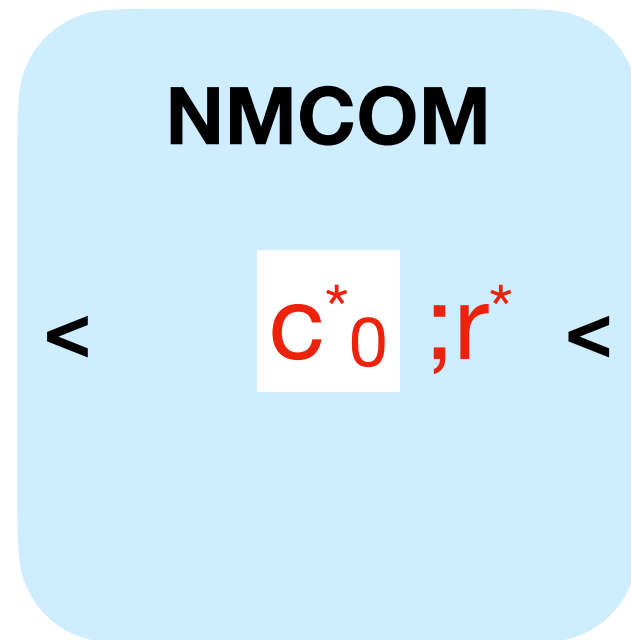
$x, \mathbf{a}, \mathbf{c}, \mathbf{z}$

# Soundness (Via Extraction)

PoKExtractor(x)



$\xrightarrow{\mathbf{a}}$



$\xrightarrow{\mathbf{c}^*_1}$

$\xleftarrow{\mathbf{c}^*_0, r^*}$

$$\mathbf{c} = \mathbf{c}_0 \oplus \mathbf{c}_1$$

$$V_{\Sigma}(x, \mathbf{a}, \mathbf{c}, \mathbf{z}) = 1$$

$x, \mathbf{a}, \mathbf{c}, \mathbf{z}$

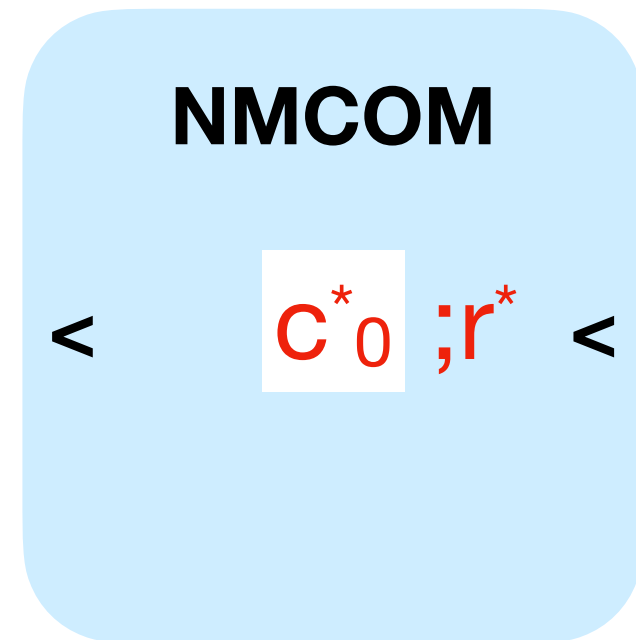


# Soundness (Via Extraction)

PoKExtractor(x)



$\xrightarrow{\mathbf{a}}$



$$\mathbf{c} = \mathbf{c}_0 \oplus \mathbf{c}_1$$

$$V_{\Sigma}(x, \mathbf{a}, \mathbf{c}, \mathbf{z}) = 1$$

$\xrightarrow{\mathbf{c}^*_1}$

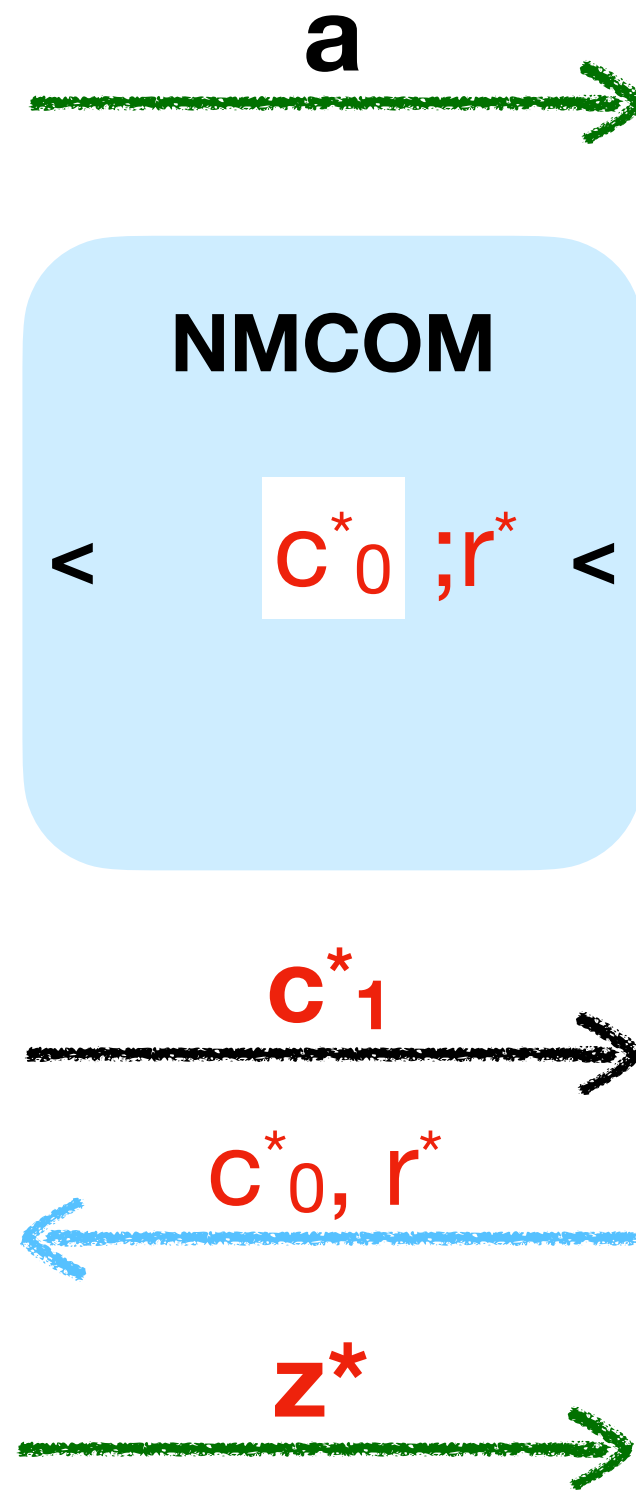
$\xleftarrow{\mathbf{c}^*_0, r^*}$

$x, \mathbf{a}, \mathbf{c}, \mathbf{z}$

$\xrightarrow{\mathbf{z}^*}$

# Soundness (Via Extraction)

PoKExtractor(x)



$$\mathbf{c} = \mathbf{c}_0 \oplus \mathbf{c}_1$$

$$\mathbf{c}^* = \mathbf{c}_0^* \oplus \mathbf{c}_1^*$$

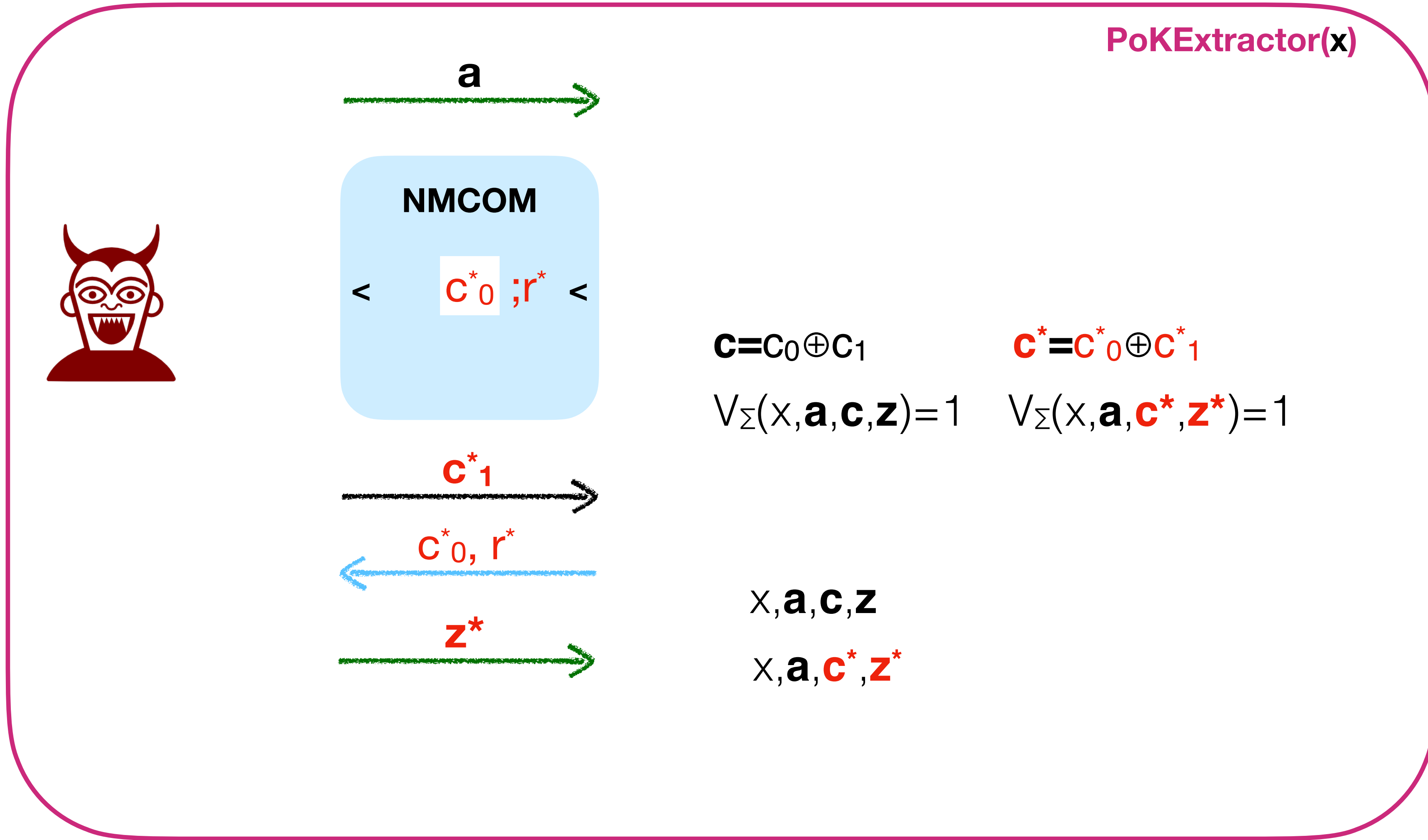
$$V_{\Sigma}(x, \mathbf{a}, \mathbf{c}, \mathbf{z}) = 1$$

$$V_{\Sigma}(x, \mathbf{a}, \mathbf{c}^*, \mathbf{z}^*) = 1$$

$x, \mathbf{a}, \mathbf{c}, \mathbf{z}$

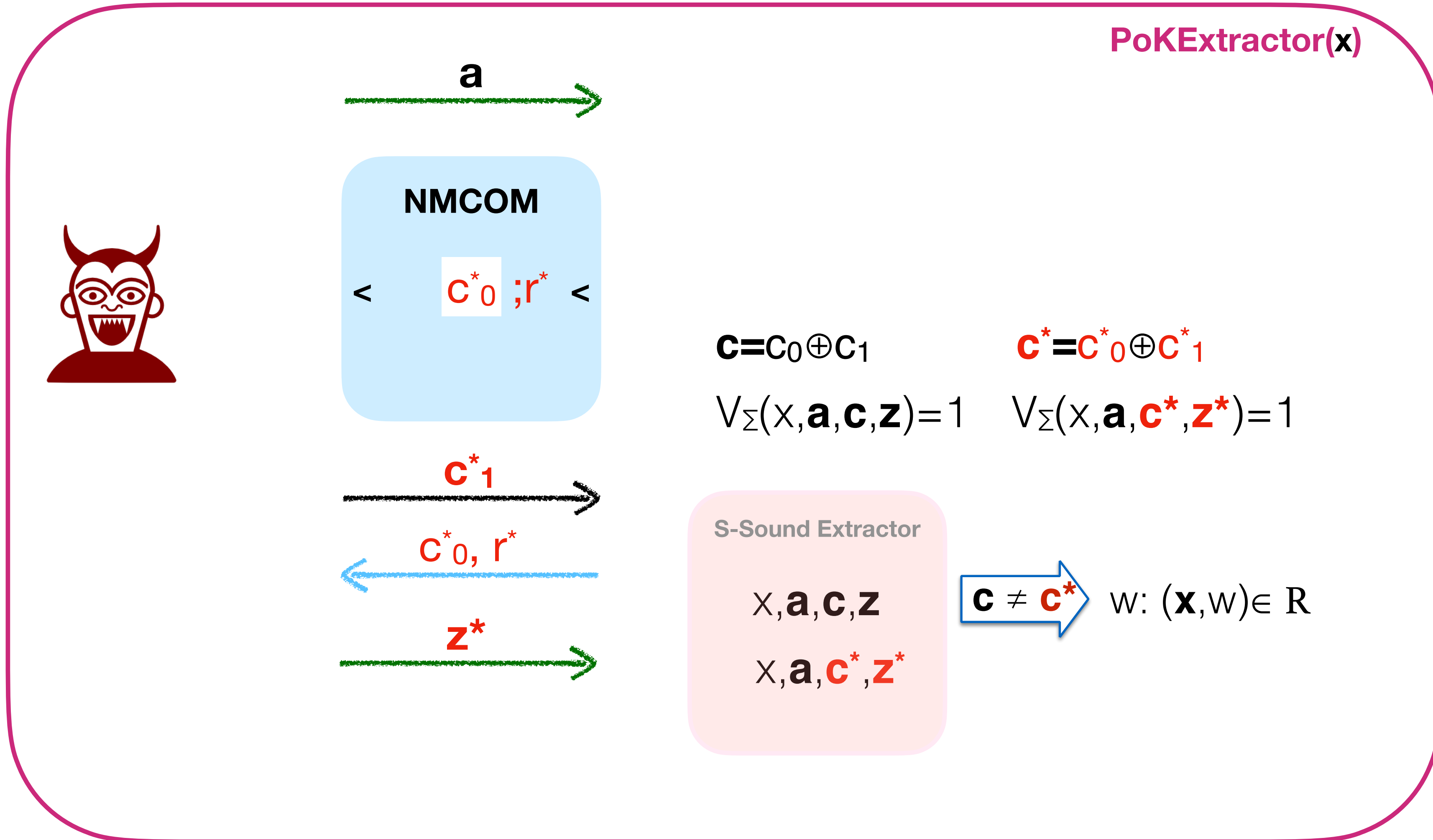
$x, \mathbf{a}, \mathbf{c}^*, \mathbf{z}^*$

# Soundness (Via Extraction)



Hiding of NMCOM guarantees that  $\mathbf{c} \neq \mathbf{c}^*$

# Soundness (Via Extraction)



Hiding of NMCOM guarantees that  $\mathbf{c} \neq \mathbf{c}^*$

# Non-Malleability

$\mathbf{x} \in L$

*Sim*( $\mathbf{x}$ )

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$



$\mathbf{x}' \in L$

# Non-Malleability

$\mathbf{x} \in L$

*Sim*( $\mathbf{x}$ )

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$



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$\mathbf{x} \in L$

*Sim*( $\mathbf{x}$ )

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$

$\mathbf{a}$



$\mathbf{a}'$



$\mathbf{x}' \in L$

# Non-Malleability

$\mathbf{x} \in L$

*Sim*( $\mathbf{x}$ )

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$

$\mathbf{a}$



$\mathbf{a}'$



NMCOM

$\langle \mathbf{c}'_0; r \rangle$

$\mathbf{x}' \in L$



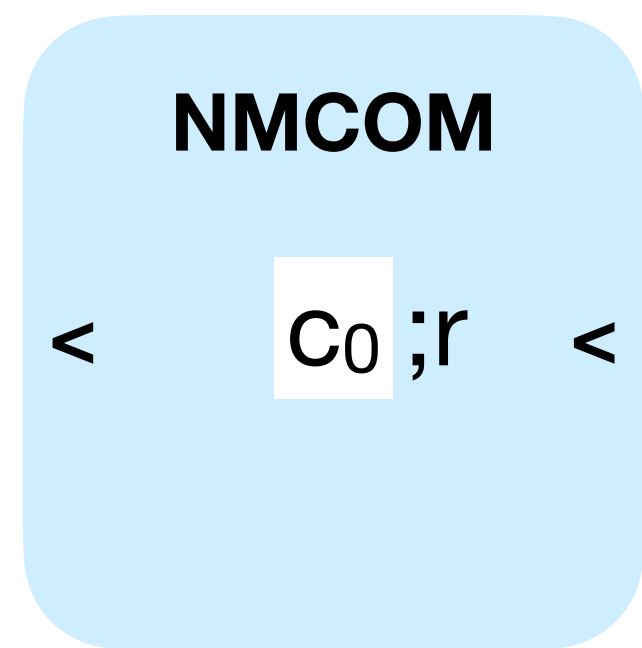
# Non-Malleability

$\mathbf{x} \in L$

*Sim*( $\mathbf{x}$ )

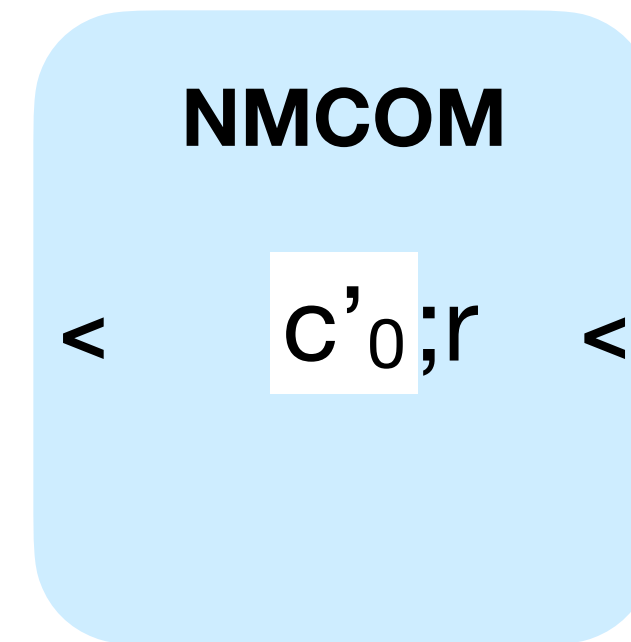
$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$

$\xrightarrow{\mathbf{a}}$



$\mathbf{x}' \in L$

$\xrightarrow{\mathbf{a}'}$

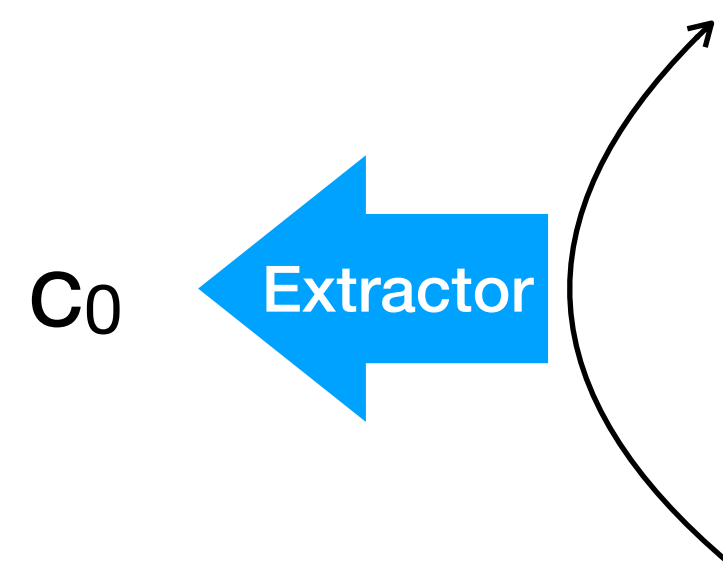


# Non-Malleability

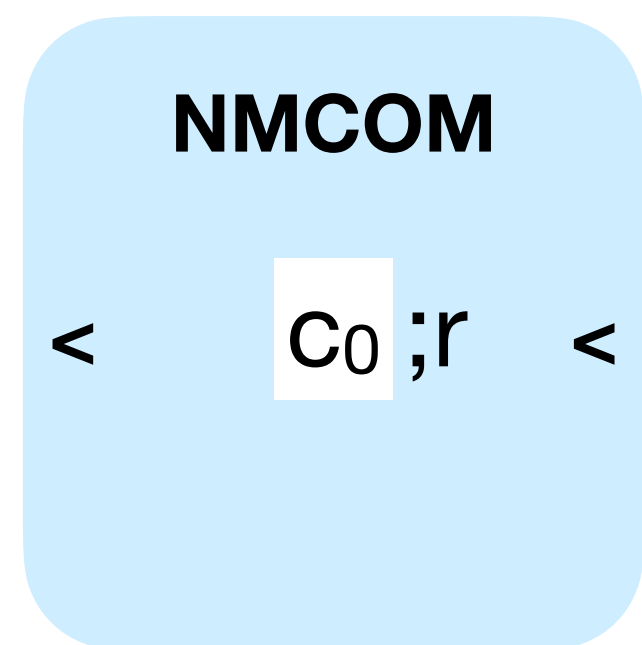
$\mathbf{x} \in L$

*Sim*( $\mathbf{x}$ )

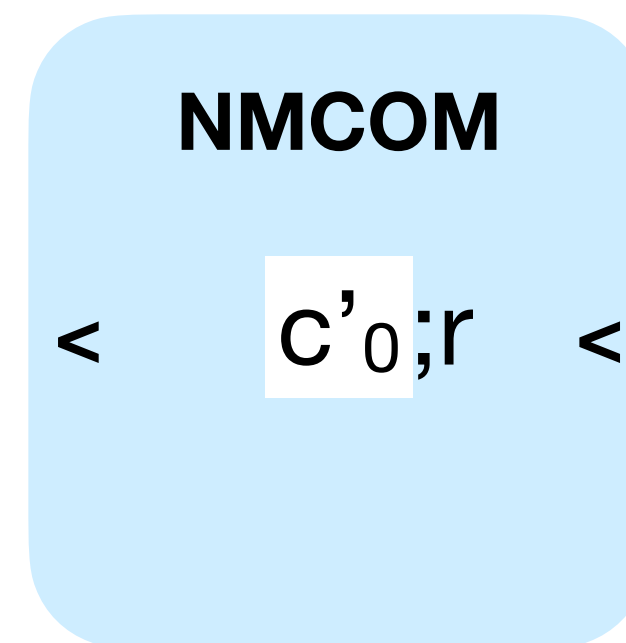
$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$



