

# Round-Optimal Black-Box Multiparty Computation from Polynomial-Time Assumptions

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The University of Edinburgh

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Technical University of Denmark

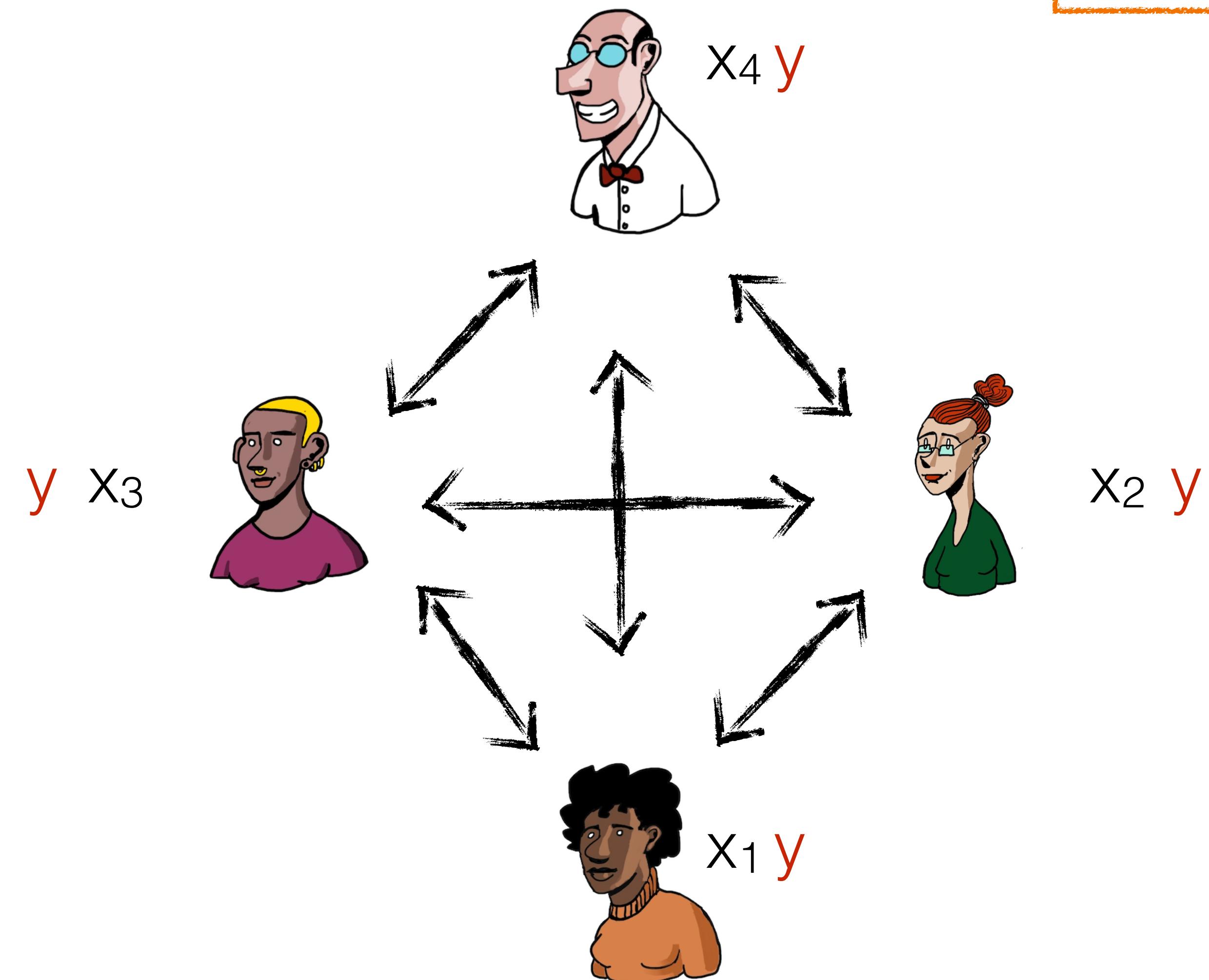
Rafail Ostrovsky

University of California, Los Angeles

Hendrik Waldner

# Multi-Party Computation (MPC)

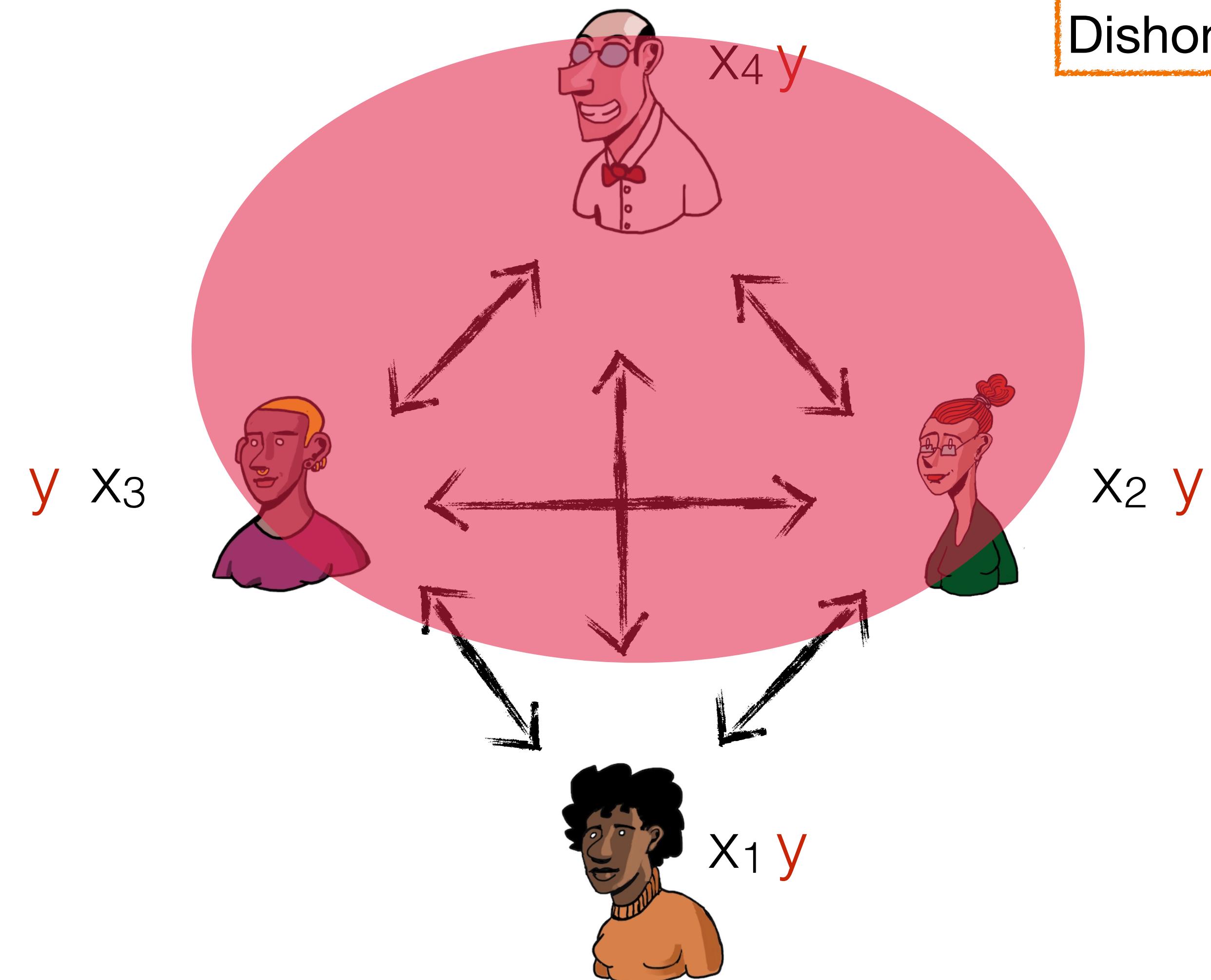
Plain model (no RO, no setup)



$$y = f(x_1, x_2, x_3, x_4)$$

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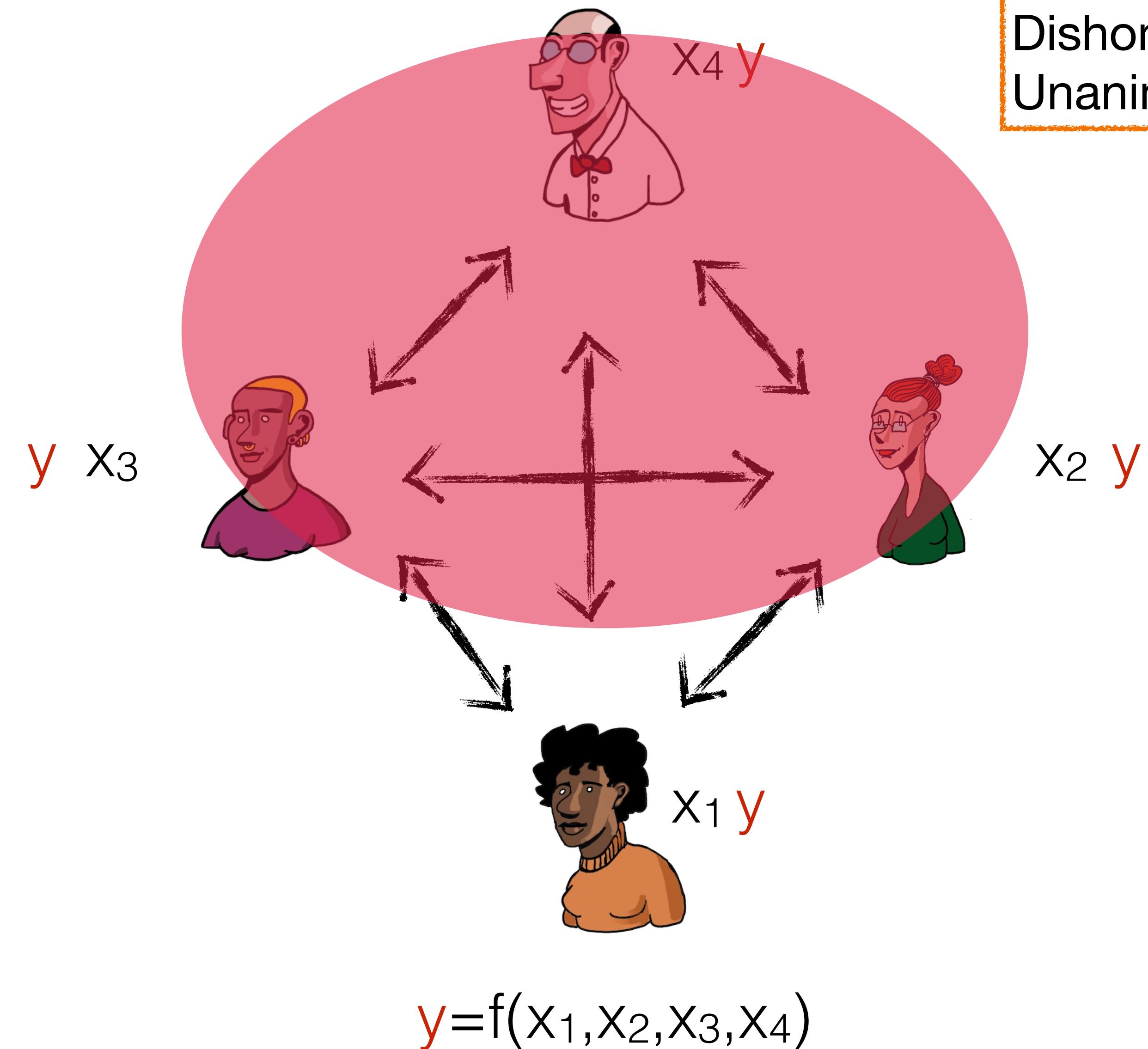
Plain model (no RO, no setup)  
Dishonest majority



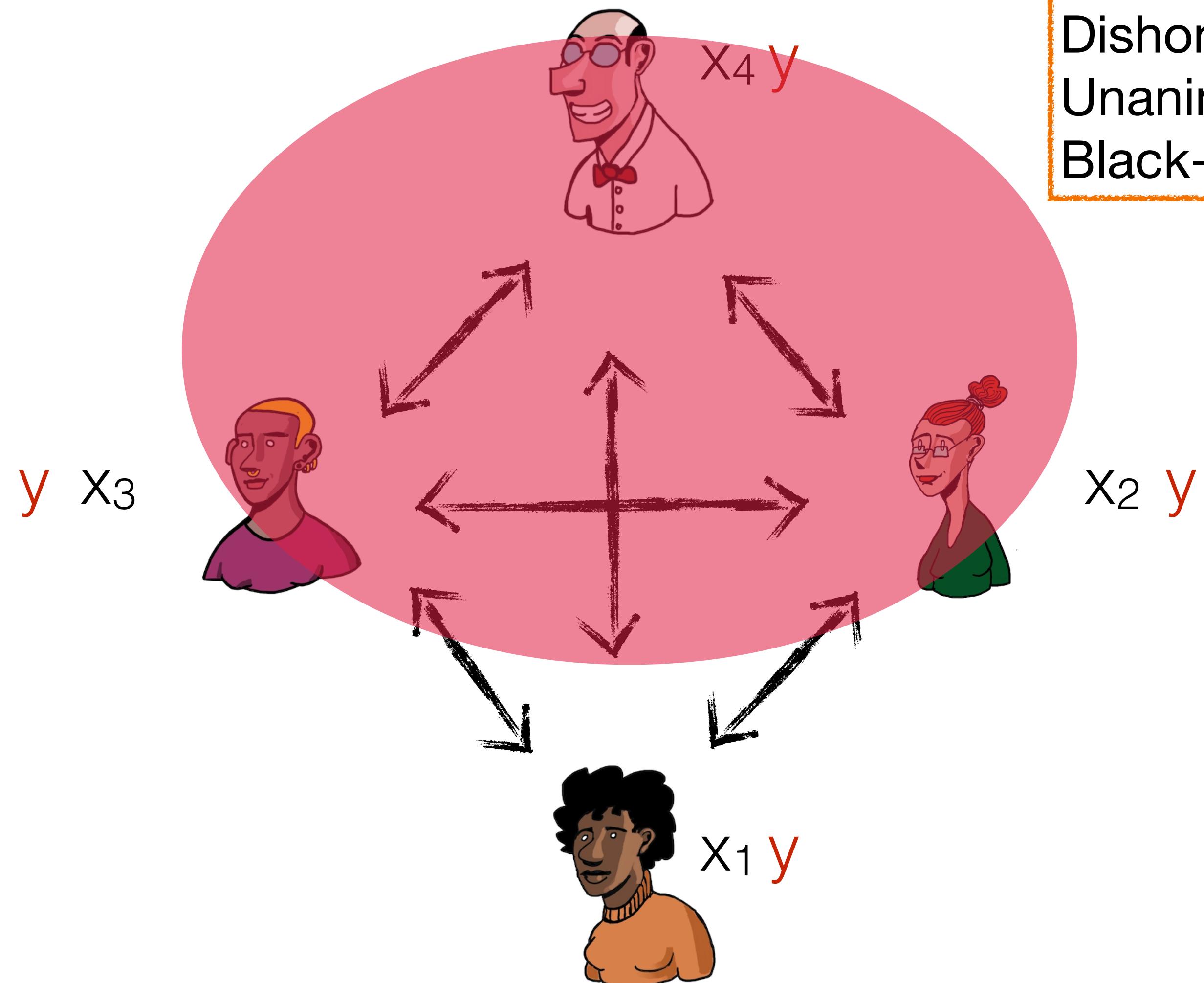
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Unanimous abort



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Black-box simulation

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What is the exact round complexity?

