

**Amit Singh Bhati** 

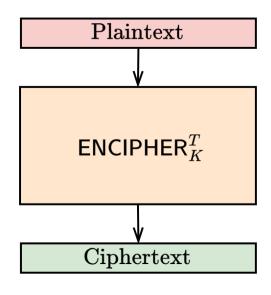
COSIC, KU Leuven; 3MI Labs, Belgium

Elena Andreeva TU Wien, Austria

# Tweakable Enciphering Modes (TEMs)



# Tweakable Enciphering Mode (TEM)[HR03]



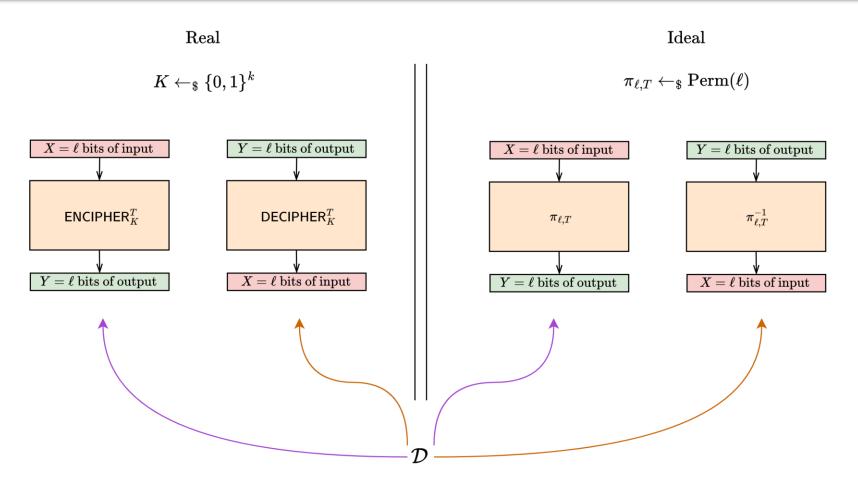
- 1. Length Preserving Encryption (LPE)
- 2. Generalization of (tweakable) block ciphers
  - Variable tweak and input size
- 3. NIST reintroduced it as accordion mode [CD+24]
- 4. Uses: disk-sector and full-disk encryption,

key-wrapping, robust AEAD [HKR17]

### What is a Secure TEM?



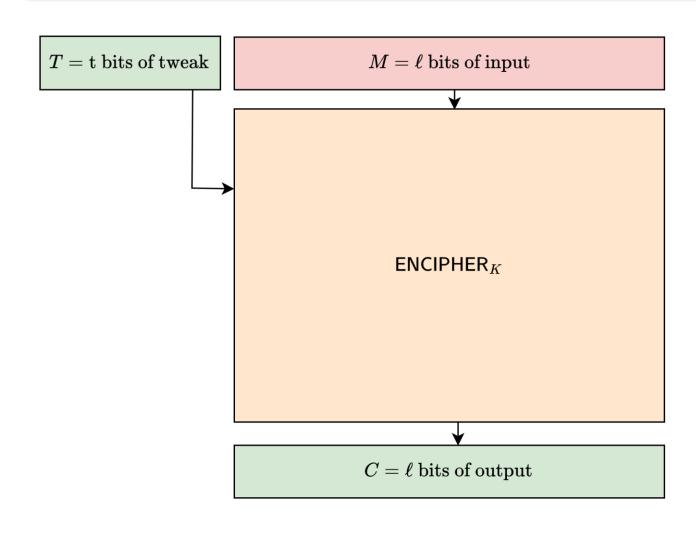
## TEM Security [HR03]

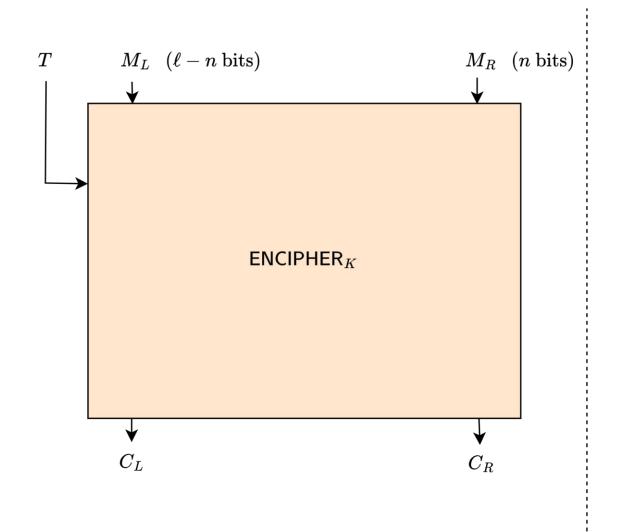


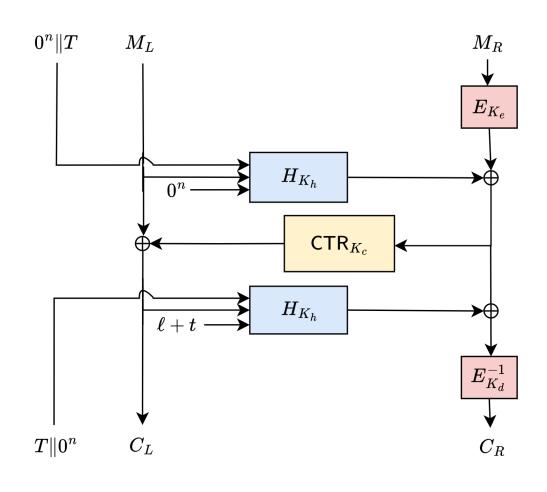
- Variable-Input-Length Strong Tweakable Pseudo-Random Permutation (VIL-STPRP)
- Analogous to IND-CCA encryption notion



- A TEM standardized for storage media encryption (2010, 2021)
- An efficient Hash-CTR-Hash design
- Built on AES and polynomial hashing
- Alias XCBv2fb

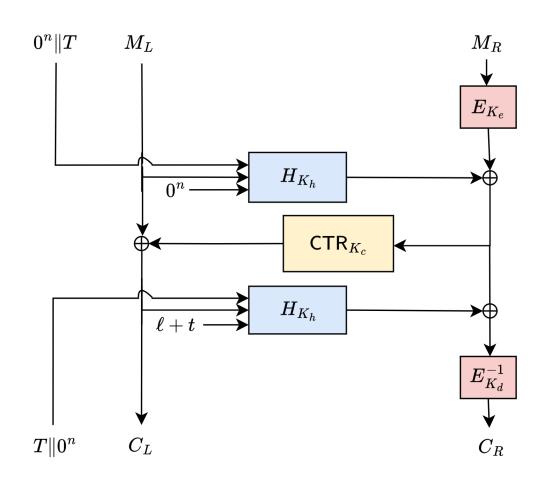






 $K_e, K_d, K_c, K_h \leftarrow K$ 

- Internal components
  - 1. CTR = Counter mode
  - 2. E = AES blockcipher
  - 3. H = a polynomial/rolling hashe.g., Polyval, GHASH



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- Internal components
  - 1. CTR = Counter mode
  - 2. E = AES blockcipher
  - 3. H = a polynomial/rolling hash e.g., Polyval, GHASH

$$\mathsf{Poly}_K(A_1\|A_2\|\ldots) = A_1K \oplus A_2K^2 \oplus \ldots$$



2010 IEEE standardized XCB-AES for storage media encryption

Padding attack found on XCB-AES [CHS13]

2021 IEEE updated XCB-AES standard with its padding-free variant XCBv2fb

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- Proven VIL-STPRP up to birthday bound for block-aligned messages [CHS13]
- Translates to security up to 2<sup>52-log</sup> queries

2021

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■ IEEE updated XCB-AES standard with its padding-free variant XCBv2fb

- Proven VIL-STPRP up to birthday bound for block-aligned messages [CHS13]
- Translates to security up to 2<sup>52-logl</sup> queries

We break XCB-AES's VIL-STPRP, STPRP and SPRP security in 2 queries

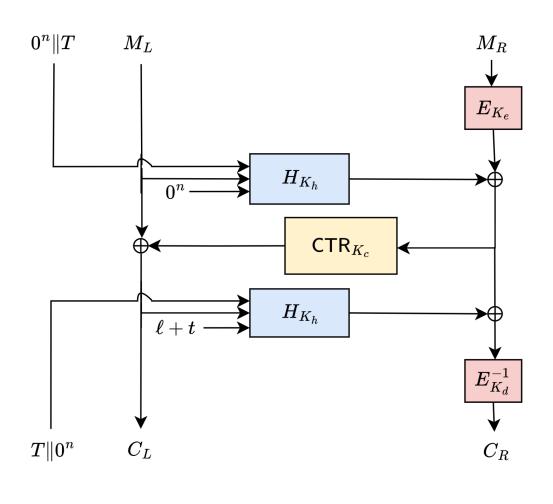
Our attack applies to all other XCB-style modes as well