$\xrightarrow{\mathbf{a}}$



$\xrightarrow{\mathbf{a}'}$



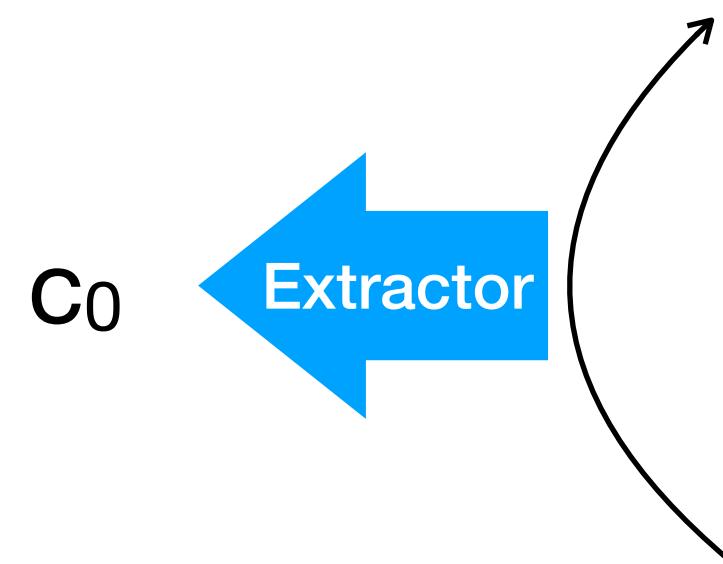
$\mathbf{x}' \in L$

# Non-Malleability

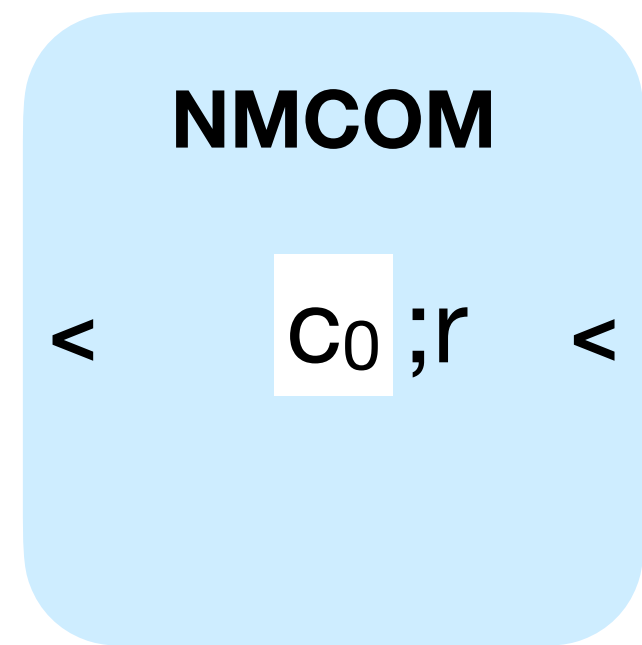
$\mathbf{x} \in L$

*Sim*( $\mathbf{x}$ )

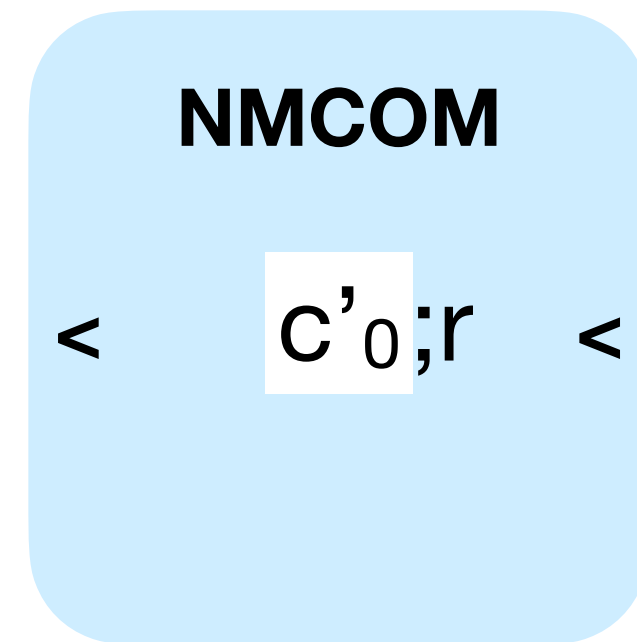
$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$



$\xrightarrow{\mathbf{a}}$



$\xrightarrow{\mathbf{a}'}$



$\mathbf{x}' \in L$

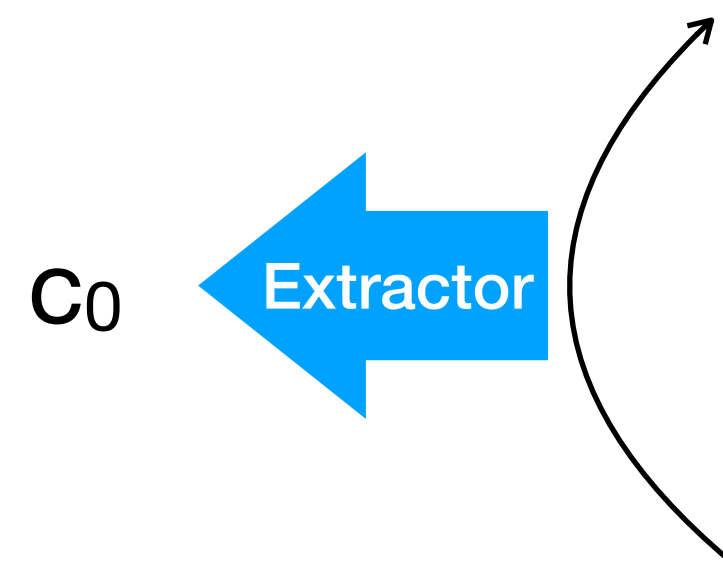
$\mathbf{C}_1 = \mathbf{C}_0 \oplus \mathbf{C}$

# Non-Malleability

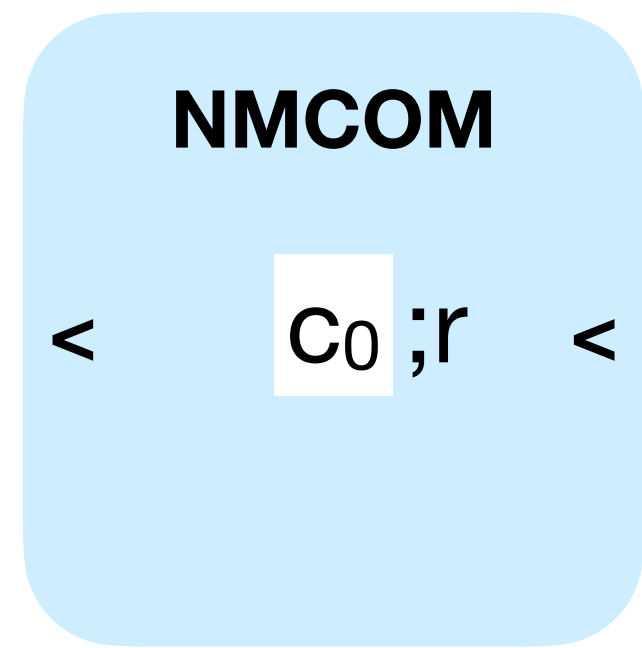
$x \in L$

*Sim*( $x$ )

$a, c, z \leftarrow \text{HVZK}_\Sigma(x)$



$a$  →

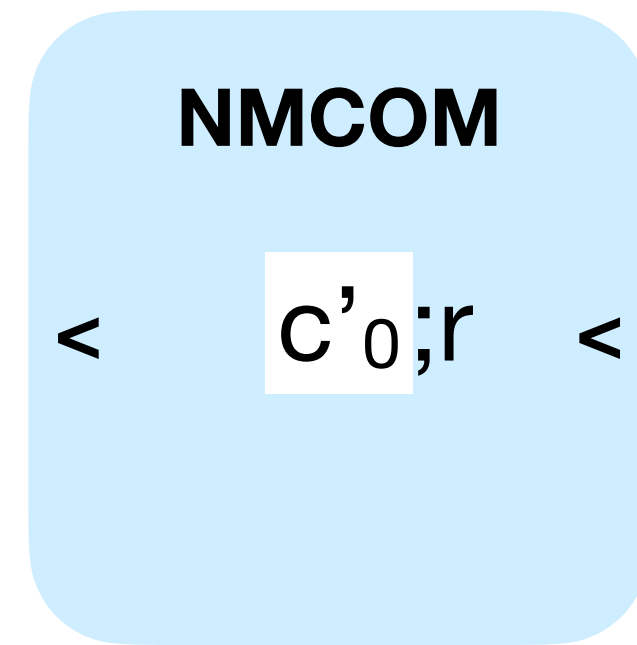


$c_1$  →

$c_1 = c_0 \oplus c$

$x' \in L$

$a'$  →

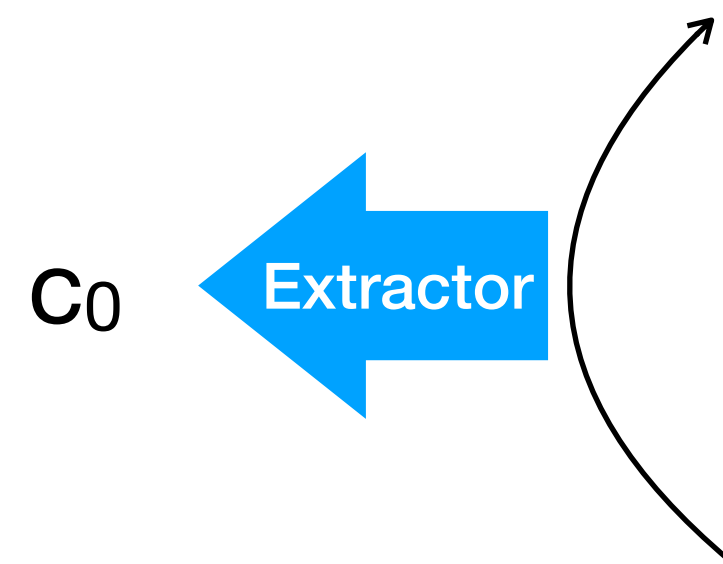


# Non-Malleability

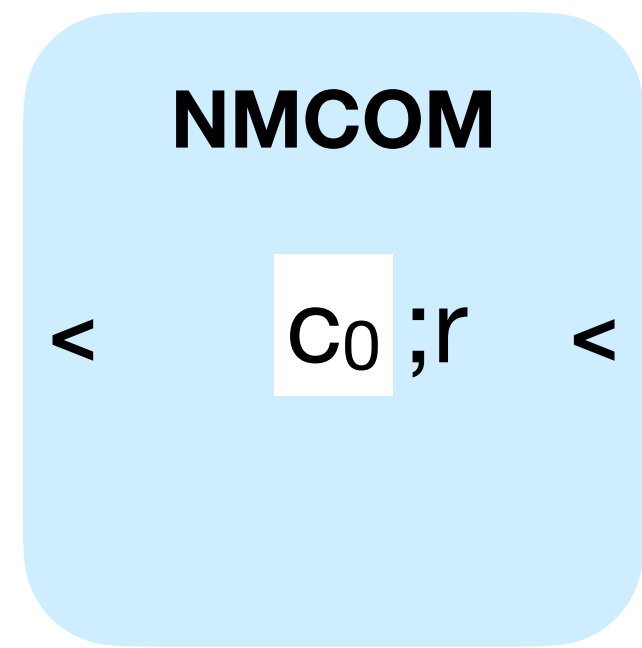
$\mathbf{x} \in L$

*Sim*( $\mathbf{x}$ )

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$



$\xrightarrow{\mathbf{a}}$

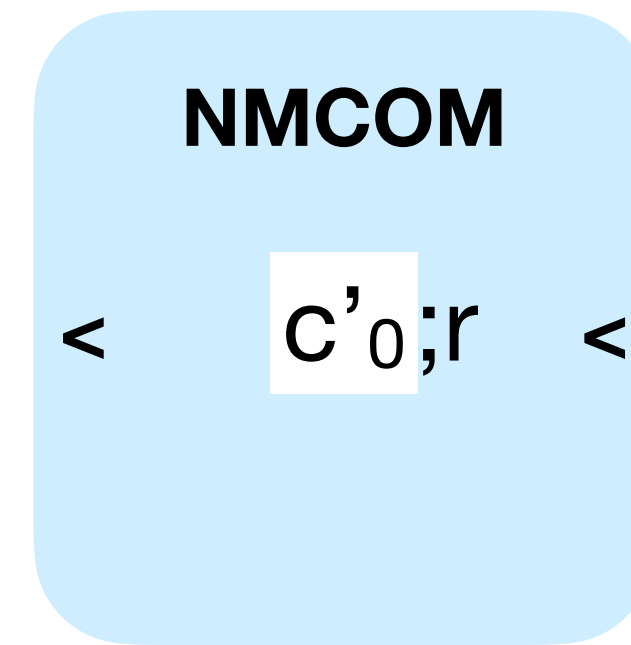


$\xrightarrow{\mathbf{c}_1}$

$\mathbf{c}_1 = \mathbf{c}_0 \oplus \mathbf{c}$

$\mathbf{x}' \in L$

$\xrightarrow{\mathbf{a}'}$



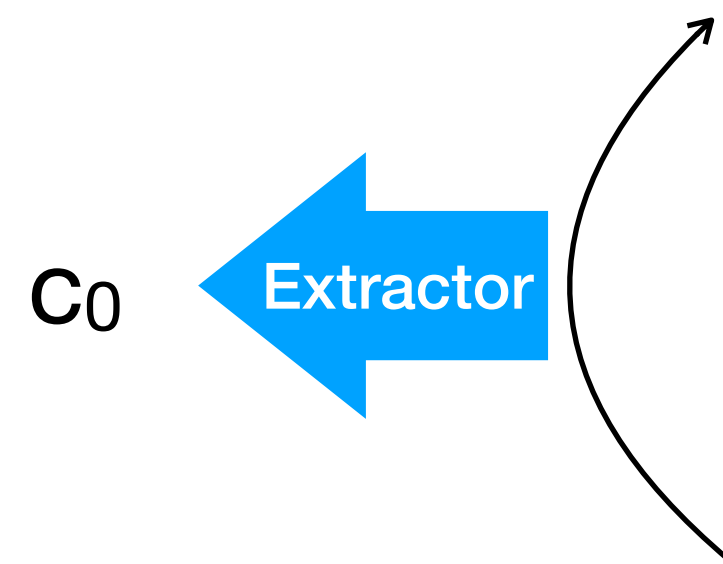
$\xrightarrow{\mathbf{c}'_1}$

# Non-Malleability

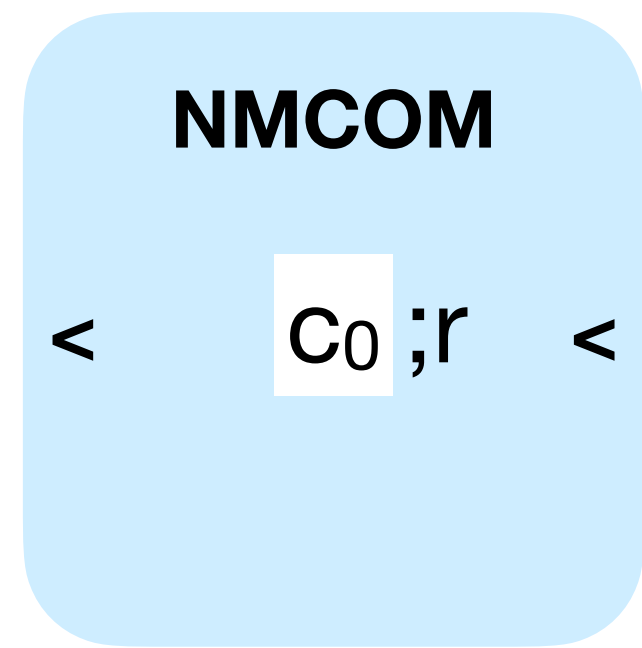
$x \in L$

$Sim(x)$

$a, c, z \leftarrow HVZK_{\Sigma}(x)$



$a$  →

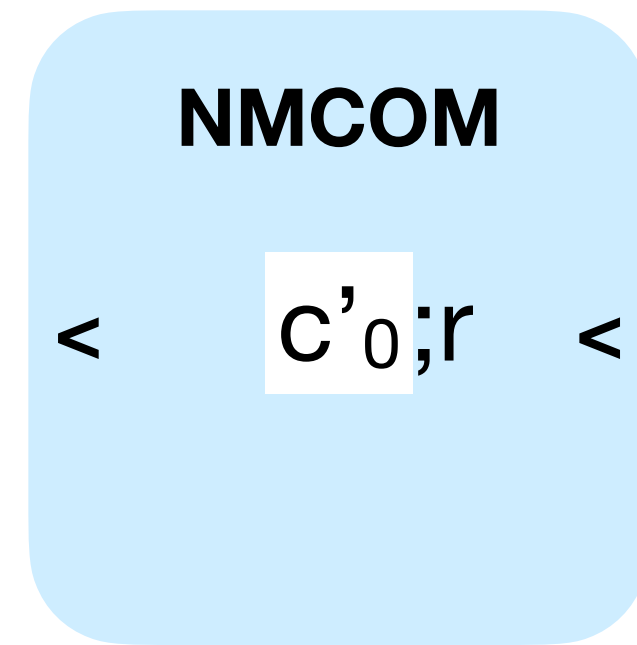


$c_1$  →

$c_1 = c_0 \oplus c$

$x' \in L$

$a'$  →



$c'_1$  →

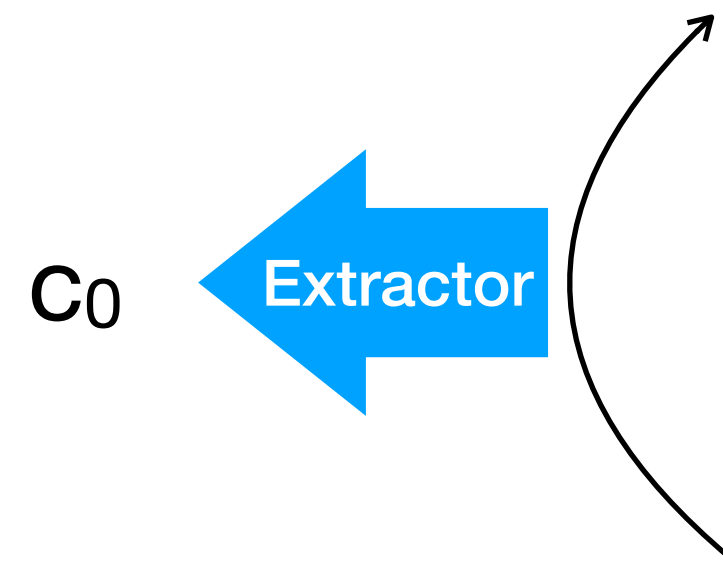
$c'_0, r'$  ←

# Non-Malleability

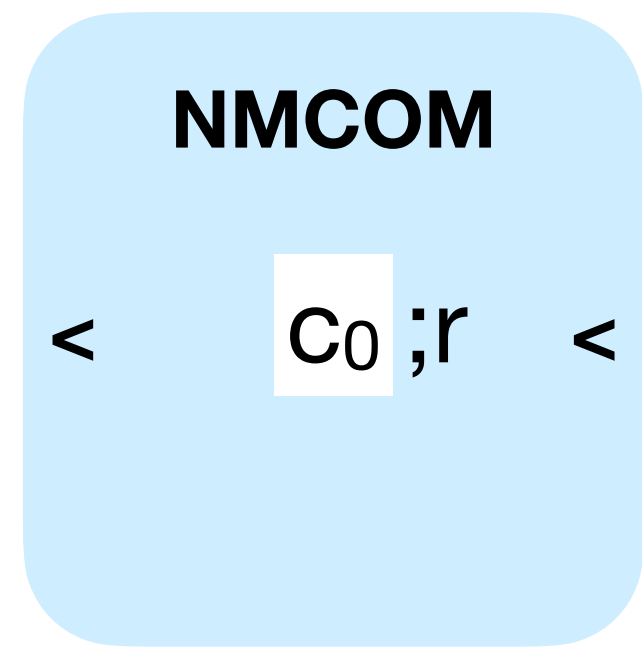
$\mathbf{x} \in L$

$\text{Sim}(\mathbf{x})$

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$



$\xrightarrow{\mathbf{a}}$



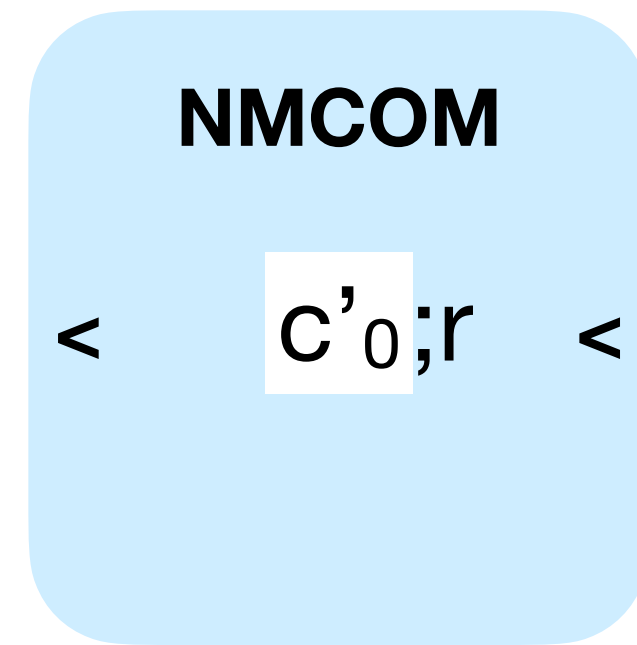
$\xrightarrow{C_1}$

$\xleftarrow{C_0, r}$

$C_1 = C_0 \oplus C$

$\mathbf{x}' \in L$

$\xrightarrow{\mathbf{a}'}$



$\xrightarrow{C'_1}$

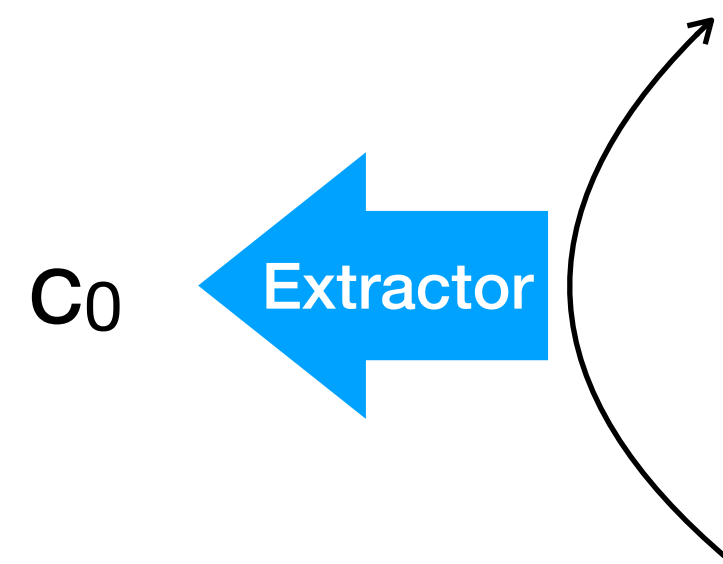
$\xleftarrow{C'_0, r'}$

# Non-Malleability

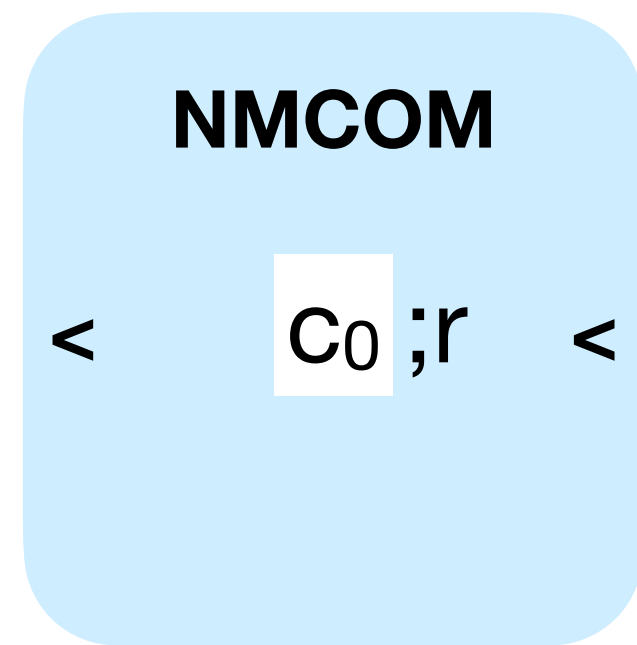
$x \in L$

*Sim*( $x$ )

