# An easy attack on AEZ

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FSE 2017 Rump Session

- Lightweight cryptograpy is required for the IoT
- Here is a concrete example:
- Toilet in my hotel is remote controlled!
- Some models use Bluetooth!
- Important confidentiality and authenticity issues!
- Man in the dattack!
- Denial of attack!
- ► Targeted attacks:  $\stackrel{\frown}{=}$   $\stackrel{\rightarrow$
- Welcome to the Internet of

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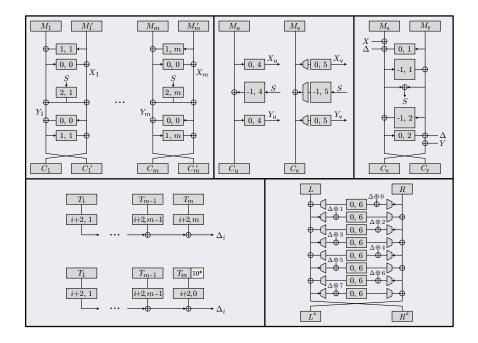
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### An easy attack on AEZ

# AEZ

Viet Tung Hoang, Ted Krovetz & Phillip Rogaway Robust Authenticated-Encryption AEZ and the Problem That It Solves EUROCRYPT 2015

- Very strong security goal: robust authenticated encryption
- Very complex design: huge state, many subcases
- Third round CAESAR candidate
- Tor is considering using AEZ



# Previous results on AEZ

### AEZv3: birthday attack recovers the key

## [Asiacrypt 2015]

### Patched in AEZv4

- Using Blake2 for key derivation
- Bigger is better?

AEZv4: birthday attack recovers the key

[FSE 2017]

# Previous results on AEZ

AEZv3: birthday attack recovers the key

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AEZv4: birthday attack recovers the key

[FSE 2017]

# Previous results on AEZ

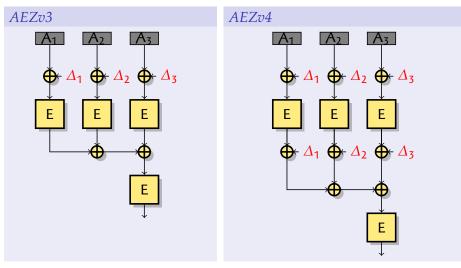
AEZv3: birthday attack recovers the key

### [Asiacrypt 2015]

- Patched in AEZv4
  - Using Blake2 for key derivation
  - Bigger is better?
- AEZv4: birthday attack recovers the key [FSE 2017]

# AEZ-MAC (PMAC variant)

### With empty message, AEZ turns into a MAC



# $\begin{array}{c} \mathsf{P} \\ \downarrow \\ \mathsf{E} \\ \mathsf{A}_{\mathsf{i}} \xrightarrow{\mathsf{E}} \\ \mathsf{C} \end{array}$

# XEX construction

- ►  $E(P \oplus \Delta_i) \oplus \Delta_i$  is a tweakable block cipher If  $i \mapsto \Delta_i$  is an  $\varepsilon$ -AXU function
- ► Common constructions  $(L = E_k(0))$ ►  $\Delta_i = i \cdot L$  (OCB1, OCB3) ►  $\Delta_i = 2^i \cdot L$  (OCB2)
- AEZv3 (subkeys J, L)
  Δ<sub>i</sub> = 8 · J ⊕ (i mod 8) · J ⊕ 2<sup>[(i-1)/8]</sup> · L
- AEZv4 (subkeys J, L)
  △<sub>i</sub> = L ⊕ (2<sup>3+L(i-1)/8</sup> + (i 1 mod 8)) ⋅ J

# A closer look

# AEZv4 offsets $\Delta_{i} = L \oplus \left(2^{3+\lfloor (i-1)/8 \rfloor} + (i-1 \mod 8)\right) \cdot J$

## Addition between GF(2<sup>128</sup>) elements?

- $\Delta_{i} = L \oplus 2^{3 + \lfloor (i-1)/8 \rfloor} \cdot J \oplus (i-1 \mod 8) \cdot J$ 
  - ▶ 2<sup>×</sup> is actually  $\alpha^{x}$ , with  $\alpha$  a generator ( $\alpha^{128} = \alpha^7 \oplus \alpha^2 \oplus \alpha \oplus 1$ )
  - (i 1 mod 8) is one of  $\{0, 1, \alpha, \alpha \oplus 1, \alpha^2, \alpha^2 \oplus 1, \alpha^2 \oplus \alpha, \alpha^2 \oplus \alpha \oplus 1\}$
- Is it injective?
  - ► No!

$$\Delta_{40} = \mathsf{L} \oplus \alpha^7 \cdot \mathsf{J} \oplus (\alpha^2 \oplus \alpha \oplus 1) \cdot \mathsf{J}$$

# A closer look

### AEZv4 offsets

- $\Delta_{i} = L \oplus \left(2^{3 + \lfloor (i-1)/8 \rfloor} + (i 1 \text{ mod } 8)\right) \cdot J$ 
  - Addition between GF(2<sup>128</sup>) elements?
  - ►  $\Delta_i = L \oplus 2^{3+\lfloor (i-1)/8 \rfloor} \cdot J \oplus (i-1 \mod 8) \cdot J$ 
    - ▶  $2^x$  is actually  $\alpha^x$ , with  $\alpha$  a generator ( $\alpha^{128} = \alpha^7 \oplus \alpha^2 \oplus \alpha \oplus 1$ )
    - (i 1 mod 8) is one of {0, 1,  $\alpha$ ,  $\alpha \oplus 1$ ,  $\alpha^2$ ,  $\alpha^2 \oplus 1$ ,  $\alpha^2 \oplus \alpha$ ,  $\alpha^2 \oplus \alpha \oplus 1$ }

### Is it injective?

► No!

$$\Delta_{40} = \mathsf{L} \oplus \alpha^7 \cdot \mathsf{J} \oplus (\alpha^2 \oplus \alpha \oplus 1) \cdot \mathsf{J}$$

# A closer look

### AEZv4 offsets

- $\Delta_{i} = L \oplus \left(2^{3 + \lfloor (i-1)/8 \rfloor} + (i 1 \mod 8)\right) \cdot J$ 
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  - Is it injective?
    - No!

$$\Delta_{40} = \mathsf{L} \oplus \alpha^7 \cdot \mathsf{J} \oplus (\alpha^2 \oplus \alpha \oplus 1) \cdot \mathsf{J}$$

•  $\Delta_{1001} = \mathsf{L} \oplus \alpha^{128} \cdot \mathsf{J} = \mathsf{L} \oplus (\alpha^7 \oplus \alpha^2 \oplus \alpha \oplus 1) \cdot \mathsf{J}$ 

# Conclusion

### Forgery attack

- Swap A<sub>40</sub> and A<sub>1001</sub> → same tag
- Swap  $P_{79,80}$  and  $P_{2001,2002} \rightsquigarrow C_{79,80}$  and  $C_{2001,2002}$  swapped
- Similar to OTR attack
- Easy to patch: AEZv5?
- Even provably secure ciphers can be broken!
- Don't use AEZv4 to secure your toilet!