

Consensus in the presence of Overlapping Faults and Total Omission Setting

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Byzantine Agreement



Byzantine Agreement

Inputs

- Validity

- Consistency

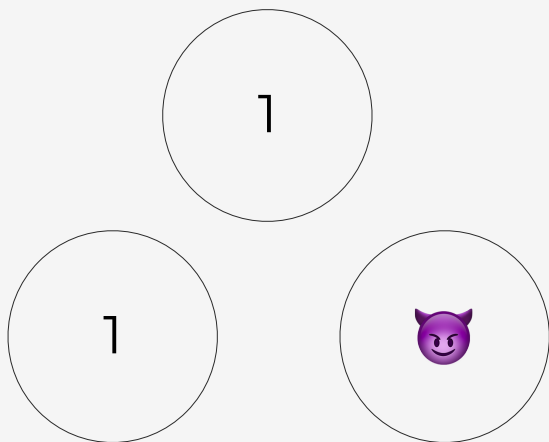
- Termination

Outputs



Byzantine Agreement

Inputs



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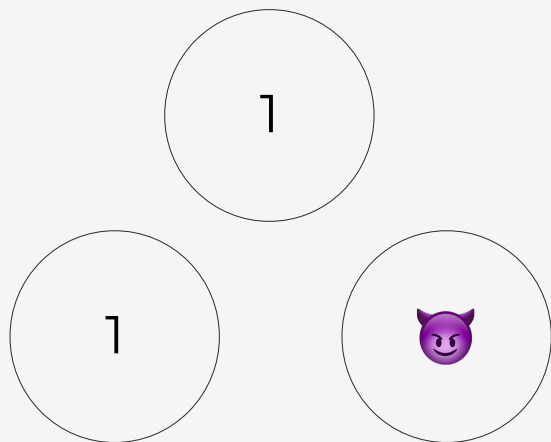
• Termination

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Byzantine Agreement

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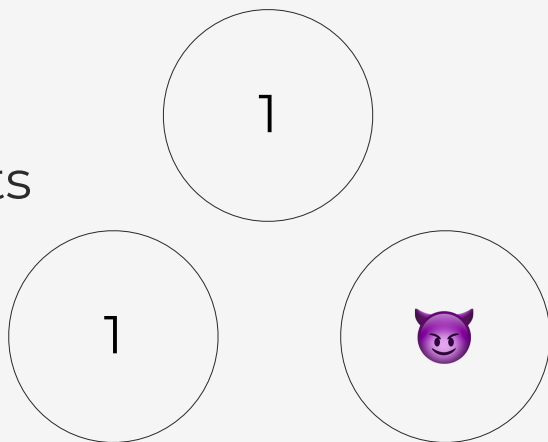


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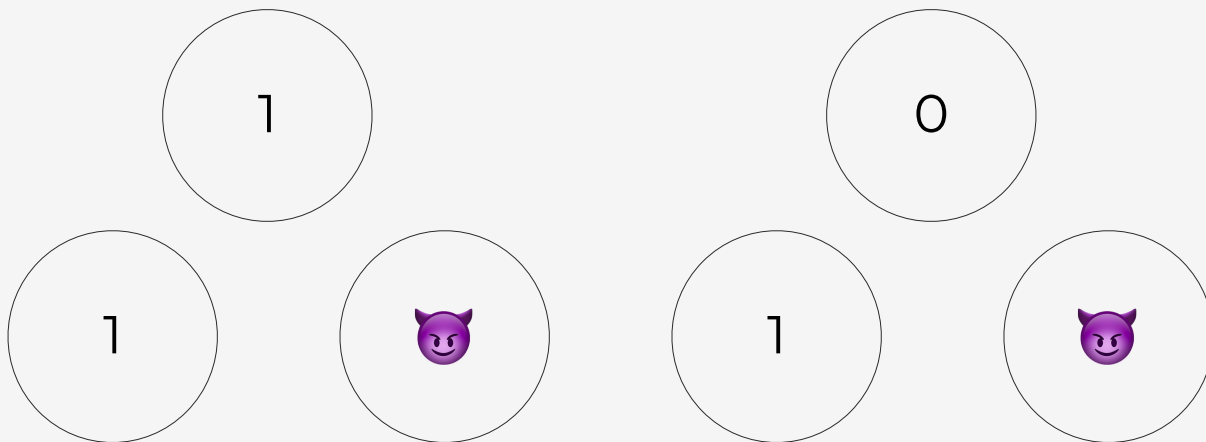
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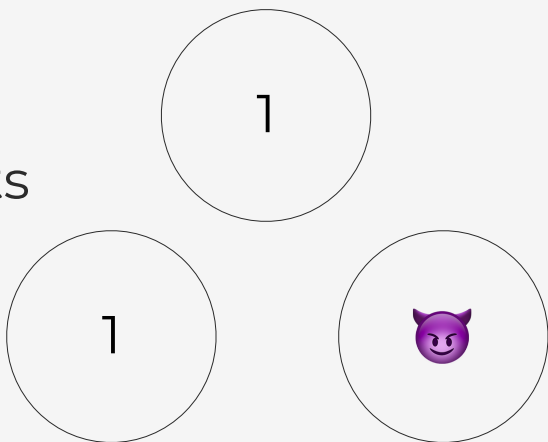


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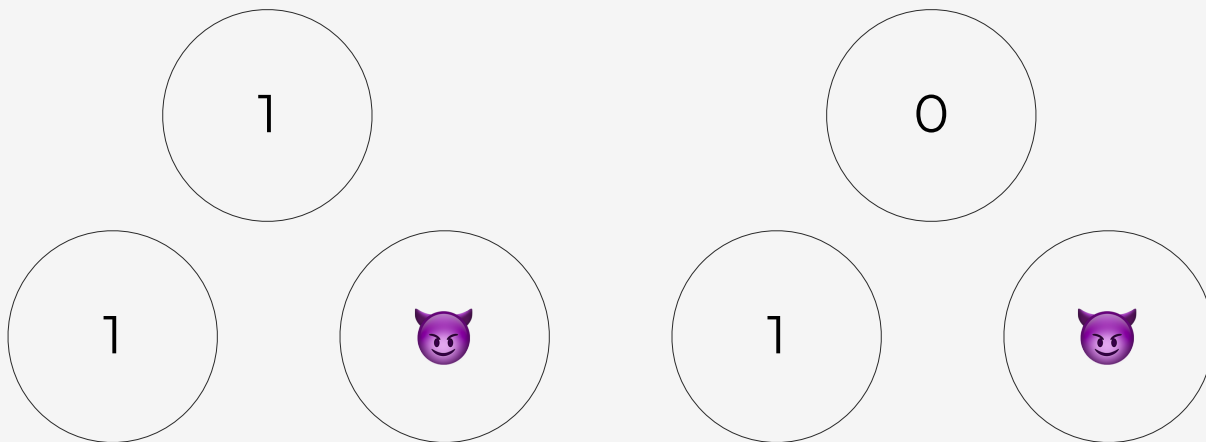
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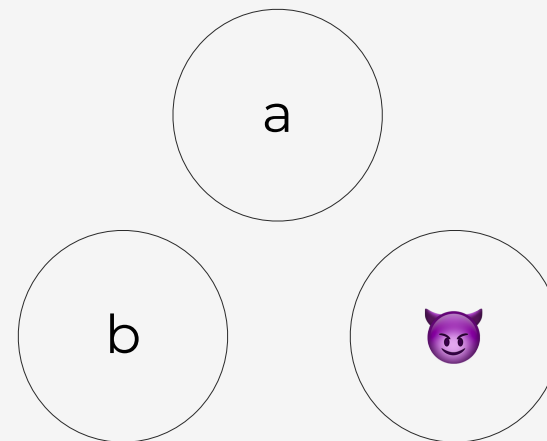
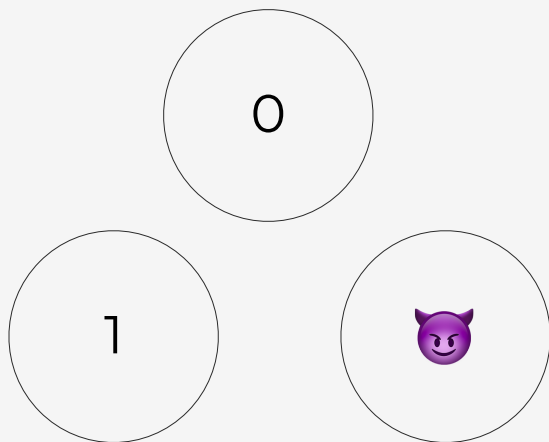
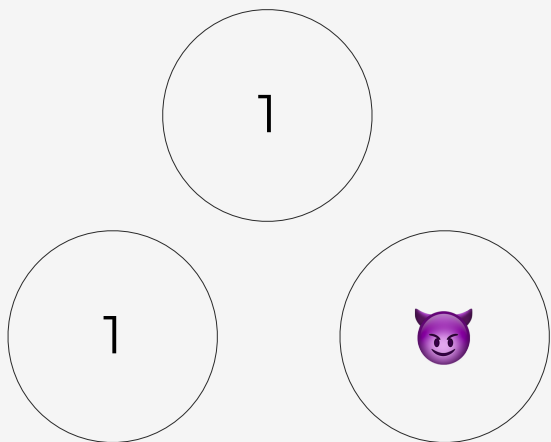
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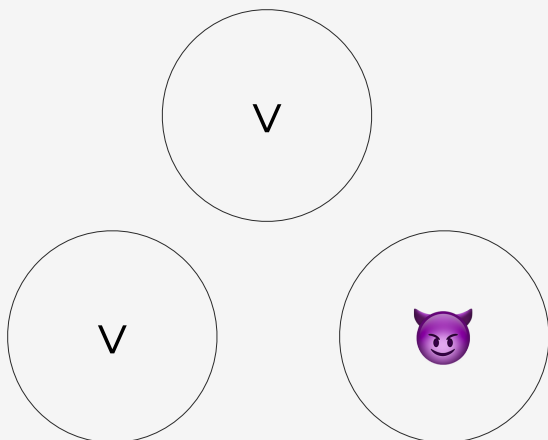
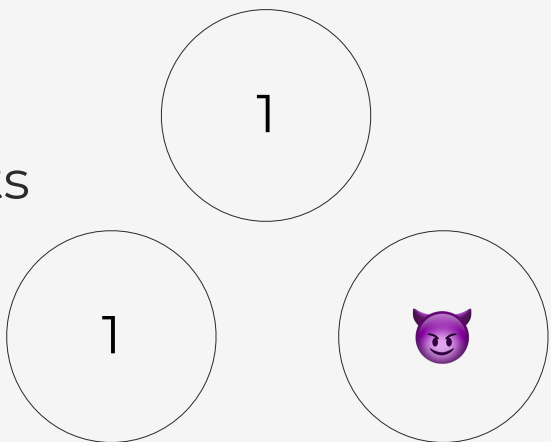