2021

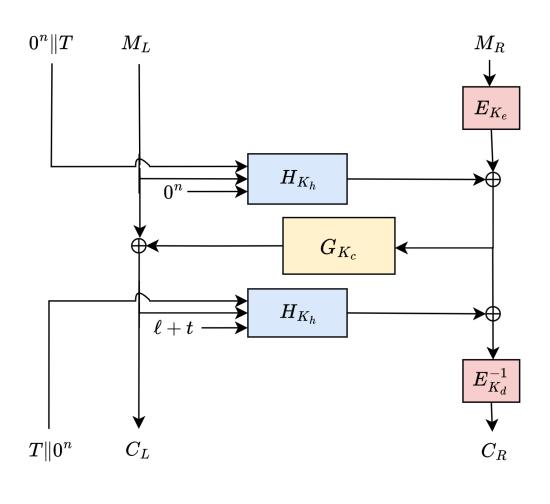
2024

# Our Result 1: A 2-Query Plaintext Recovery Attack

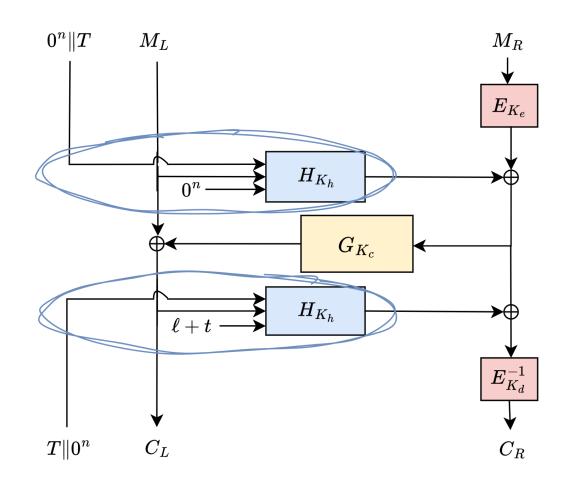




 $K_e, K_d, K_c, K_h \leftarrow K$ 



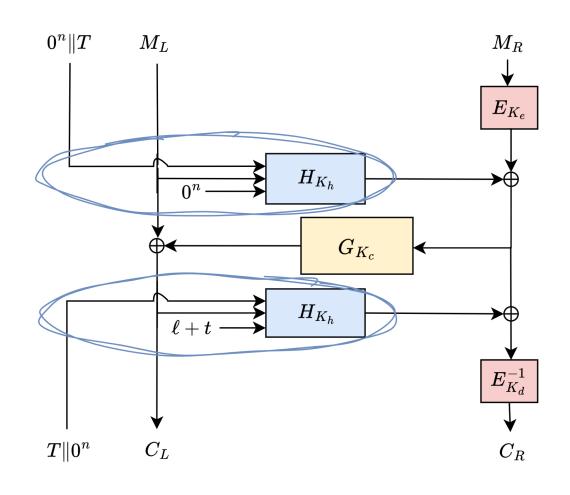
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$$K_e, K_d, K_c, K_h \leftarrow K$$

$$egin{aligned} ullet & H_{K_h}(0^n \| T, M_L, 0^n) \ &= \mathsf{Poly}_{K_h}(0^n \| \mathsf{pad}_n(T) \| \mathsf{pad}_n(M_L) \| 0^n) \end{aligned}$$

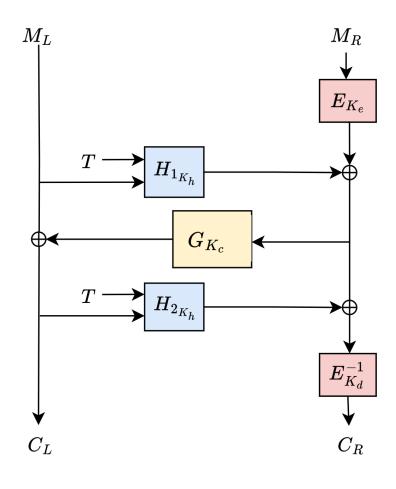
$$egin{aligned} ullet & H_{K_h}(T\|0^n,C_L,\ell+t) \ &= \mathsf{Poly}_{K_h}(\mathsf{pad}_n(T)\|0^n\|\mathsf{pad}_n(C_L)\|\mathsf{bin}_n(\ell+t)) \end{aligned}$$



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$$egin{aligned} \mathsf{Poly}_K(A_1 \| A_2 \| (A_3 \oplus \Delta) \| A_4) &= A_1 K \oplus A_2 K^2 \oplus (A_3 \oplus \Delta) K^3 \oplus A_4 K^4 \ &= A_1 K \oplus A_2 K^2 \oplus A_3 K^3 \oplus A_4 K^4 \ \oplus \ \Delta K^3 \ &= \mathsf{Poly}_K(A_1 \| A_2 \| A_3 \| A_4) \ \oplus \ \mathsf{Poly}_K(0^n \| 0^n \| \Delta \| 0^n) \end{aligned}$$

$$egin{aligned} H_1(K_h,T,M_L\oplus \Delta) &= \mathsf{Poly}_{K_h}(0^n\|\mathsf{pad}_n(T)\|\mathsf{pad}_n(M_L\oplus \Delta)\|0^n) \ &= \mathsf{Poly}_{K_h}(0^n\|\mathsf{pad}_n(T)\|\mathsf{pad}_n(M_L)\|0^n) \ \oplus \ \mathsf{Poly}_{K_h}(0^n\|0^{|\mathsf{pad}_n(T)|}\|0^x\|\Delta\|0^y\|0^n) \end{aligned}$$

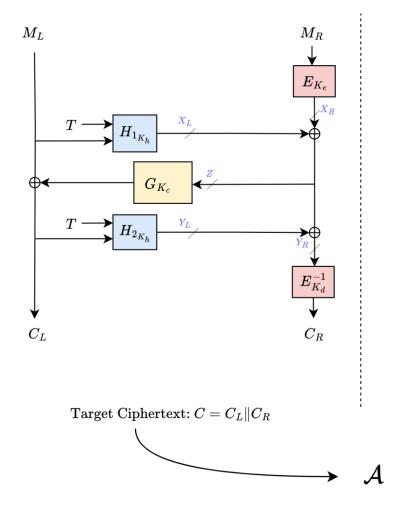
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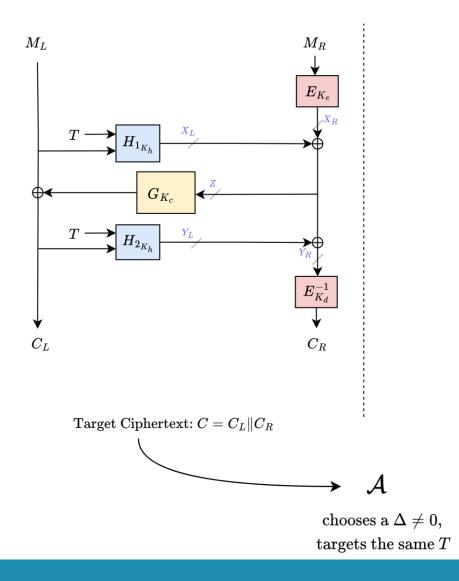
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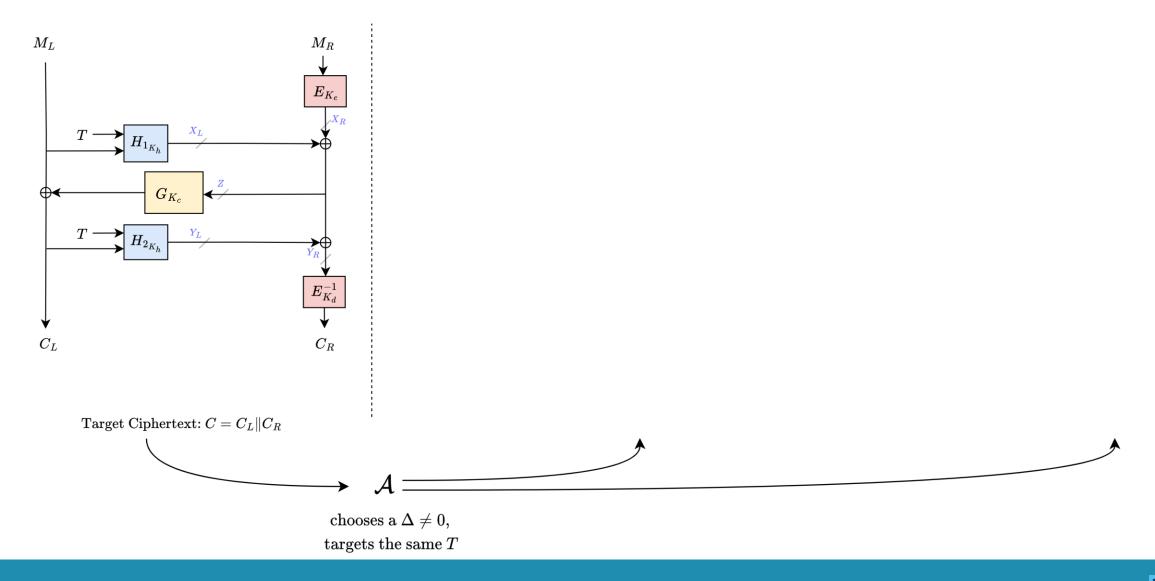
$$egin{aligned} H_2(K_h,T,C_L\oplus\Delta) &= \mathsf{Poly}_{K_h}(\mathsf{pad}_n(T)\|0^n\|\mathsf{pad}_n(C_L\oplus\Delta)\|\mathsf{bin}_n(\ell+t)) \ &= \mathsf{Poly}_{K_h}(\mathsf{pad}_n(T)\|0^n\|\mathsf{pad}_n(C_L)\|\mathsf{bin}_n(\ell+t)) \ \oplus \ \mathsf{Poly}_{K_h}(0^{|\mathsf{pad}_n(T)|}\|0^n\|0^x\|\Delta\|0^y\|0^n) \end{aligned}$$

