

Multi-Client Functional Encryption with Public Inputs and Strong Security

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Talk is given by: Robert Schädlich¹



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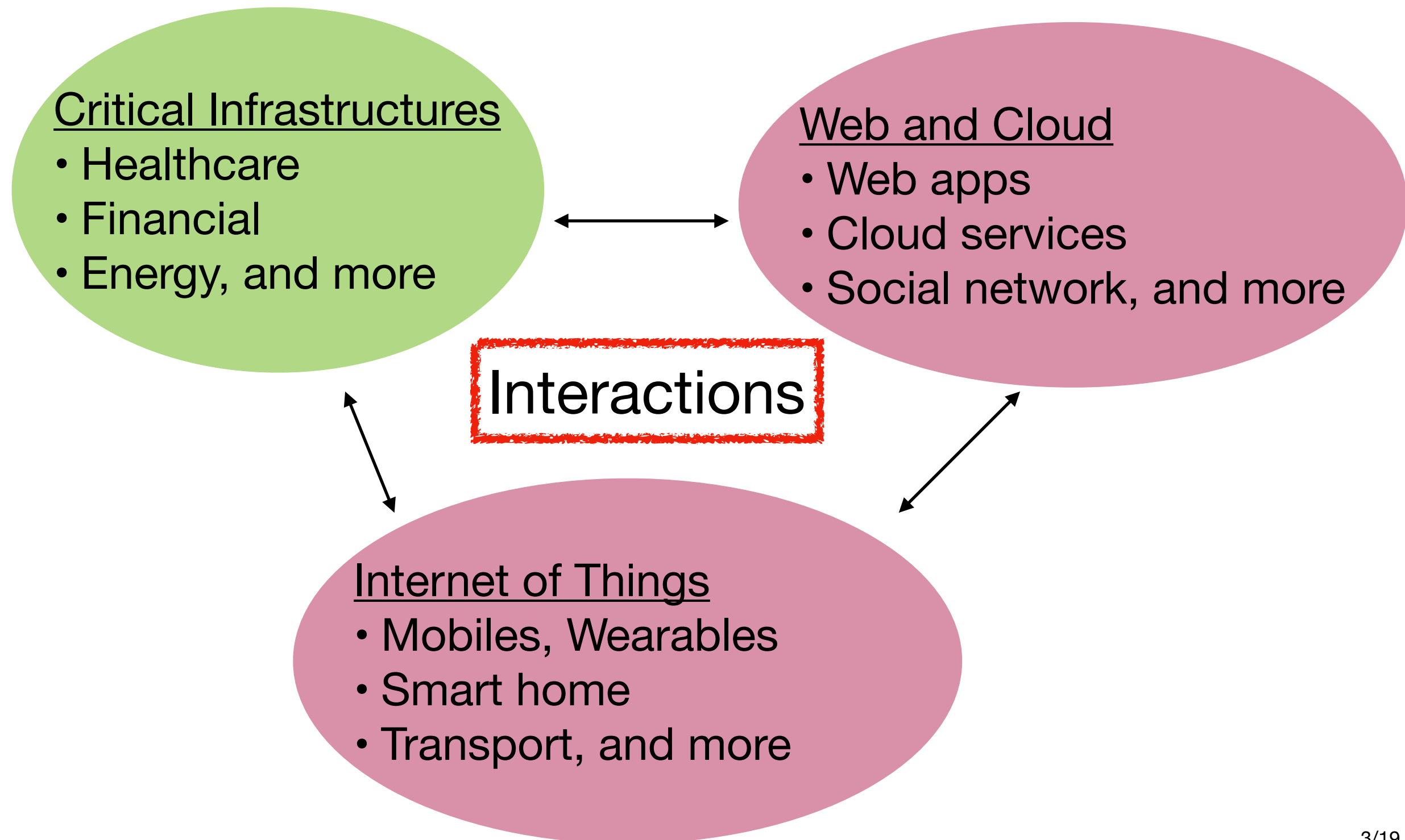
³ LTCI, Telecom Paris, Institut Polytechnique de Paris, France

Outline

1. Motivation: Multiple Senders in Functional Encryption
2. Related Works
 - a. Fine-Grained Access Control in Functional Encryption
 - b. Revisiting Existing Security Notions
3. Our Contributions
4. Technical Highlights: Achieving Adaptive Security
5. Conclusion

Evolution of Information

Multiple sources, Complex Ecosystems

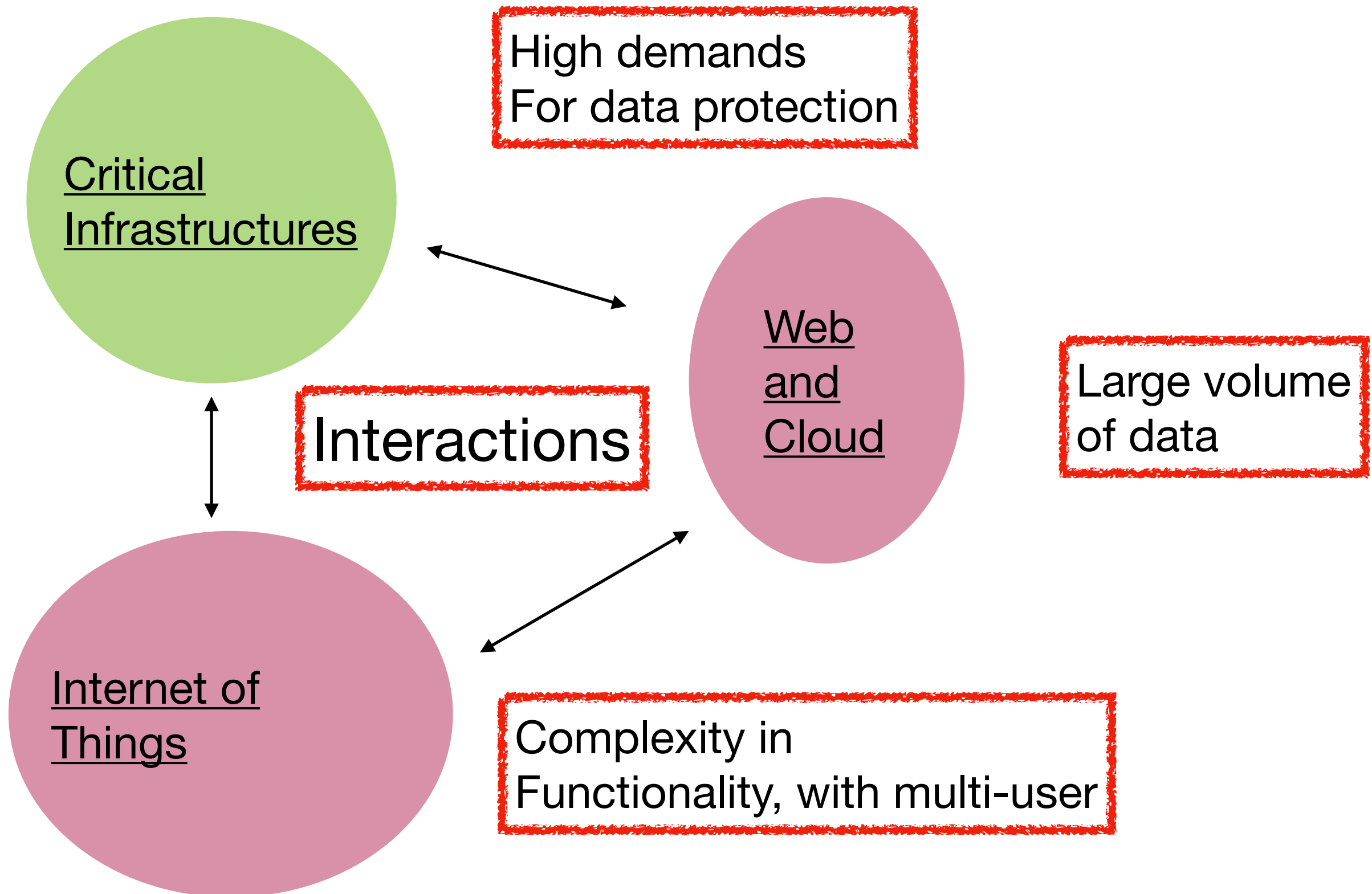


Evolution of Information

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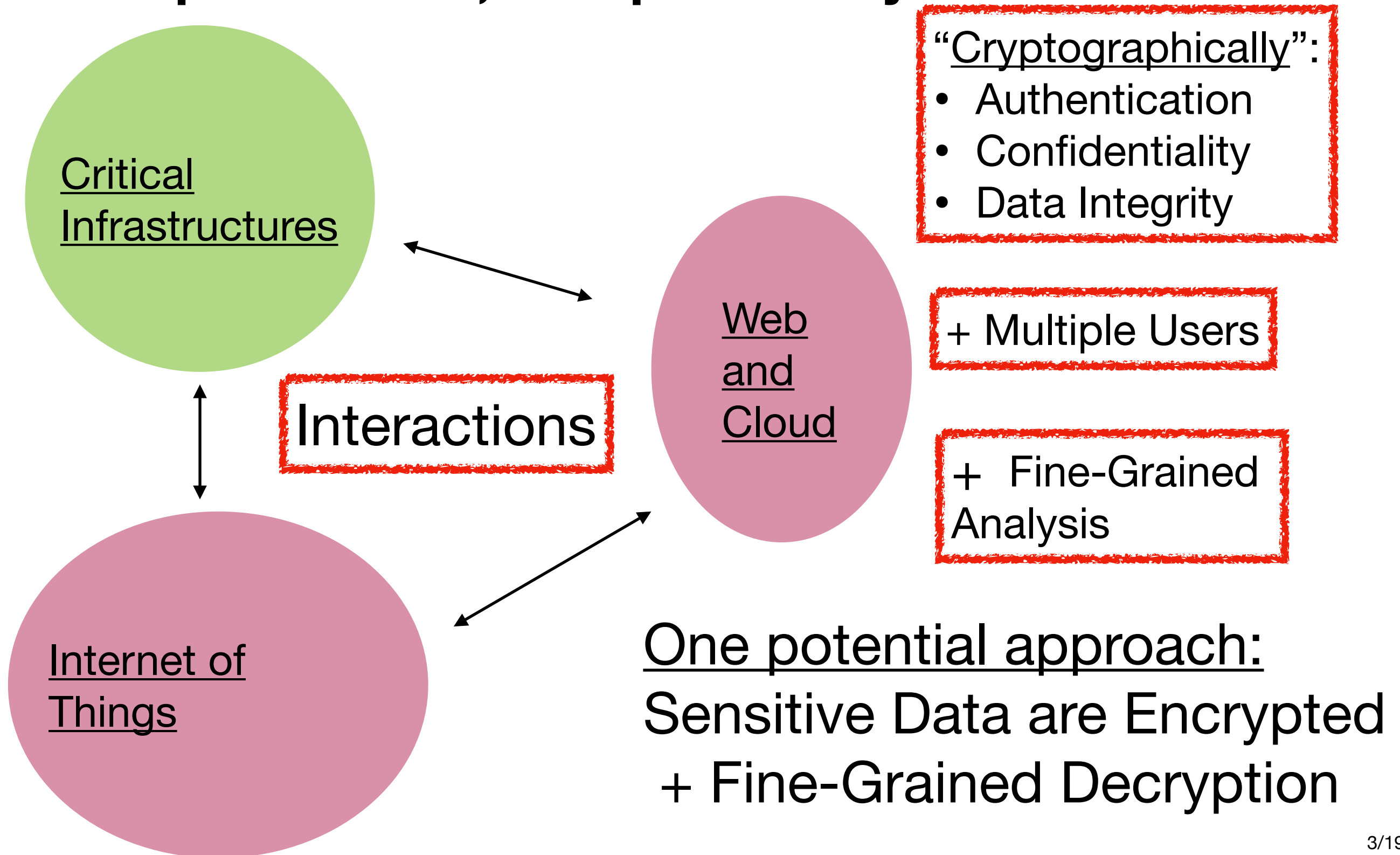


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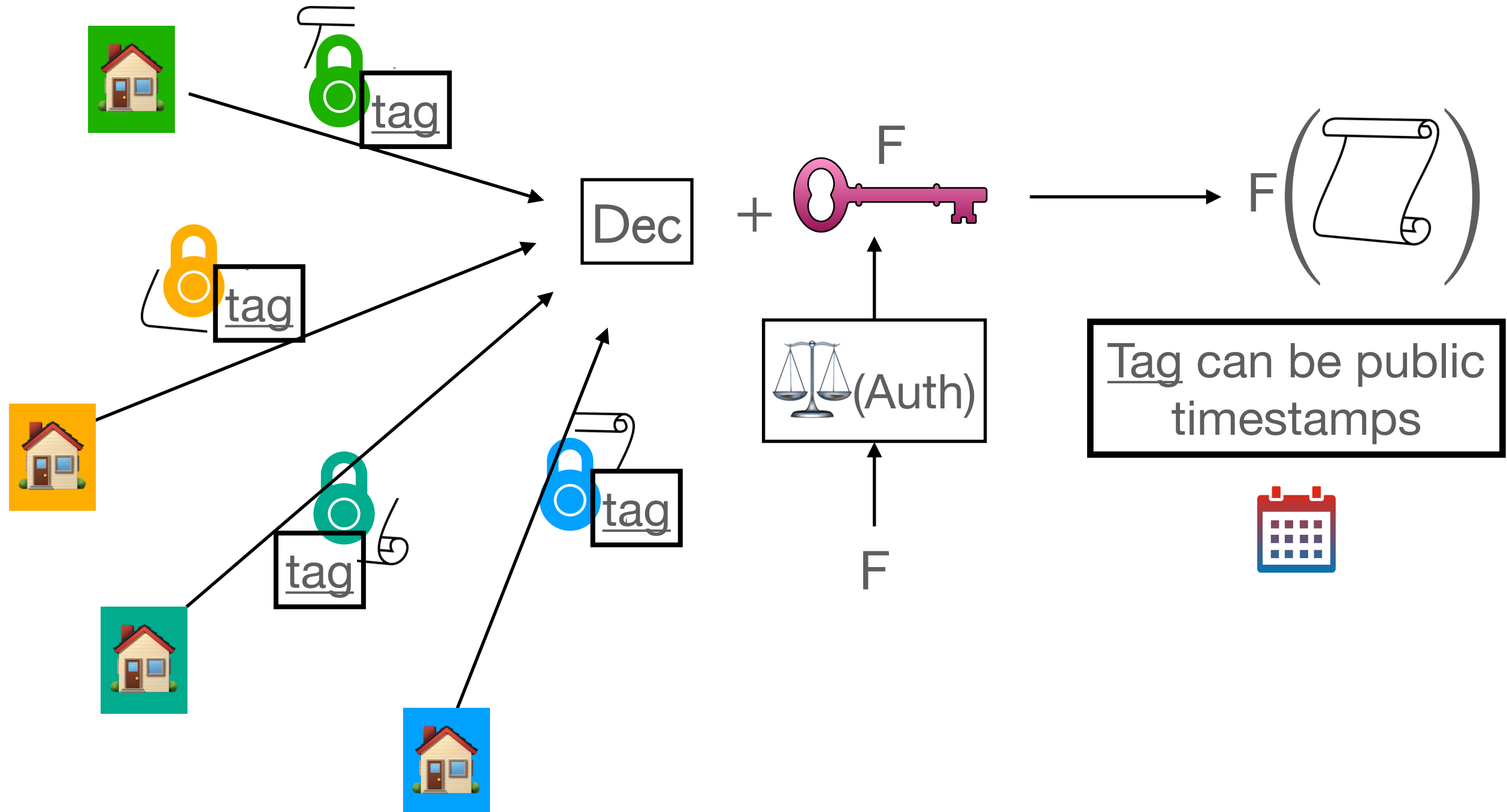
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Evolution of Information

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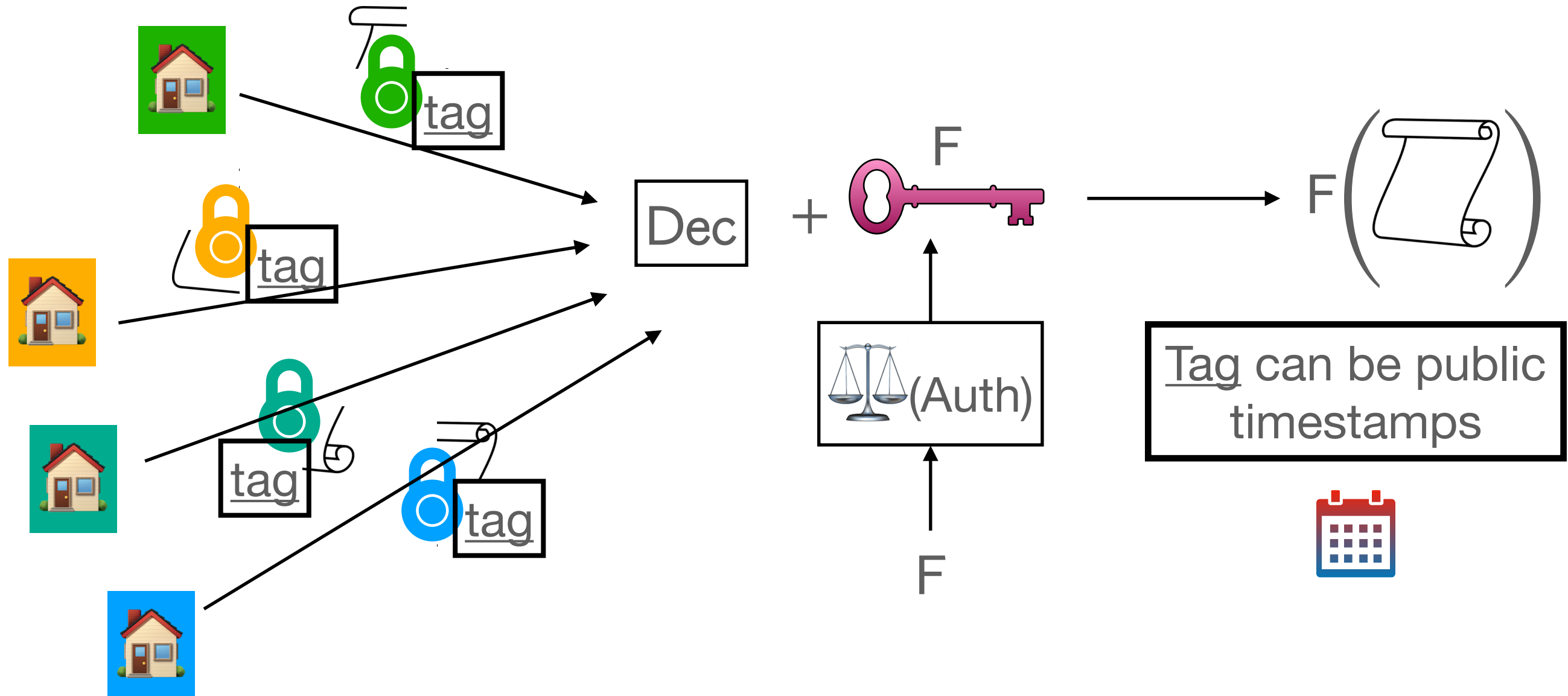


Multi-Client Functional Encryption (MCFE) [GGG+14, CDGPP18]



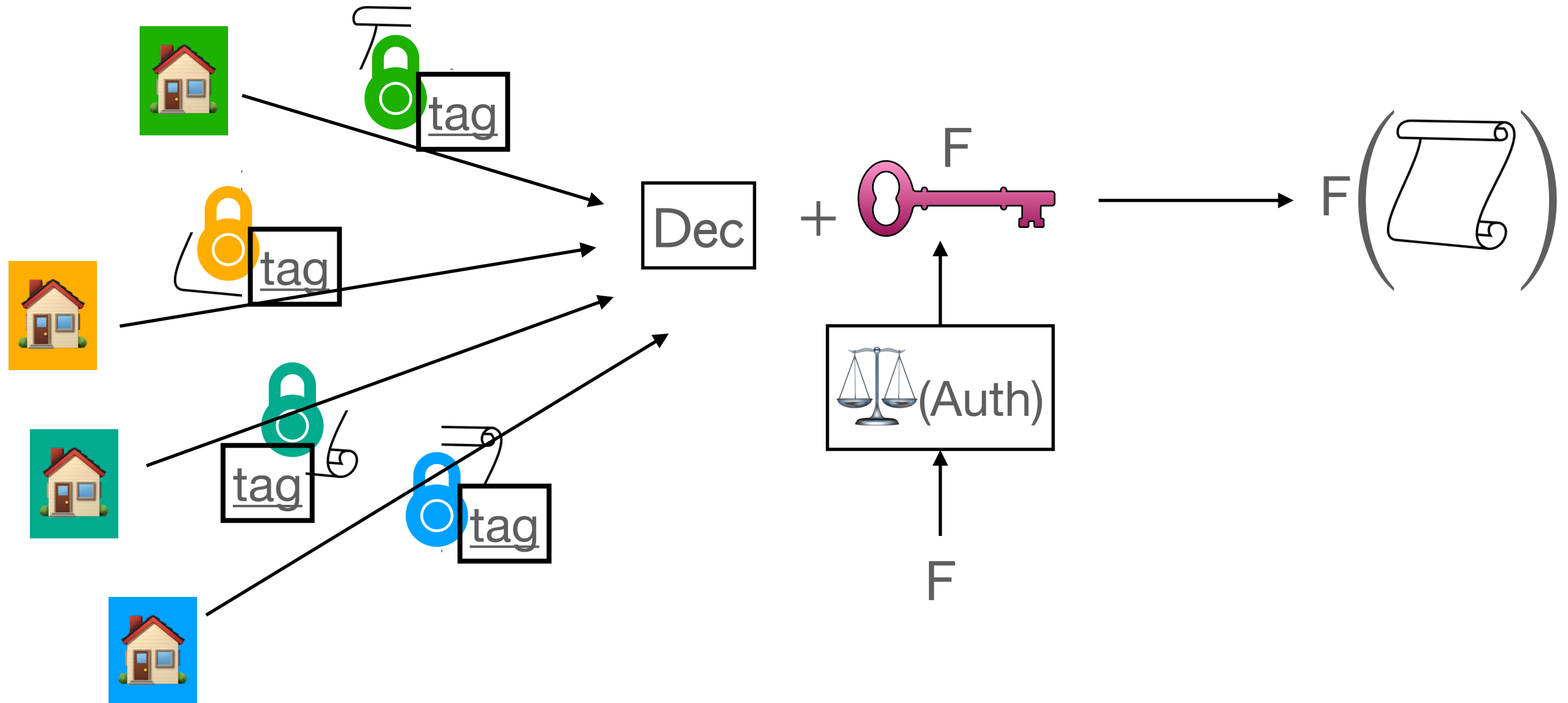
MCFE [GGG+14,CDGPP18]

How to Encrypt?