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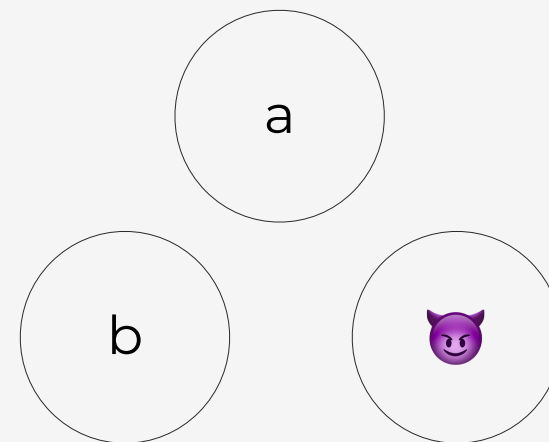
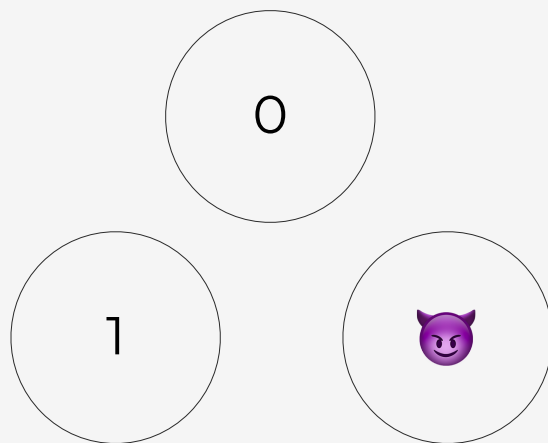
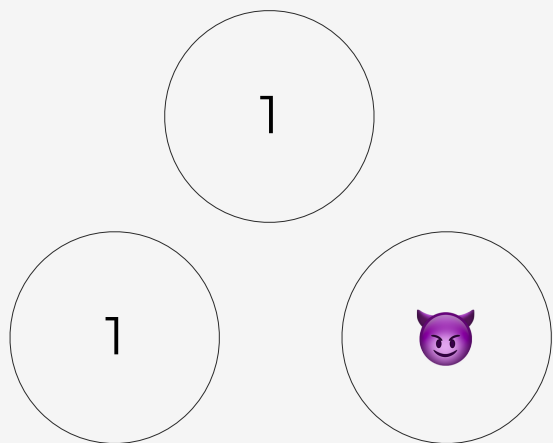


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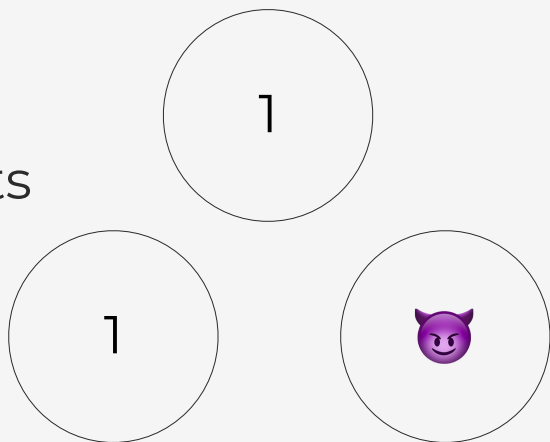


Byzantine Agreement

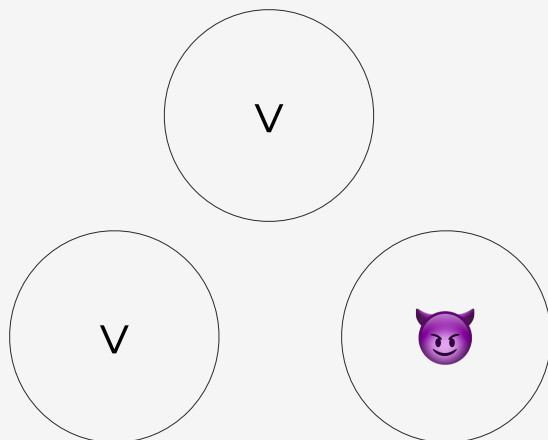
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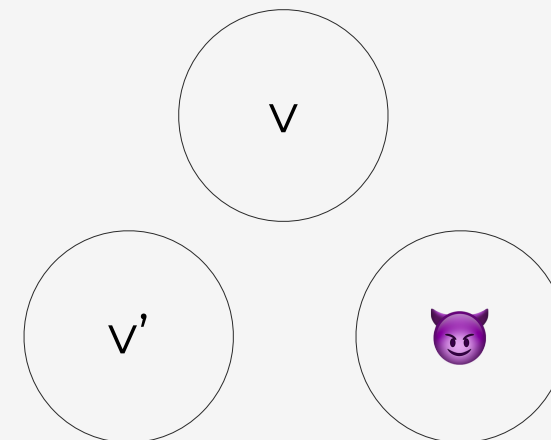
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Outputs



Mixed Fault Model



Mixed Fault Model

- Send Omission(Ghost👻)
- Receive Omission(Zombie🧟)
- Byzantine Corruption
- Full-Omission(Overlapping Faults)