$a, c, z \leftarrow \text{HVZK}_\Sigma(x)$



$a$  →



$c_1$  →

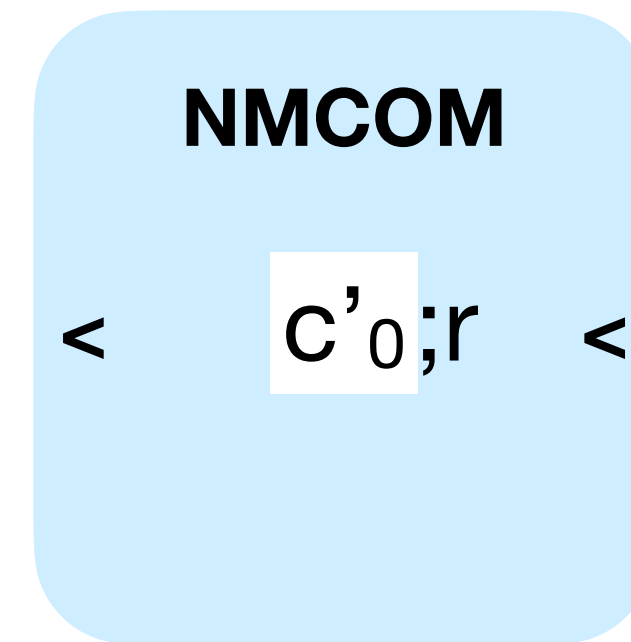
←  $c_0, r$

$c_1 = c_0 \oplus c$

If  $(c_0, r)$  is a valid opening

$x' \in L$

$a'$  →



$c'_1$  →

←  $c'_0, r'$

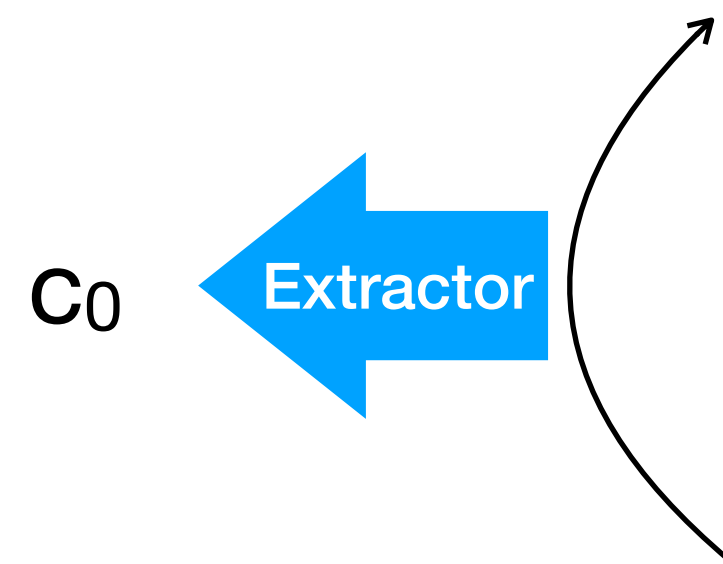


# Non-Malleability

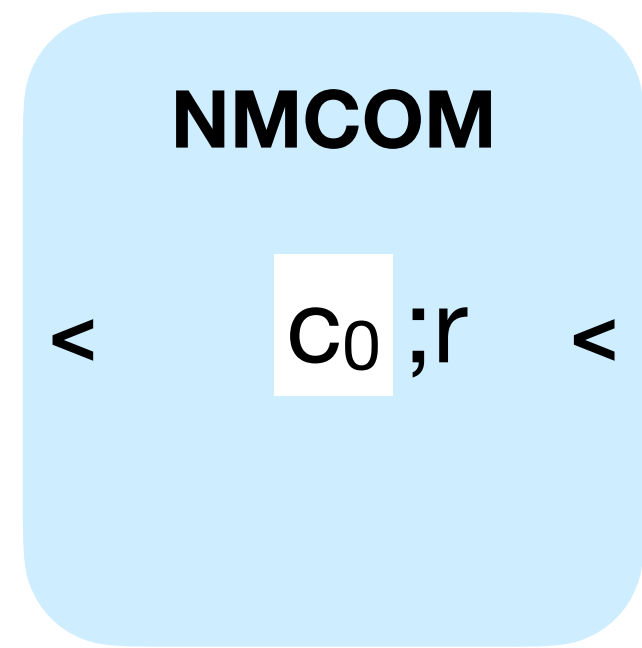
$x \in L$

$Sim(x)$

$a, c, z \leftarrow HVZK_{\Sigma}(x)$



$a$  →



$c_1$  →

←  $c_0, r$

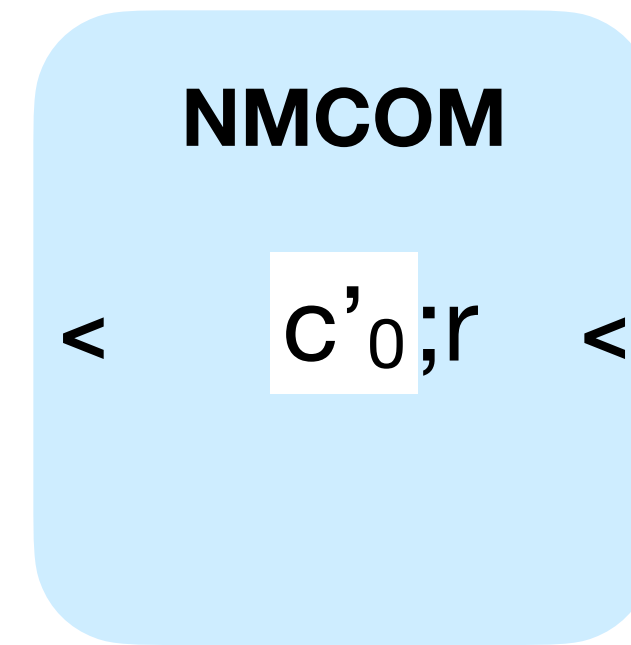
$z$  →

$c_1 = c_0 \oplus c$

If  $(c_0, r)$  is a valid opening

$x' \in L$

$a'$  →



$c'_1$  →

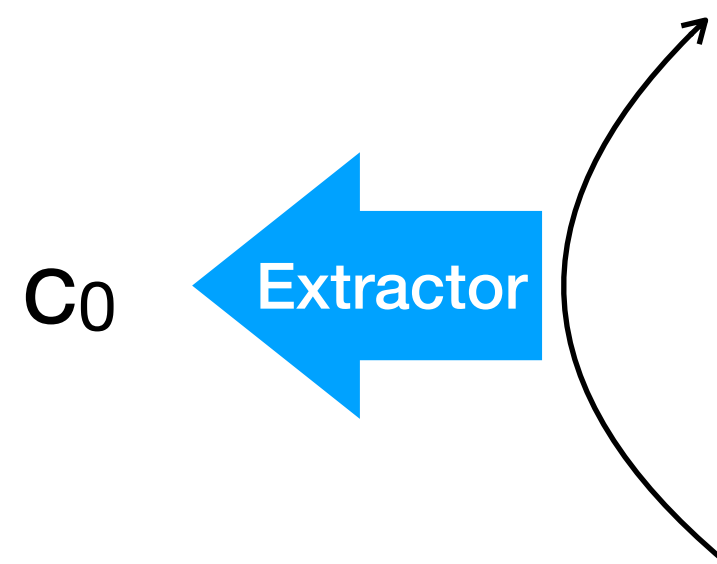
←  $c'_0, r'$

# Non-Malleability

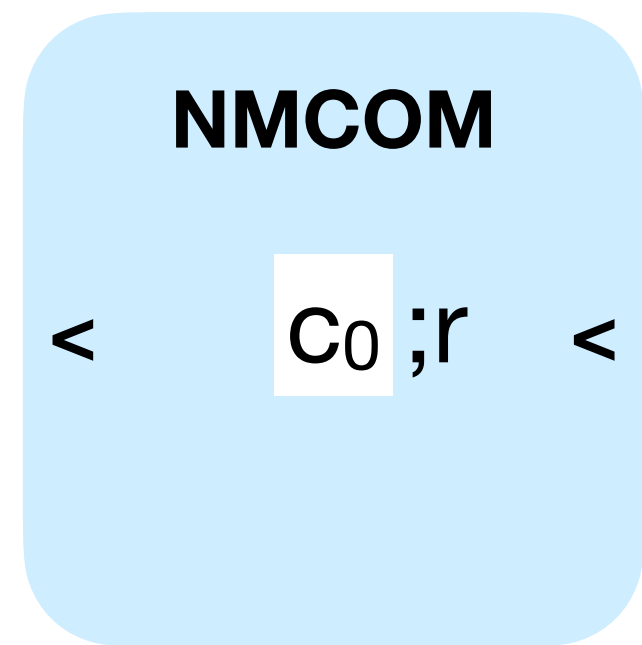
$x \in L$

$Sim(x)$

$a, c, z \leftarrow HVZK_{\Sigma}(x)$



$a$  →



$c_1$  →

←  $c_0, r$

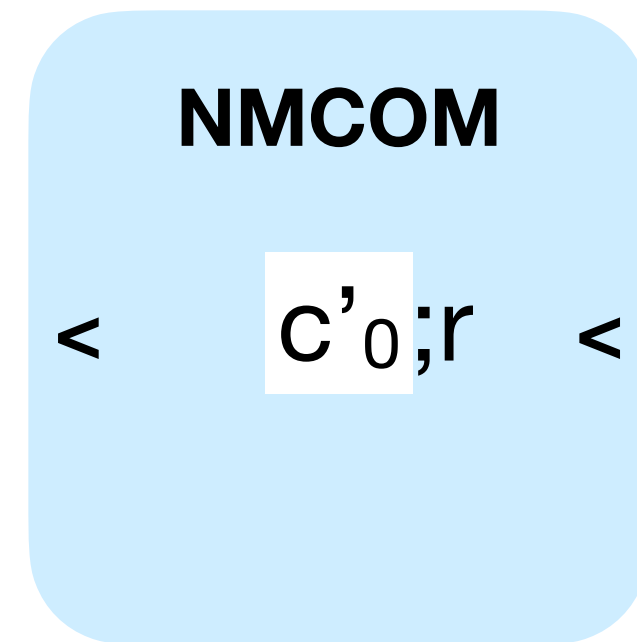
$z$  →

$c_1 = c_0 \oplus c$

If  $(c_0, r)$  is a valid opening

$x' \in L$

$a'$  →



$c'_1$  →

←  $c'_0, r'$

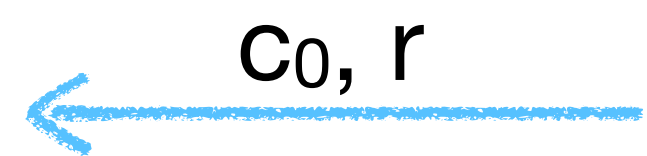
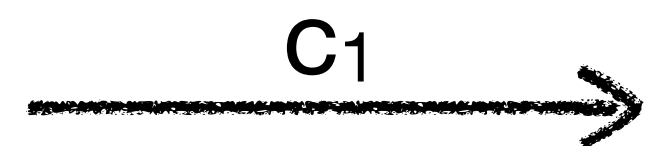
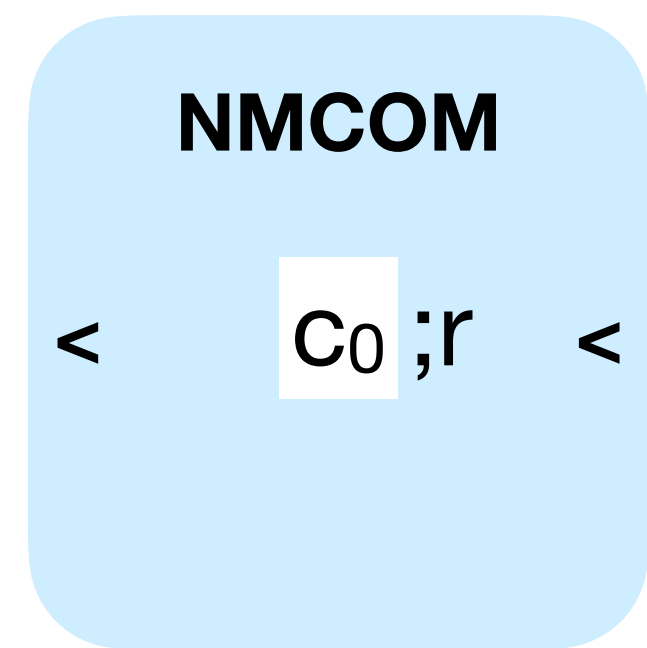
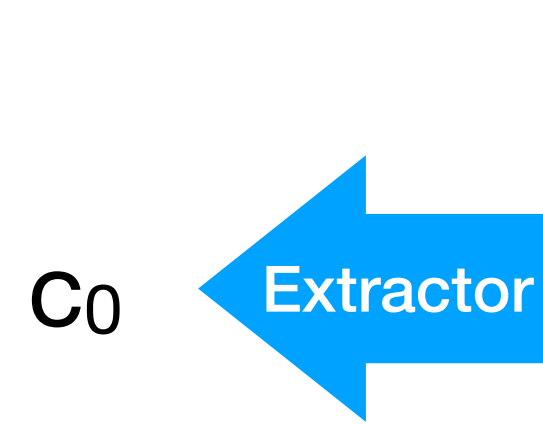
$z'$  →

# Non-Malleability

$x \in L$

*Sim*( $x$ )

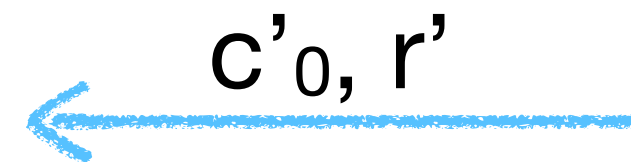
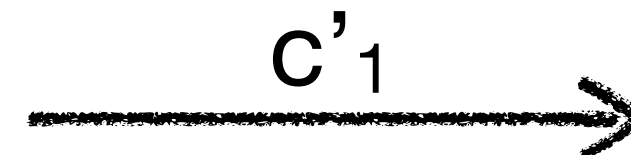
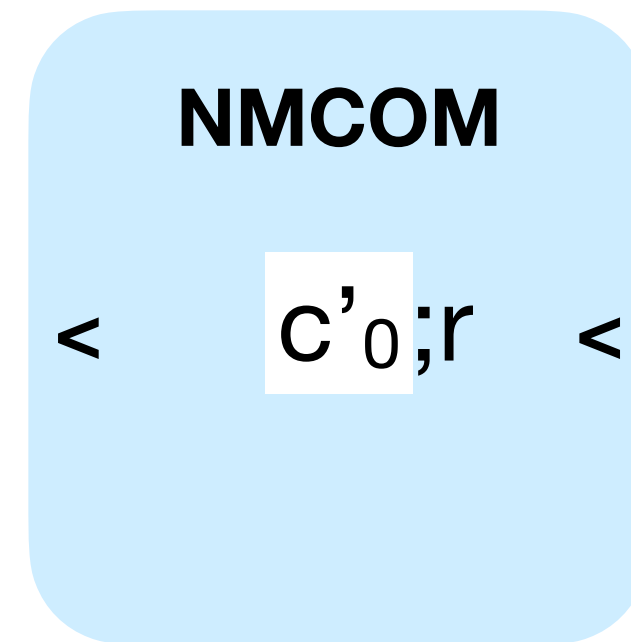
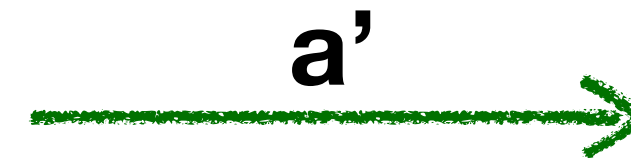
$a, c, z \leftarrow \text{HVZK}_\Sigma(x)$



$c_1 = c_0 \oplus c$

If  $(c_0, r)$  is a valid opening

$x' \in L$



$c' = c'_0 \oplus c'_1$

$V_\Sigma(x', a', c', z') = 1$

# Non-Malleability

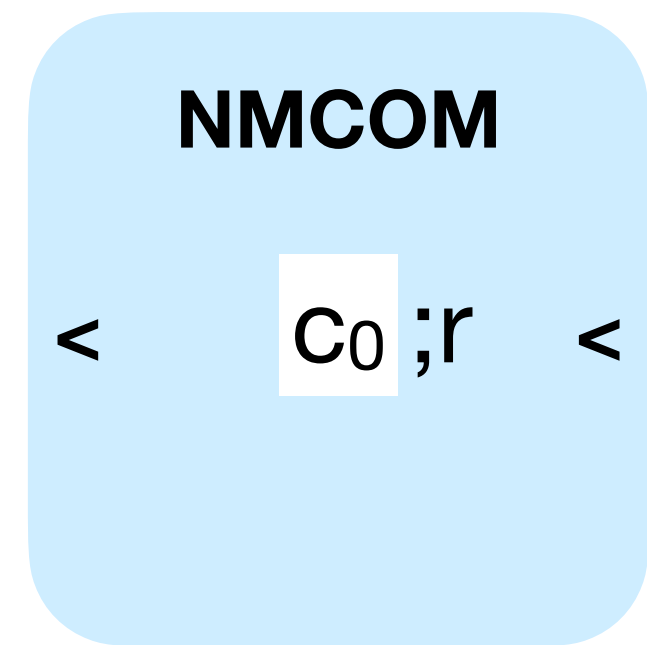
$x \in L$

*Sim*( $x$ )