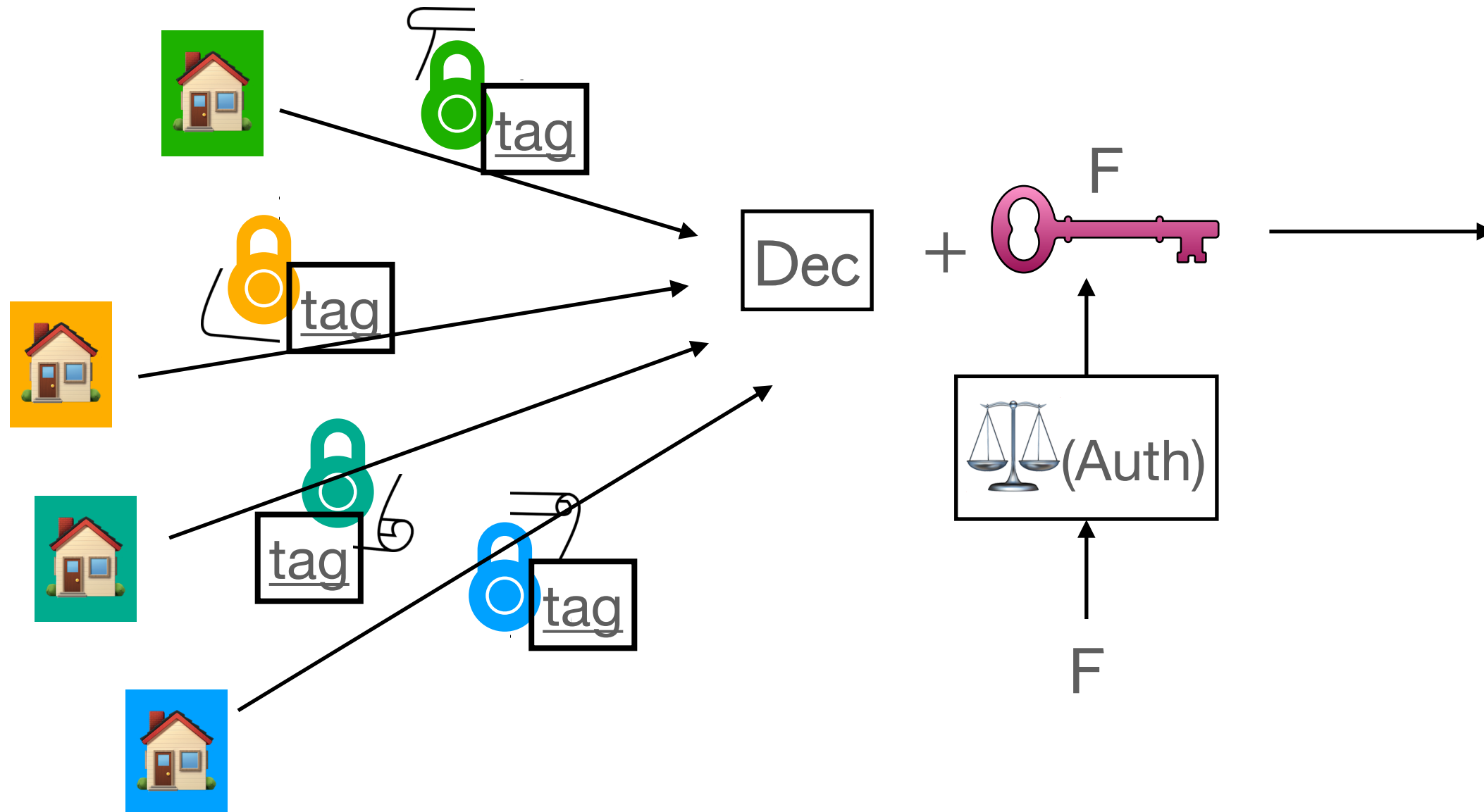
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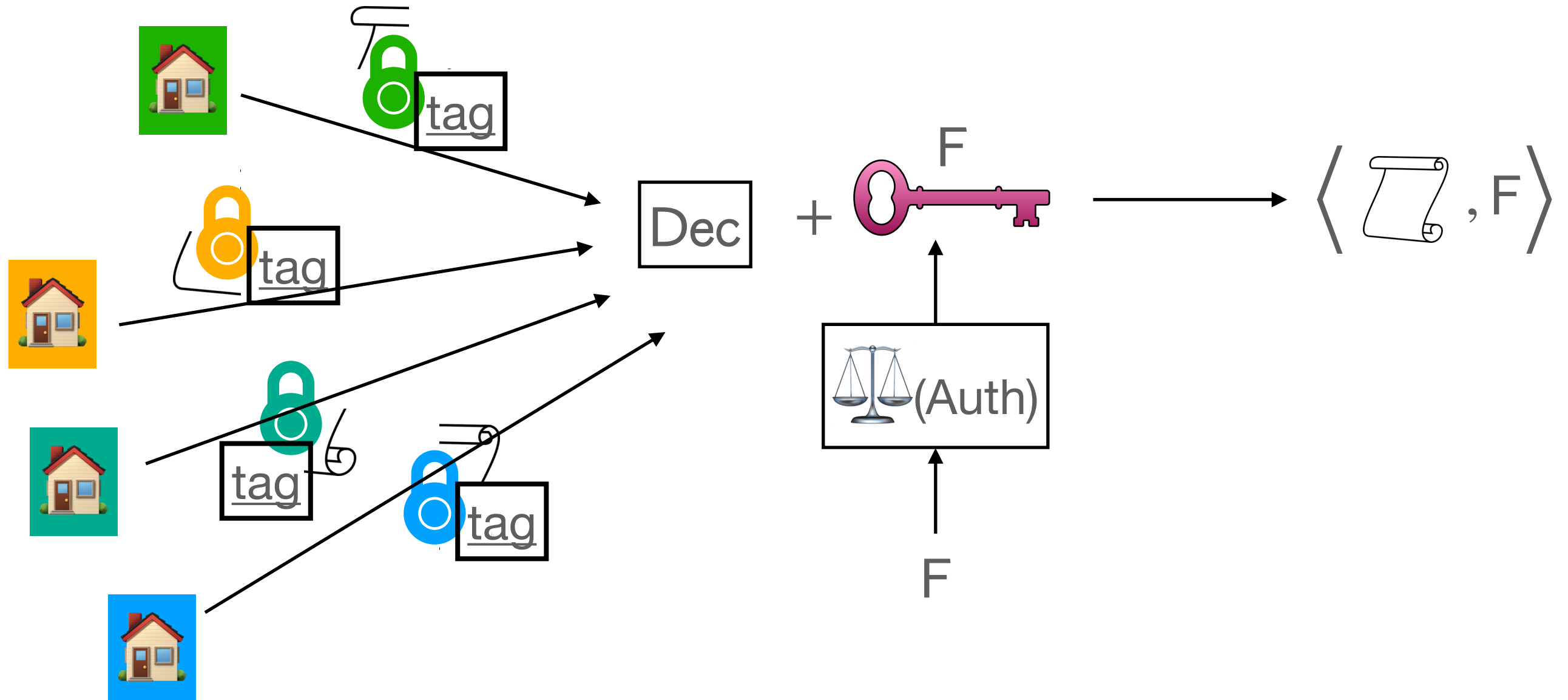
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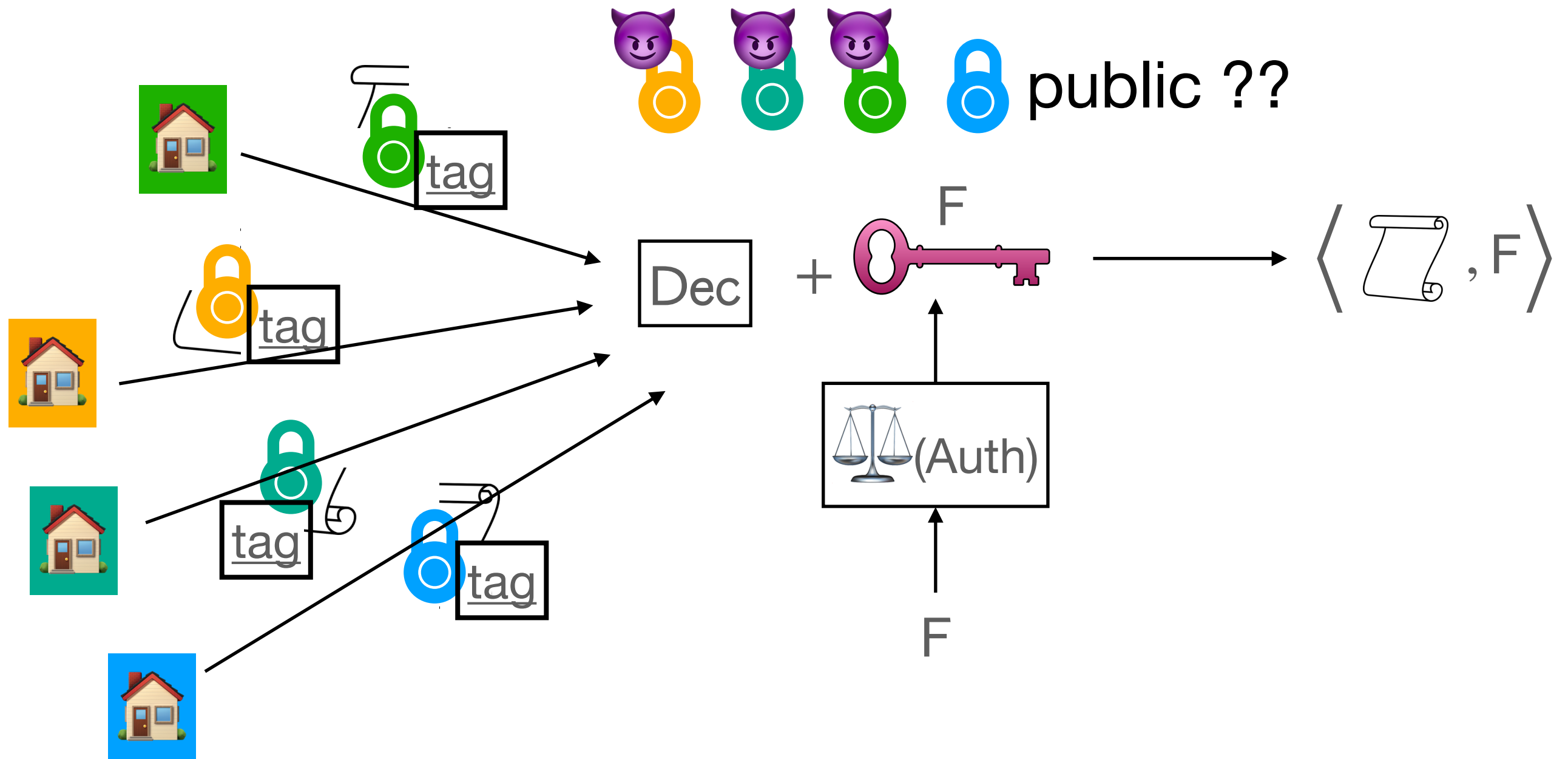
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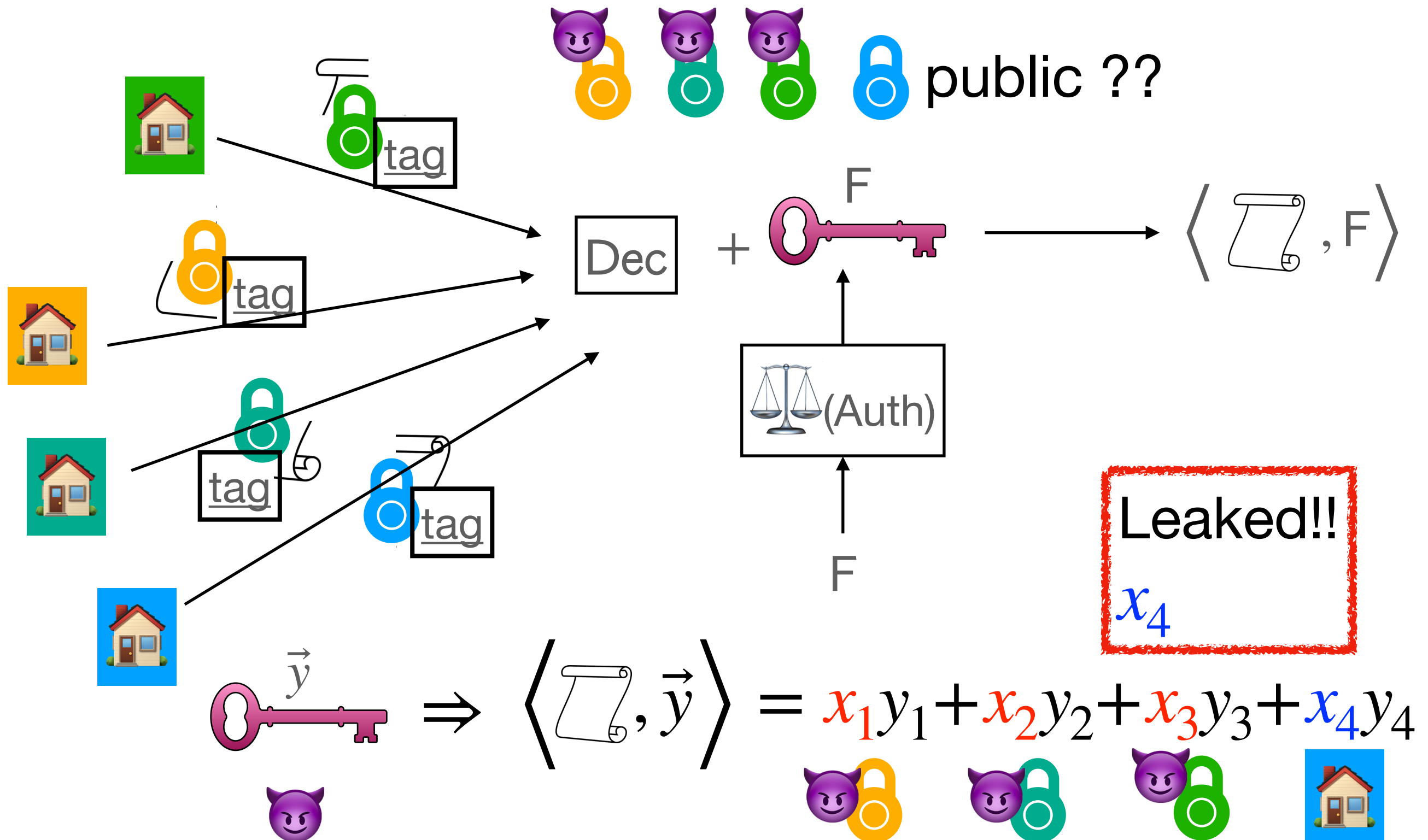
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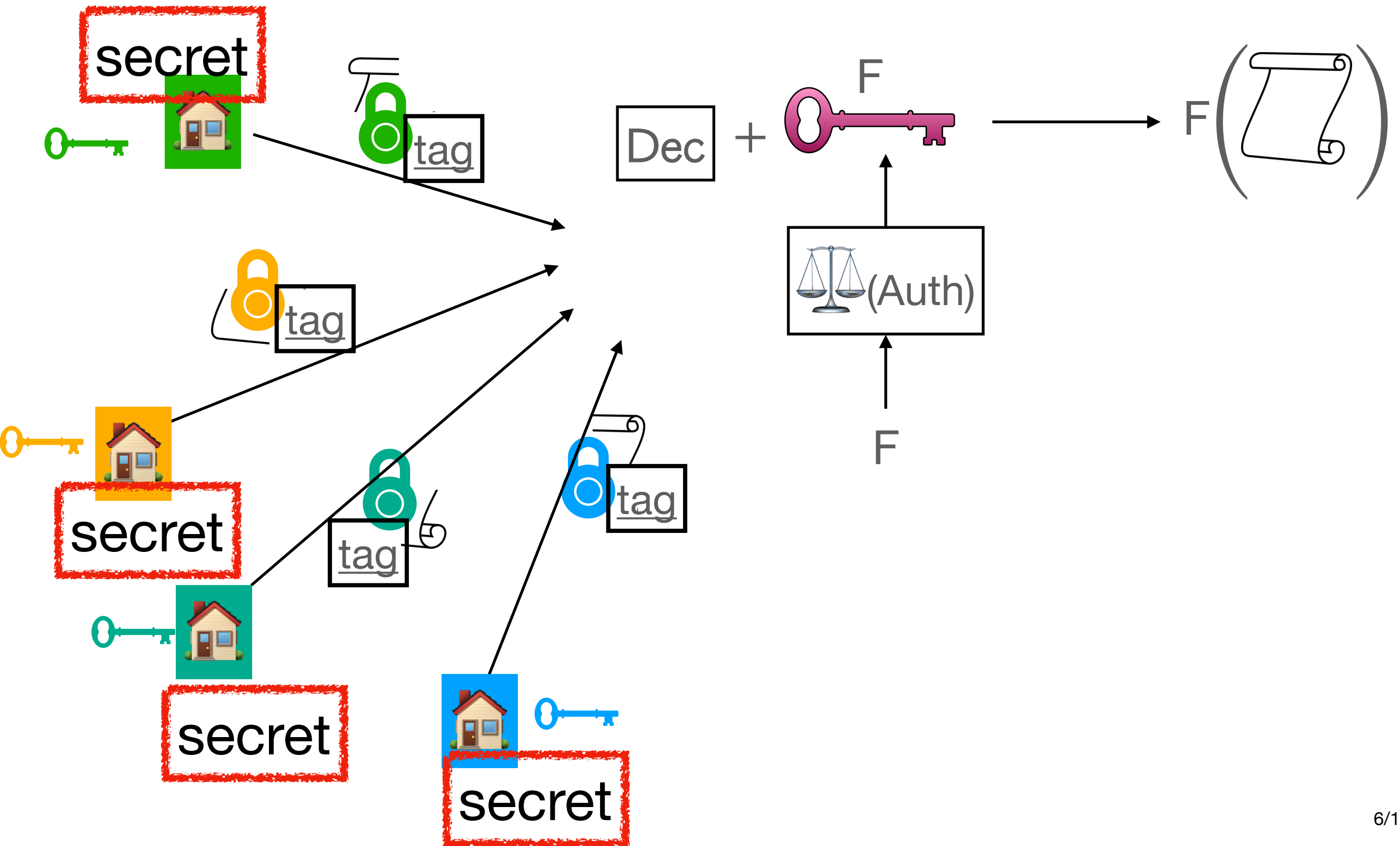
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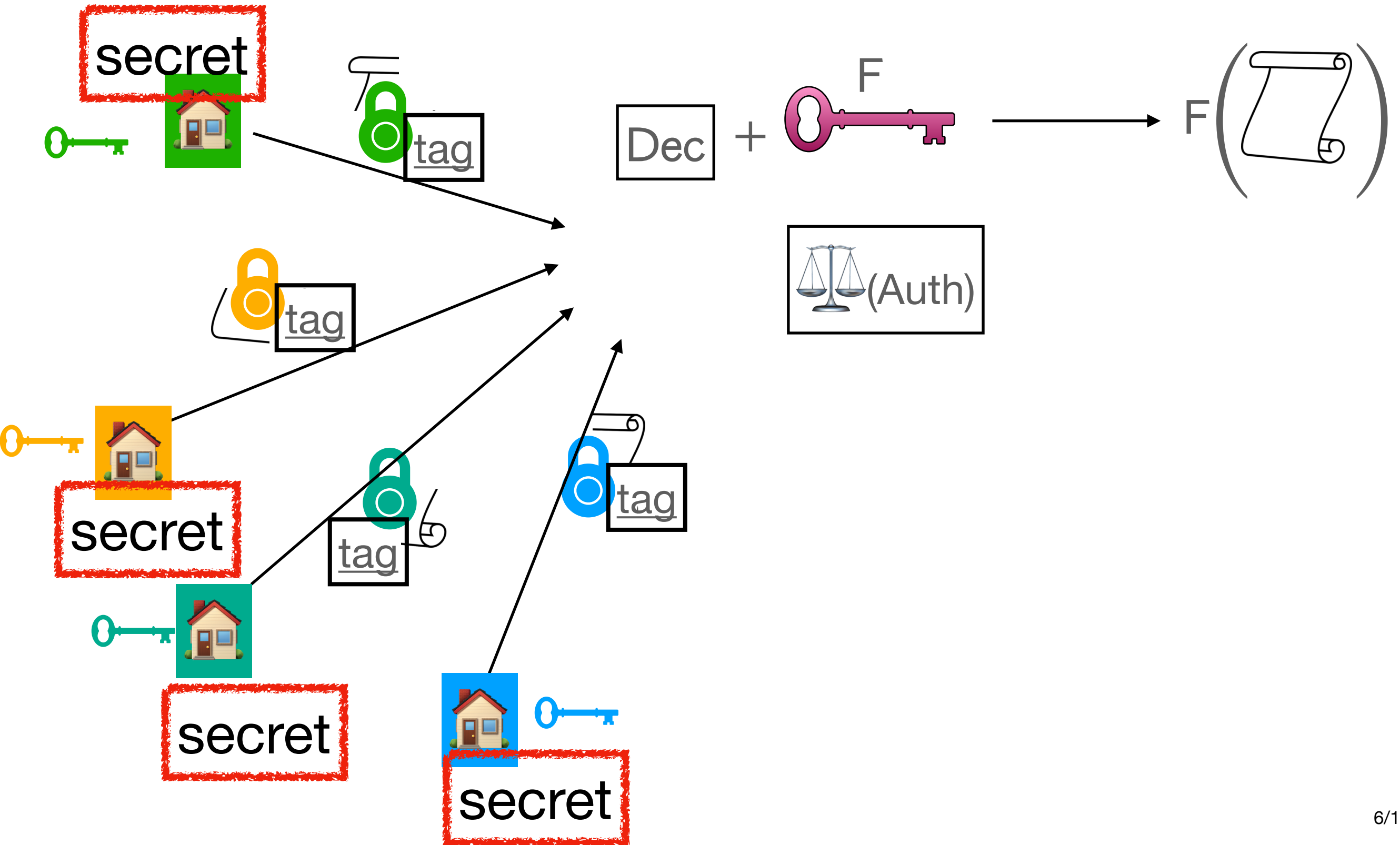
Changes in Model

