

# Chosen-Ciphertext Secure Dual-Receiver Encryption in the Standard Model Based on Post-Quantum Assumptions

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# Preliminaries



Preliminaries  
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Contributions  
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Summary  
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- Chosen-Ciphertext Security

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## Definition of DRE

- $\text{gen}(1^\lambda)$  : takes security parameter, outputs one public/secret key pair  $(pk, sk)$
- $\text{enc}(pk^R, pk^S, m)$  : takes two (independent) public keys and a message, outputs ciphertext  $c$
- $\text{dec}(sk^i, pk^R, pk^S, c)$  : takes one secret key, both public keys and a ciphertext  $c$ , outputs message  $m^i$

# Dual-Receiver Encryption

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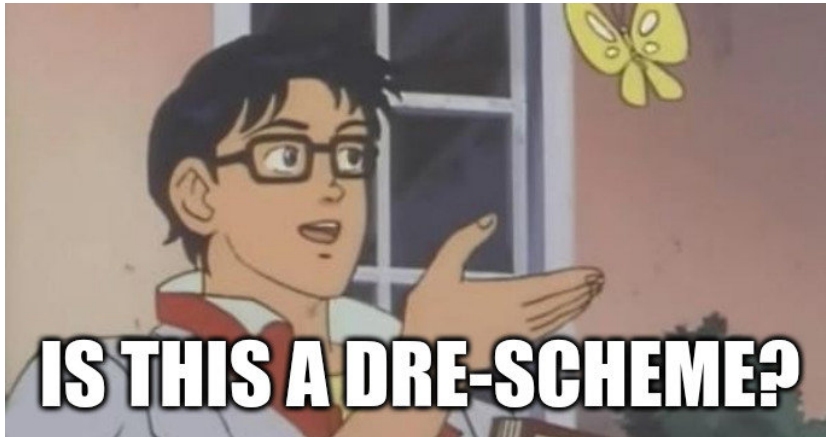
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- This is called **soundness**
- Formal definition as usual through a game

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$(\mathbf{c}, pk^{R'})$   
 $\longrightarrow$

if  $R' \in \{S, R\} \wedge \mathbf{c} \neq \mathbf{c}^*$   
 then  $\mathbf{m} = \text{dec}(sk^{R'}, pk^R, pk^S, \mathbf{c})$   
 else  $\mathbf{m} = \perp$

$\mathbf{m}'$   
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- Slightly different decryption oracle  $\mathcal{O}$
- With soundness this collapses to the PKE CCA definition

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  - Dolev-Yao model for automated theorem provers
- Key Exchange with Incriminating Abort
- PKE with Non-Interactive Opening
- ... and many more

# Related Work



Preliminaries  
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Contributions  
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Summary  
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# Related Work

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  - Sound PQ DRE schemes (which are not CCA)
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  - PQ CCA DRE schemes (which are not sound)
- ... but no sound CCA PQ DRE scheme

# Our contributions

Preliminaries  
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# Our contributions

- Showing that no previously known PQ CCA DRE scheme satisfies soundness by constructing malicious ciphertexts



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- Showing that no previously known PQ CCA DRE scheme satisfies soundness by constructing malicious ciphertexts
- Construction of two efficient PQ CCA DRE schemes with soundness
- ...one based on LWE, one based on LPN
- First DRE scheme based on LPN
- Inspired by Kiltz, Masny, and Pietrzak (2014)
- Both use the hybrid encryption paradigm

