



上海交通大學

SHANGHAI JIAO TONG UNIVERSITY

More Efficient Public-Key Cryptography with Leakage and Tamper Resilience

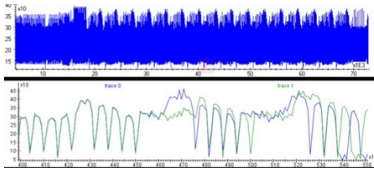
Shuai Han, Shengli Liu, Dawu Gu

Shanghai Jiao Tong University

PKC 2024, Sydney, Australia



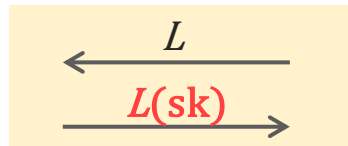
Key Leakage



Side-Channel Attacks

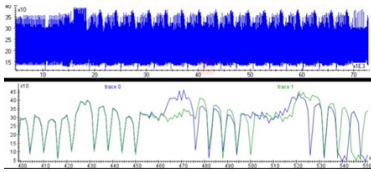
- Power
- Time
- Sound
- ...

Passive attacks



Key Leakages

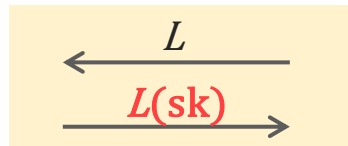
Key Leakage



Side-Channel Attacks

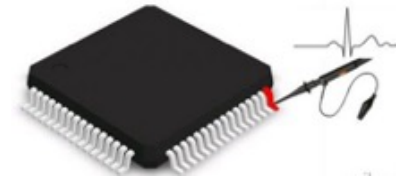
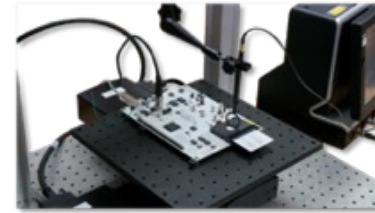
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Passive attacks



Key Leakages

Key Tampering

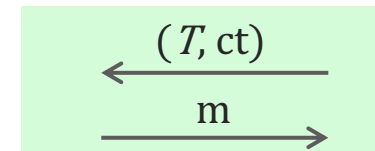


- Fault injection
- Memory tampering
- ...

Active attacks

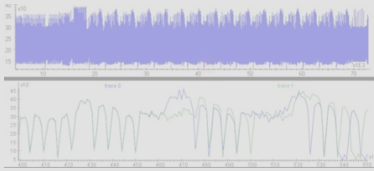


$$m \leftarrow \text{Dec}(T(sk), ct)$$



Operating under **Tampered keys**

Key Leakage

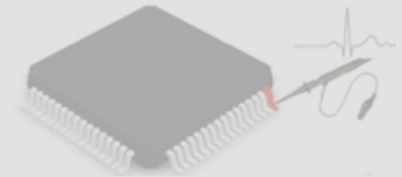
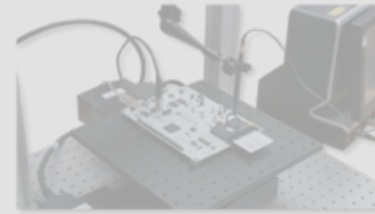


Side-Channel Attacks

- Power
- Time
- Sound
- ...

Passive attacks

Key Tampering



- Fault injection
- Memory tampering
- ...

Active attacks

How to achieve security resilient to both **Leakage & **Tampering** attacks?**

① CTL model (Continual Tampering & Leakage)

[Kalai et al., C11]

- + **Strong** security guarantee: **Continual** tampering & leakage attacks
- Require **additional mechanisms**: Key-updating or Self-destruct

Schemes	Efficiency
SIG [Kalai et al., C11]	signature > 20 group elements
CCA-PKE [Fujisaki-Xagawa, AC16]	ciphertext > 8 group elements

- Rely on **heavy tools**:

tSE-NIZK (true-Simulation Extractable NIZK)

[Dodis et al., AC10]

or OT-LF (One-Time Lossy Filter)

[Qin-Liu, AC13]

② BLT model (Bounded Leakage & Tampering)

[Damgård et al., AC13]

- **Mild** security guarantee:

- **Leakage:** Bounded amount

[Naor-Segev, C09]

- **Tampering:** Bounded number, No post-challenge, Arbitrary functions

+ **No additional mechanisms**

Schemes	Efficiency
SIG [Faonio-Venturi, AC16] [Dodis et al., AC10]	signature > 34 group elements
CCA-PKE [Faonio-Venturi, AC16] [Qin-Liu, AC13]	ciphertext > 19 group elements

- Rely on **heavy tools:** tSE-NIZK or OT-LF

③ sLTR model (strong Leakage & Tampering-Resilience) [Sun et al., ACNS19]

- **Mild** security guarantee:
 - **Leakage:** Bounded amount [Naor-Segev, C09]
 - **Tampering:** Unbounded number, Allow post-challenge tampering,
For specific functions (e.g., $\mathcal{T}_{\text{affine}}$) [Bellare-Kohno, EC03]

+ No additional mechanisms

Schemes	Efficiency
CCA-PKE [Sun et al., ACNS19]	$ \text{ciphertext} > 20$ group elements

- Rely on heavy tools: tSE-NIZK

④ pcBLT model (post-challenge BLT)

[Chakraborty-Rangan, CT-RSA19]

- **Mild** security guarantee:
 - **Leakage:** Bounded amount
 - **Tampering:** Bounded number, Allow post-challenge tampering,
For arbitrary functions
- Require **additional mechanisms:** Split-state

Schemes	Efficiency
CCA-PKE [Chakraborty-Rangan, CT-RSA19]	$ \text{ciphertext} > 20$ group elements

- Rely on **heavy tools:** tSE-NIZK

Security Resilient to Both Leakage & Tampering Attacks



Schemes	Efficiency	Model
SIG [Kalai et al., C11]	signature > 20 group elements	CTL
CCA-PKE [Fujisaki-Xagawa, AC16]	ciphertext > 8 group elements	CTL
SIG [Faonio-Venturi, AC16] [Dodis et al., AC10]	signature > 34 group elements	BLT
CCA-PKE [Faonio-Venturi, AC16] [Qin-Liu, AC13]	ciphertext > 19 group elements	BLT
CCA-PKE [Sun et al., ACNS19]	ciphertext > 20 group elements	sLTR
CCA-PKE [Chakraborty-Rangan, CT-RSA19]	ciphertext > 20 group elements	pcBLT

All rely on somewhat **heavy tools** like tSE-NIZK or OT-LF!

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All rely on somewhat **heavy tools** like tSE-NIZK or OT-LF!



How to achieve security resilient to both Leakage & Tampering attacks, More efficiently?