$a, c, z \leftarrow \text{HVZK}_\Sigma(x)$

$c_0$  ← Extractor

$a$  →



$c_1$  →

←  $c_0, r$

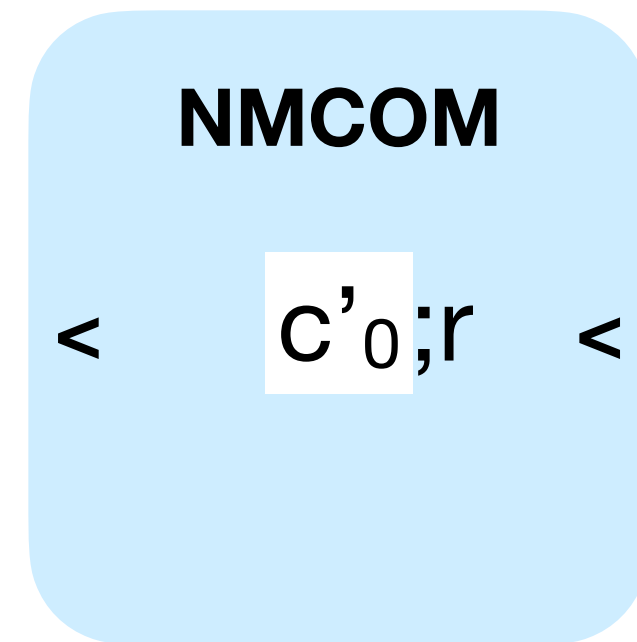
$z$  →

$c_1 = c_0 \oplus c$

If  $(c_0, r)$  is a valid opening

$x' \in L$

$a'$  →



$c'_1$  →

←  $c'_0, r'$

$z'$  →

$c' = c'_0 \oplus c'_1$

$V_\Sigma(x', a', c', z') = 1$

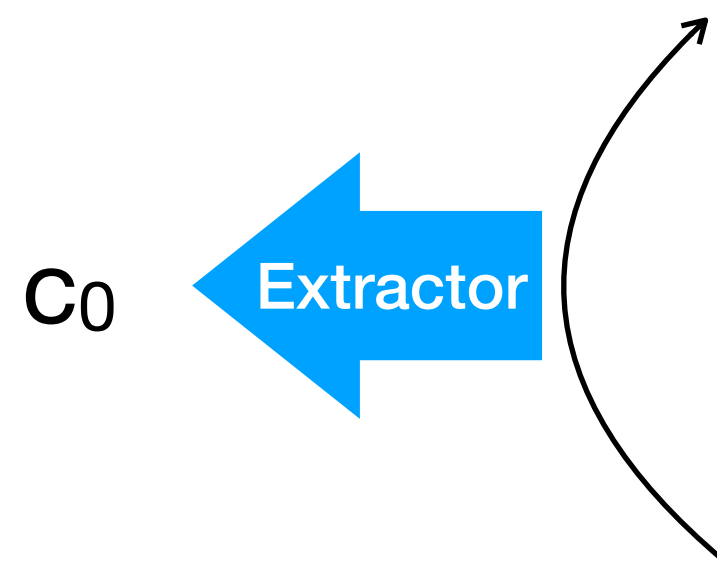
$x, a', c', z'$

# Non-Malleability

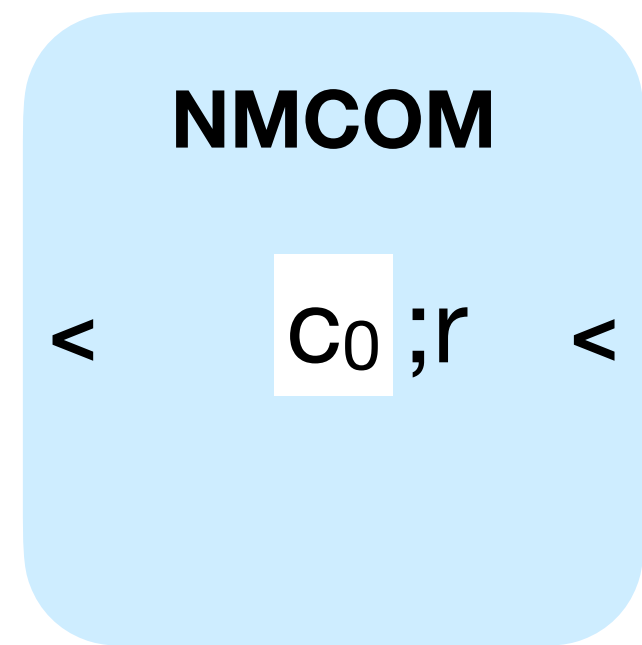
$x \in L$

$Sim(x)$

$a, c, z \leftarrow HVZK_{\Sigma}(x)$



$a$  →



$c_1$  →

←  $c_0, r$

$z$  →

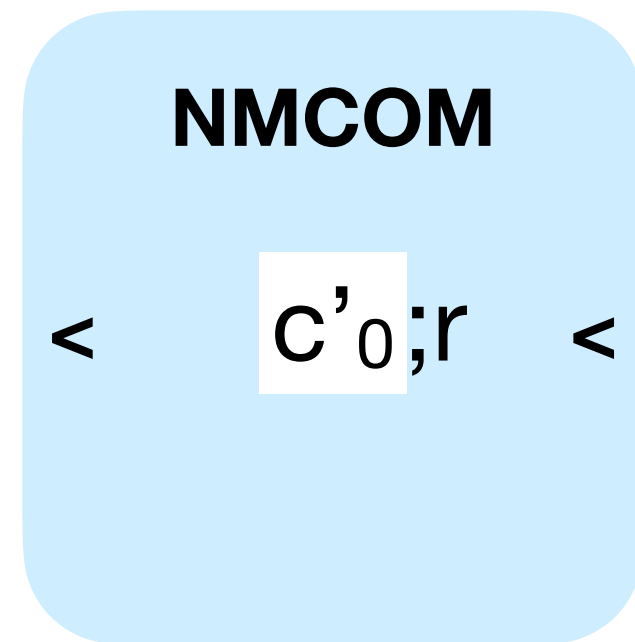
$c_1 = c_0 \oplus c$

If  $(c_0, r)$  is a valid opening

$x' \in L$

PoKExtractor(x)

$a'$  →



$c'_1$  →

←  $c'_0, r'$

$z'$  →

$c' = c'_0 \oplus c'_1$

$V_{\Sigma}(x', a', c', z') = 1$

$x, a', c', z'$

# Non-Malleability

$\mathbf{x} \in L$

*Sim*( $\mathbf{x}$ )

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$

$\mathbf{a}$



$\mathbf{a}'$

$\mathbf{x}' \in L$

PoKExtractor( $\mathbf{x}$ )

$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$

$V_\Sigma(\mathbf{x}', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$

$\mathbf{x}, \mathbf{a}', \mathbf{c}', \mathbf{z}'$

# Non-Malleability

$\mathbf{x} \in L$

*Sim*( $\mathbf{x}$ )

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$

$\mathbf{a}$



$\mathbf{a}'$

NMCOM

$\langle \mathbf{c}^*_0 ; r^* \rangle$

$\mathbf{x}' \in L$

PoKExtractor( $\mathbf{x}$ )

$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$

$V_\Sigma(\mathbf{x}', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$

$\mathbf{x}, \mathbf{a}', \mathbf{c}', \mathbf{z}'$

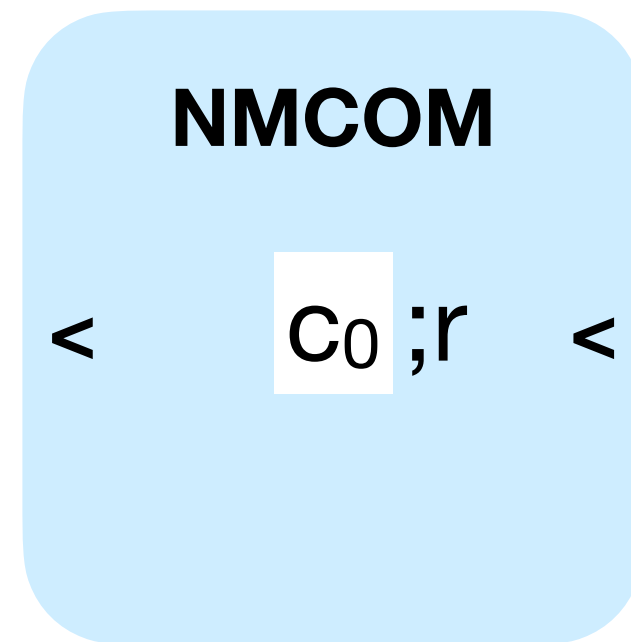
# Non-Malleability

$\mathbf{x} \in L$

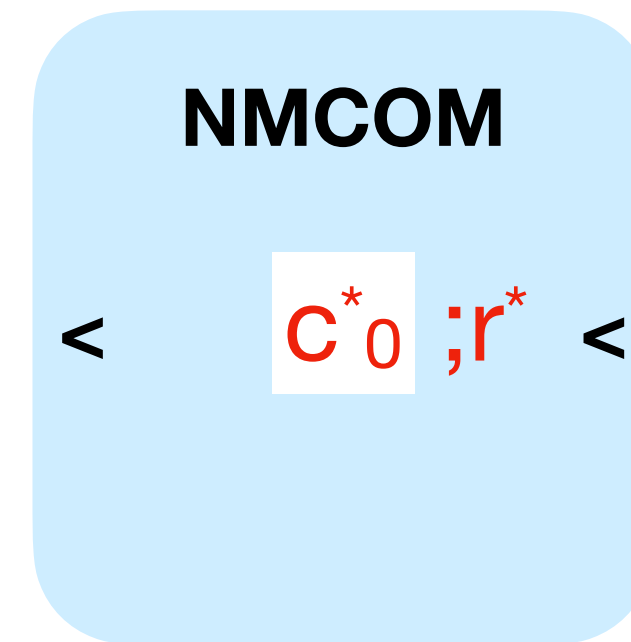
*Sim*( $\mathbf{x}$ )

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$

$\xrightarrow{\mathbf{a}}$



$\xrightarrow{\mathbf{a}'}$



$\mathbf{x}' \in L$

**PoKExtractor**( $\mathbf{x}$ )

$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$

$V_\Sigma(\mathbf{x}', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$

$\mathbf{x}, \mathbf{a}', \mathbf{c}', \mathbf{z}'$

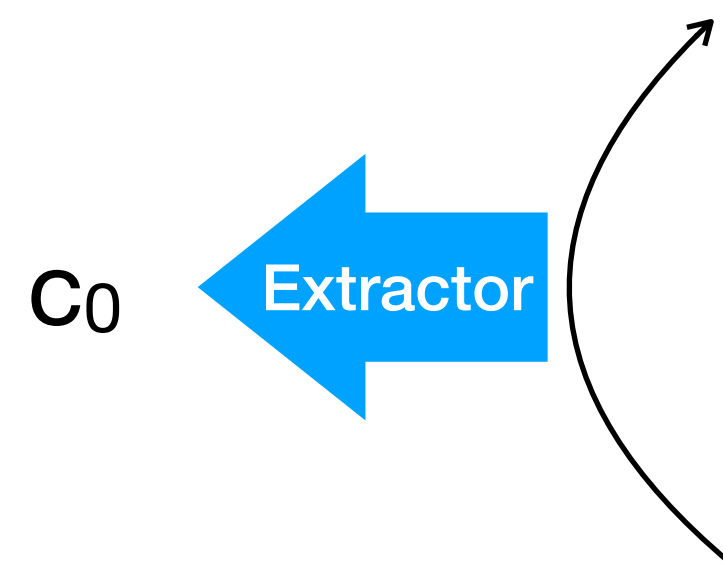


# Non-Malleability

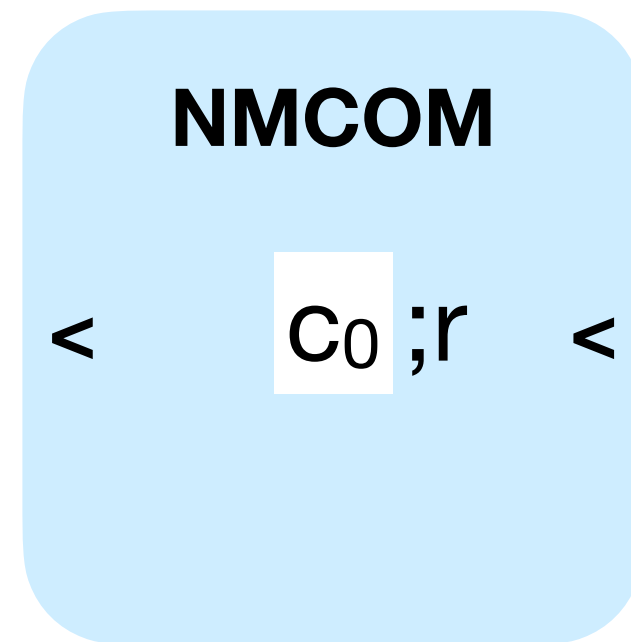
$\mathbf{x} \in L$

*Sim*( $\mathbf{x}$ )

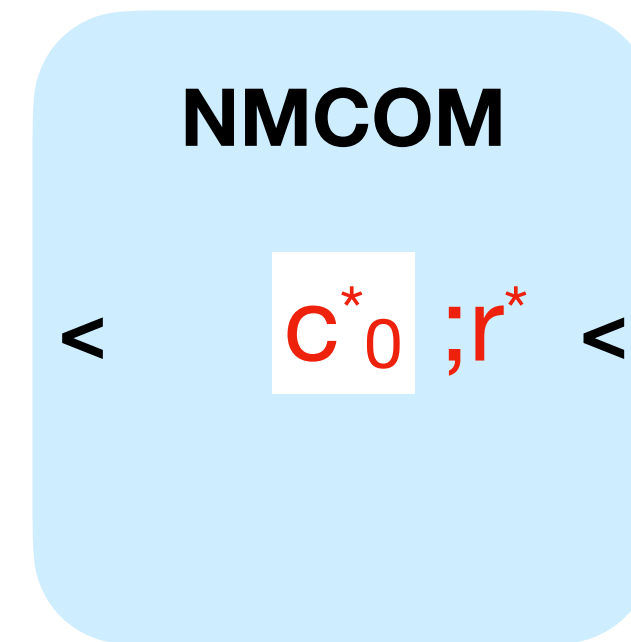
$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$



$\xrightarrow{\mathbf{a}}$



$\xrightarrow{\mathbf{a}'}$



$\mathbf{x}' \in L$

PoKExtractor( $\mathbf{x}$ )

$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$

$V_\Sigma(\mathbf{x}', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$

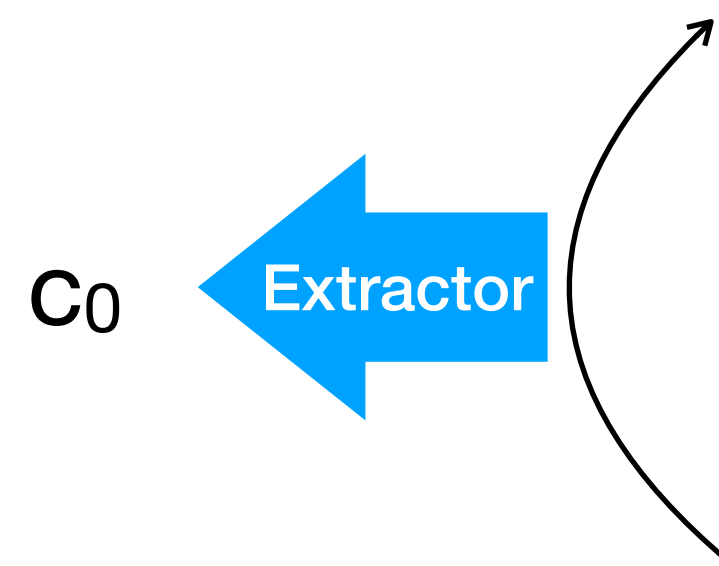
$\mathbf{x}, \mathbf{a}', \mathbf{c}', \mathbf{z}'$

# Non-Malleability

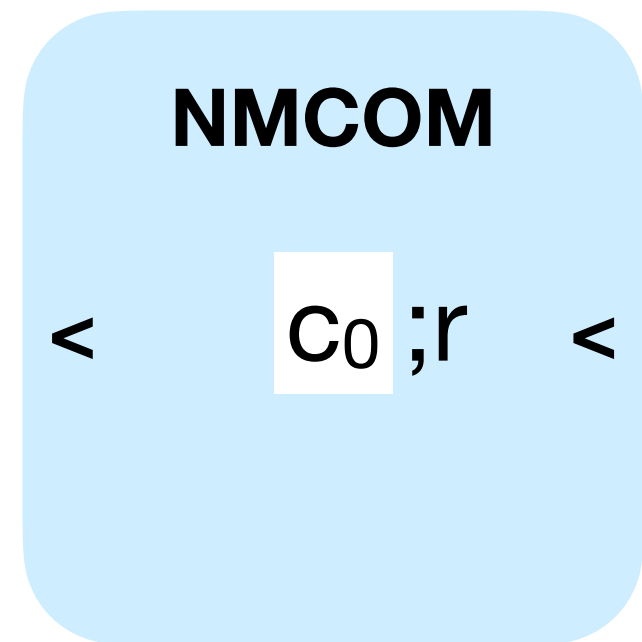
$\mathbf{x} \in L$

*Sim*( $\mathbf{x}$ )

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$



$\mathbf{a}$  →

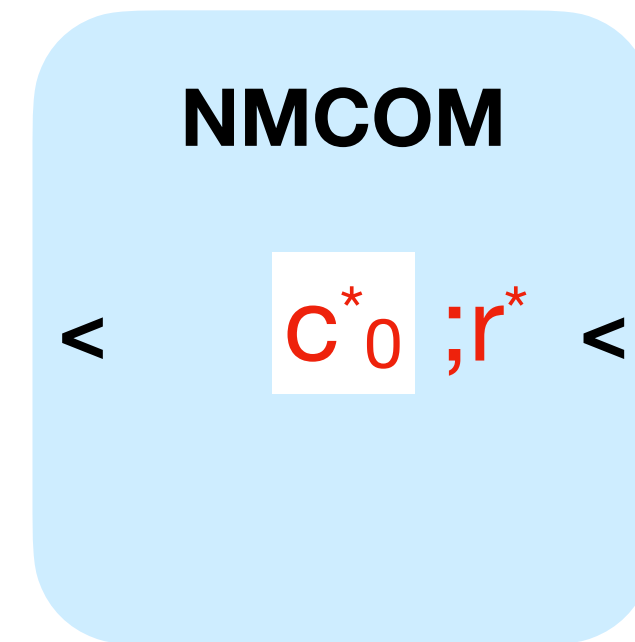


$C_1$  →

$\mathbf{x}' \in L$

PoKExtractor( $\mathbf{x}$ )

$\mathbf{a}'$  →



$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$

$V_\Sigma(\mathbf{x}', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$

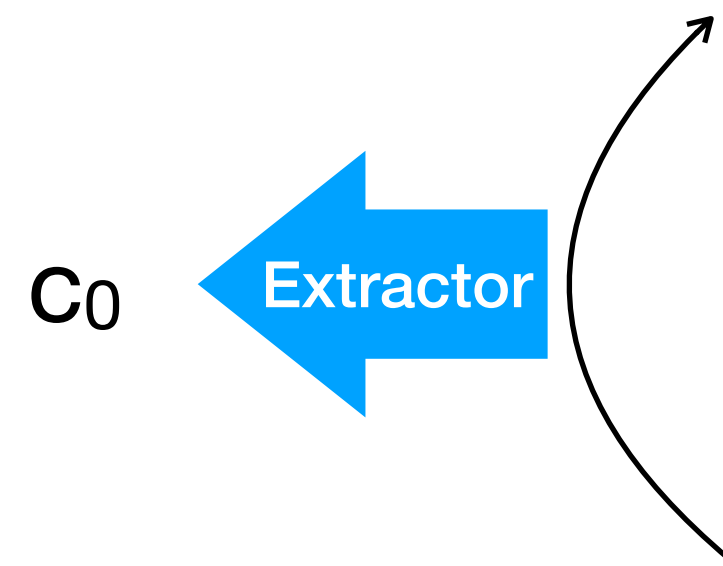
$\mathbf{x}, \mathbf{a}', \mathbf{c}', \mathbf{z}'$

# Non-Malleability

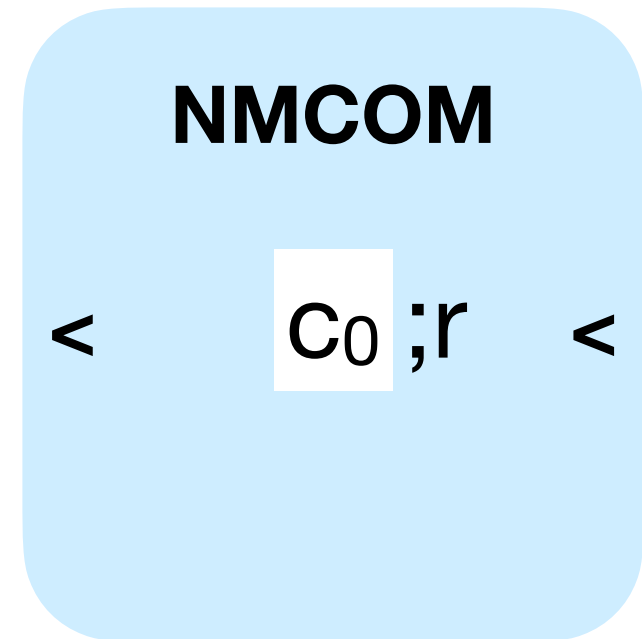
$x \in L$

*Sim*( $x$ )

$a, c, z \leftarrow \text{HVZK}_\Sigma(x)$



$a$  →



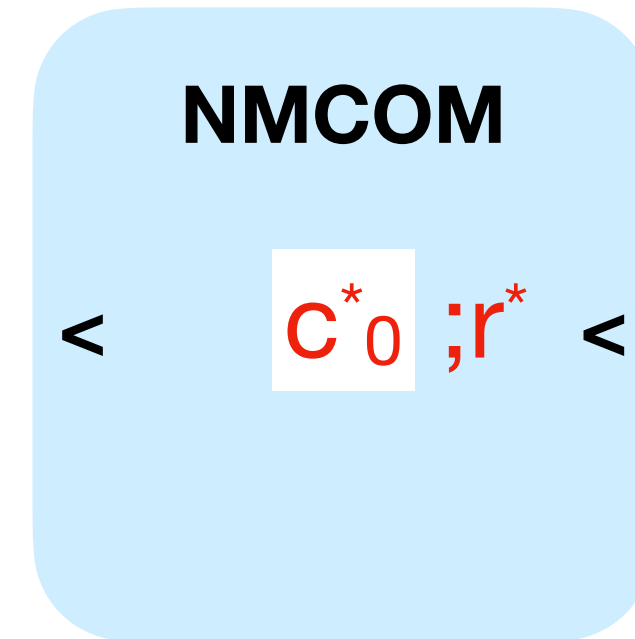
$C_1$  →



$x' \in L$

PoKExtractor( $x$ )