# The State of the Art on Round Optimal MPC

Optimal round complexity: 4-round [GK90, KO04, GMPP16]

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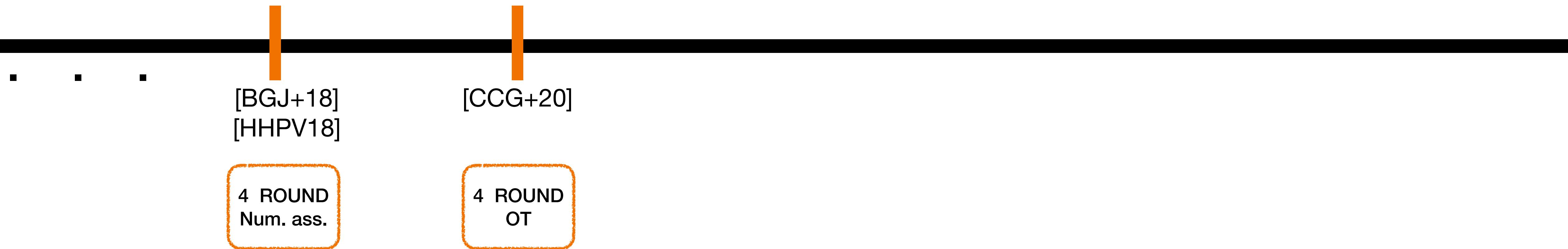
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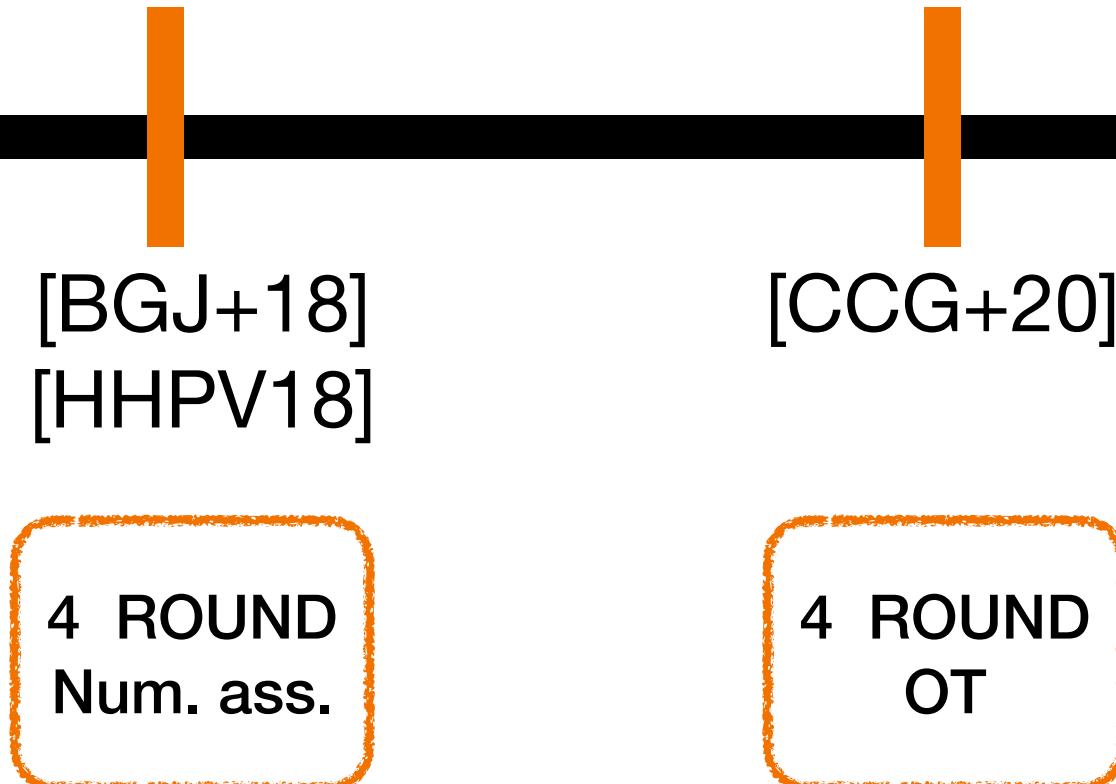
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Can we close the gap?

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OUTER PROTOCOL

Secure  
against  $(m-1)/3$  malicious  
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$m$  Servers



$n$  Clients



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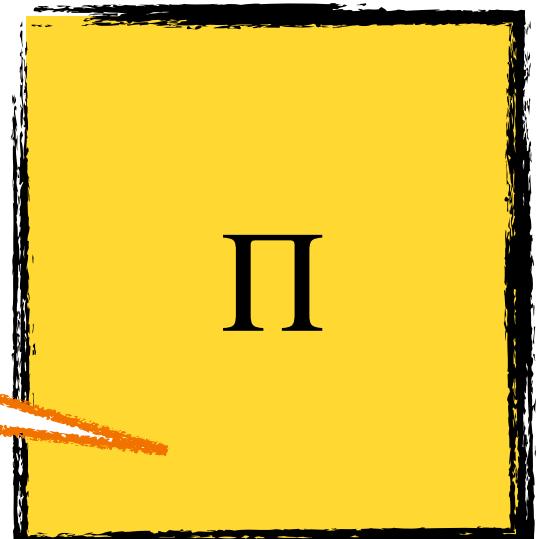
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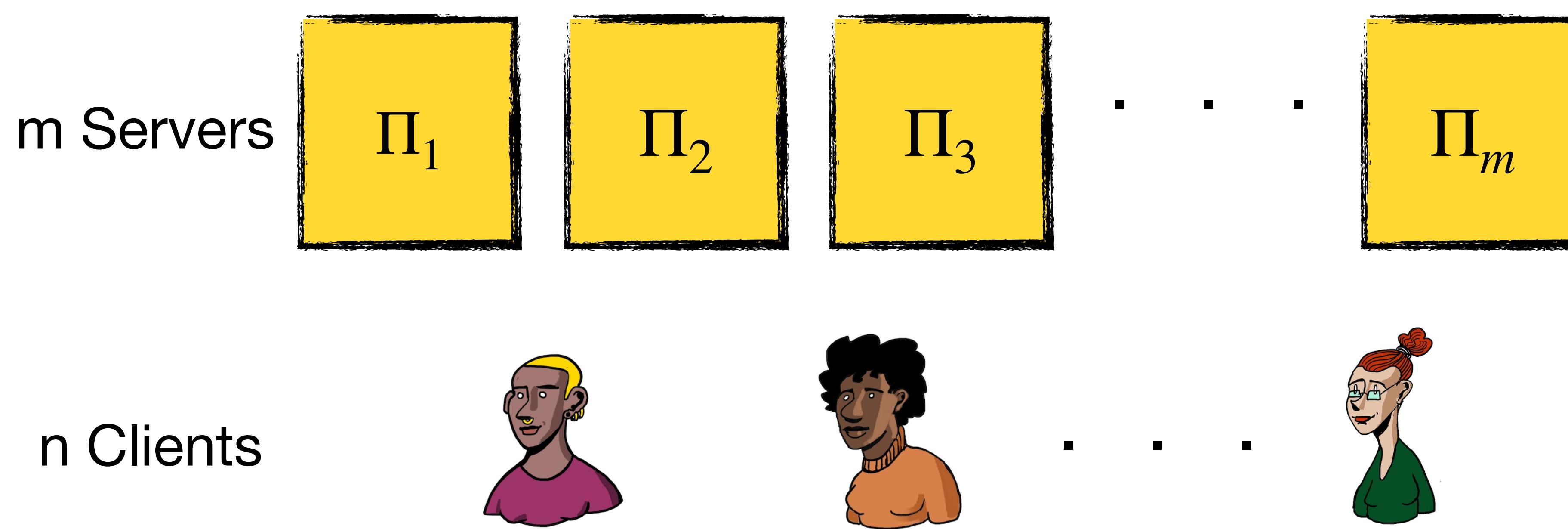


INNER  
PROTOCOL

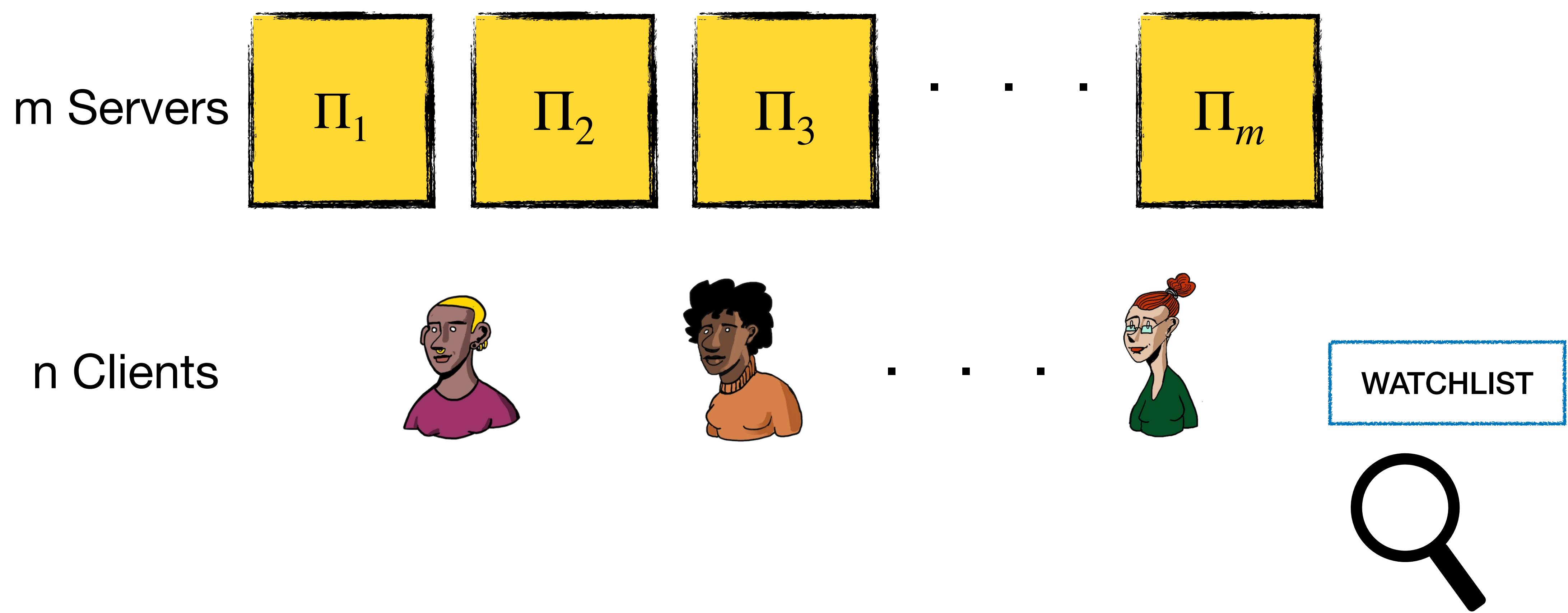
Semi-honest  
(dishonest-majority) security