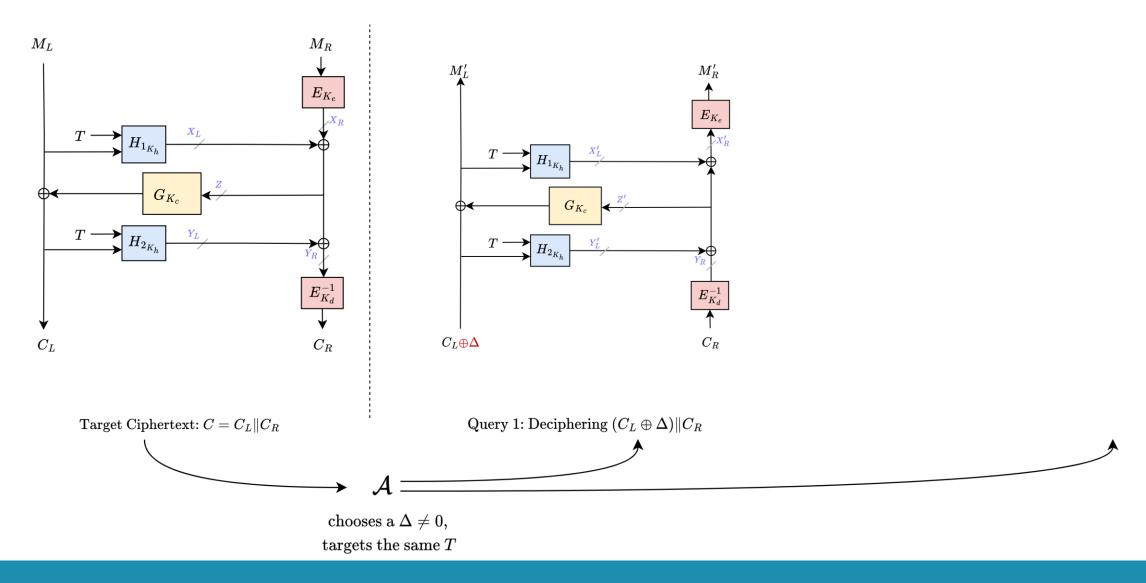
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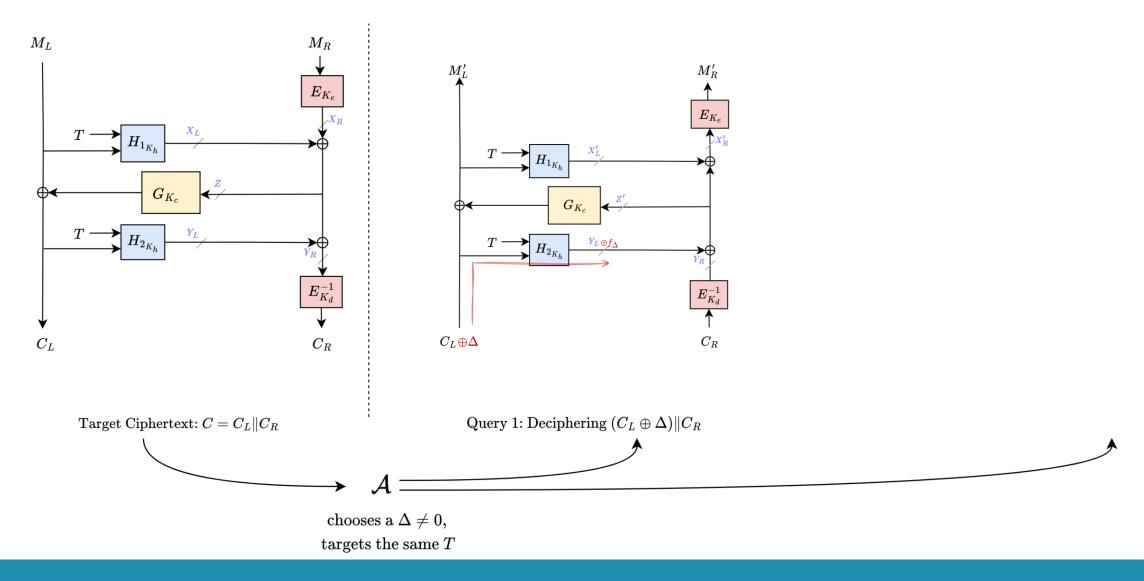
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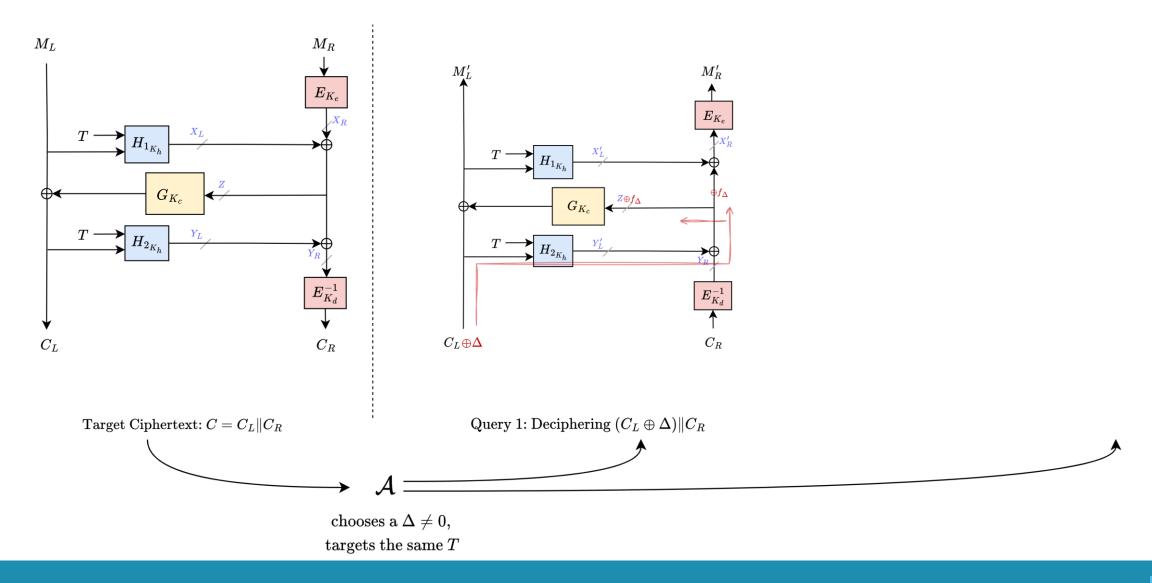