MCFE [GGG+14,CDGPP18] - **Secret** Encryption Keys



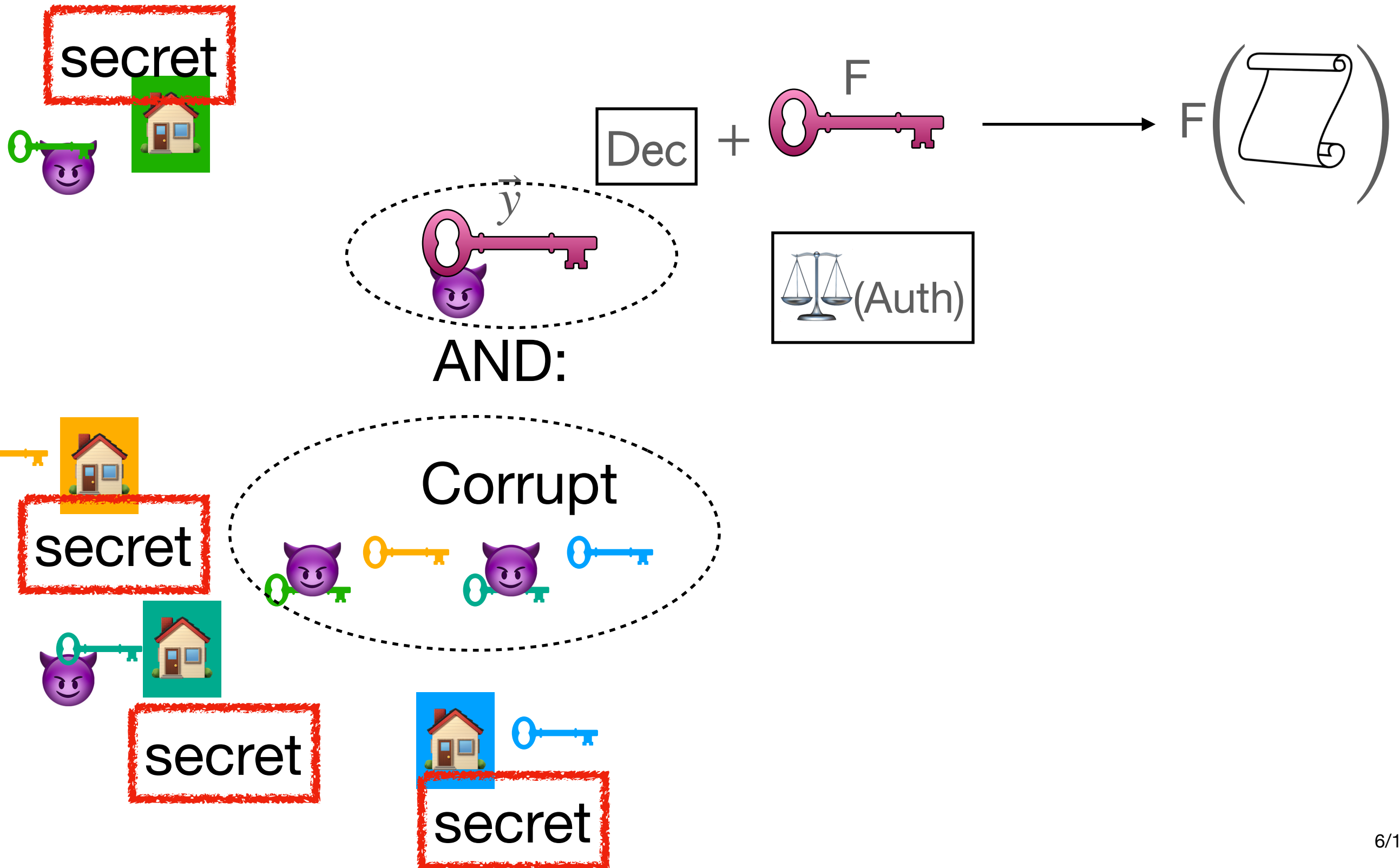
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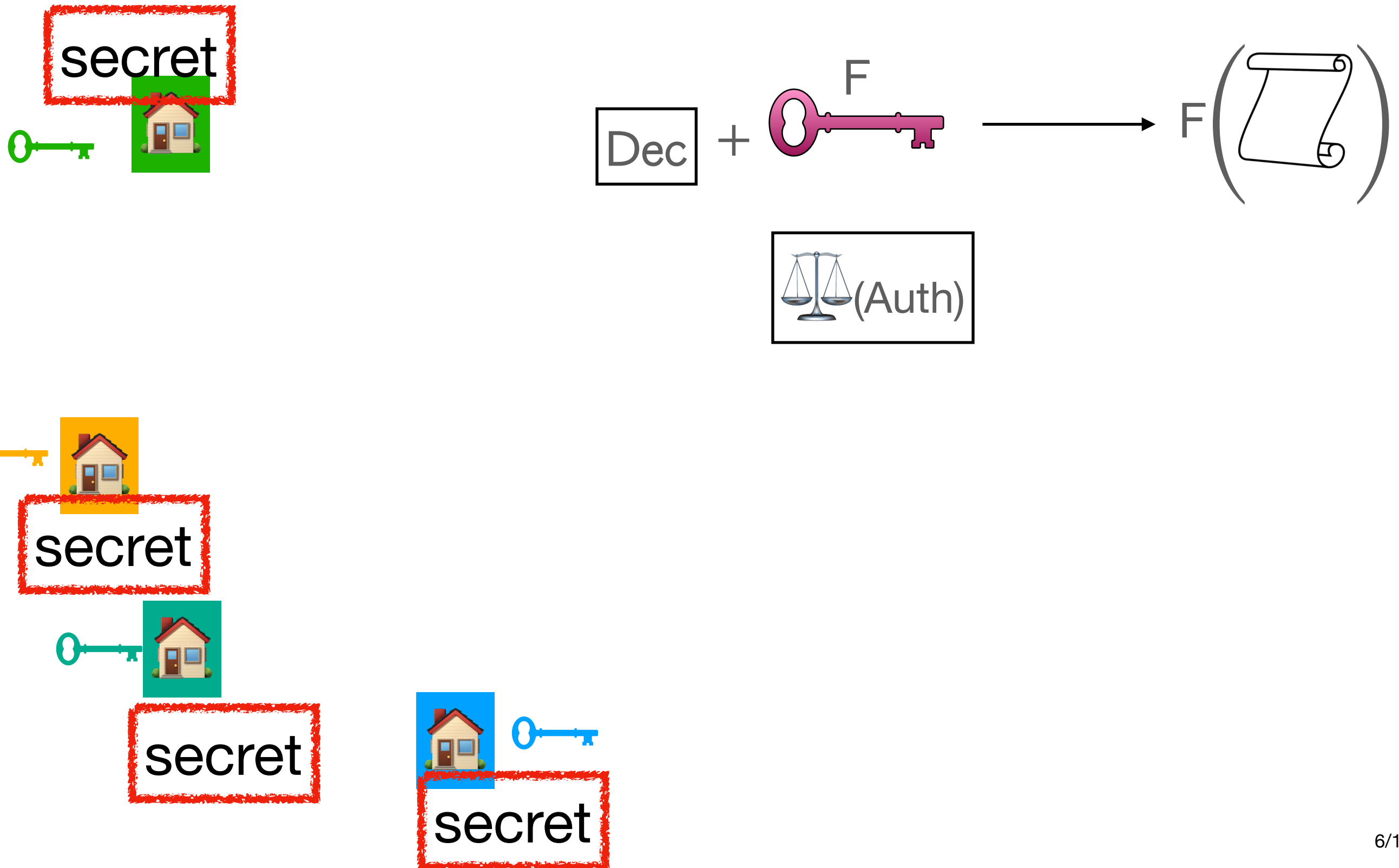
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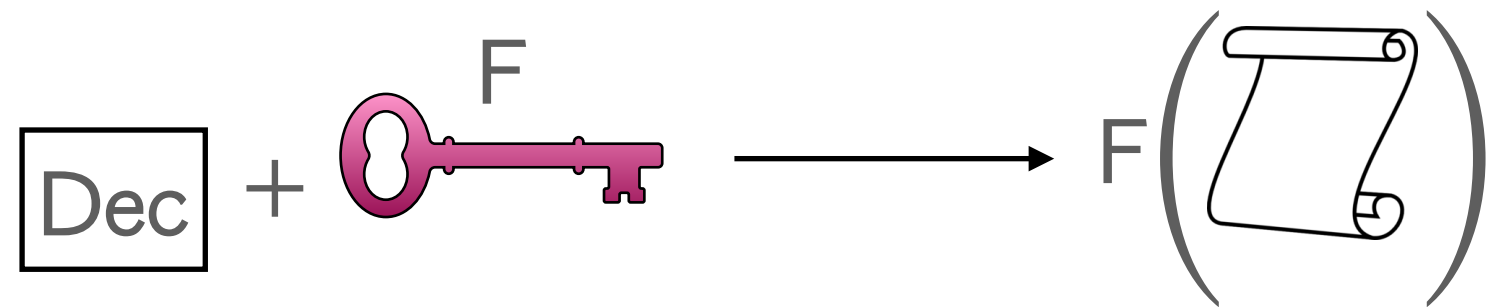
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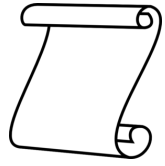
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[GGG+14,CDGPP18]

“vanilla” syntax

$\underline{F}(\text{scroll})$:

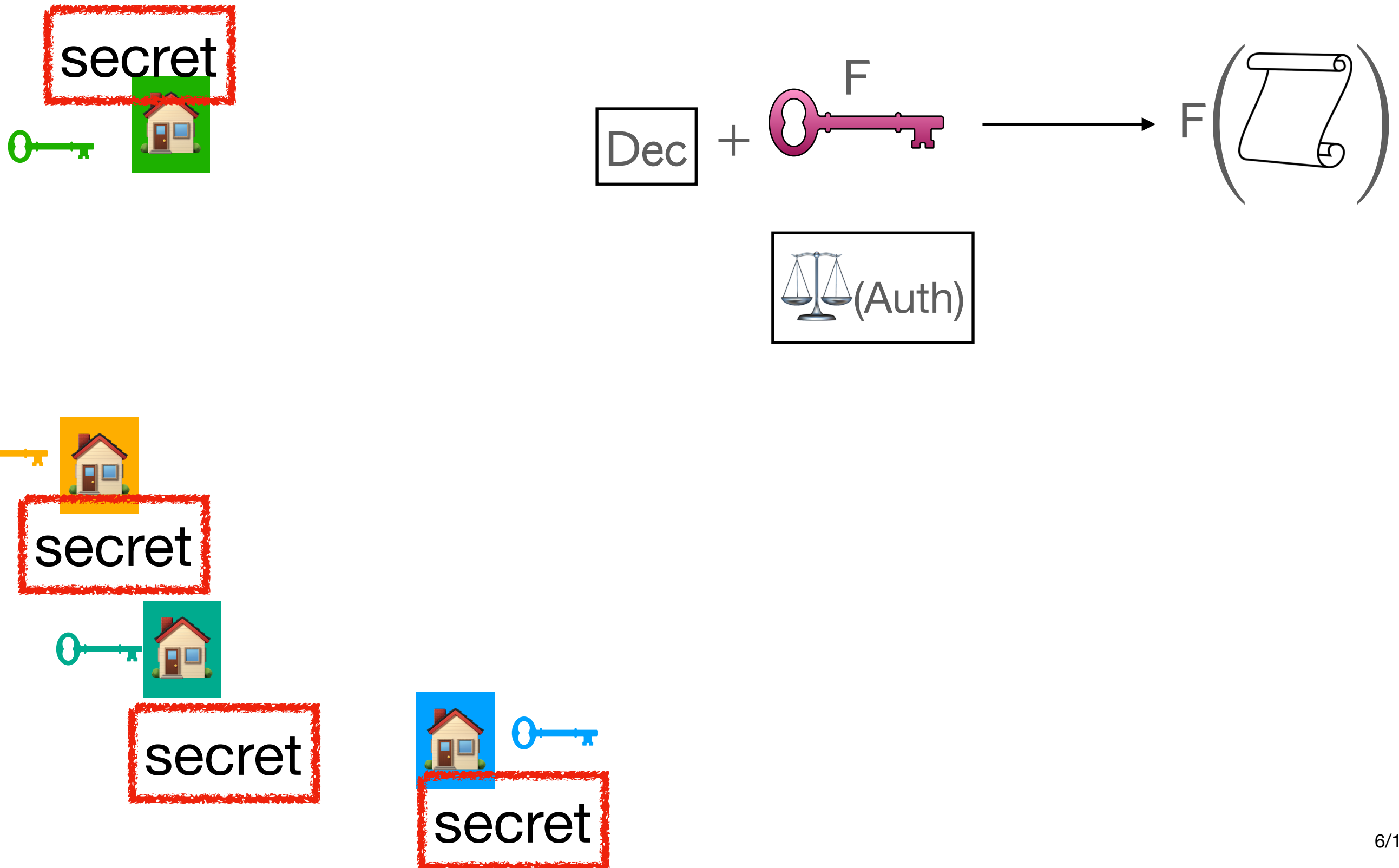
Parse **Att**,  = 

If **Pol(Att) = True** then 

Else “Nothing”