Omissions



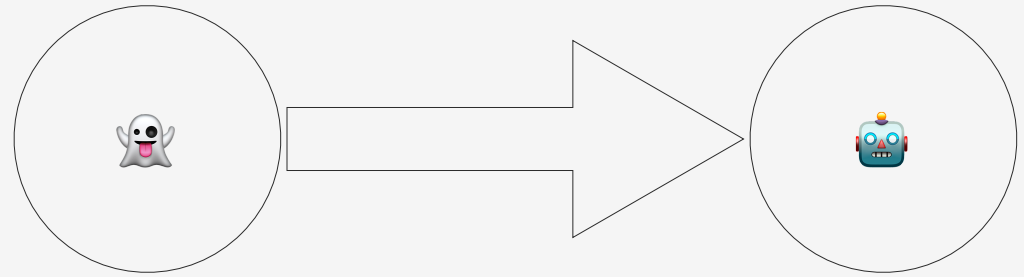
Omissions

- Send Omission 🙈



Omissions

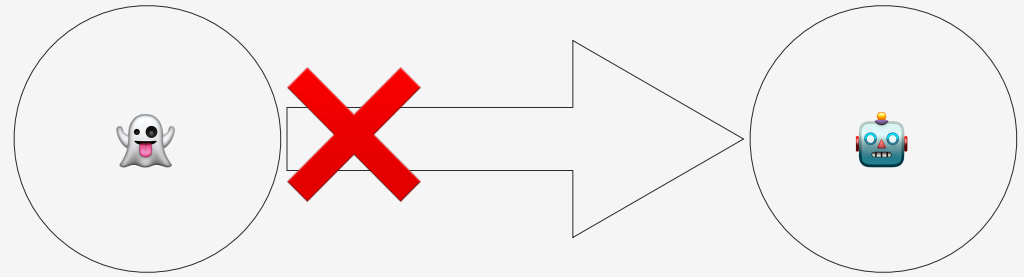
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Omissions

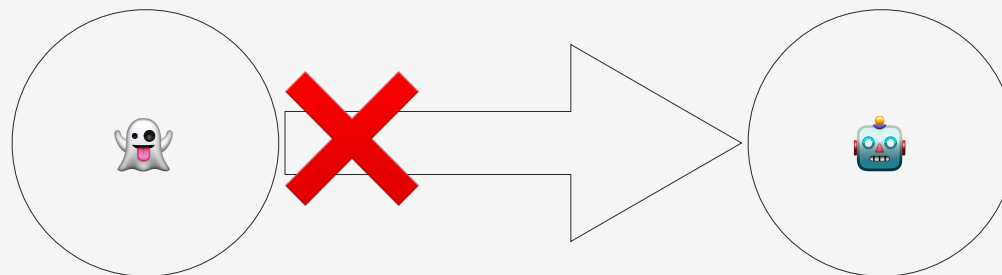
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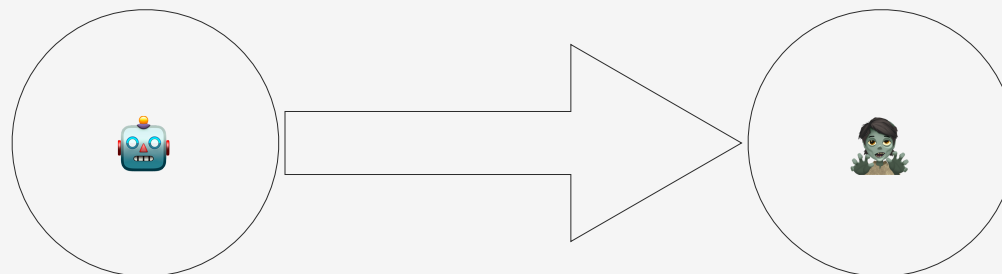


Omissions

- Send Omission 🙈



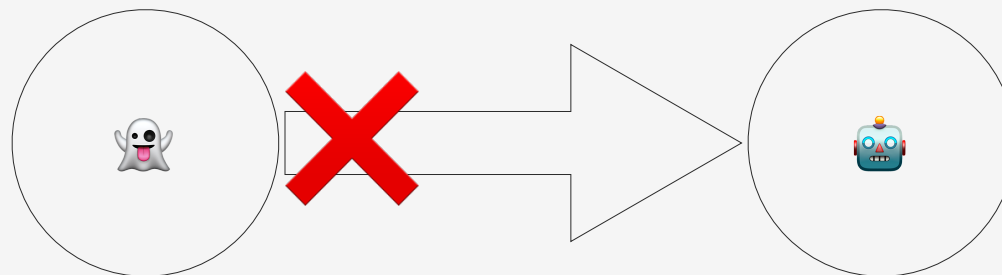
- Receive Omission 🧟



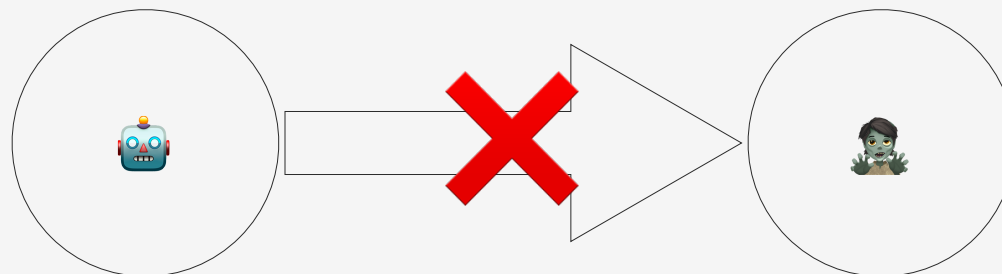


Omissions

- Send Omission 🙈



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Variant of Uniformity (Undead)

- Receive Omission



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It is allowed to output a flag $Z=True$ to indicate it is actually receive omission.

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When it sets itself as Send Omission, it must be the case it is send omission.

It must output the “correct” value if it is not receive omission.



Basic Idea: Self-Detection



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- **Receive Omission Detection**



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- **Send Omission Detection**

If a party knows at least one nonfaulty party has not received the message it is expected to send, it can detect itself as send omission.



Our Starting Point: Zombies and Ghosts[LS2022]

Undead Weak Multicast



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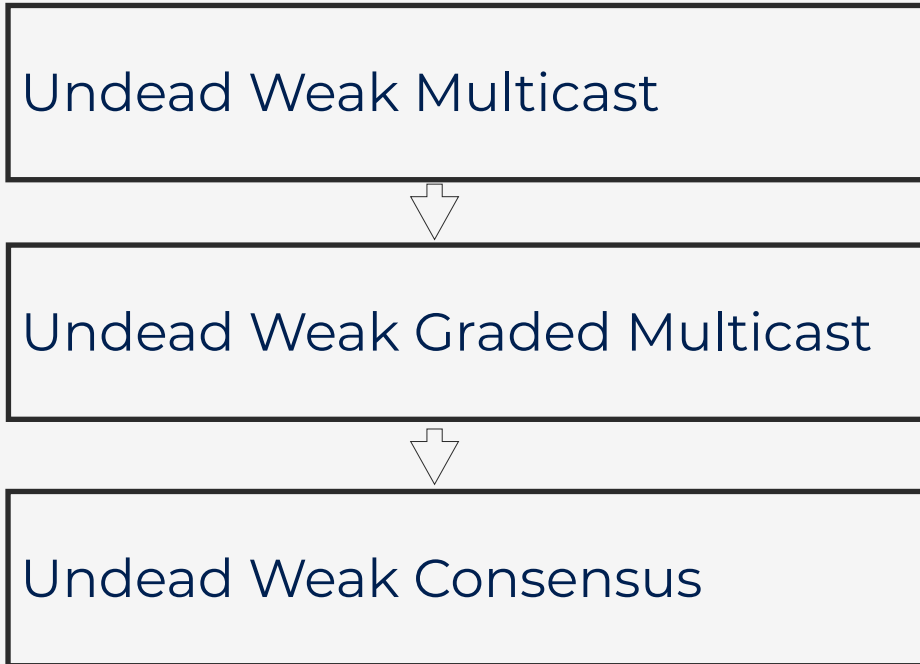
Undead Weak Multicast