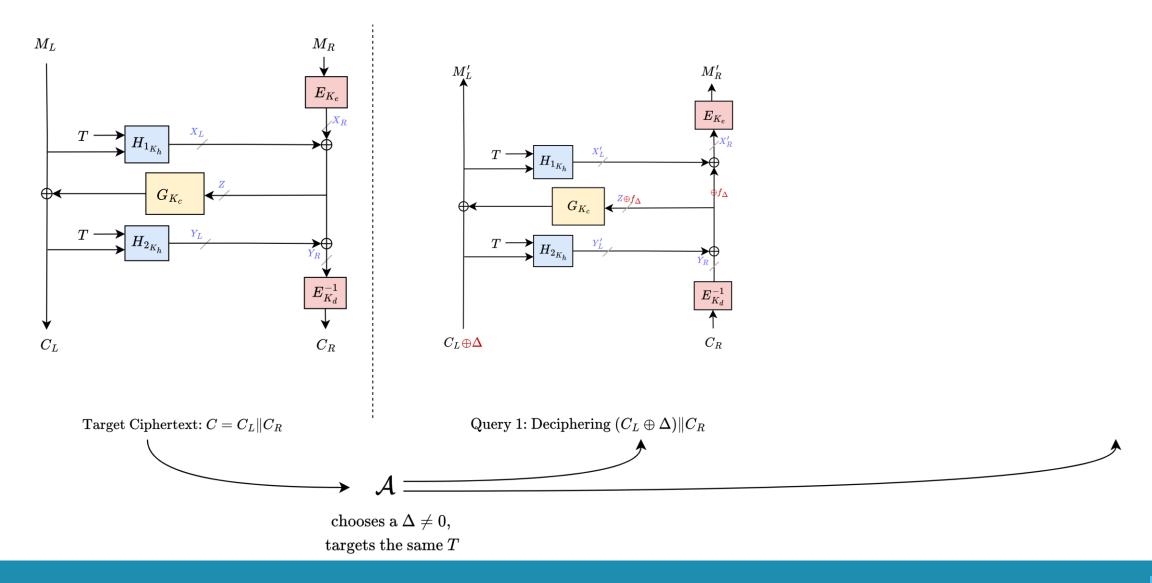


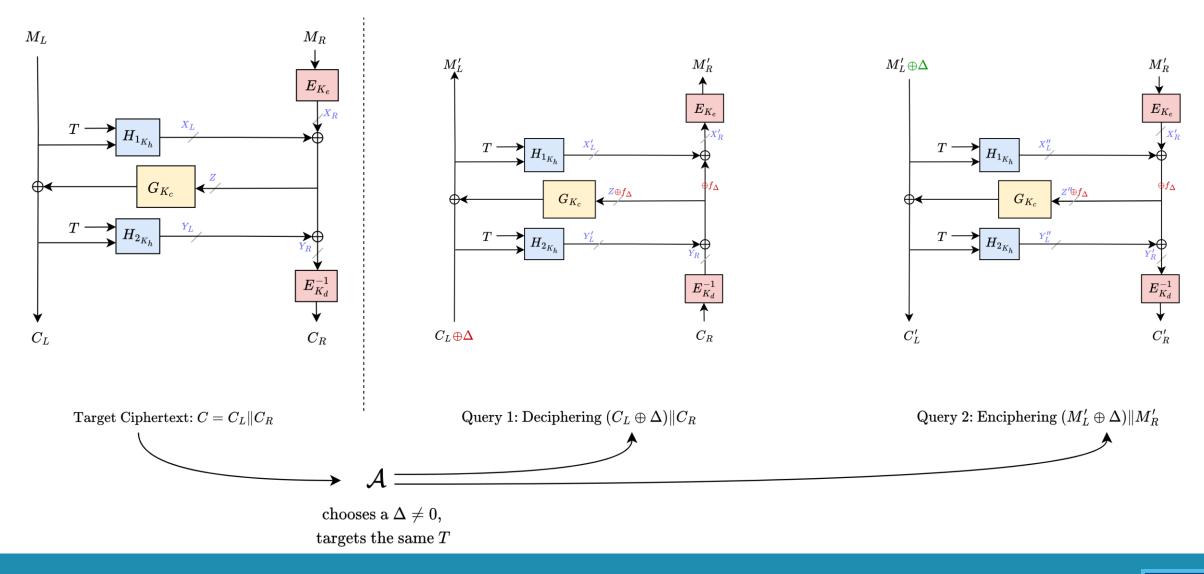


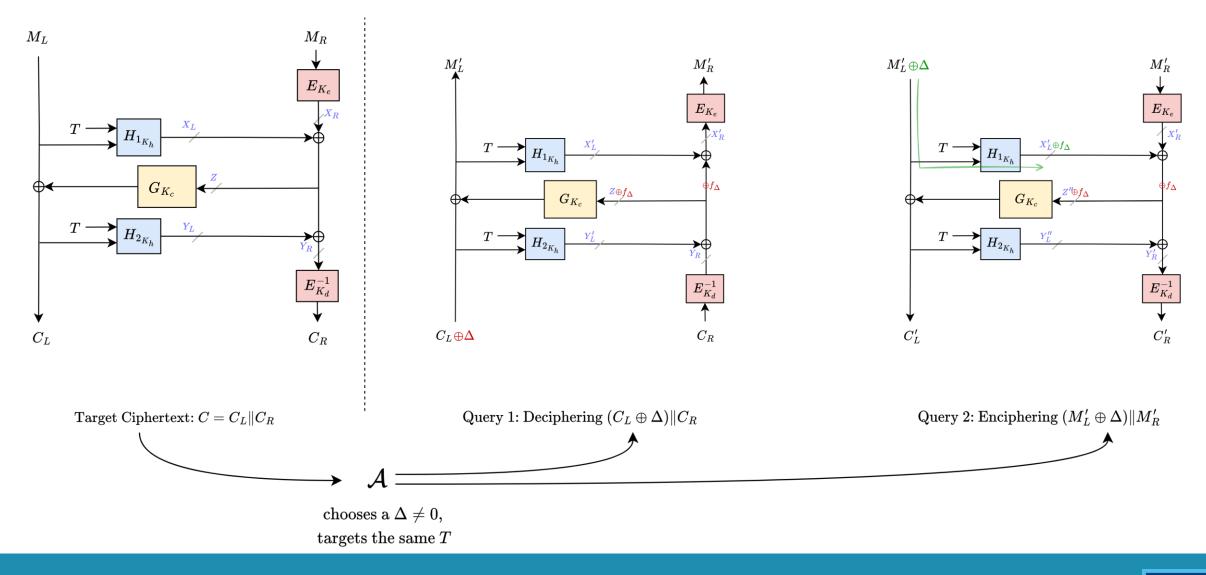


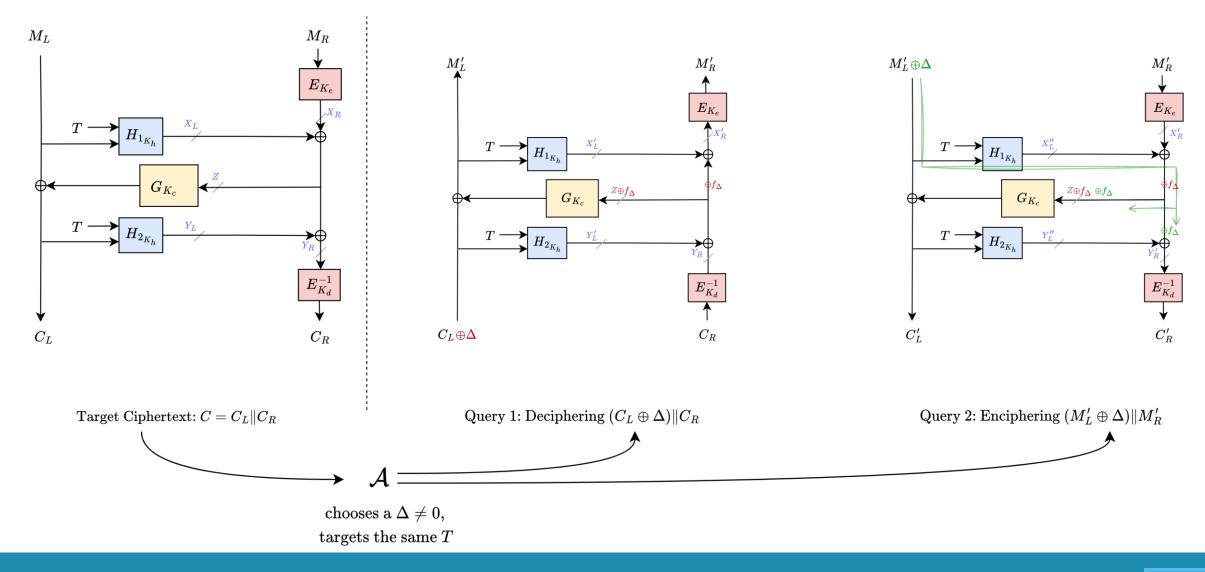


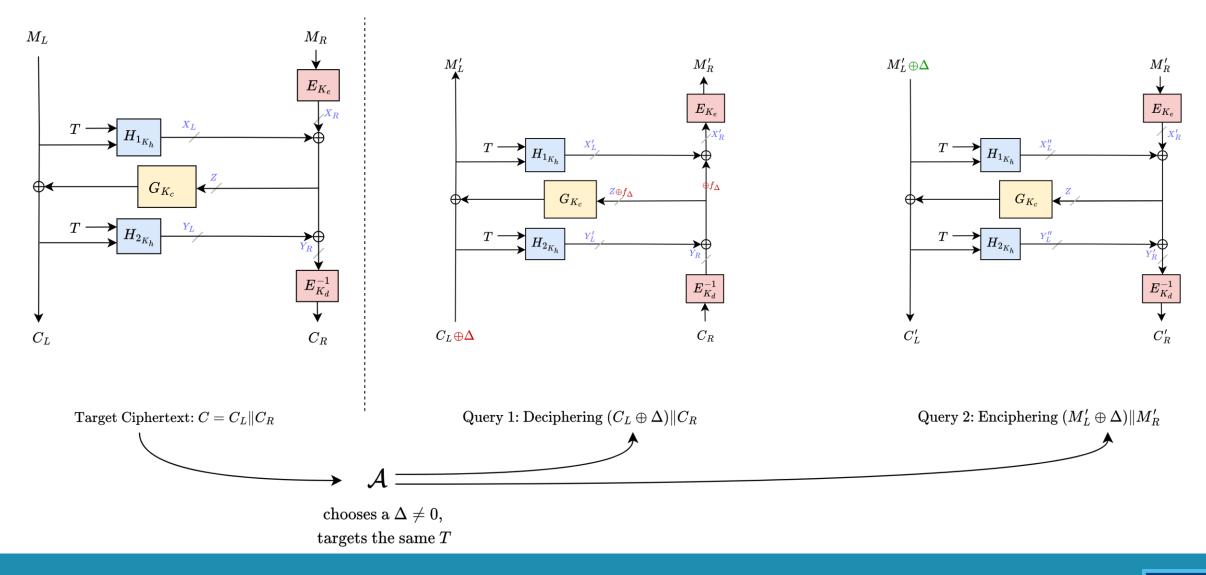


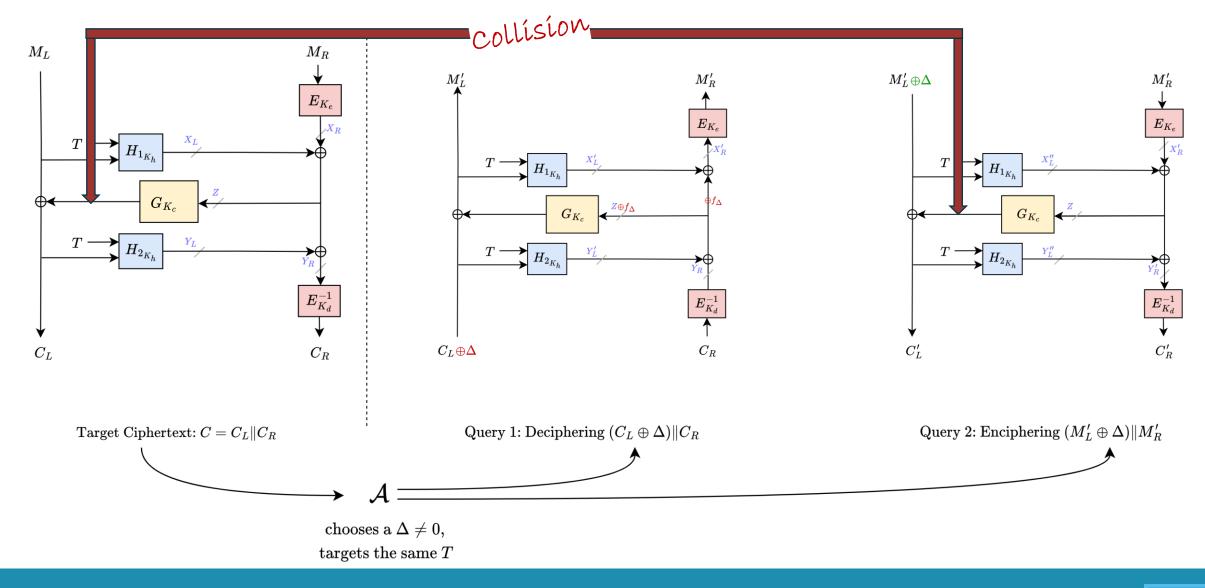


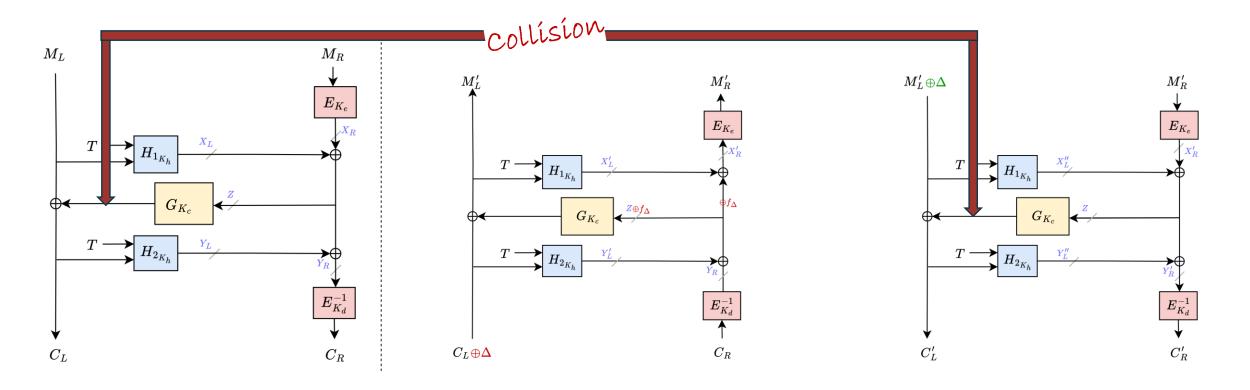




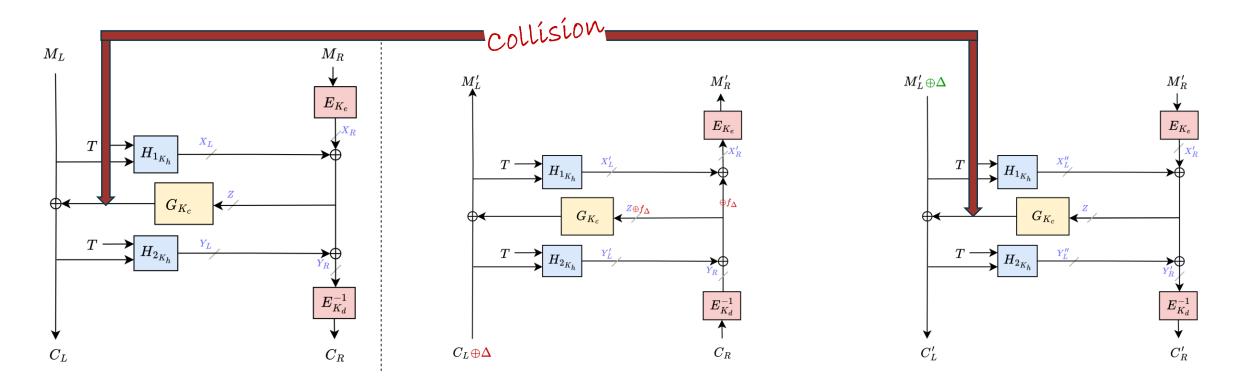








$$M_L \oplus C_L = (M_L' \oplus \Delta) \oplus C_L'$$



$$M_L\oplus C_L=(M_L'\oplus\Delta)\oplus C_L'$$
  $Message$   $M_L=(M_L'\oplus\Delta)\oplus C_L'\oplus C_L$  Recovered