$a'$  →



$C^*_1$  →

$c' = c'_0 \oplus c'_1$

$V_\Sigma(x', a', c', z') = 1$

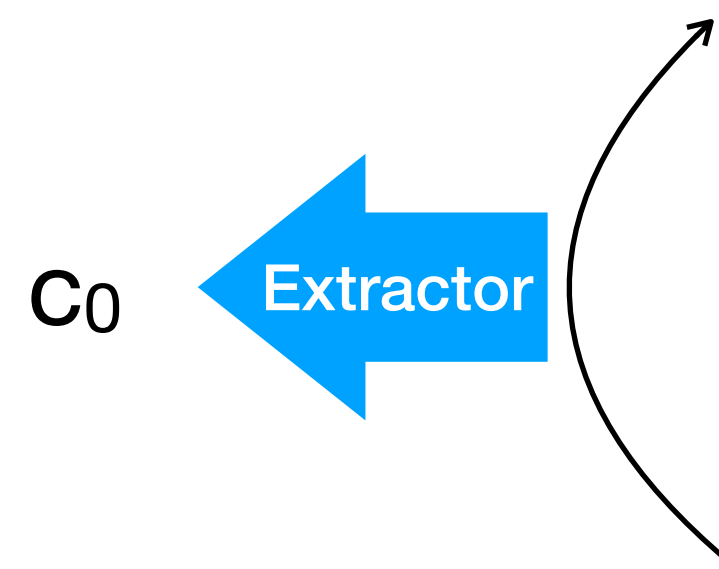
$x, a', c', z'$

# Non-Malleability

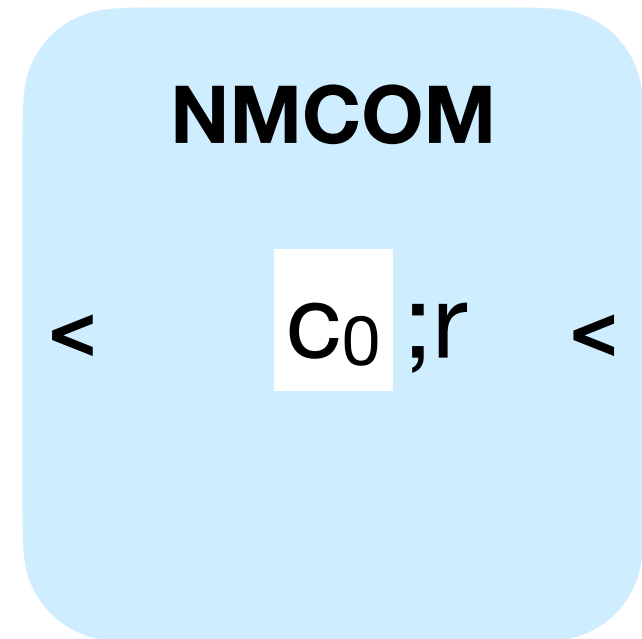
$x \in L$

*Sim*( $x$ )

$a, c, z \leftarrow \text{HVZK}_\Sigma(x)$



$a$  →



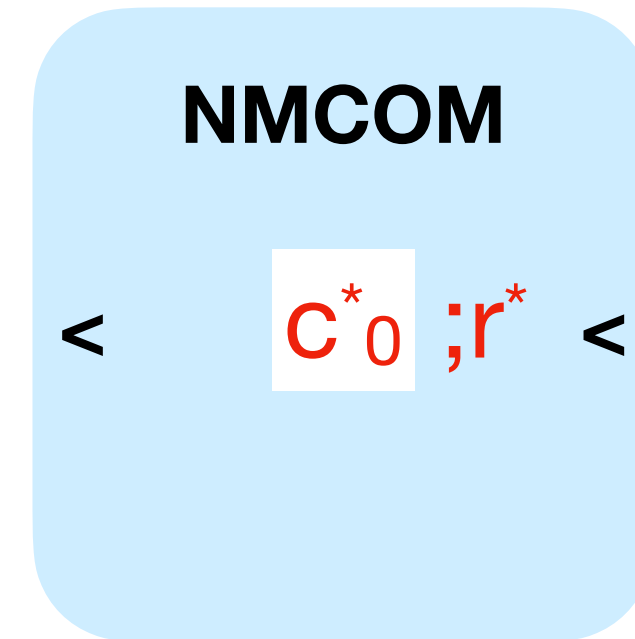
$c_1$  →



$x' \in L$

PoKExtractor( $x$ )

$a'$  →



$c^*_1$  →

$c^*_0, r^*$  ←

$c' = c'_0 \oplus c'_1$

$V_\Sigma(x', a', c', z') = 1$

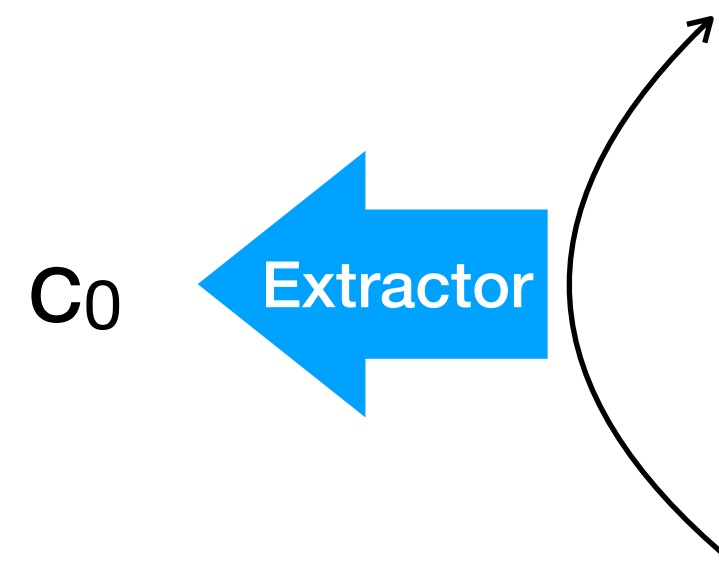
$x, a', c', z'$

# Non-Malleability

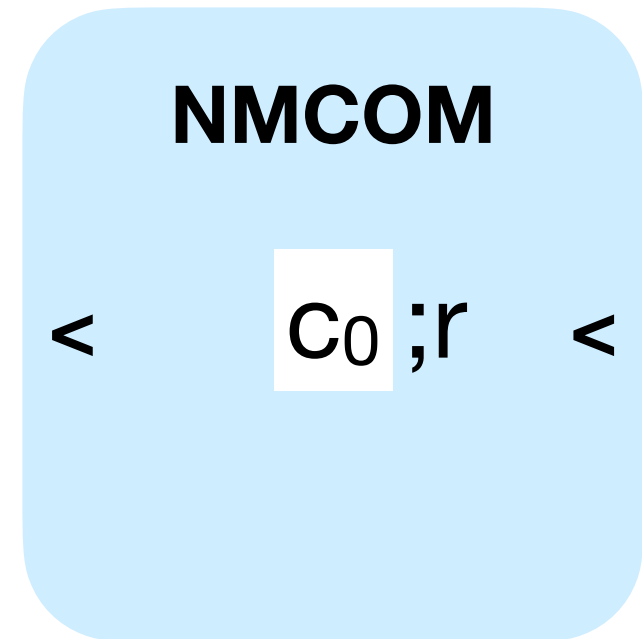
$x \in L$

$Sim(x)$

$a, c, z \leftarrow HVZK_{\Sigma}(x)$



$a$  →



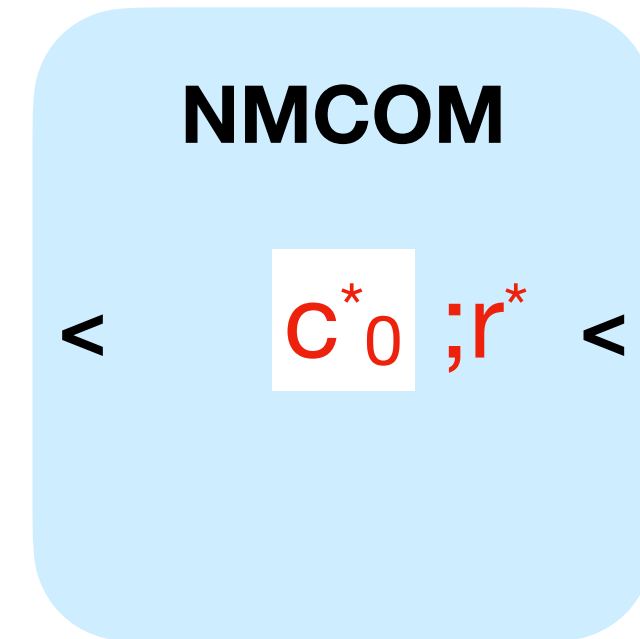
$c_1$  →

←  $c_0, r$

$x' \in L$

**PoKExtractor(x)**

$a'$  →



$c^*_1$  →

←  $c^*_0, r^*$

$c' = c'_0 \oplus c'_1$

$V_{\Sigma}(x', a', c', z') = 1$

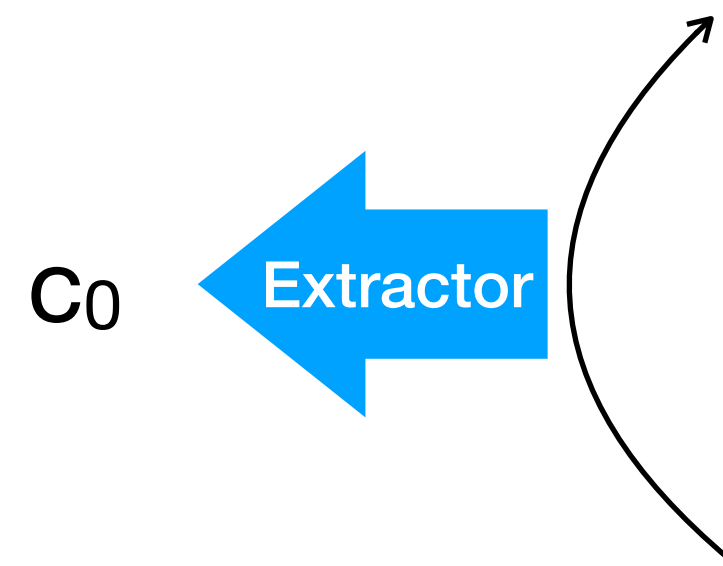
$x, a', c', z'$

# Non-Malleability

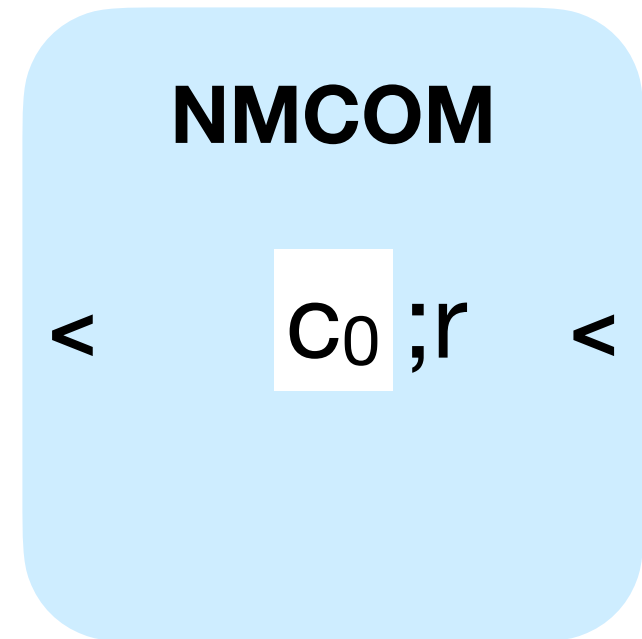
$x \in L$

*Sim*( $x$ )

$a, c, z \leftarrow \text{HVZK}_\Sigma(x)$



$a$  →



$c_1$  →

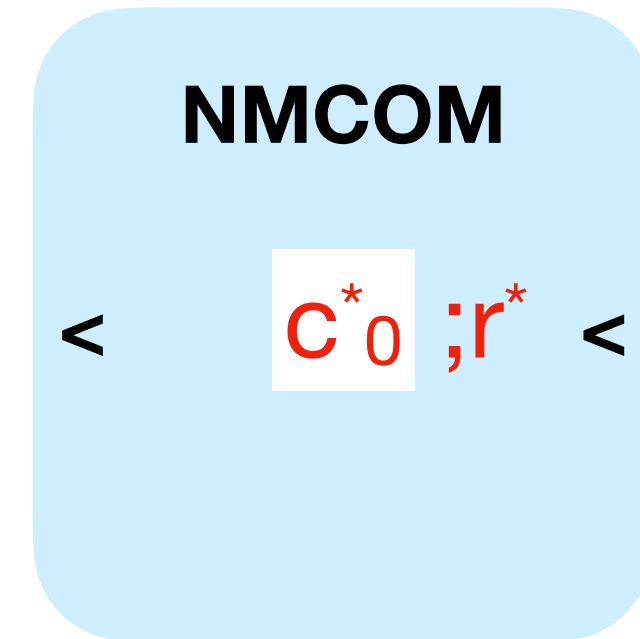
←  $c_0, r$

$z$  →

$x' \in L$

PoKExtractor( $x$ )

$a'$  →



$c^*_1$  →

←  $c^*_0, r^*$

$c' = c'_0 \oplus c'_1$

$V_\Sigma(x', a', c', z') = 1$

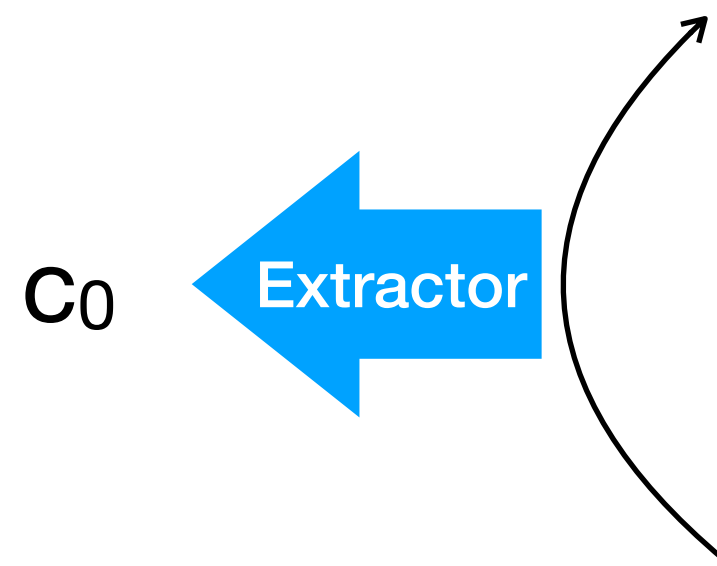
$x, a', c', z'$

# Non-Malleability

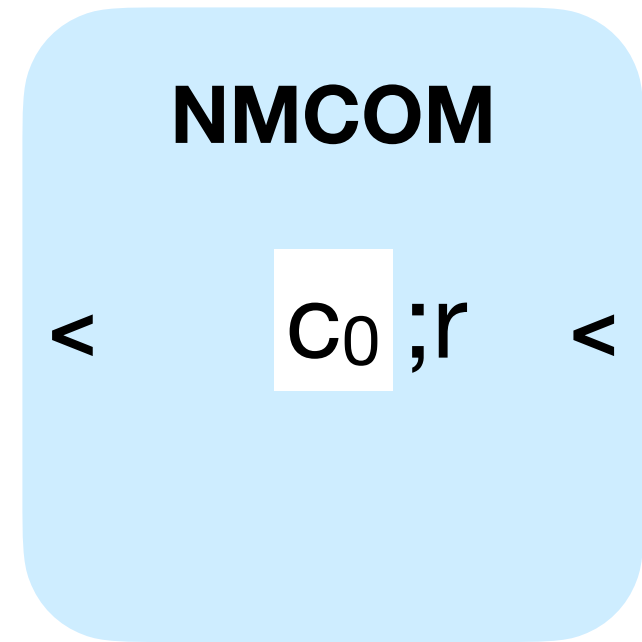
$x \in L$

*Sim*( $x$ )

$a, c, z \leftarrow \text{HVZK}_\Sigma(x)$



$a$  →



$C_1$  →

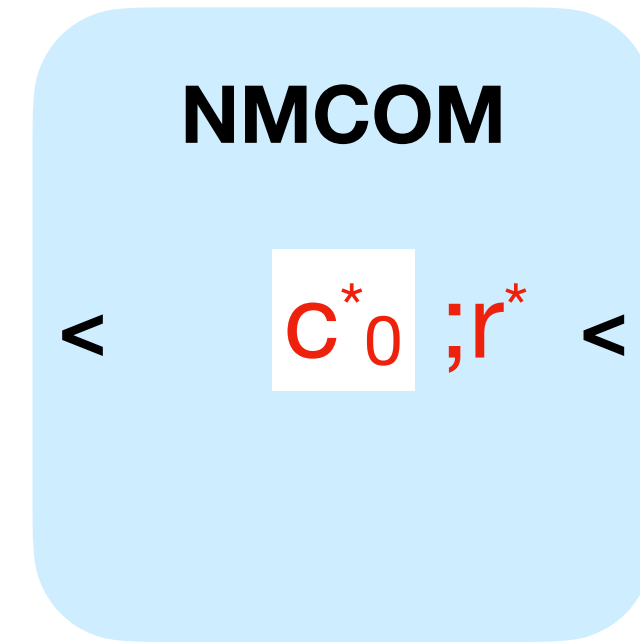
←  $C_0, r$

$z$  →

$x' \in L$

PoKExtractor( $x$ )

$a'$  →



$C^*_1$  →

←  $C^*_0, r^*$

$z^*$  →

$c' = c'_0 \oplus c'_1$

$V_\Sigma(x', a', c', z') = 1$

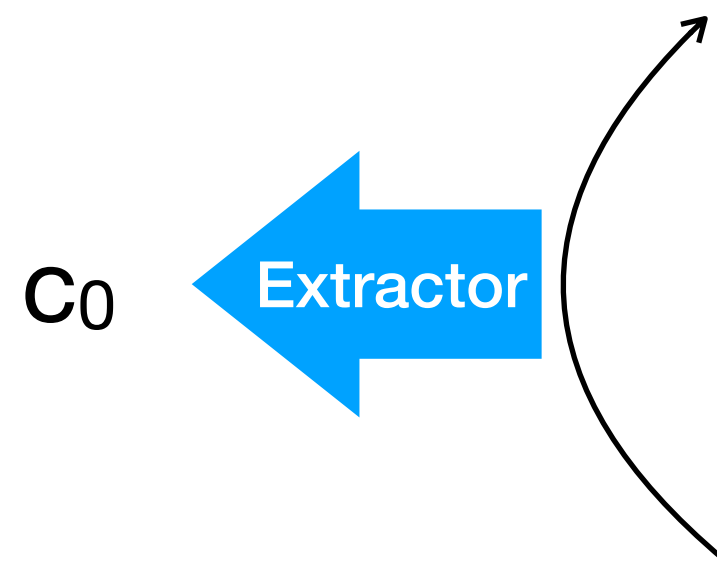
$x, a', c', z'$

# Non-Malleability

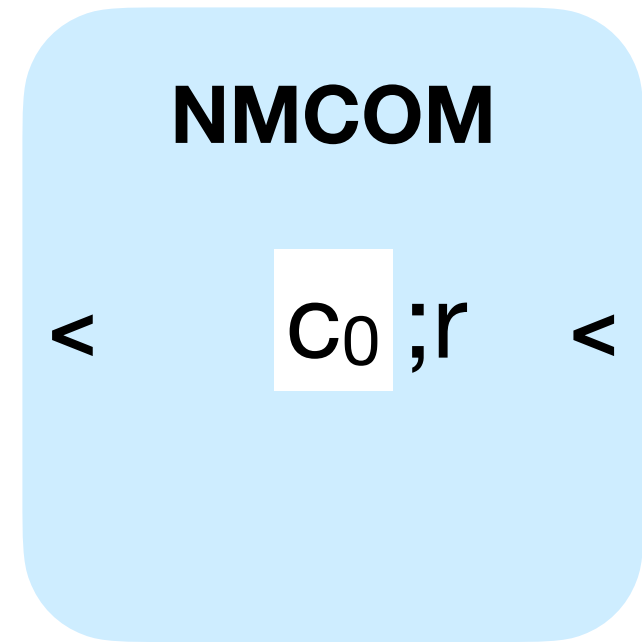
$x \in L$

*Sim*( $x$ )

$a, c, z \leftarrow \text{HVZK}_\Sigma(x)$



$a$  →



$C_1$  →

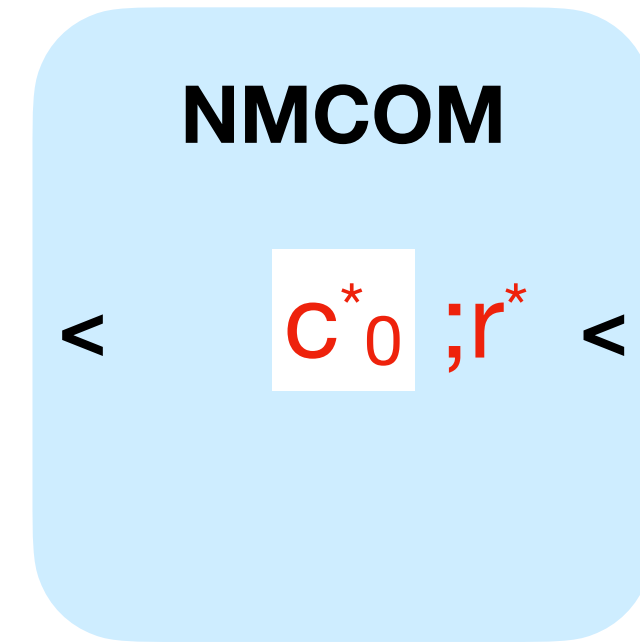
←  $C_0, r$

$z$  →

$x' \in L$

PoKExtractor( $x$ )