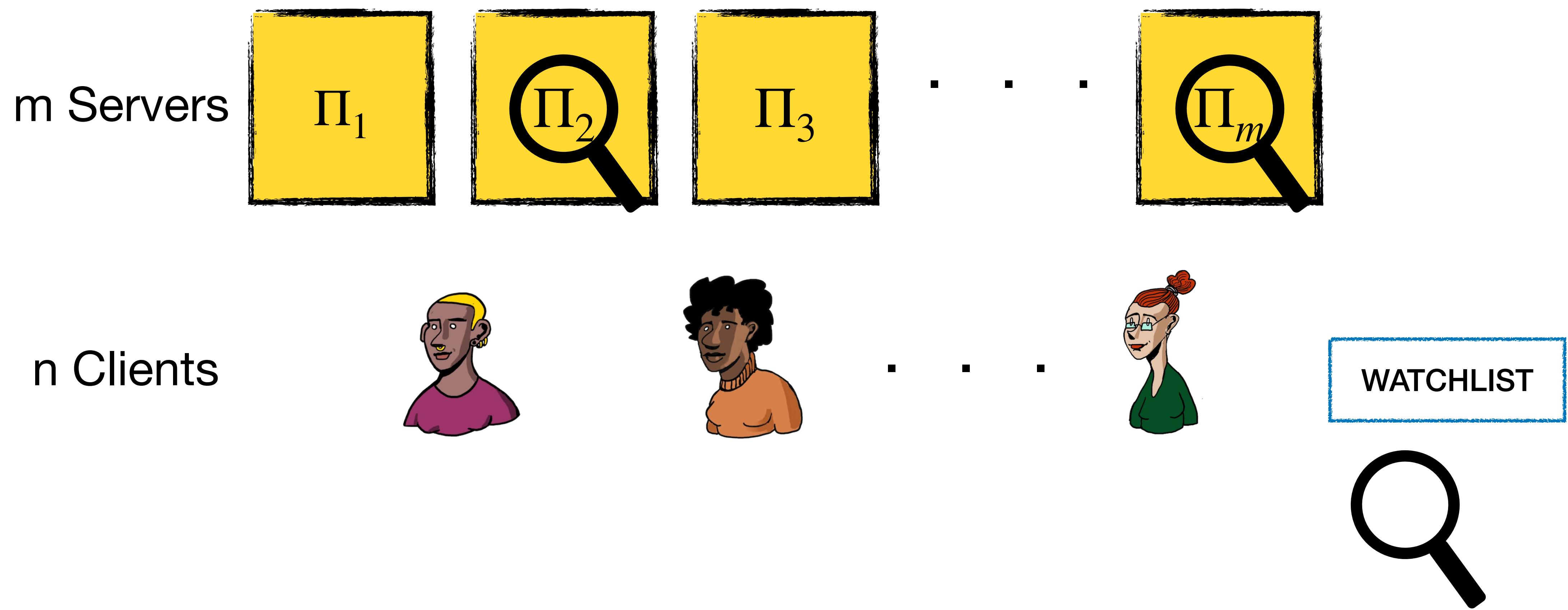
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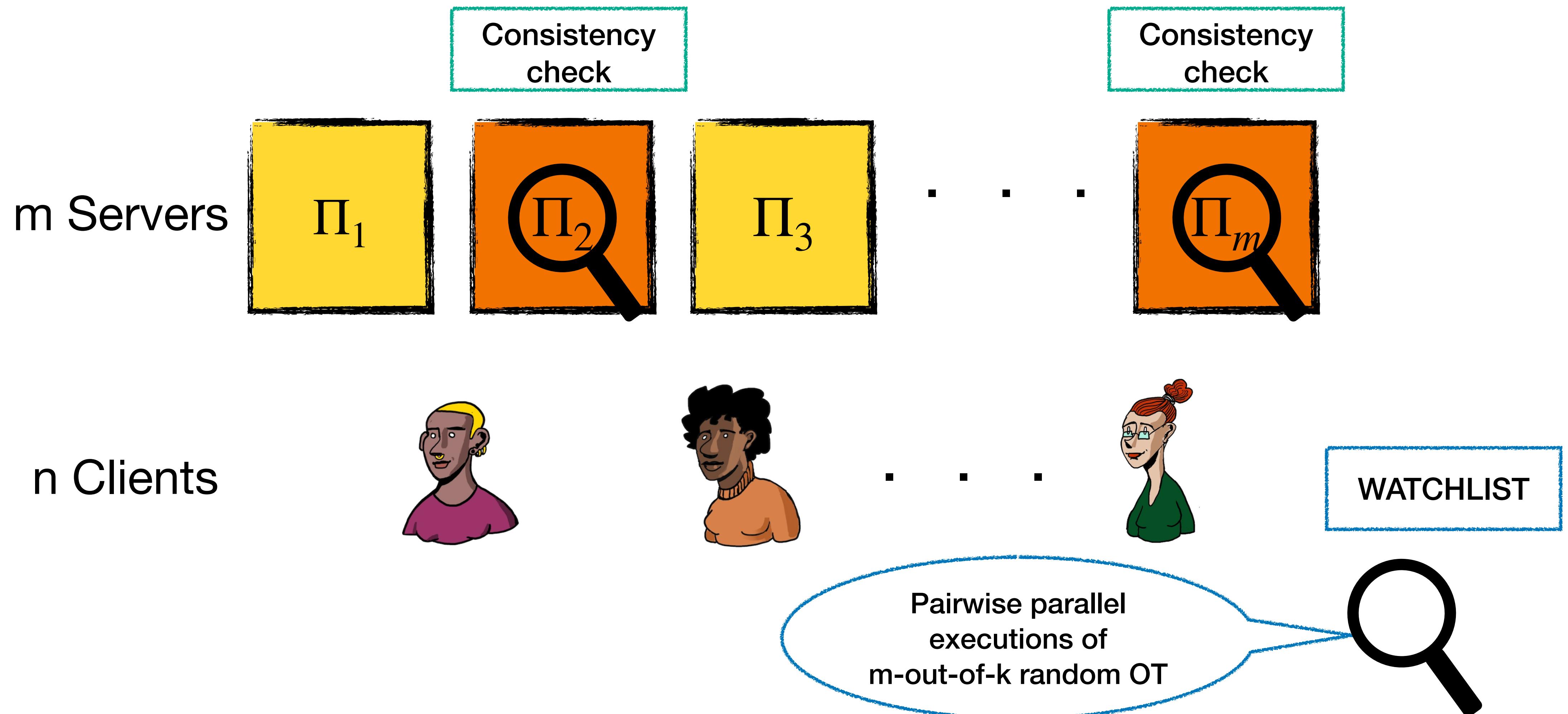
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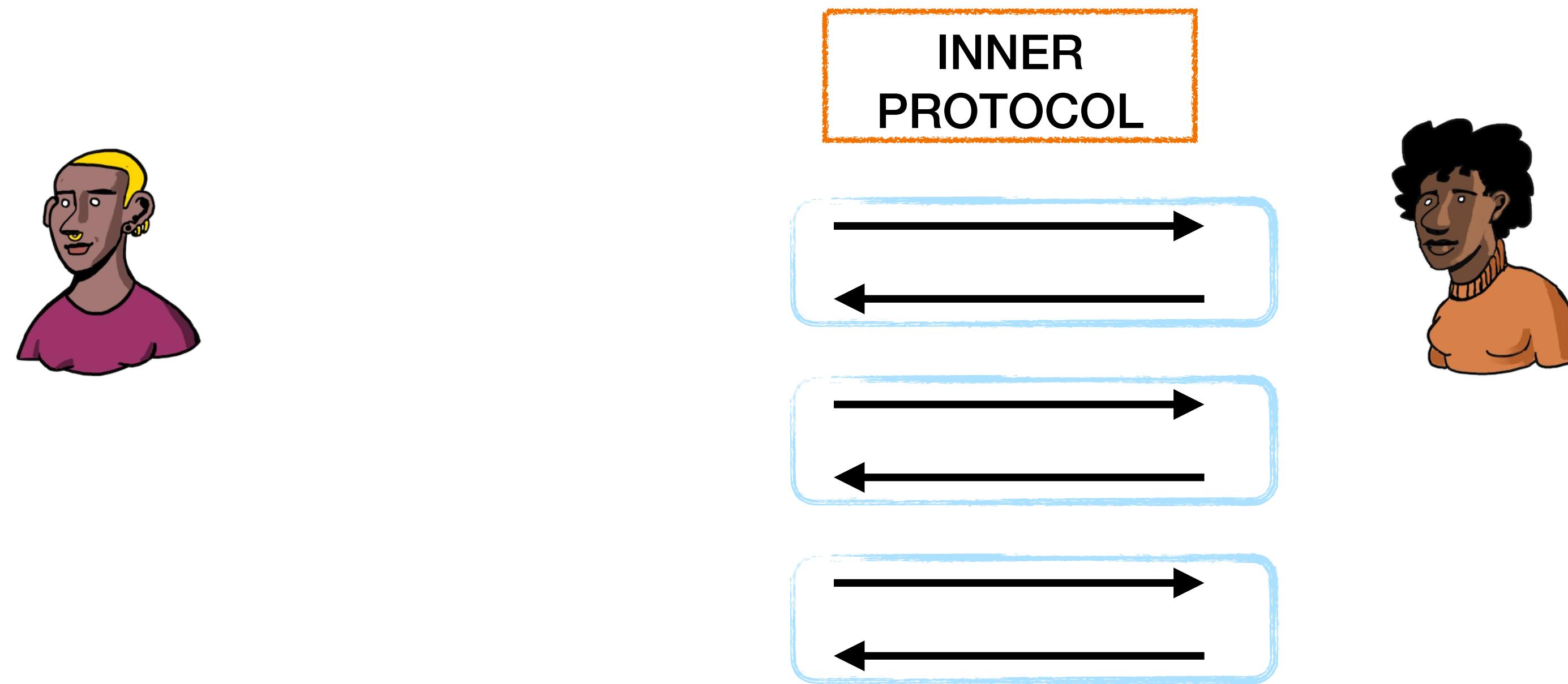
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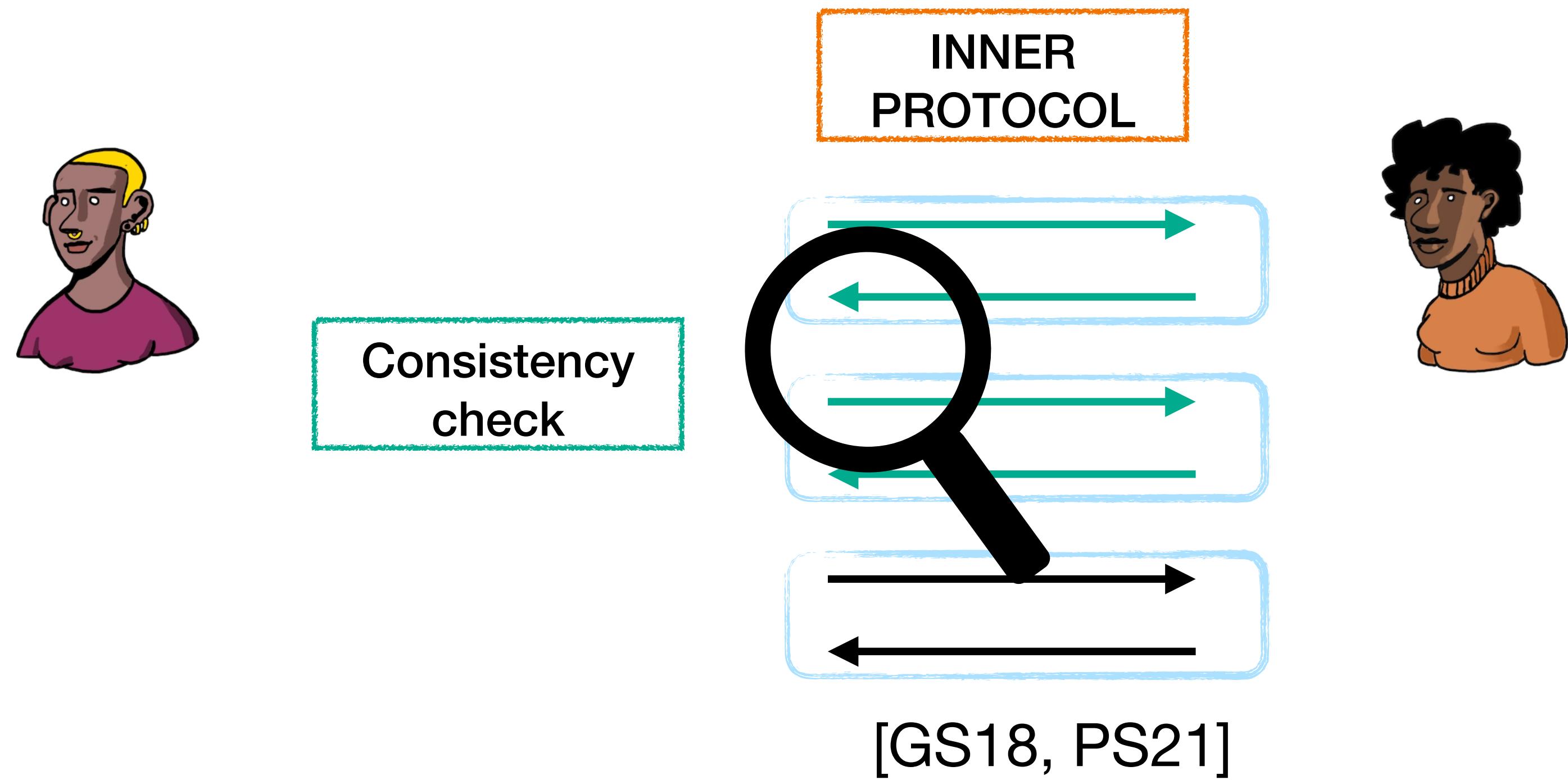
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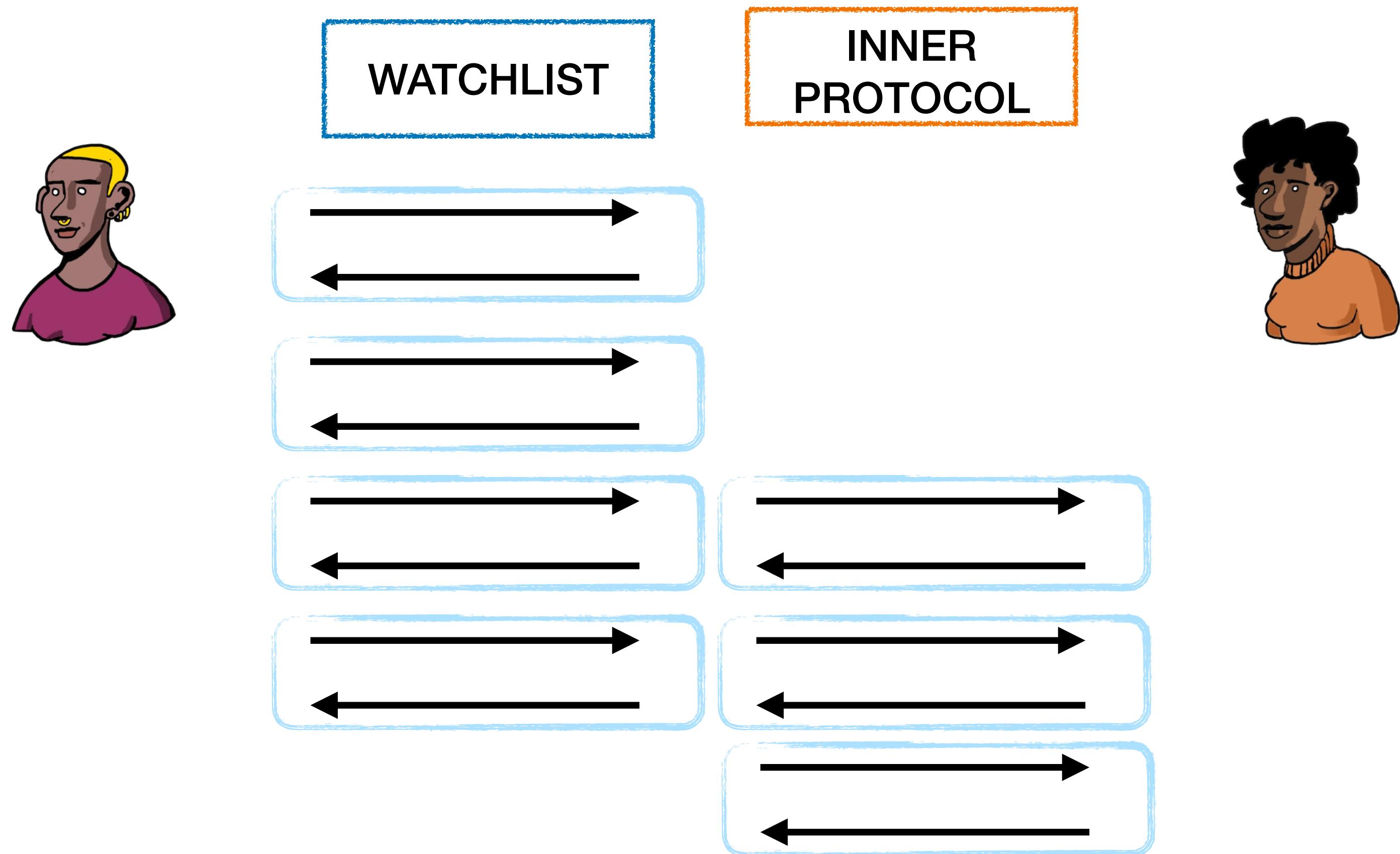


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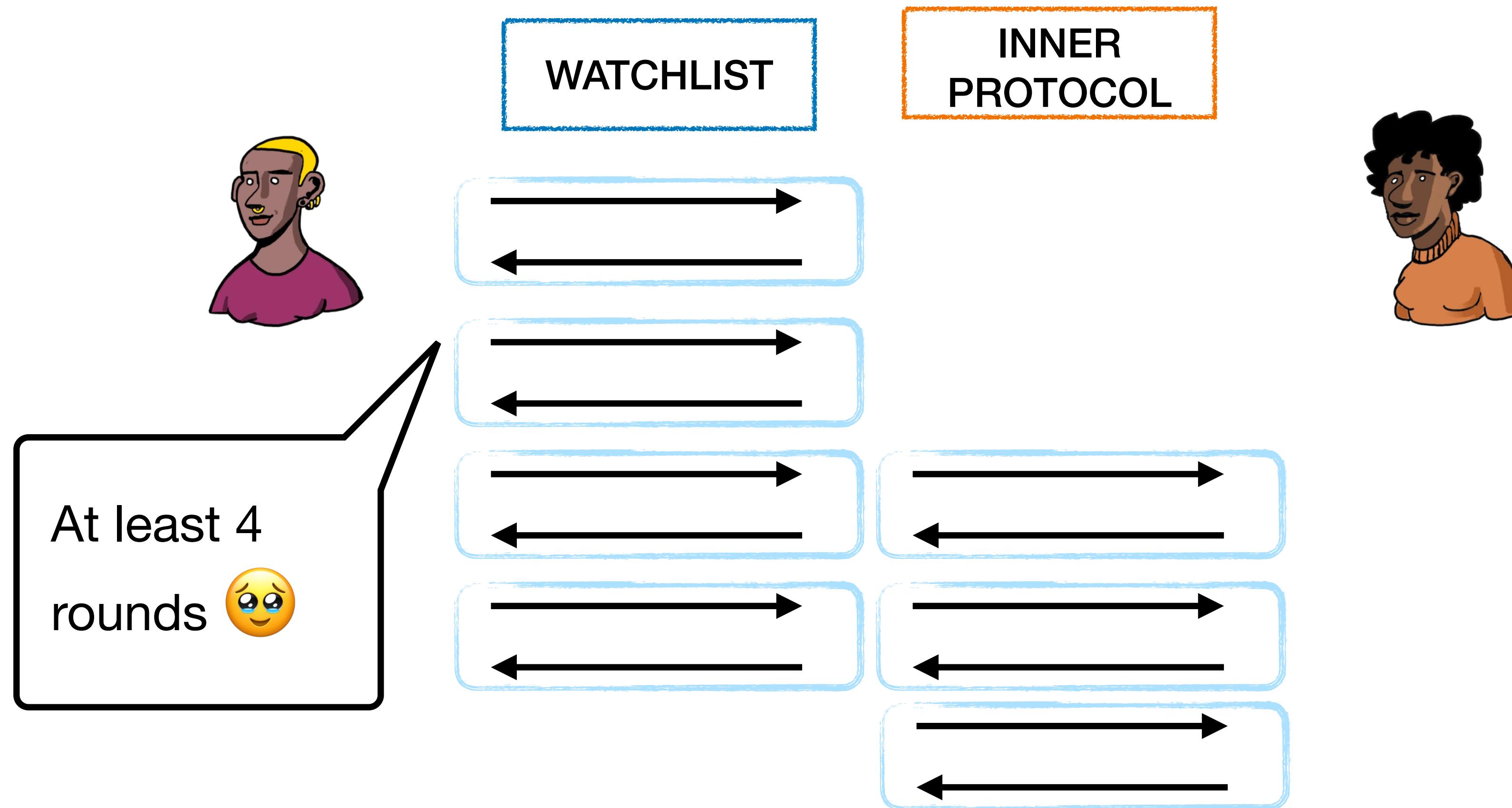
[PS21] A. Patra and A. Srinivasan. Three-round secure multiparty computation from black-box two-round oblivious transfer. In CRYPTO2021