# Our contributions - LPN

## Hybrid encryption

```
3 :  $\mathbf{s} \leftarrow_{\$} \{0, 1\}^n$   
4 :  $(dk, mk) := \text{KDF}(\mathbf{s})$   
9 :  $\phi := \text{SKE.enc}(dk, \mathbf{M})$   
10 :  $\sigma := \text{MAC.sign}(mk, (\mathbf{c}_0, \mathbf{c}_1, \phi))$ 
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- The secret  $s$  of the asymmetric part is only used to derive MAC and SKE keys
- The encryption is then symmetric
- Makes encryption smaller and faster for larger messages

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## Soundness

7 : **if**  $\left\| \mathbf{c}_0^R - \mathbf{s}^\top \mathbf{A}^R \right\|_w > \beta$  output  $\perp$

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9 : **if**  $\left\| \mathbf{c}_1^R - \mathbf{s}^\top (\mathbf{A}_1^R + \text{FRD}(\mathbf{H}(\mathbf{c}_0))\mathbf{G}) \right\|_w > \frac{\alpha m}{2}$

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- Consistency check can be done with only the public keys
- “Soundness check” nearly for free

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$$6 : \mathbf{c}_0 = (\mathbf{s}^\top \mathbf{A}^R + \mathbf{e}^R, \mathbf{s}^\top \mathbf{A}^S + \mathbf{e}^S)$$

$$8 : \mathbf{c}_1 = (\mathbf{s}^\top (\mathbf{A}_1^R + \text{FRD}(\mathbf{H}(\mathbf{c}_0)))\mathbf{G}) + (\mathbf{e}^R)^\top \mathbf{T}^R, \\ \mathbf{s}^\top (\mathbf{A}_1^S + \text{FRD}(\mathbf{H}(\mathbf{c}_0)))\mathbf{G} + (\mathbf{e}^S)^\top \mathbf{T}^S)$$

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# Our contributions - LPN

## “Double trapdoor”

Need to change public key  =  $A_1^R$  from  $A_1^R = A^R \cdot R^R$  to  $A_1^R = A^R \cdot R^R + X$  for  $A^R$  and  $X$  known matrices

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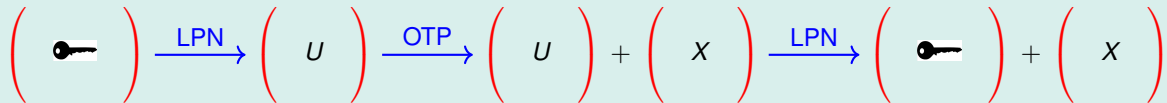


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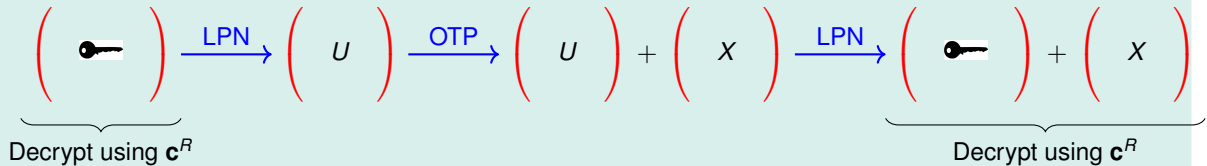
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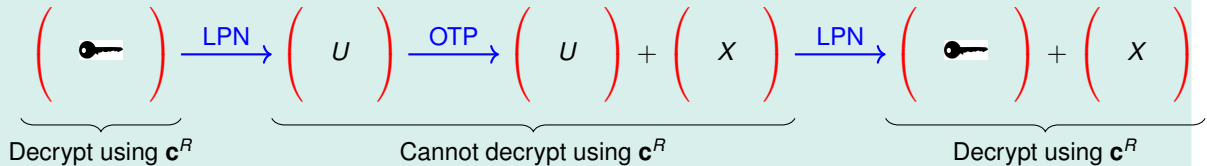




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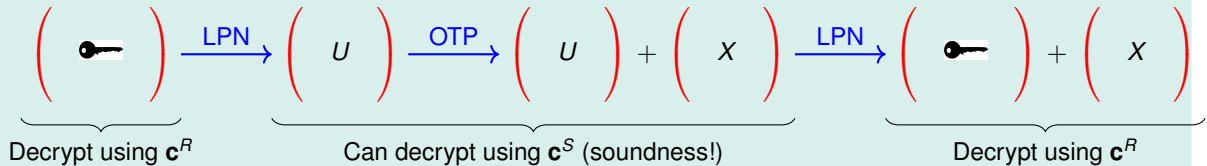
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# Our contributions - LWE



Preliminaries  
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Contributions  
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Summary  
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- Similar construction and soundness check
- Proof easier thanks to  $A_1$  being statistical indistinguishable from randomness
- Bigger ciphertexts, but smaller keys

# Summary

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- First sound Post-Quantum CCA secure Dual-Receiver Encryption schemes in the standard model
- Known primitives, allows relatively easy implementation
- Room for optimizations like R-LWE, compression techniques etc

# Summary

Thank you for your attention. Any questions?

# Sizes of the constructions

Table: Sizes of  $\text{PKE}_{\text{LWE-DRE}}$

	$ pk $ for one party	$ sk $	$ c $
Generic sizes	$\lceil \log q \rceil \cdot (n \cdot (m + \bar{m}))$	$\lceil \log q \rceil \cdot (m \cdot \bar{m})$	$\lceil \log q \rceil \cdot (2 \cdot (m + \bar{m}))$