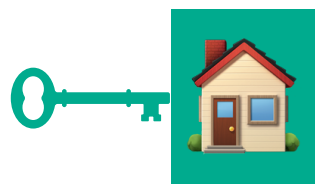
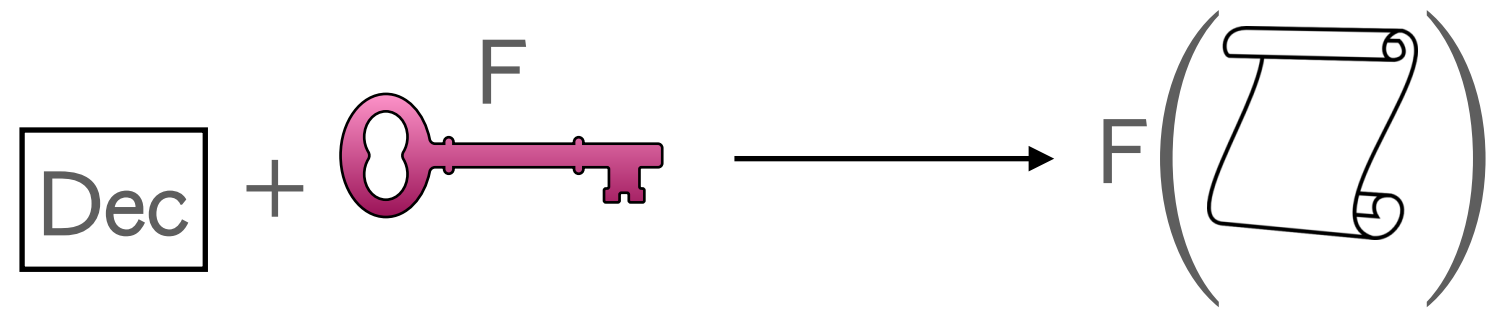
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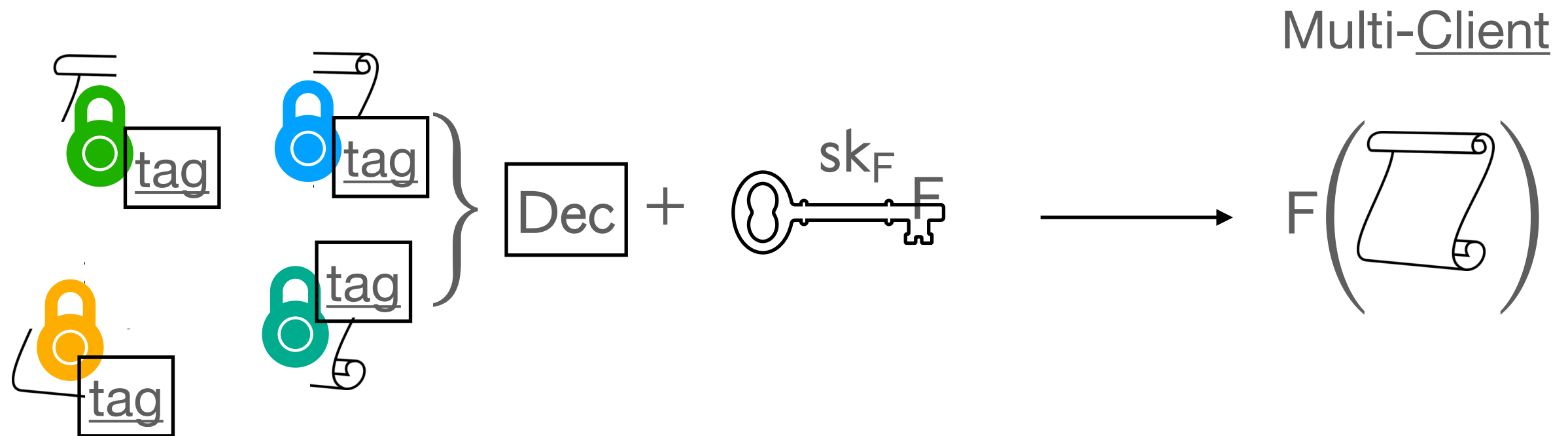
MCFE [GGG+14,CDGPP18] - **Secret** Encryption Keys



🤔 Syntactical:
NOT allow public-**Att**

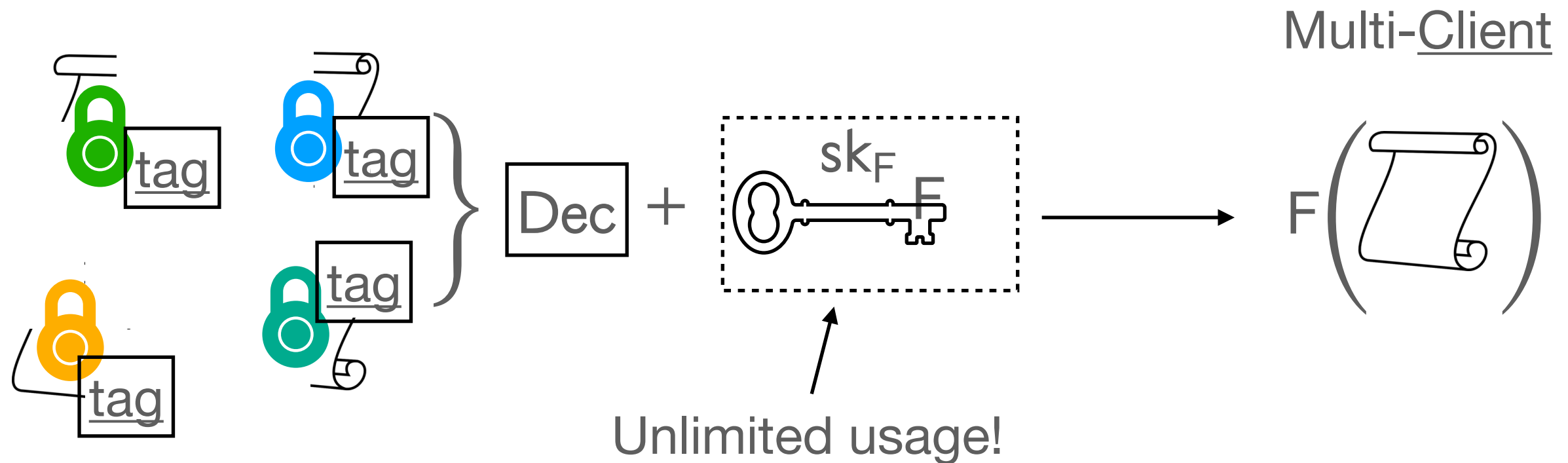
Motivation - Usage of Keys

MCFE [GGG+14, GKL+13, CDGPP18]



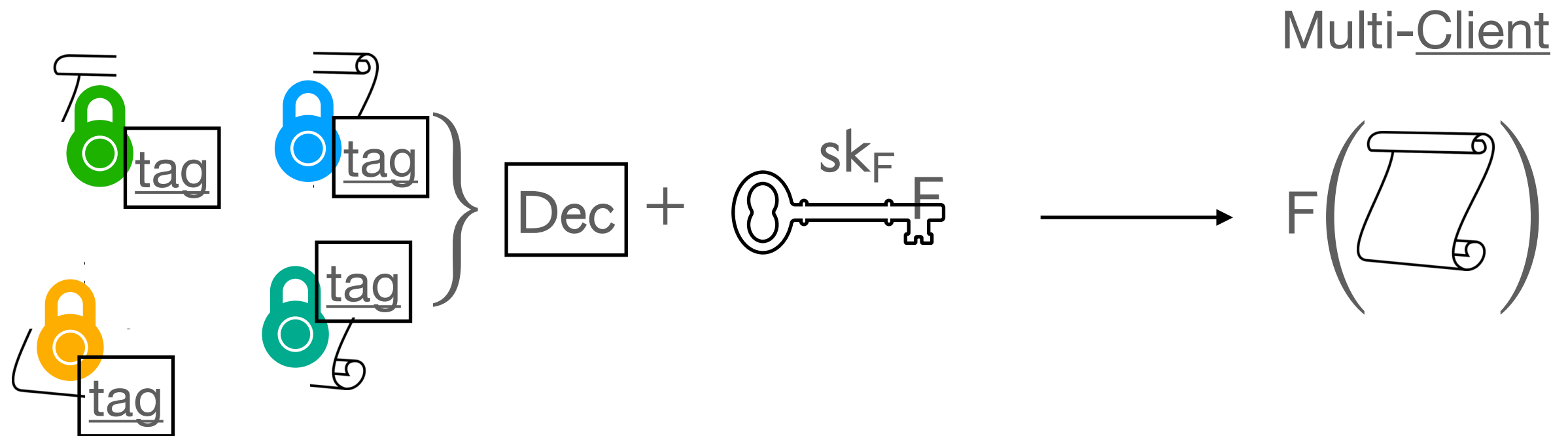
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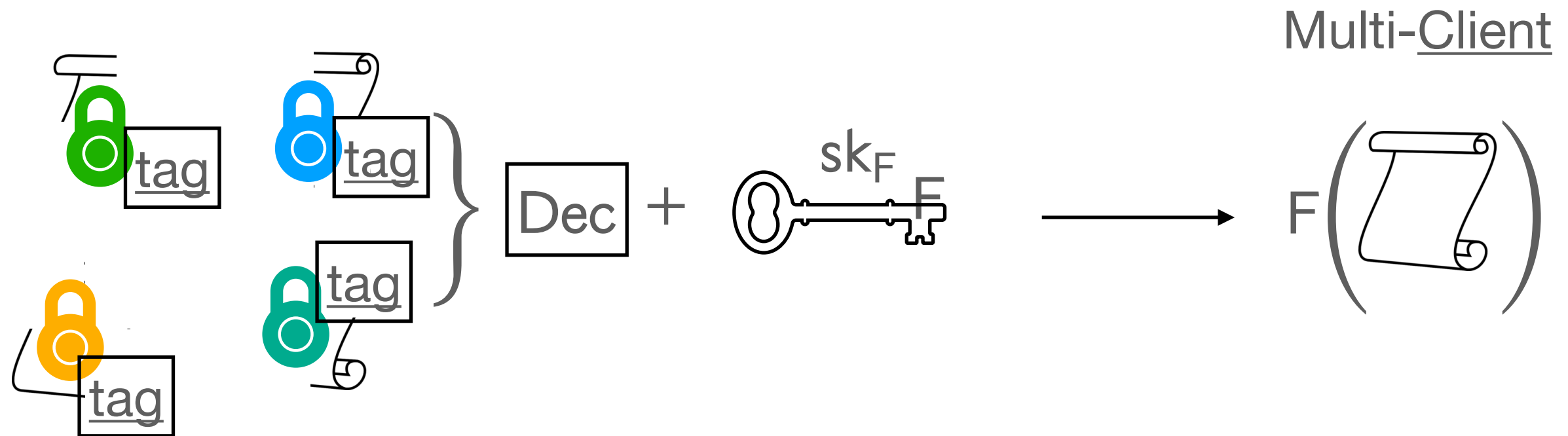
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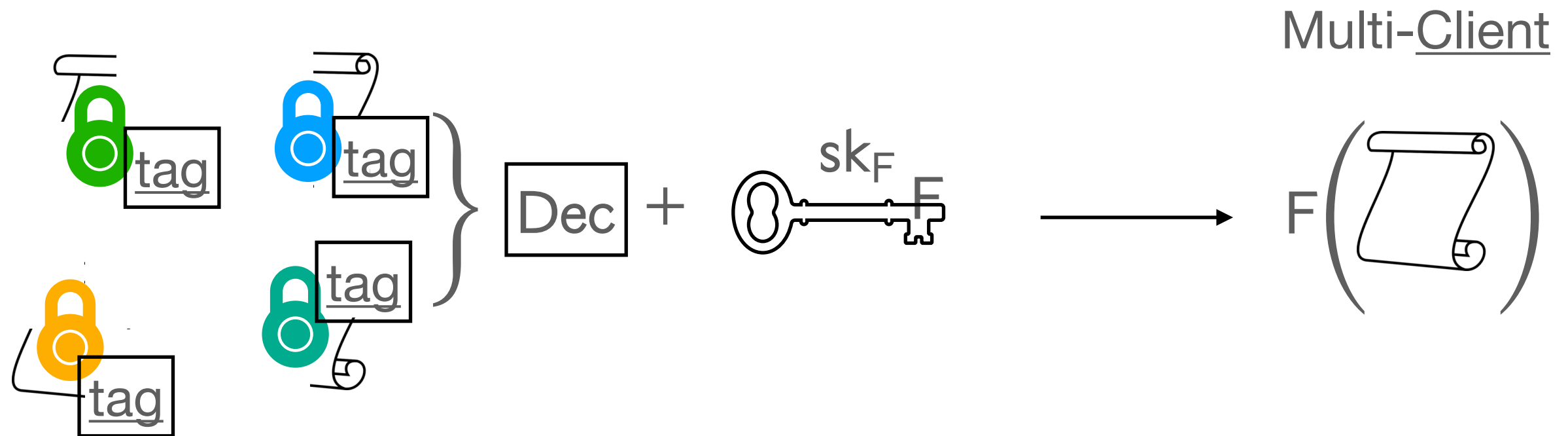
MCFE [GGG+14, GKL+13, CDGPP18]



[ACGU20]: control keys
In Multi-Input FE [GGG+14] { **Secret** Encryption Keys
Only **one** encryptor 


Motivation - Usage of Keys

MCFE [GGG+14, GKL+13, CDGPP18]



 **Efficiency**

Related Works

Multi-Client with Fine-Grained Access Control [NPP22]

Related Works

Multi-Client with Fine-Grained Access Control [NPP22]



First definitions for MCFE with key control

Related Works

Multi-Client with Fine-Grained Access Control [NPP22]



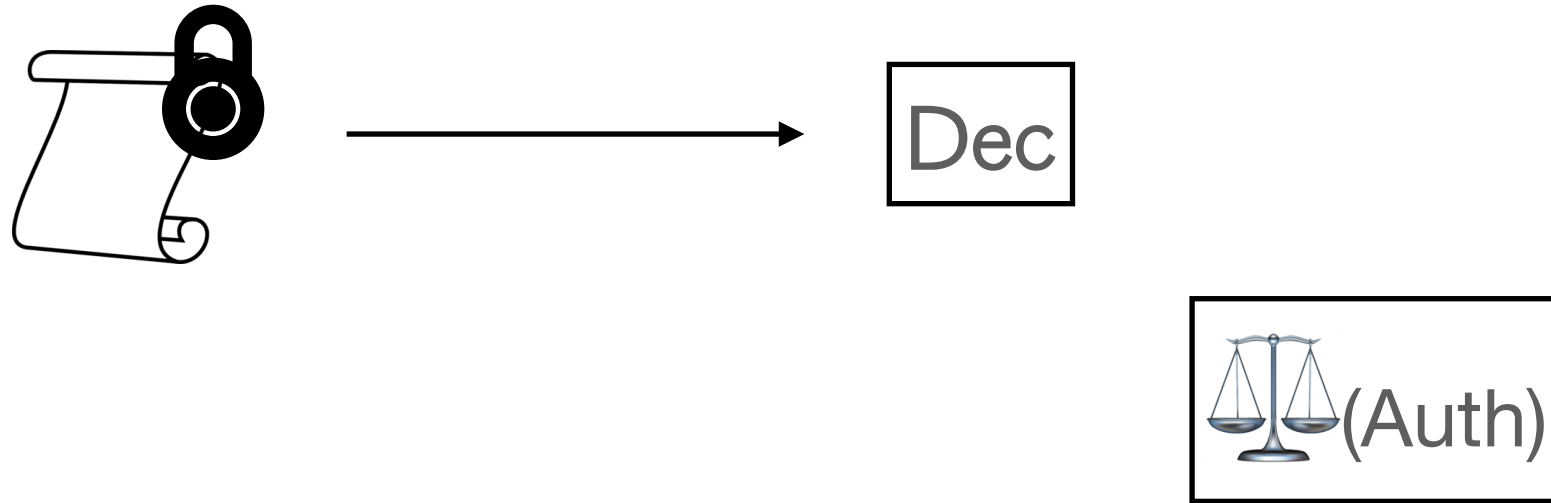
First definitions for MCFE with key control



Concrete MCFE for scalar Inner Products
with Linear Secret Sharing for key controlling

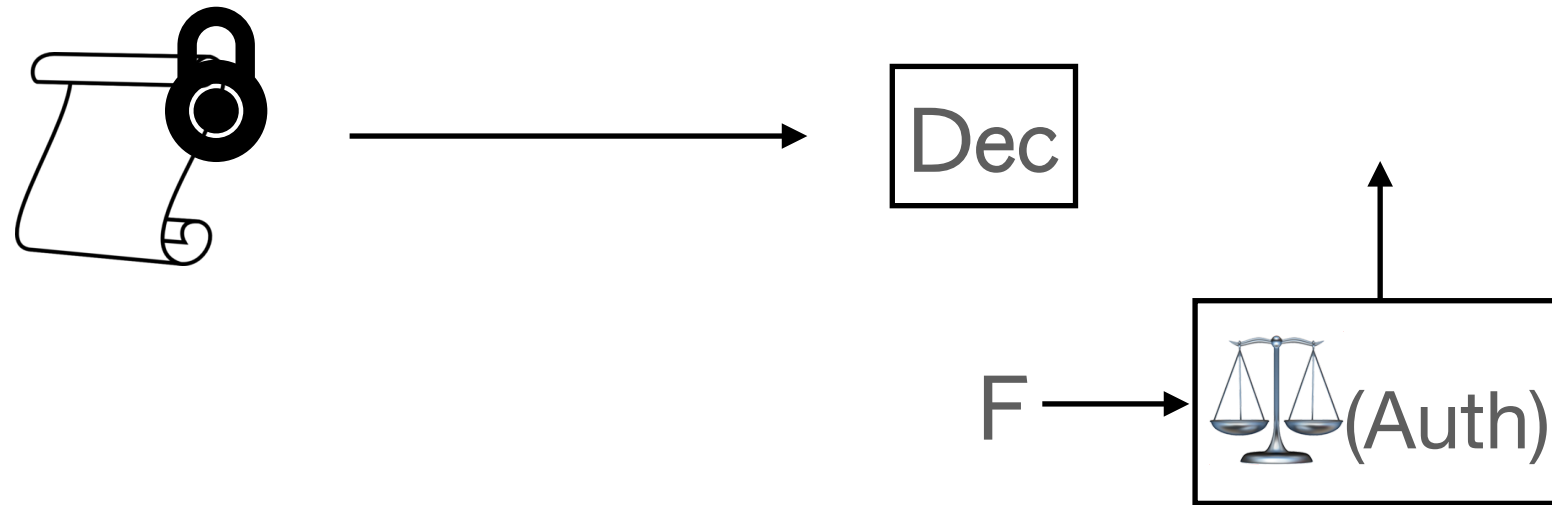
Motivation - Security Model

How do we define a “secure” FE ?