$a'$  →



$C^*_1$  →

←  $C^*_0, r^*$

$z^*$  →

$$c' = c'_0 \oplus c'_1$$

$$V_\Sigma(x', a', c', z') = 1$$

$$c^* = c^*_0 \oplus c^*_1$$

$$V_\Sigma(x', a', c^*, z^*) = 1$$

$x, a', c', z'$

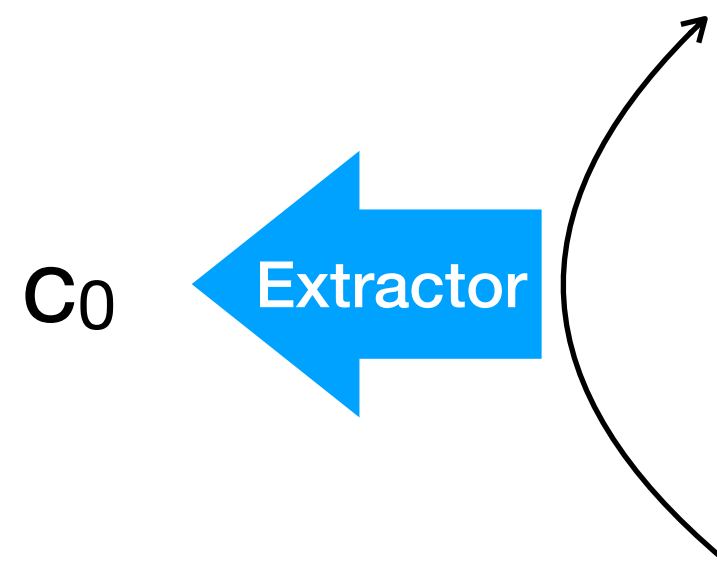


# Non-Malleability

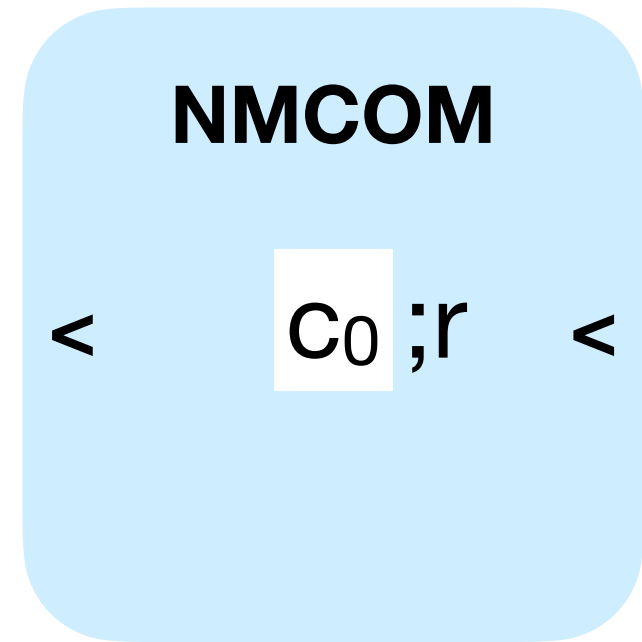
$x \in L$

*Sim*( $x$ )

$a, c, z \leftarrow \text{HVZK}_\Sigma(x)$



$a$



$c_1$

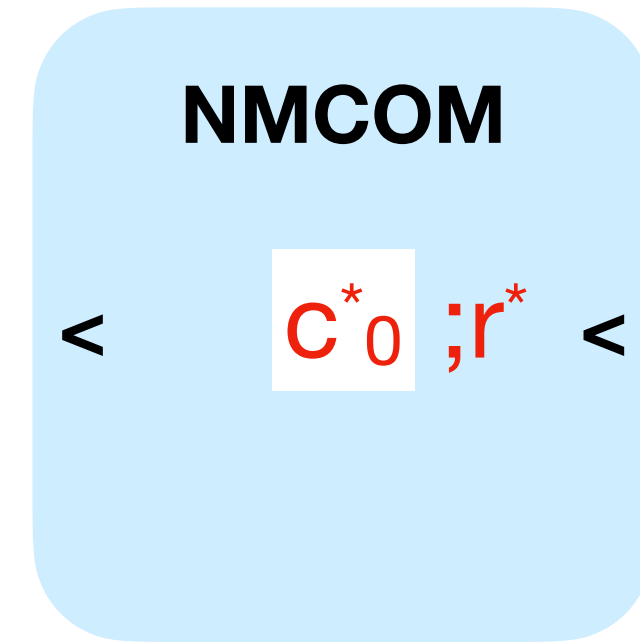
$c_0, r$

$z$

$x' \in L$

PoKExtractor( $x$ )

$a'$



$c^*_1$

$c^*_0, r^*$

$z^*$

$$c' = c'_0 \oplus c'_1$$

$$V_\Sigma(x', a', c', z') = 1$$

$$c^* = c^*_0 \oplus c^*_1$$

$$V_\Sigma(x', a', c^*, z^*) = 1$$

$x, a', c', z'$

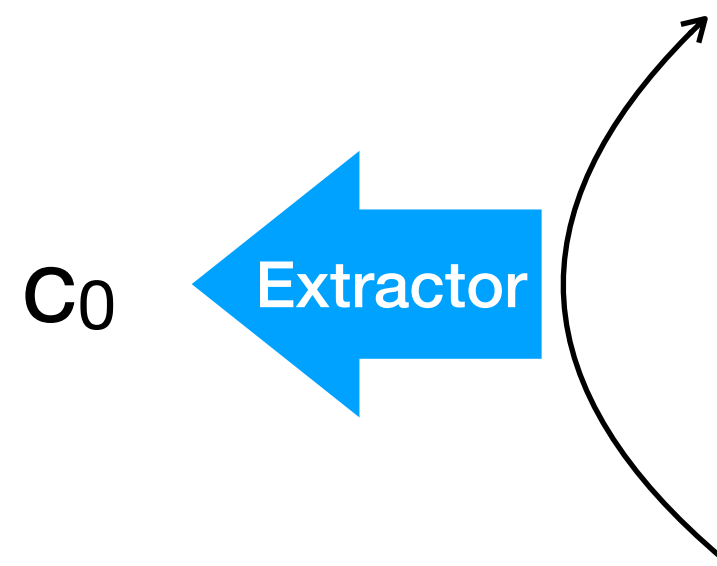
$x, a, c^*, z^*$

# Non-Malleability

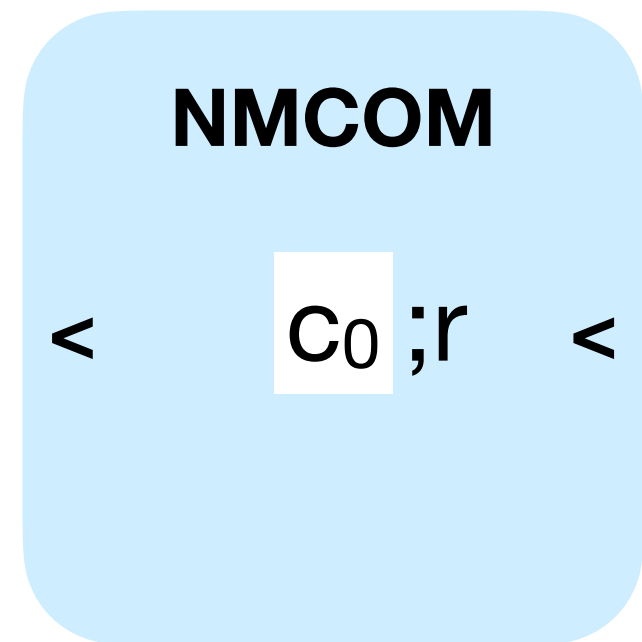
$\mathbf{x} \in L$

*Sim*( $\mathbf{x}$ )

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow \text{HVZK}_\Sigma(\mathbf{x})$



$\xrightarrow{\mathbf{a}}$



$\xrightarrow{C_1}$

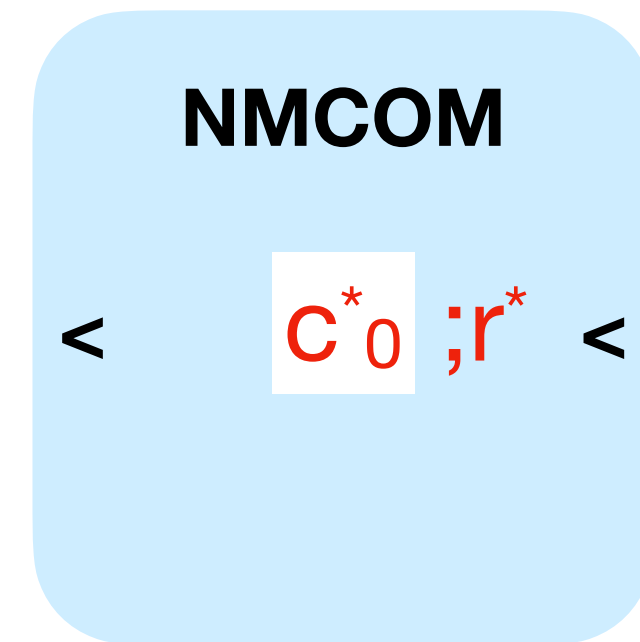
$\xleftarrow{C_0, r}$

$\xrightarrow{\mathbf{z}}$

$\mathbf{x}' \in L$

PoKExtractor( $\mathbf{x}$ )

$\xrightarrow{\mathbf{a}'}$



$\xrightarrow{C^*_1}$

$\xleftarrow{C^*_0, r^*}$

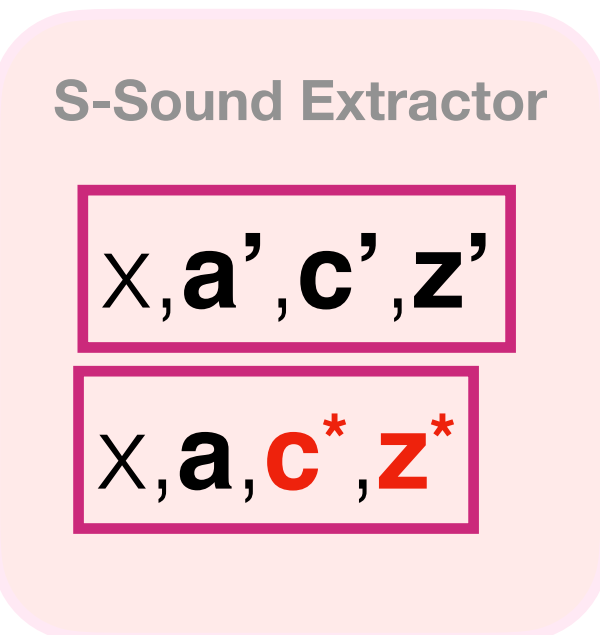
$\xrightarrow{\mathbf{z}'}$

$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$

$V_\Sigma(\mathbf{x}', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$

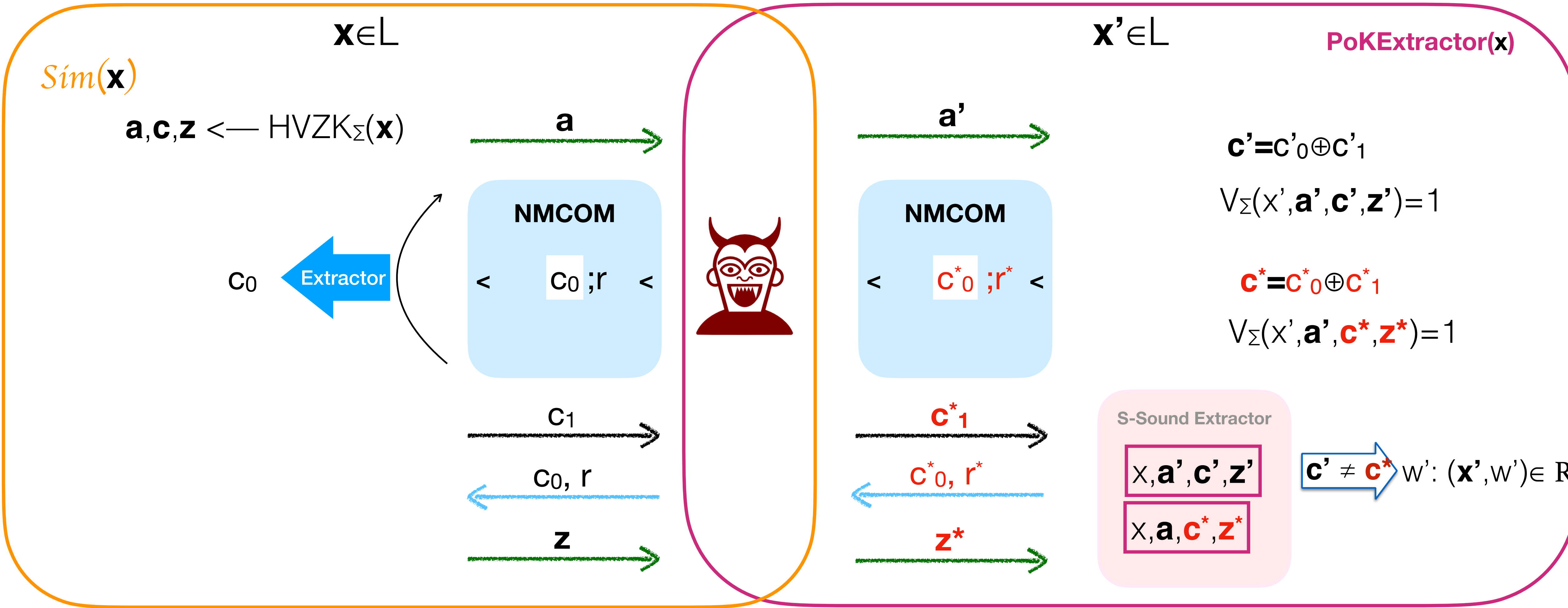
$\mathbf{c}^* = \mathbf{c}^*_0 \oplus \mathbf{c}^*_1$

$V_\Sigma(\mathbf{x}', \mathbf{a}', \mathbf{c}^*, \mathbf{z}^*) = 1$



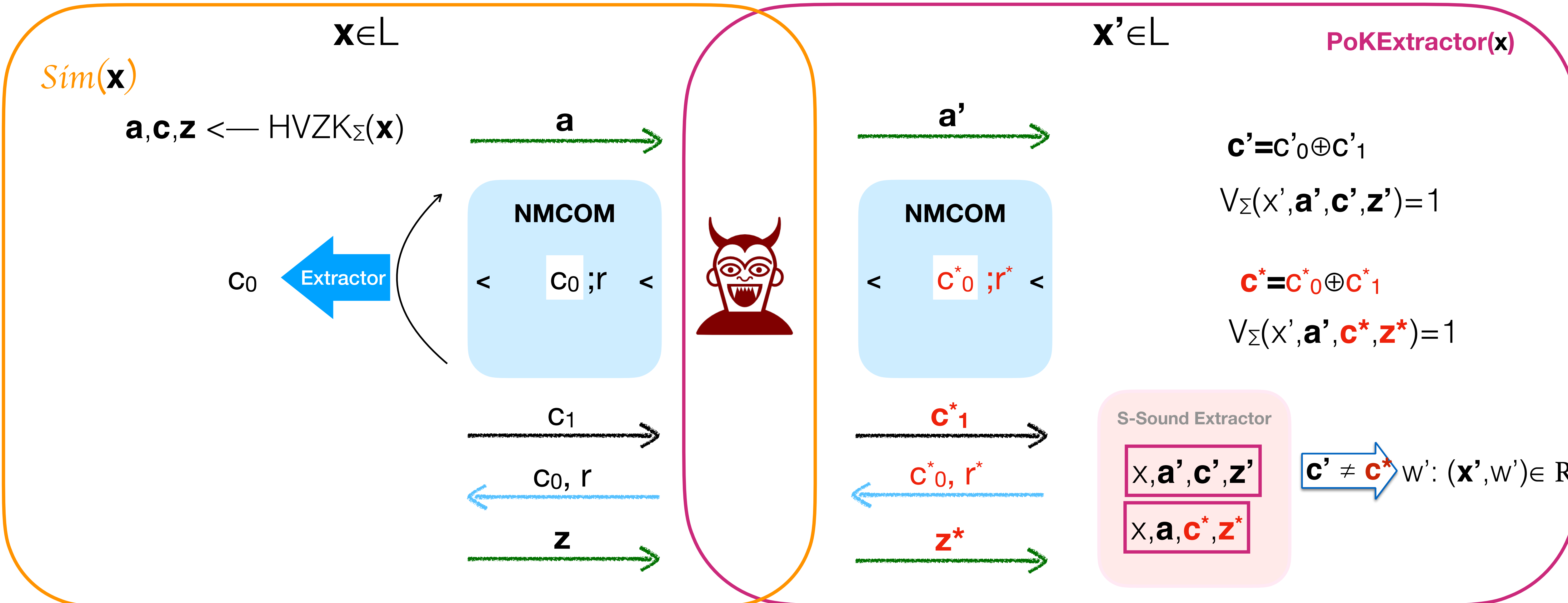
$\mathbf{c}' \neq \mathbf{c}^* \Rightarrow w': (\mathbf{x}', w') \in R$

# Non-Malleability



Hiding of NMCOM guarantees that  $c' \neq c^*$

# Non-Malleability

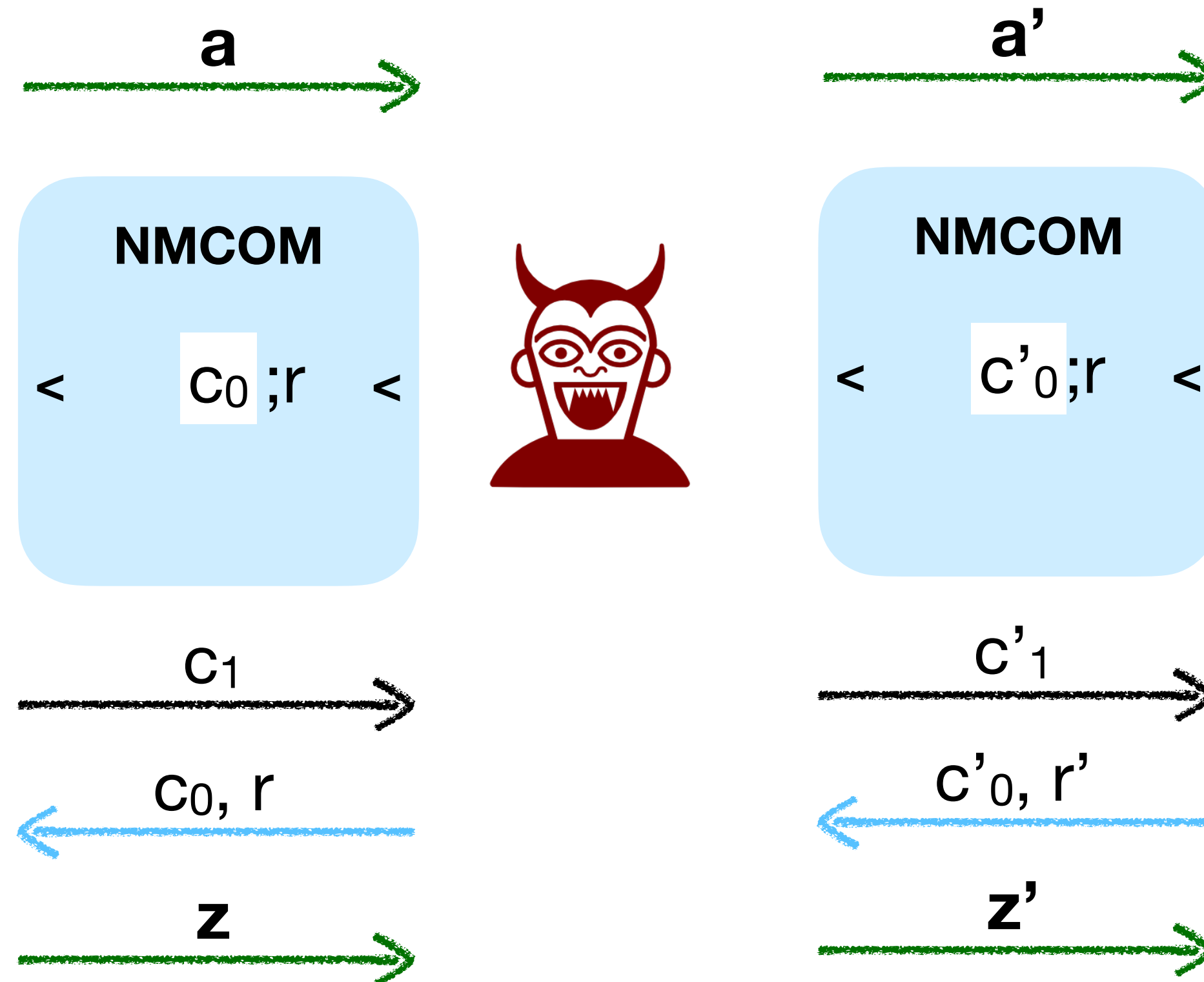
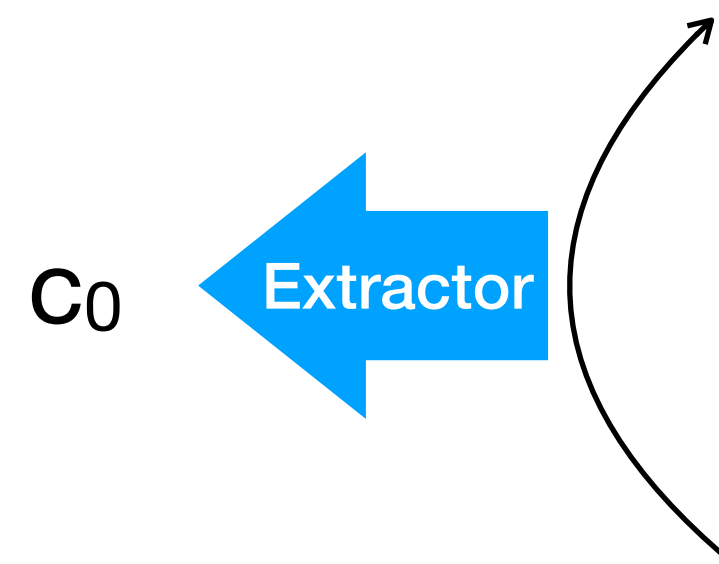


Hiding of NMCOM guarantees that  $c' \neq c^*$   
 But we are running the extractor of NMCOM!