Contributions: More Efficient SIG and CCA-PKE in the LTR Setting



Schemes	Efficiency	Model
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CCA-PKE [Chakraborty-Rangan, CT-RSA19]	ciphertext > 20 group elements	pcBLT
Our SIG	signature = 4 group elements	sLTR
Our CCA-PKE	ciphertext = 6 group elements	sLTR

5~8x shorter

1.3~3.3x shorter

Schemes	Efficiency	Model
Our SIG	signature = 4 group elements	sLTR
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Features

- **Direct** construction over asymmetric pairing groups
- Based on the standard MDDH (including SXDH, k-Linear) assumptions
- In the standard model
- **Leakage** rate: $1/4 - o(1)$ (our SIG) or $1/3 - o(1)$ (our CCA-PKE)
- **Tampering** functions: **affine functions** $\mathcal{T}_{\text{affine}}$

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sLTR Security Model

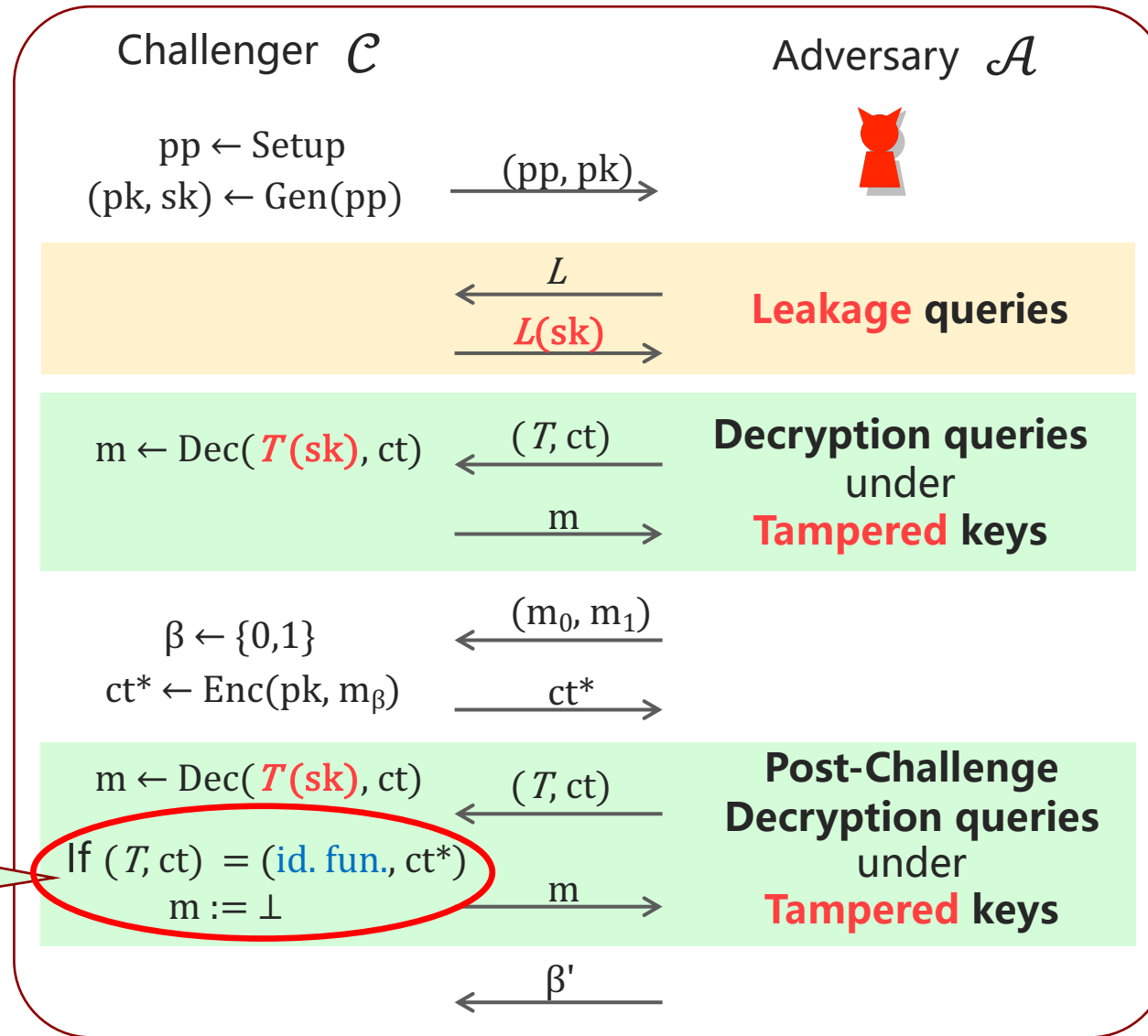
02 -

Our SIG Construction

03 -

Our CCA-PKE Construction

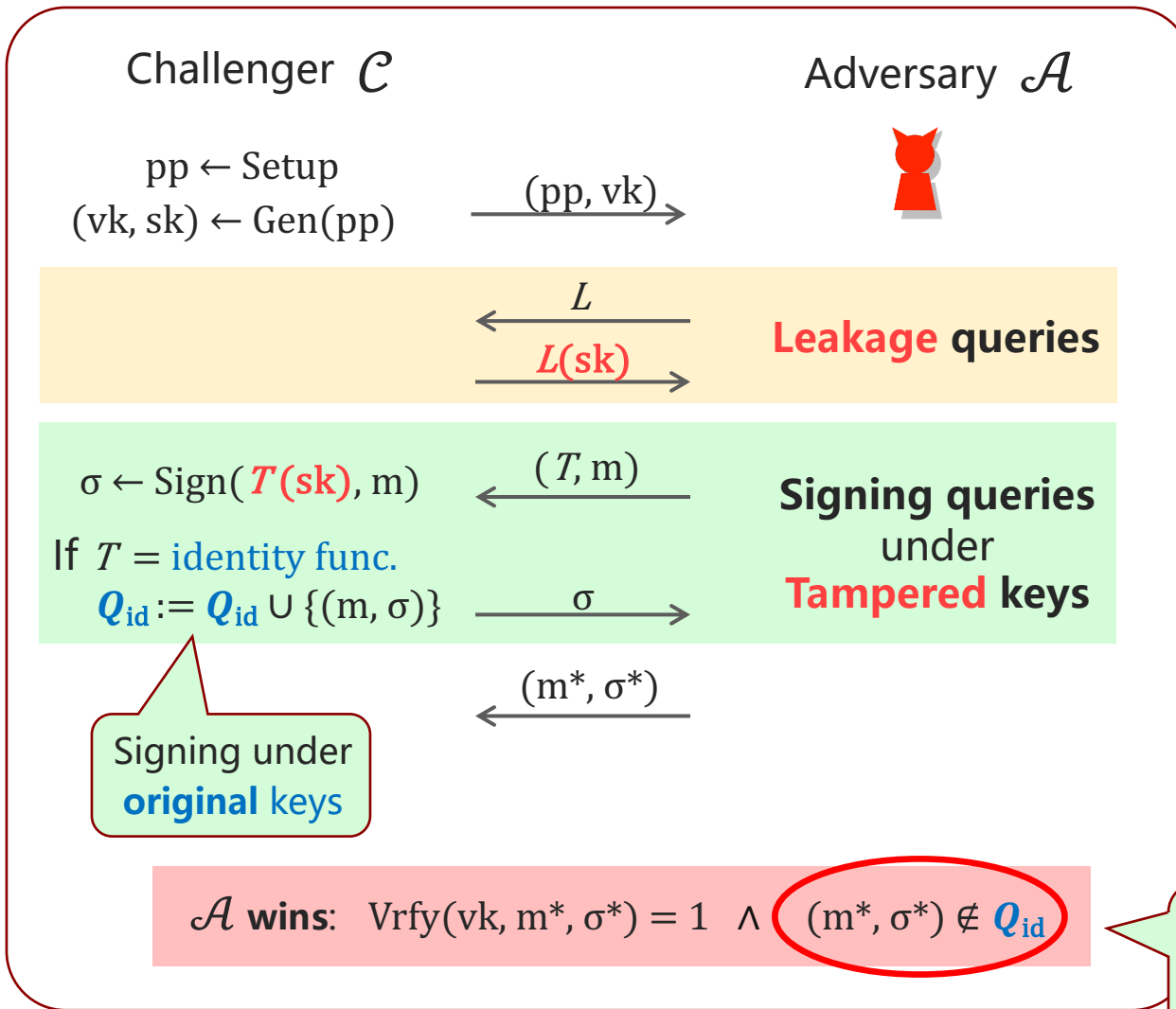
Recap: sLTR model for PKE [Sun et al., ACNS19]