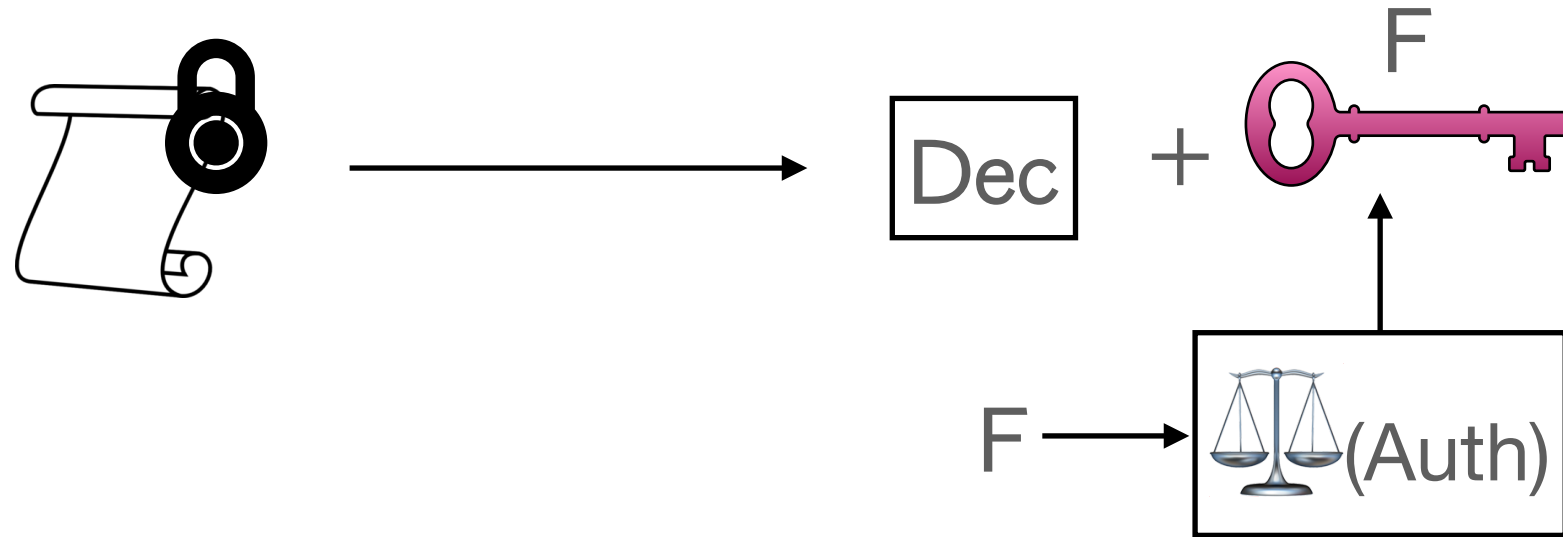
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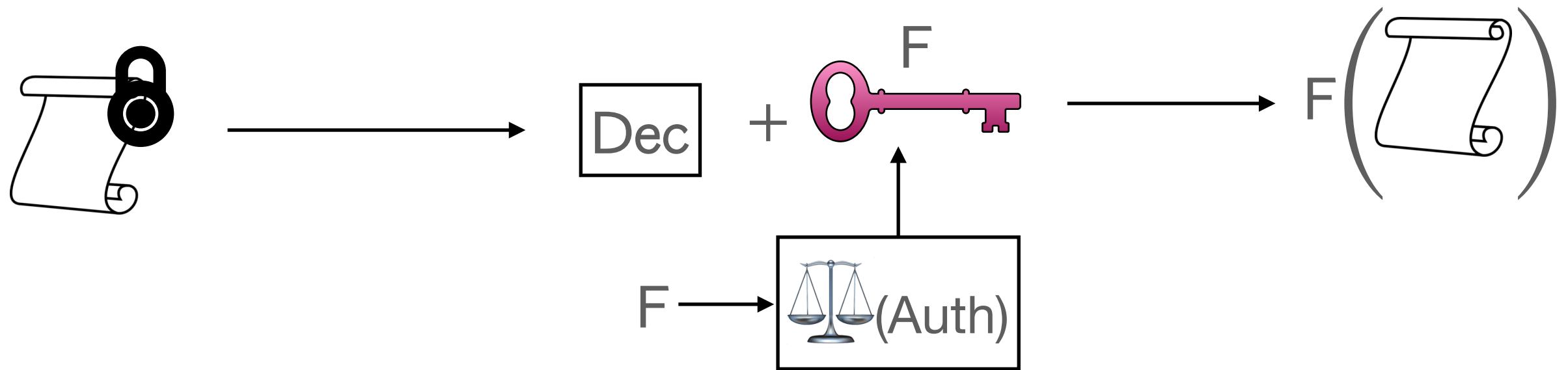
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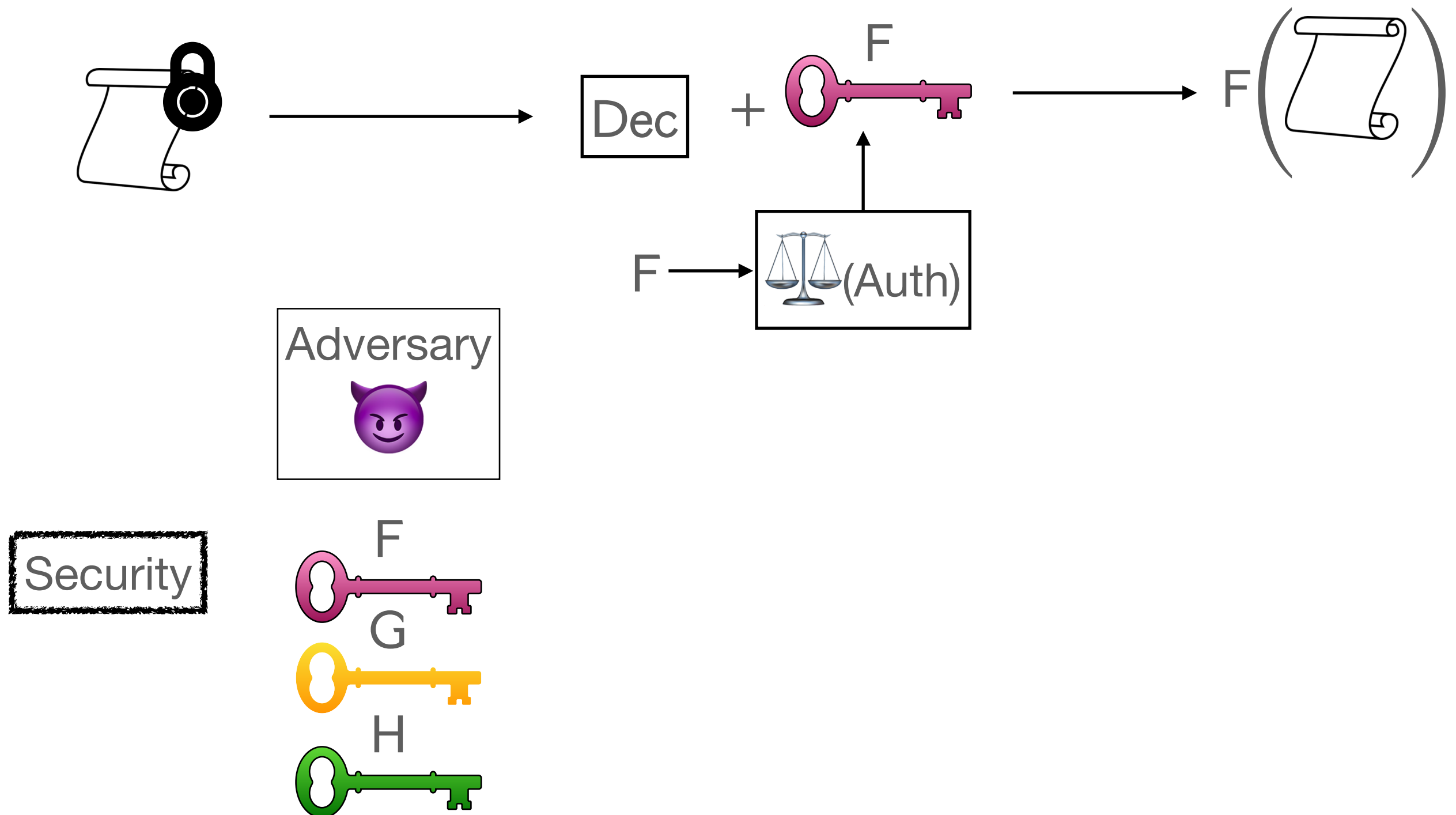
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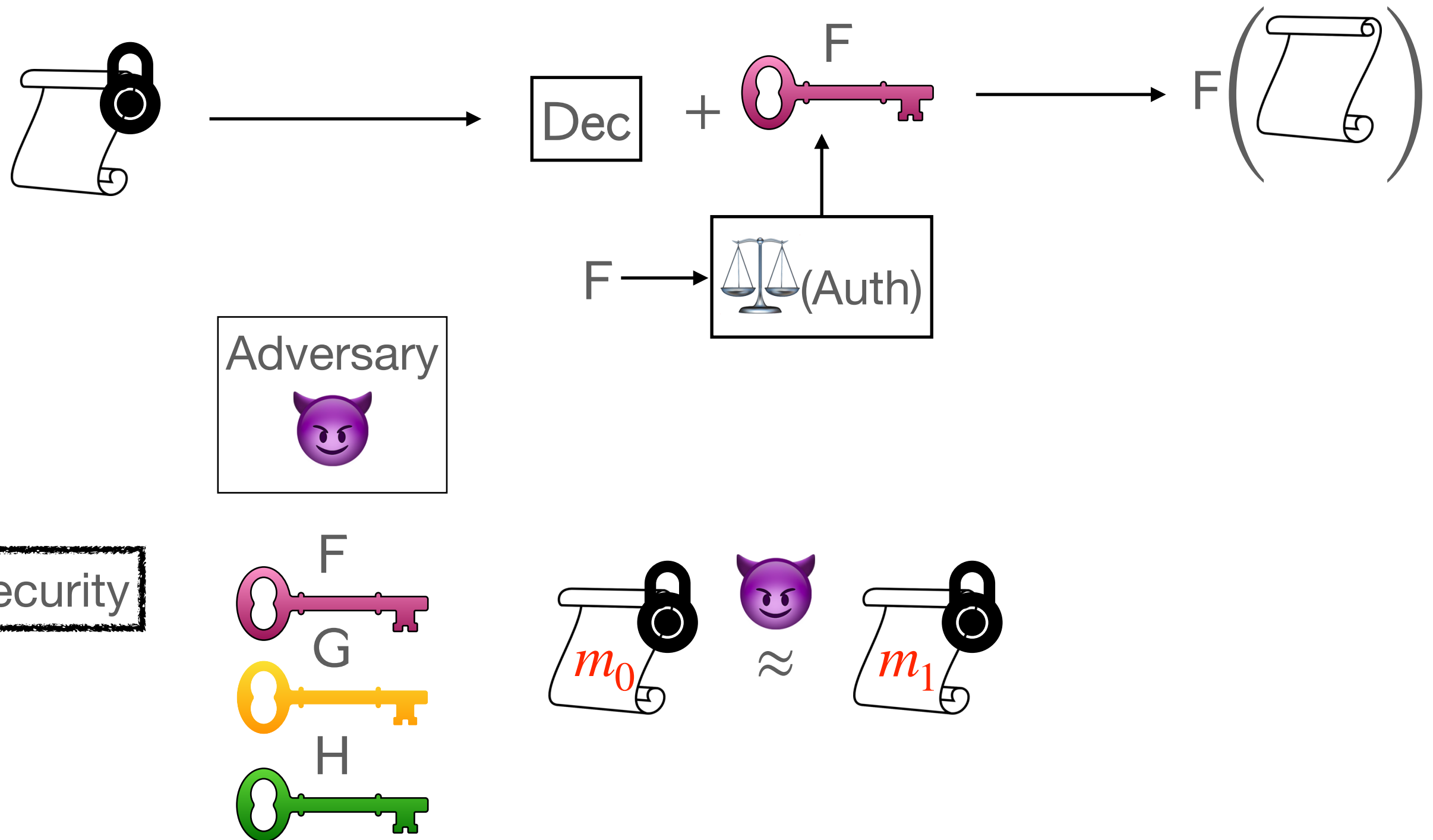
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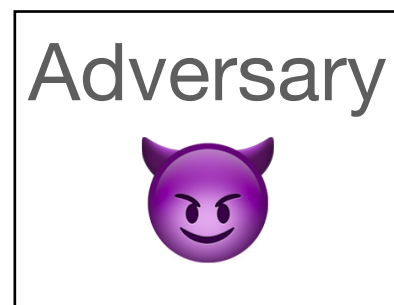
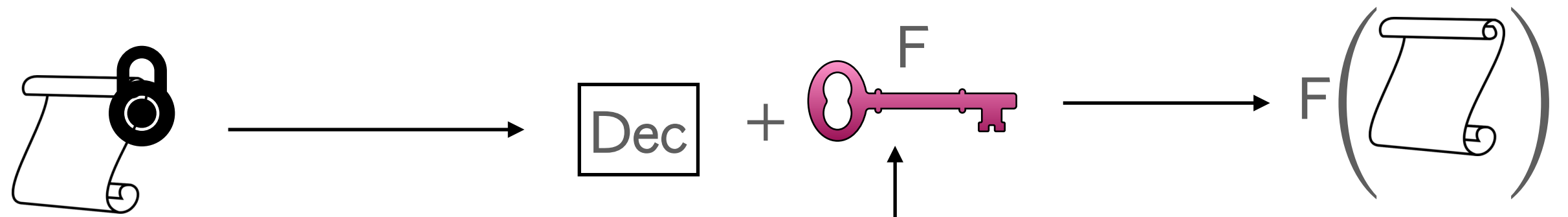
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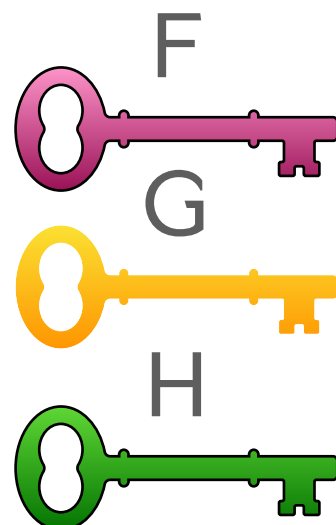


Motivation - Security Model

How do we define a “secure” FE ?



Security



$$\begin{aligned} F(m_0) &= F(m_1) \\ G(m_0) &= G(m_1) \\ H(m_0) &= H(m_1) \end{aligned}$$

Motivation - Security Model

How do we define a “secure” MCFE ?