# Why Does This Work?



## Root Cause: A Shared Difference Property



 $ullet H_{\mathrm{sum}}(K,T,M,C) = H_1(K,T,M) \oplus H_2(K,T,C)$ 

- $ullet H_{\mathrm{sum}}(K,T,M,C) = H_1(K,T,M) \oplus H_2(K,T,C)$
- $\bullet \quad H_{\mathrm{sum}}(K,T,M\oplus {\color{red}\Delta},C\oplus {\color{black}\Delta}) = H_1(K,T,M\oplus {\color{red}\Delta}) \oplus H_2(K,T,C\oplus {\color{black}\Delta})$

- $ullet H_{ ext{sum}}(K,T,M,C) = H_1(K,T,M) \oplus H_2(K,T,C)$
- $egin{aligned} ullet H_{ ext{sum}}(K,T,M \oplus \Delta,C \oplus \Delta) &= H_1(K,T,M \oplus \Delta) \oplus H_2(K,T,C \oplus \Delta) \ &= H_1(K,T,M) \oplus oldsymbol{f_\Delta} \oplus H_2(K,T,C) \oplus oldsymbol{f_\Delta} \ &= H_1(K,T,M) \oplus H_2(K,T,C) \end{aligned}$

- $ullet H_{\mathrm{sum}}(K,T,M,C) = H_1(K,T,M) \oplus H_2(K,T,C)$
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$$H_{\mathrm{sum}}(K,T,M{\oplus}{\Delta},C{\oplus}{\Delta}) \ = H_{\mathrm{sum}}(K,T,M,C)$$

due to separability of polynomial hash

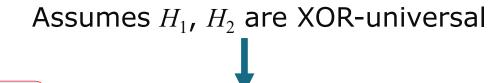
Our attack was first disclosed on 13<sup>th</sup> Feb 2024 in our CRYPTO'24 submission. Had quite a rollercoaster with a case of established reviewer misconduct during submissions, before making it to CRYPTO'25.



Existing proofs based on XOR-universal hash functions

Assumes  $H_1$ ,  $H_2$  are XOR-universal Implies  $H_{\mathrm{sum}}$  is universal CTR IV unpredictable and hard to collide Independent and random CTR key streams up to birthday bound

Existing proofs based on XOR-universal hash functions



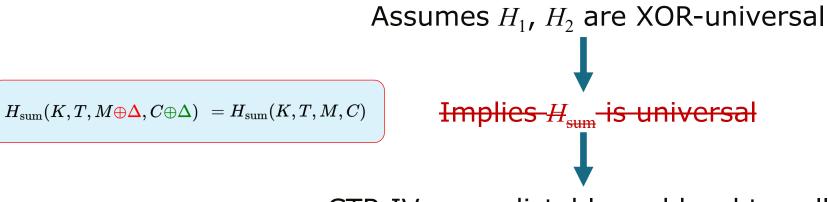
$$H_{\mathrm{sum}}(K,T,M{\oplus}{\Delta},C{\oplus}{\Delta}) = H_{\mathrm{sum}}(K,T,M,C)$$

Implies  $H_{\text{sum}}$  is universal

CTR IV unpredictable and hard to collide

Independent and random CTR key streams up to birthday bound

Existing proofs based on XOR-universal hash functions

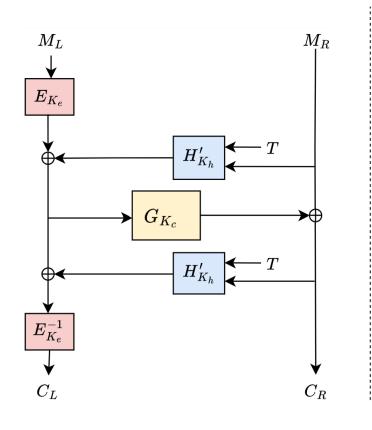


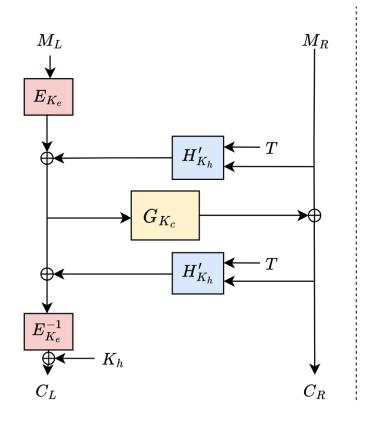
CTR IV unpredictable and hard to collide

Independent and random CTR key streams up to birthday bound

# Our Result 2: Applications of Shared Difference Attack to Other XCB-style TEMs

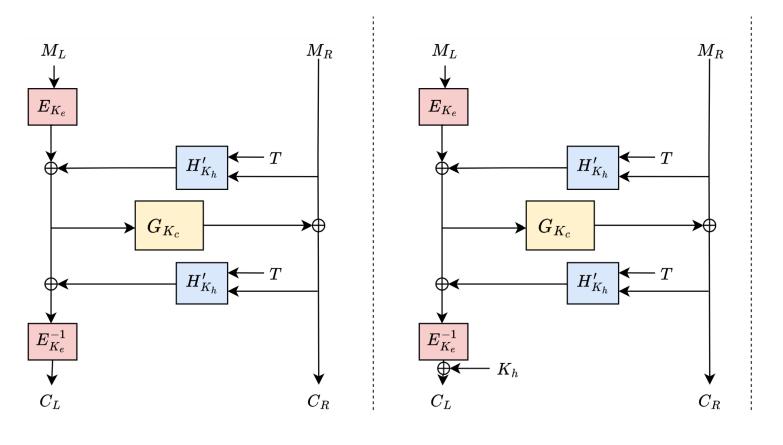


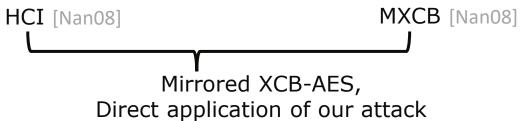


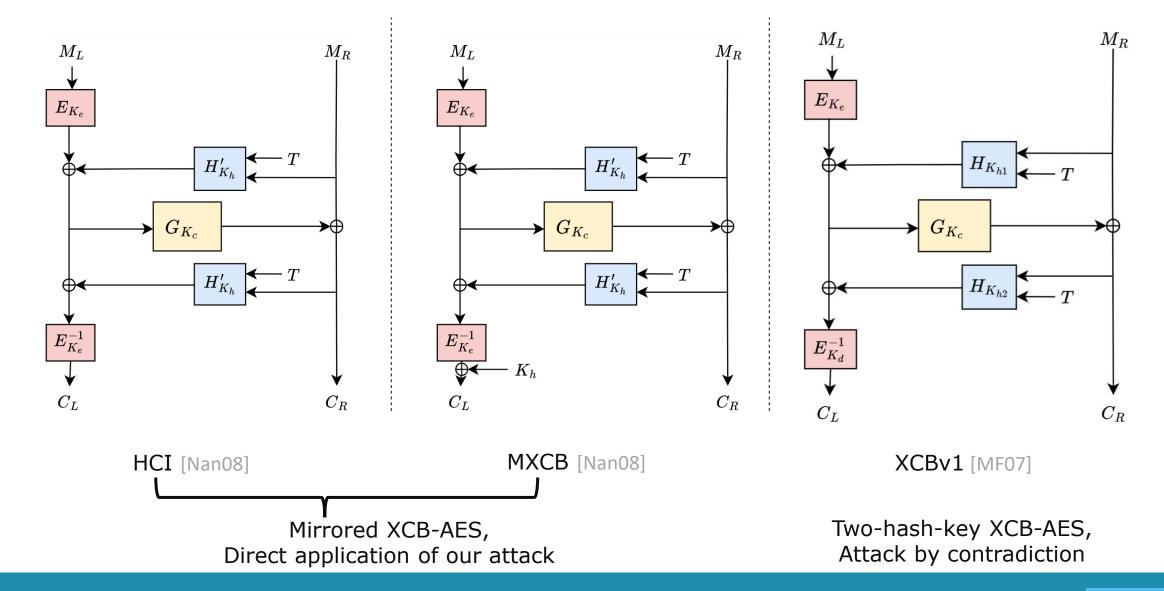


HCI [Nan08]

MXCB [Nan08]