Minimal restriction!

sLTR-CCA security:
 $|\Pr[\beta' = \beta] - 1/2|$
 = negligible

sLTR model (strong Leakage & Tampering-Resilience) for SIG



➤ Counterpart to the sLTR model for PKE [Sun et al., ACNS19]

- **Leakage:** Bounded amount [Naor-Segev, C09]
 - **Tampering:** Unbounded number, For specific functions [Bellare-Kohno, EC03]
- + **No additional mechanisms**

Minimal restriction!

Strong existential unforgeability!

sLTR-CMA security: $\Pr[\mathcal{A} \text{ wins}] = \text{negligible}$

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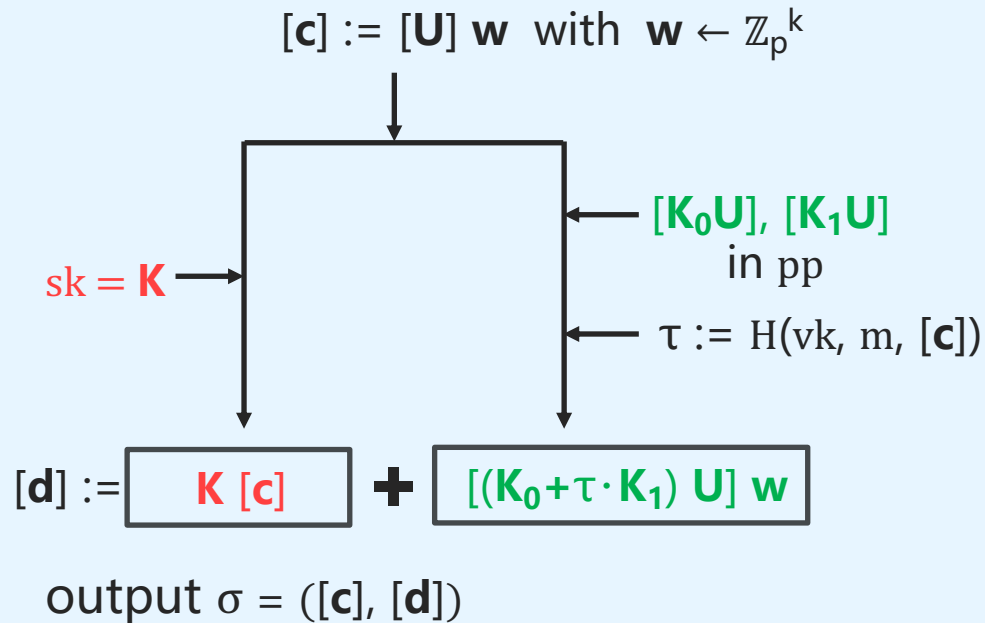
More Efficient & Direct Construction of SIG



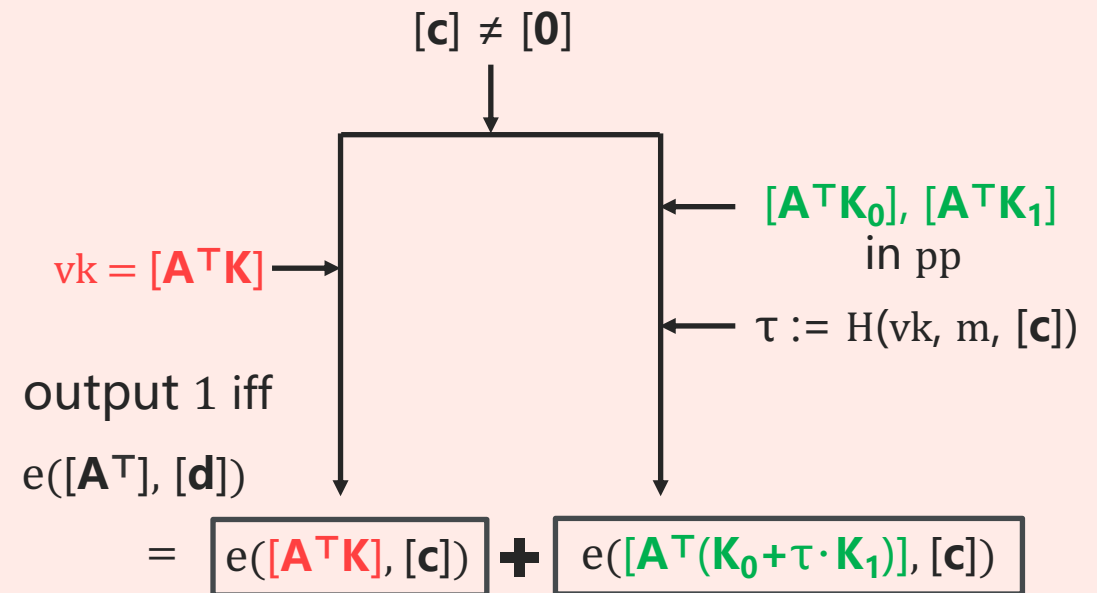
Setup \rightarrow $pp = ([\mathbf{U}], [\mathbf{K}_0\mathbf{U}], [\mathbf{K}_1\mathbf{U}], [\mathbf{A}], [\mathbf{A}^\top\mathbf{K}_0], [\mathbf{A}^\top\mathbf{K}_1])$, with $\mathbf{U}, \mathbf{A} \in \mathbb{Z}_p^{(k+1) \times k}$, $\mathbf{K}_0, \mathbf{K}_1 \in \mathbb{Z}_p^{(k+1) \times (k+1)}$

Gen \rightarrow (vk, sk) : $sk = \mathbf{K}$, $vk = [\mathbf{A}^\top\mathbf{K}]$, with $\mathbf{K} \in \mathbb{Z}_p^{(k+1) \times (k+1)}$

Sign($sk = \mathbf{K}$, m) \rightarrow σ :



Vrfy($vk = [\mathbf{A}^\top\mathbf{K}]$, m , $\sigma = ([\mathbf{c}], [\mathbf{d}])$) \rightarrow 1/0:



More Efficient & Direct Construction of SIG

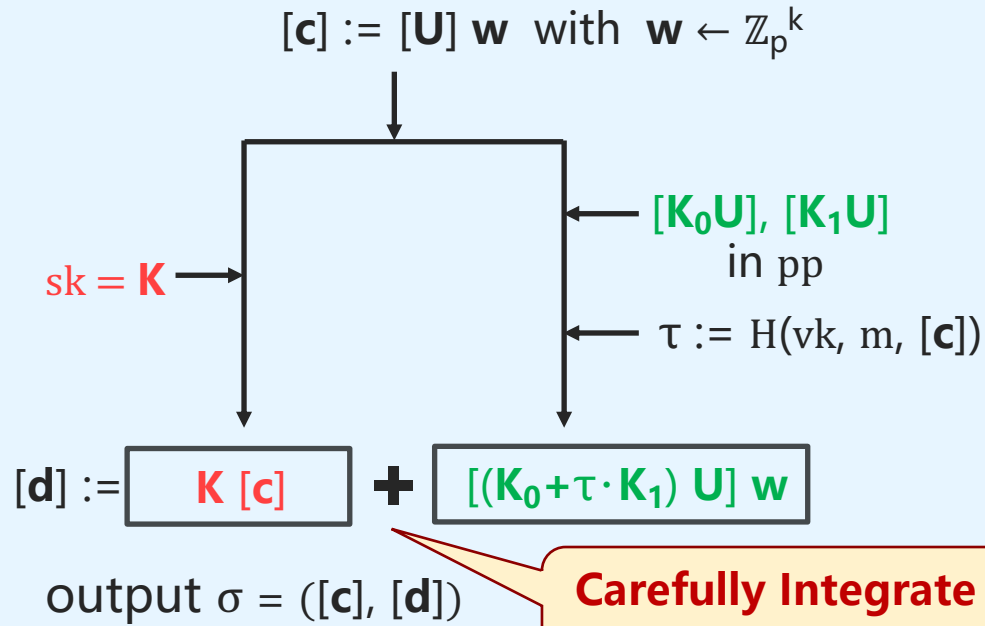


Setup \rightarrow pp = ($[\mathbf{U}]$, $[\mathbf{K}_0\mathbf{U}]$, $[\mathbf{K}_1\mathbf{U}]$, $[\mathbf{A}]$, $[\mathbf{A}^\top\mathbf{K}_0]$, $[\mathbf{A}^\top\mathbf{K}_1]$), with $\mathbf{U}, \mathbf{A} \in \mathbb{Z}_p^{(k+1) \times k}$, $\mathbf{K}_0, \mathbf{K}_1 \in \mathbb{Z}_p^{(k+1) \times (k+1)}$

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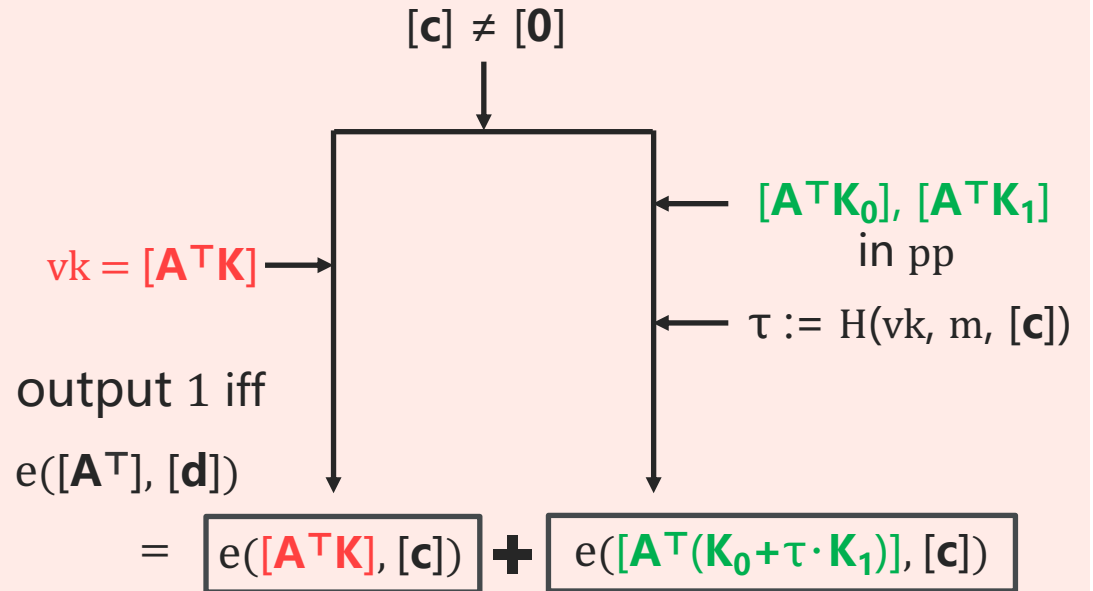
Leakage & Tampering on \mathbf{K} , but not on $\mathbf{K}_0, \mathbf{K}_1$

Sign(sk = \mathbf{K} , m) \rightarrow σ :



Carefully Integrate the two components

Vrfy(vk = $[\mathbf{A}^\top\mathbf{K}]$, m, $\sigma = ([\mathbf{c}], [\mathbf{d}])$) \rightarrow 1/0:



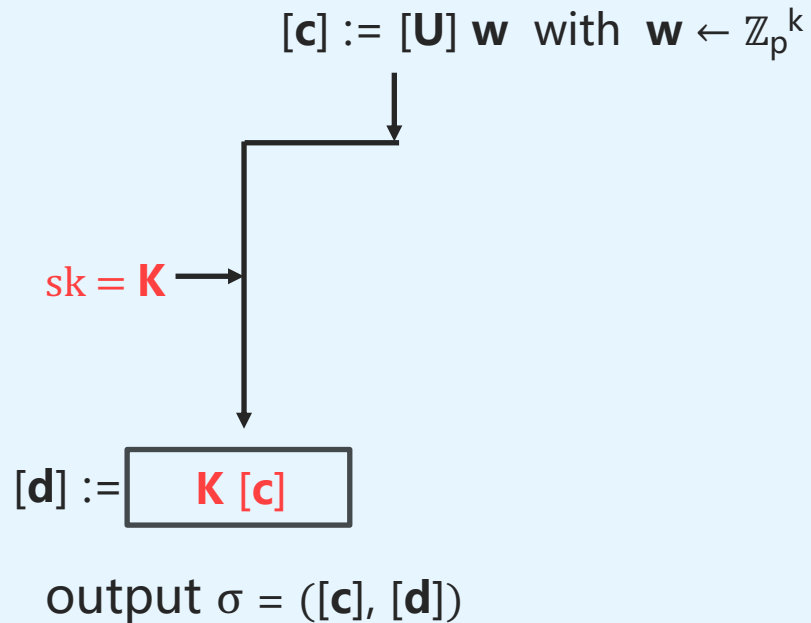
Construction of SIG: The First Component