Challenger: $b \xleftarrow{\$} \{0,1\}$



Chall

Enc

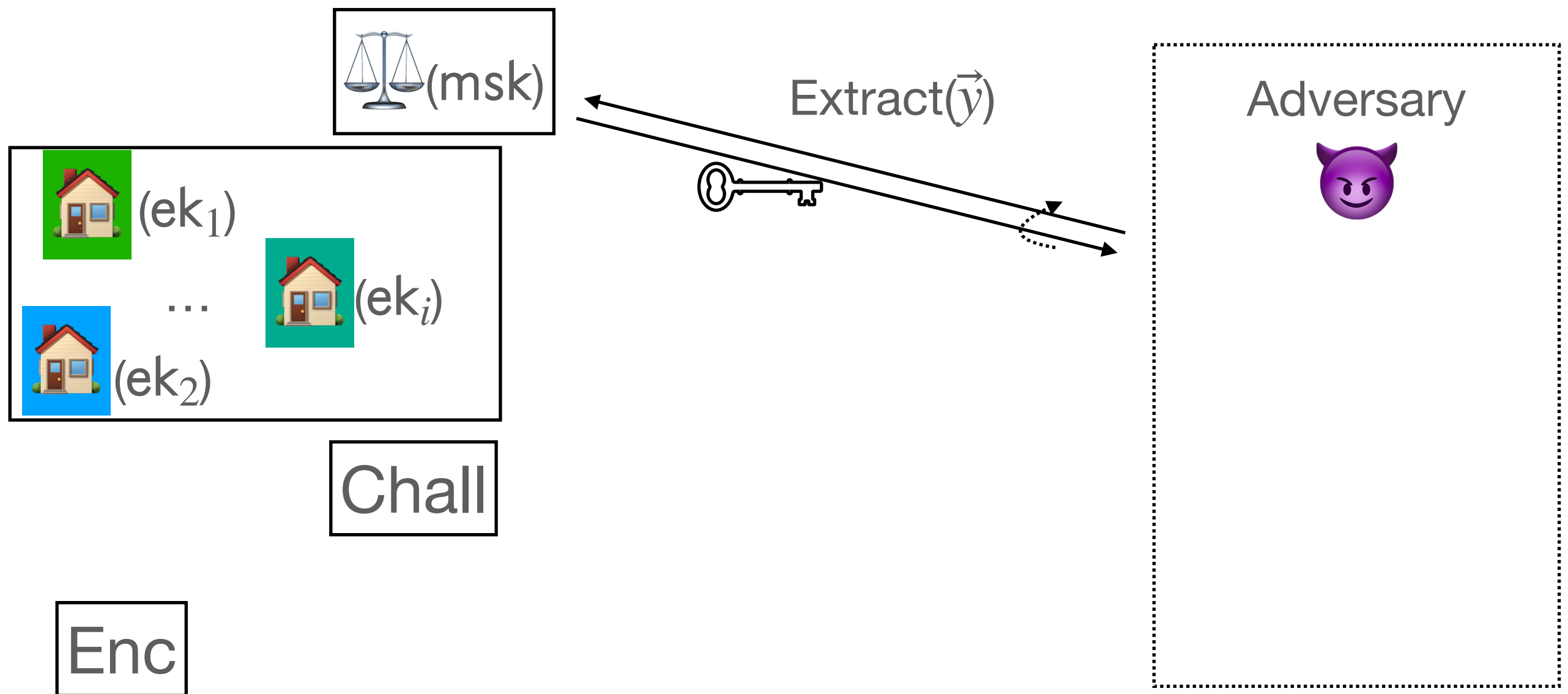
Adversary



Motivation - Security Model

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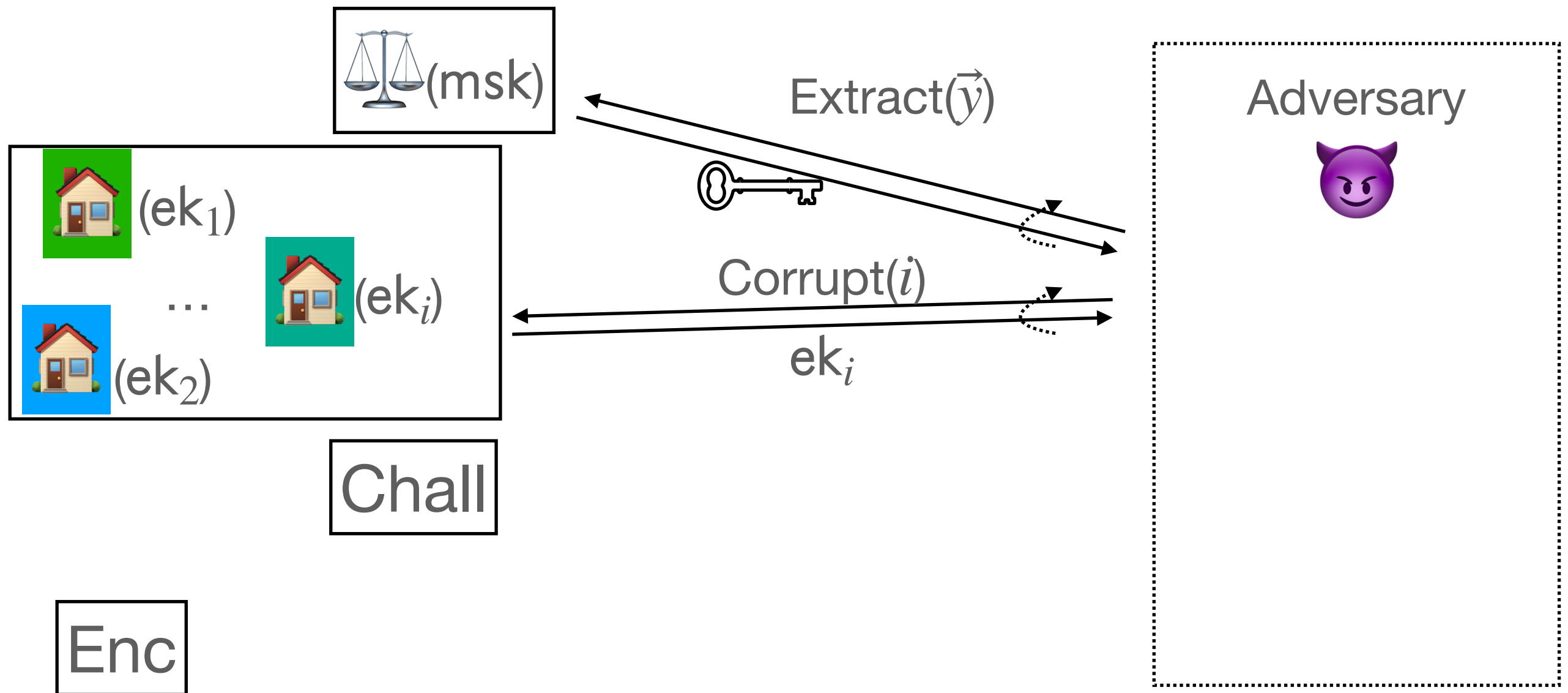
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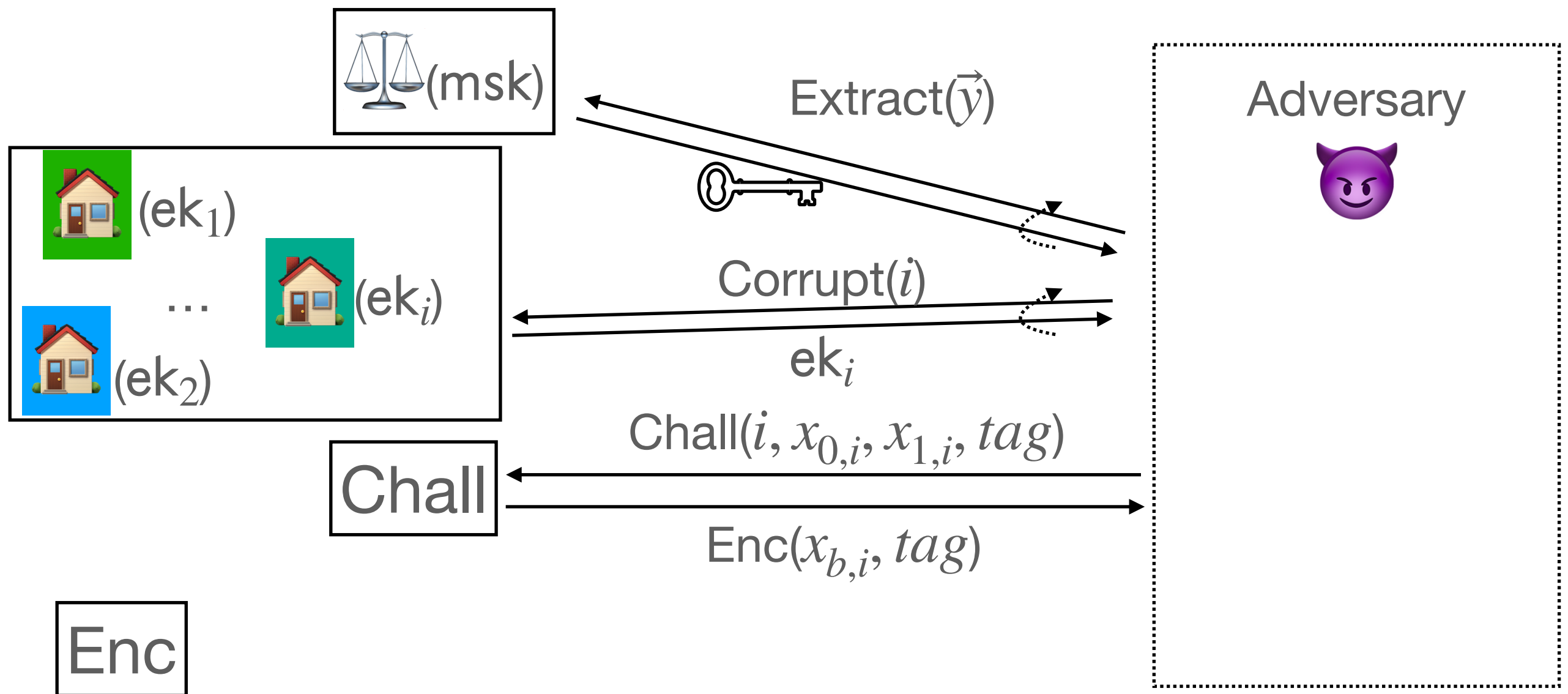
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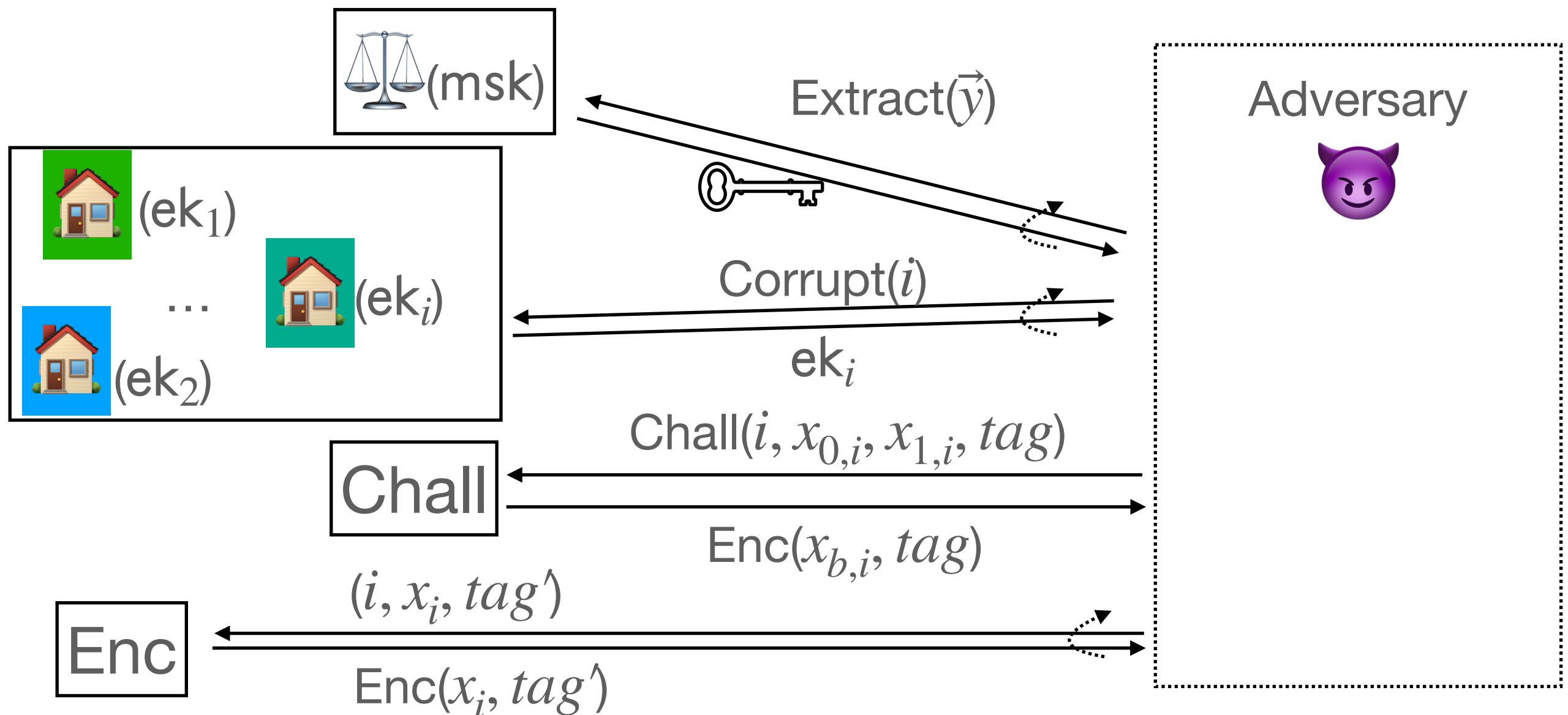


Secret Keys: $Enc + 1$ chall security $\Rightarrow$ multi-chall security

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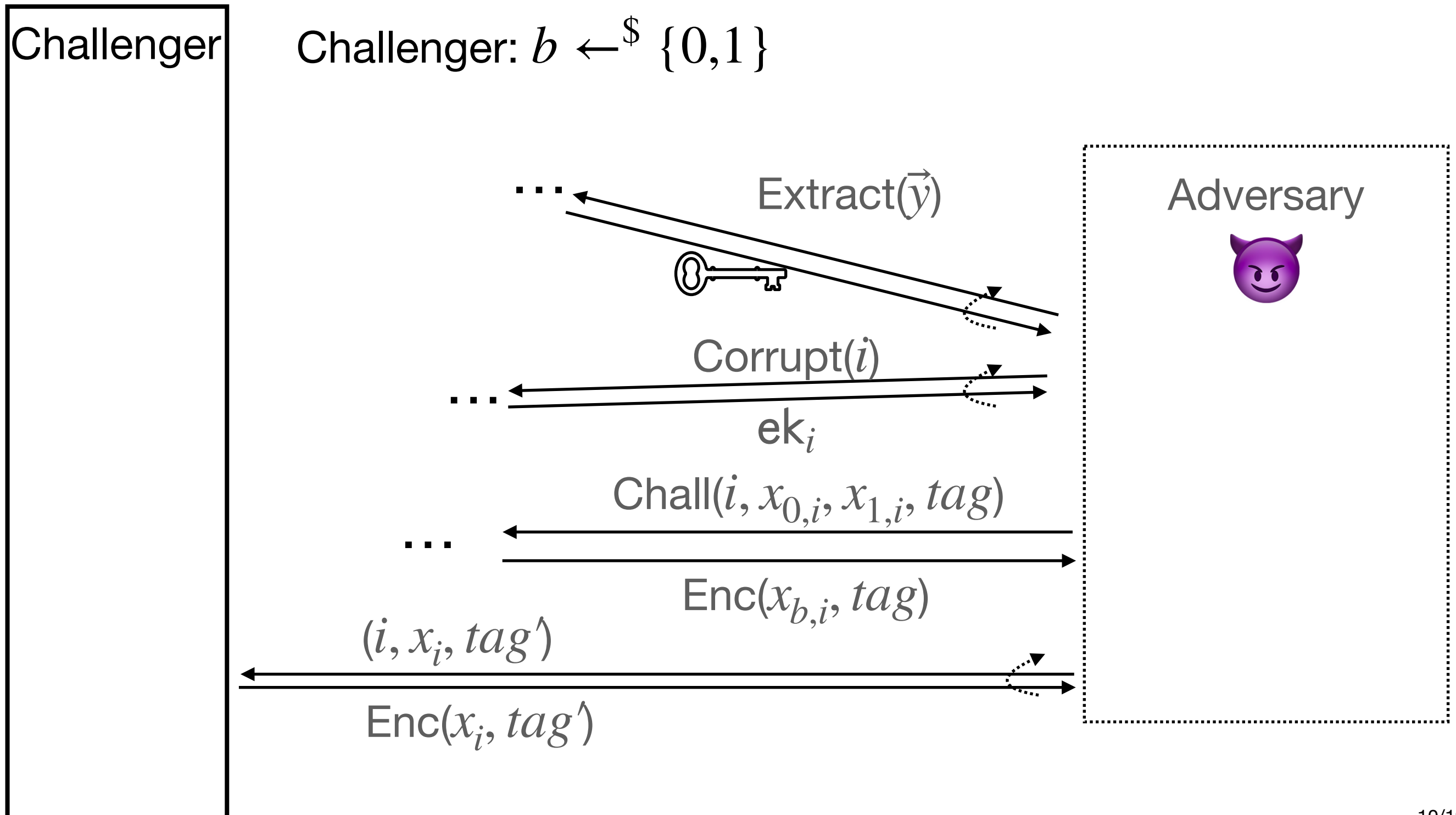
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Motivation - Security Model

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Motivation - Security Model

How do we define a “secure” MCFE ?

Win if $b' = b$

$b' \in \{0,1\}$

Adversary



Extract($\vec{y}$)



Corrupt(i)

ek_i

Chall($i, x_{0,i}, x_{1,i}, tag$)

Enc($x_{b,i}, tag$)

(i, x_i, tag')

Enc(x_i, tag')

Challenger

Challenger: $b \leftarrow^{\$} \{0,1\}$

Motivation - Security Model

How do we define a “secure” MCFE ?

Win if $b' = b$

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Adversary



$$\langle \vec{x}_0 - \vec{x}_1, \vec{y} \rangle = 0$$



Extract($\vec{y}$)



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[CDGPP'18]

Corrupt(i)

$\Rightarrow x_{0,i} = x_{1,i}$

🤔 Justified?

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Motivation - Security Model

A “secure” MCFE - the case of Inner Products

Adversary



[CDGPP'18]

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Motivation - Security Model

A “secure” MCFE - the case of Inner Products

[CDGPP'18]

Corrupt(i)

$$\Rightarrow x_{0,i} = x_{1,i}$$

—> Follow-ups with **same** constraint:

[ABKW19],[ABG19],[LT19],

[CDG+20],[AGT21],[SV23]

Adversary



[CDGPP'18]

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Justified?

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A “secure” MCFE - the case of Inner Products

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[CDGPP'18]

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🤔 Justified?

From [CDGPP18]:

MCFE is **Secret** Encryption Keys

⇒ Usually deterministic

⇒

Corrupt(i)

$$\Rightarrow x_{0,i} = x_{1,i}$$

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A “secure” MCFE - the case of Inner Products

[CDGPP'18]

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[CDGPP'18]

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🤔 Justified?



🤔 Modeling Problem:

Why can't we do better?

(/i.e., weaker condition

$\Rightarrow$ considering stronger attacker

$\Rightarrow$ stronger security guarantee)

Related Works

Improved Security Notion for (D)MCFE

Optimal Security Notion for Decentralized Multi-Client Functional Encryption [NPP'23]

Adversary



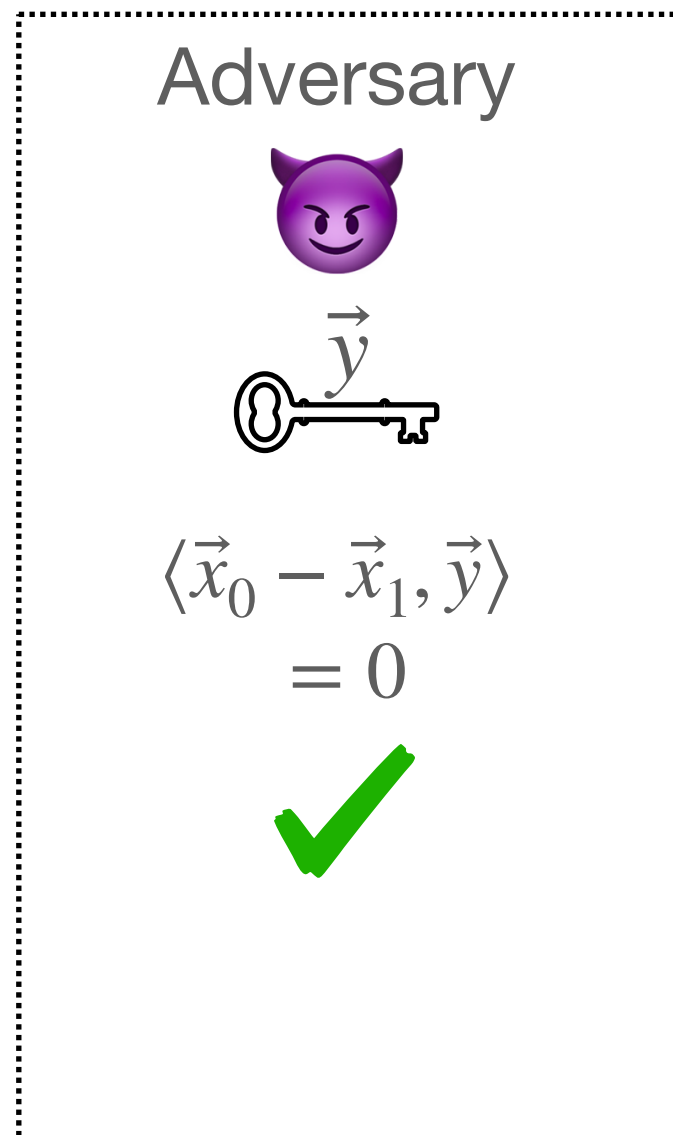
Computing scalar
inner products:

$$F(\cdot) = \langle \cdot, param \rangle$$

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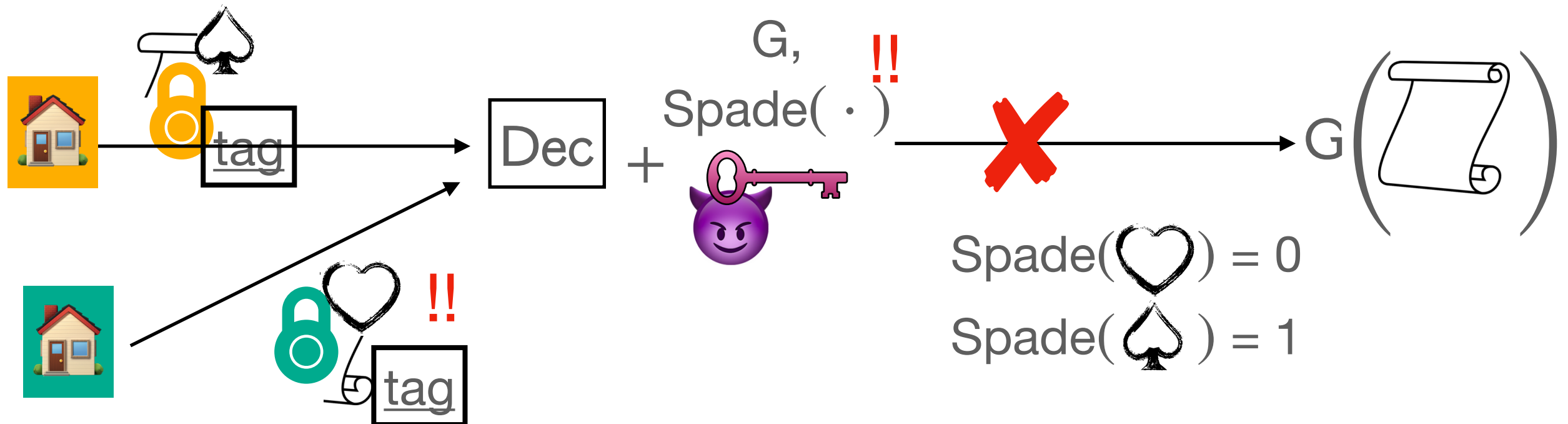
+ Optimality
proof : this is
the least we
require 🎉

Computing scalar
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Research Question - Combining All Together

Controlling Keys (*as per* [NPP22]) in the Optimal Setting (*as per* [NPP23])

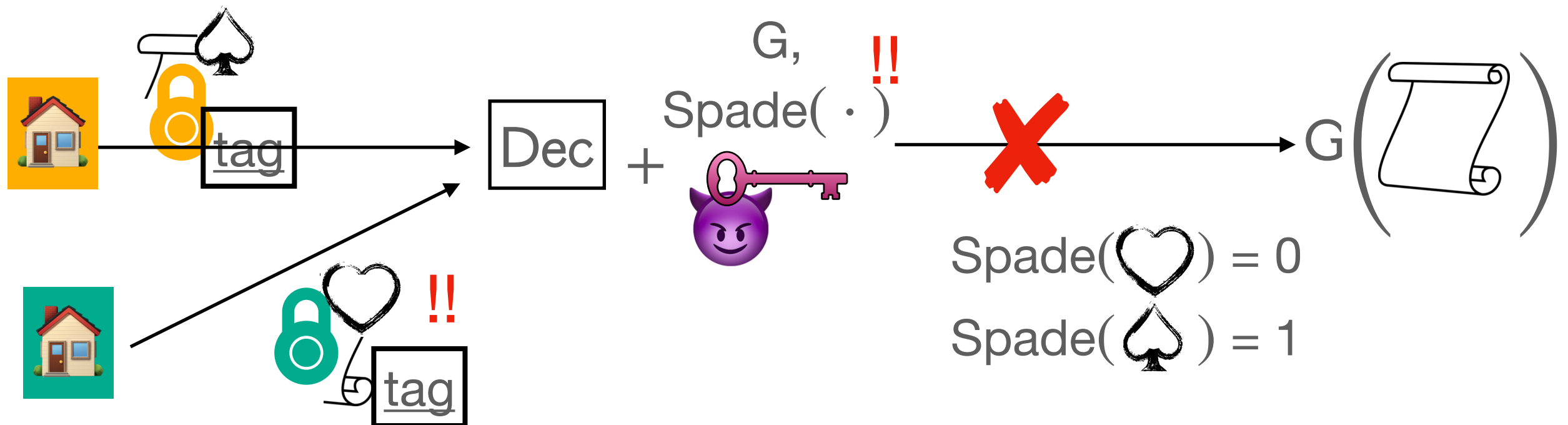


🤔 public-key FE [BSW11],
secret-key MCFE [GGG+14,
CDG+18]

Syntactical Problem:
NOT allow public-Att

Research Question - Combining All Together

Controlling Keys (*as per* [NPP22]) in the Optimal Setting (*as per* [NPP23])