# **Summary of Results**

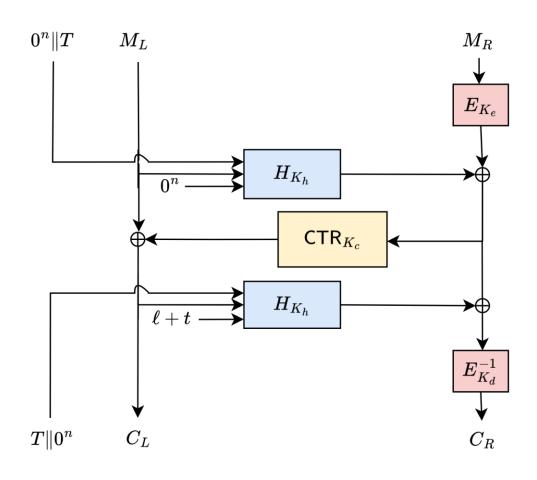
Attack	Schemes	Message length	Attack type	# queries
LRW1 CCA attack by Khairallah [Kha23]	XCBv1, XCBv2, XCBv2fb	n bits	recovery of n bits	3
Shared difference attack [This work]	XCBv1	all $m > n$ bits	recovery of $m-n$ bits	4
	XCBv2, XCBv2fb, HCI, MXCB	all $m > n$ bits	recovery of $m-n$ bits	2
Flipped parts attack [This work]	HCI	all $m > n$ bits	distinguishing attack	3

m can be arbitrarily large

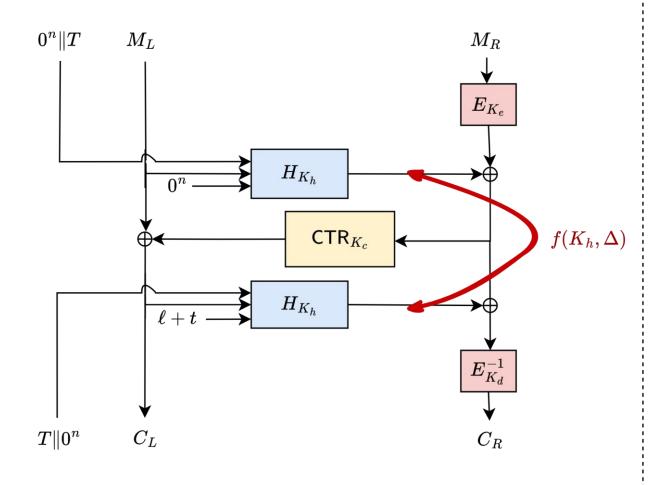


#### Countermeasures for XCB

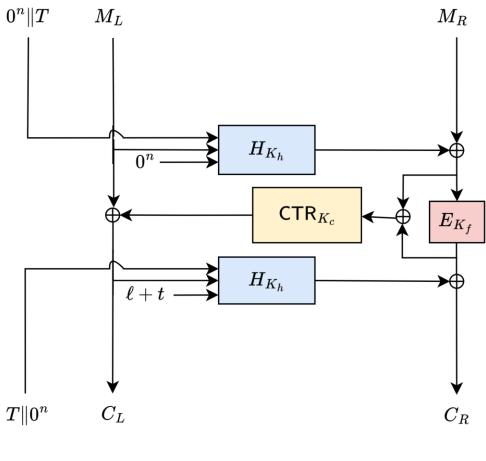




XCB style

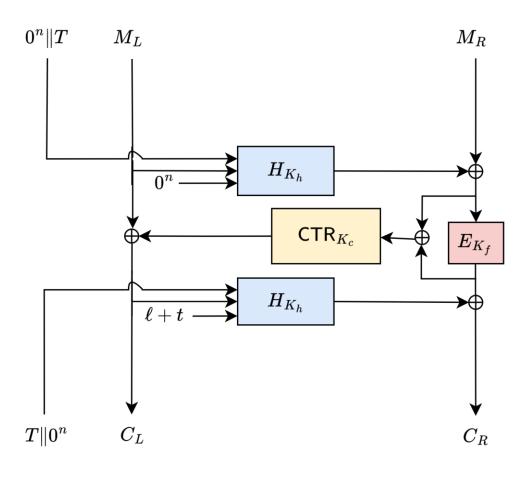


- XCB style
  - Insecure in current form



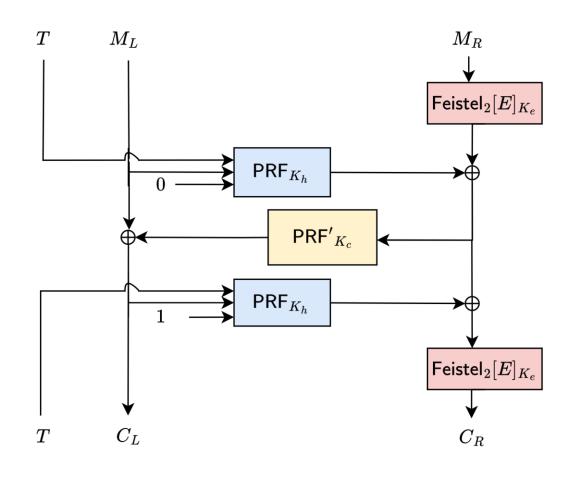
Avoid the Sum

- XCB style
  - Insecure in current form



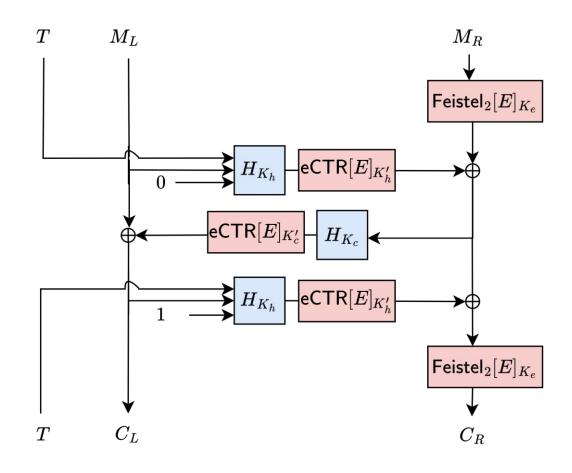
Avoid the Sum

- XCB style
  - Insecure in current form
- HCTR2 style [CHB23]
  - AES-128, PolyVal
  - 64-bit STPRP security
  - 1.1 cpb on Gracemont



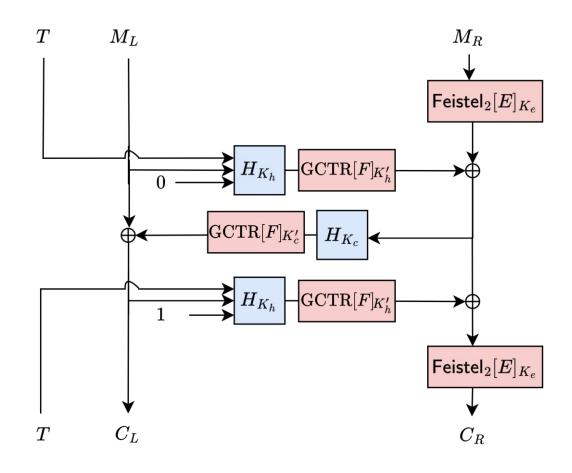
Use Inseparable Hashes

- XCB style
  - Insecure in current form
- HCTR2 style [CHB23]
  - AES-128, PolyVal
  - 64-bit STPRP security
  - 1.1 cpb on Gracemont
- GEM style [BVA24]



Use Inseparable Hashes

- XCB style
  - Insecure in current form
- HCTR2 style [CHB23]
  - AES-128, PolyVal
  - 64-bit STPRP security
  - 1.1 cpb on Gracemont
- GEM style [BVA24]
  - AES-128, PolyVal
  - 128-bit STPRP security
  - 1.4 cpb on Gracemont



Use Inseparable Hashes

- XCB style
  - Insecure in current form
- HCTR2 style [CHB23]
  - AES-128, PolyVal
  - 64-bit STPRP security
  - 1.1 cpb on Gracemont
- GEM style [BVA24]
  - Butterknife [ACL+22], PolyVal
  - 128-bit STPRP security
  - 1.1 cpb on Gracemont

#### Conclusion



#### Conclusion

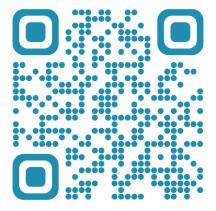
- 1. Introduced shared difference attack against XCB
  - Breaking SPRP, STPRP, VIL-STPRP security of all XCB variants
  - Including XCB-AES; a 15 year old IEEE standard
- 2. Pinpointed exact flaw in existing analyses
- 3. Presented some countermeasures HCTR2 and GEM

Impact: IEEE has officially removed XCB-AES from 1619.2 standard

Takeaway: 1. Efforts toward TEM design and analysis through NIST's accordion initiative are essential

2. To protect innovation, we must enforce clear professional consequences for reviewer misconduct





(ia.cr/2024/1554)

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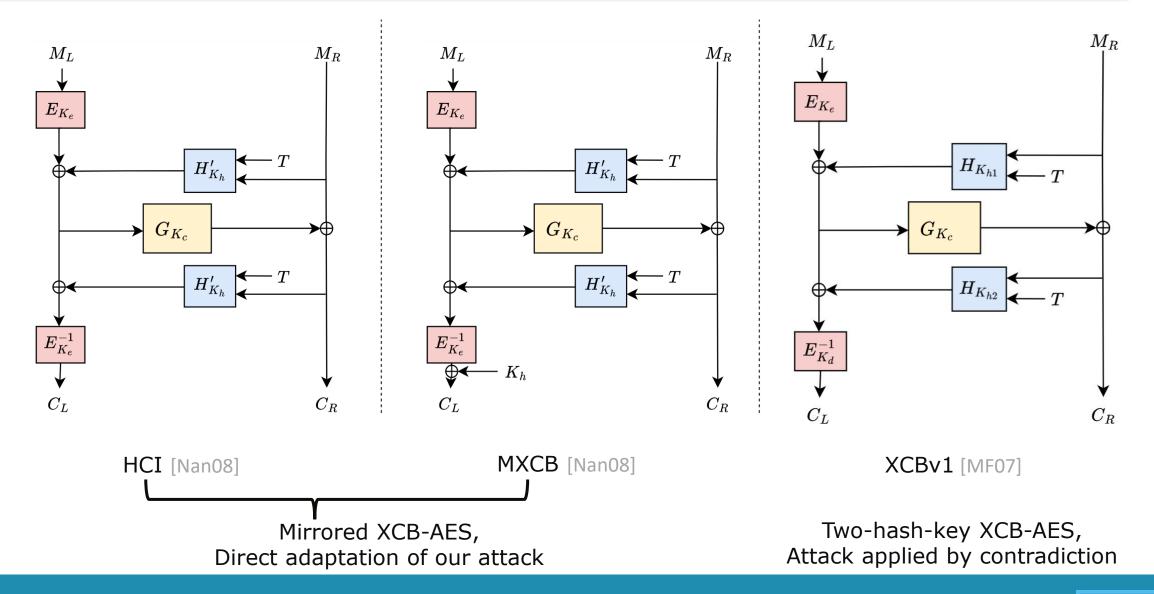
"Knowledge gained without ethics is a loss, not a gain"