Undead Weak Graded Multicast

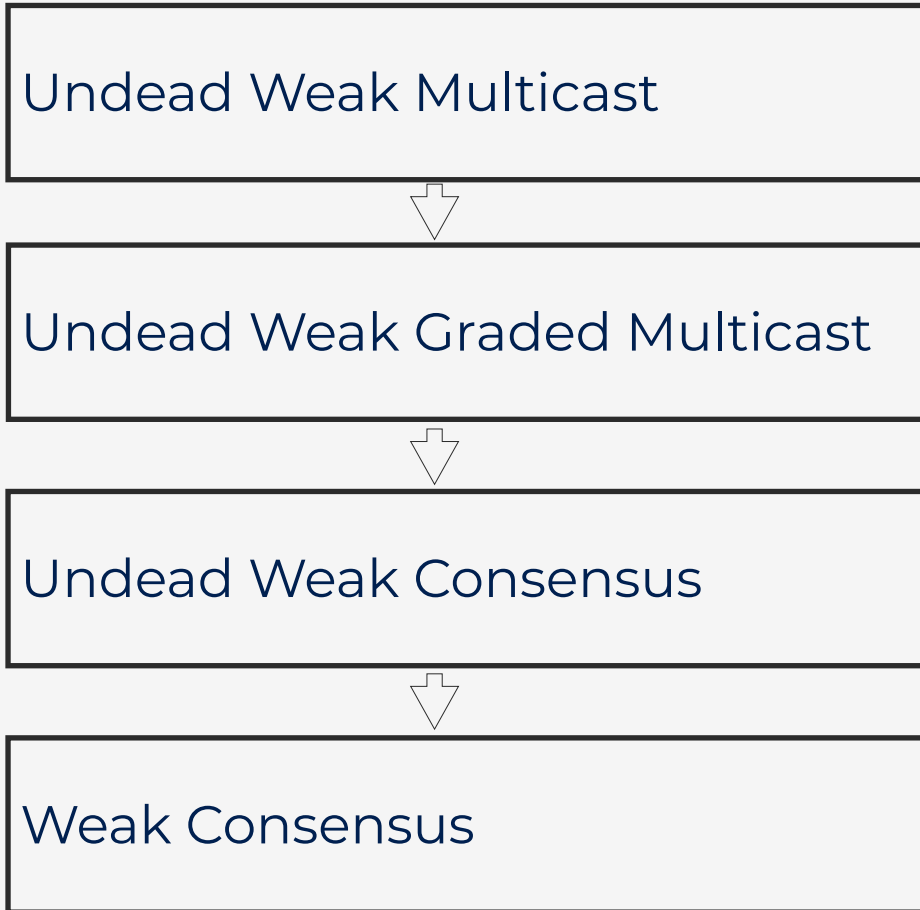


Our Starting Point: Zombies and Ghosts[LS2022]



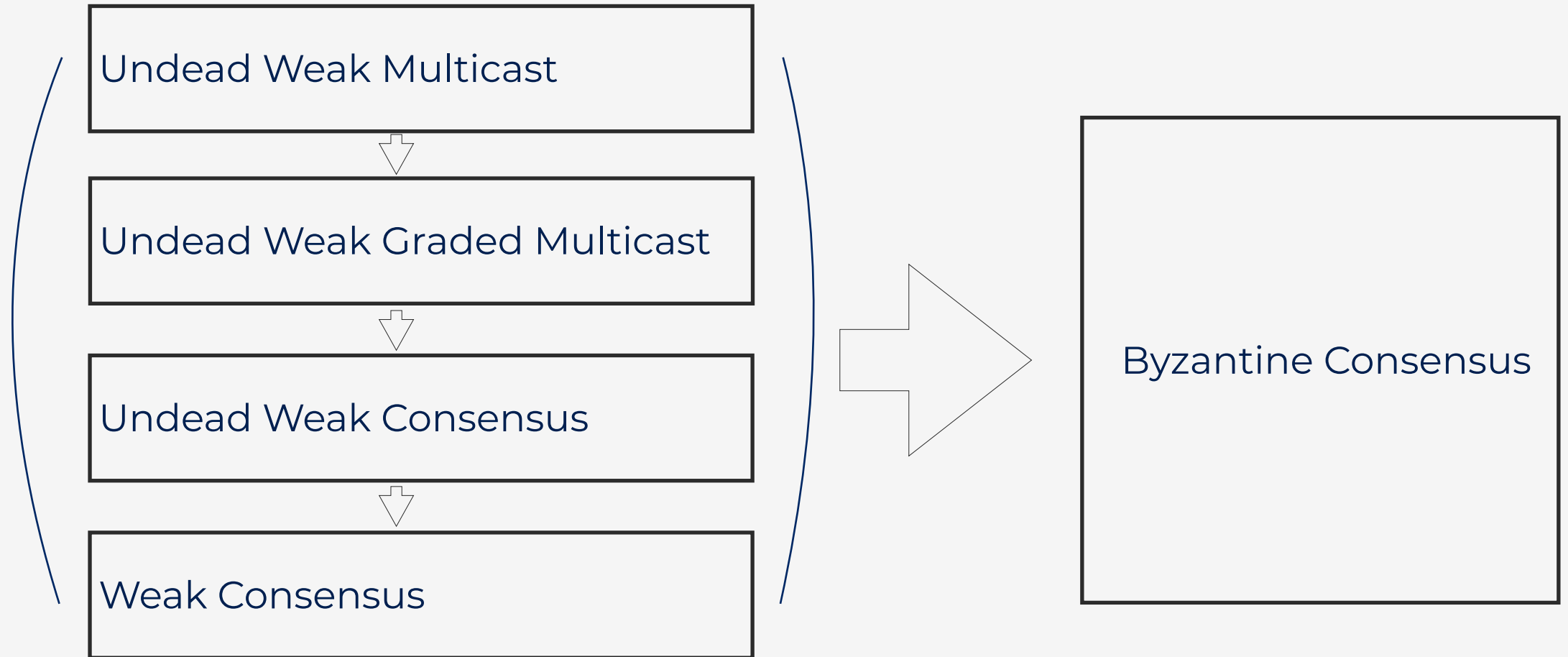


Our Starting Point: Zombies and Ghosts[LS2022]