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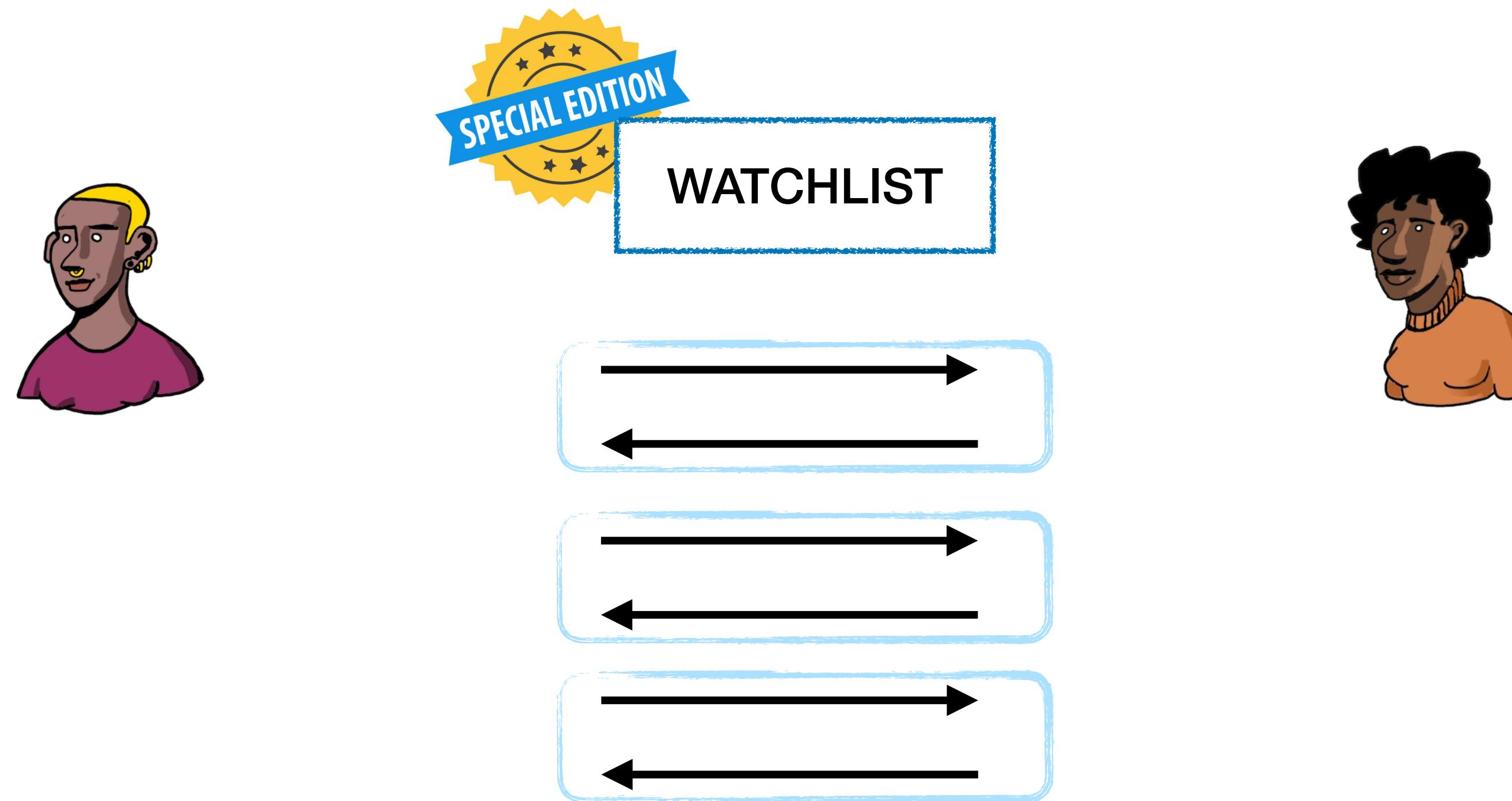
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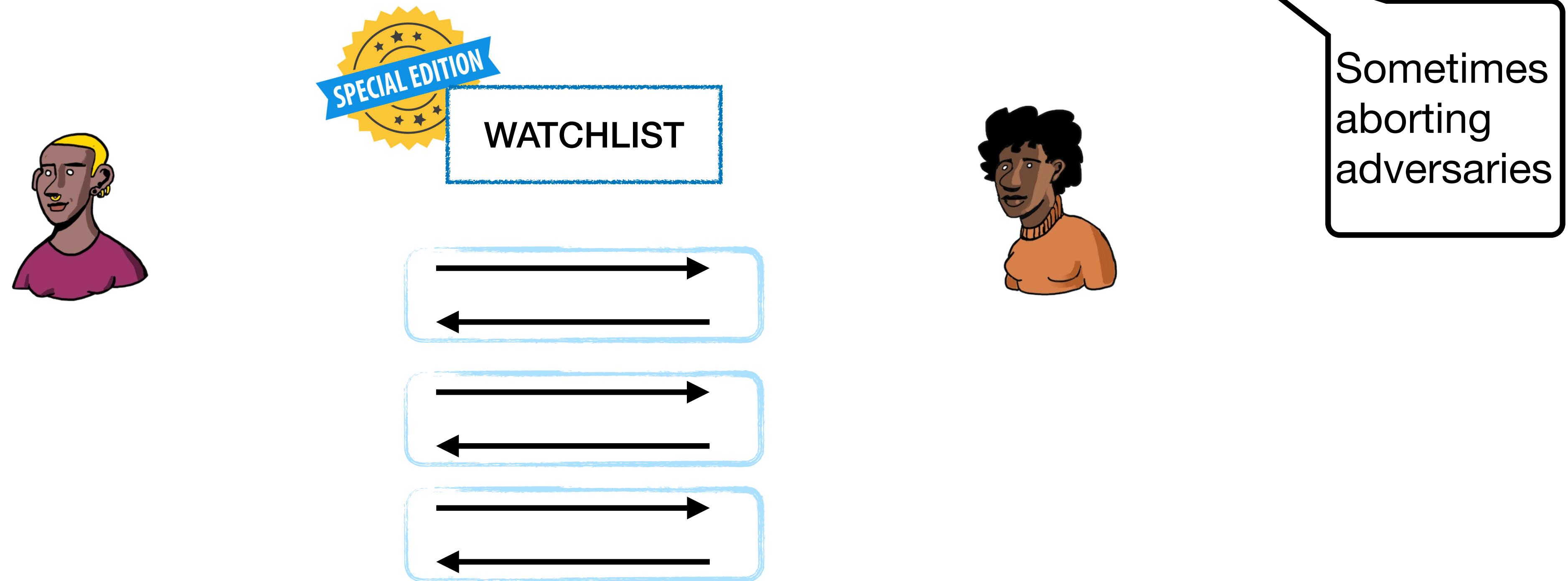
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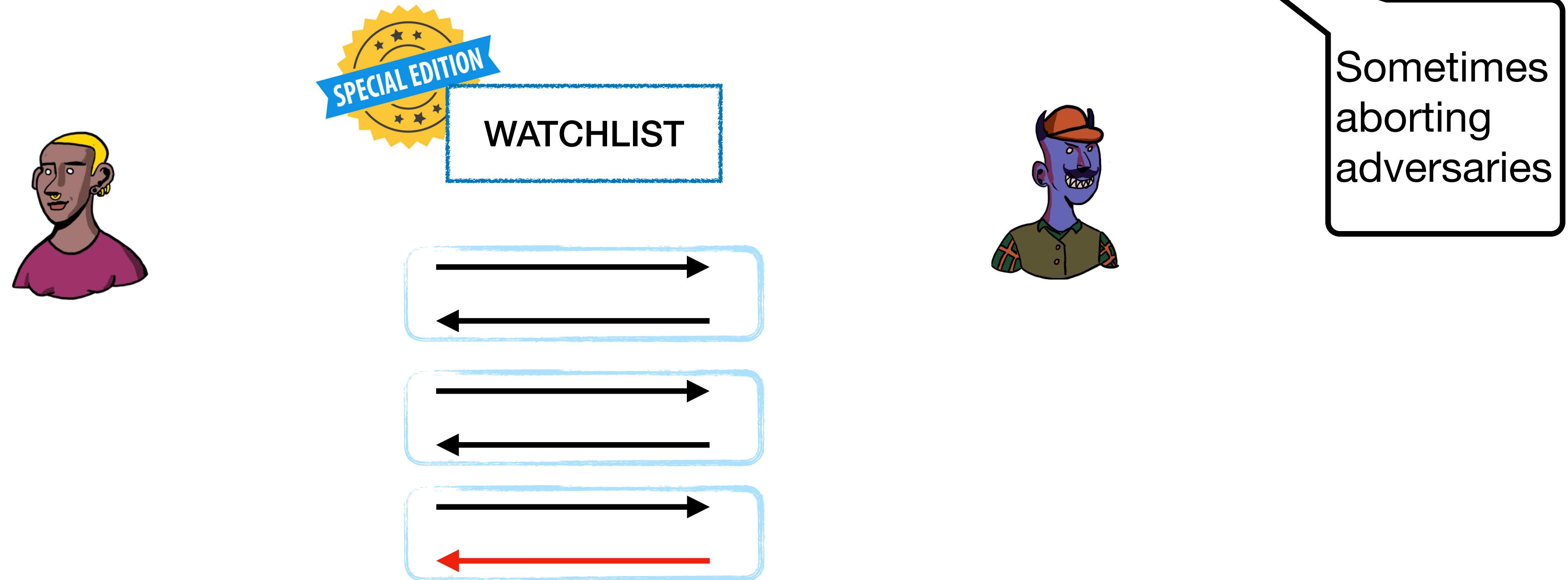
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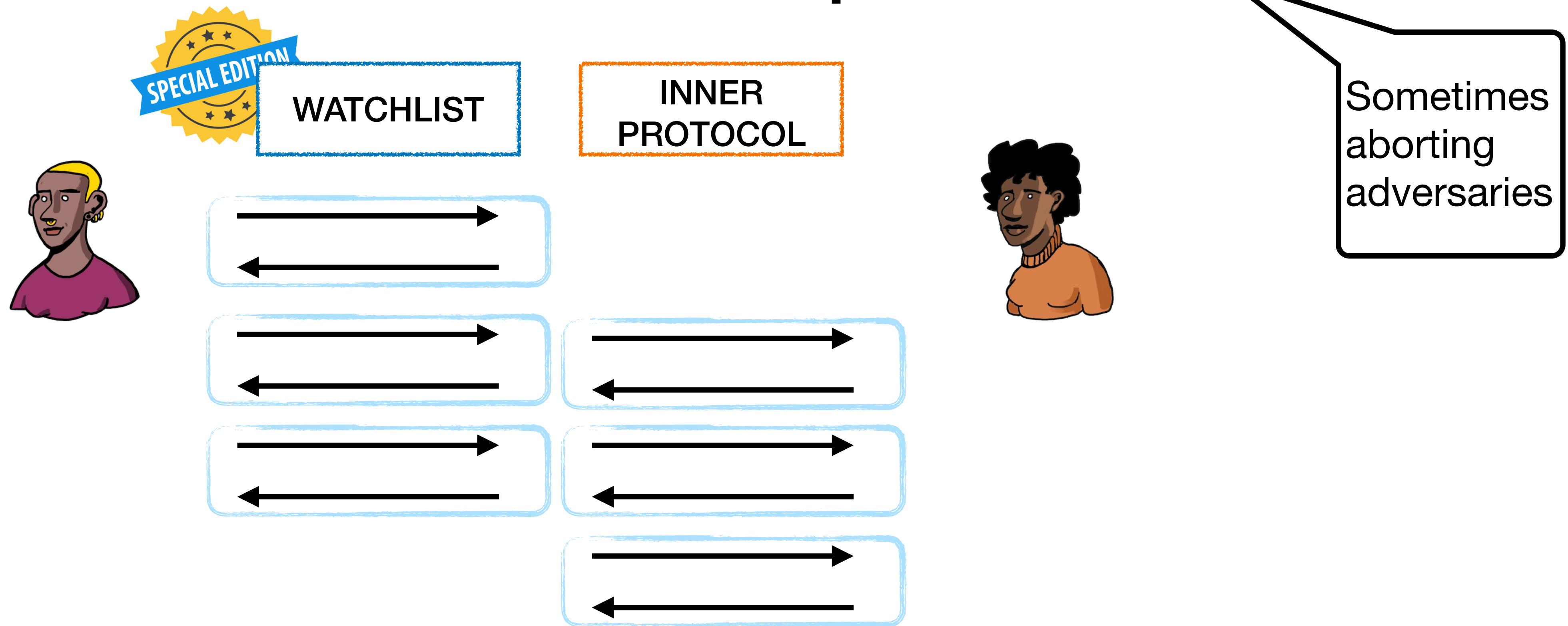
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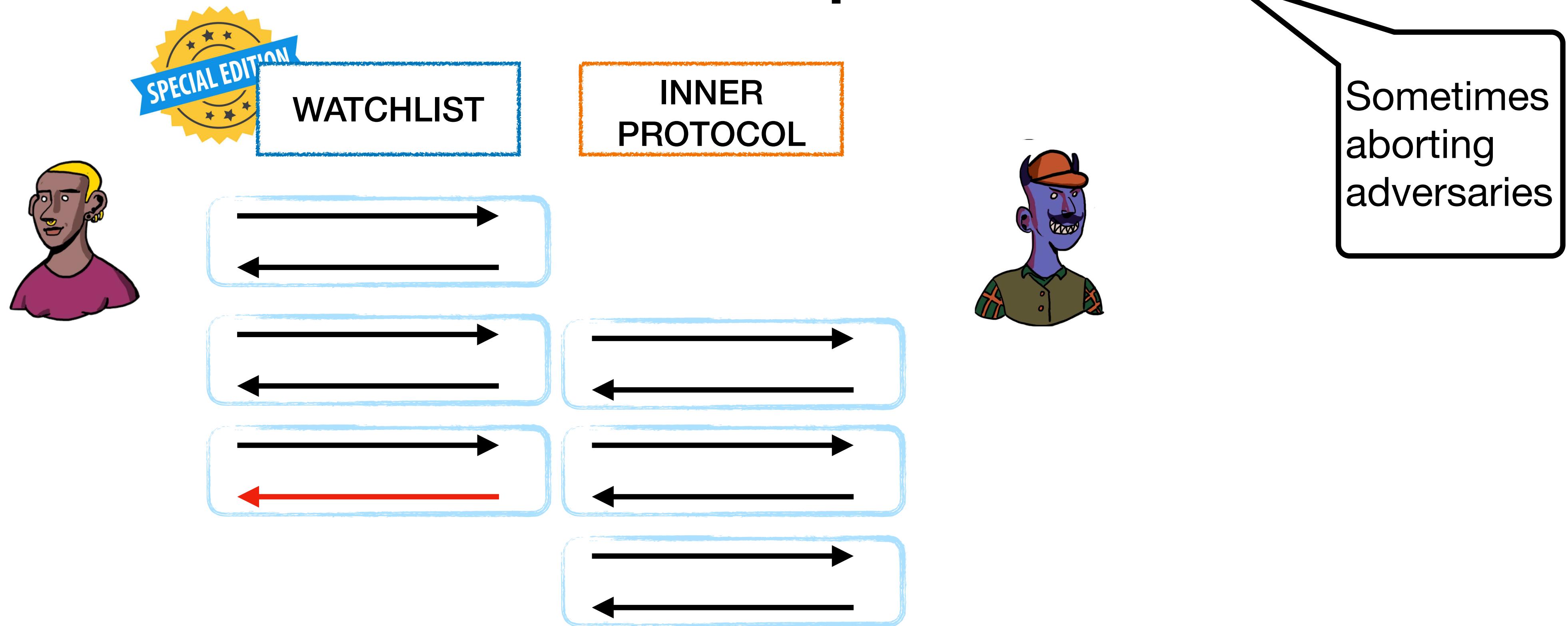