# Reduction to non-malleability

$Sim(\mathbf{x})$

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow HVZK_{\Sigma}(\mathbf{x})$



$\mathbf{c}_1 = \mathbf{c}_0 \oplus \mathbf{c}$

If  $(c_0, r)$  is a valid opening

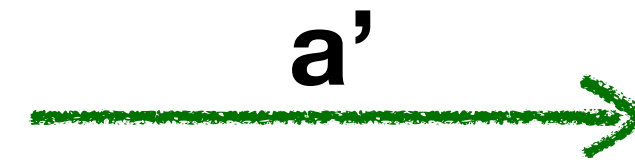
$$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$$

$$V_{\Sigma}(x', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$$

# Reduction to non-malleability

*Sim*(**x**)

**a, c, z**  $\leftarrow$  HVZK $_{\Sigma}$ (**x**)



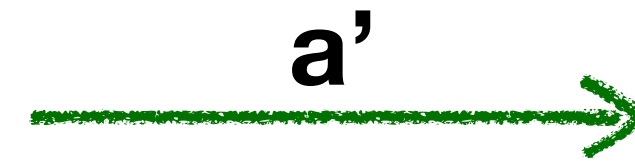
$$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$$

$$V_{\Sigma}(x', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$$

# Reduction to non-malleability

*Sim*(**x**)

**a, c, z**  $\leftarrow$  HVZK $_{\Sigma}$ (**x**)



Challenge messages

( $m_0, m_1$ )

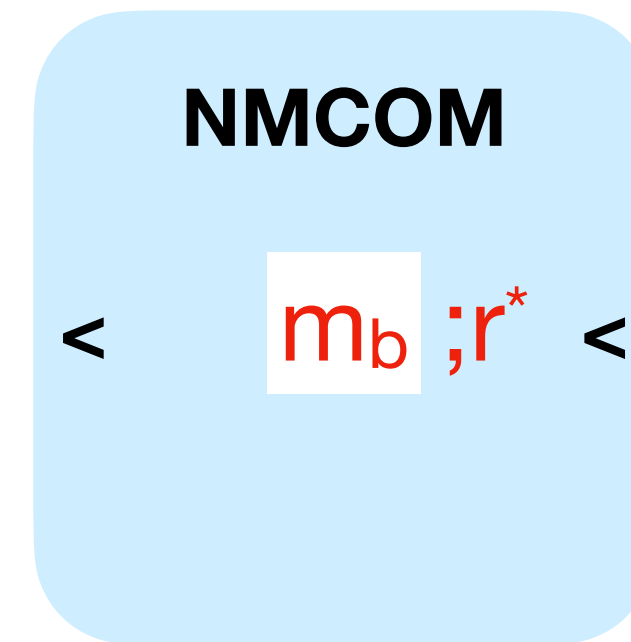
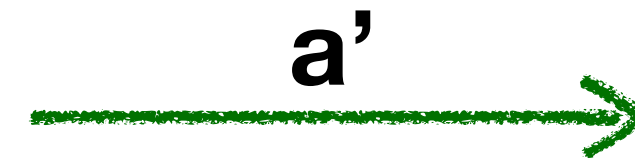
$$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$$

$$V_{\Sigma}(x', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$$

# Reduction to non-malleability

$Sim(\mathbf{x})$

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow HVZK_{\Sigma}(\mathbf{x})$



Challenge messages

$(m_0, m_1)$

$$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$$

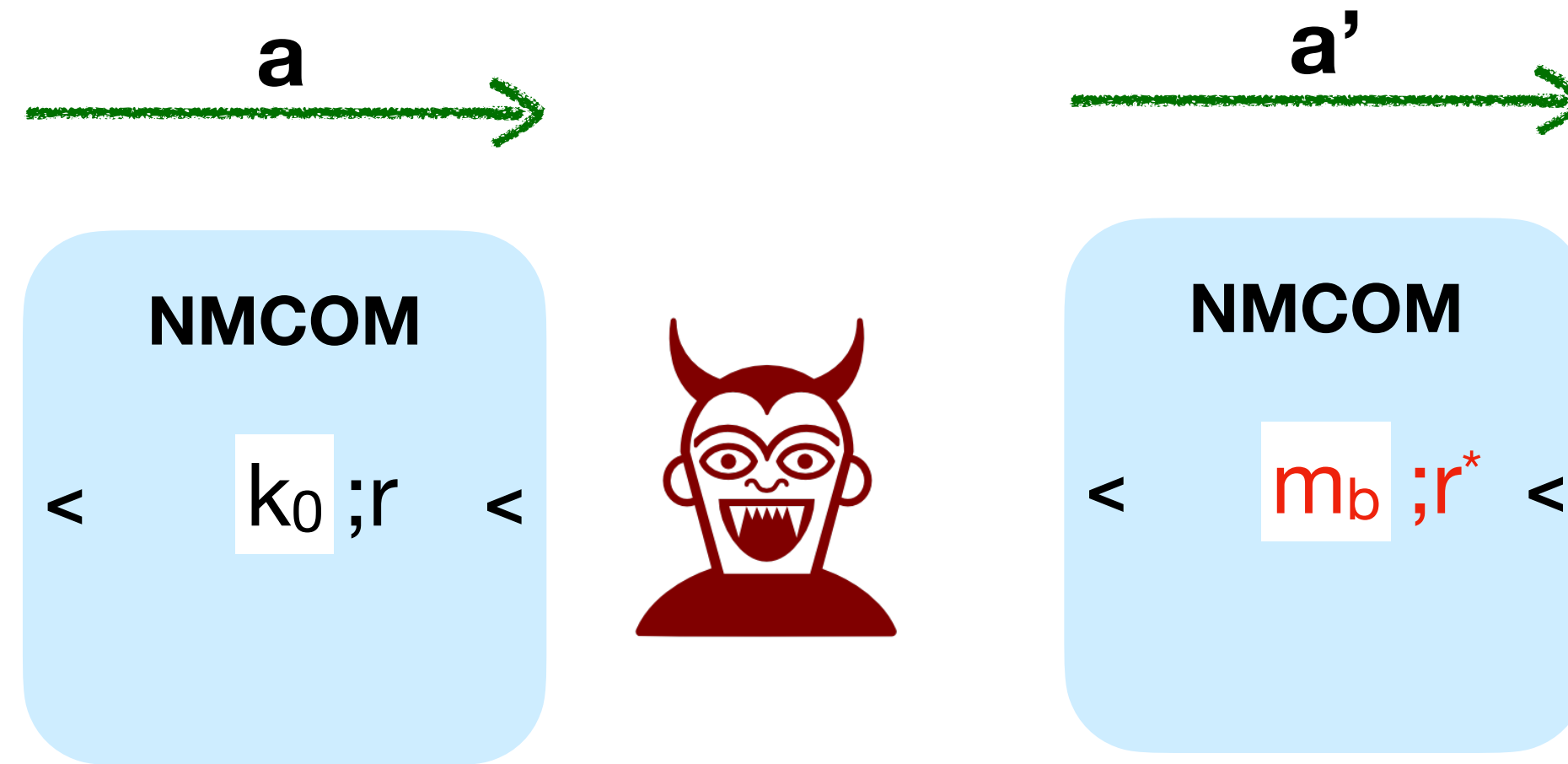
$$V_{\Sigma}(x', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$$



# Reduction to non-malleability

$Sim(\mathbf{x})$

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow HVZK_{\Sigma}(\mathbf{x})$



Challenge messages

$(m_0, m_1)$

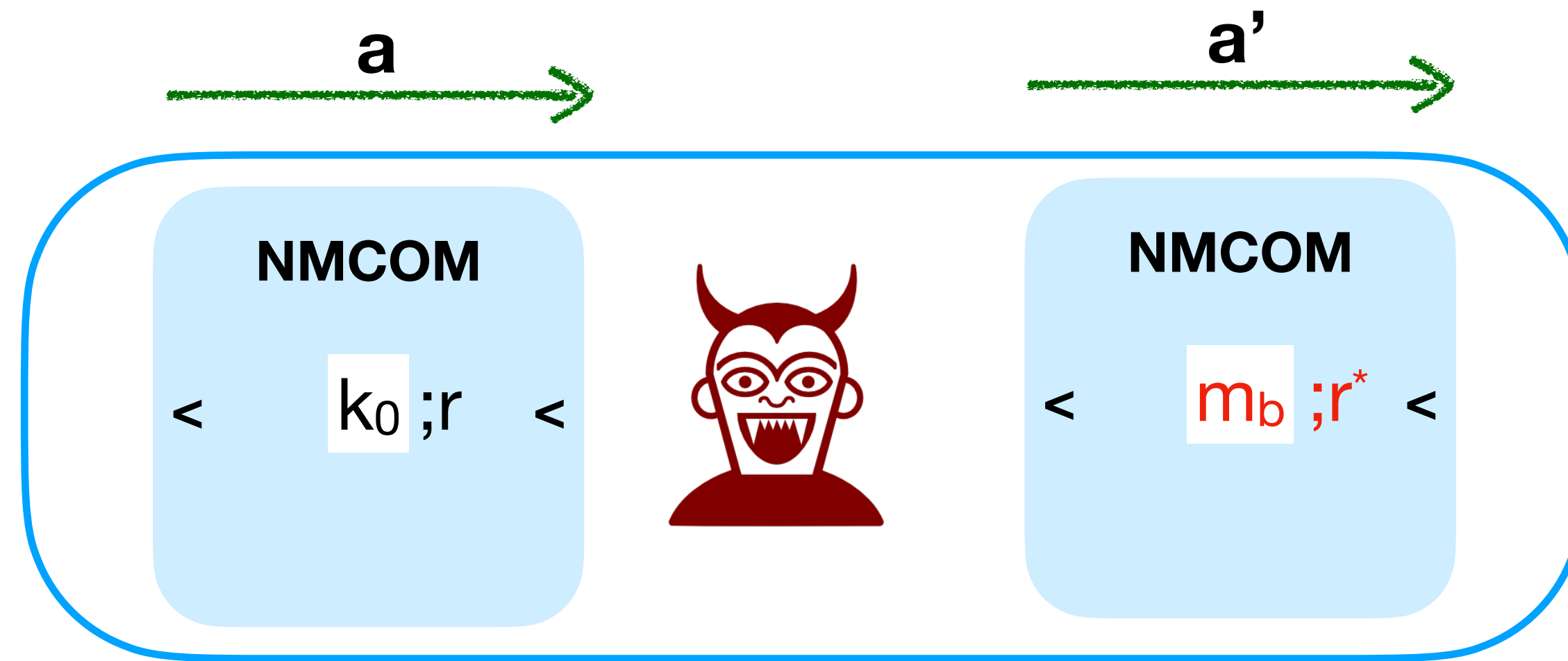
$$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$$

$$V_{\Sigma}(x', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$$

# Reduction to non-malleability

$Sim(\mathbf{x})$

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow HVZK_{\Sigma}(\mathbf{x})$



Challenge messages

$(m_0, m_1)$

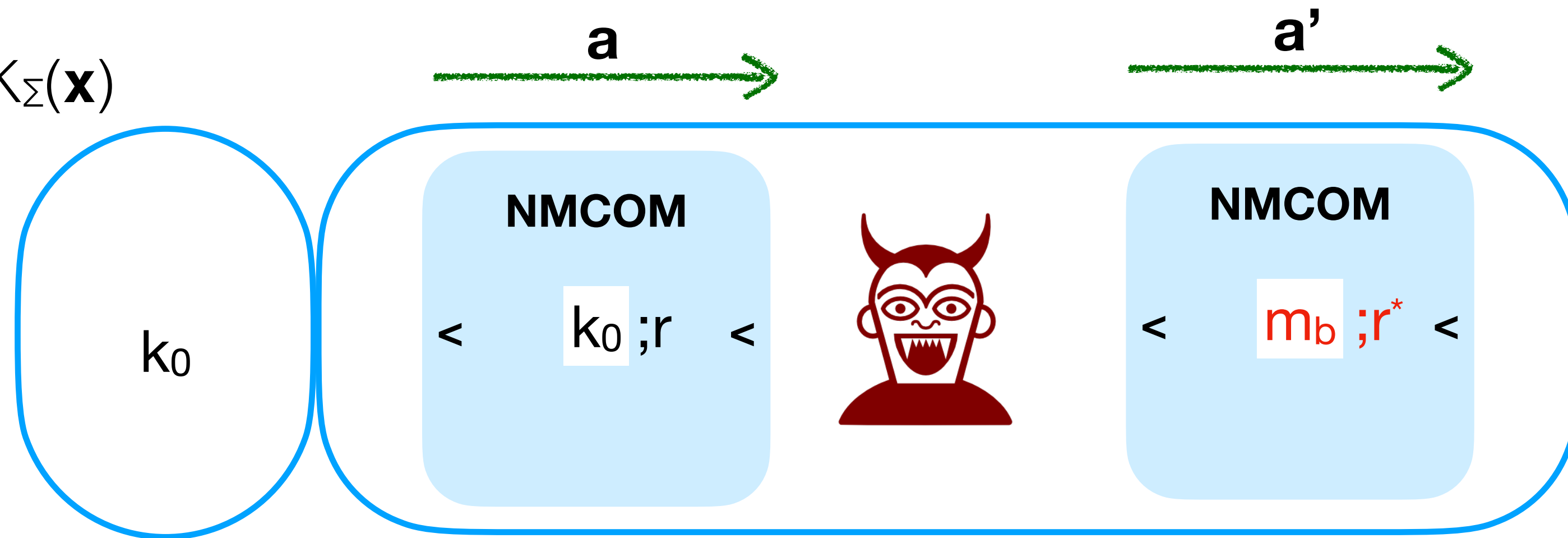
$$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$$

$$V_{\Sigma}(x', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$$

# Reduction to non-malleability

$Sim(\mathbf{x})$

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow HVZK_{\Sigma}(\mathbf{x})$



Challenge messages

$(m_0, m_1)$

$$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$$

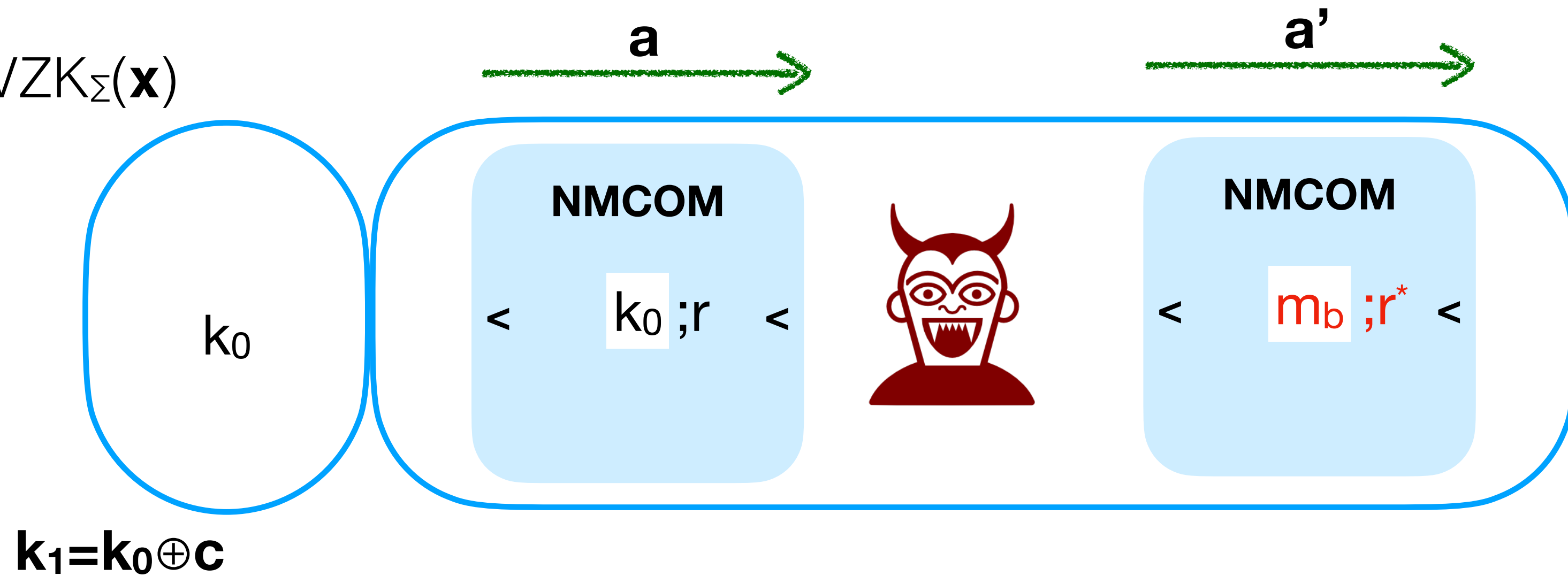
$$V_{\Sigma}(x', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$$

$k_0$  is an input to the distinguisher

# Reduction to non-malleability

*Sim*(**x**)

**a, c, z**  $\leftarrow$  HVZK $_{\Sigma}$ (**x**)



Challenge messages

$(m_0, m_1)$

$$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$$

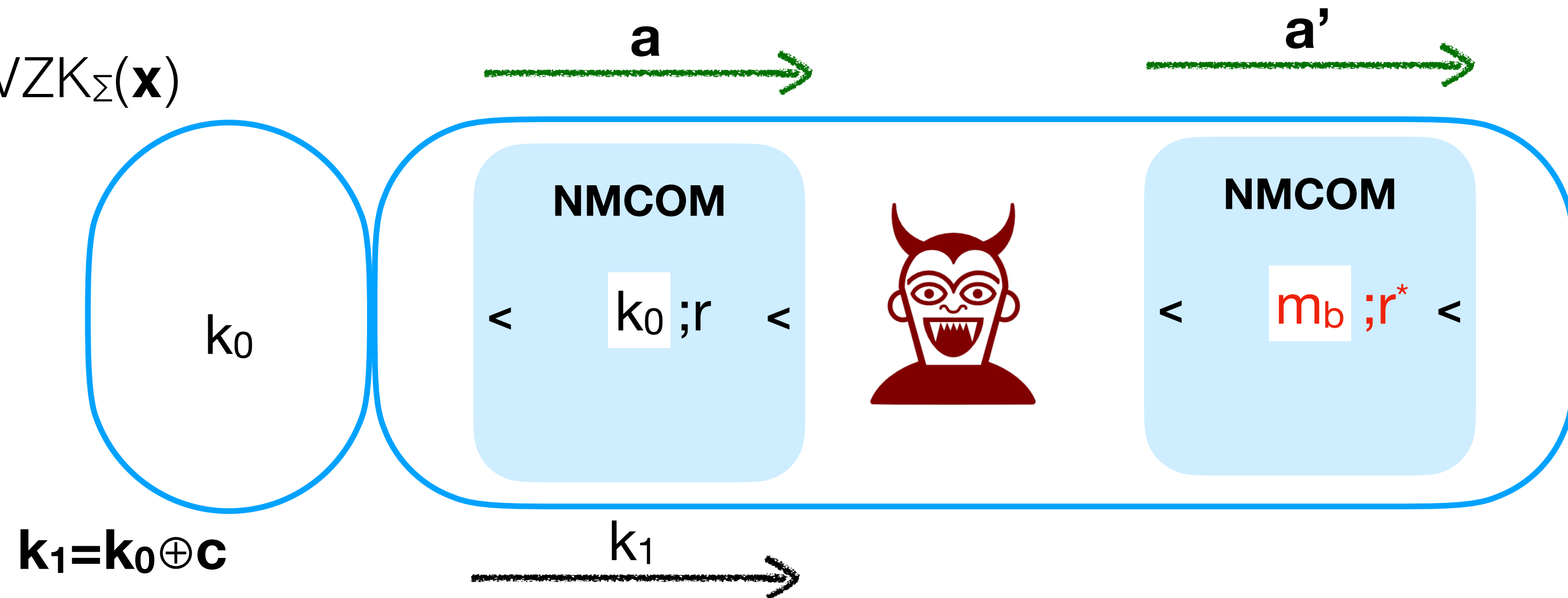
$$V_{\Sigma}(x', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$$