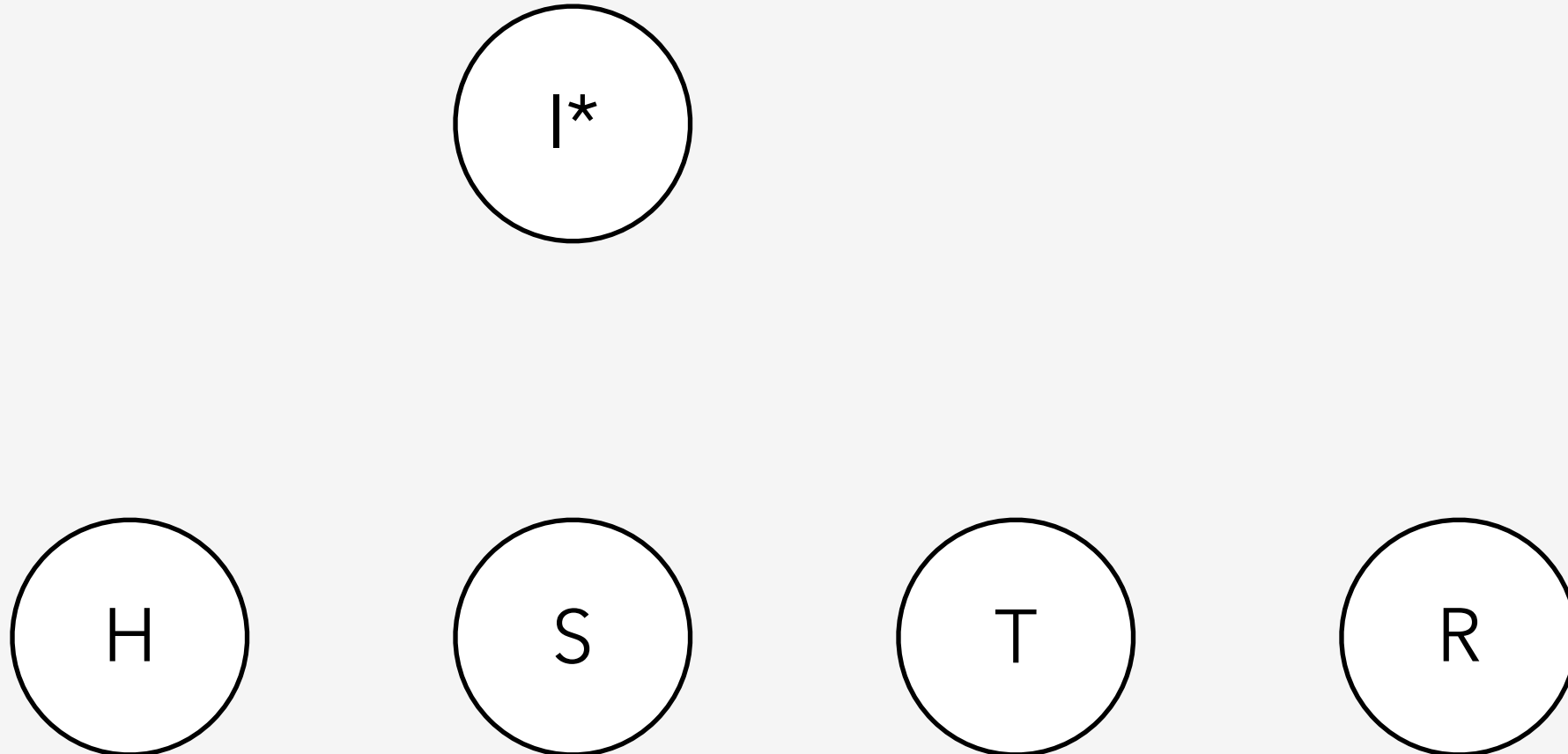


Our Starting Point: Zombies and Ghosts[LS2022]



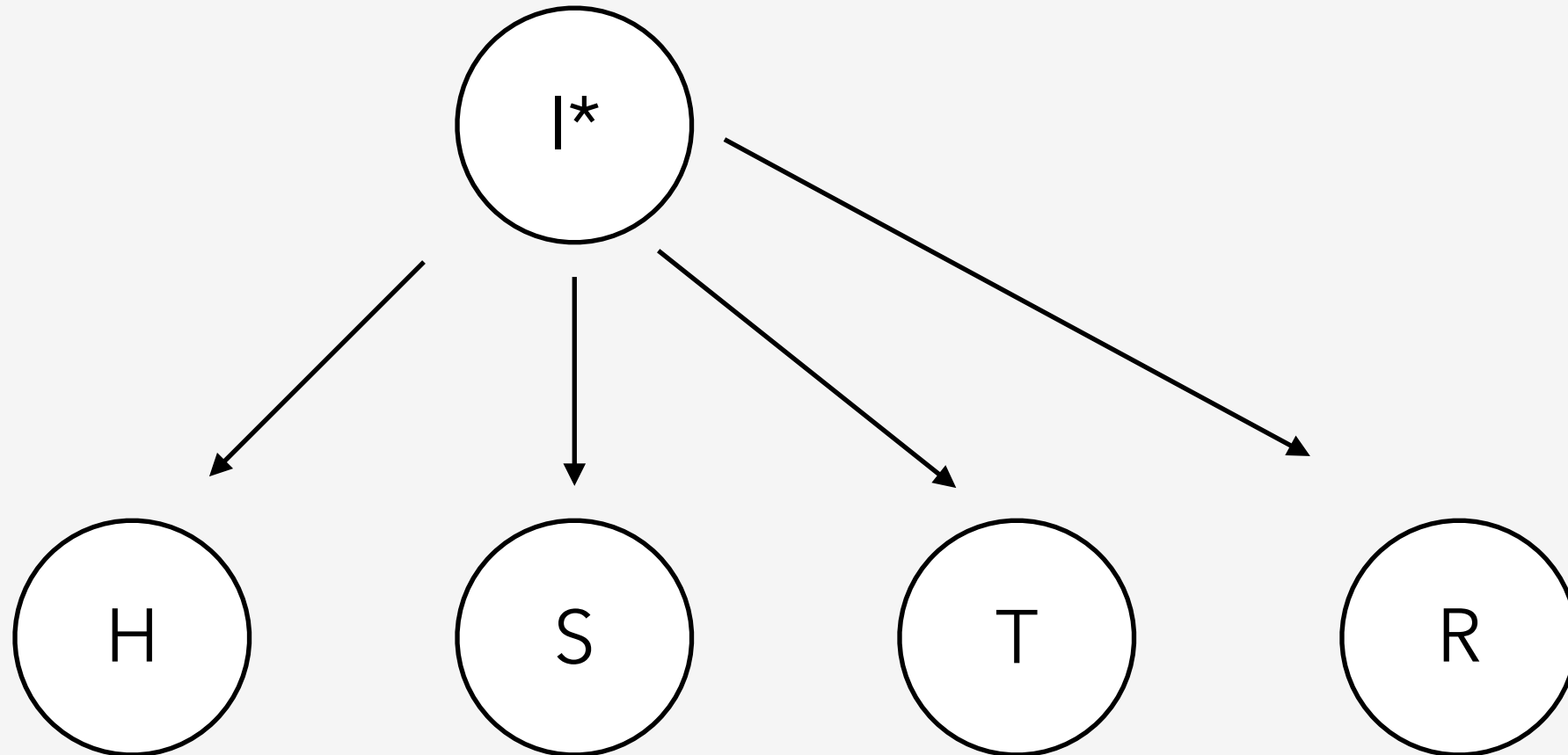


Undead Weak Multicast[LS23]



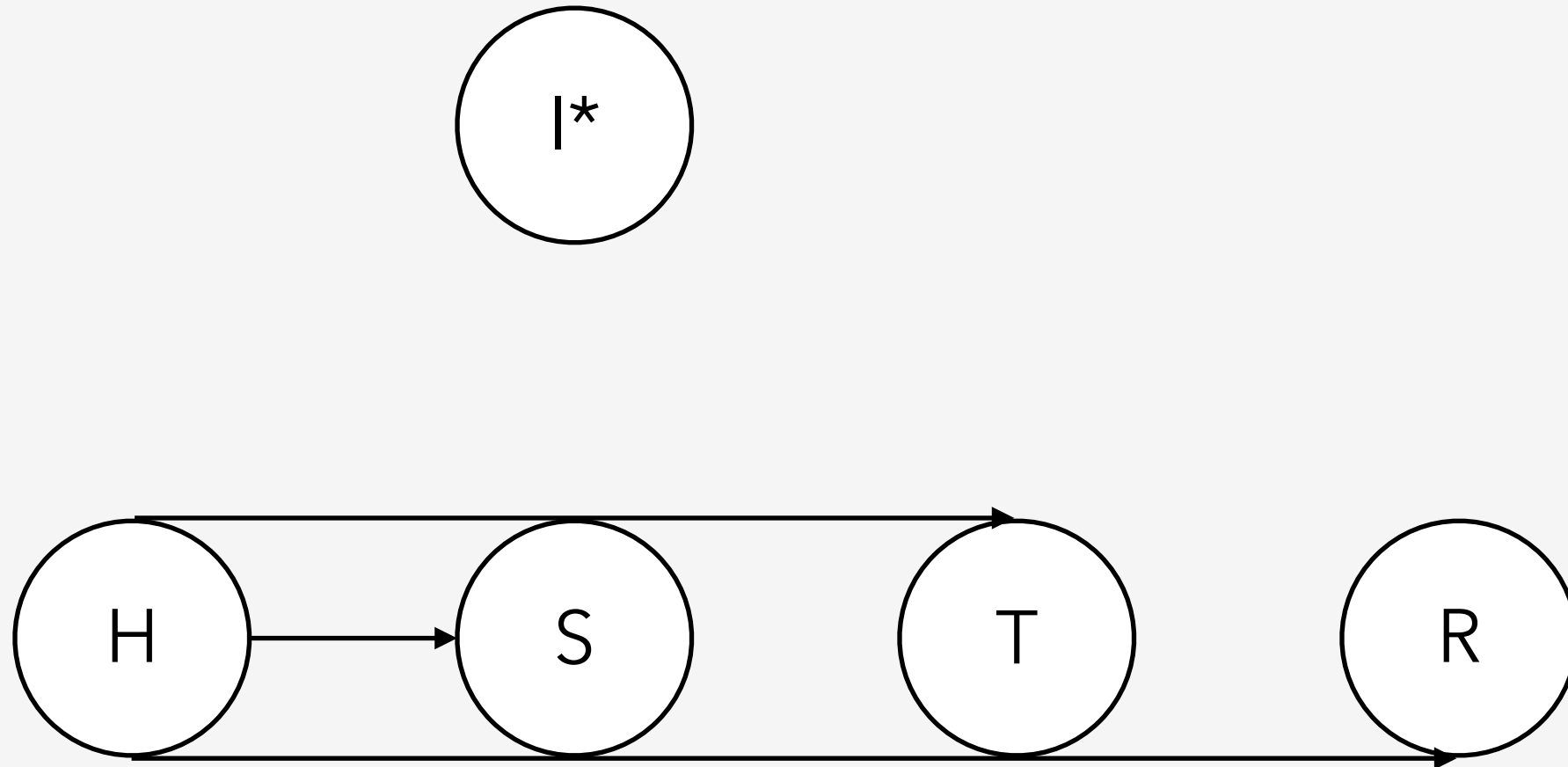


Undead Weak Multicast[LS23]