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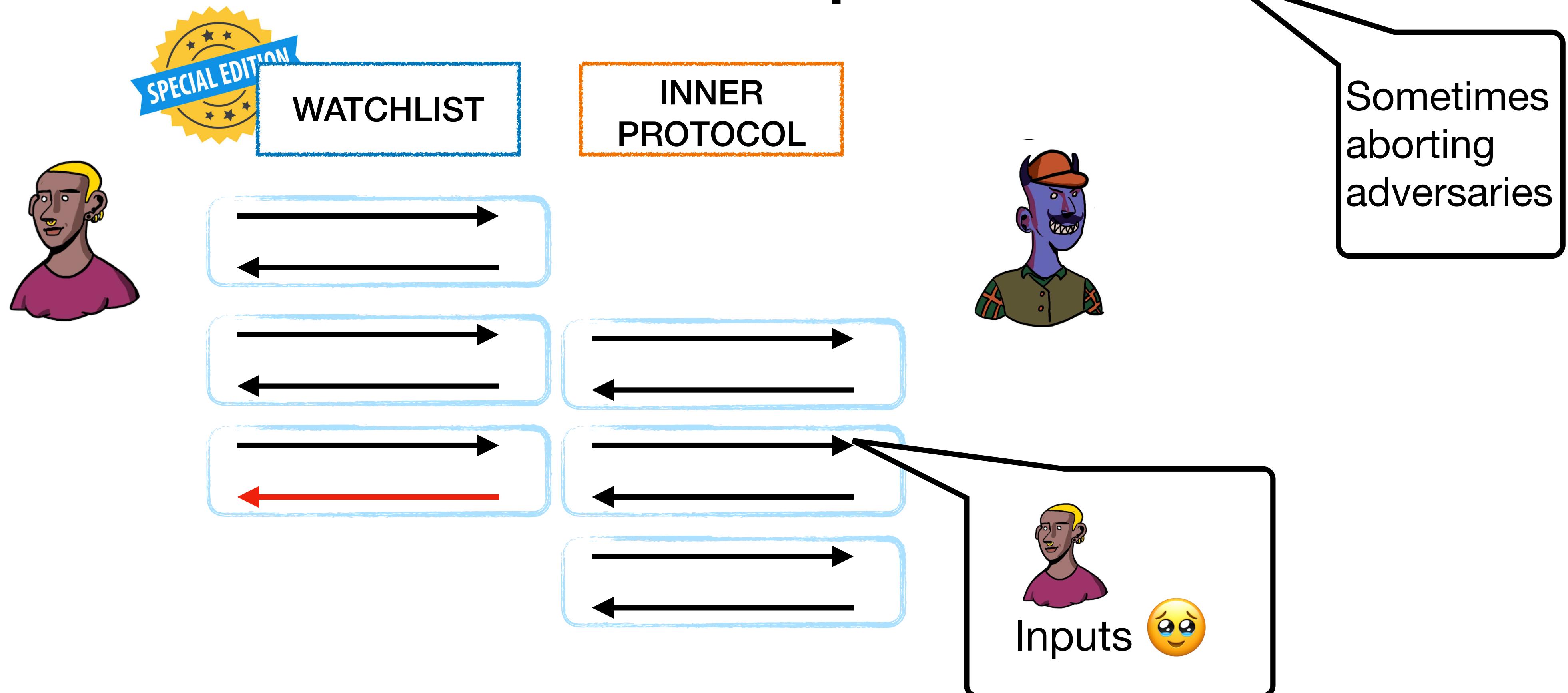
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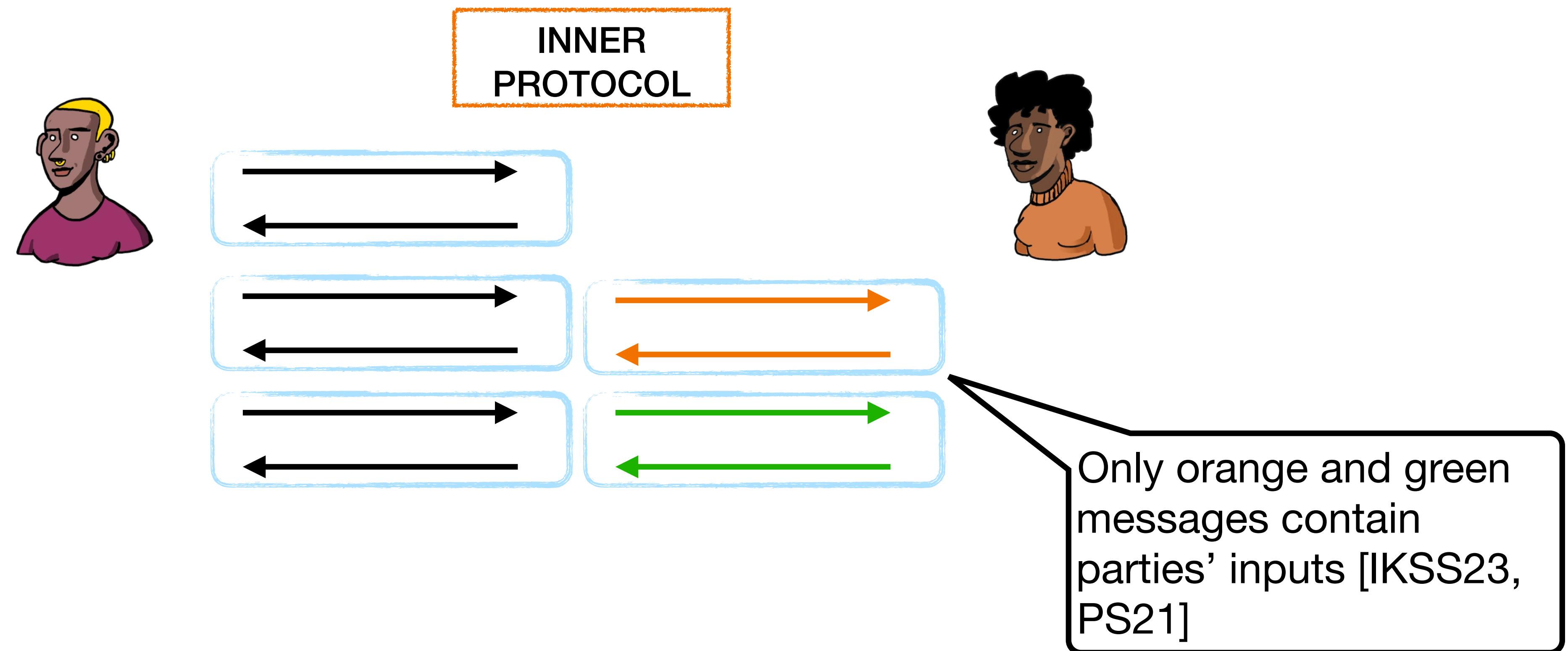
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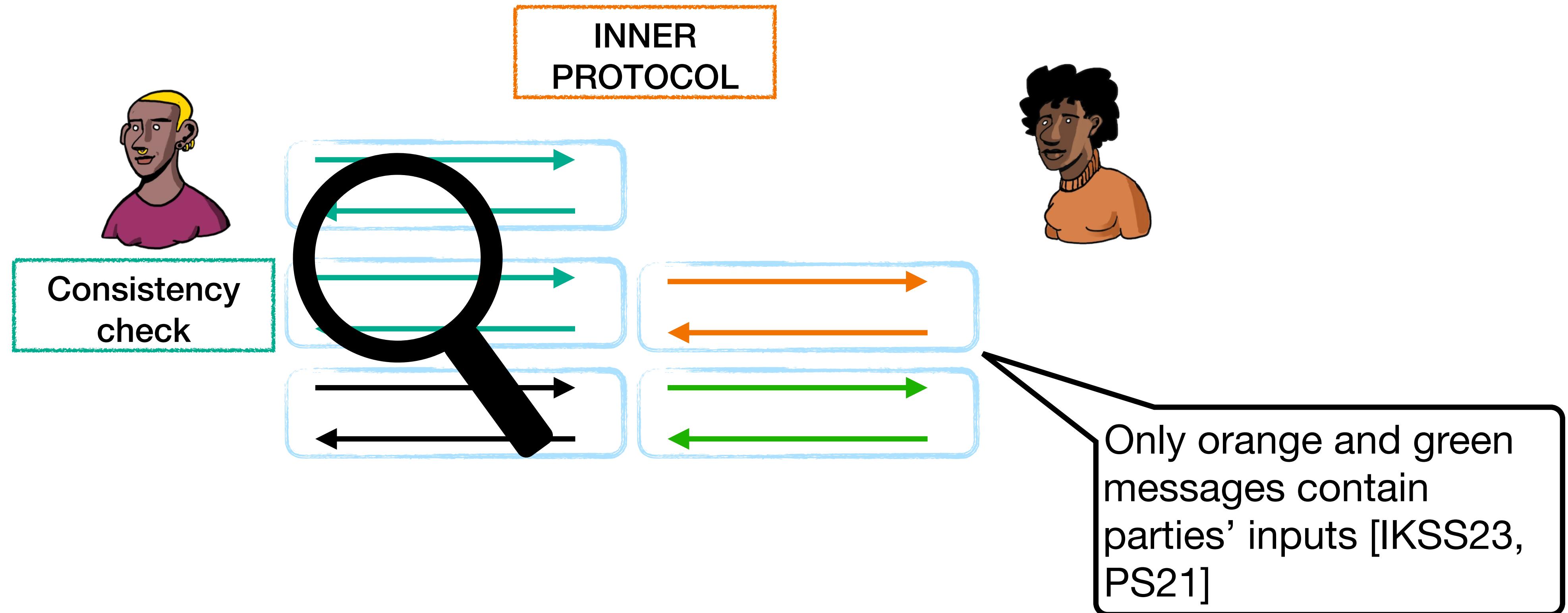
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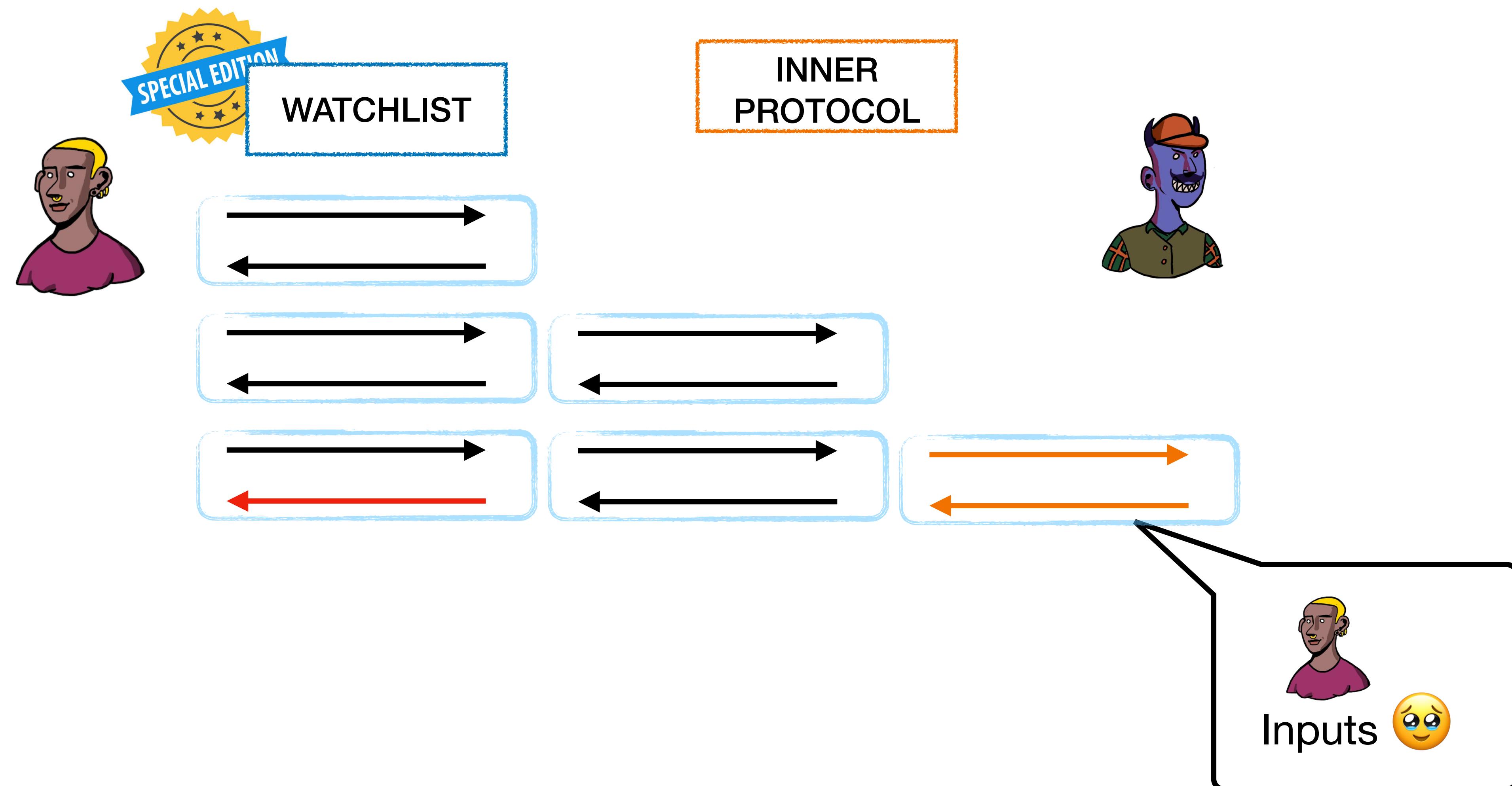
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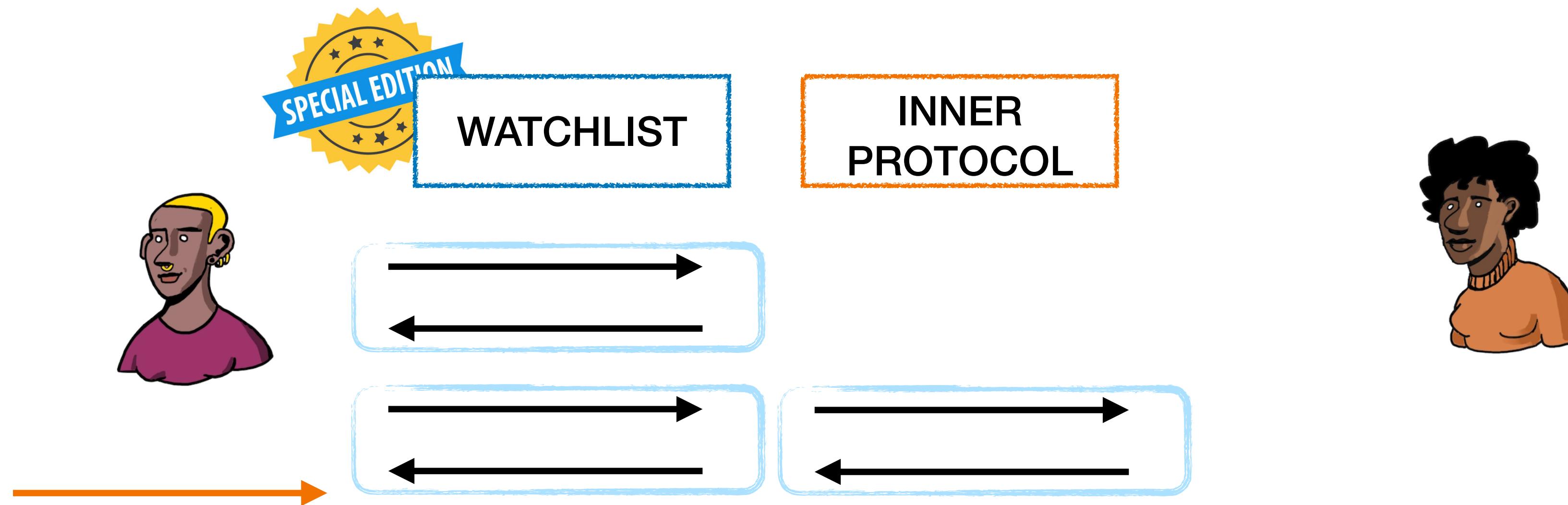