$k_0$  is an input to the distinguisher

# Reduction to non-malleability

$Sim(\mathbf{x})$

$\mathbf{a}, \mathbf{c}, \mathbf{z} \leftarrow HVZK_{\Sigma}(\mathbf{x})$



Challenge messages

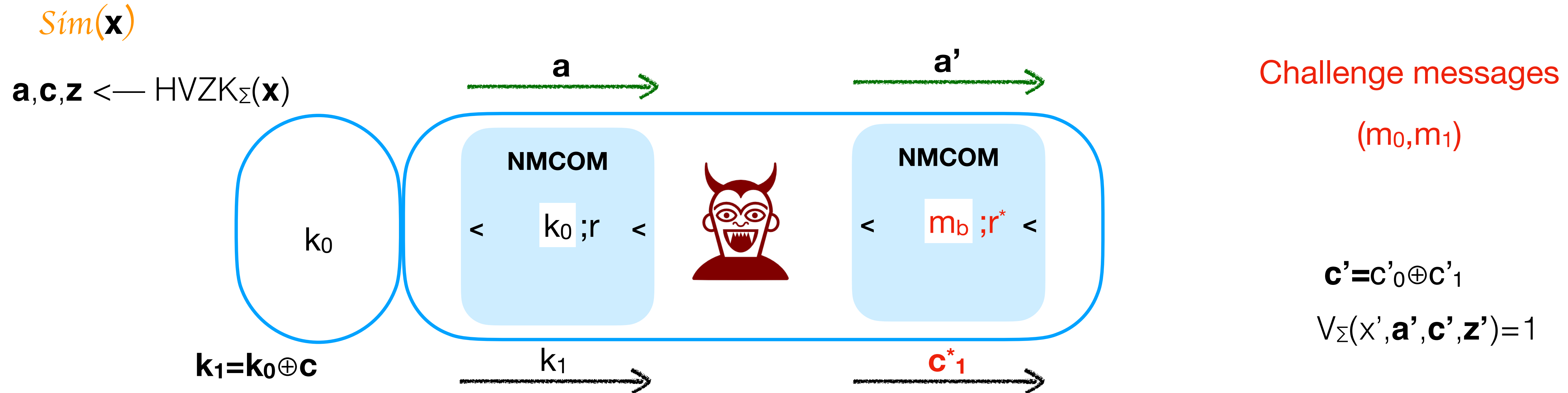
$(m_0, m_1)$

$$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$$

$$V_{\Sigma}(x', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$$

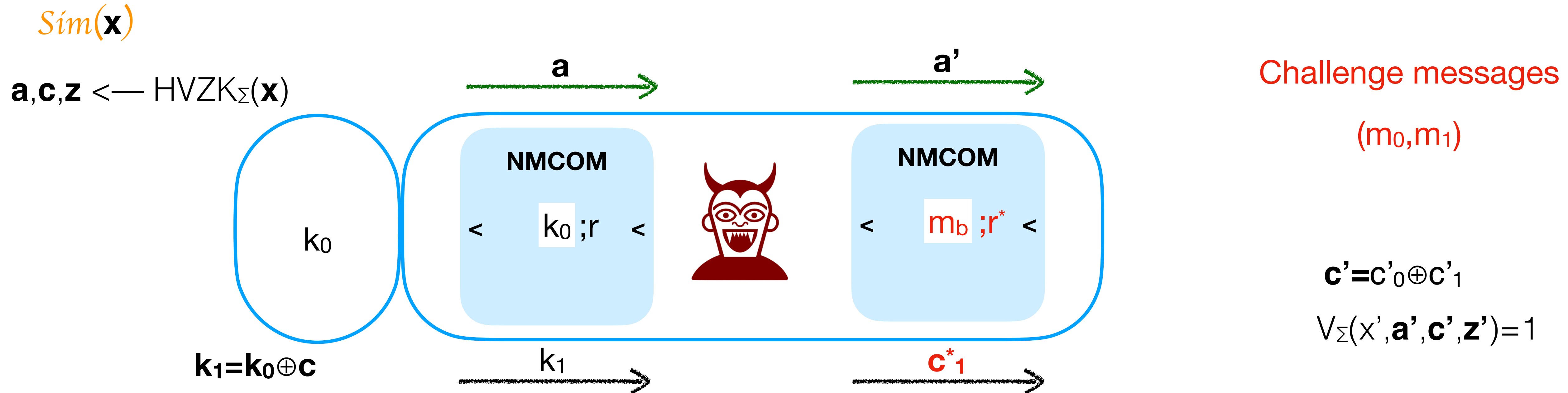
$k_0$  is an input to the distinguisher

# Reduction to non-malleability



$\mathbf{k}_0$  is an input to the distinguisher

# Reduction to non-malleability



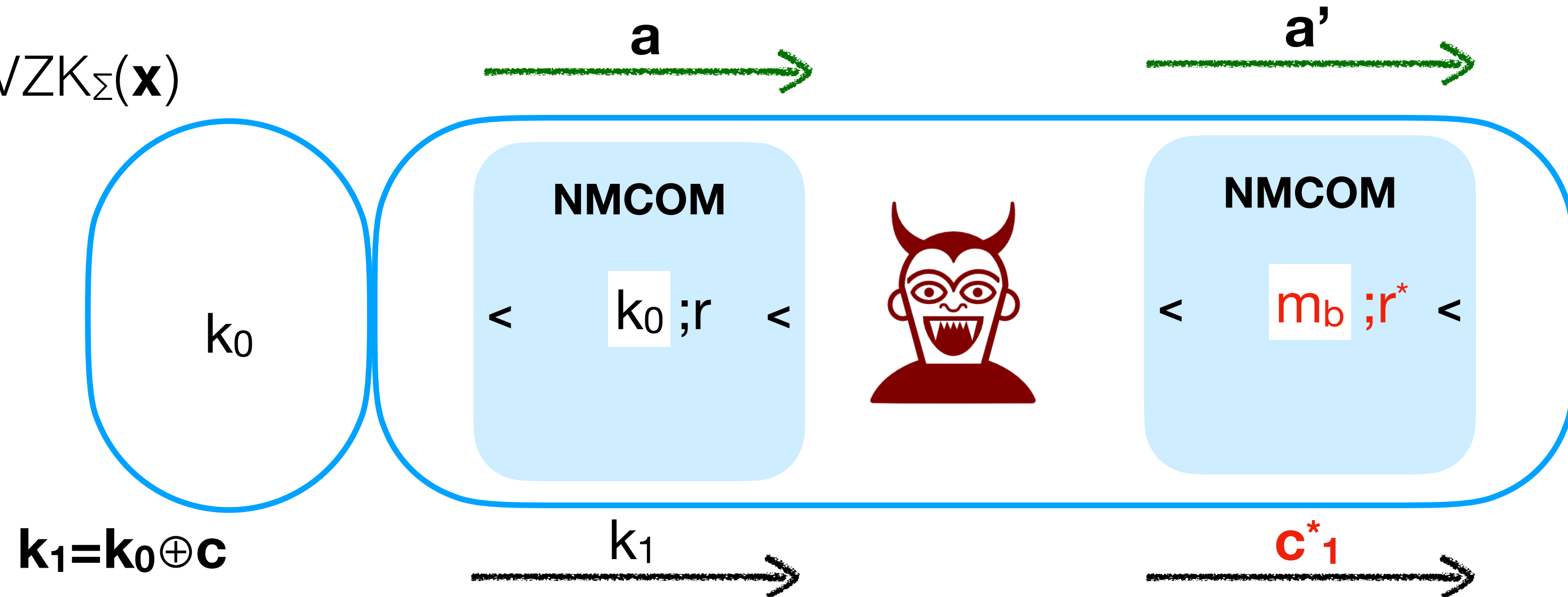
$k_0$  is an input to the distinguisher

With high probability  $\mathbf{c}' = \mathbf{c}^* \rightarrow$

# Reduction to non-malleability

*Sim*(**x**)

**a, c, z**  $\leftarrow$  HVZK $_{\Sigma}$ (**x**)



Challenge messages

( $m_0, m_1$ )

$$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$$

$$V_{\Sigma}(x', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$$

$k_0$  is an input to the distinguisher

With high probability  $\mathbf{c}' = \mathbf{c}^* \rightarrow$

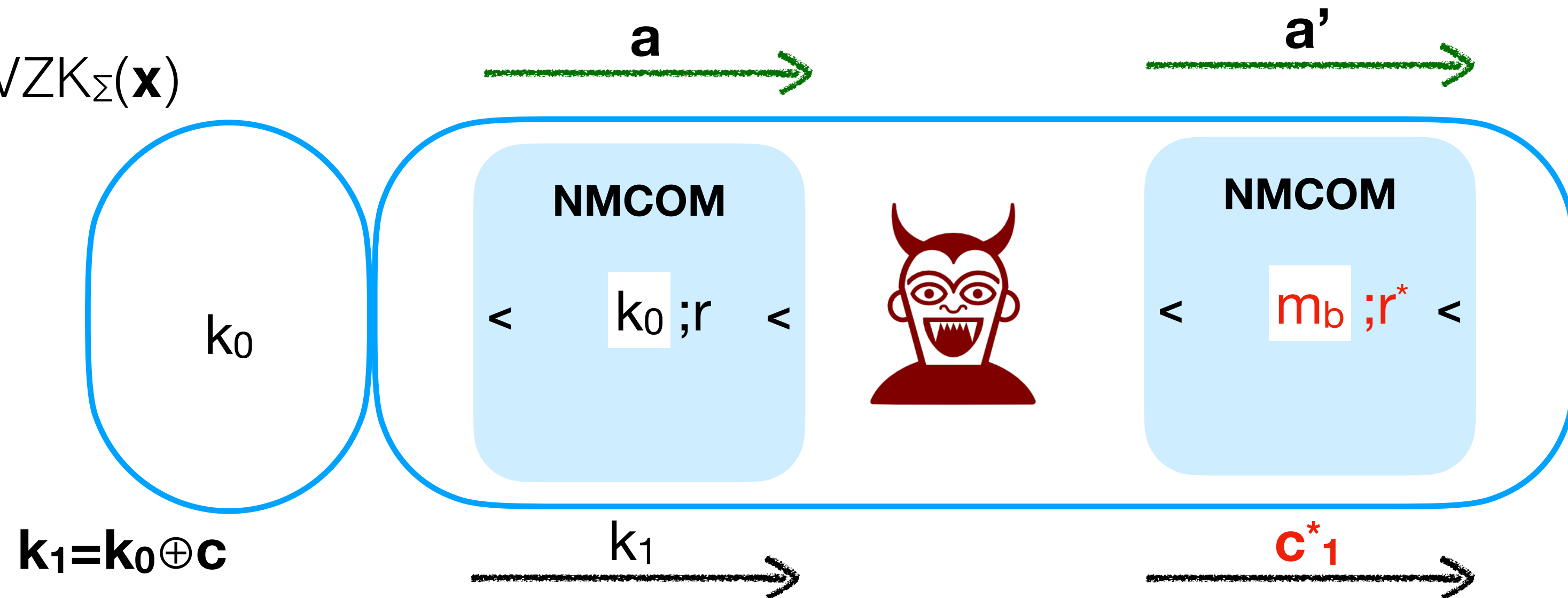
$$\mathbf{c}'_0 \oplus \mathbf{c}'_1 = \mathbf{c}' = \mathbf{c}^* = m_b \oplus \mathbf{c}^*_1 \rightarrow$$



# Reduction to non-malleability

*Sim*(**x**)

**a, c, z**  $\leftarrow$  HVZK $_{\Sigma}$ (**x**)



Challenge messages

( $m_0, m_1$ )

$$\mathbf{c}' = \mathbf{c}'_0 \oplus \mathbf{c}'_1$$

$$V_{\Sigma}(x', \mathbf{a}', \mathbf{c}', \mathbf{z}') = 1$$

$k_0$  is an input to the distinguisher

With high probability  $\mathbf{c}' = \mathbf{c}^* \rightarrow$

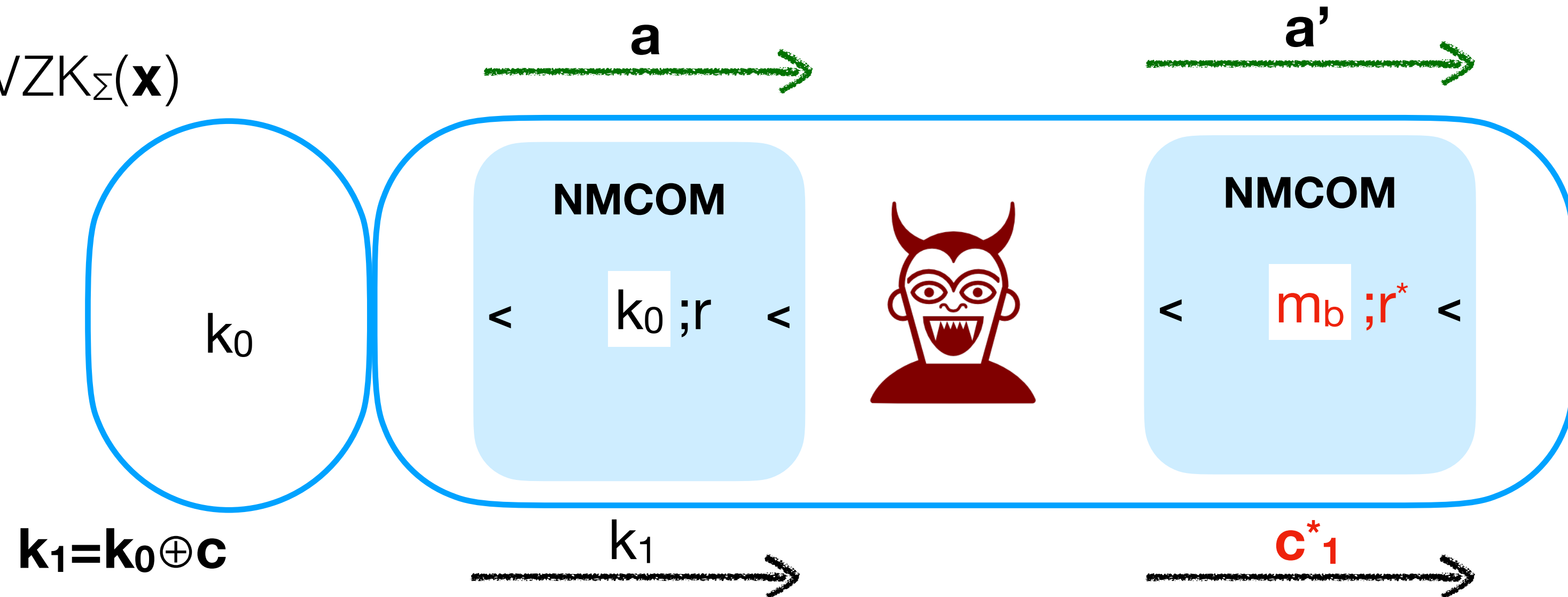
$$\mathbf{c}'_0 \oplus \mathbf{c}'_1 = \mathbf{c}' = \mathbf{c}^* = m_b \oplus \mathbf{c}^*_1 \rightarrow$$

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# Reduction to non-malleability

*Sim*(**x**)

**a, c, z**  $\leftarrow$  HVZK $_{\Sigma}$ (**x**)



Challenge messages

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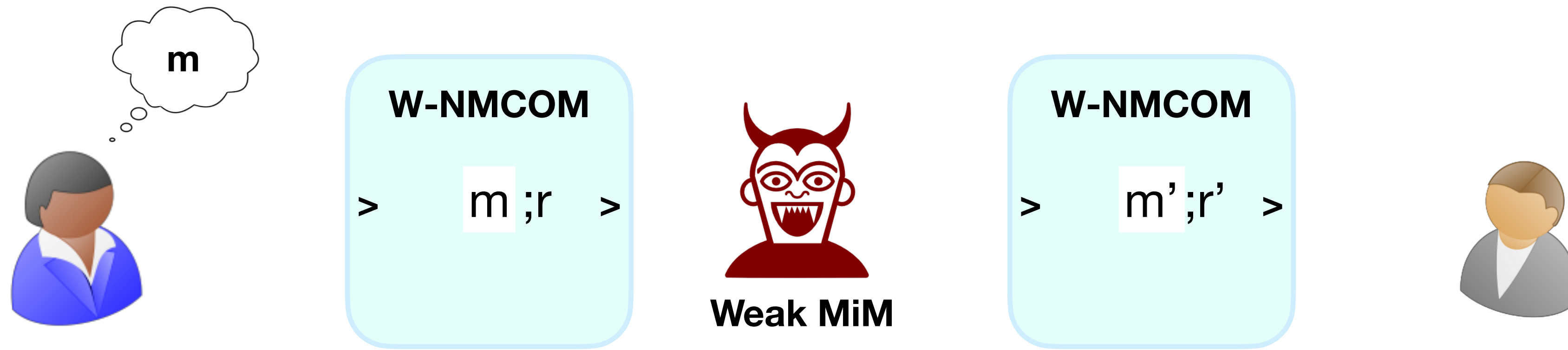
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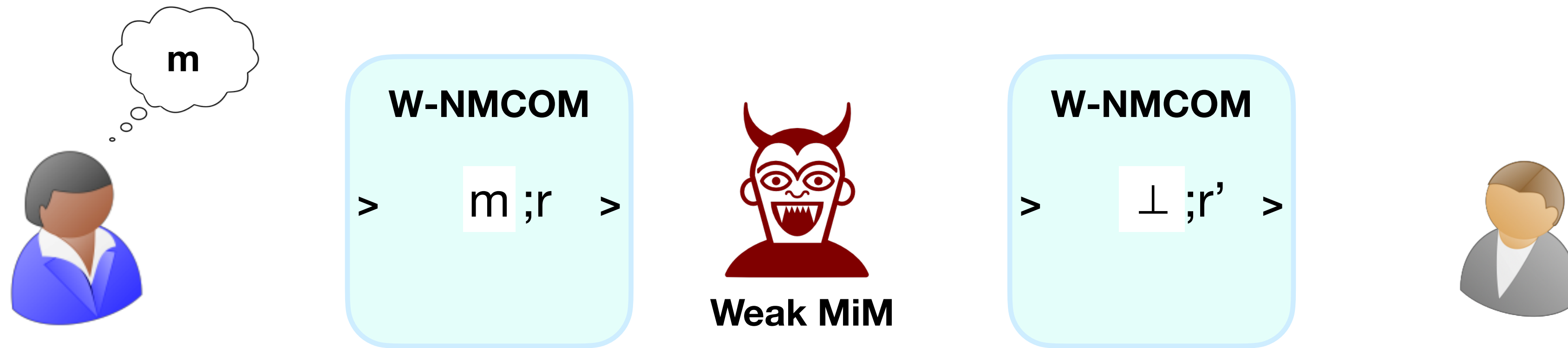
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$$m_b = \mathbf{c}'_0 \oplus \mathbf{c}'_1 \oplus \mathbf{c}^*_1$$

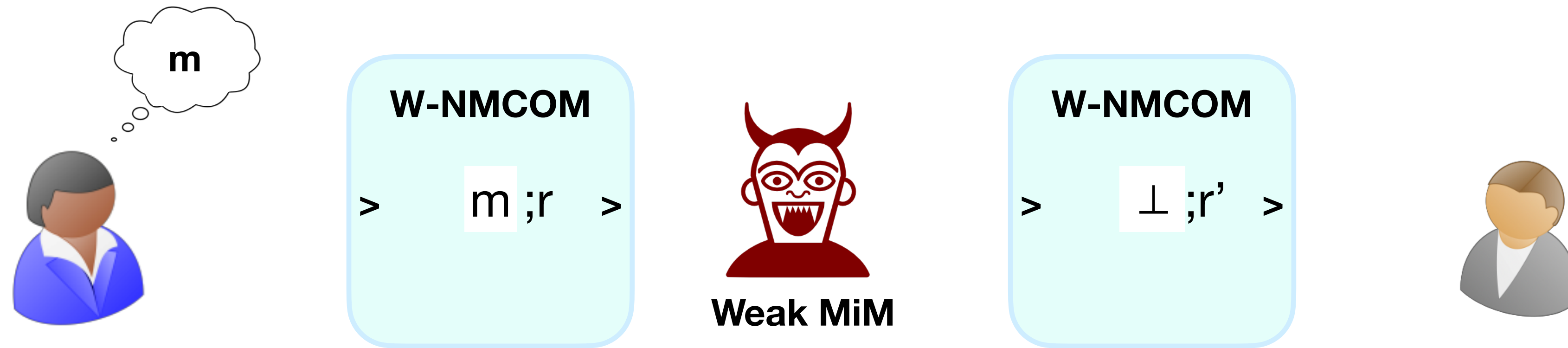
# Weak Non-Malleable Commitments



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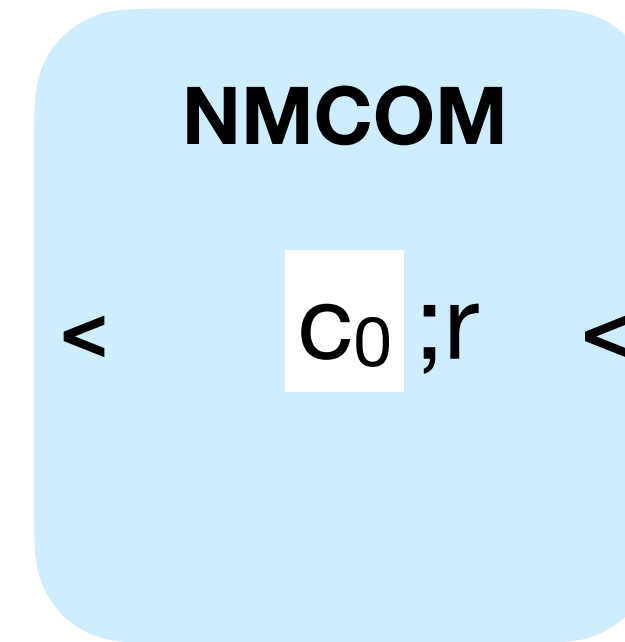
[BGR+15] Hai Brenner, Vipul Goyal, Silas Richelson, Alon Rosen, and Margarita Vald. Fast non-malleable commitments. CCS 2015

[GRRV14] Vipul Goyal, Silas Richelson, Alon Rosen, and Margarita Vald. FOCS 2014

# Weak non-malleability may suffice



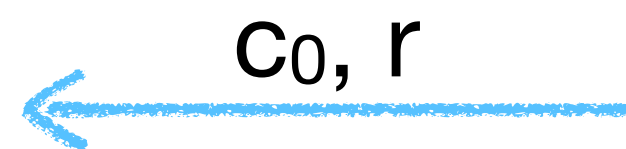
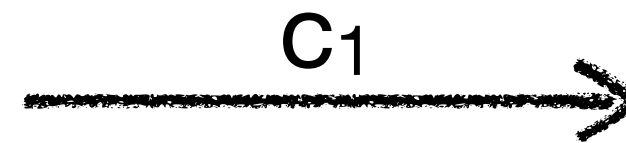
$$\mathbf{a} \leftarrow P_{\Sigma}(x, w)$$



If  $(c_0, r)$  is a valid opening

$$\mathbf{c} = \mathbf{c}_0 \oplus \mathbf{c}_1$$

$$z \leftarrow P_{\Sigma}(x, w, \mathbf{c})$$

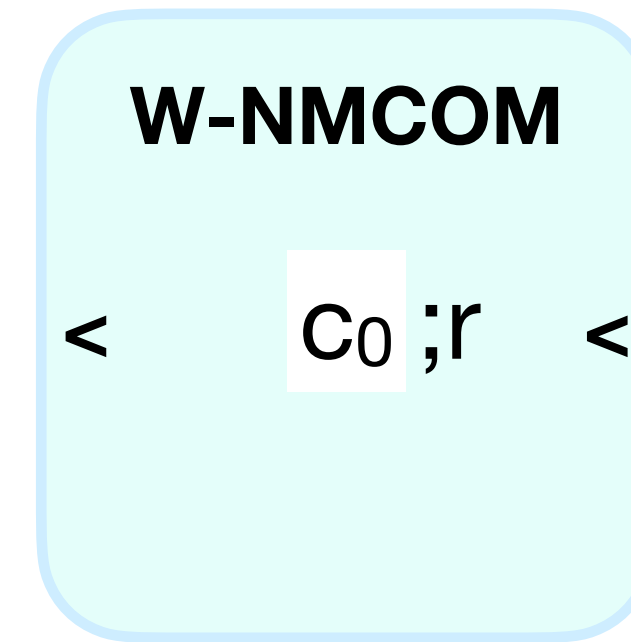


$$V_{\Sigma}(x, a, c, z) = 1$$

# Weak non-malleability may suffice



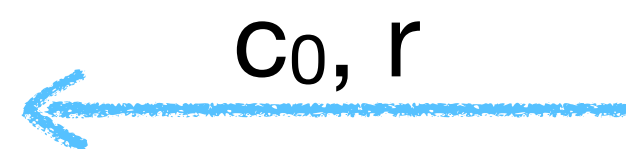
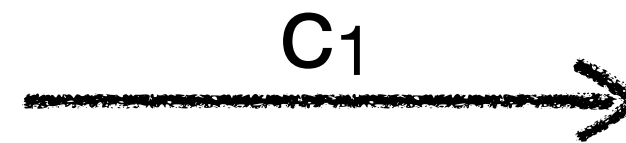
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[GMO16] Irene Giacomelli, Jesper Madsen, and Claudio Orlandi. ZKBoo: Faster zero-knowledge for Boolean circuits. USENIX 2016

[CDG+17] Melissa Chase, David Derler, Steven Goldfeder, Claudio Orlandi, Sebastian Ramacher, Christian Rechberger, Daniel Slamanig, and Greg Zaverucha. Post-quantum zero-knowledge and signatures from symmetric-key primitives. CCS 2017

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- Adaptive input, parallel/concurrent composition

[GMO16] Irene Giacomelli, Jesper Madsen, and Claudio Orlandi. ZKBoo: Faster zero-knowledge for Boolean circuits. USENIX 2016

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Thanks