Exact sizes	61.45MB	58.49MB	91.45kB

Table: Sizes of  $\text{PKE}_{\text{LPN-DRE}}$

	$ pk $ for one party	$ sk $	$ c $
Generic sizes	$2 \cdot n \cdot m$	$m^2$	$4 \cdot m$
Exact sizes	351.13MB	351.13MB	26.5kB

# Our contributions - LPN

$\text{gen}(1^\lambda)$

---

1 :  $\mathbf{A} \leftarrow \$ \mathbb{Z}_2^{n \times m}, \mathbf{R} \leftarrow \text{Ber}_p^{m \times m}$   
 2 :  $\mathbf{A}_1 = \mathbf{A} \cdot \mathbf{R}$   
 3 : **return**  $(pk, sk) := ((\mathbf{A}, \mathbf{A}_1), \mathbf{R})$

$\text{enc}(pk^R, pk^S, M)$

---

1 : parse  $pk^R = (\mathbf{A}^R, \mathbf{A}_1^R)$   
 2 : parse  $pk^S = (\mathbf{A}^S, \mathbf{A}_1^S)$   
 3 :  $\mathbf{s} \leftarrow \$ \{0, 1\}^n$   
 4 :  $(dk, mk) := \text{KDF}(\mathbf{s})$   
 5 :  $\mathbf{e}^R, \mathbf{e}^S \leftarrow \text{Ber}_p^m$   
 6 :  $\mathbf{c}_0 = (\mathbf{s}^\top \mathbf{A}^R + \mathbf{e}^R, \mathbf{s}^\top \mathbf{A}^S + \mathbf{e}^S)$   
 7 :  $\mathbf{T}^R, \mathbf{T}^S \leftarrow \text{Ber}_p^{m \times m}$   
 8 :  $\mathbf{c}_1 = (\mathbf{s}^\top (\mathbf{A}_1^R + \text{FRD}(\mathbf{H}(\mathbf{c}_0)))\mathbf{G}) + (\mathbf{e}^R)^\top \mathbf{T}^R,$   
 $\mathbf{s}^\top (\mathbf{A}_1^S + \text{FRD}(\mathbf{H}(\mathbf{c}_0)))\mathbf{G}) + (\mathbf{e}^S)^\top \mathbf{T}^S)$   
 9 :  $\phi := \text{SKE.enc}(dk, M)$   
 10 :  $\sigma := \text{MAC.sign}(mk, (\mathbf{c}_0, \mathbf{c}_1), \phi)$   
 11 : **return**  $\mathbf{c} = (\mathbf{c}_0, \mathbf{c}_1, \phi, \sigma)$

$\text{dec}(sk^R, pk^R, pk^S, \mathbf{C})$

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1 : parse  $pk^R = (\mathbf{A}^R, \mathbf{A}_1^R)$   
 2 : parse  $pk^S = (\mathbf{A}^S, \mathbf{A}_1^S)$   
 3 : parse  $sk^R = (\mathbf{R}^R)$   
 4 : parse  $\mathbf{C} = (\mathbf{c}_0^R, \mathbf{c}_0^S, \mathbf{c}_1^R, \mathbf{c}_1^S, \phi, \sigma)$   
 5 :  $\mathbf{c}_t^R := \mathbf{c}_1^R - \mathbf{c}_0^R \mathbf{R}^R$   
 6 :  $\mathbf{s} := \text{decode}_G(\mathbf{c}_t^R) \cdot \text{FRD}(\mathbf{H}(\mathbf{c}_0))^{-1}$   
 7 : **if**  $\left\| \mathbf{c}_0^R - \mathbf{s}^\top \mathbf{A}^R \right\|_w > \beta$  **output**  $\perp$   
 8 : **if**  $\left\| \mathbf{c}_0^S - \mathbf{s}^\top \mathbf{A}^S \right\|_w > \beta$  **output**  $\perp$   
 9 : **if**  $\left\| \mathbf{c}_1^R - \mathbf{s}^\top (\mathbf{A}_1^R + \text{FRD}(\mathbf{H}(\mathbf{c}_0)))\mathbf{G} \right\|_w > \frac{\alpha m}{2}$   
 10 : **if**  $\left\| \mathbf{c}_1^S - \mathbf{s}^\top (\mathbf{A}_1^S + \text{FRD}(\mathbf{H}(\mathbf{c}_0)))\mathbf{G} \right\|_w > \frac{\alpha m}{2}$   
 11 :  $(dk, mk) = \text{KDF}(\mathbf{s})$   
 12 : **if**  $1 == \text{MAC.Vfy}(mk, (\mathbf{c}_0, \mathbf{c}_1), \phi), \sigma)$   
 13 : **return**  $\mathbf{M} = \text{SKE.dec}(dk, \phi)$   
 14 : **else return**  $\mathbf{M} = \perp$

# References

- [1] Eike Kiltz, Daniel Masny, and Krzysztof Pietrzak. “Simple Chosen-Ciphertext Security from Low-Noise LPN”. In: *PKC 2014*. Ed. by Hugo Krawczyk. Vol. 8383. LNCS. Springer, Heidelberg, Mar. 2014, pp. 1–18. DOI: 10.1007/978-3-642-54631-0\_1.