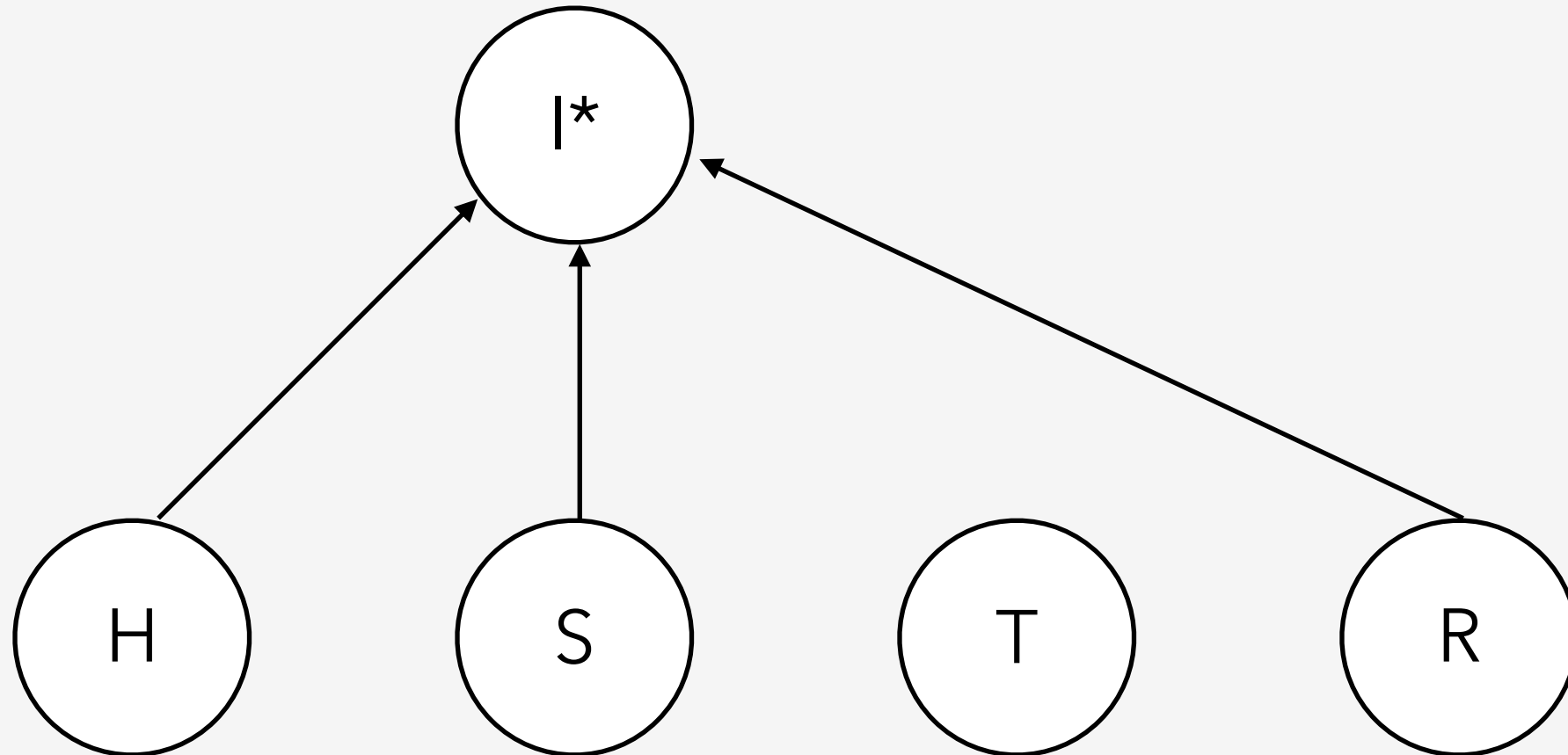


Undead Weak Multicast[LS23]



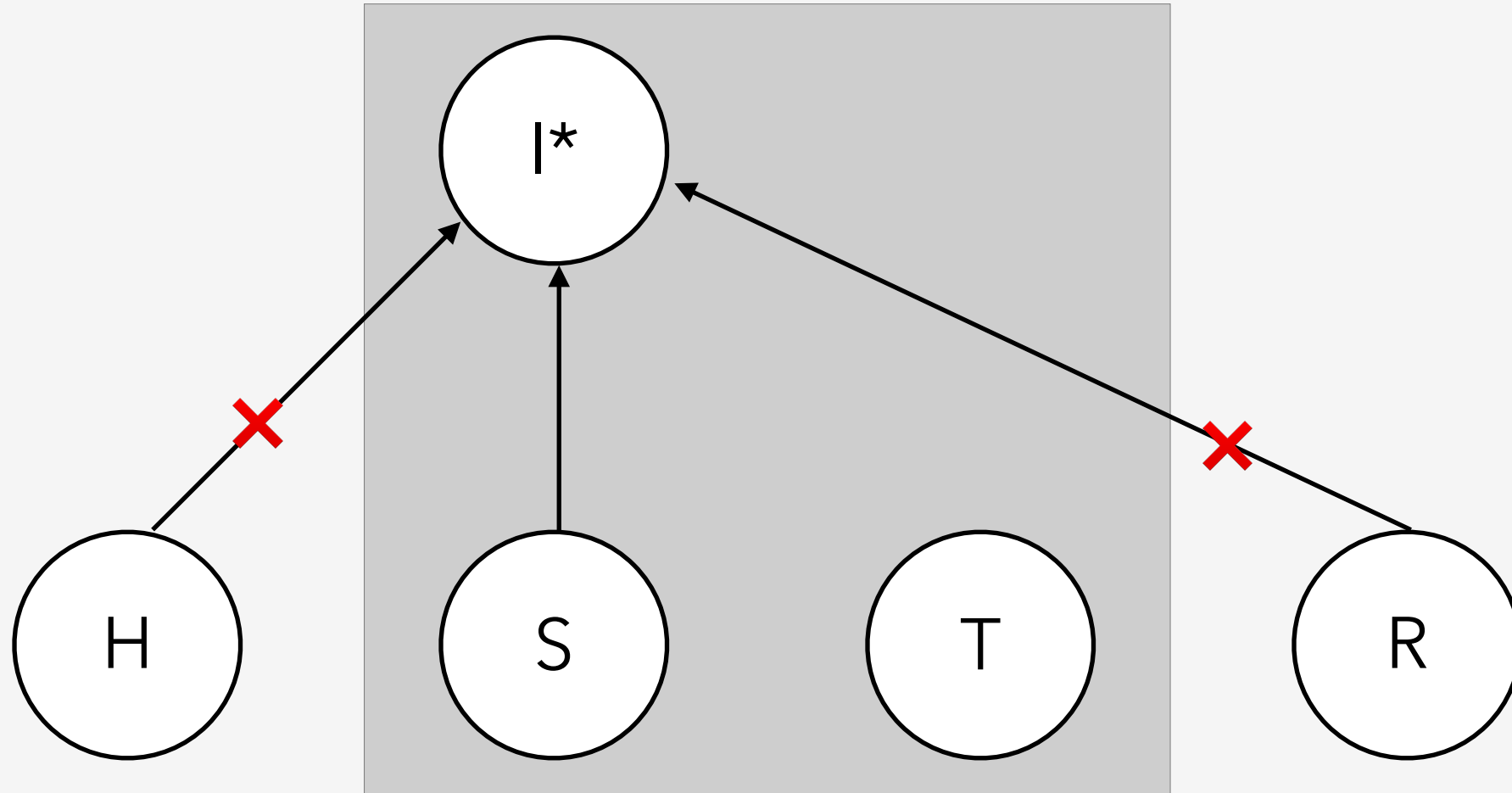


Undead Weak Multicast[LS23]