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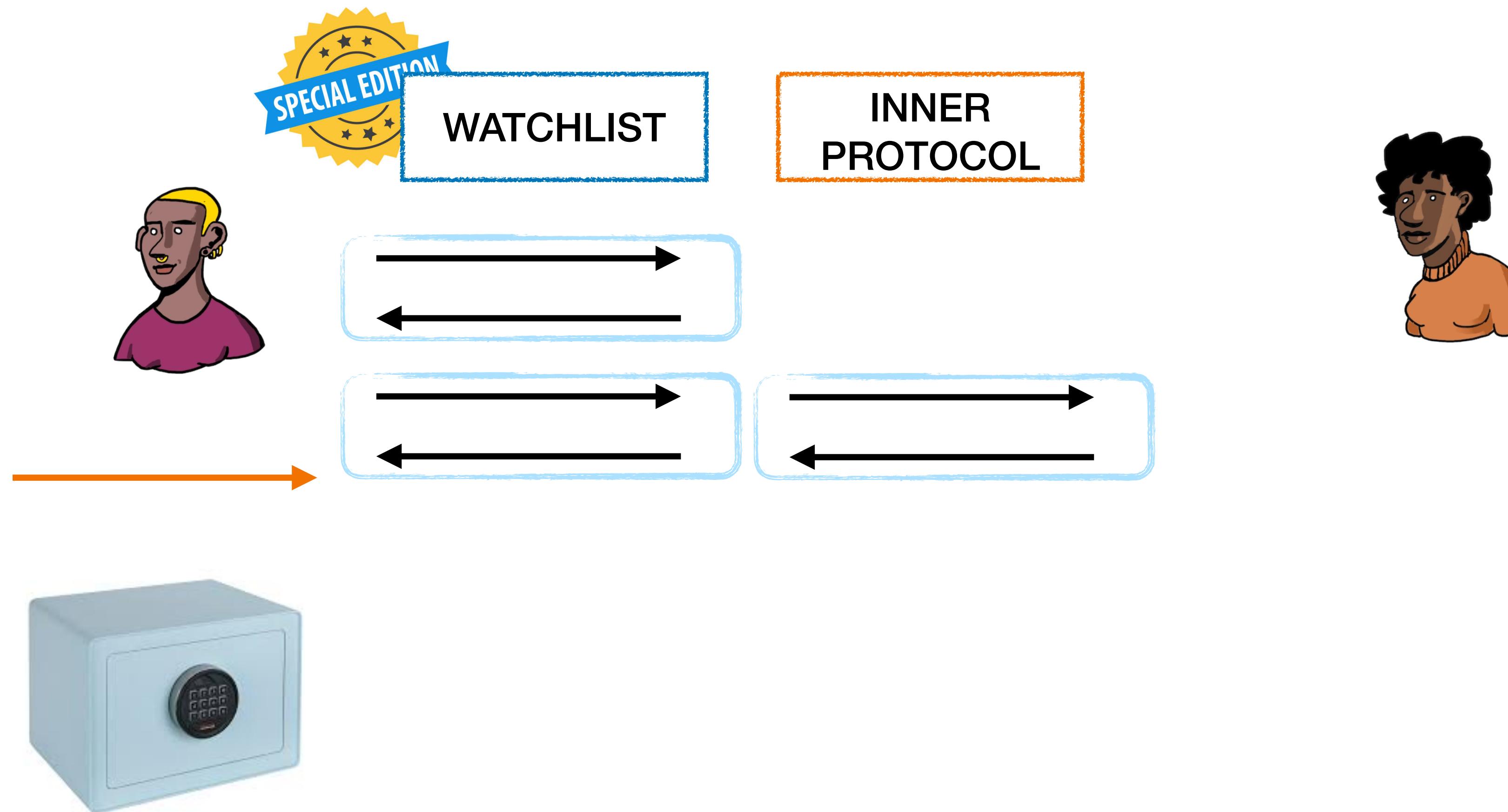
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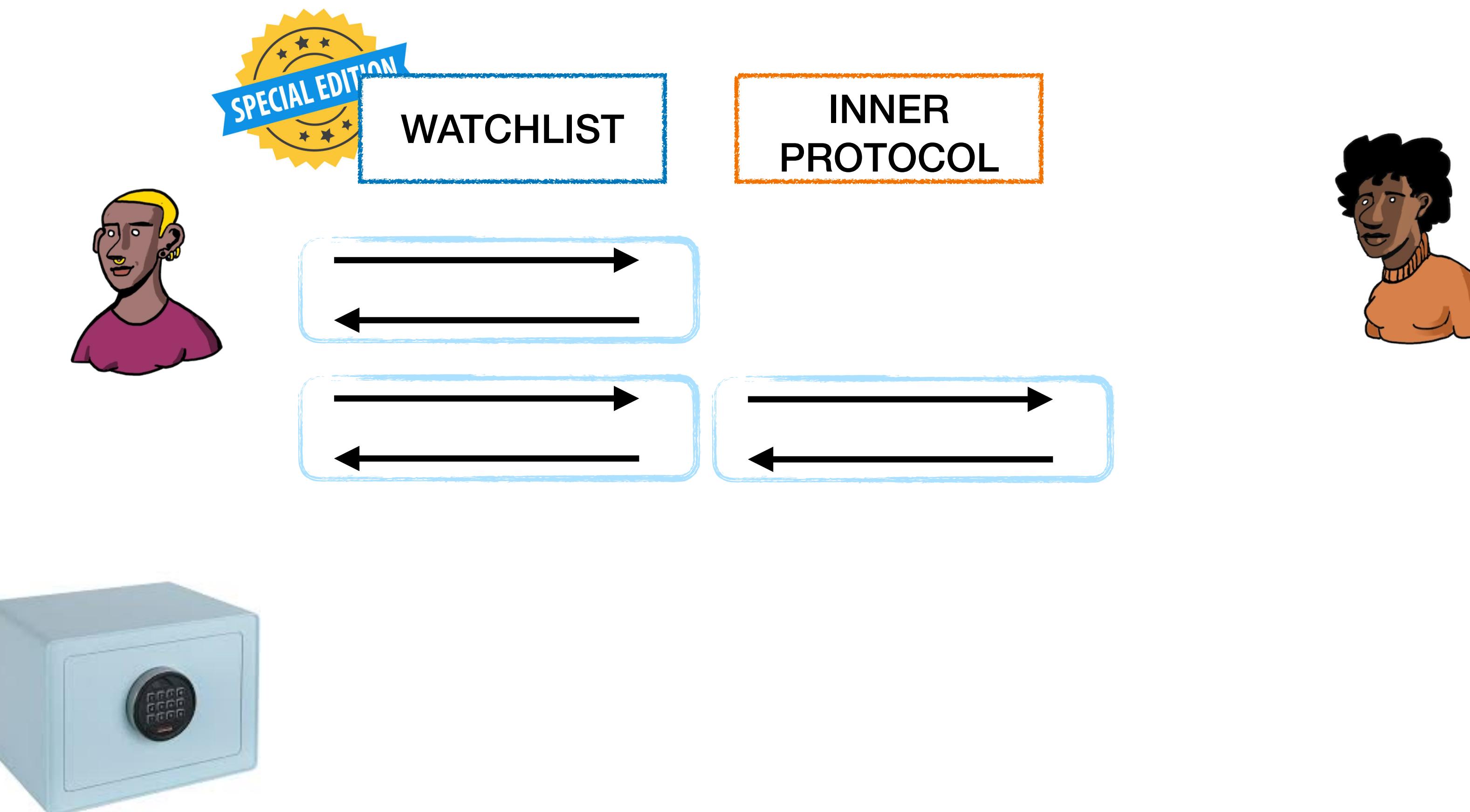
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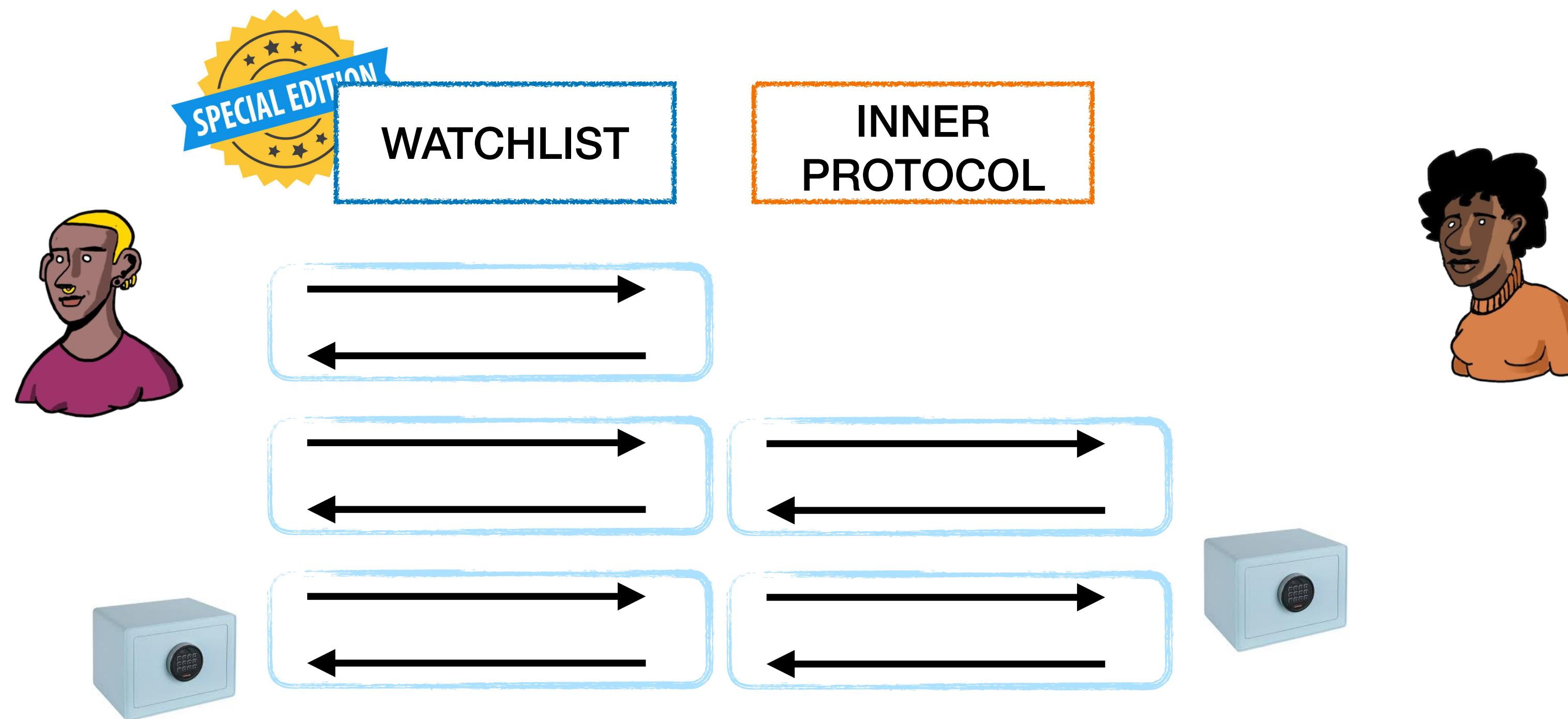
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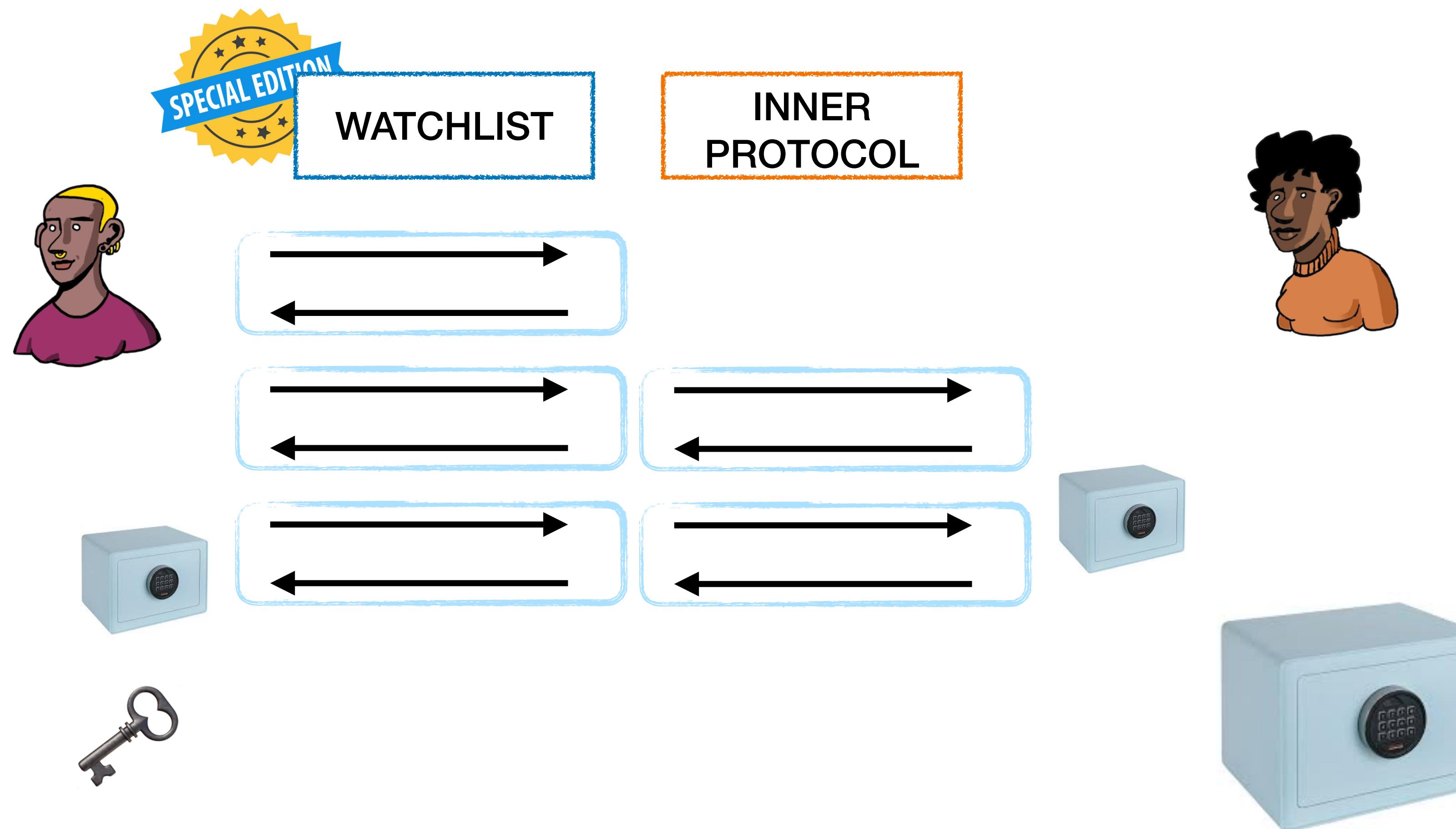
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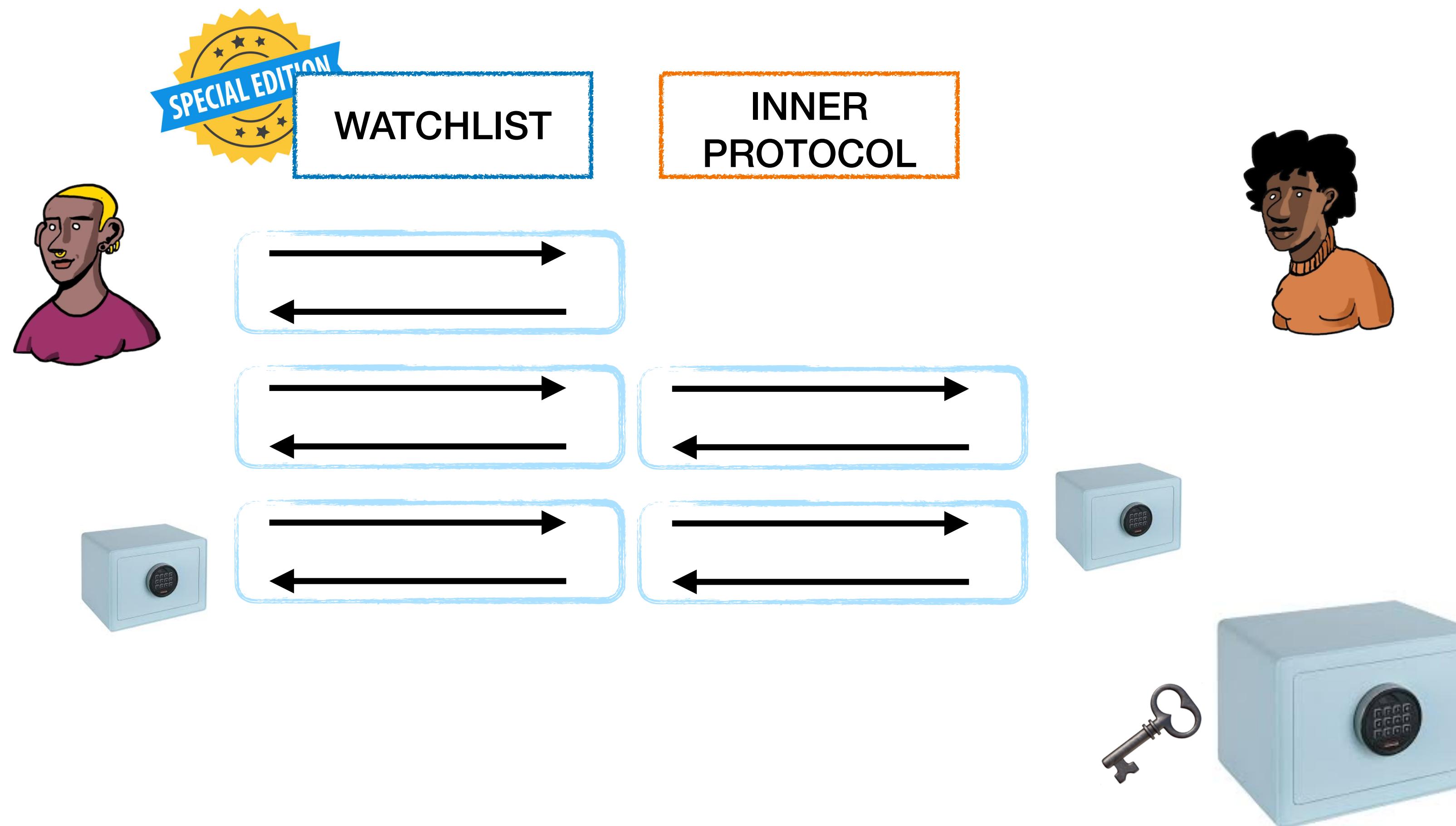