- Aristotle (attributed)



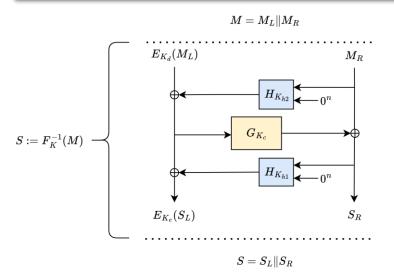
# **Backup Slides**



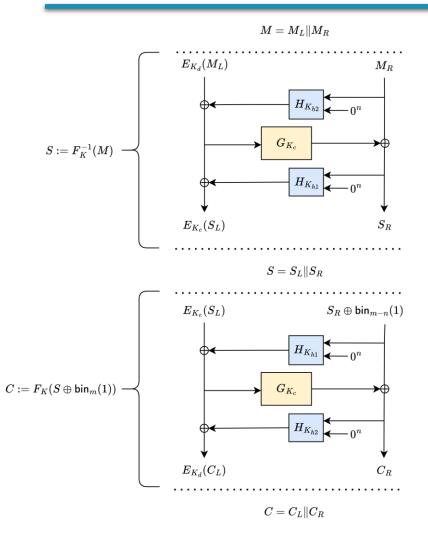


# Shared Difference Attack by Contradiction on XCBv1

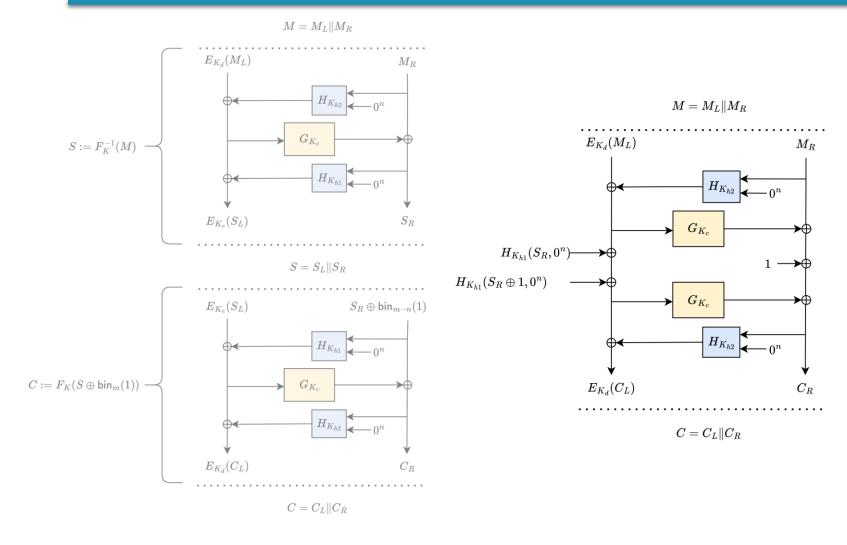
# Attack by Contradiction on XCBv1

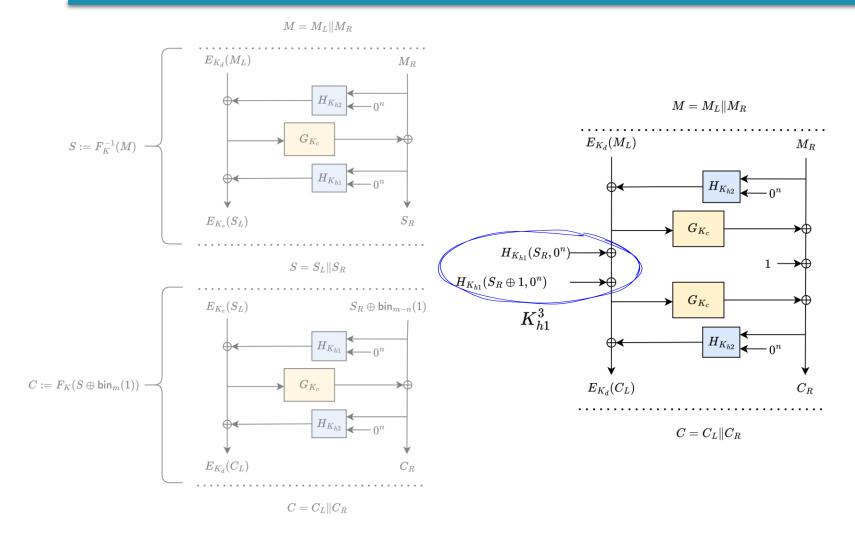


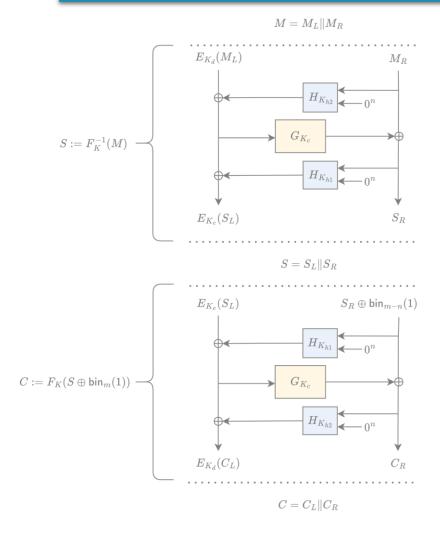
### Attack by Contradiction on XCBv1

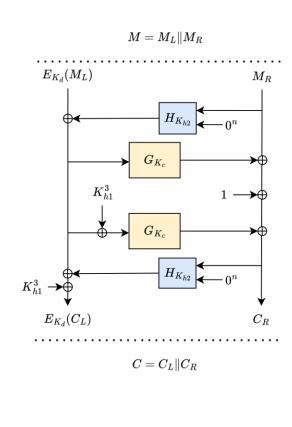


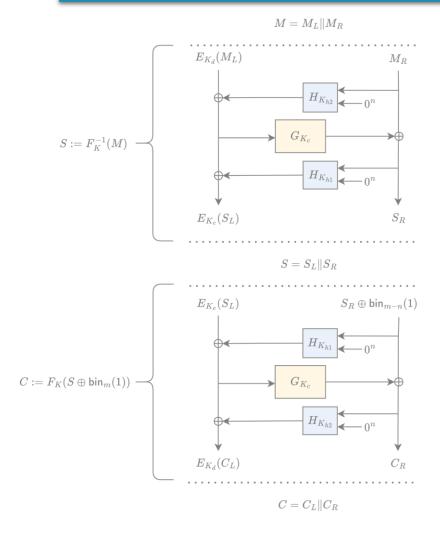
#### Attack by Contradiction on XCBv1

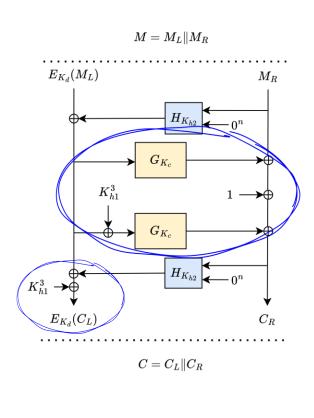


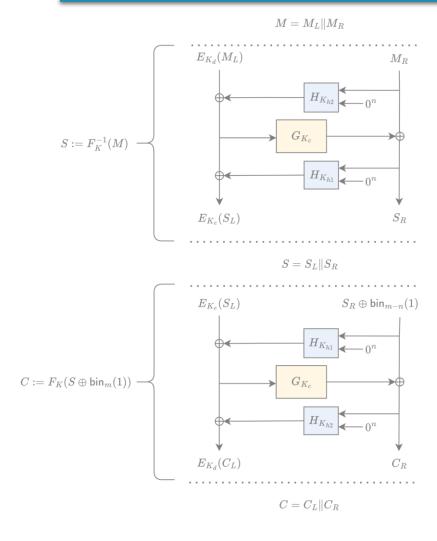


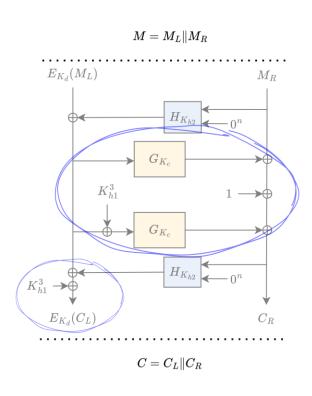


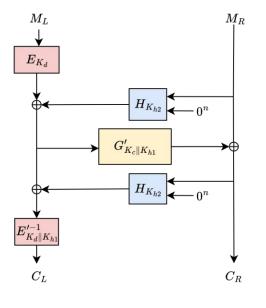


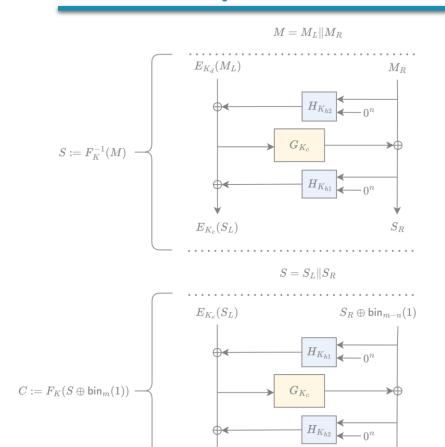




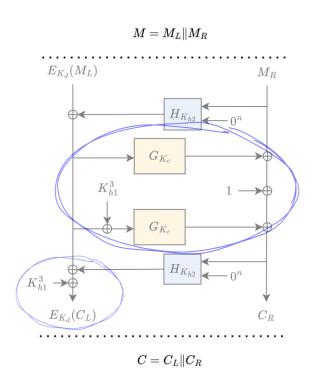


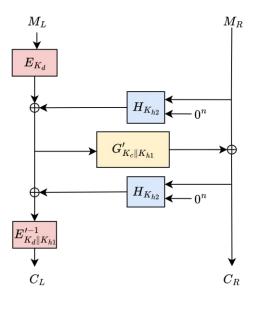






 $E_{K_d}(C_L)$ 



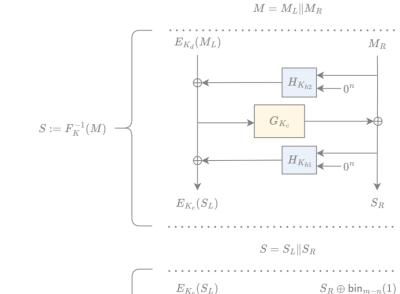


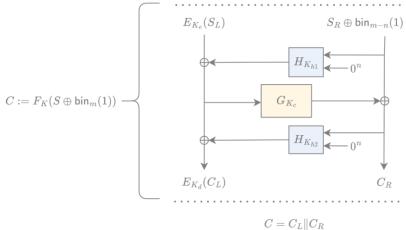
 $\mathsf{SPRP}(\mathsf{SPRP}^{-1}(M) \oplus \gamma)$ 