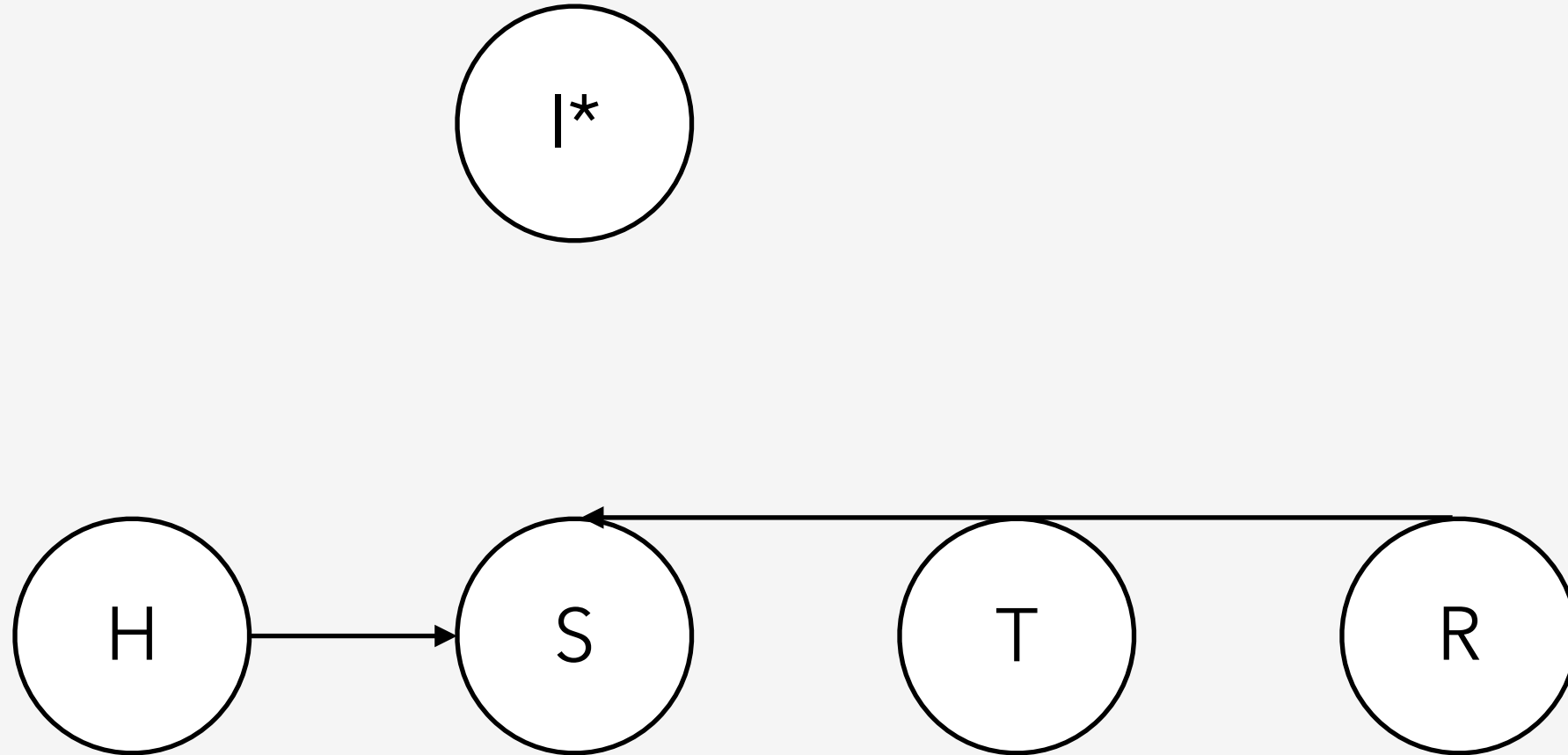


Failed to detect a Full-Omission Sender



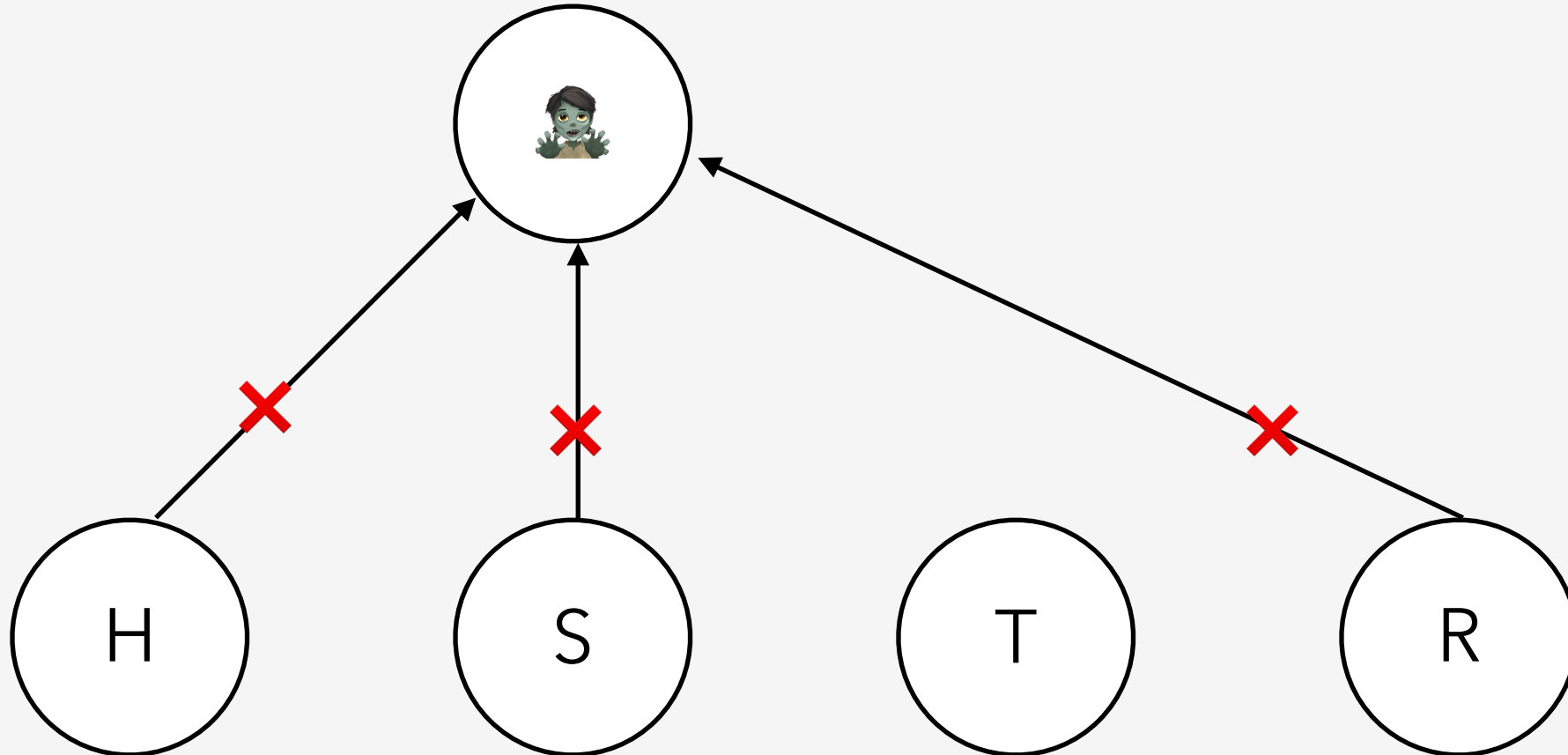


Our Solution Against Overlapping Faults



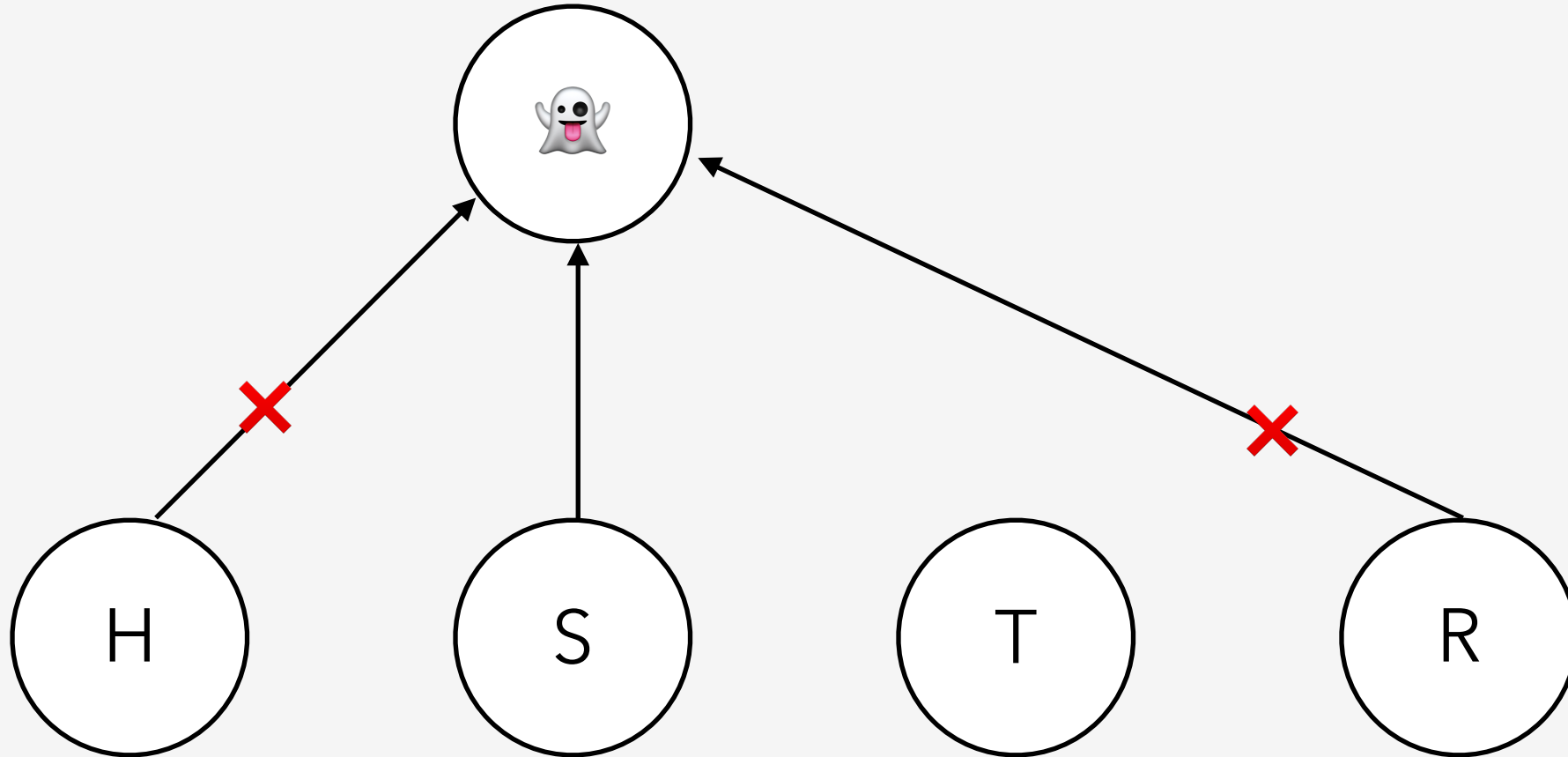


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Second Starting Point: Previous Lower Bound [ELT22]

If receive omissions are forced to become zombies and stop participating from the beginning of the protocol, there is no Byzantine Agreement Protocol with $2t + s + r \geq n$.

Closes the Door, Leaves a Window

Our Result: There is a Byzantine Agreement Protocol with $s + r = n$.