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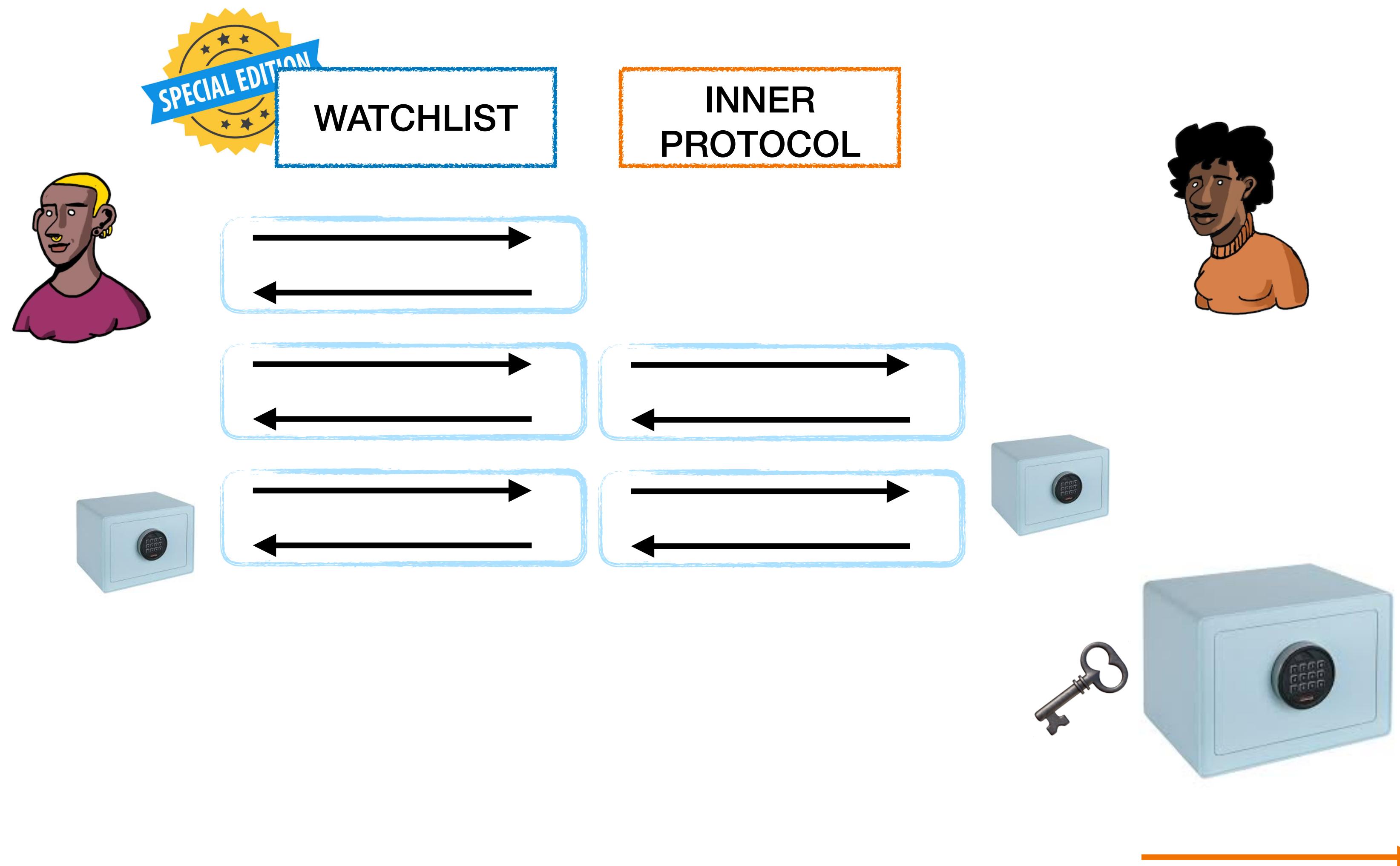
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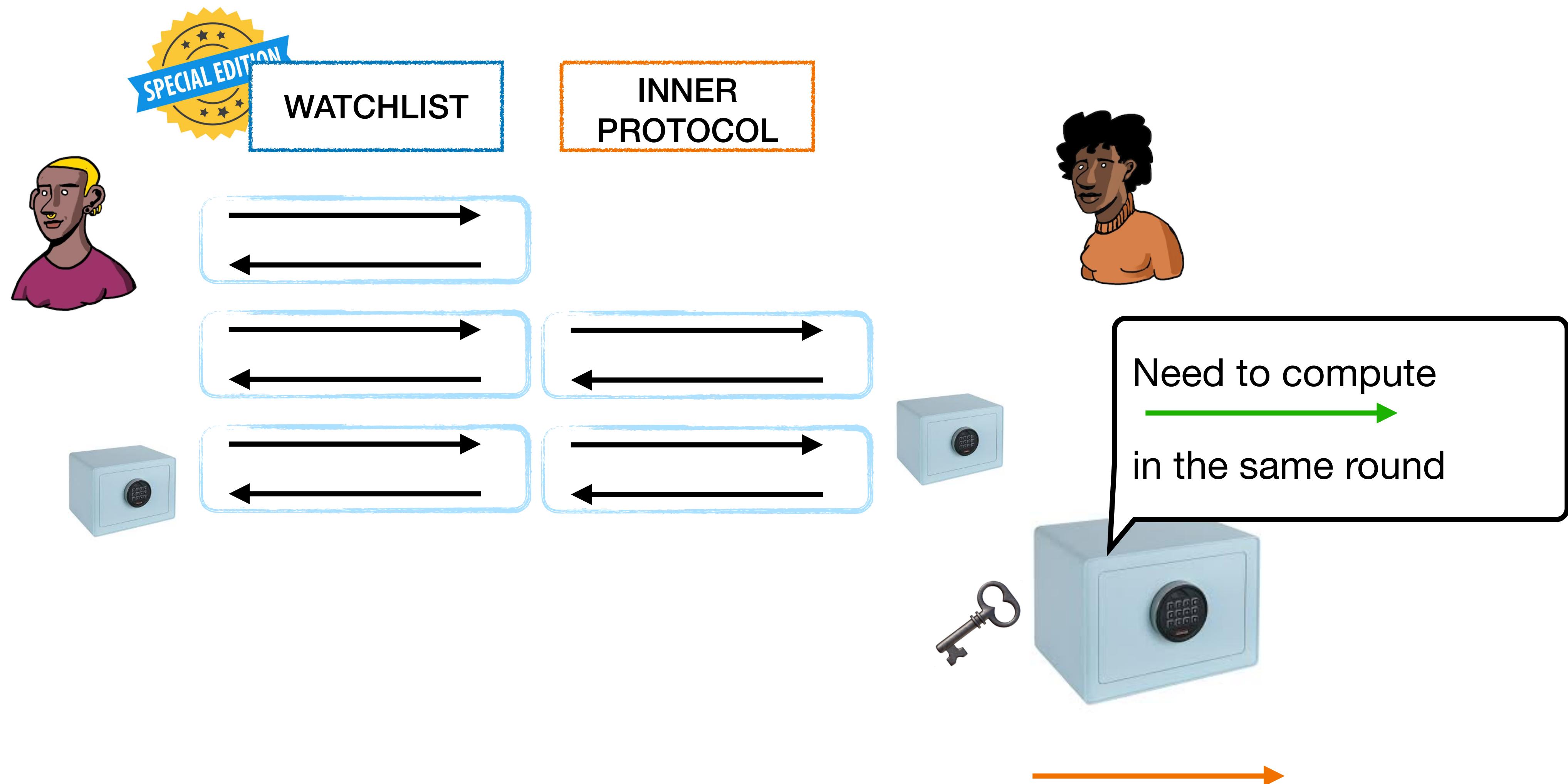
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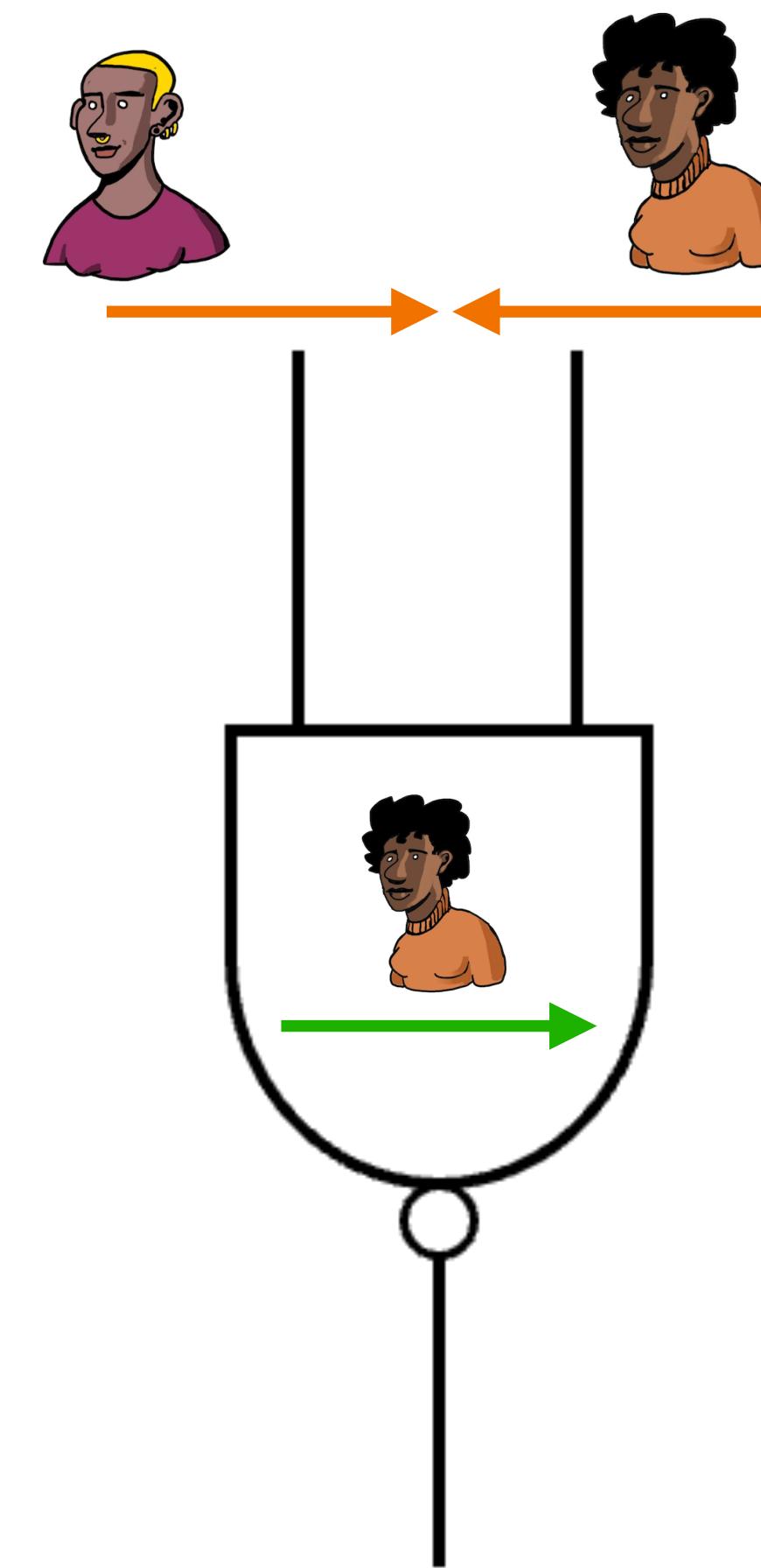
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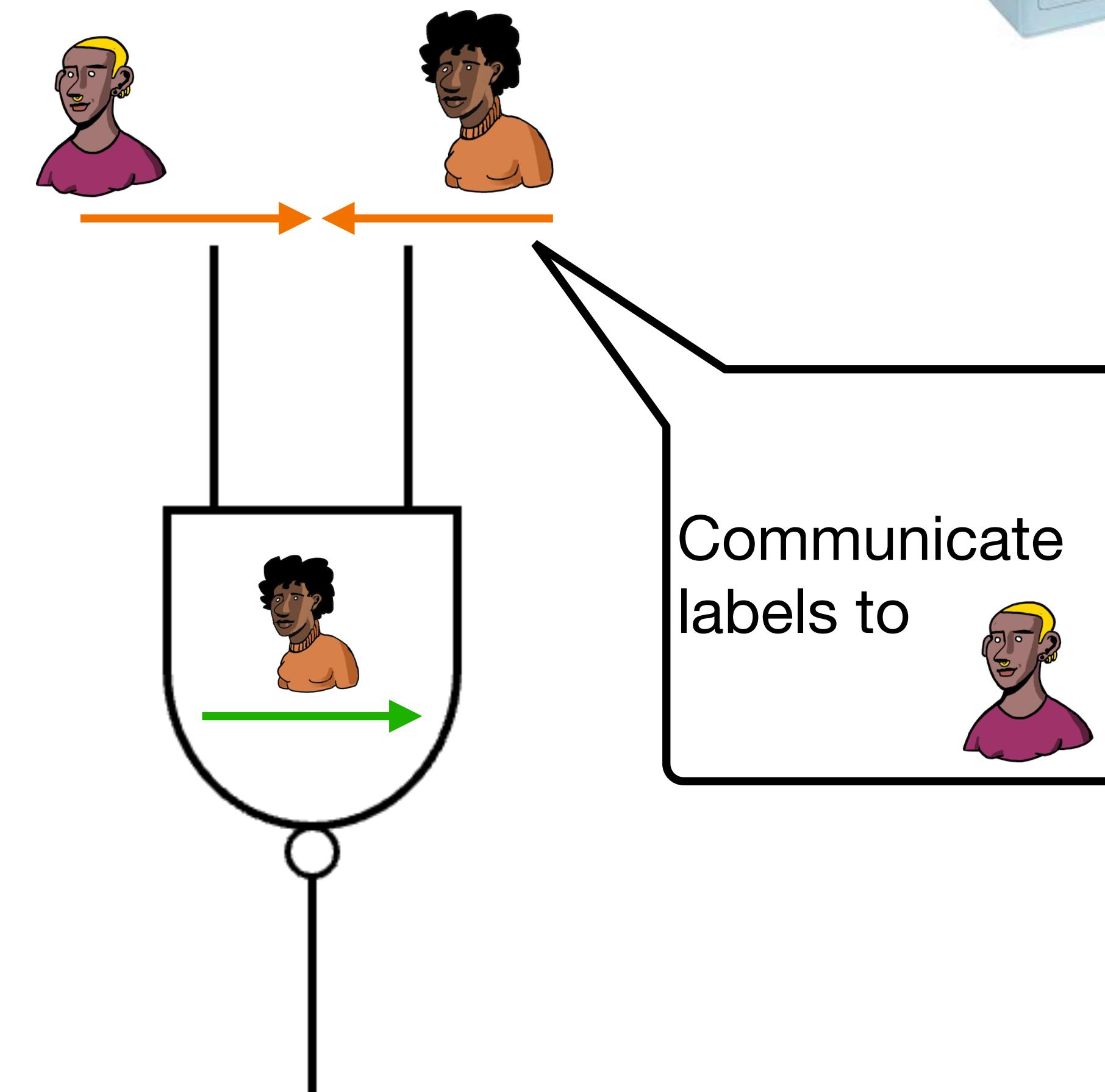
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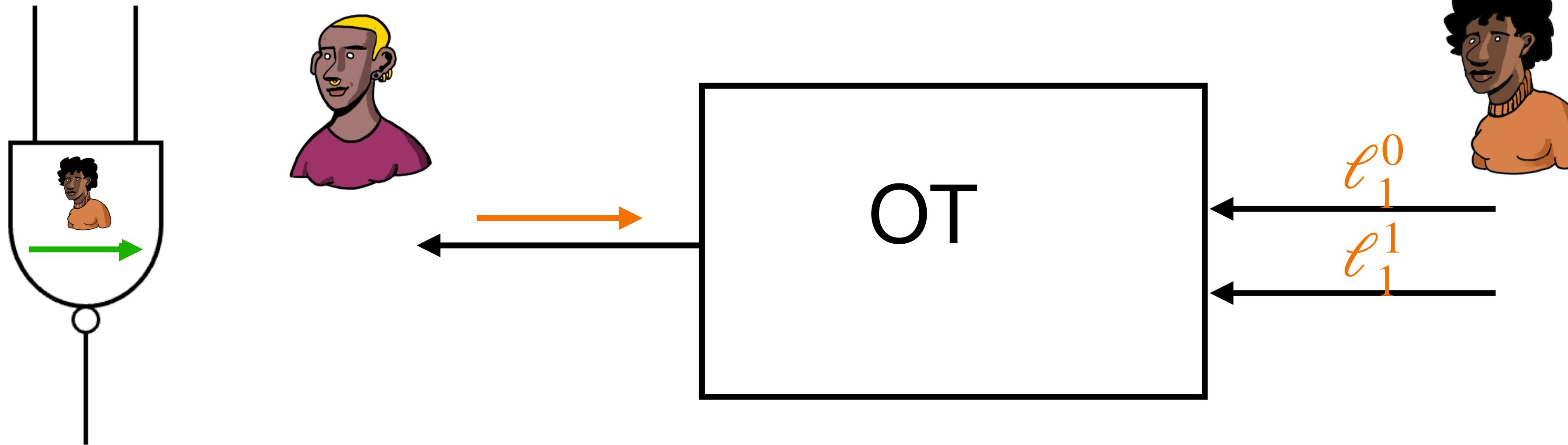