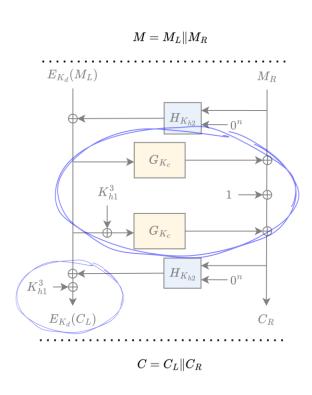
 $C = C_L \| C_R$ 

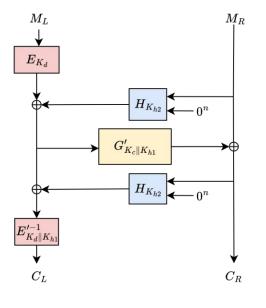
Naor-Reingold, 2002

PRI(M)





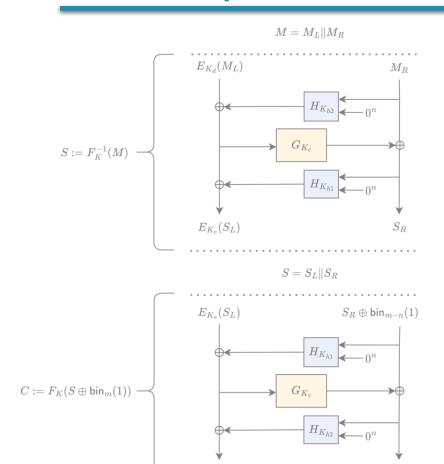




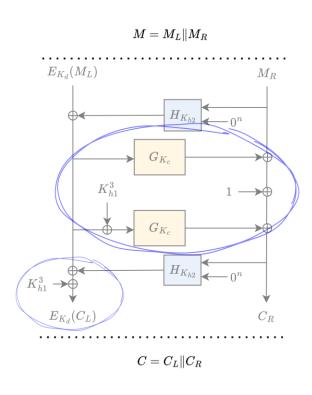
 $\mathsf{SPRP}(\mathsf{SPRP}^{-1}(M) \oplus \gamma)$ 

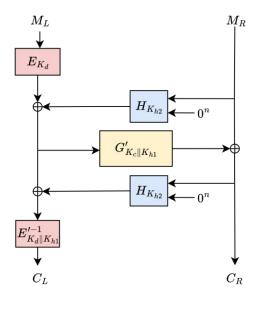
Naor-Reingold, 2002

-PRI(M)Shared Difference Attack



 $E_{K_d}(C_L)$ 





 $\frac{\mathsf{SPRP}}{\mathsf{SPRP}^{-1}}(M) \oplus \gamma)$ 

 $C = C_L \| C_R$ 

Naor-Reingold, 2002

-PRI(M)Shared Difference Attack

# Separability contradicts XOR-Universality of Sum



• For any two inputs  $(T,M) \neq (T',M')$ , output Y, and random secret key K,

$$\Pr(H_1(K,T,M) \oplus H_1(K,T',M') = Y) \leq \epsilon_1$$

• For any two inputs  $(T,M) \neq (T',M')$ , output Y, and random secret key K,

$$\Pr(H_1(K,T,M) \oplus H_1(K,T',M') = Y) \leq \ell/2^n$$

• For any two inputs  $(T,M) \neq (T',M')$ , output Y, and random secret key K,

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 $H_1$  is XOR-universal

• For any two inputs  $(T,M) \neq (T',M')$ , output Y, and random secret key K,

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 $H_1$  is XOR-universal

• For any two inputs  $(T,C) \neq (T',C')$ , output Y, and random secret key K,

$$\Pr(H_2(K,T,C)\oplus H_2(K,T',C')=Y)\leq \ell/2^n$$

 $H_2$  is XOR-universal

• For any two inputs  $(T,M) \neq (T',M')$ , output Y, and random secret key K,

$$\Pr(H_1(K,T,M) \oplus H_1(K,T',M') = Y) \leq \ell/2^n$$

 $H_1$  is XOR-universal

• For any two inputs  $(T,C) \neq (T',C')$ , output Y, and random secret key K,

$$\Pr(H_2(K,T,C)\oplus H_2(K,T',C')=Y)\leq \ell/2^n$$

 $H_2$  is XOR-universal

• For any two inputs  $(T,M,C) \neq (T',M',C')$ , output Y, and random secret key K,

$$\Pr(H_{\mathrm{sum}}(K,T,M,C)\oplus H_{\mathrm{sum}}(K,T',M',C')=0\ )\leq \epsilon_{\mathrm{sum}}$$

• For any two inputs  $(T,M) \neq (T',M')$ , output Y, and random secret key K,

$$\Pr(H_1(K,T,M) \oplus H_1(K,T',M') = Y) \leq \ell/2^n$$

 $H_1$  is XOR-universal

• For any two inputs  $(T,C) \neq (T',C')$ , output Y, and random secret key K,

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 $H_2$  is XOR-universal

• For any two inputs  $(T,M,C) \neq (T',M',C')$ , output Y, and random secret key K,

$$\Pr(H_{ ext{sum}}(K,T,M,C)\oplus H_{ ext{sum}}(K,T',M',C')=0\ )\leq \epsilon_{ ext{sum}}$$
  $M\oplus \Delta,C\oplus \Delta$ 

• For any two inputs  $(T,M) \neq (T',M')$ , output Y, and random secret key K,

$$\Pr(H_1(K,T,M) \oplus H_1(K,T',M') = Y) \leq \ell/2^n$$

 $H_1$  is XOR-universal

• For any two inputs  $(T,C) \neq (T',C')$ , output Y, and random secret key K,

$$\Pr(H_2(K,T,C) \oplus H_2(K,T',C') = Y) \leq \ell/2^n$$

 $H_2$  is XOR-universal

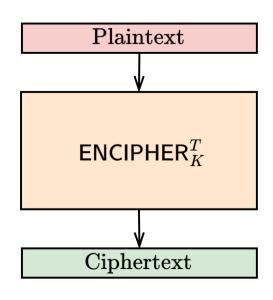
• For any two inputs  $(T,M,C) \neq (T',M',C')$ , output Y, and random secret key K,

$$\Pr(H_{\text{sum}}(K,T,M,C)\oplus H_{\text{sum}}(K,T',M',C')=0)=1$$
 
$$M\oplus \Delta,C\oplus \Delta$$

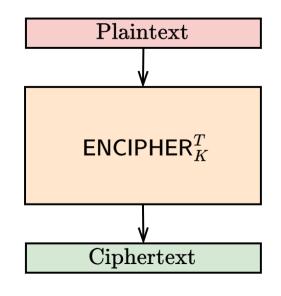
 $H_{\text{sum}}$  is not XOR-universal

#### Where are TEMs Used in Real-World?





- 1. Key-wrapping and swap-file encryption
- 2. Disk-sector and full-disk encryption



- 1. Key-wrapping and swap-file encryption
- 2. Disk-sector and full-disk encryption









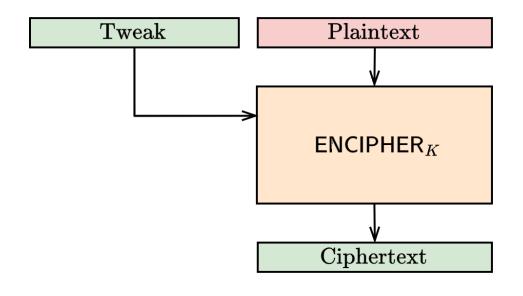




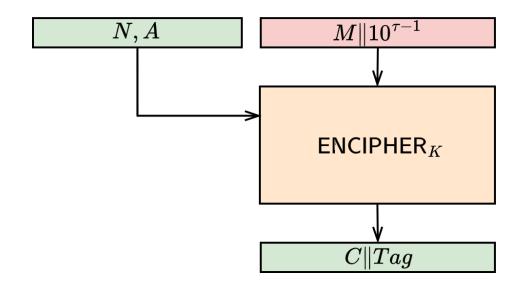






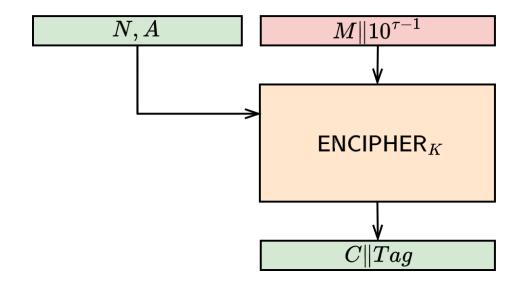


- 1. Key-wrapping and swap-file encryption
- 2. Disk-sector and full-disk encryption



Encode-then-Encipher (EtE) [BR00]

- 1. Key-wrapping and swap-file encryption
- 2. Disk-sector and full-disk encryption
- 3. Robust authenticated encryption [HKR17]
  - 1. Resisting nonce-misuse and
  - 2. Decryptional leakage (RUP) [AB+14]



Encode-then-Encipher (EtE) [BR00]

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Goals also covered under NIST's accordion call