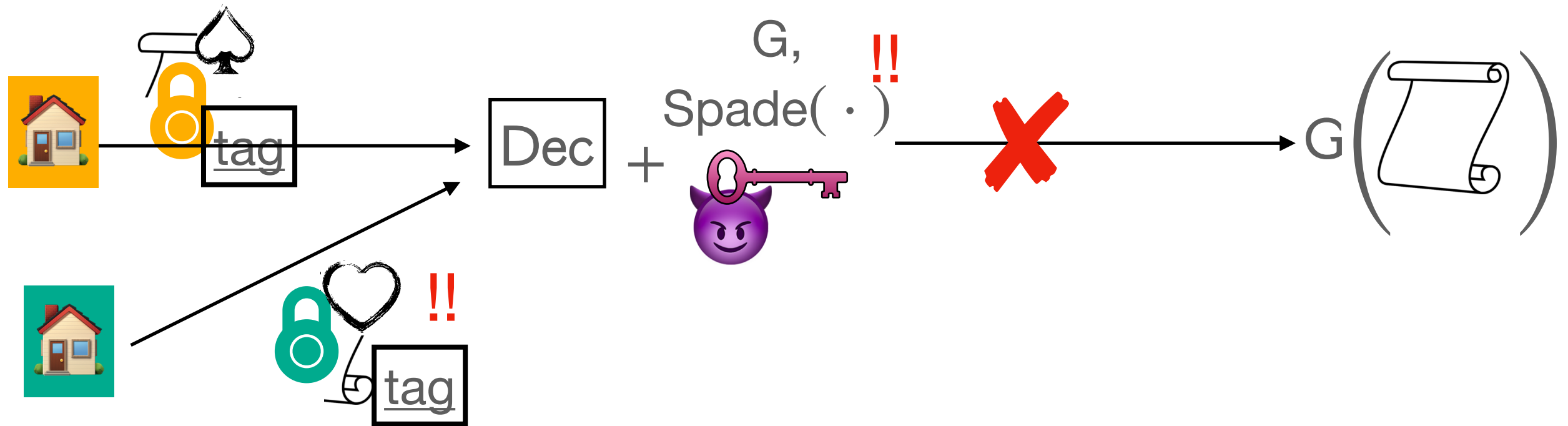
Tag, ♠, ♥ :
can be public

🤔 public-key FE [BSW11],
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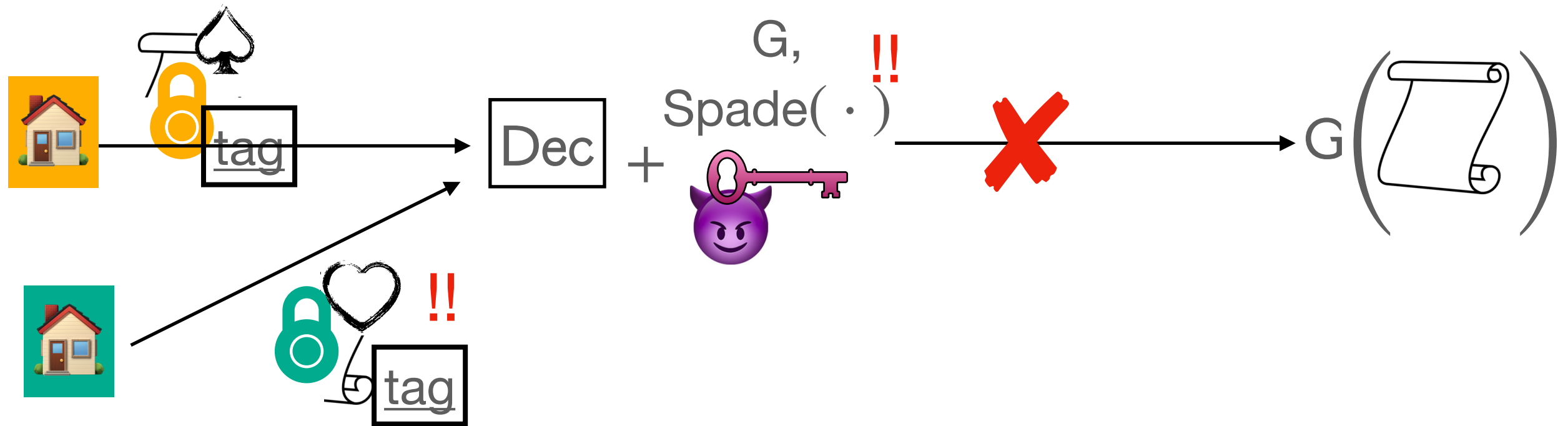
Our Result

Controlling Keys in the Optimal Setting



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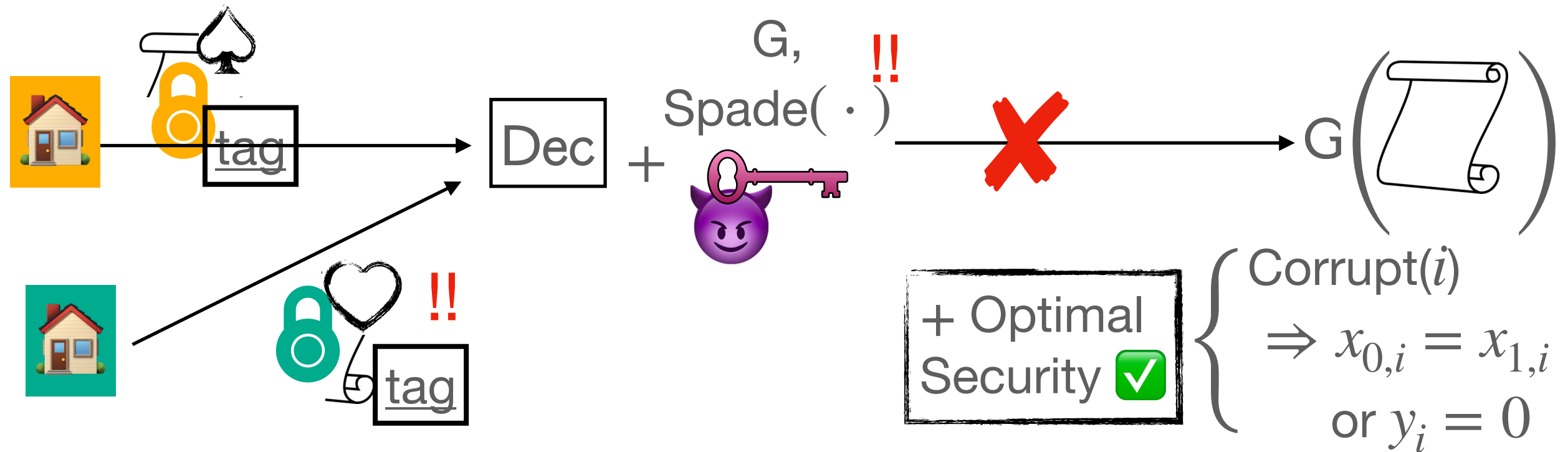
Controlling Keys in the Optimal Setting



✓ Refine Syntax of MCFE:
With **public**-inputs

Our Result

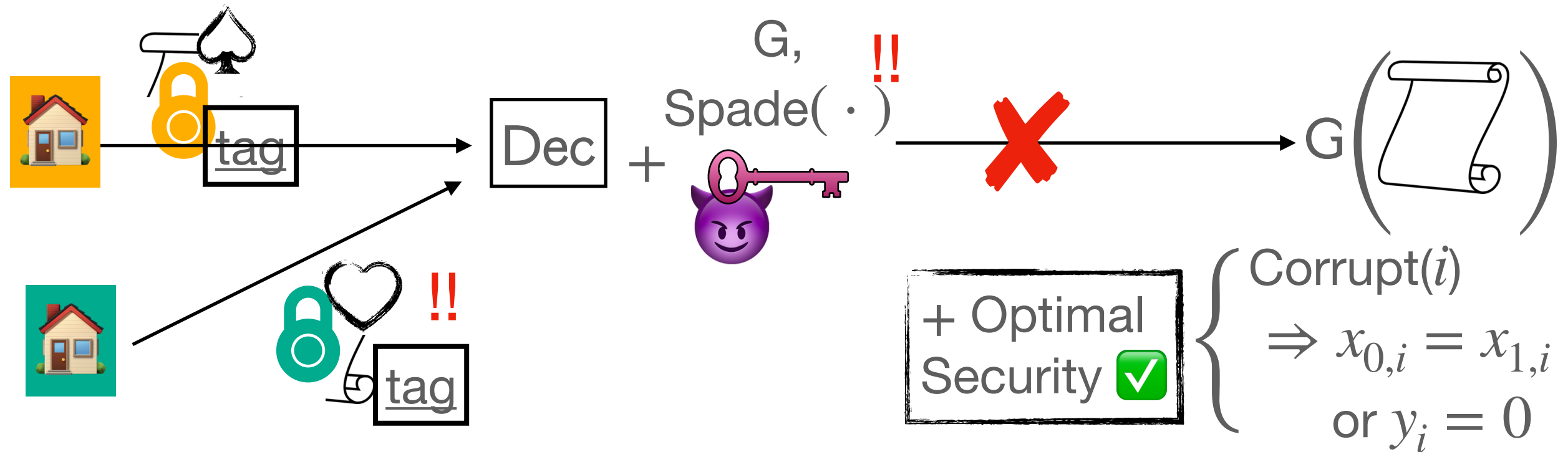
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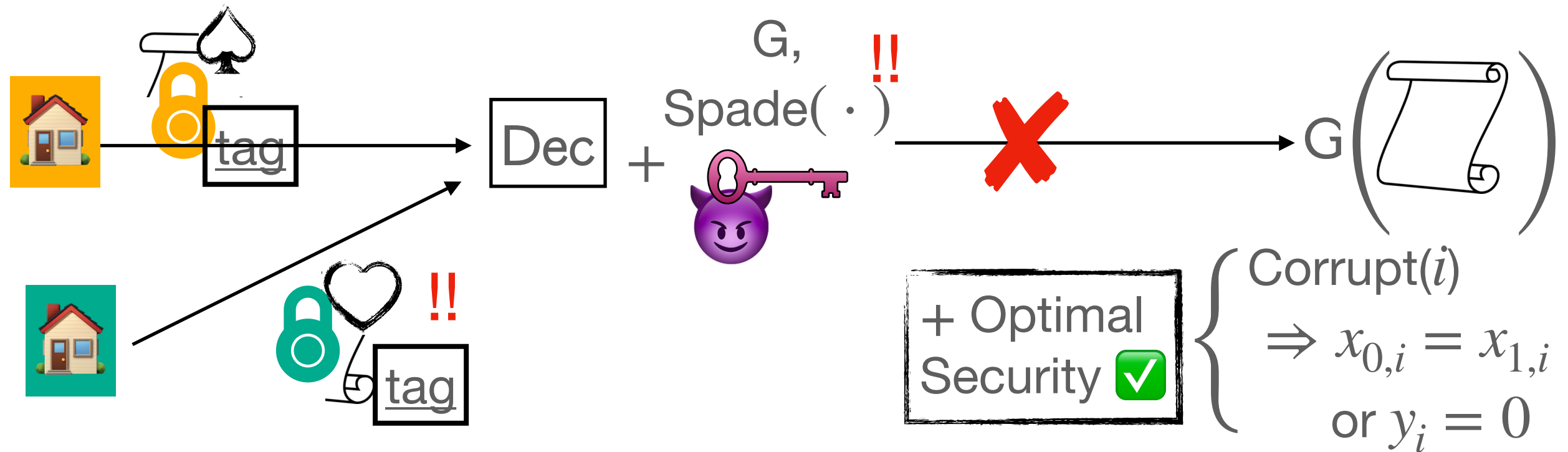


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✓ Identify Implications:
MCFE + optimal security
⇒ **public**-key FE

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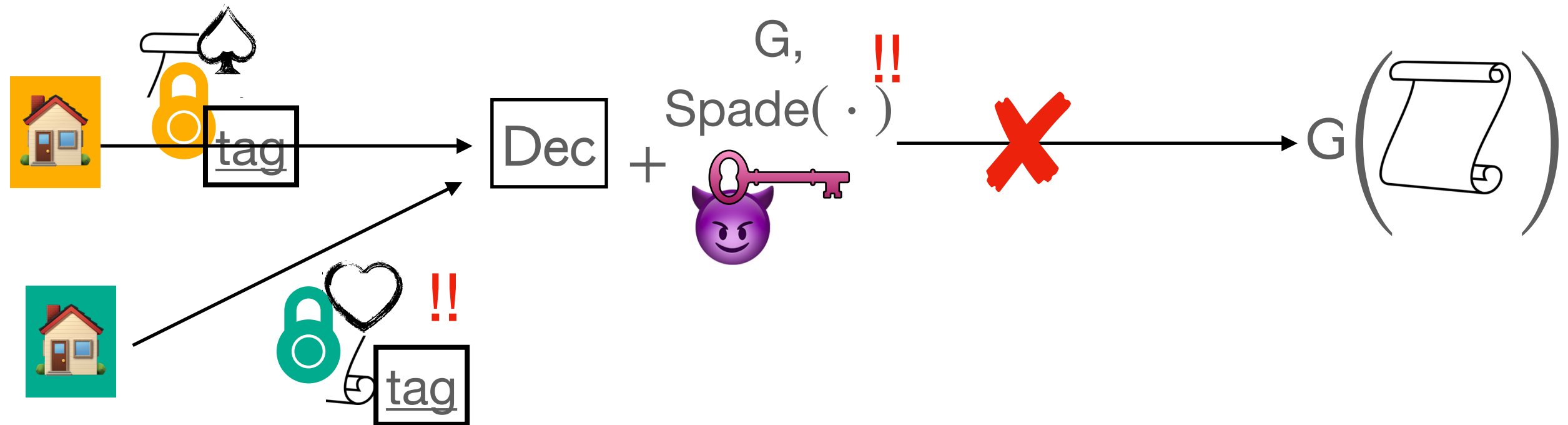


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MCFE + optimal security
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Key-Policy
Attribute-based
Encryption,
Public- or **private**-att 🎉

Our Result

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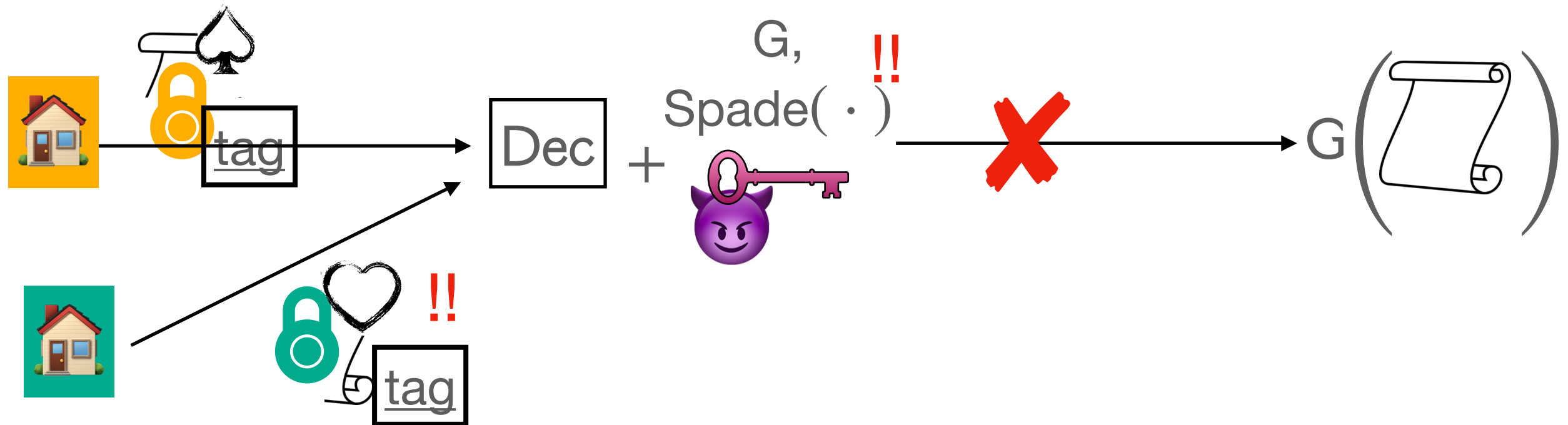


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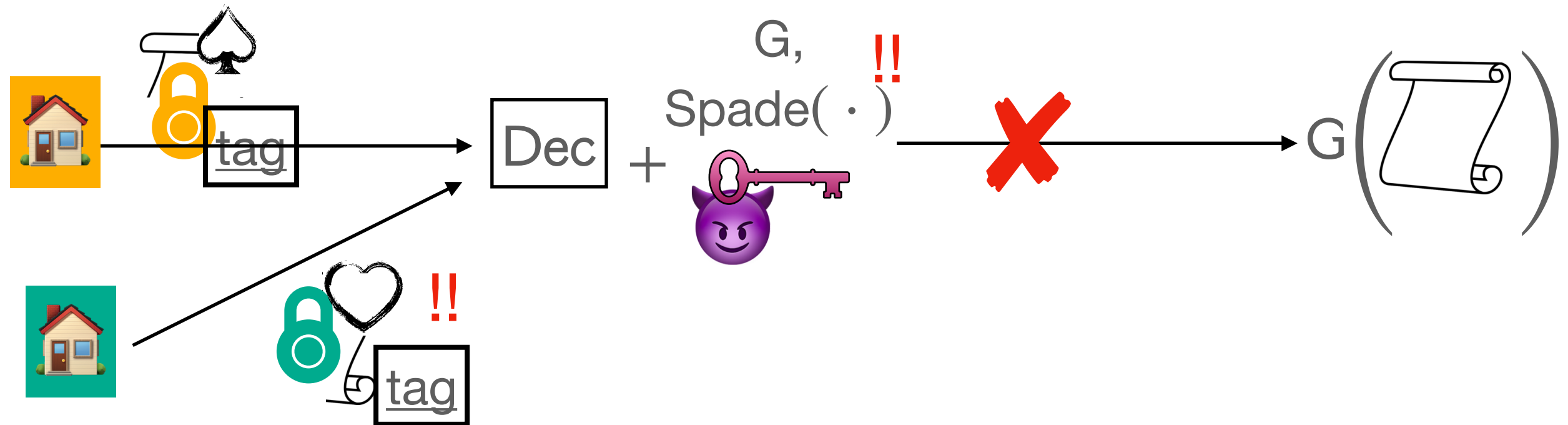
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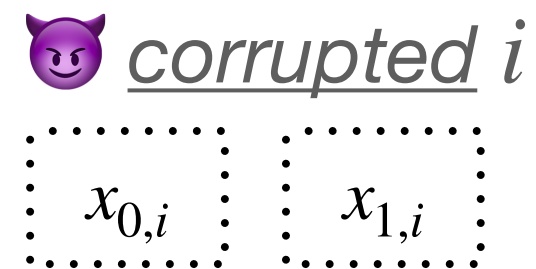
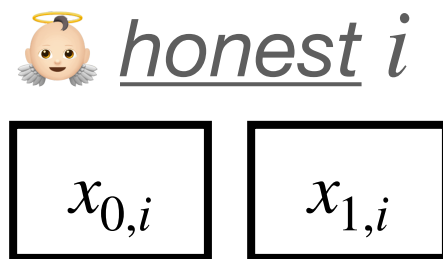
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- ✓ Concret MCFE for
Inner Products
from Pairings in ROM,
Stronger Security
improving
[NPP22,NPP23,ATY23]

Recall: The Admissibility from [NPP23]

Concrete conditions for IP, MCFE, **one subvector/client**

For all $(x_{0,i}, x_{1,i})_i$,
for all $\vec{y}$



$$\vec{y} = \left(\begin{bmatrix} \text{---} \\ y_i \\ \text{---} \end{bmatrix} \right)_i$$

$$(1) \quad \sum_{\text{angel emoji } \text{honest } i} \left\langle \boxed{x_{0,i}}, \begin{bmatrix} \text{---} \\ y_i \\ \text{---} \end{bmatrix} \right\rangle = \sum_{\text{angel emoji } \text{honest } i} \left\langle \boxed{x_{1,i}}, \begin{bmatrix} \text{---} \\ y_i \\ \text{---} \end{bmatrix} \right\rangle$$

MCFE

$$(2) \quad \boxed{\text{key icon}}^{\text{devil emoji}}_{(ek)} \left\langle \text{dotted box } x_{0,i}, \begin{bmatrix} \text{---} \\ y_i \\ \text{---} \end{bmatrix} \right\rangle = \left\langle \text{dotted box } x_{1,i}, \begin{bmatrix} \text{---} \\ y_i \\ \text{---} \end{bmatrix} \right\rangle$$

On Security: Admissibility All Over Again

Implications of Pub-Inputs & Strong Admissibility



Our
Work!