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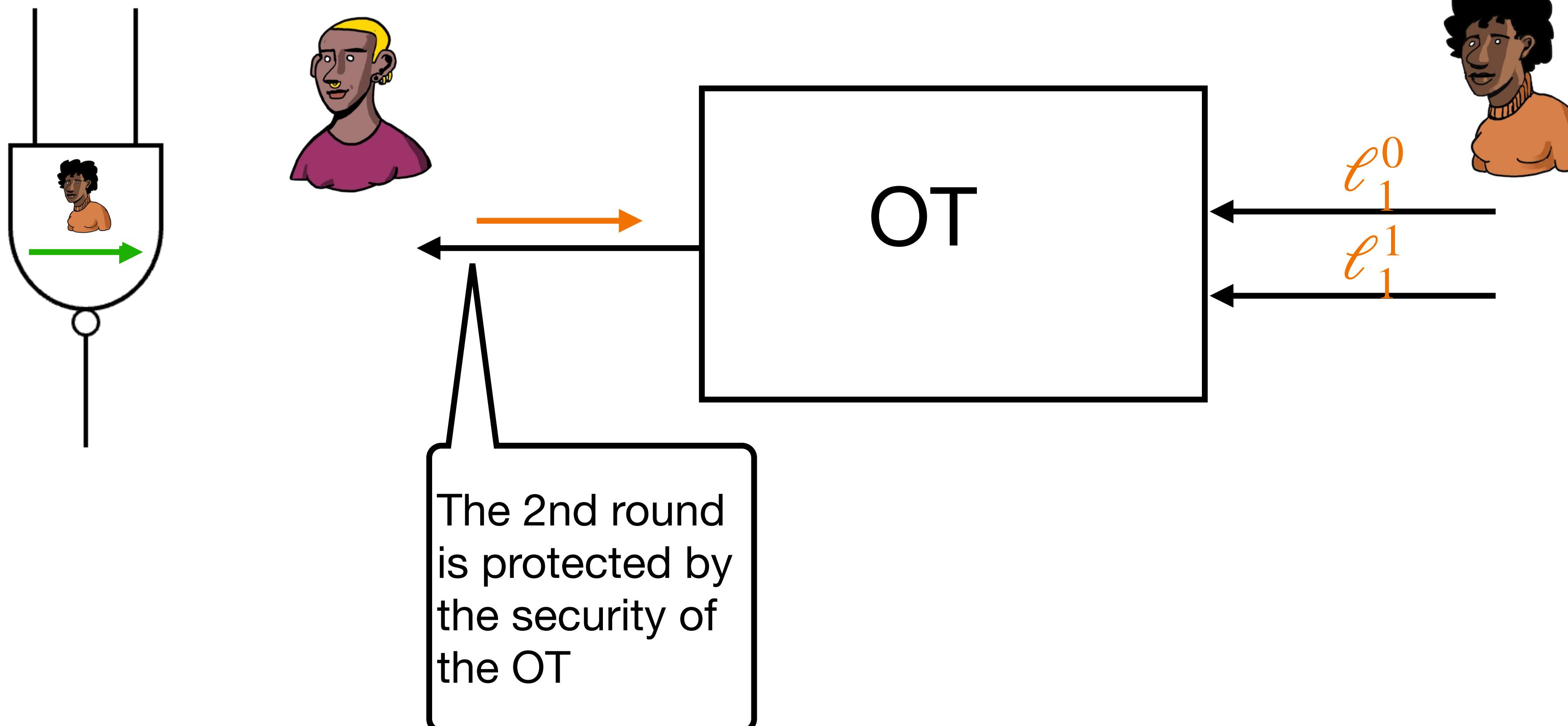
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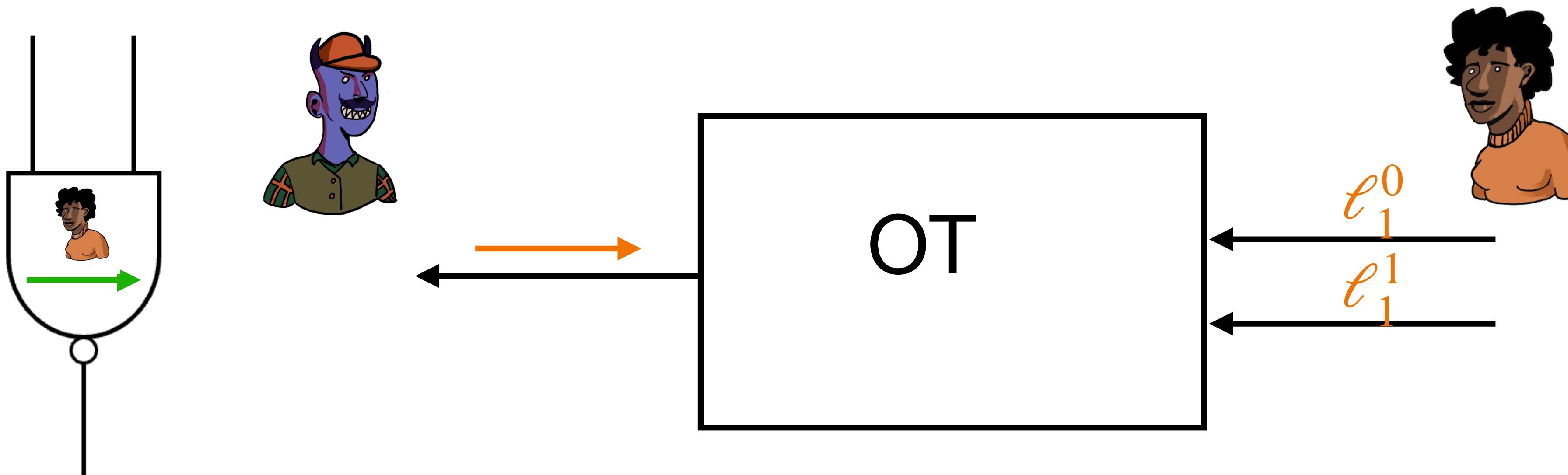
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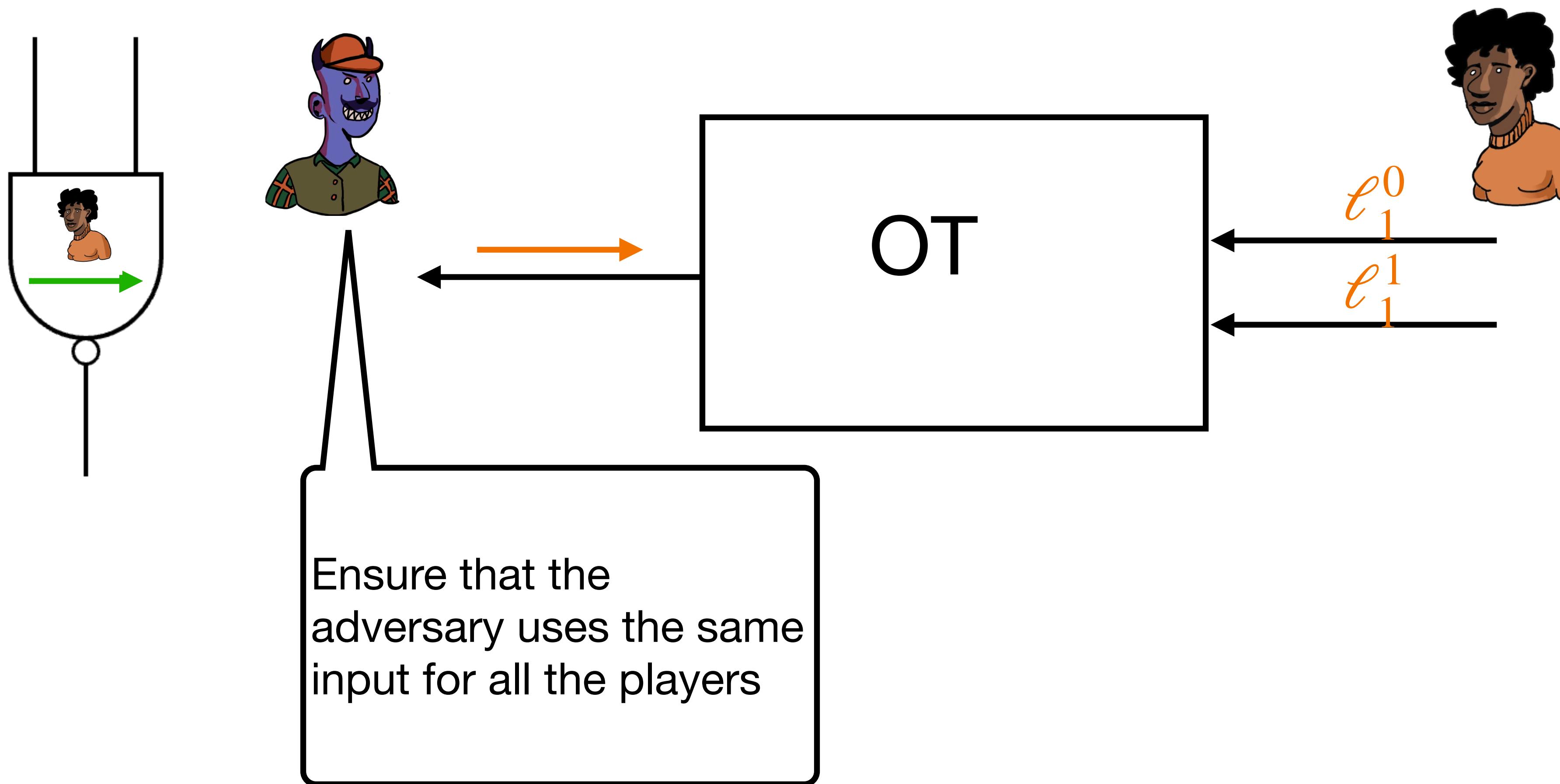
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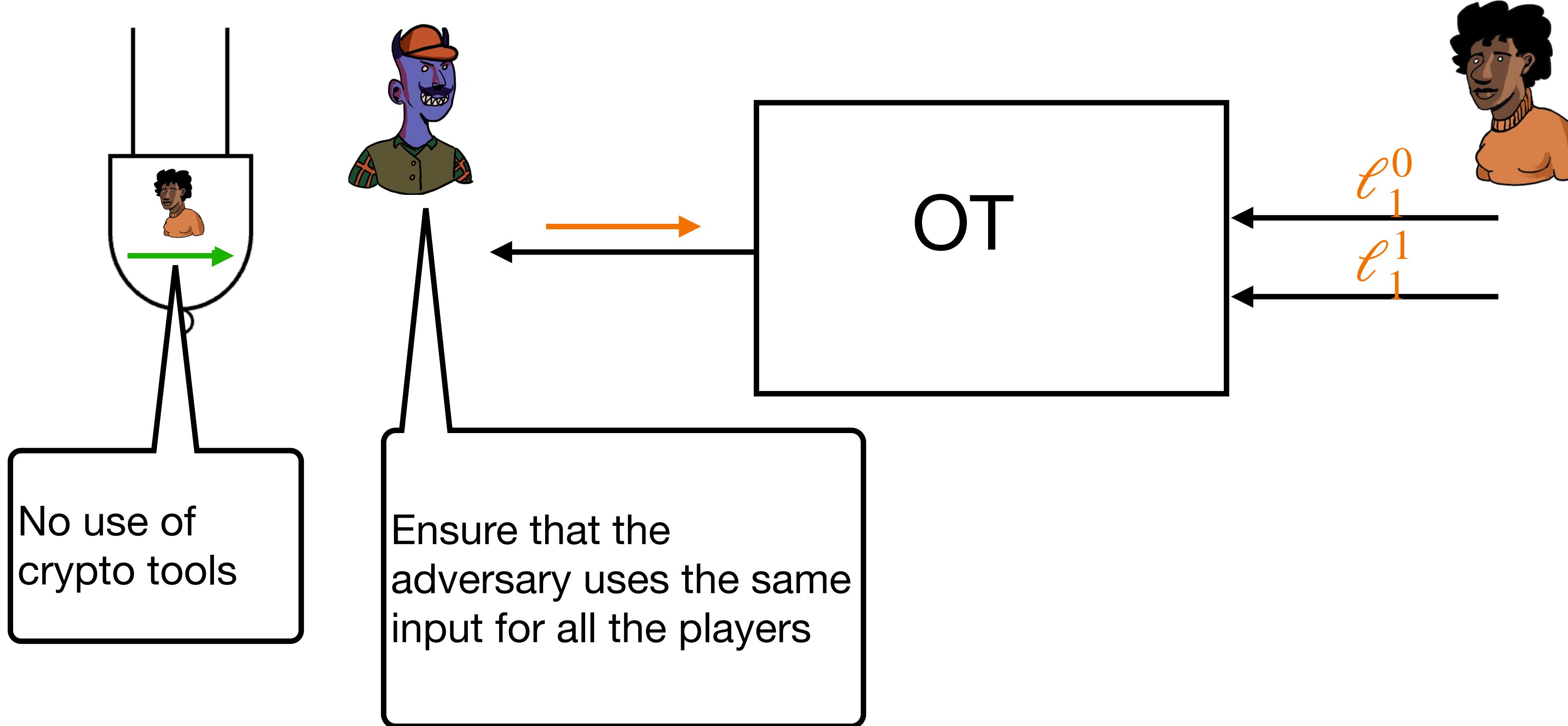
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