A Consensus Protocol with $s+r=n$ ($s < n$)



A Consensus Protocol with $s+r=n$ ($s < n$)

Undead Very Weak Multicast



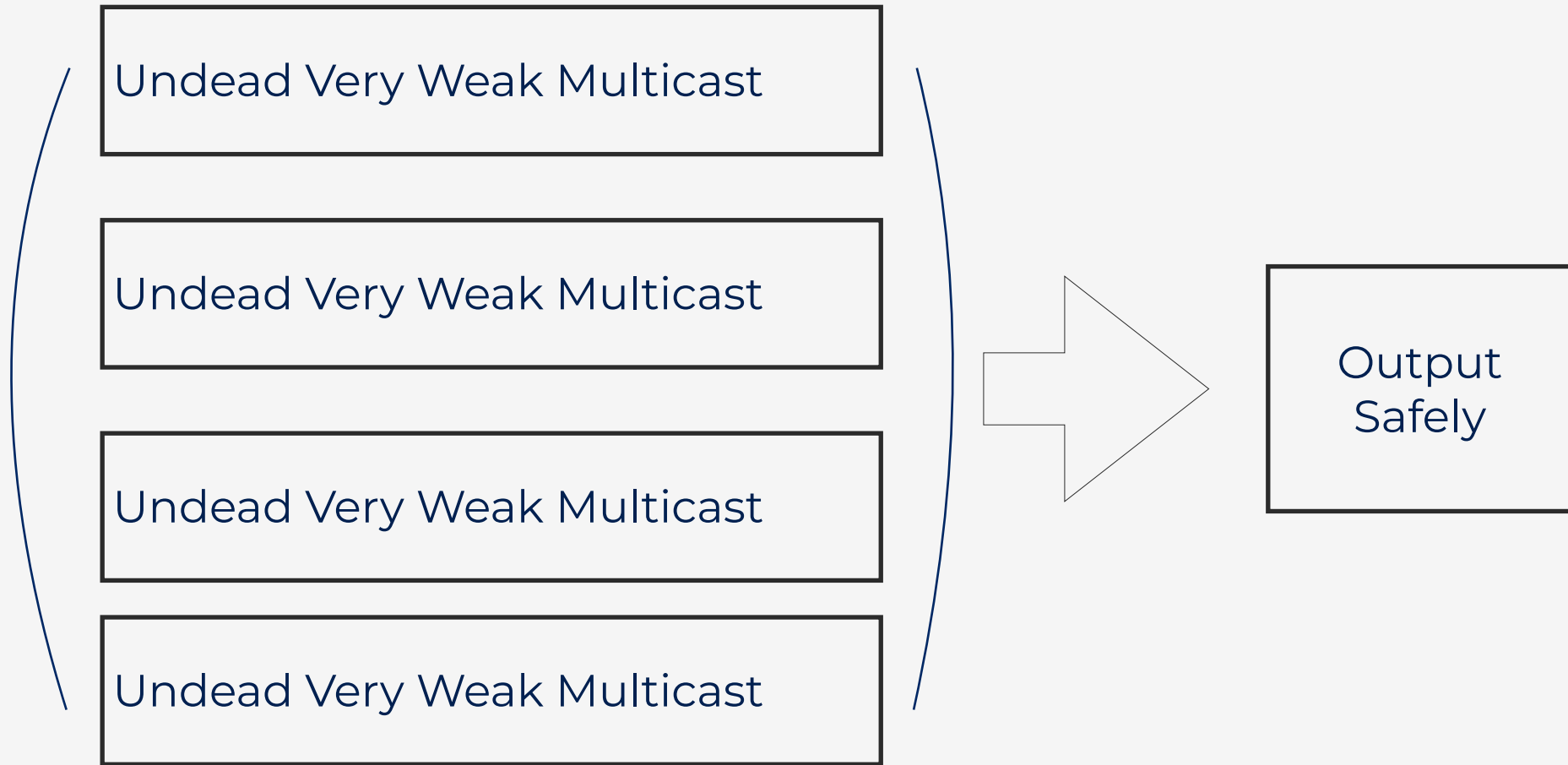
A Consensus Protocol with $s+r=n$ ($s < n$)



For $s+1$ Different Leaders



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Total Omission Setting ($s+r=n$)



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- **Optimal Resilience**

Impossibility proof for Agreement with $s + r > n$ (with overlapping).



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Thank you!