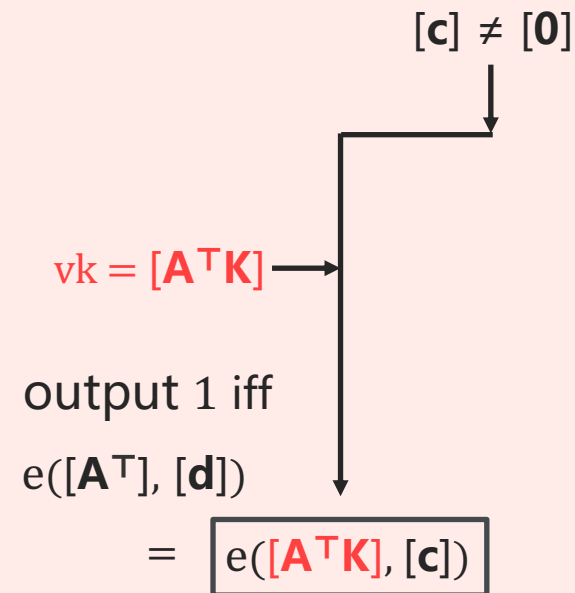
First Component (related to K)

Gen \rightarrow (vk, sk): $sk = K$, $vk = [A^T K]$, with $K \in \mathbb{Z}_p^{(k+1) \times (k+1)}$

Sign($sk = K$, m) $\rightarrow \sigma$:



Vrfy($vk = [A^T K]$, m , $\sigma = ([c], [d])$) \rightarrow 1/0:



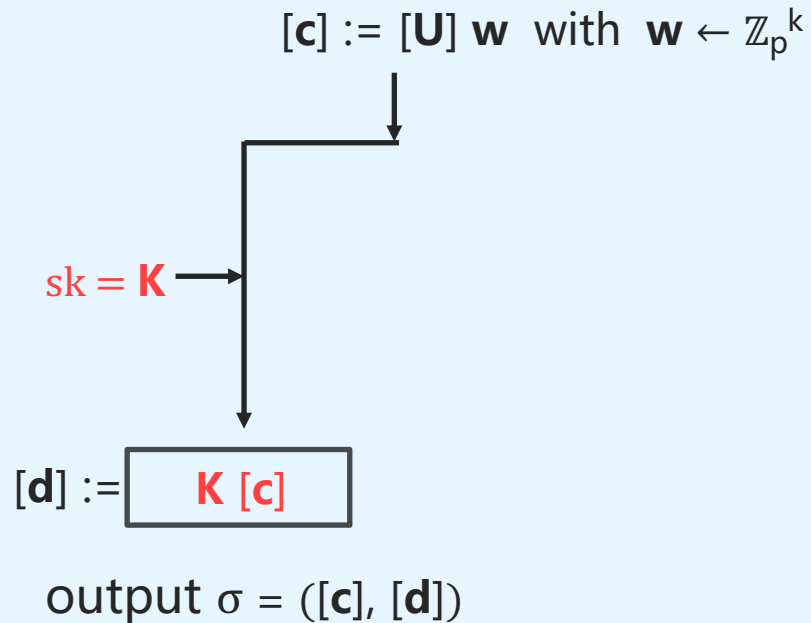
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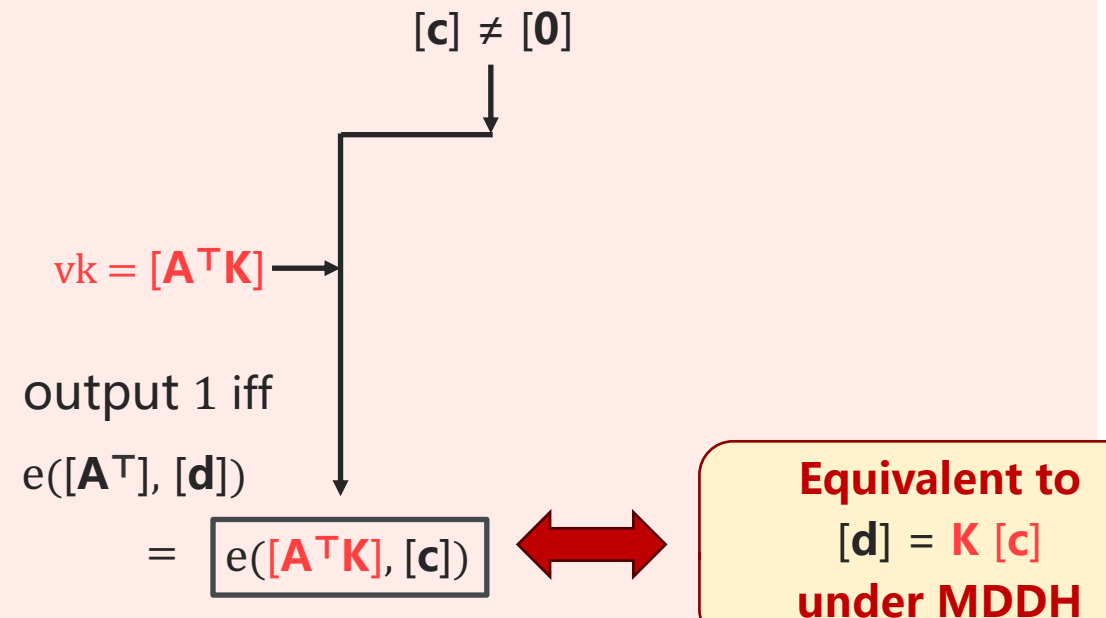
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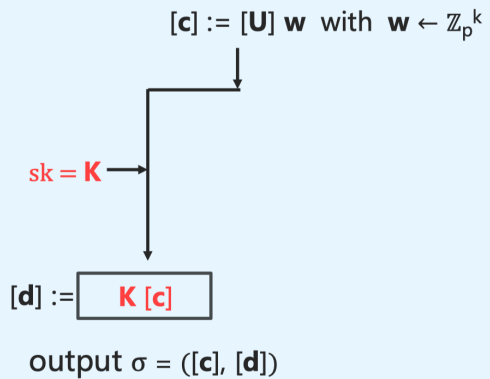
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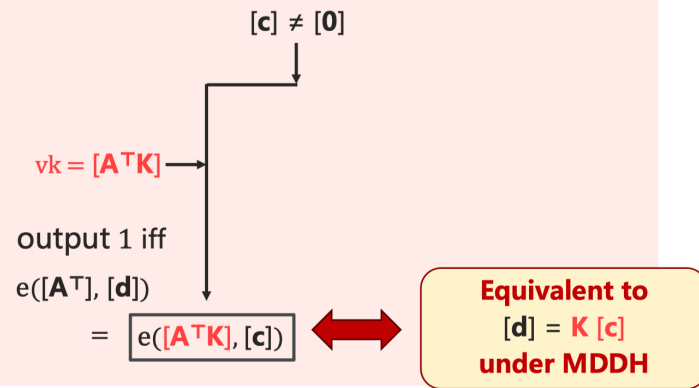
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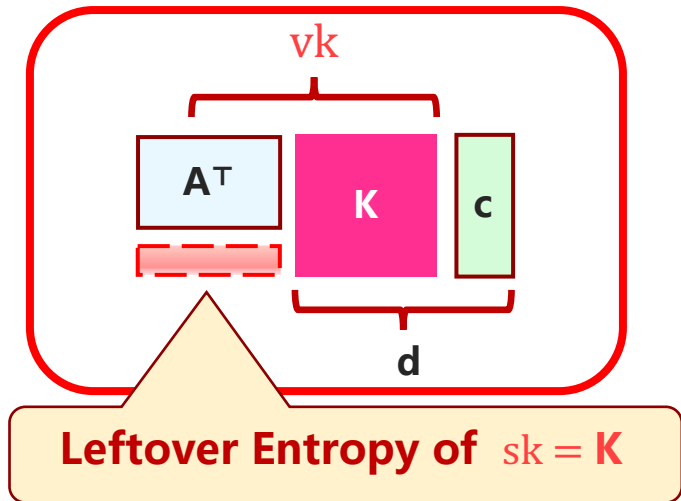
Vrfy($vk = [A^T K]$, m , $\sigma = ([c], [d])$) \rightarrow 1/0:



**Security against No-Message Attacks
(No Signing Queries) under Key Leakages**

- Given **only** $vk = [A^T K]$, it is hard to produce $\sigma = ([c], [d])$ to pass Vrfy:

$$[c] \neq [0] \quad \wedge \quad [d] = K [c]$$



- ... even in the presence of additional **leakage** $L(sk) = L(K)$

Construction of SIG: The Second Component

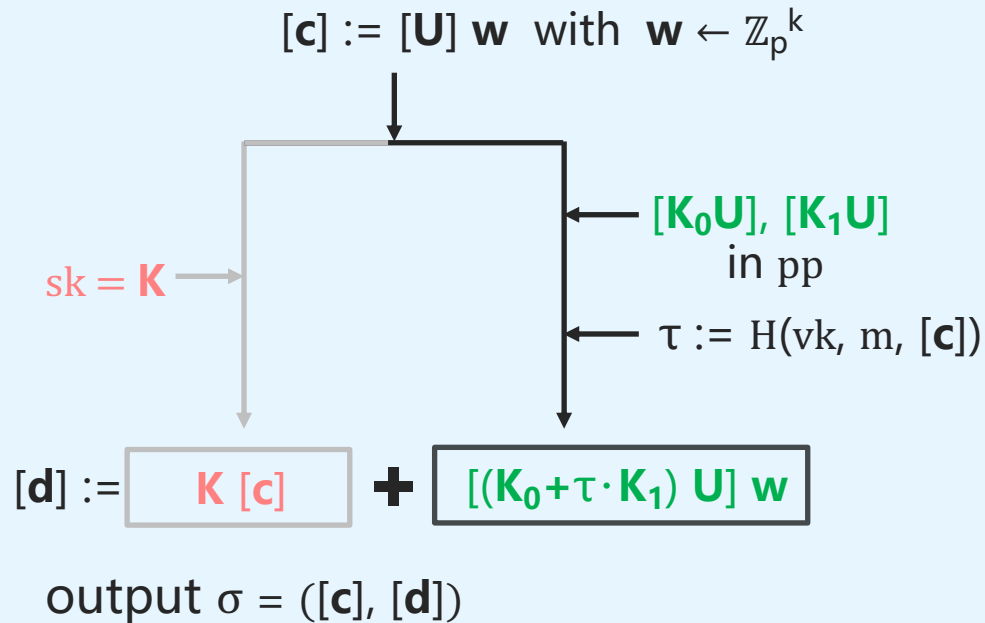


First Component (related to K)

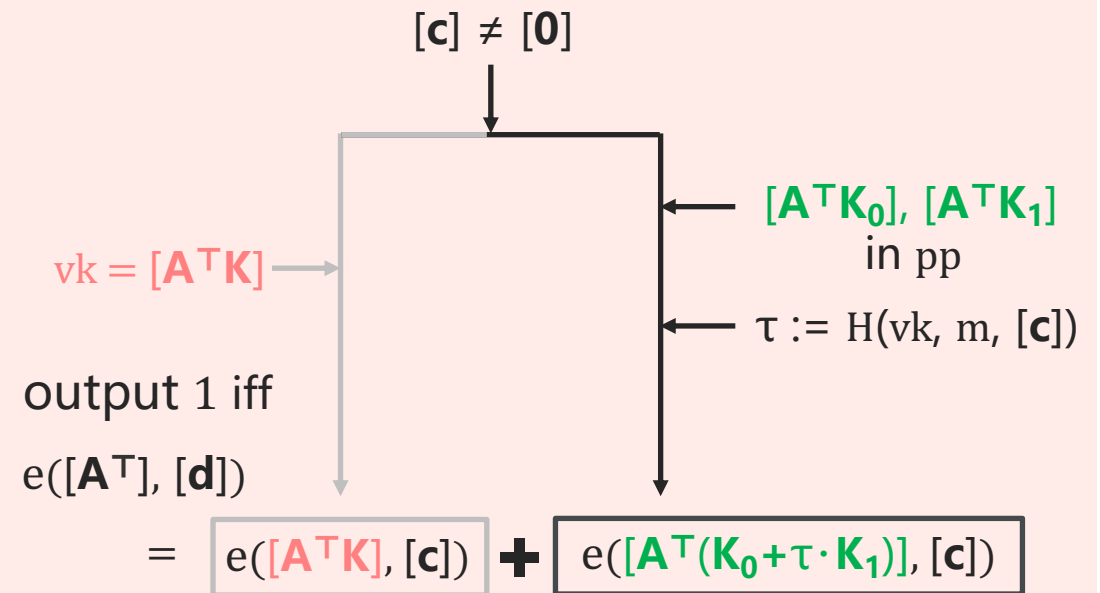
Second Component (related to K_0, K_1)

Setup \rightarrow pp = ($[U], [K_0U], [K_1U], [A], [A^TK_0], [A^TK_1]$), with $U, A \in \mathbb{Z}_p^{(k+1) \times k}$, $K_0, K_1 \in \mathbb{Z}_p^{(k+1) \times (k+1)}$

Sign($sk = K, m$) $\rightarrow \sigma$:



Vrfy($vk = [A^TK], m, \sigma = ([c], [d])$) \rightarrow 1/0:



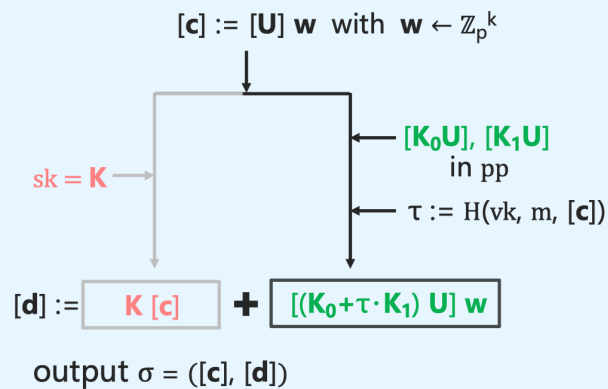
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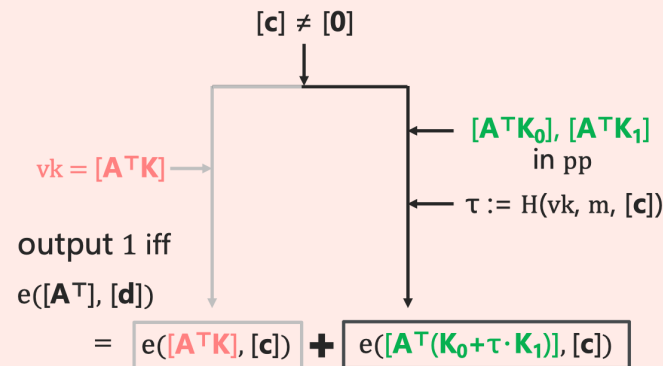
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Sign($sk = K, m$) $\rightarrow \sigma$:



Vrfy($vk = [A^TK], m, \sigma = ([c], [d])$) $\rightarrow 1/0$:



Masking First Component during Signing Queries under **Tampered Keys**

- Essentially the **OTSS-NIZK** (One-Time Simulation-Sound NIZK) proposed in [Kiltz-Wee, EC15]
- ... but **OTSS** is **insufficient**: multiple signing queries contain **multiple** NIZK proofs
- We resort to another property as observed in [Kiltz-Wee, EC15]:
 - randomized PRF on τ** which can mask First Component

Security of SIG: Putting Two Components Together



First Component (related to K)



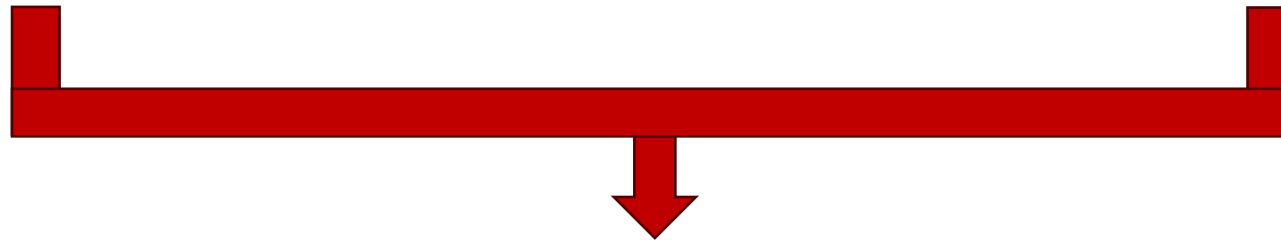
Second Component (related to K_0, K_1)



Security against **No-Message Attacks**
(No Signing Queries) under **Key Leakages**



Masking First Component during
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sLTR-CMA security for SIG
under **Key Leakages & Tampered Keys**

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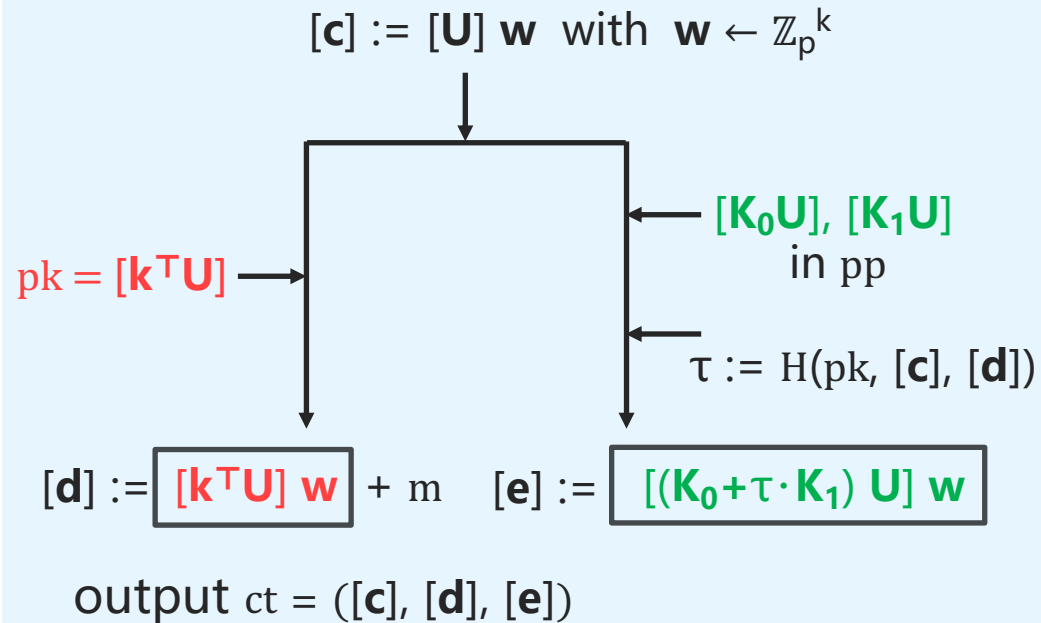
More Efficient & Direct Construction of CCA-PKE



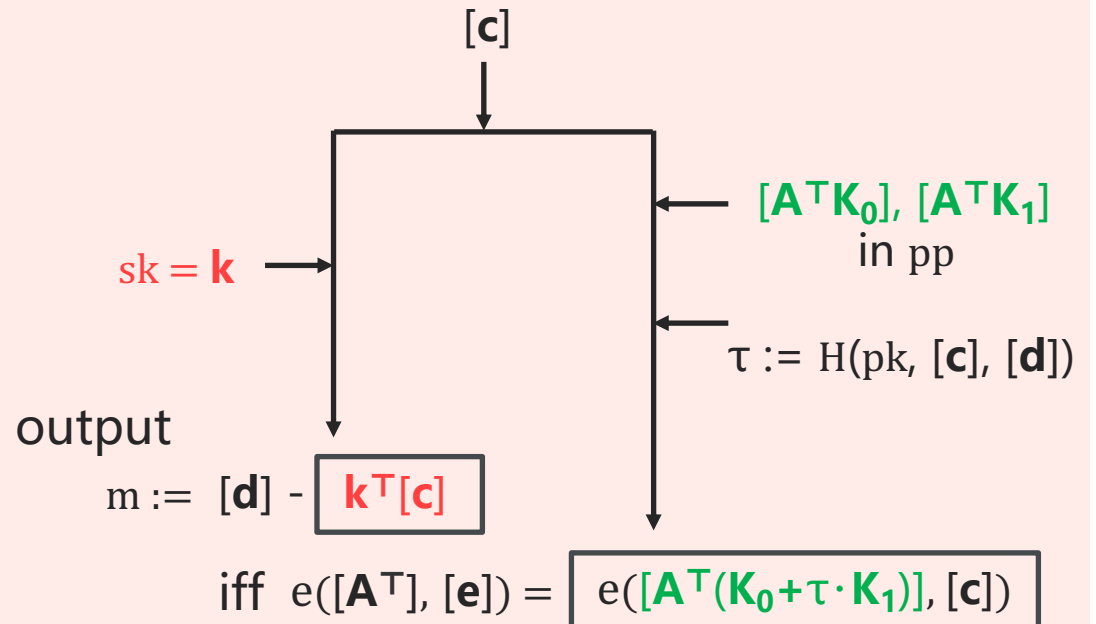
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Enc($pk = [\mathbf{k}^\top\mathbf{U}]$, m) \rightarrow ct:



Dec($sk = \mathbf{k}$, ct = $([\mathbf{c}], [\mathbf{d}], [\mathbf{e}])$) \rightarrow m/\perp :



More Efficient & Direct Construction of CCA-PKE

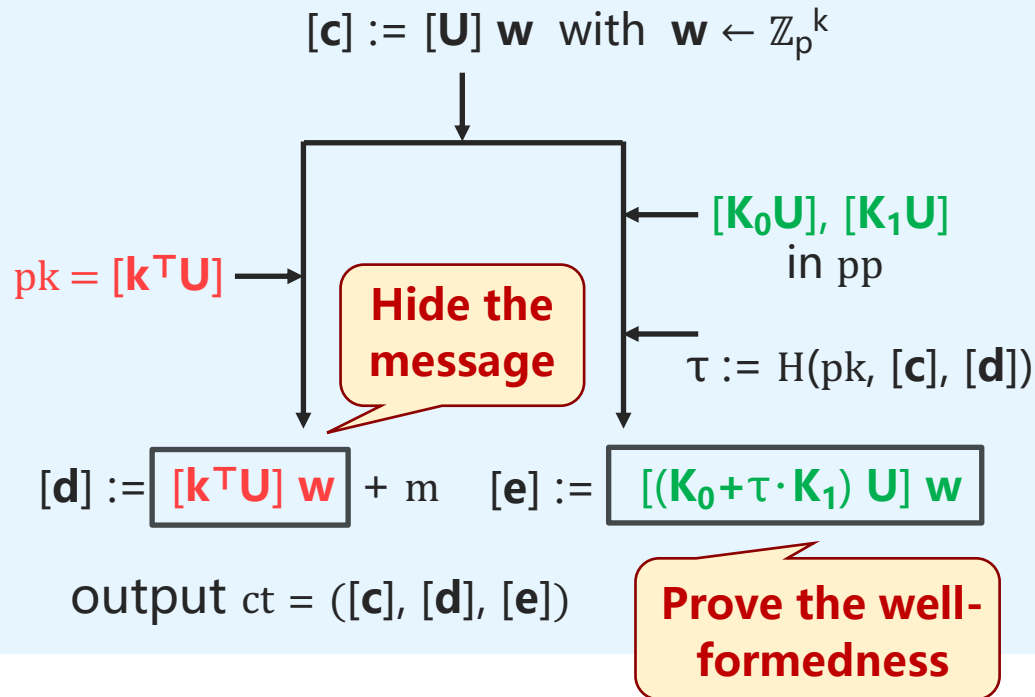


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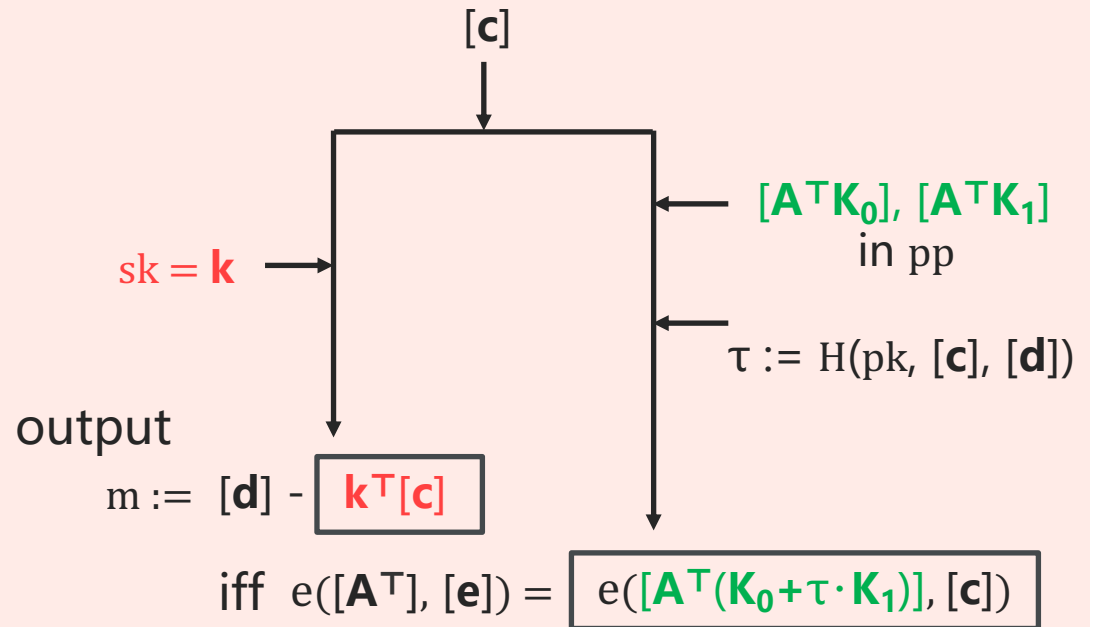
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Dec(sk = \mathbf{k} , ct = ($[\mathbf{c}]$, $[\mathbf{d}]$, $[\mathbf{e}]$)) \rightarrow m/ \perp :



Security of PKE: Putting Two Components Together



First Component (related to k)



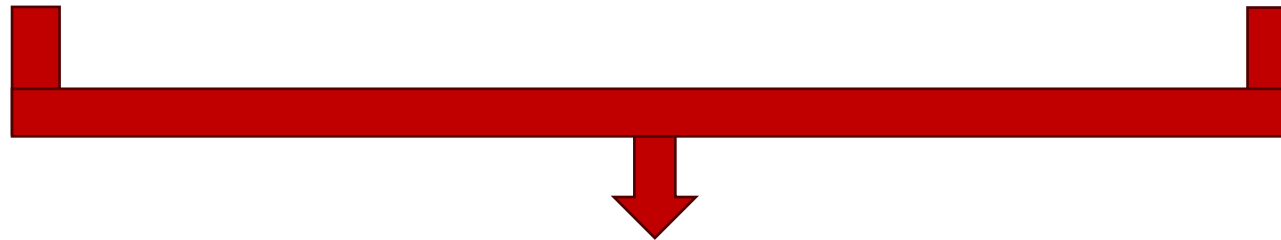
Second Component (related to K_0, K_1)



CPA Security under Key Leakages



Reject Decryption Queries
under Tampered Keys



sLTR-CCA security for PKE
under Key Leakages & Tampered Keys

- **More Efficient** SIG and CCA-PKE with leakage & tamper resilience
 - ✓ Direct construction, avoid using tSE-NIZK

Schemes	Efficiency	Model
Our SIG	signature = 4 group elements	sLTR
Our CCA-PKE	ciphertext = 6 group elements	sLTR

5~8x shorter

1.3~3.3x shorter

- New **sLTR security for SIG**: counterpart to the sLTR security for PKE
- The first SIG with **strong existential unforgeability** in the LTR setting

Thanks! Questions?

[ePrint: ia.cr/2023/1965](https://ia.cr/2023/1965)