MCFE: Pub-Inputs,
Allowing repetitions $\vec{x}_i$

On Security: Admissibility All Over Again

Implications of Pub-Inputs & Strong Admissibility

🥳 Our
Work!

MCFE: Pub-Inputs,
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#clients
 $n = 1$

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Our
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#clients
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Strong Admissibility:

$$\boxed{\text{key}}^{\text{devil}}_{\text{key}}(ek) \left\langle \boxed{\vec{x}_0}, \boxed{\vec{y}} \right\rangle = \left\langle \boxed{\vec{x}_1}, \boxed{\vec{y}} \right\rangle$$

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+ Static Corruption $\boxed{\text{key}}^{\text{evil}}(\text{ek})$

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#clients
 $n = 1$

Strong Admissibility:

Admissibility in
Public-key FE !!

$$\boxed{\text{key}}^{\text{devil}}(\text{ek}) \left\langle \boxed{\vec{x}_0}, \boxed{\vec{y}} \right\rangle = \left\langle \boxed{\vec{x}_1}, \boxed{\vec{y}} \right\rangle$$

+ Static Corruption $\boxed{\text{key}}^{\text{devil}}(\text{ek})$

Becomes pk !!

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Public-key FE
With Pub-Inputs

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Public-key FE
With Pub-Inputs

Access control in
Public inputs

Covering syntactically
Non-pol/att-hiding
ABE !!

On Security: Admissibility All Over Again

Implications of Pub-Inputs & Strong Admissibility

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Work!

MCFE: Pub-Inputs,
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Public-key FE
With Pub-Inputs



Public-key ABE
With or w/out
Hiding properties

On Security: Admissibility All Over Again

Implications of Pub-Inputs & Strong Admissibility

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MCFE: Pub-Inputs,
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Public-key FE
With Pub-Inputs



Fix one tag for all
Enc

Public-key ABE
With or w/out
Hiding properties

Repetitions on $\vec{x}_i$
Covers basic MIFE

On Security: Admissibility All Over Again

Implications of Pub-Inputs & Strong Admissibility

Our
Work!

MCFE: Pub-Inputs,
Allowing repetitions $\vec{x}_i$



Public-key FE
With Pub-Inputs



MIFE: “vanilla”
Same functions on $\vec{x}_i$



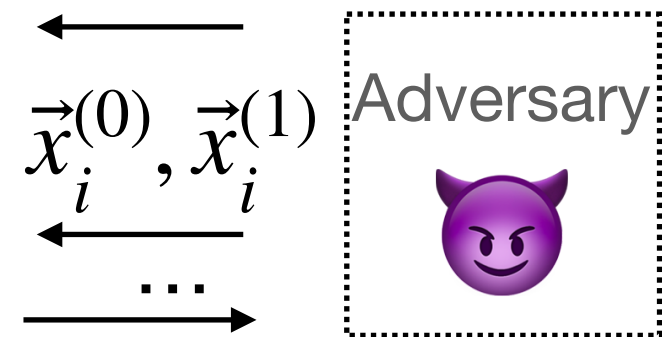
Public-key ABE
With or w/out
Hiding properties

New Techniques: Dual Paring Vector Spaces with Complexity Leveraging

In a nutshell: With Formal Changes, **Guesses are Free**

Selective

simulator : guess $(\vec{x}_i^{(0)}, \vec{x}_i^{(1)})$ from 

$$\text{View}_0^{sel} \equiv \text{View}_1^{sel} \equiv \dots \equiv \underline{\text{View}_k^{sel}}$$


Start



Guessing

Challenges $\vec{x}_i^{(0)}, \vec{x}_i^{(1)}$

New Techniques: Dual Paring Vector Spaces with Complexity Leveraging

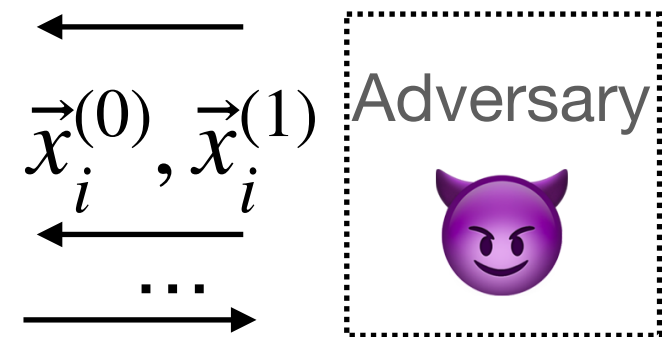
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In View_k^{sel} : Some critical step in the proof



Start

$\Rightarrow$

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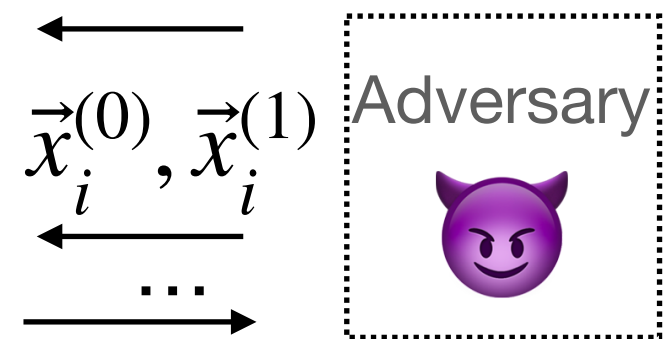
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New Techniques: Dual Pairing Vector Spaces with Complexity Leveraging

In a nutshell: With Formal Changes, **Guesses are Free**

All is formal basis changes
in *Dual Pairing Vector Spaces*

Selective

simulator : guess $(\vec{x}_i^{(0)}, \vec{x}_i^{(1)})$ from 

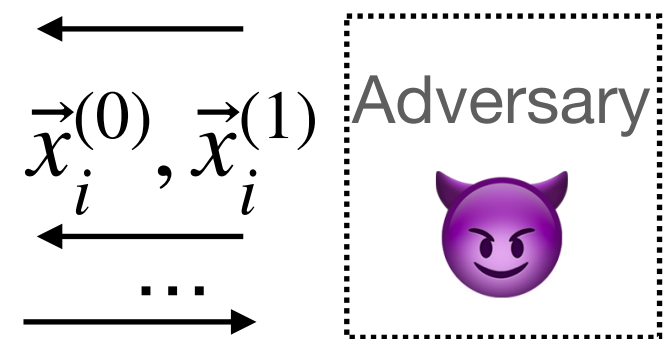
$$\text{View}_0^{sel} \equiv \text{View}_1^{sel} \equiv \dots \equiv \underline{\text{View}_k^{sel}}$$

Perfectly

Perfectly

Perfectly

In View_k^{sel} : Some critical step in the proof



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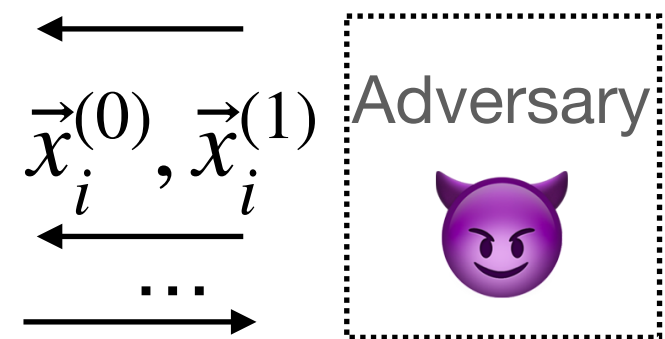
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Perfectly Perfectly Perfectly

In View_k^{sel} : Some critical step in the proof



Start

$\Rightarrow$

Loss factor over choices
of $\vec{x}_i^{(0)}, \vec{x}_i^{(1)}$ in prob of correct

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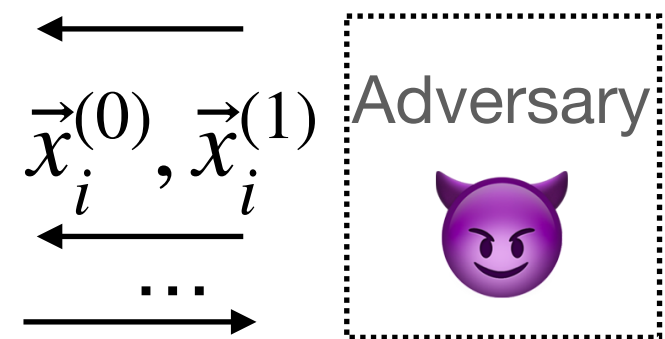
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$$0 \leq \text{diff}(\text{View}_0^{\text{sel}}; \text{View}_k^{\text{sel}}) \\ \leq \sum_i \text{diff}(\text{View}_i^{\text{sel}}; \text{View}_{i+1}^{\text{sel}}) = 0$$

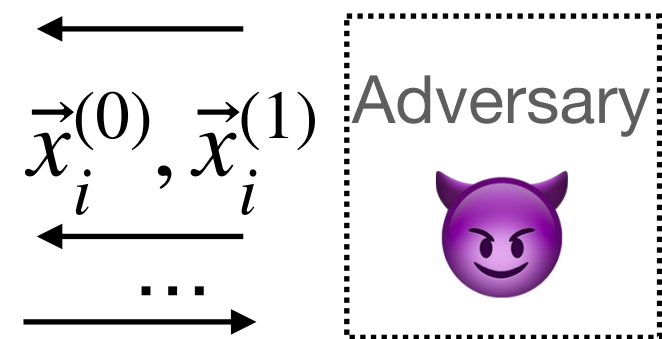
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Perfectly Perfectly Perfectly

In $\text{View}_k^{\text{sel}}$: Some critical step in the proof



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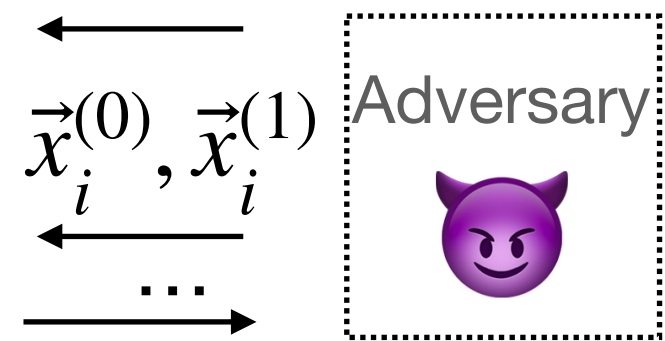
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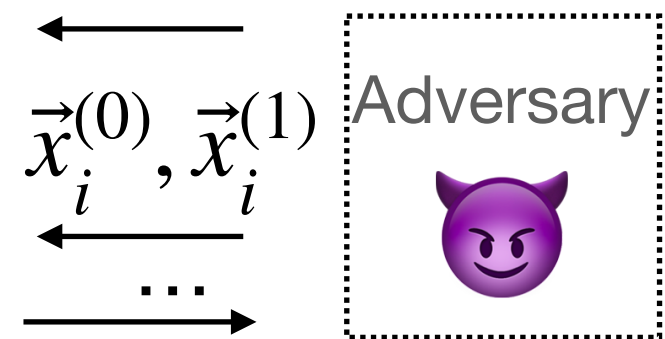
Adaptive

Simulator: no guesses

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Perfectly Perfectly Perfectly

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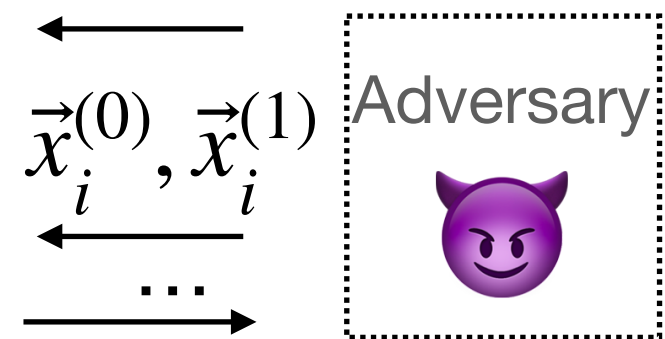
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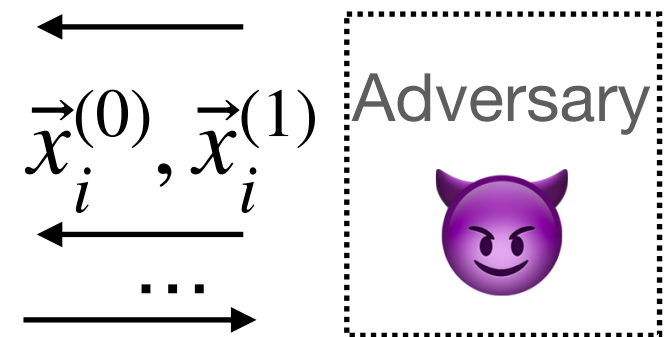
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Perfectly

Perfectly

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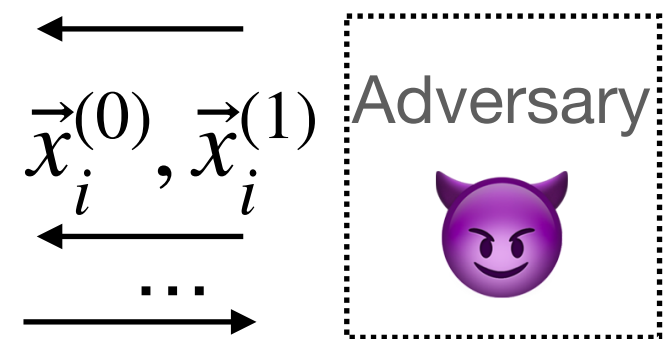
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Conclusion

Our Results:

- Definitional framework of MCFE with public inputs
- Implications from *secret-key* MCFE to *public-key* FE/KP-ABE
- **Constructions** with **sub-vectors** *per* client and **strong security**

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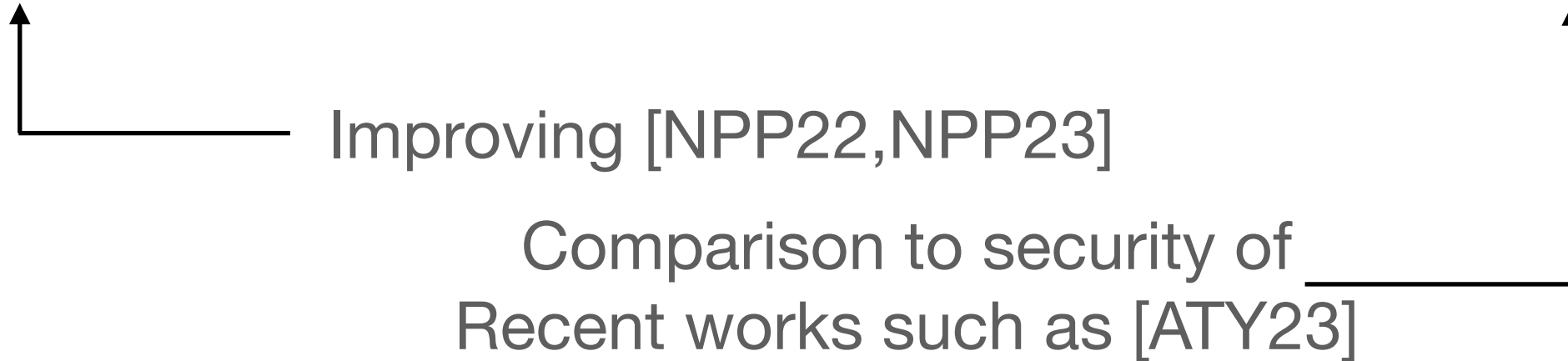
Improving [NPP22,NPP23]



Conclusion

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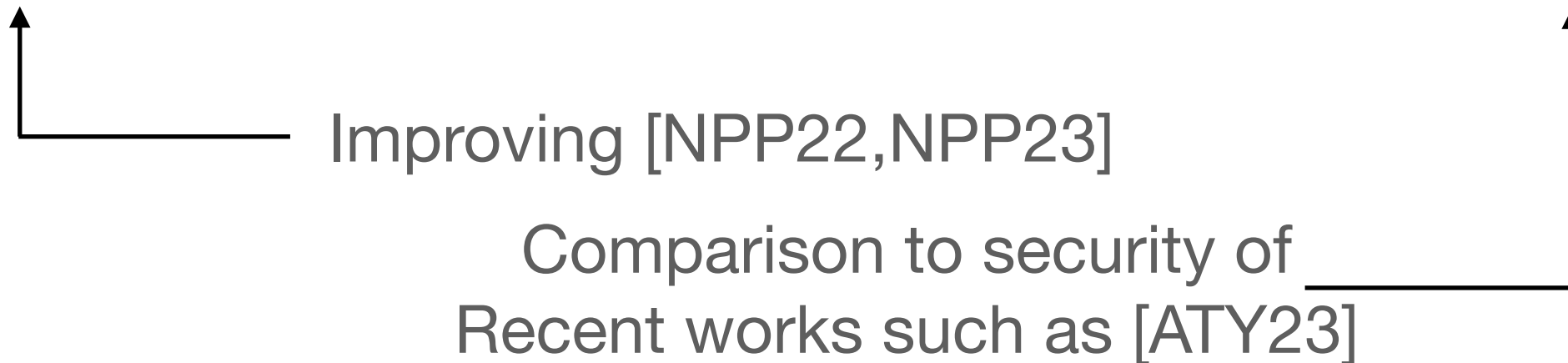
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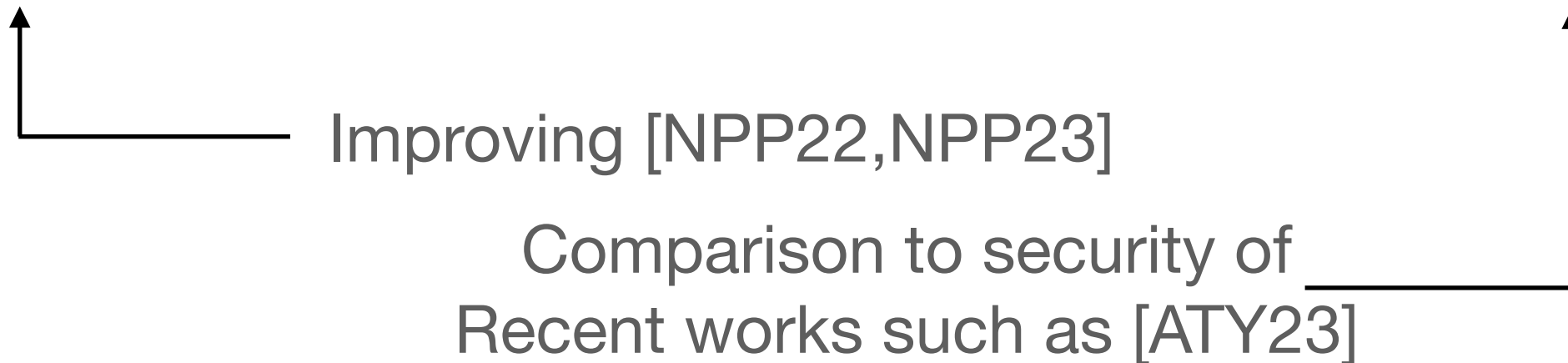


1. *Stronger Computation? E.g.
Unbounded inner products.*
2. *Generalized primitives? E.g.
Dynamic and/or decentralized.*
3. *Lattice-based constructions?*

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